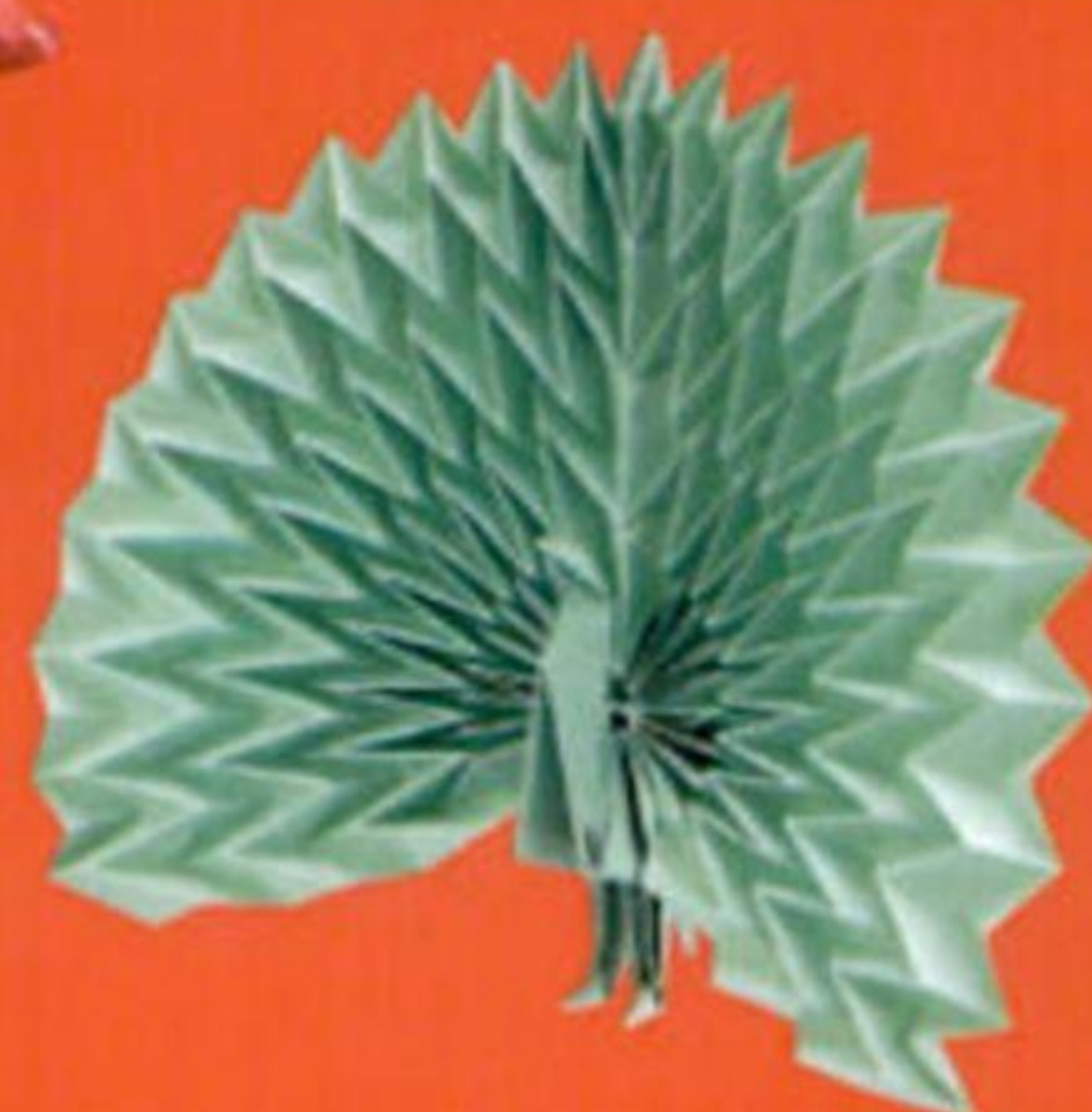
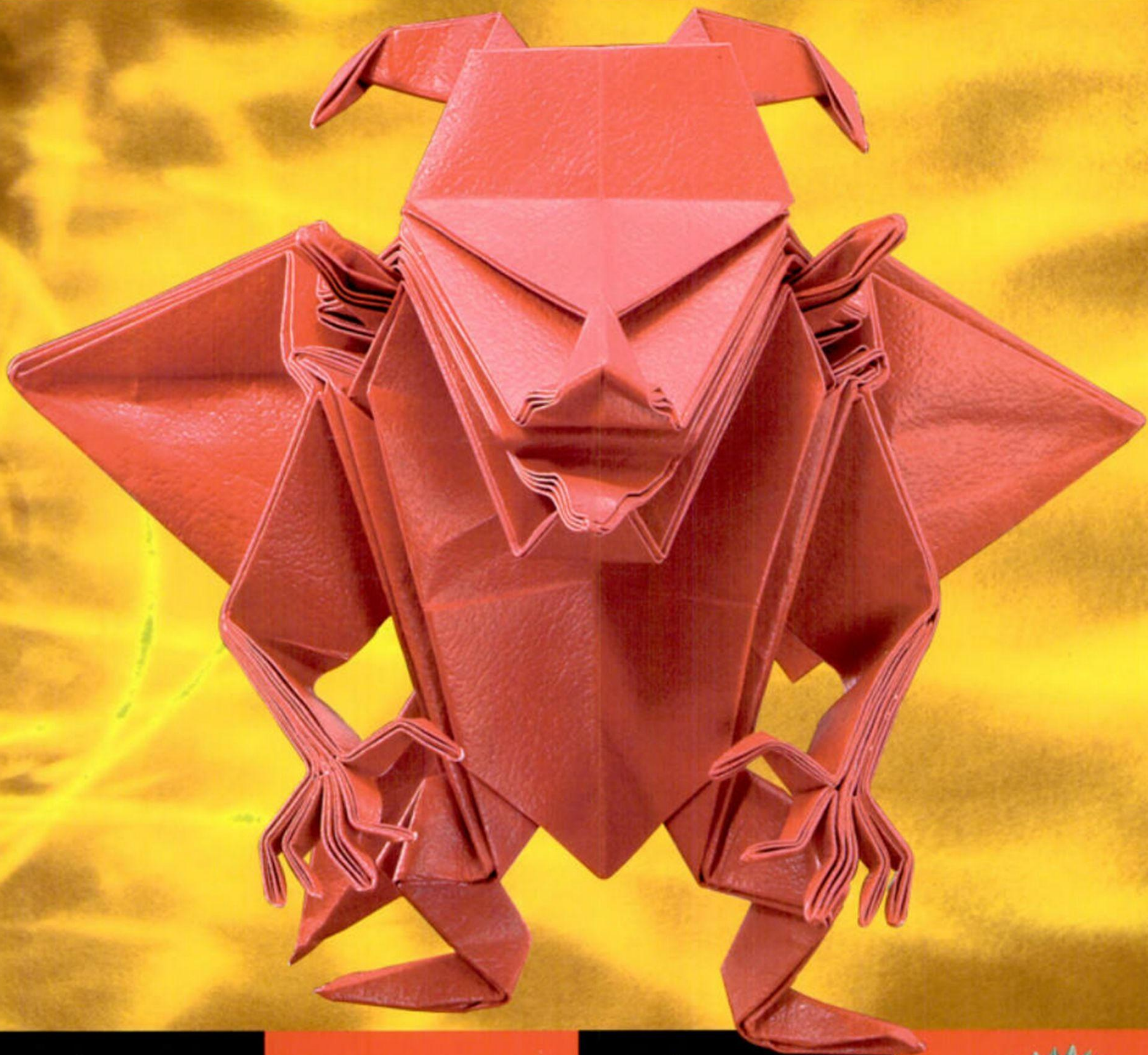


Genuine Origami

43 Mathematically-Based Models, From Simple to Complex
Jun Maekawa



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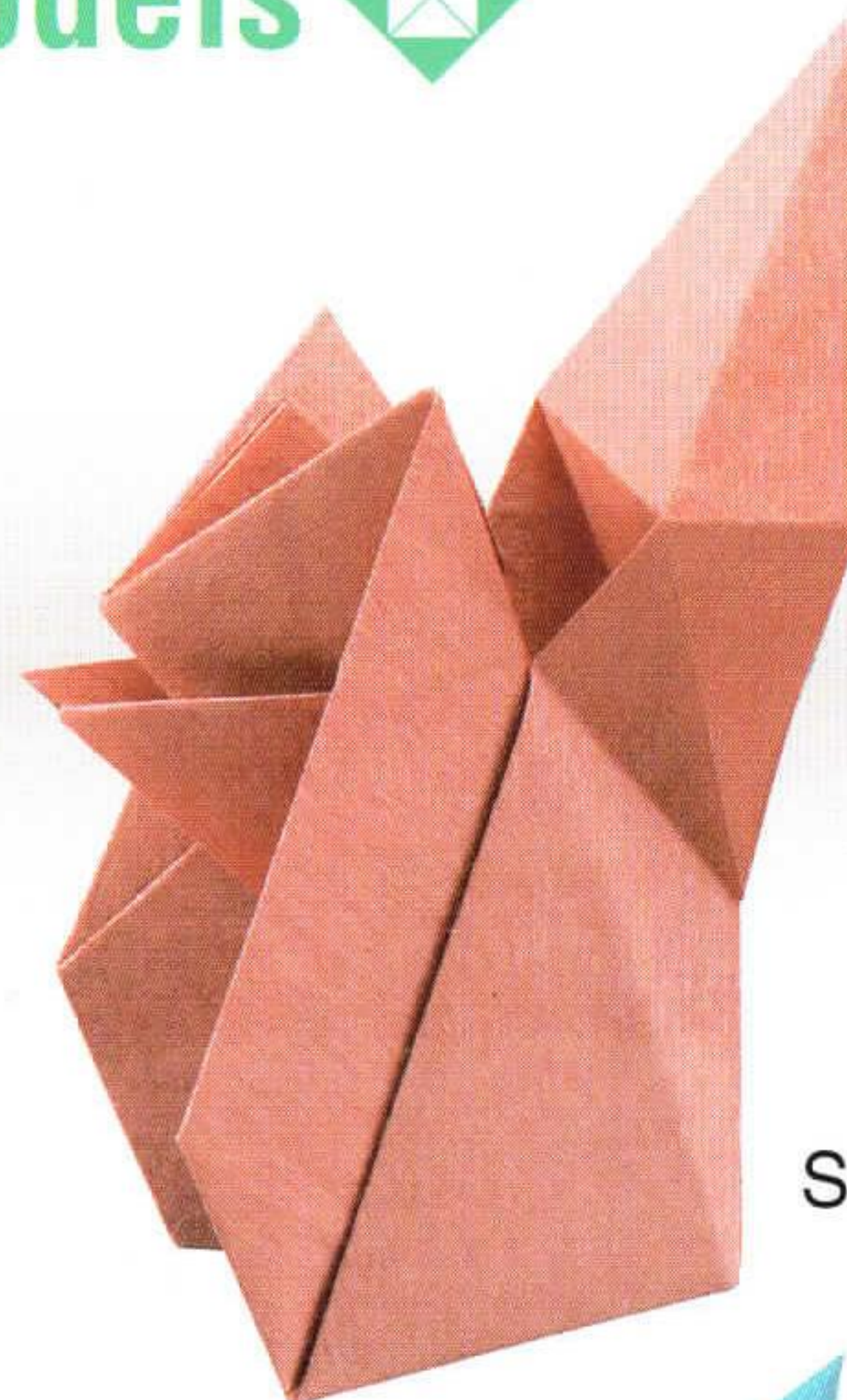
◆ Fundamental Models ◆

Learn basics even from zero.

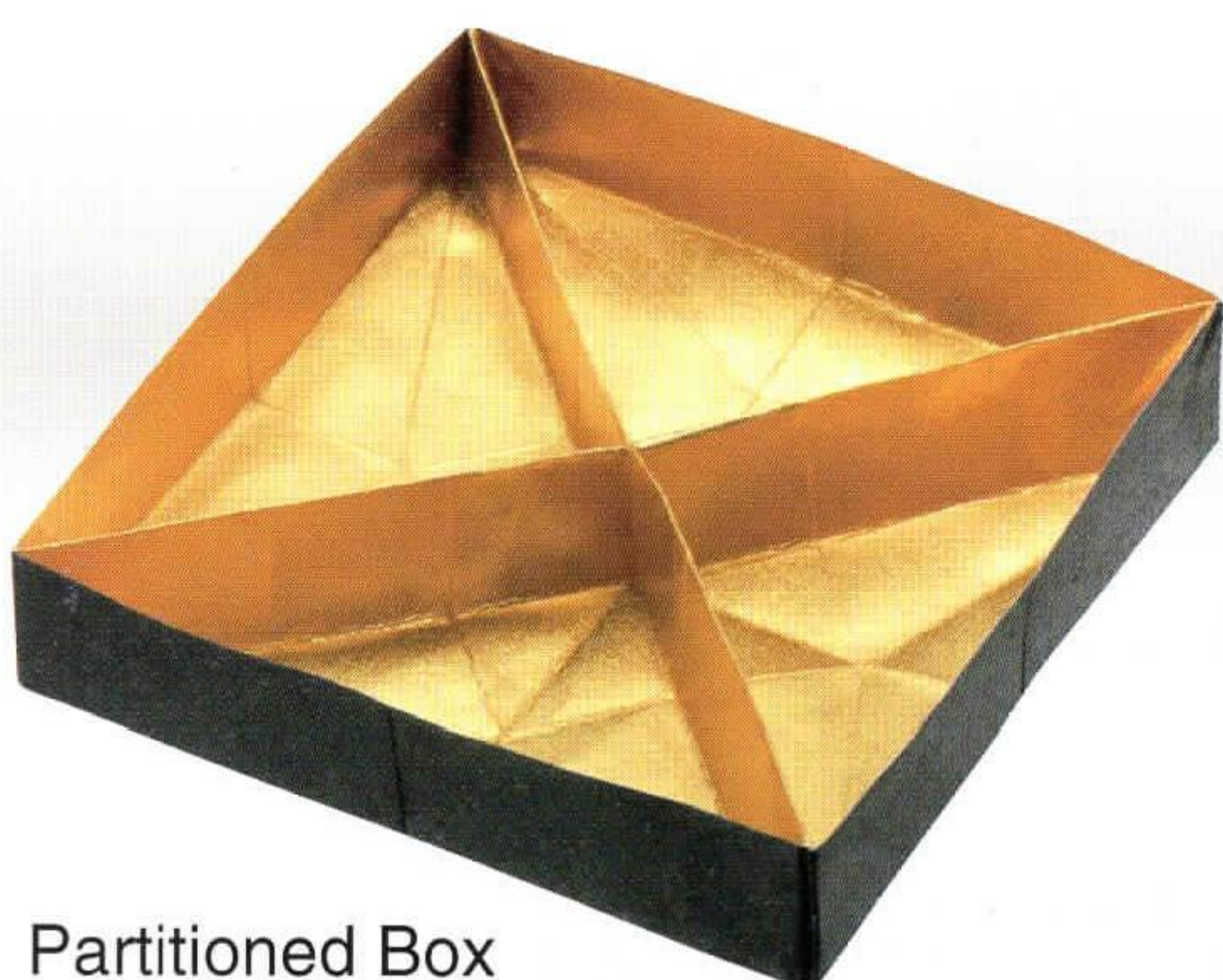
Mouse



Squirrel



Basic of basics



Partitioned Box

Conch

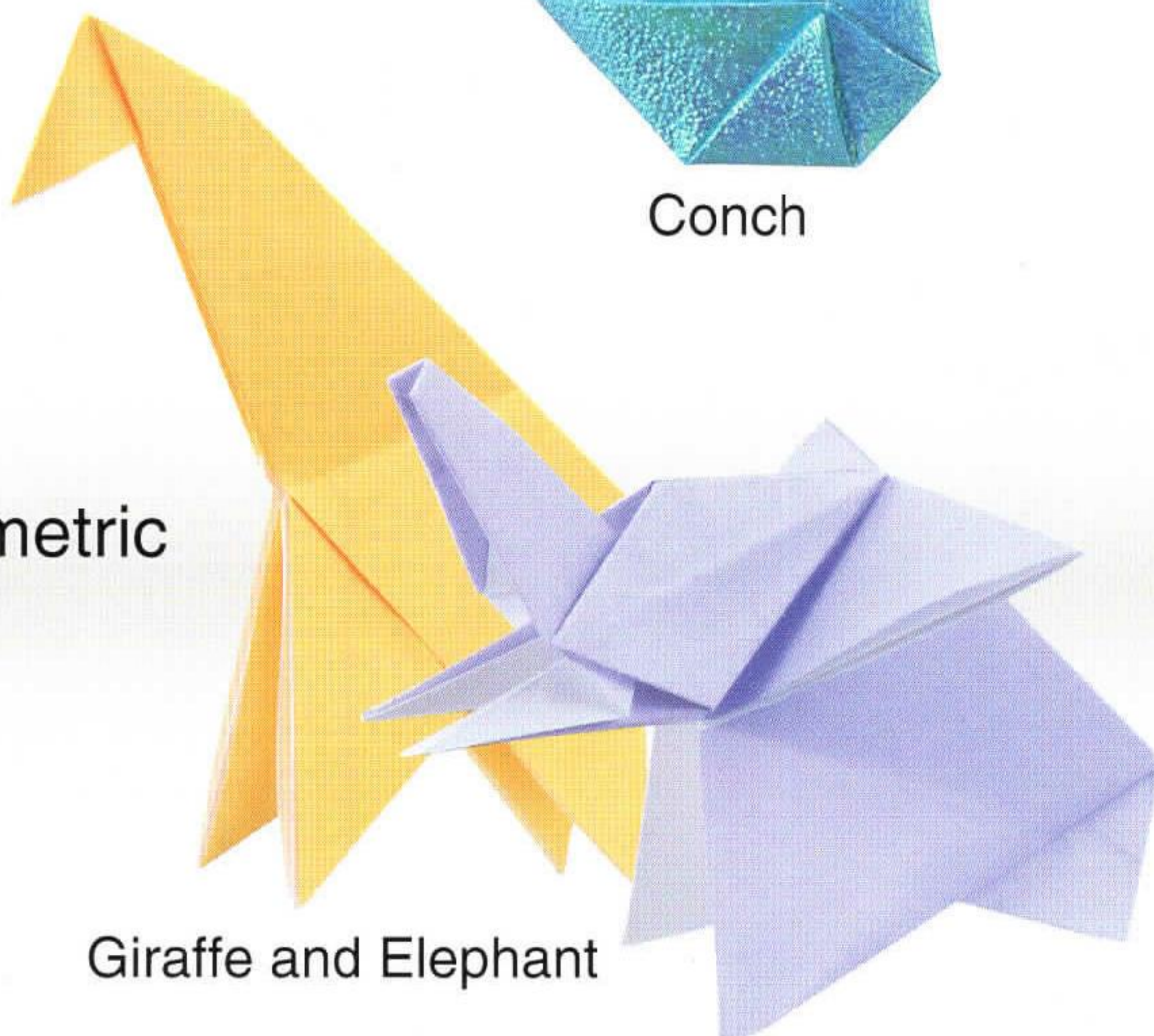


Beauty of geometric forms

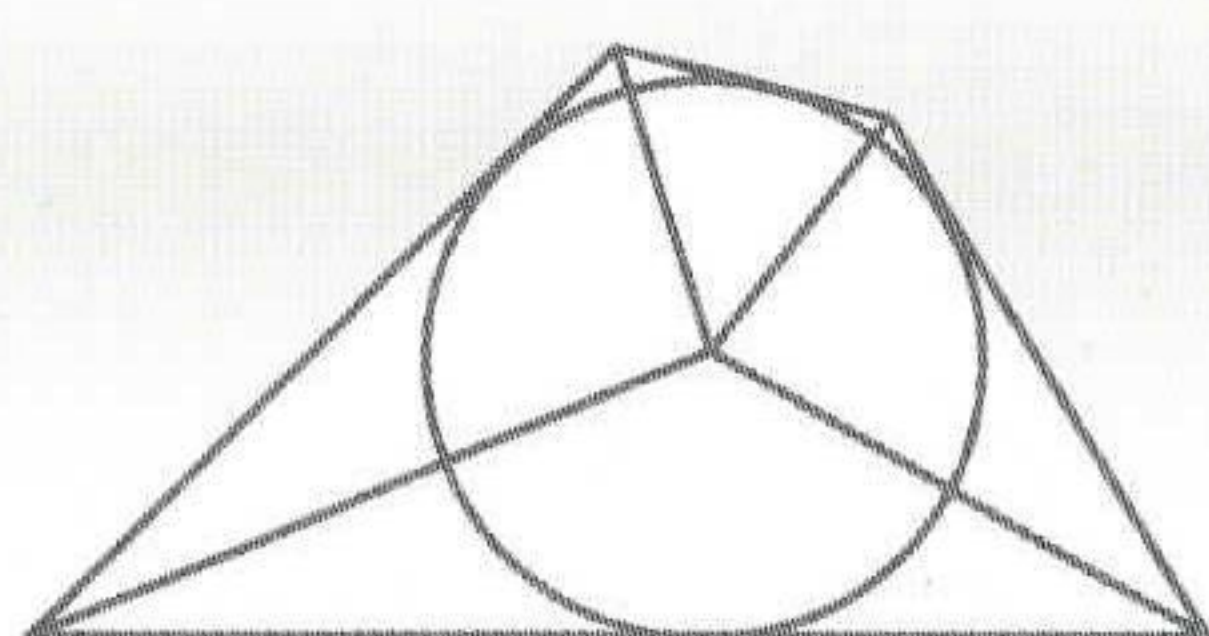


Santa Claus

Giraffe and Elephant



Experimental Mathematics

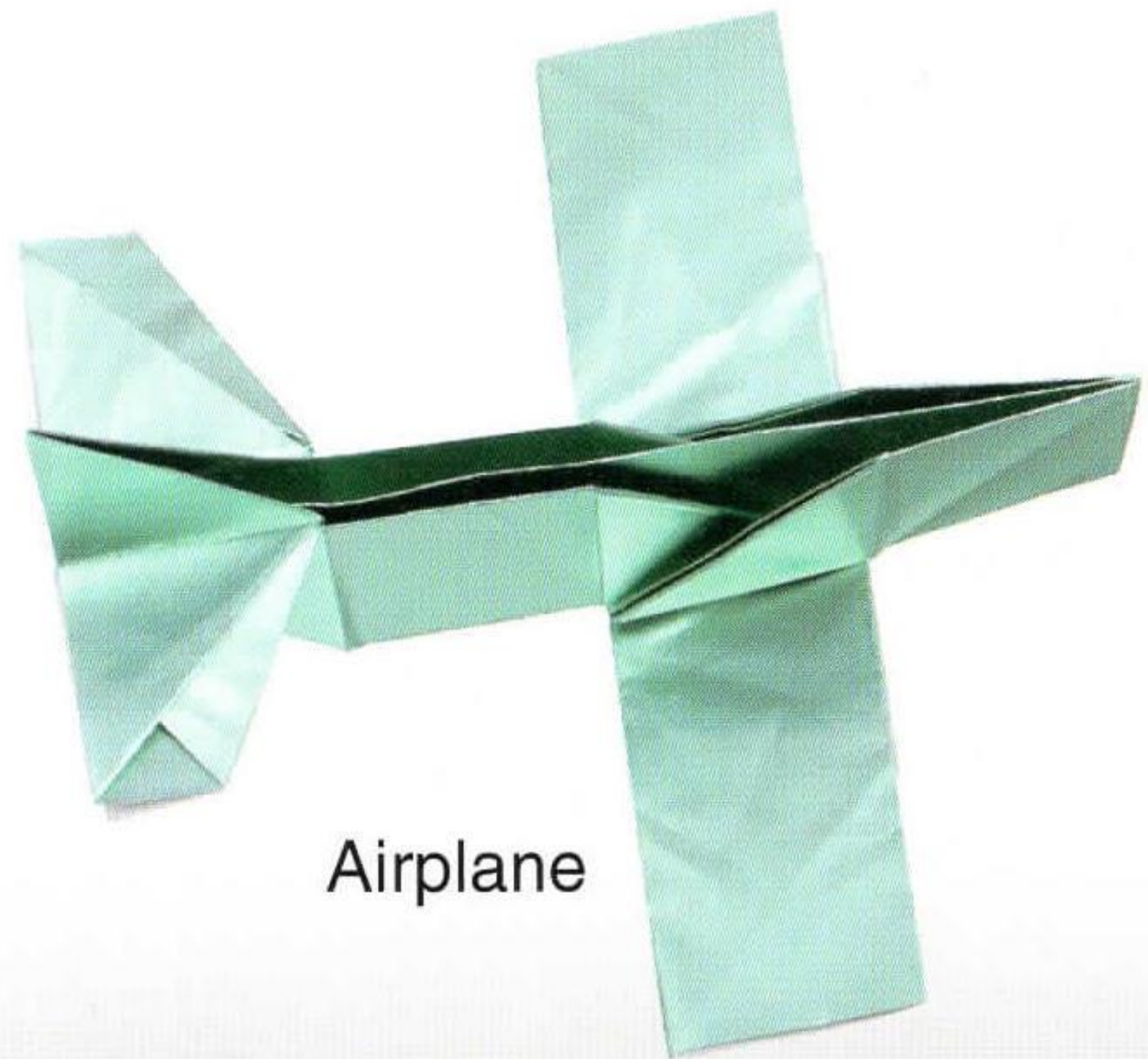


Orizuru Transformation

Simple Models

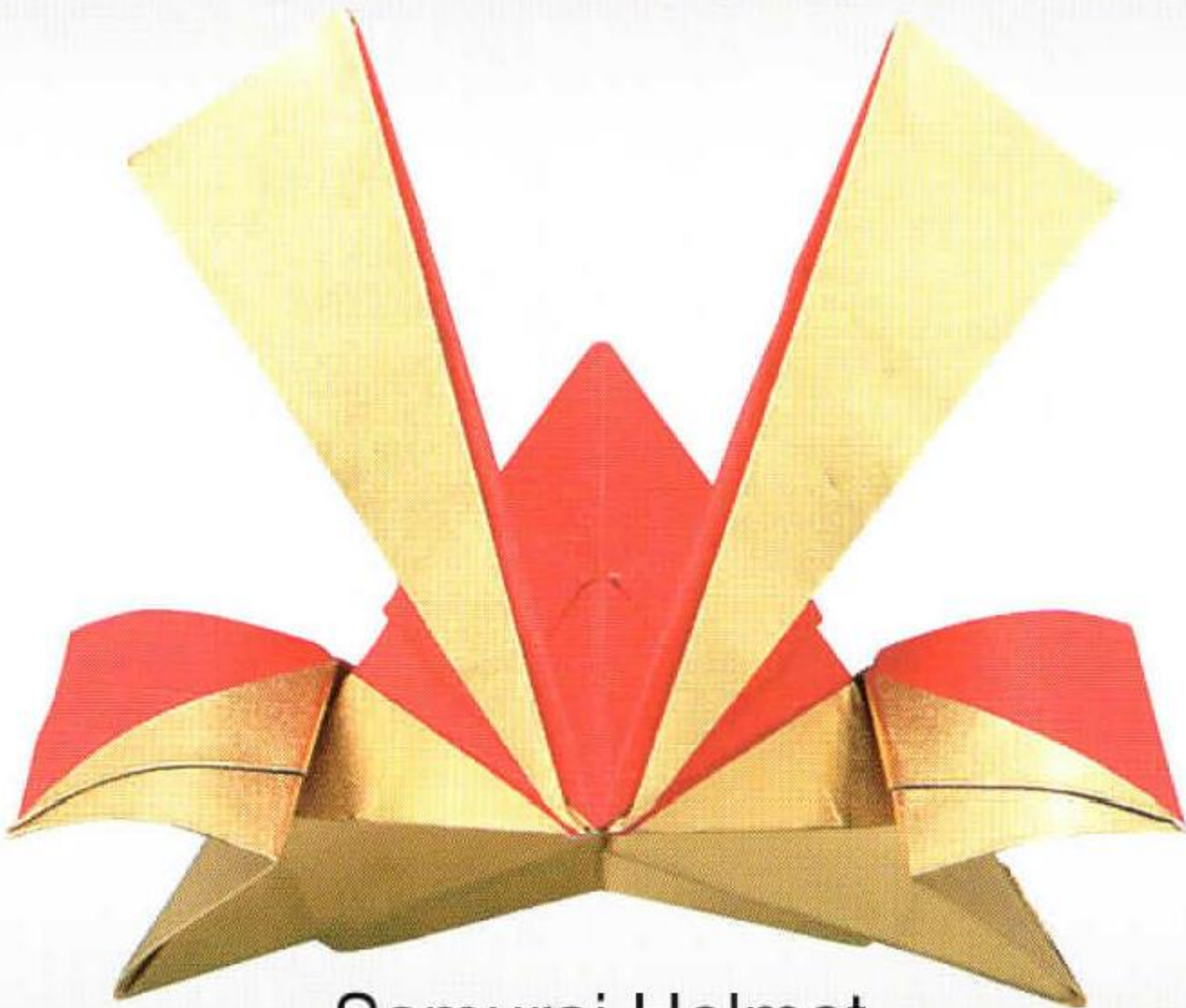


Snake

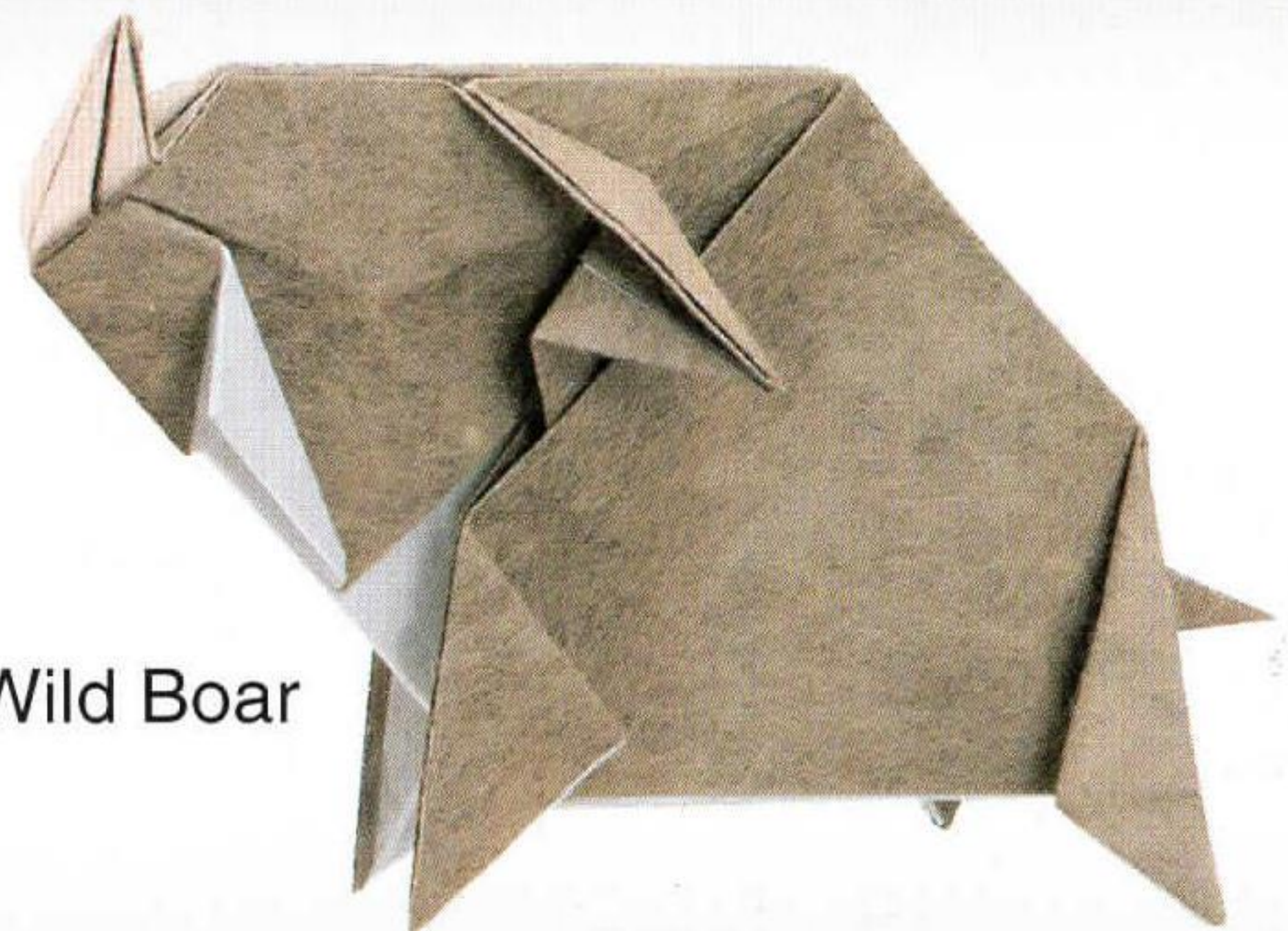


Airplane

Joy of puzzles

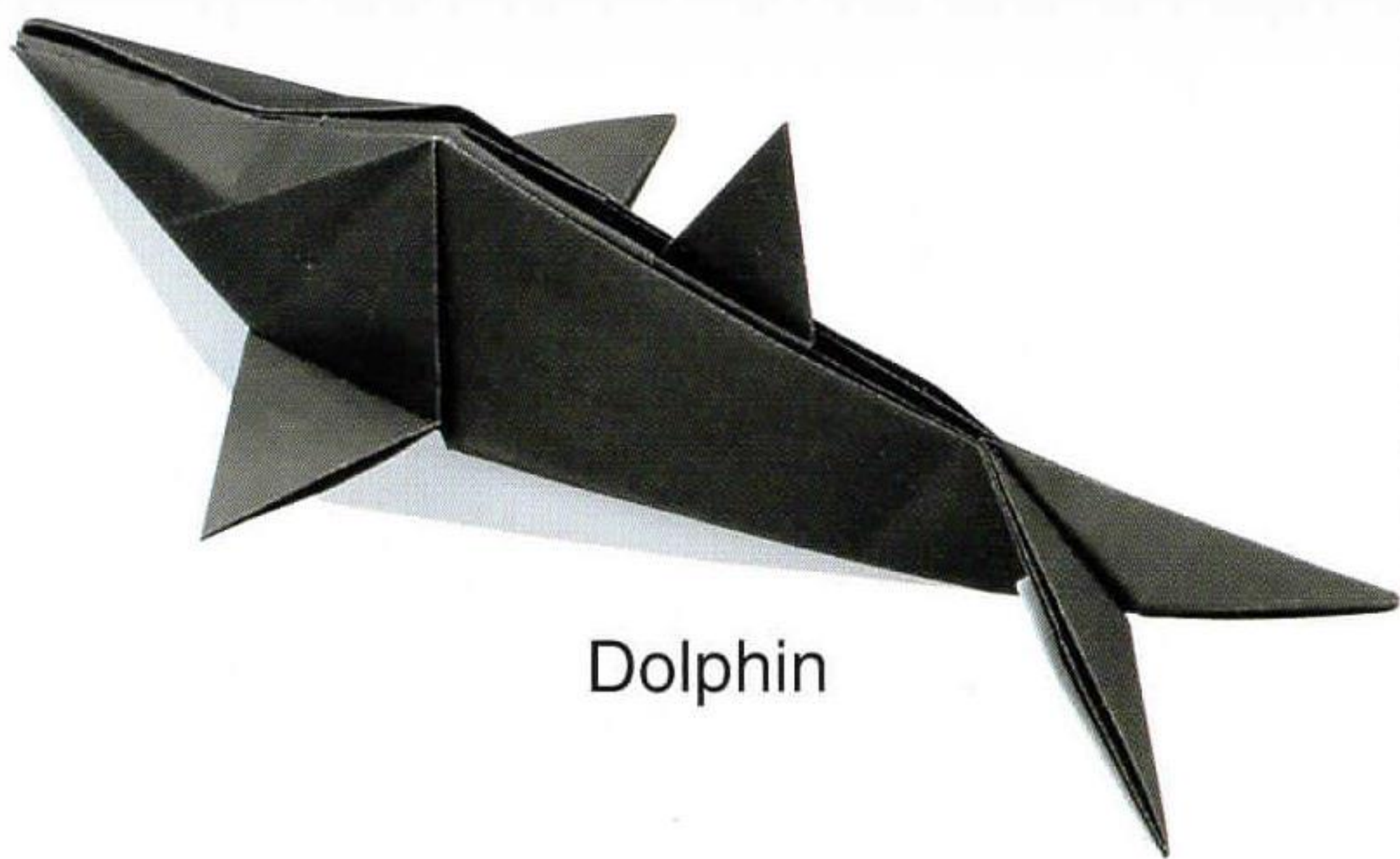


Samurai Helmet

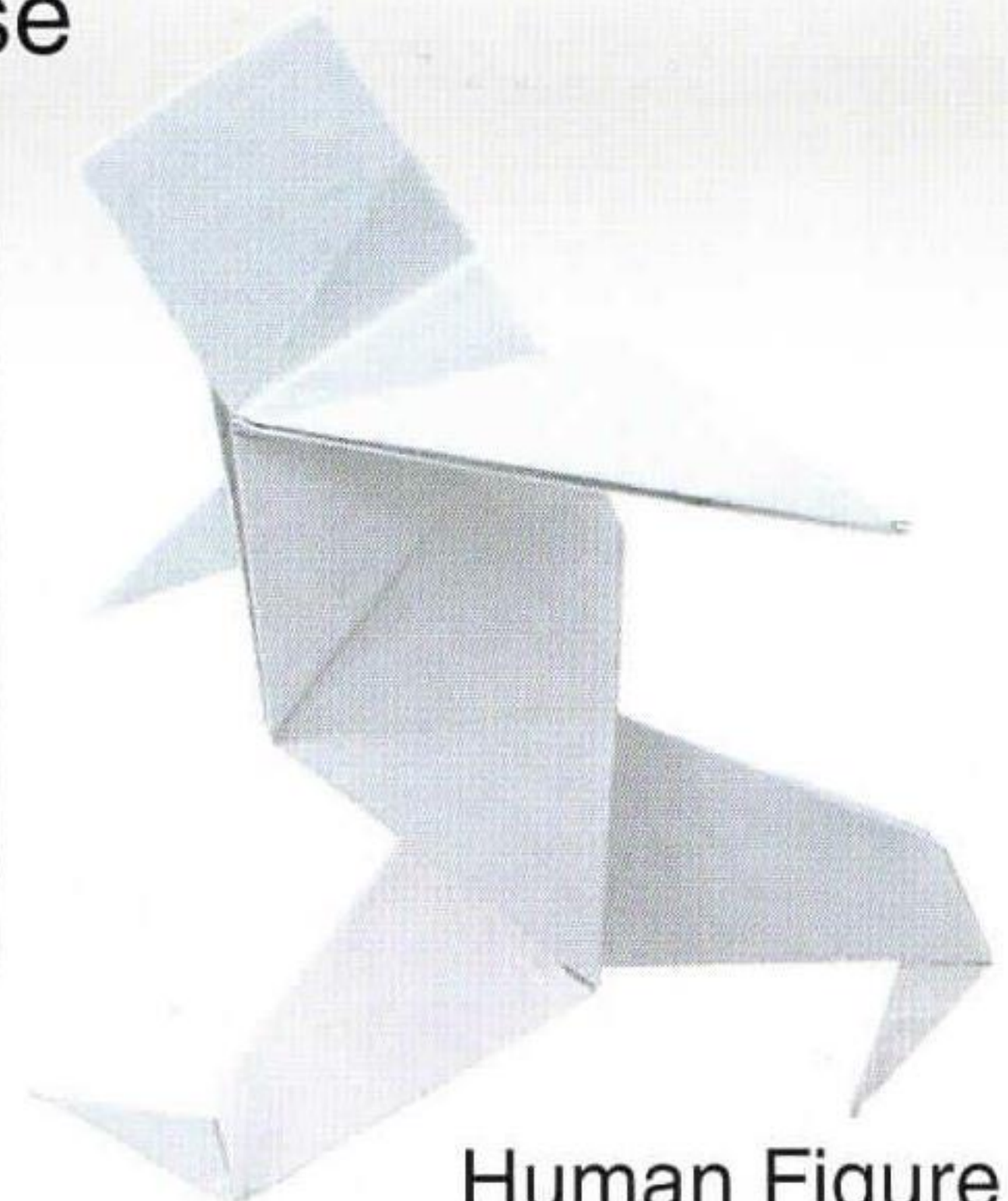
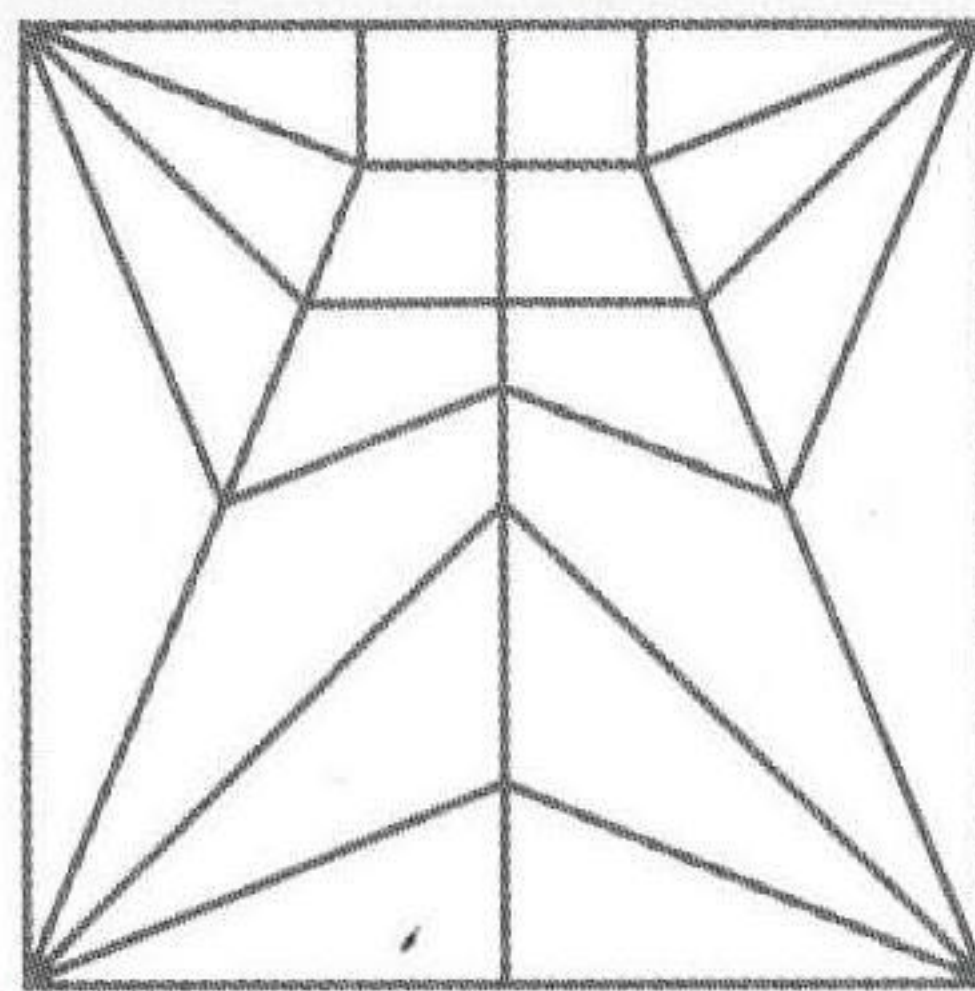


Wild Boar

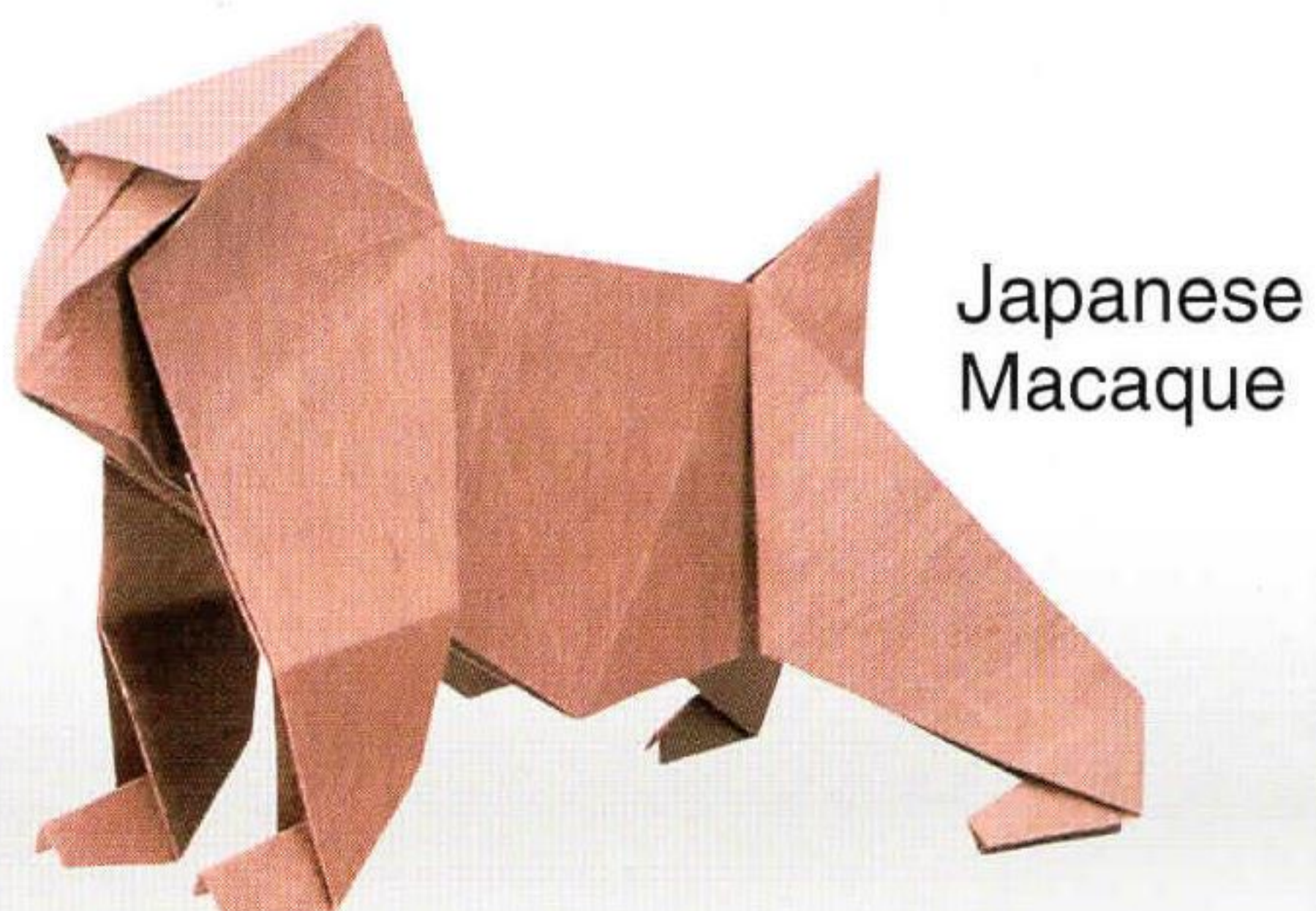
What's the crease pattern?



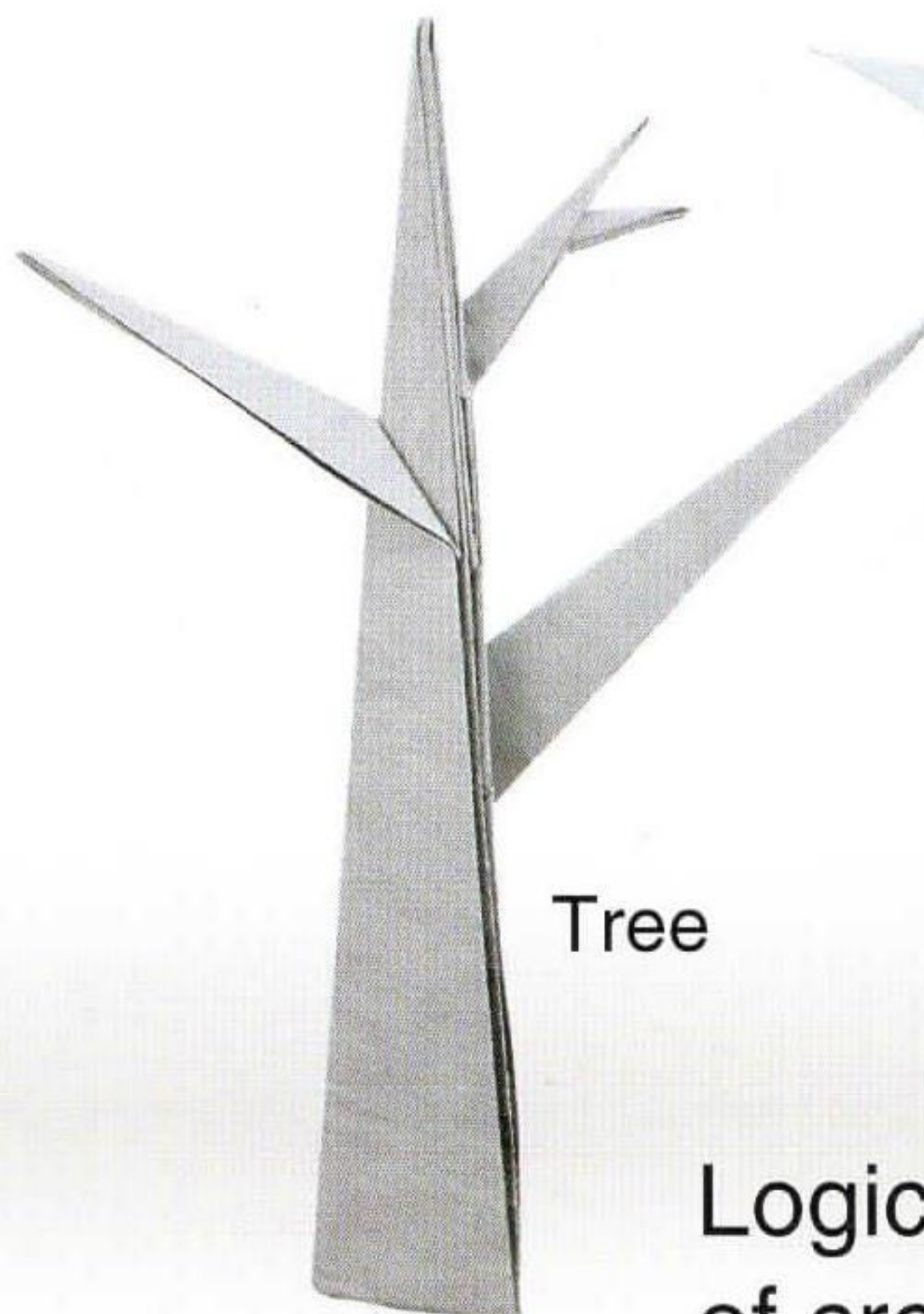
Dolphin



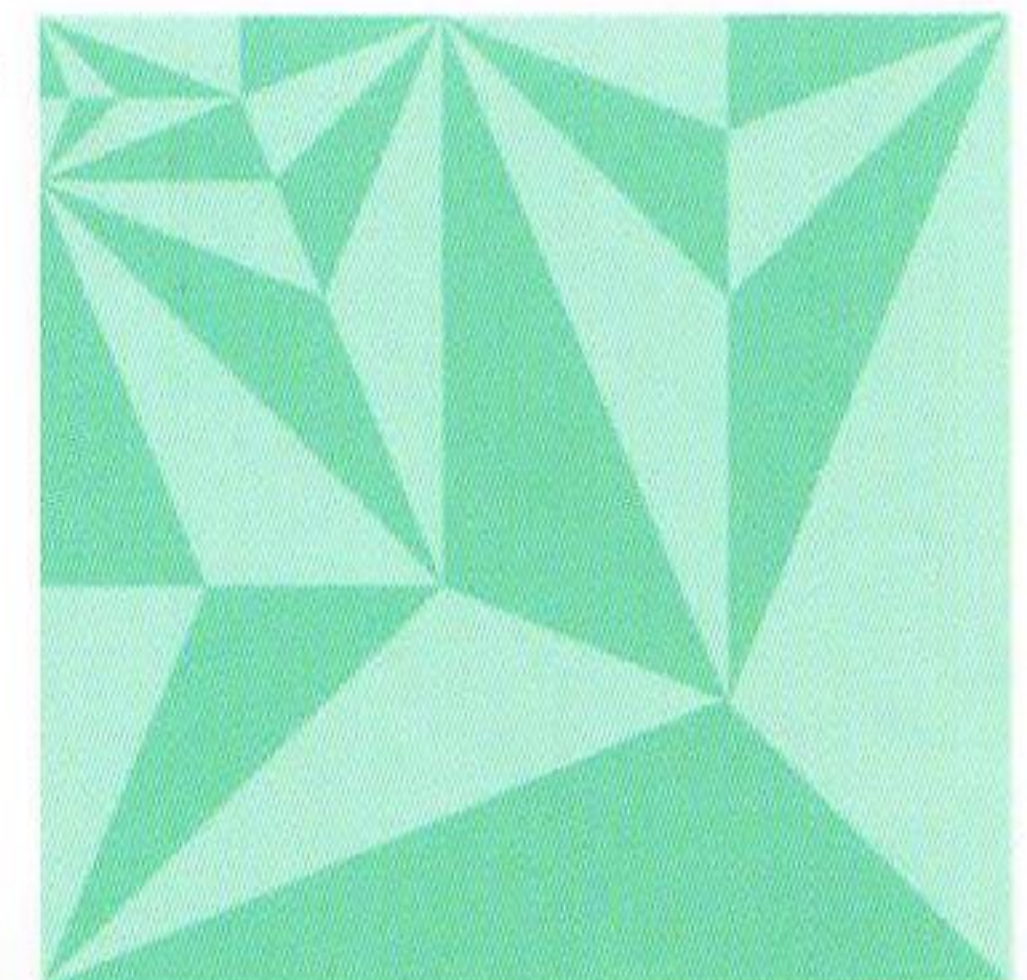
Human Figure



Japanese Macaque



Tree



Logical arrangement of creases

◆ Varieties of Origami ◆



Hina dolls

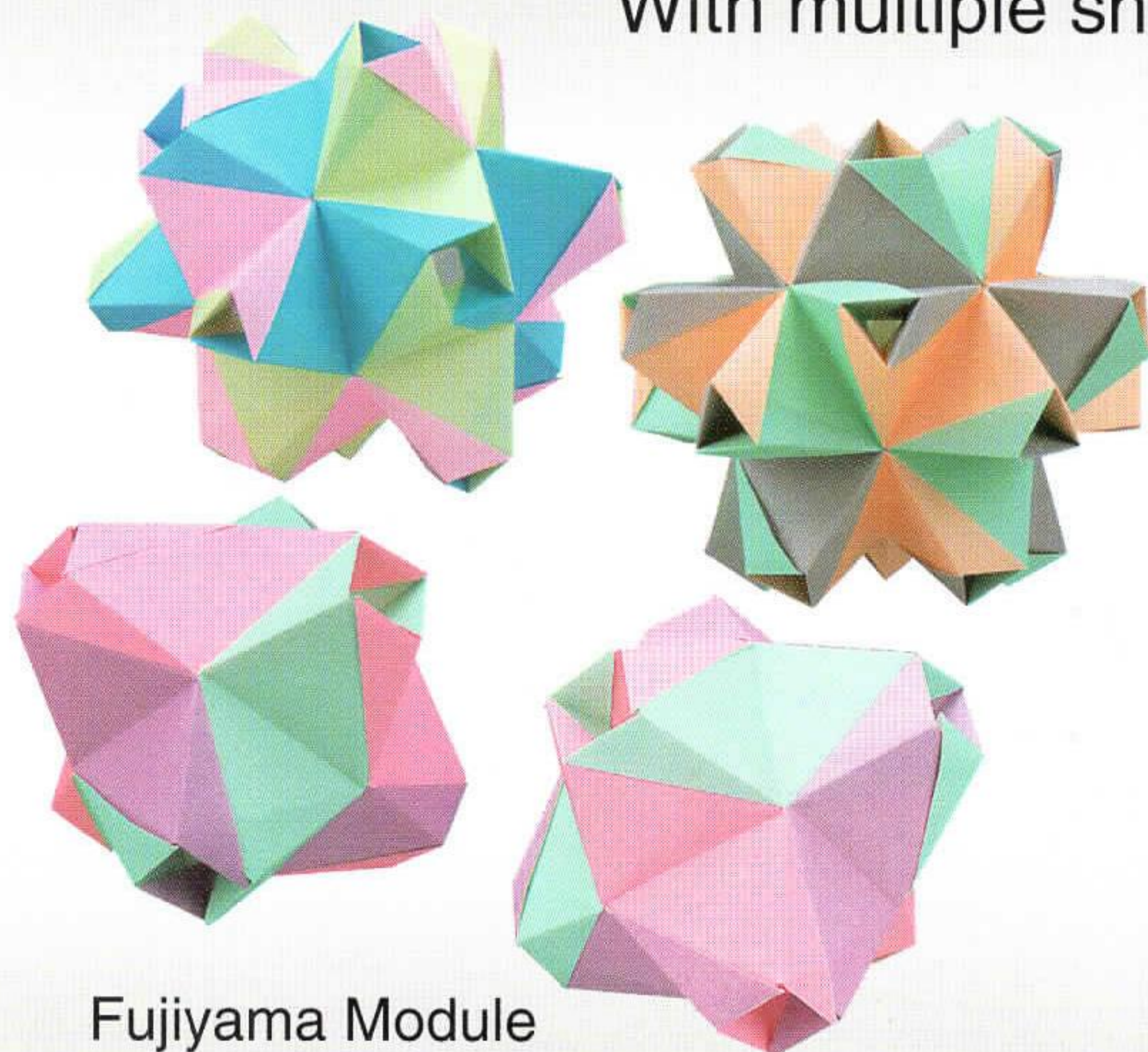


With multiple sheets.



Tea-bag Reindeer

With any kind of paper.



Fujiyama Module



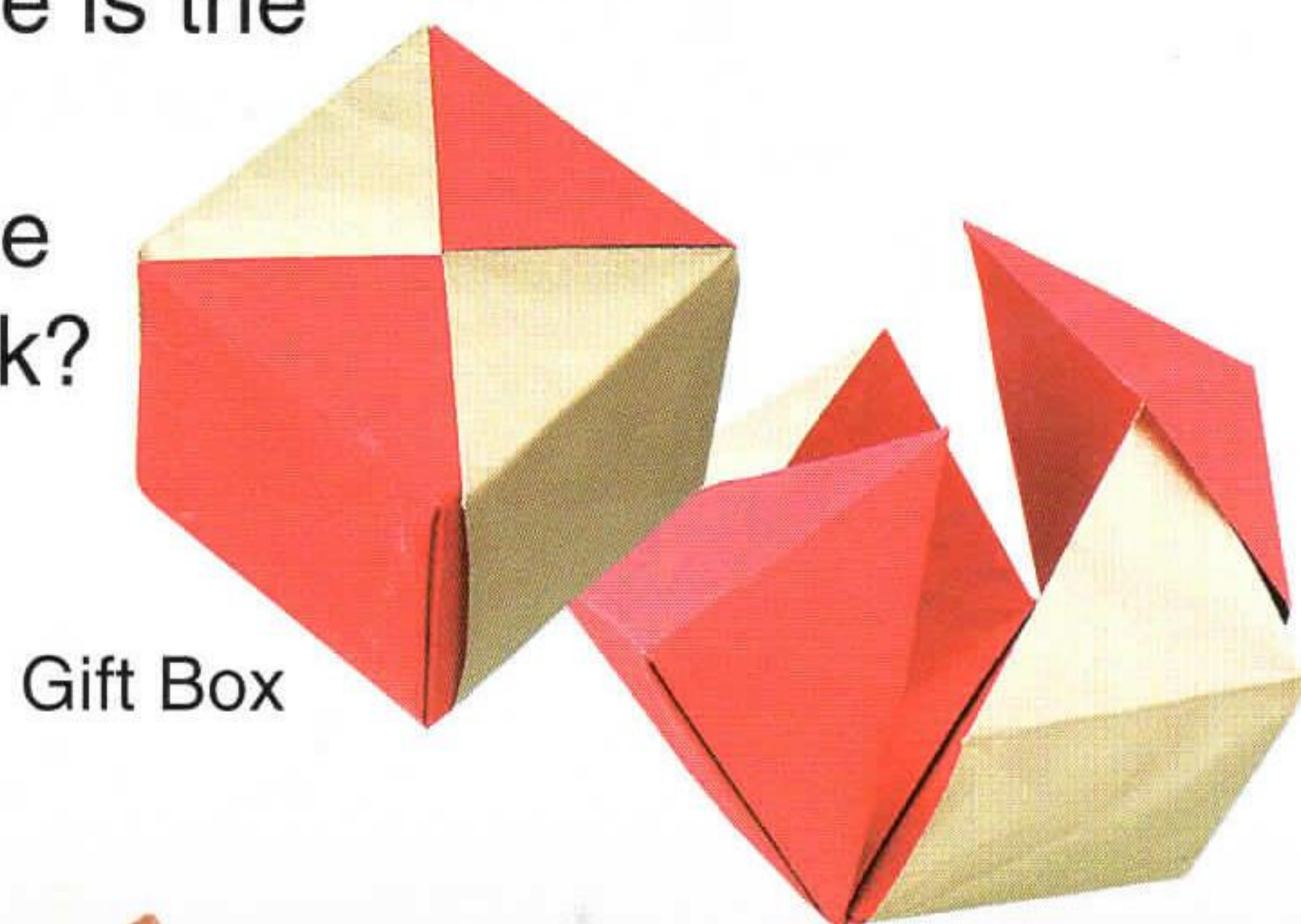
Connected
Cranes, Kotobuki

Even with cuts.

◆ Intermediate Models ◆

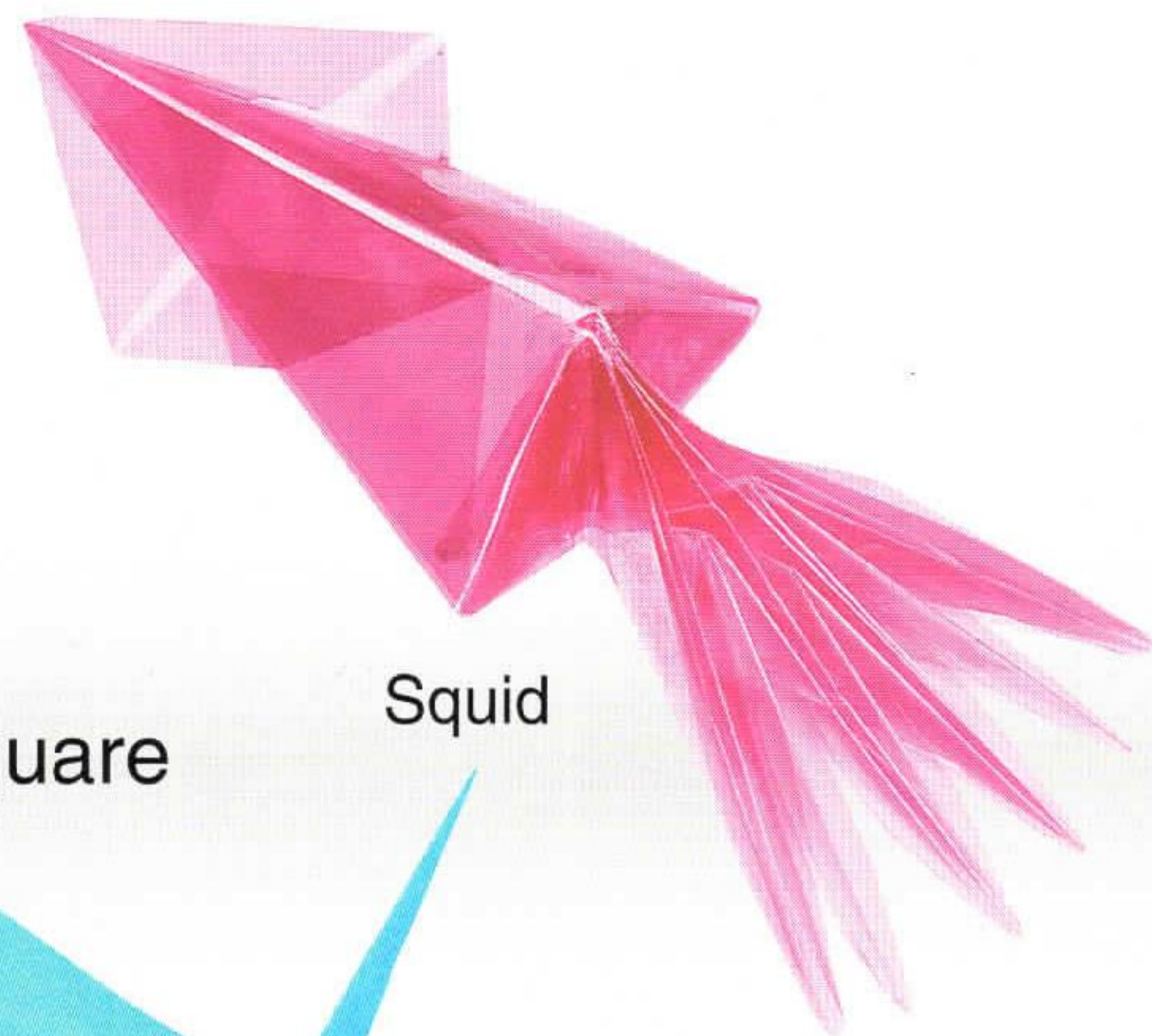
Which side is the
front?

Which side
is the back?



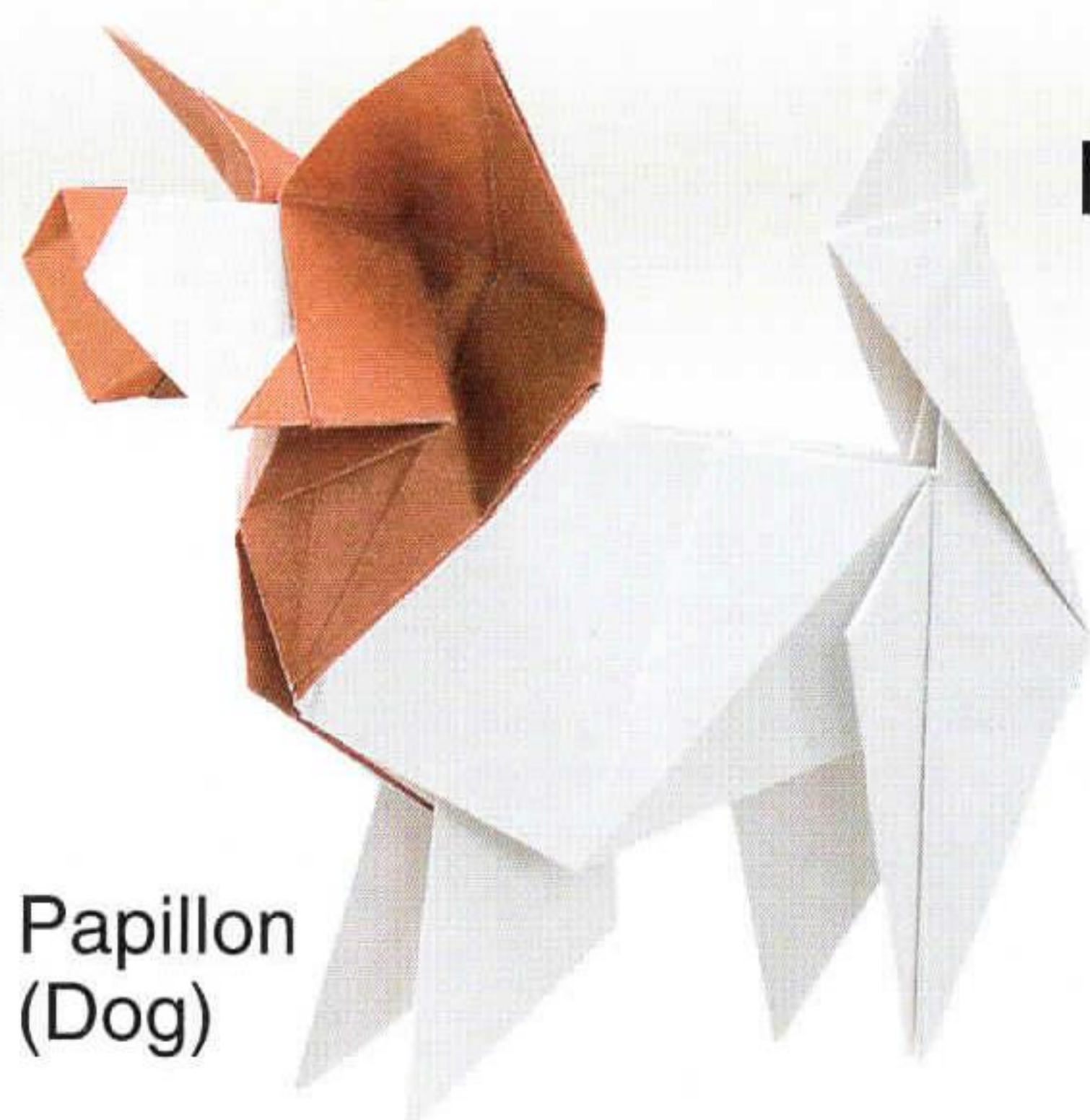
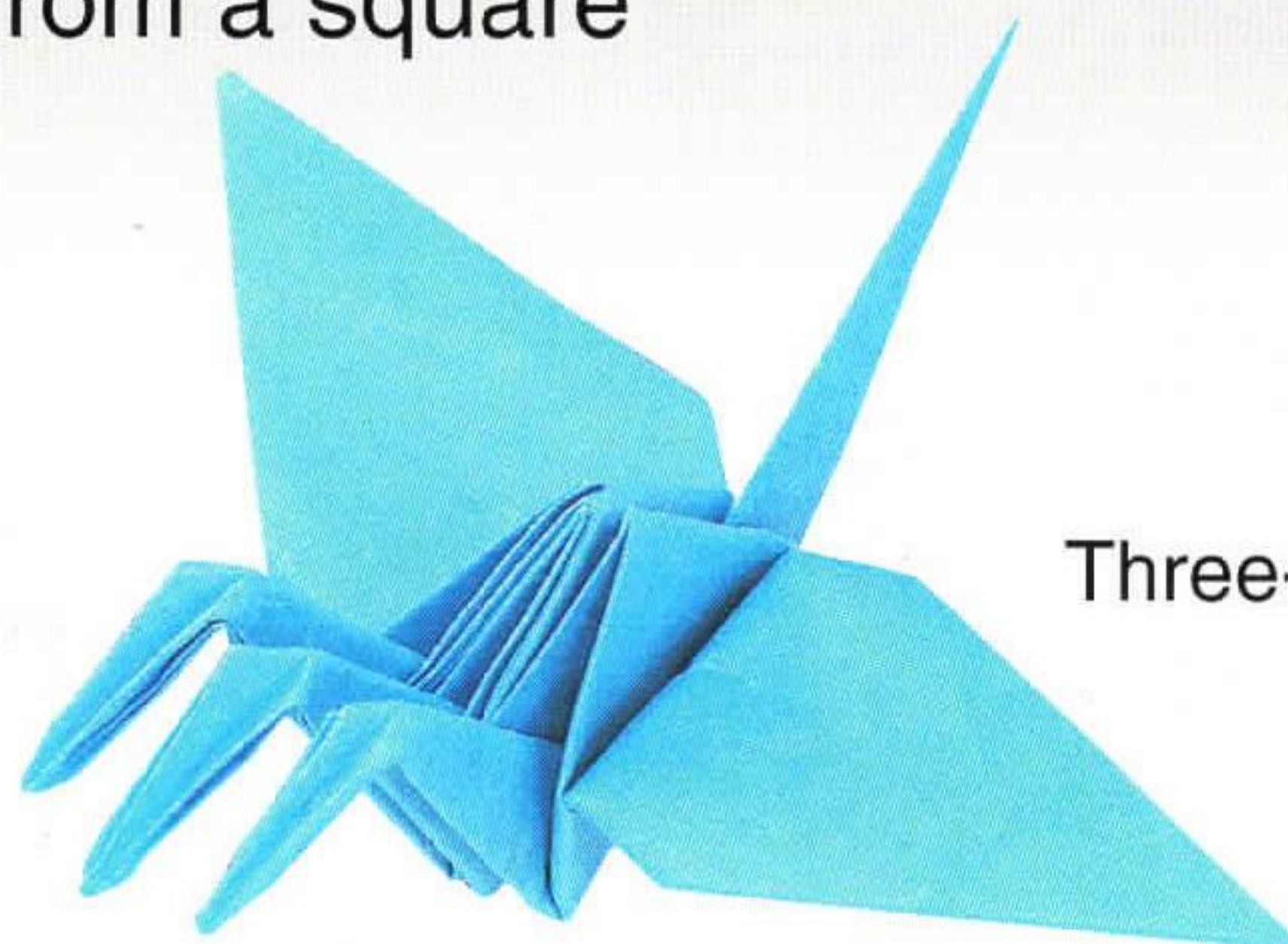
Gift Box

Many points from a square



Squid

Three-headed Crane



Papillon
(Dog)

Intermediate Models

Standing Crane

How to create crease patterns

Cow

Sheep

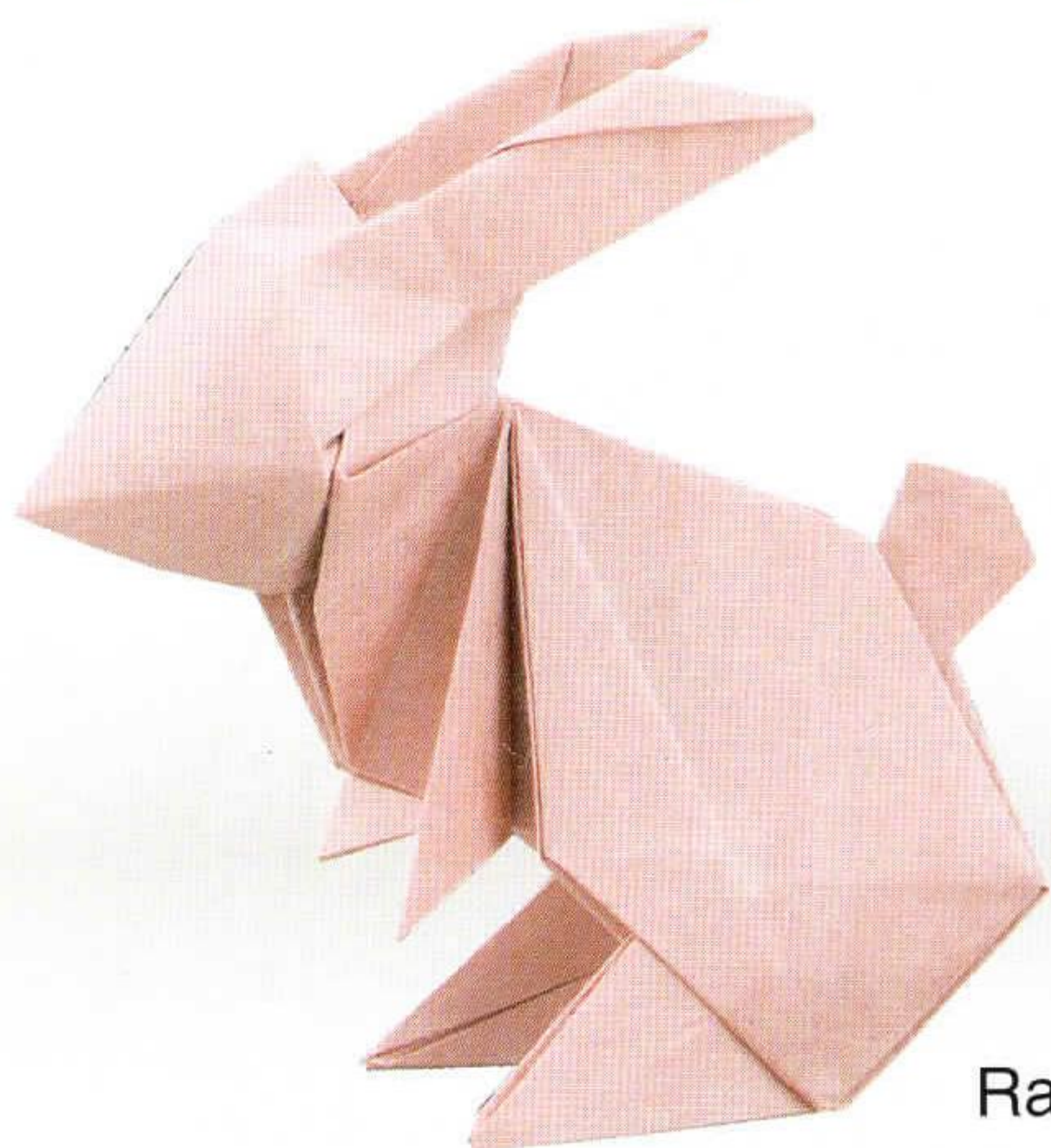
Western Dragon

Triceratops

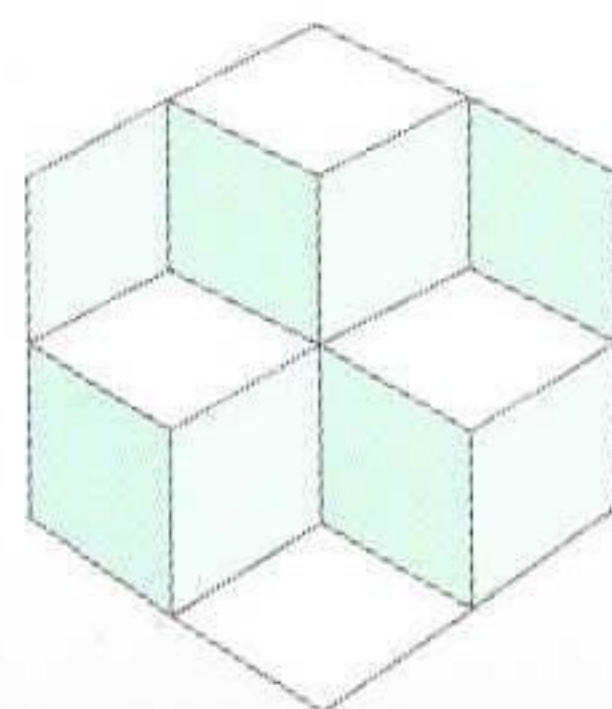
Horse

No need for a ruler or compass.

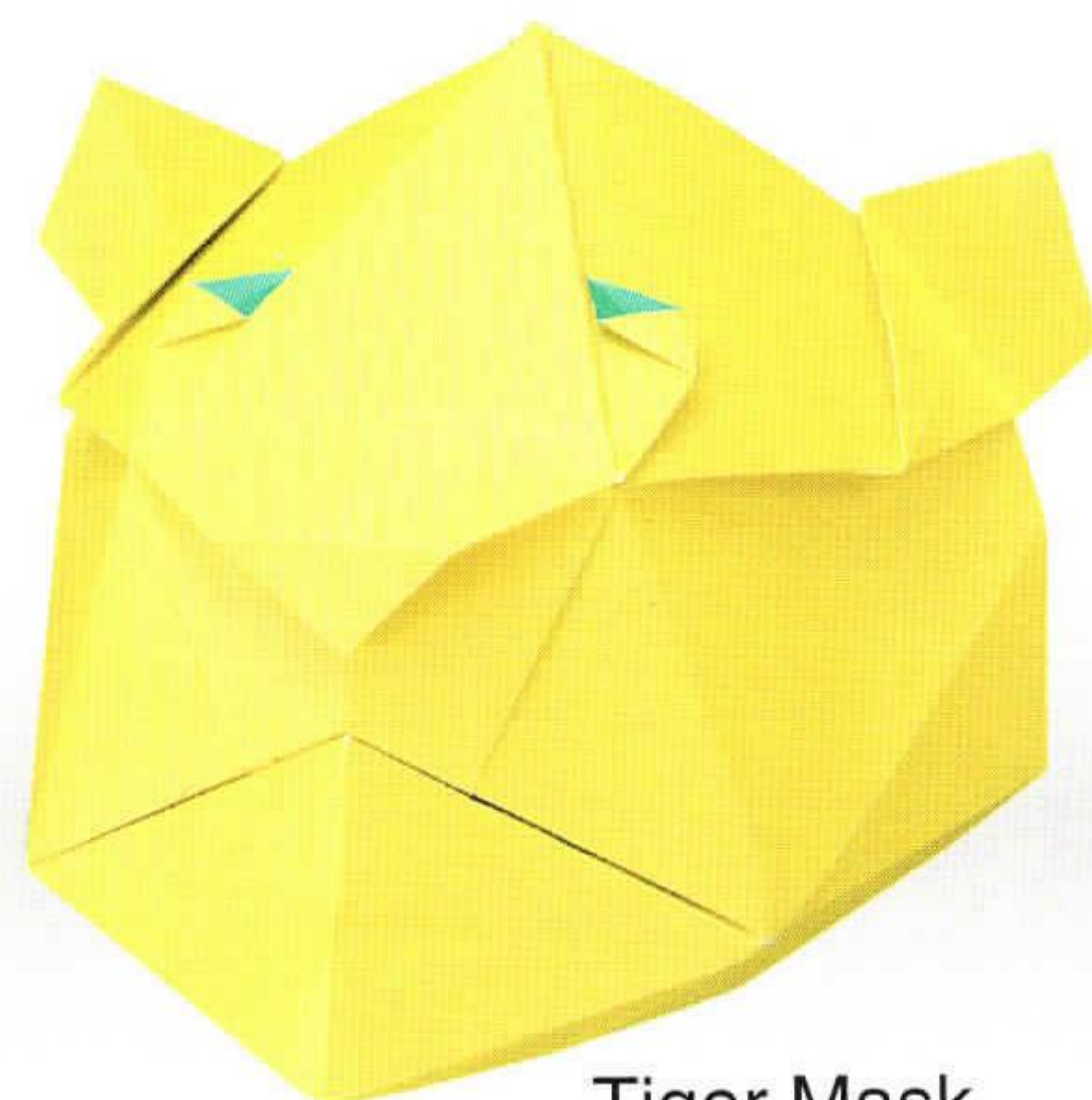
Intermediate Models



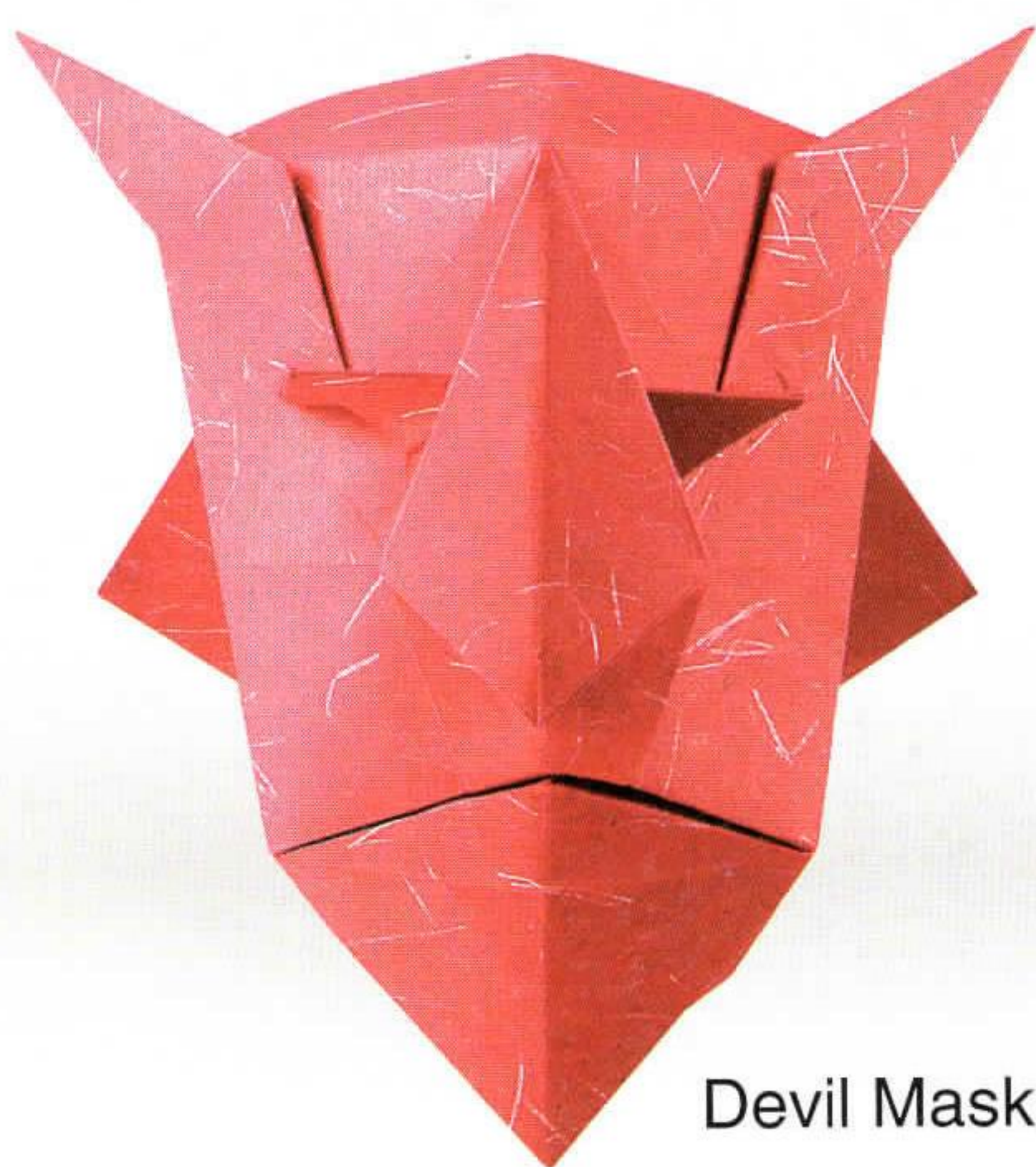
Rabbit



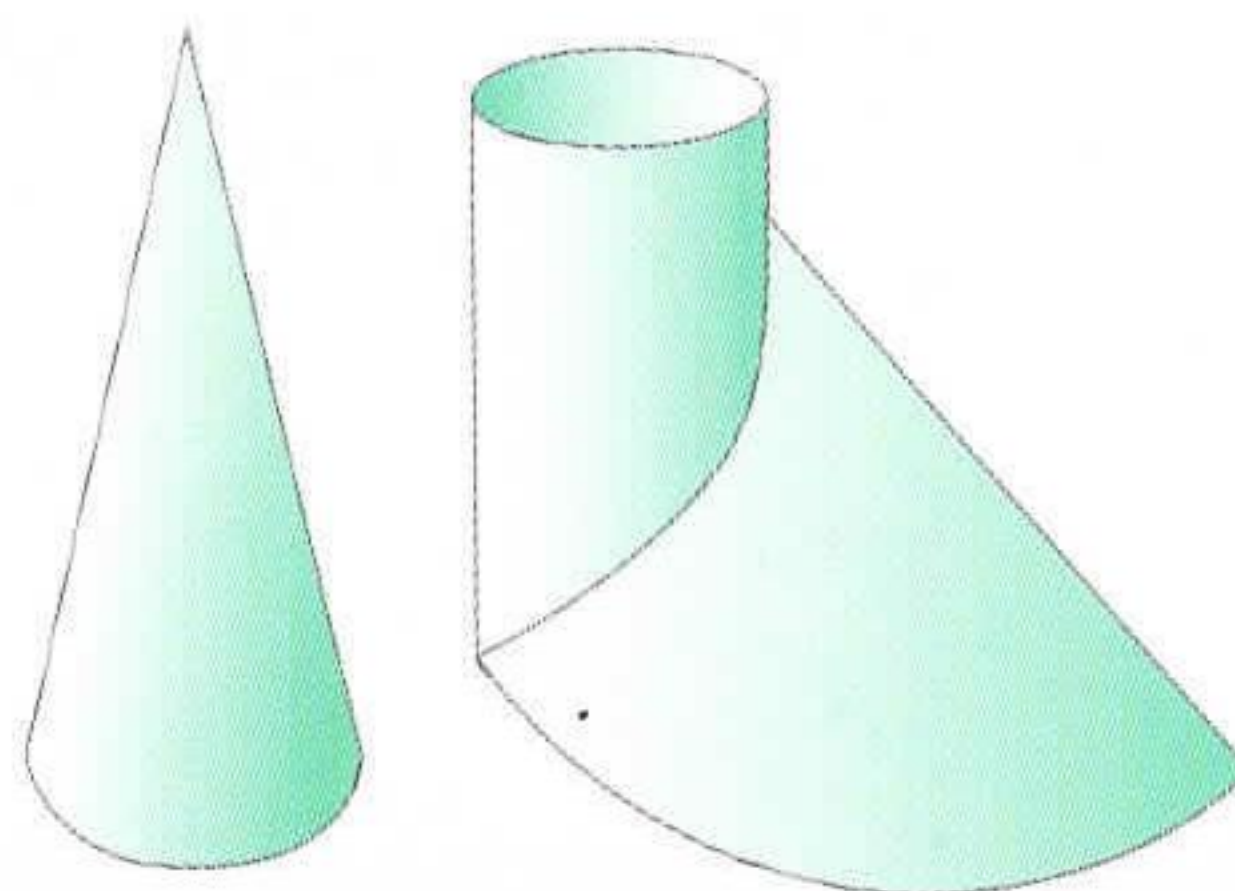
From planes to solid bodies.



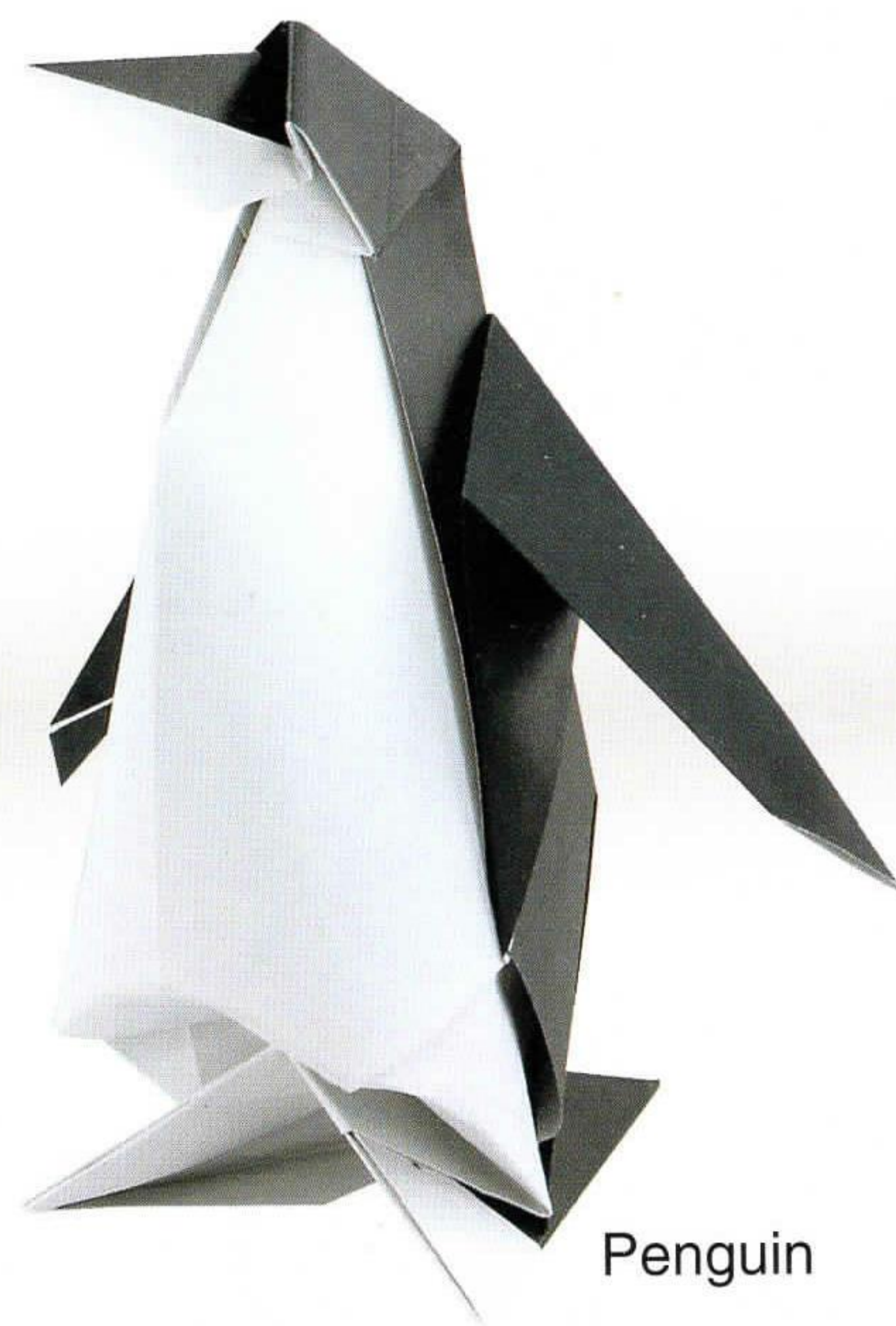
Tiger Mask



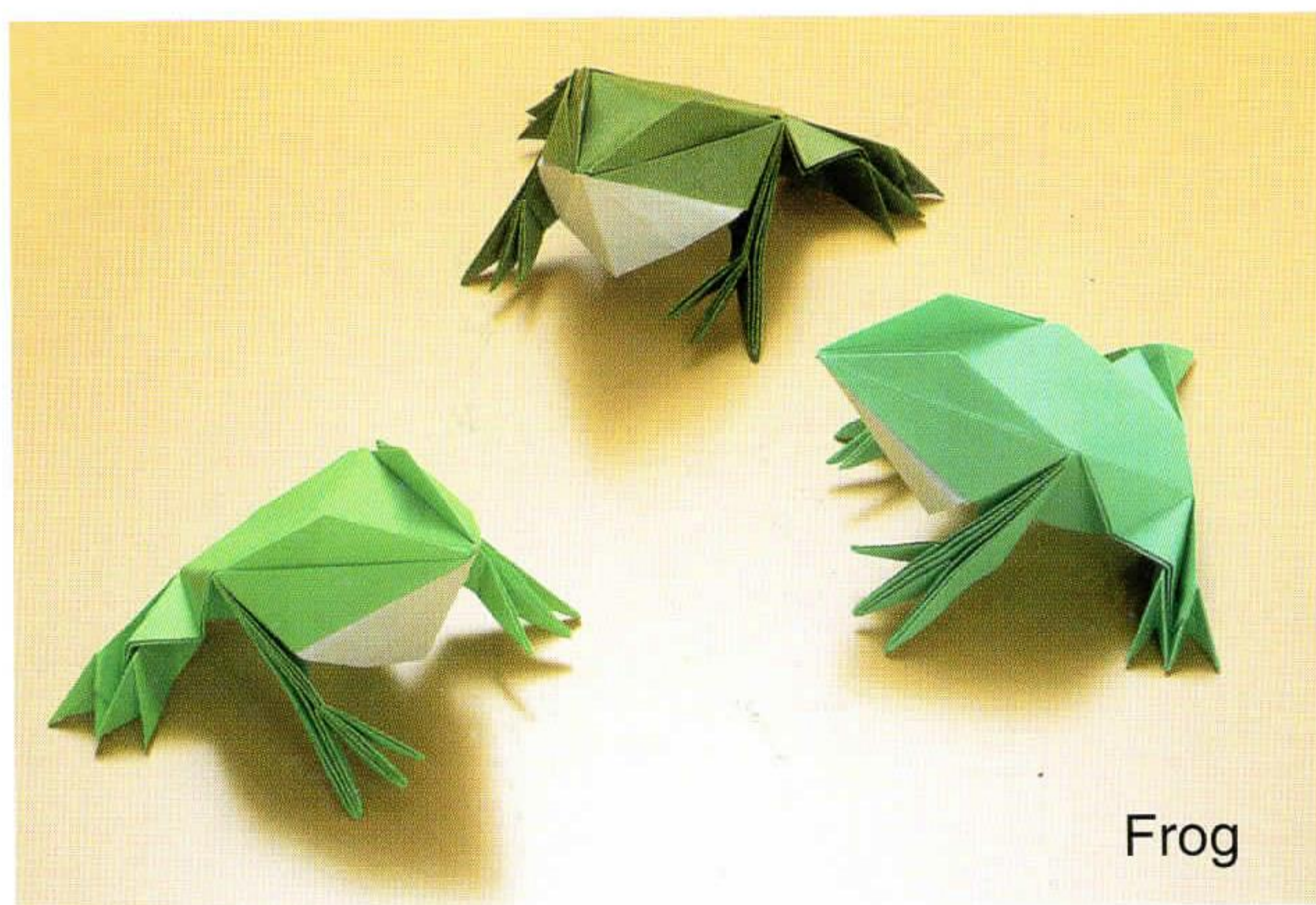
Devil Mask



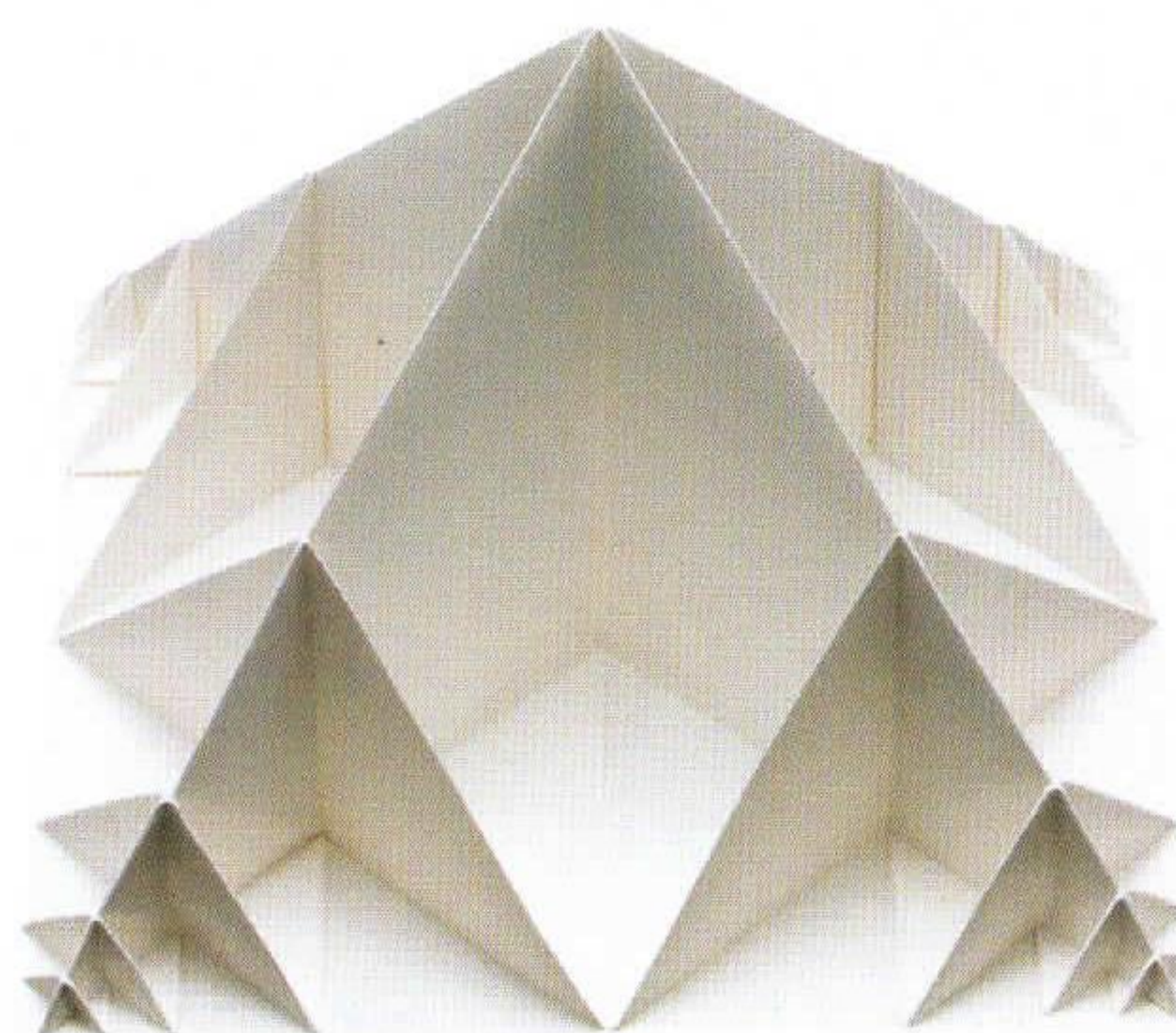
From planes to curved surfaces.



Penguin



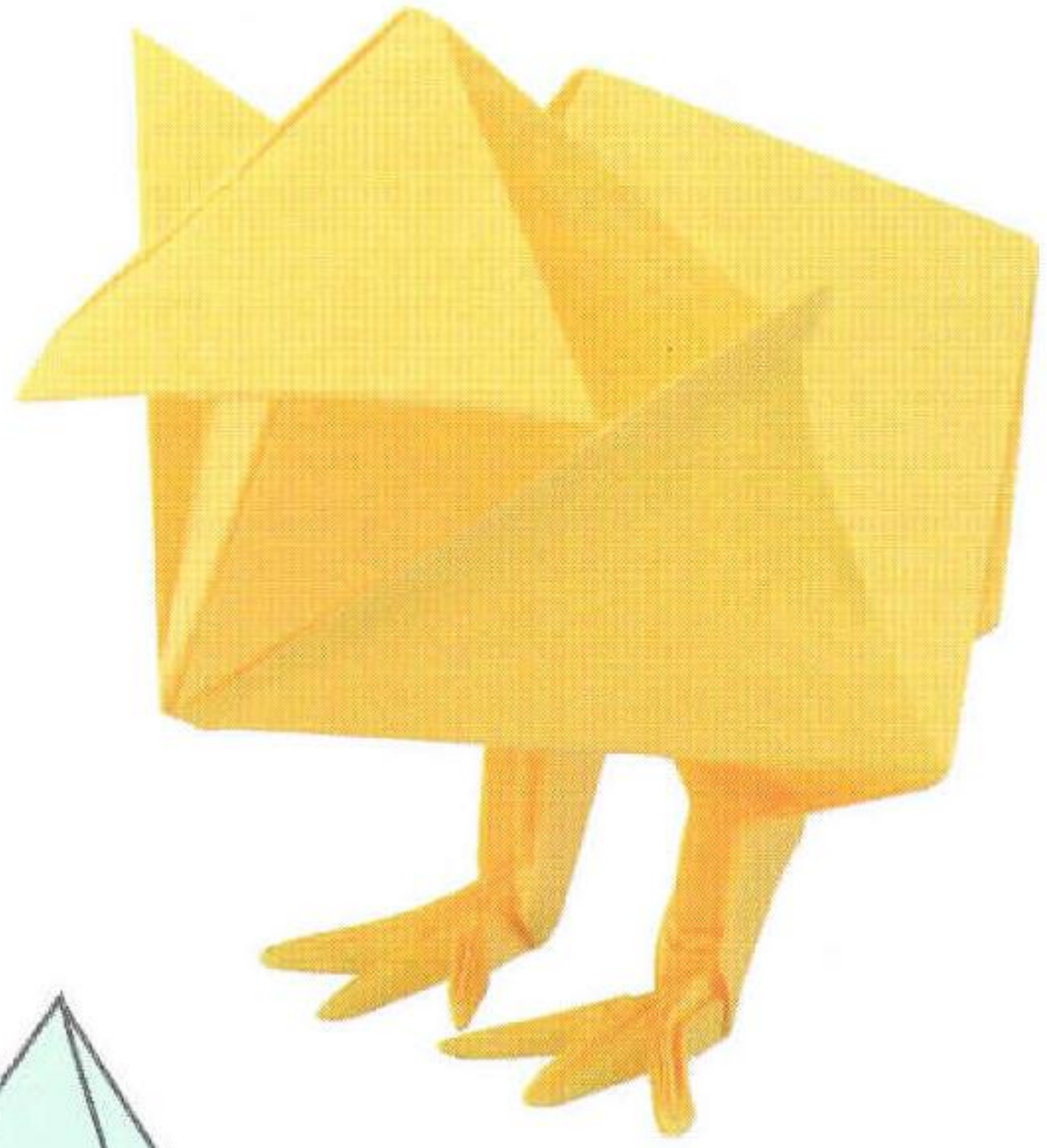
Frog



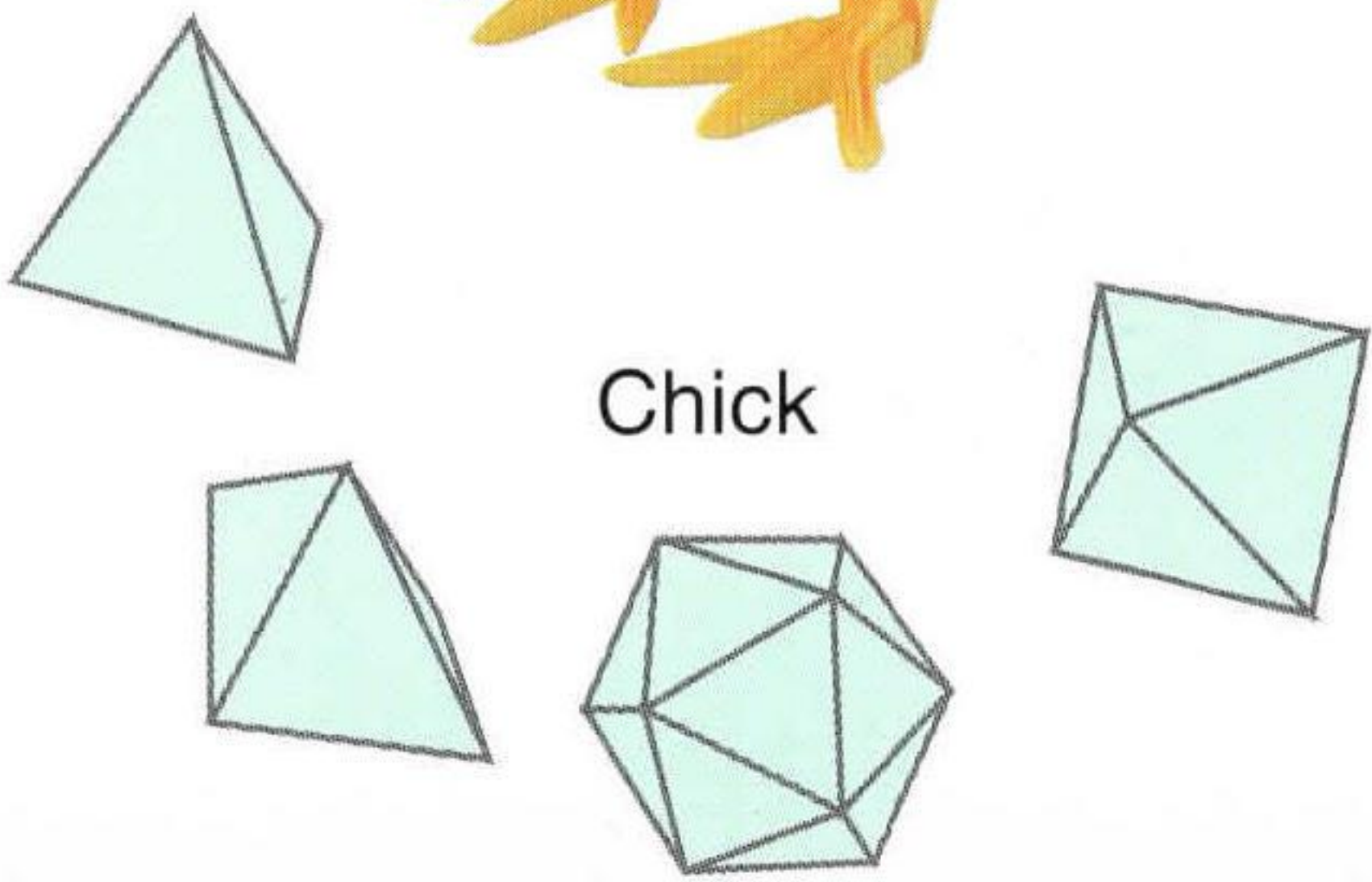
Pyramid

You can fold forever.

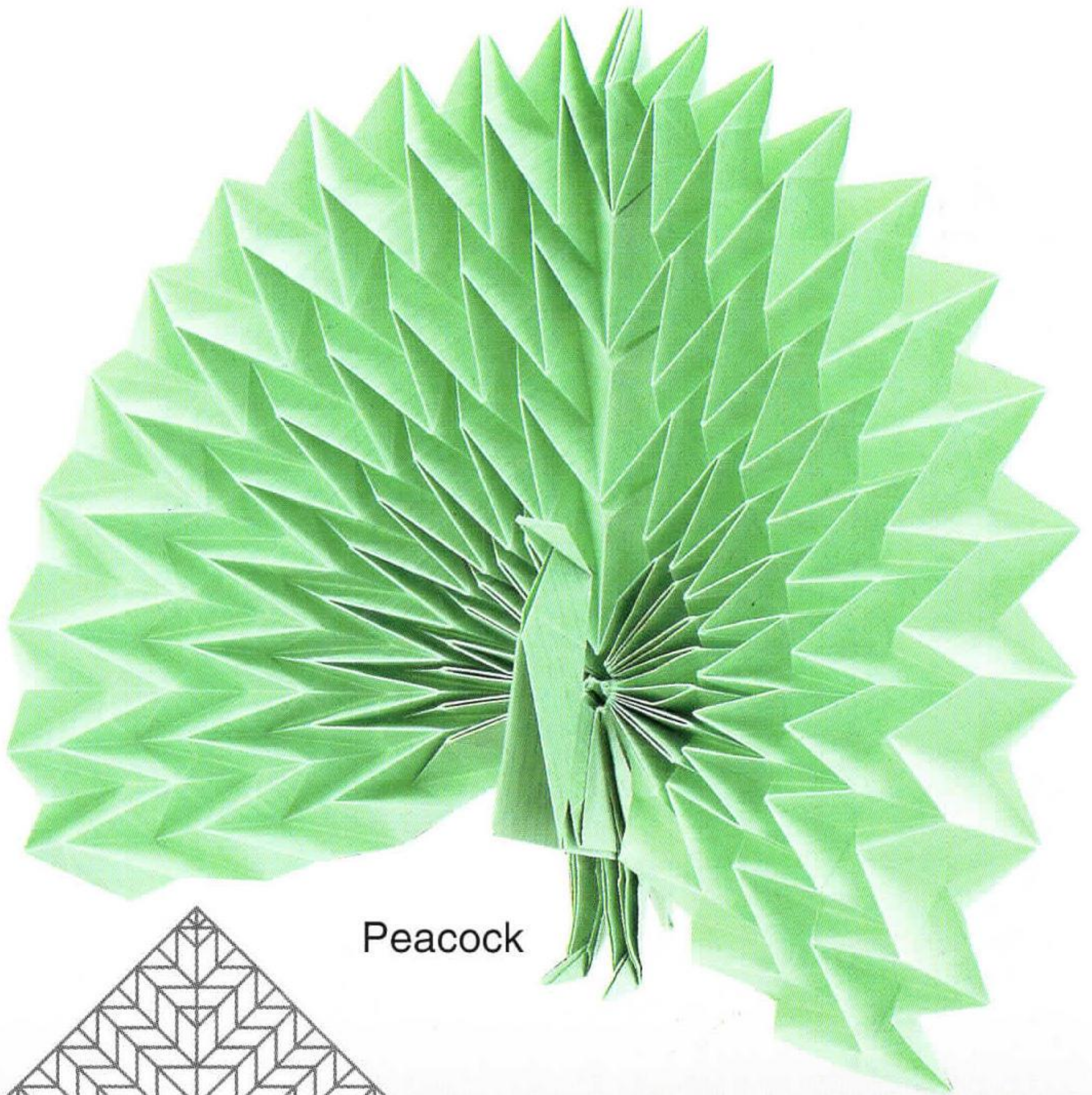
◆ Complex Models ◆



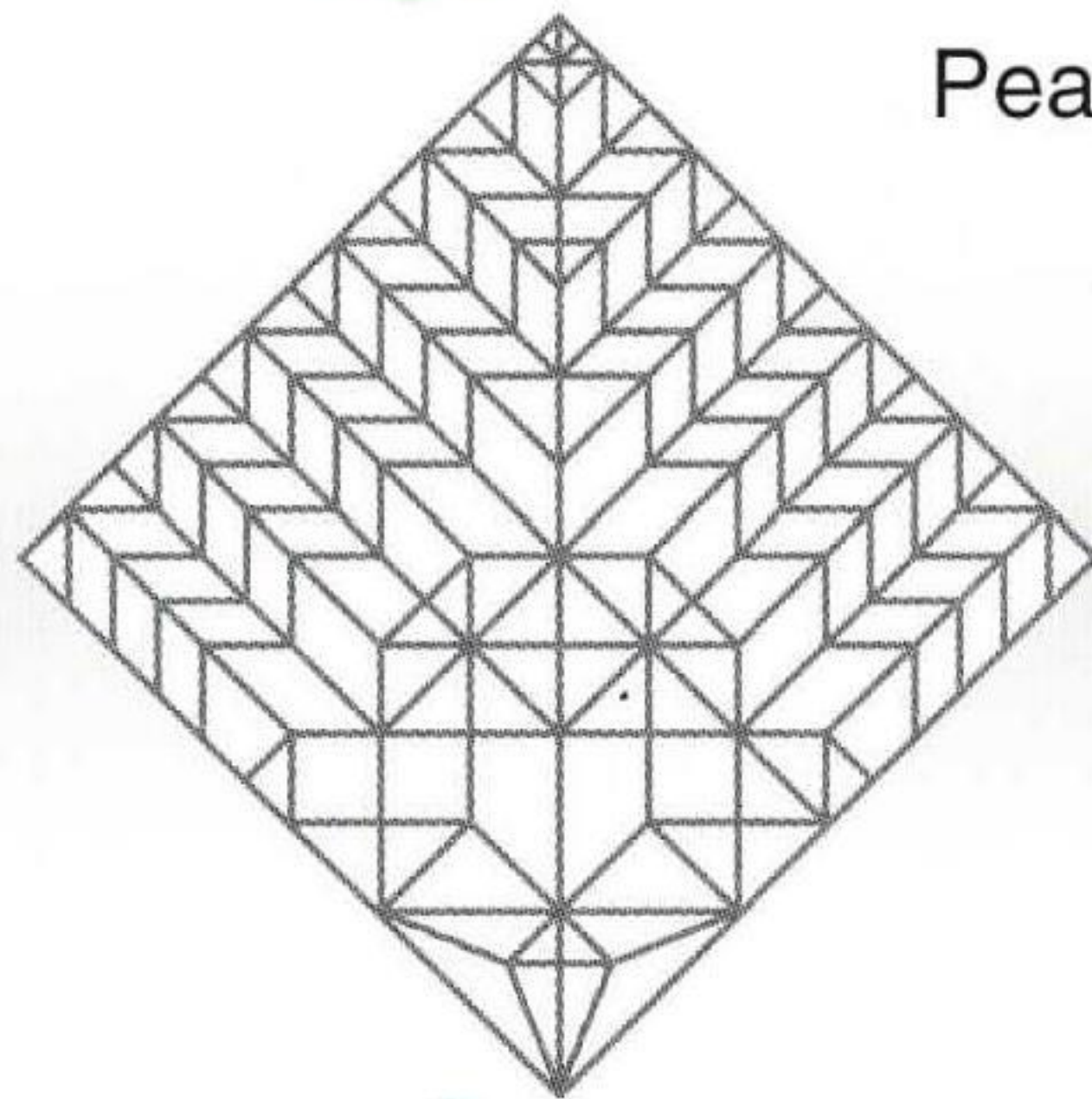
Chick



Cute polyhedra



Peacock

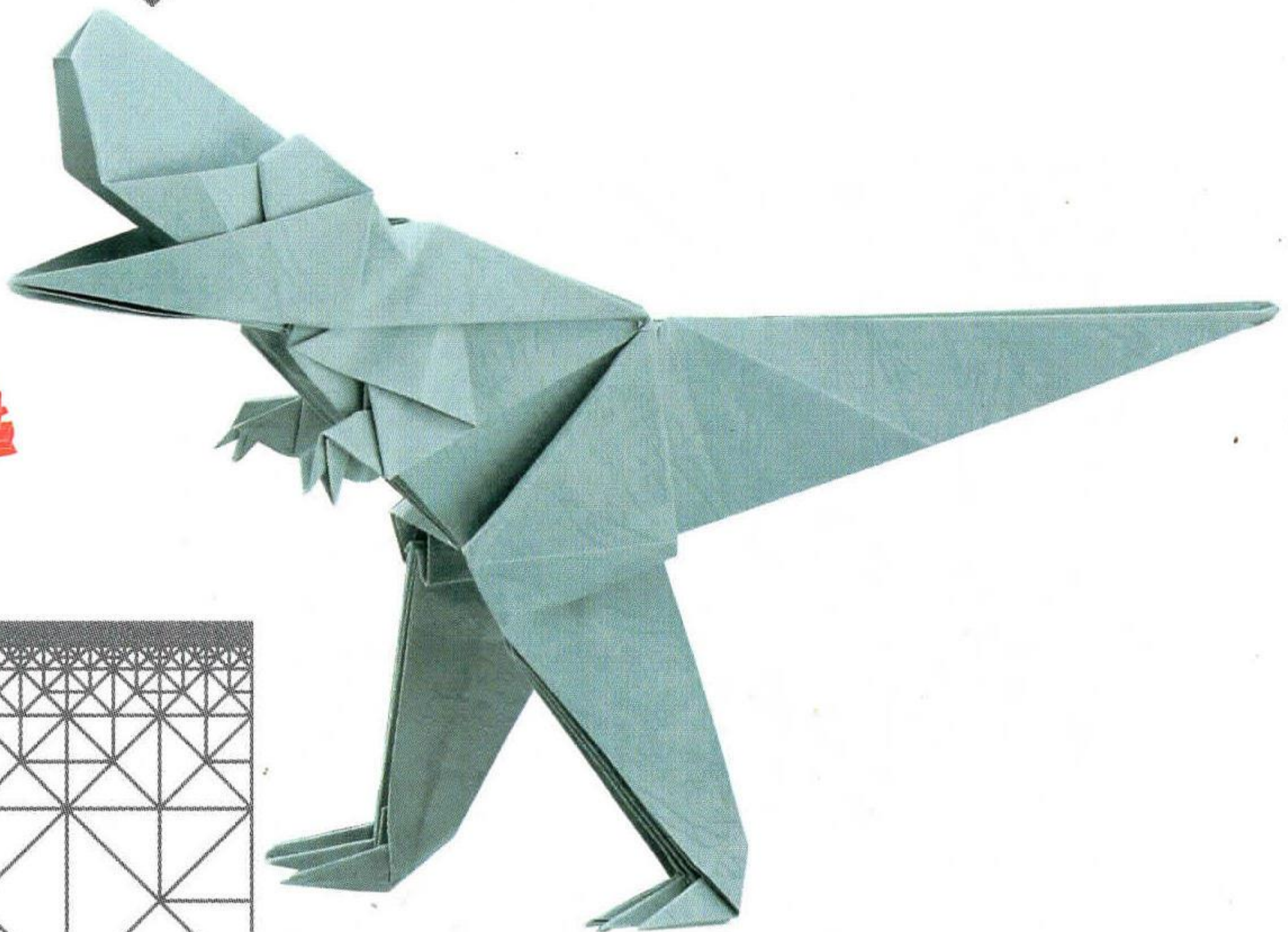


Relationship to space engineering?



Turkey

Modeling theory of the Nature.

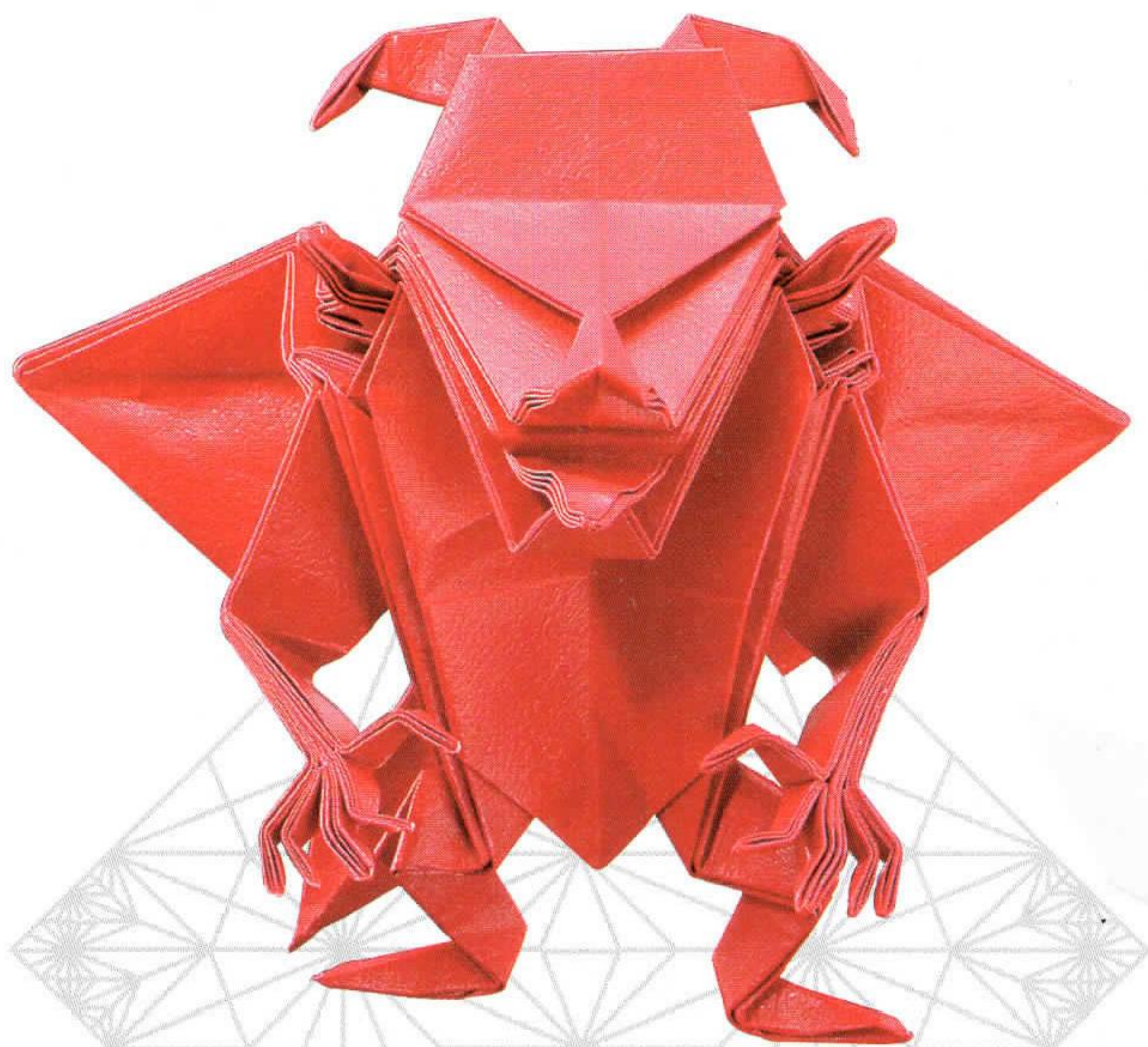


Tyrannosaurus

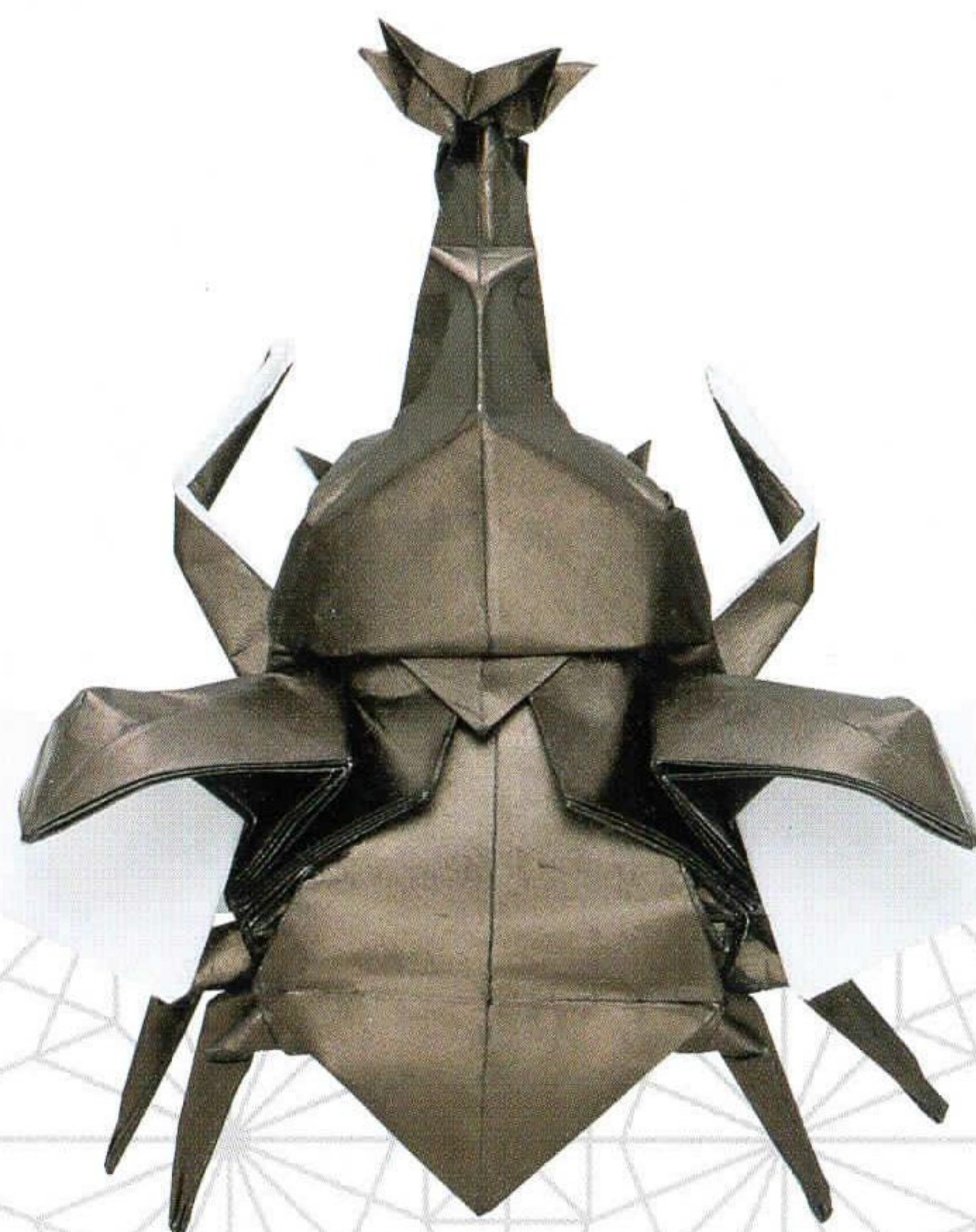
Dynamic and balanced

◆ Complex Models ◆

You had been initiated into the secrets when you fold these.



Devil

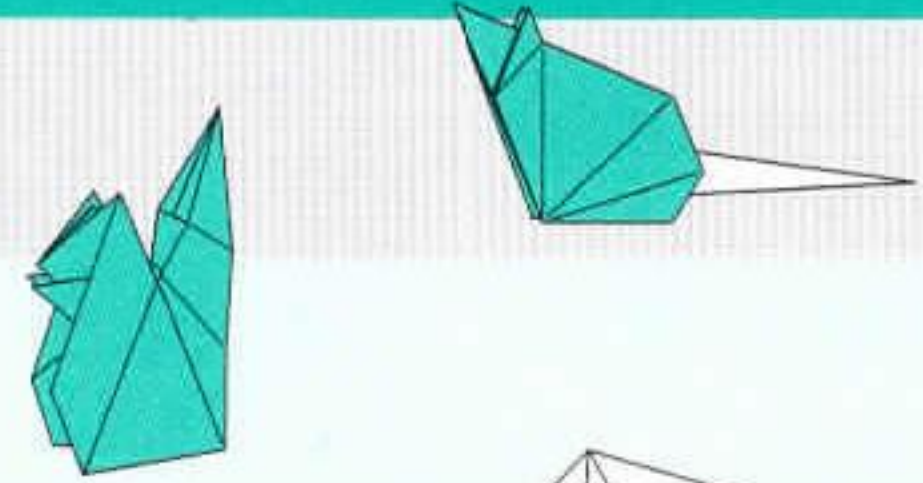

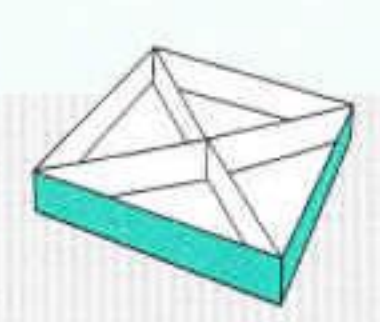
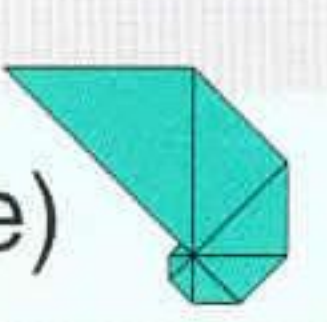

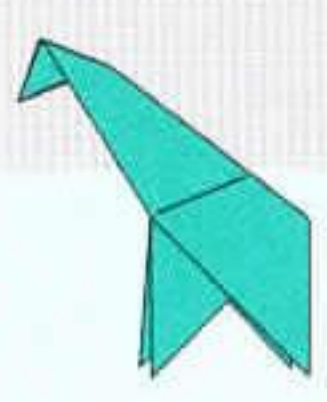
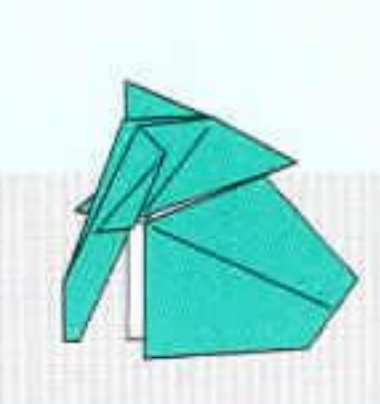
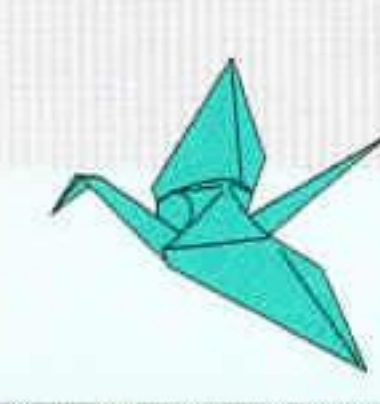
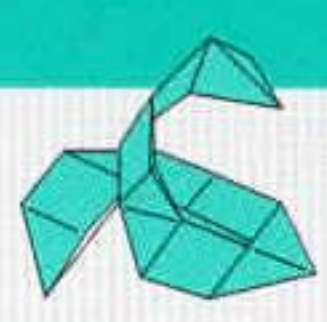
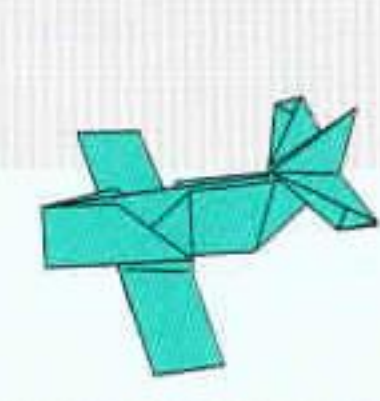


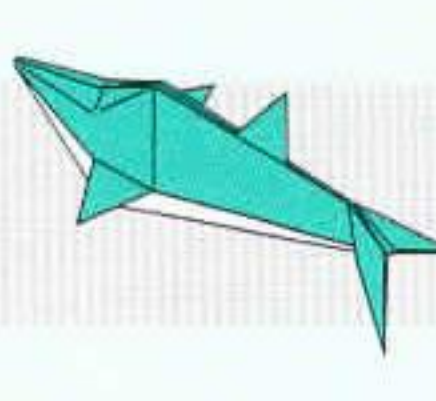
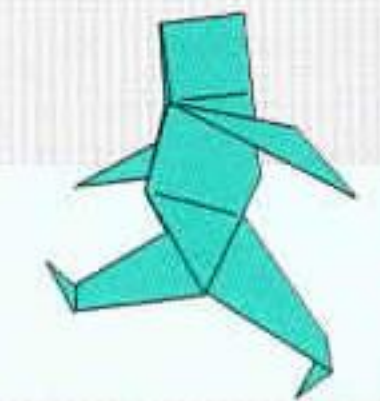
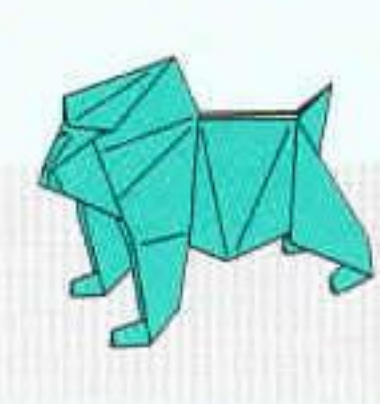
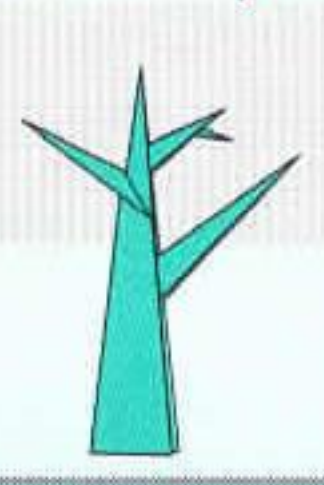
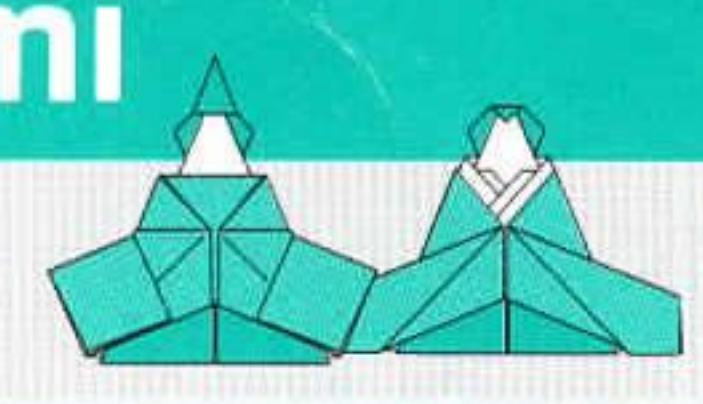
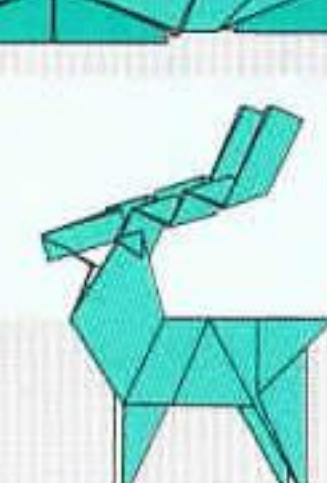
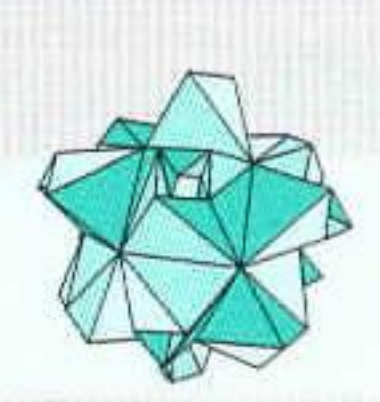






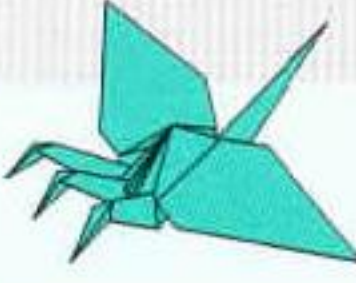

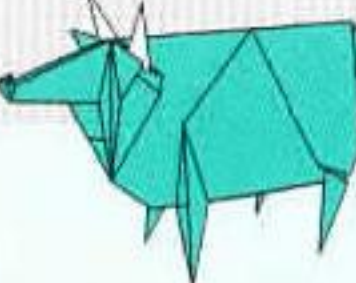
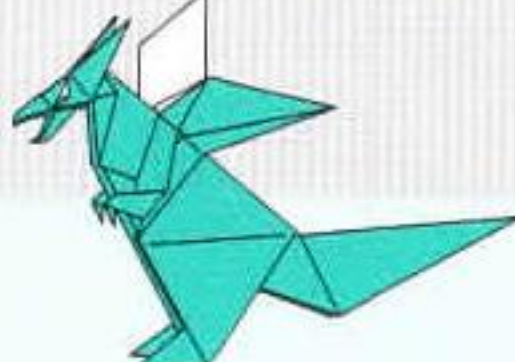
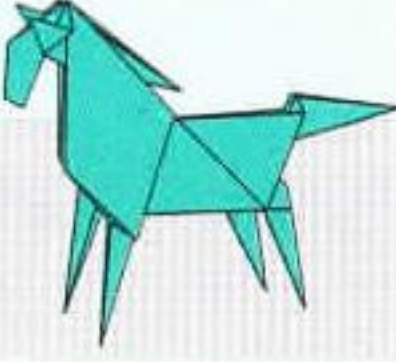
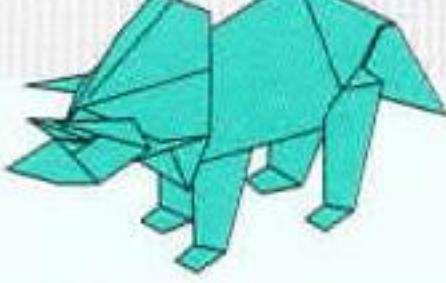


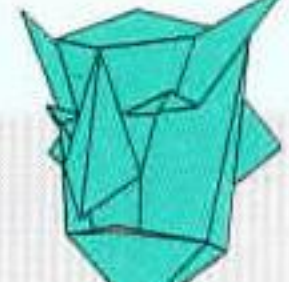






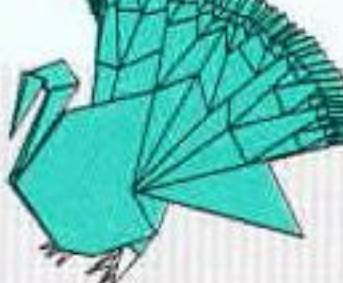
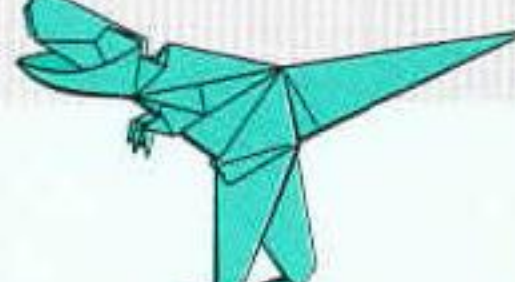

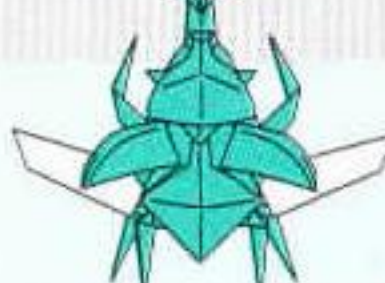

Samurai Helmet
Beetle



Eastern Dragon

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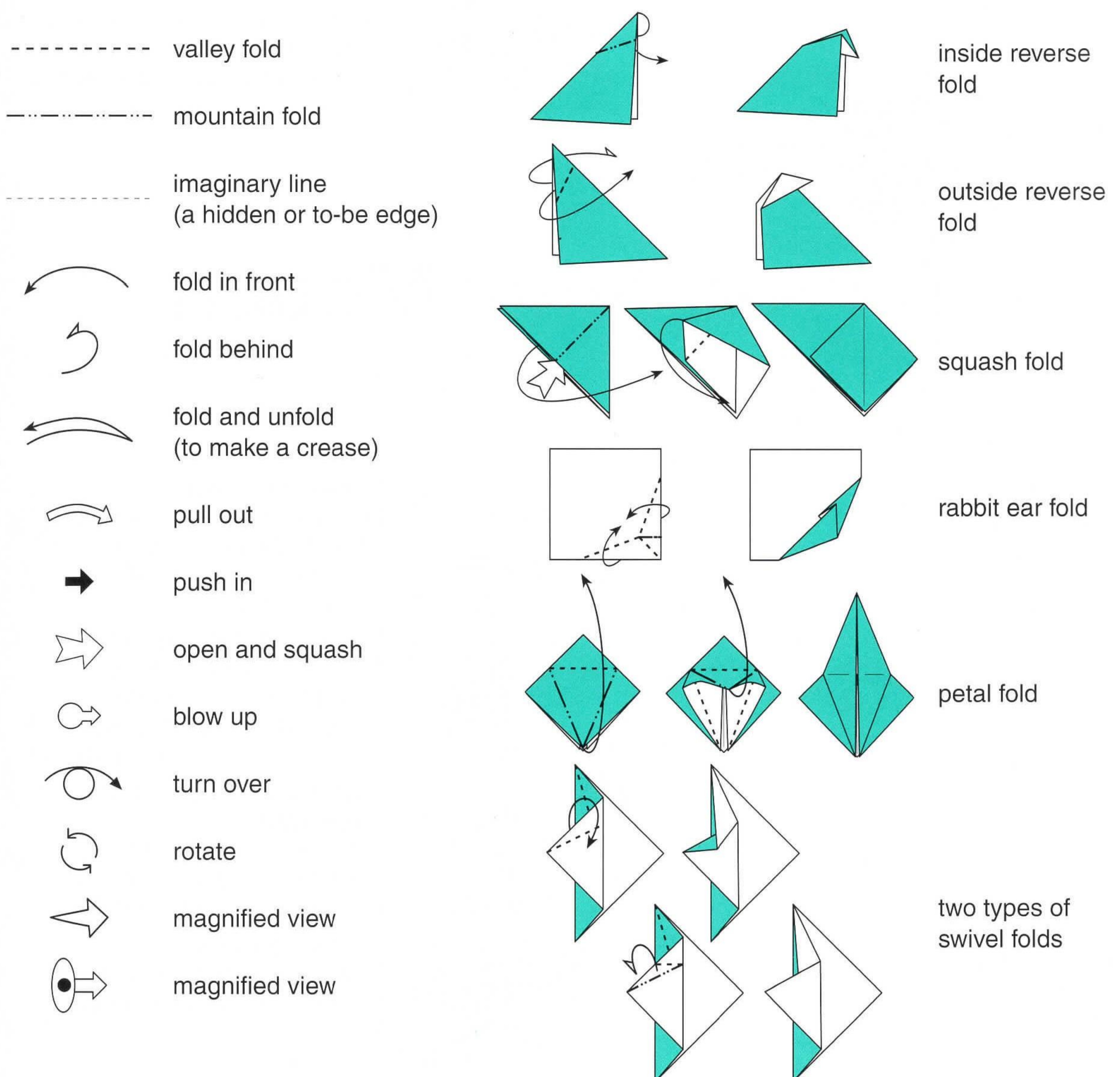
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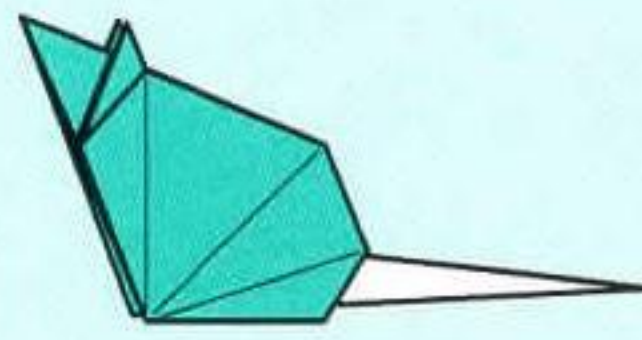
◆ Symbols and Basic Folds ◆

Before you start to make origami models, you must be familiar with the symbols and terms that have special meanings in origami.

Though there is no rule or code about the symbols, there is a standard set of symbols that is used in many origami books. I adopt that convention, which is shown below. In addition, as I have said in **Introduction**, explanations of symbols and terms are included in the diagrams so that you will be able to learn them by folding each model.

There are many techniques that are not explained in this page, but they are explained along with the diagrams. Refer the index at the end of this book.





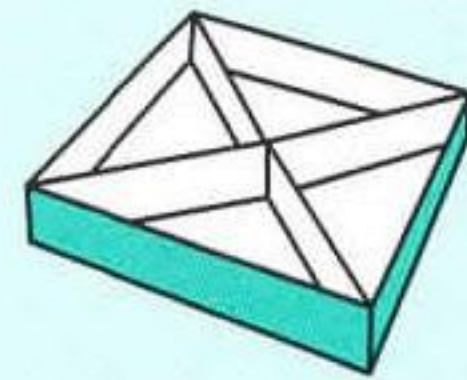
Mouse

Theme: Understand symbols
Explains basic symbols as well as techniques including inside reverse folds and rabbit ear folds.



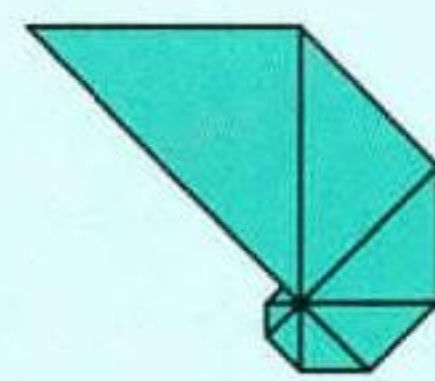
Squirrel

Theme: Base
Looks into the base, which is a halfway shape that appears in the course of a sequence. Also explains pleat folds and other techniques.



Partitioned Box

Theme: Bird base
Explains the Bird base, the most important base of all, although in a slightly bizarre way.



Conch

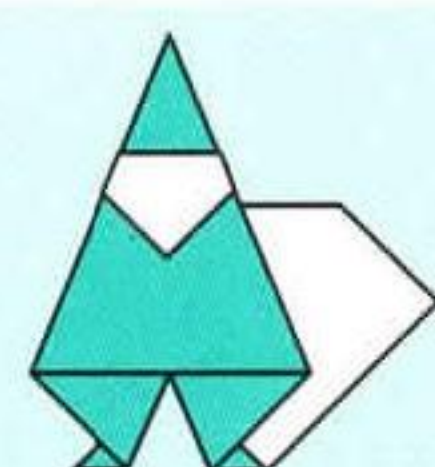
Theme: Trisection; Isosceles right triangle
Shows one of the sequences that trisect precisely a side. Also, explores the shape of isosceles right triangles.

Chapter 1

Fundamental Models

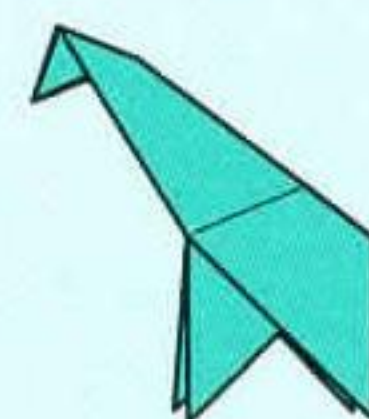
“ ‘Excellent !’ I cried. ‘Elementary.’ said he.”

Arthur Conan Doyle, Memories of Sherlock Holmes



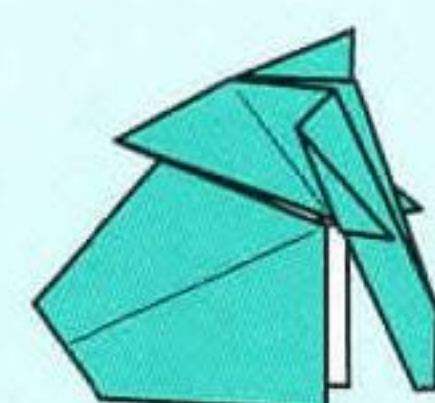
Santa Claus

Theme: Inside-out
Introduces an example of model that uses the different colors of each side of the paper. Also explains swivel folds.



Giraffe

Theme: “Mitate”; Sink fold
An example of model that use “mitate,” a form of expression where a simple shape is compared to another. Also explains sink folds.



Elephant

Theme: Blintz fold; Outside reverse fold
Illustrates the blintz fold as one of devices for origami design. Also explains outside reverse folds.



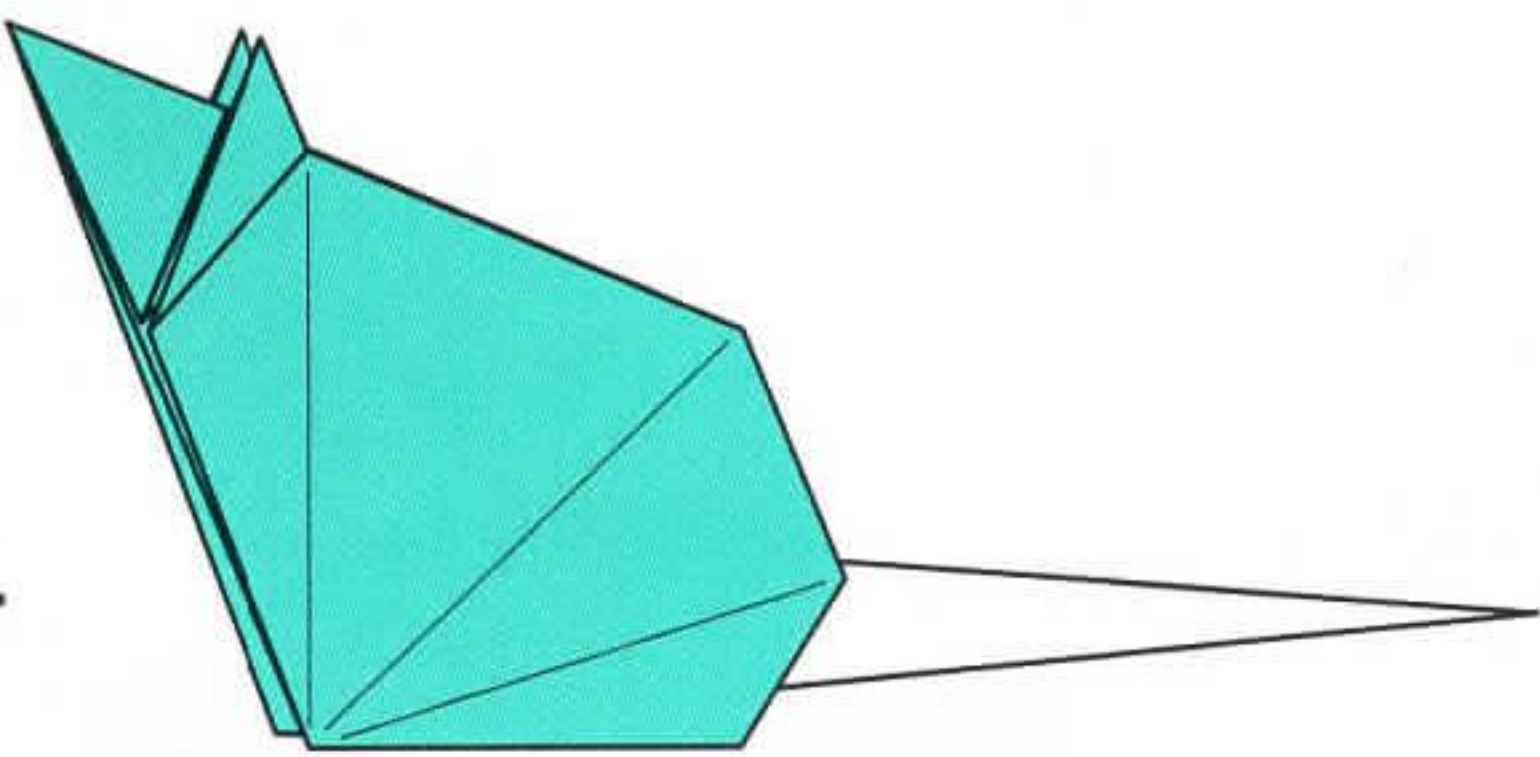
Orizuru Transformation

Theme: Geometry
Examines the geometry of origami by looking into the transformation of origami crane.

Mouse

Theme: Understand symbols

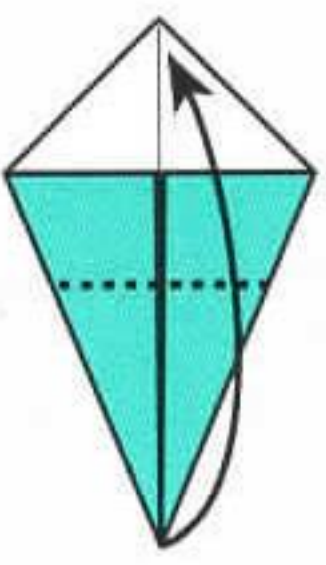
Fold using 6" (15 cm) origami paper.

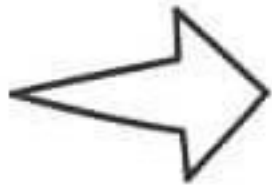
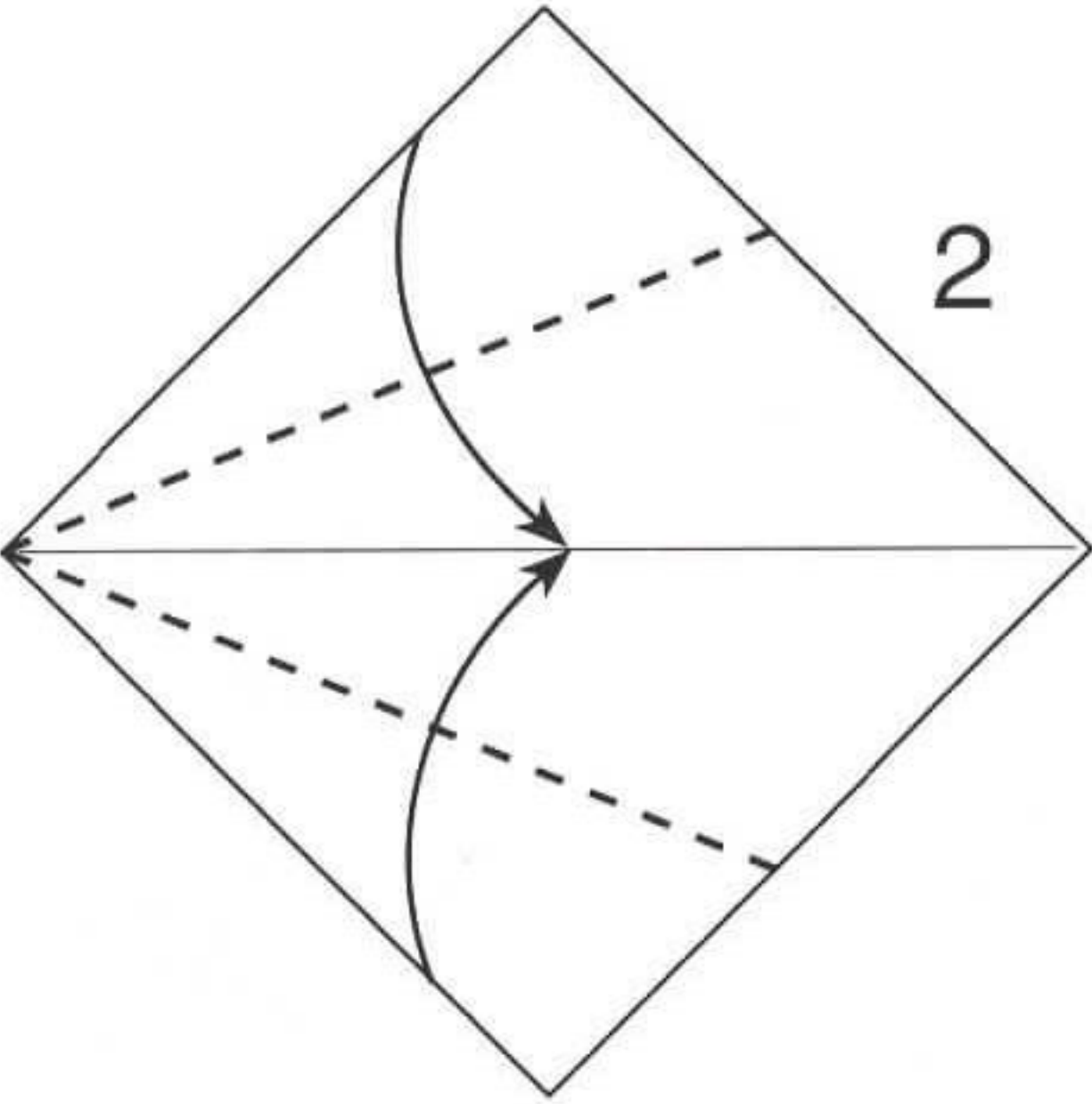
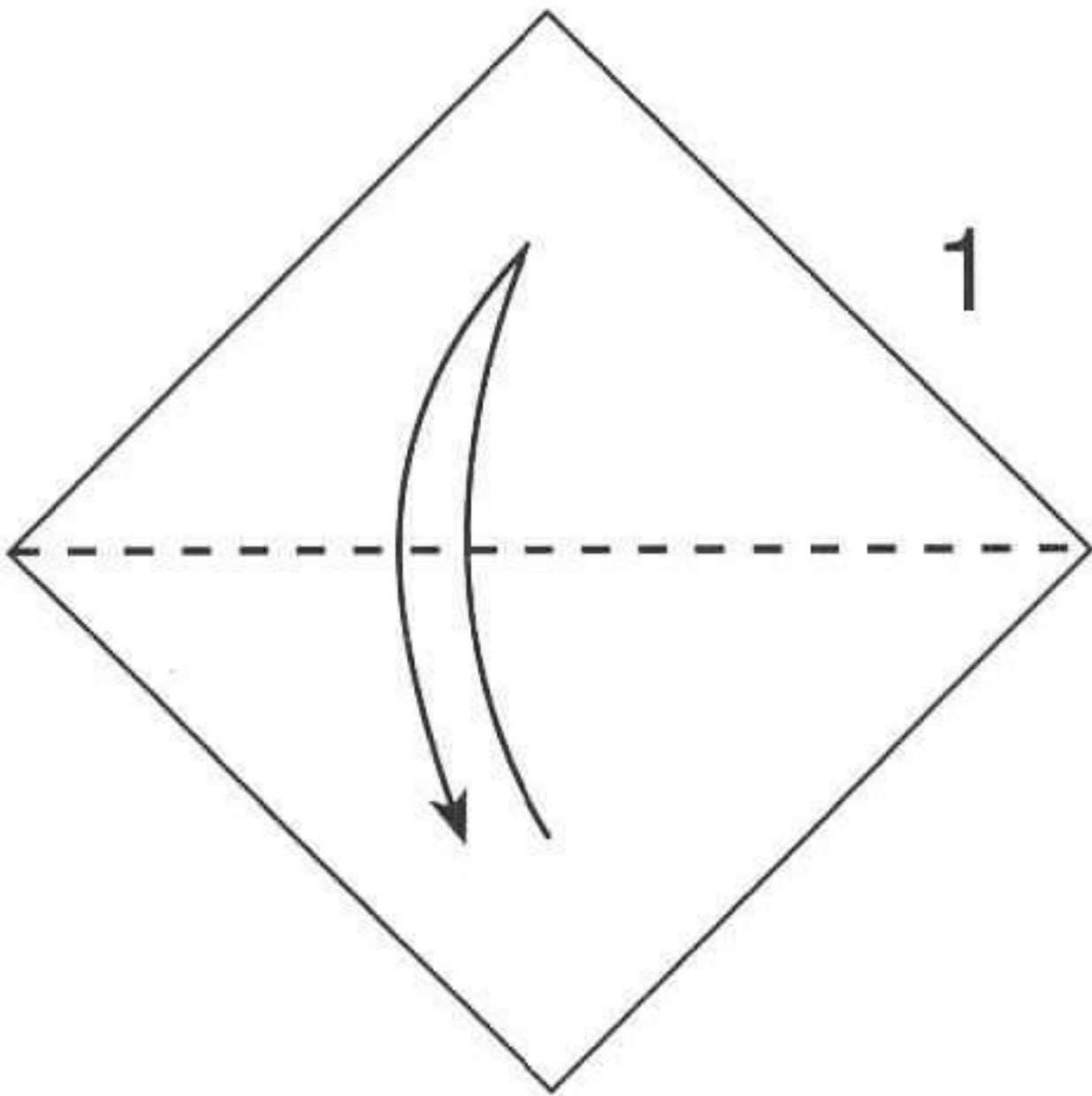


The first model is the *Mouse*, which is the first animal of the Chinese zodiac. Since the theme is to understand symbols, I have included several annoyingly-plentiful notes. Make sure to look through them.

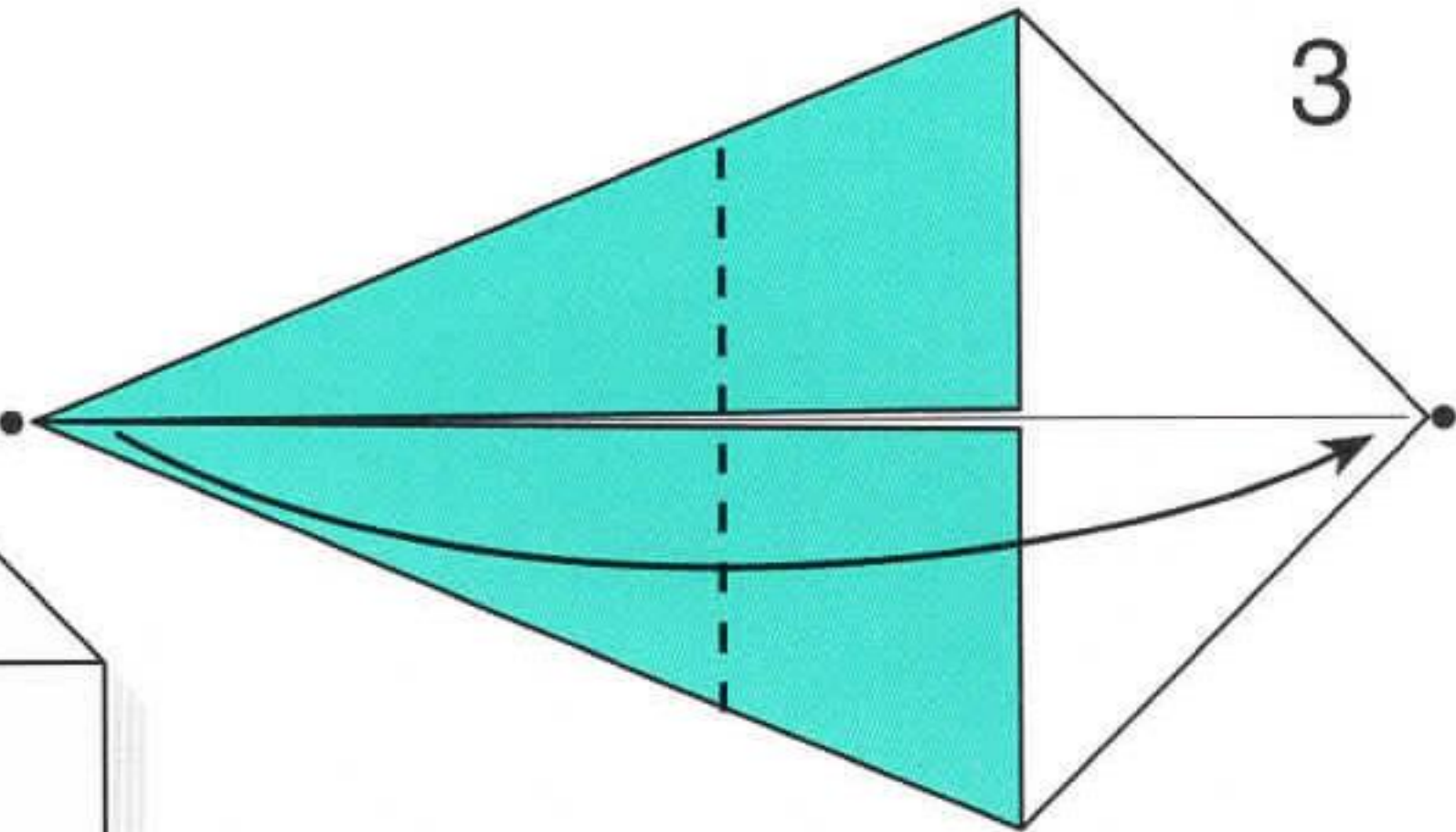
A dashed line indicates a valley fold. A reflected arrow represents **to fold and unfold**, i.e. to make a crease.

A black-headed arrow indicates **to fold**. That means almost all folds except mountain folds are expressed by such arrow.

 It may be easier to fold in the orientation shown on the left. It is often the case that you can fold easier in a different orientation than indicated in diagrams. Also note that a pair of rotating arrows changes orientation of the model, as in step 4.



➔ An inflating arrow means **magnified view next**.

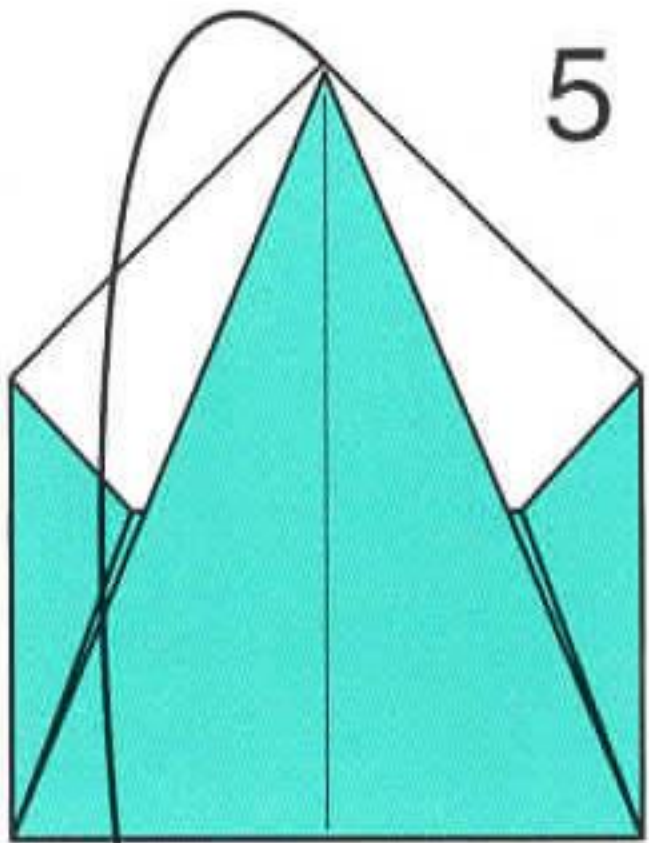
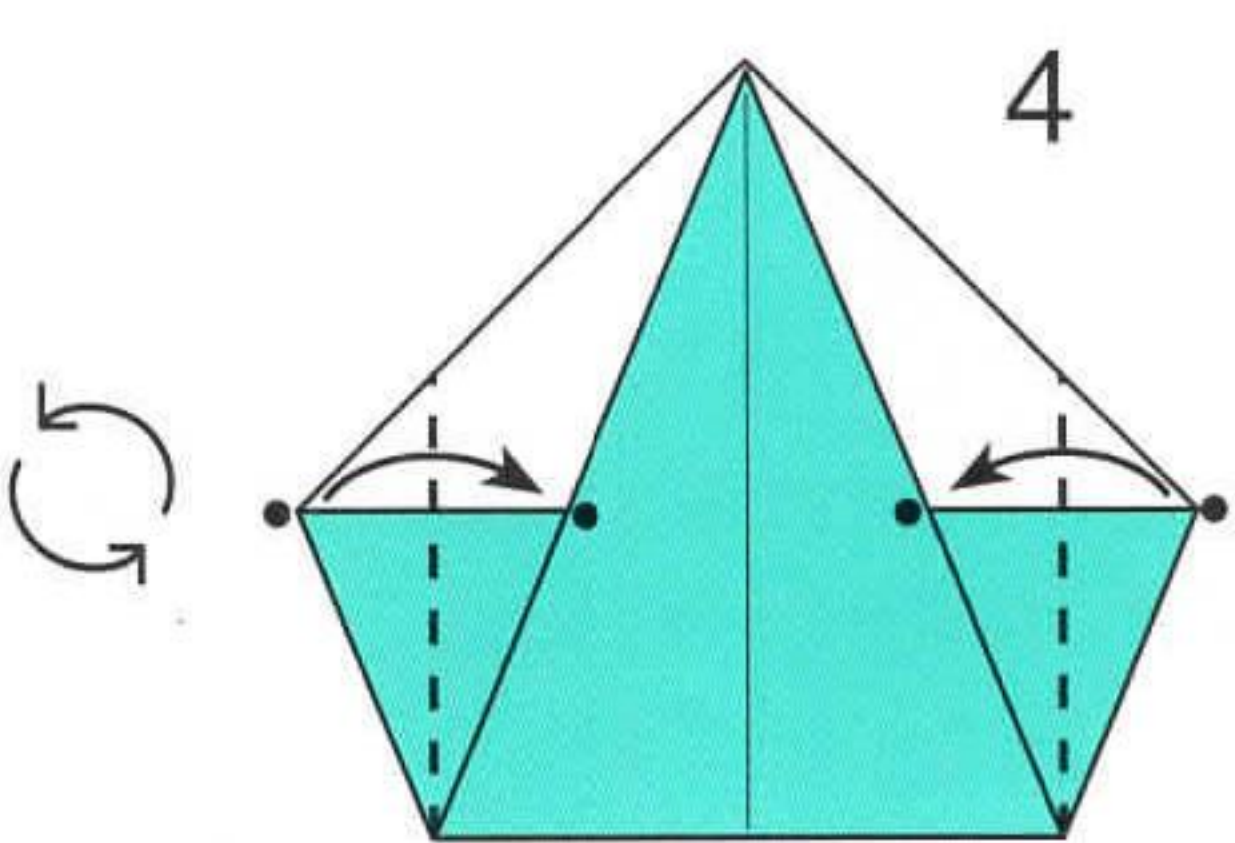


A pair of black dots (as in steps 3, 4, 9, 10) emphasizes that the points are to meet each other.

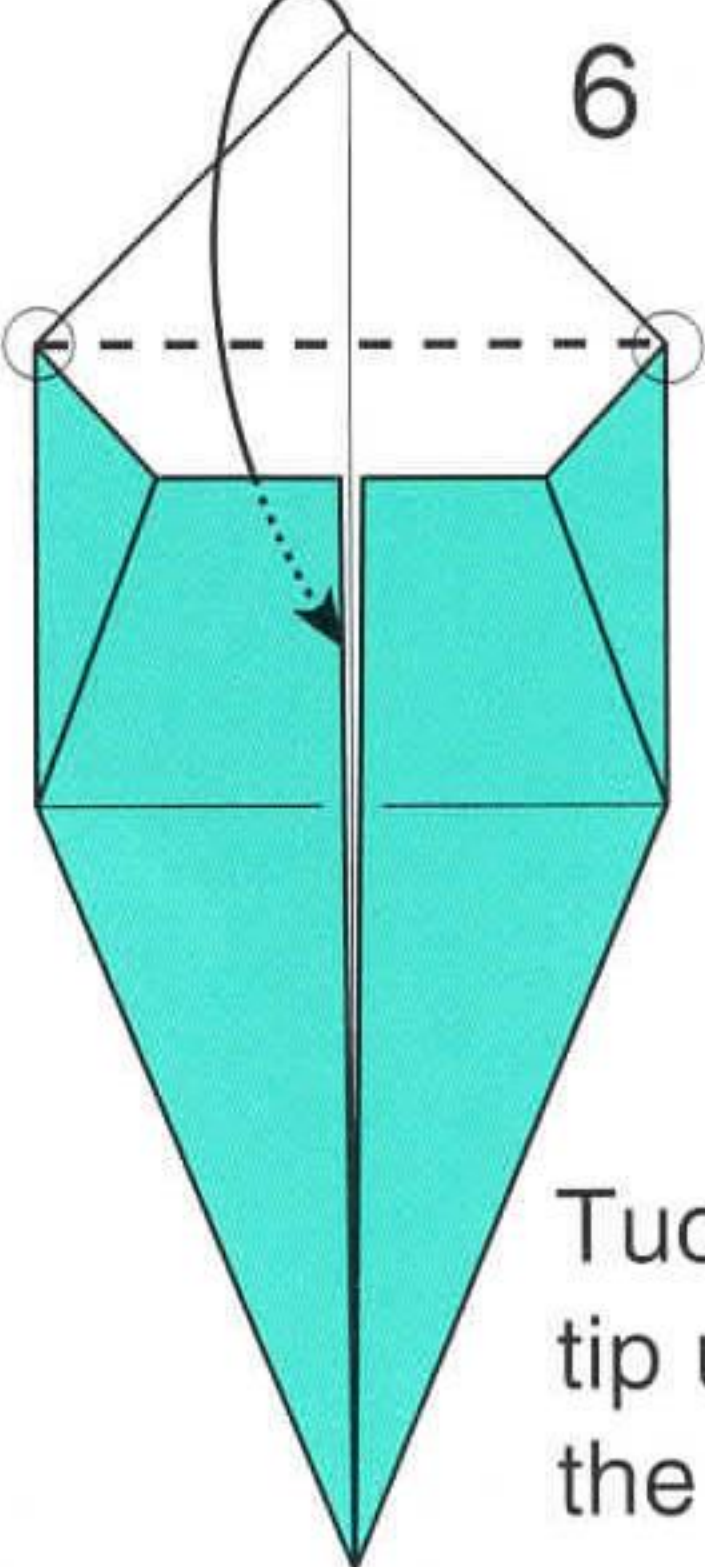
When you follow diagrams, always compare the previous step with the next one to identify the changes in shape.

A white circle (as in step 6) emphasizes a landmark of a crease line.

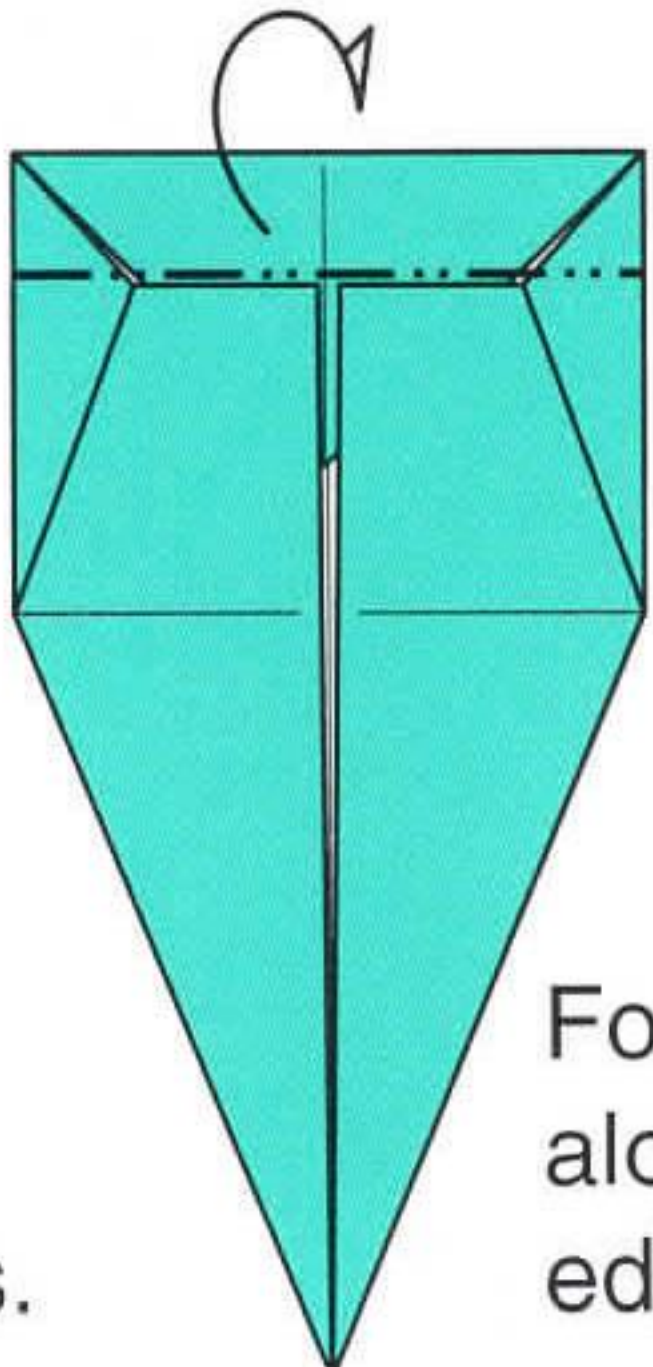
.....
A dot-and-dash line indicates a mountain fold. A white-headed arrow means fold behind. In practice, it is sometimes easier to turn over and valley fold.



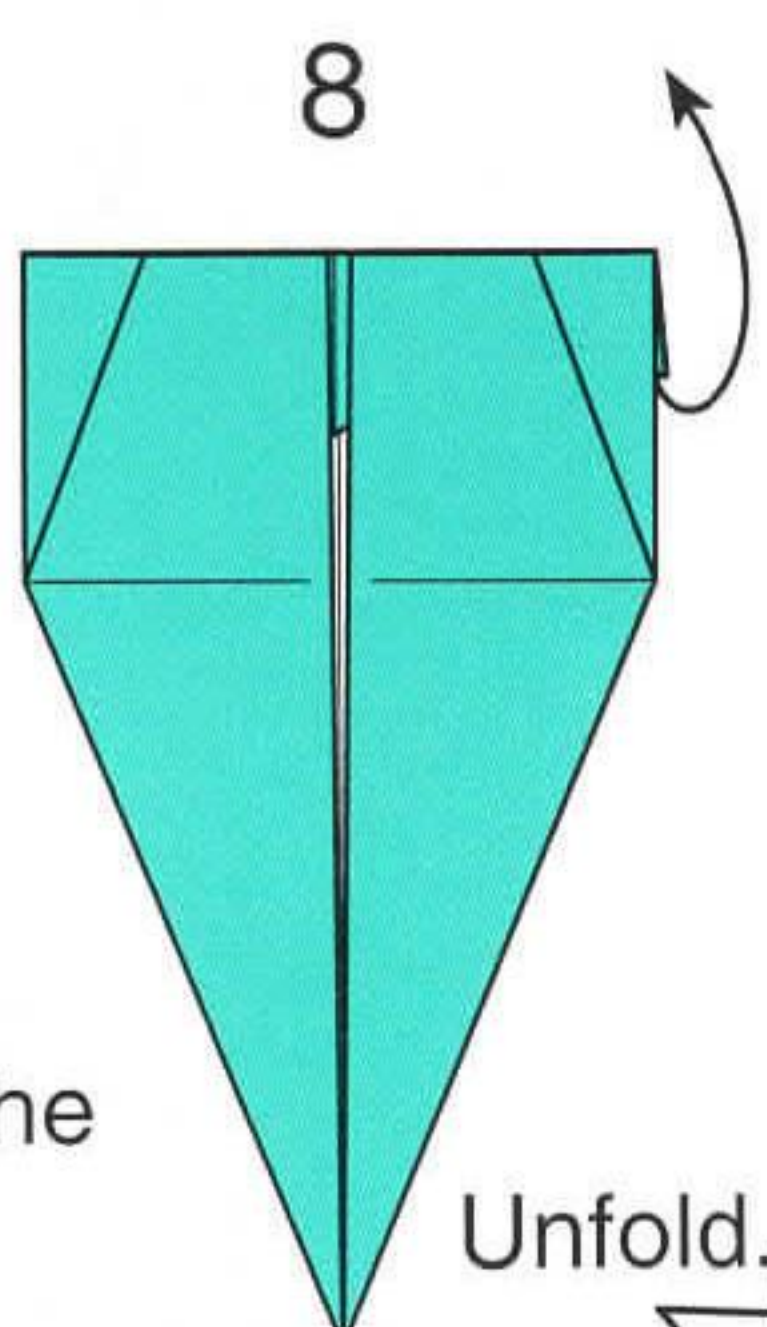
Unfold the long flap.



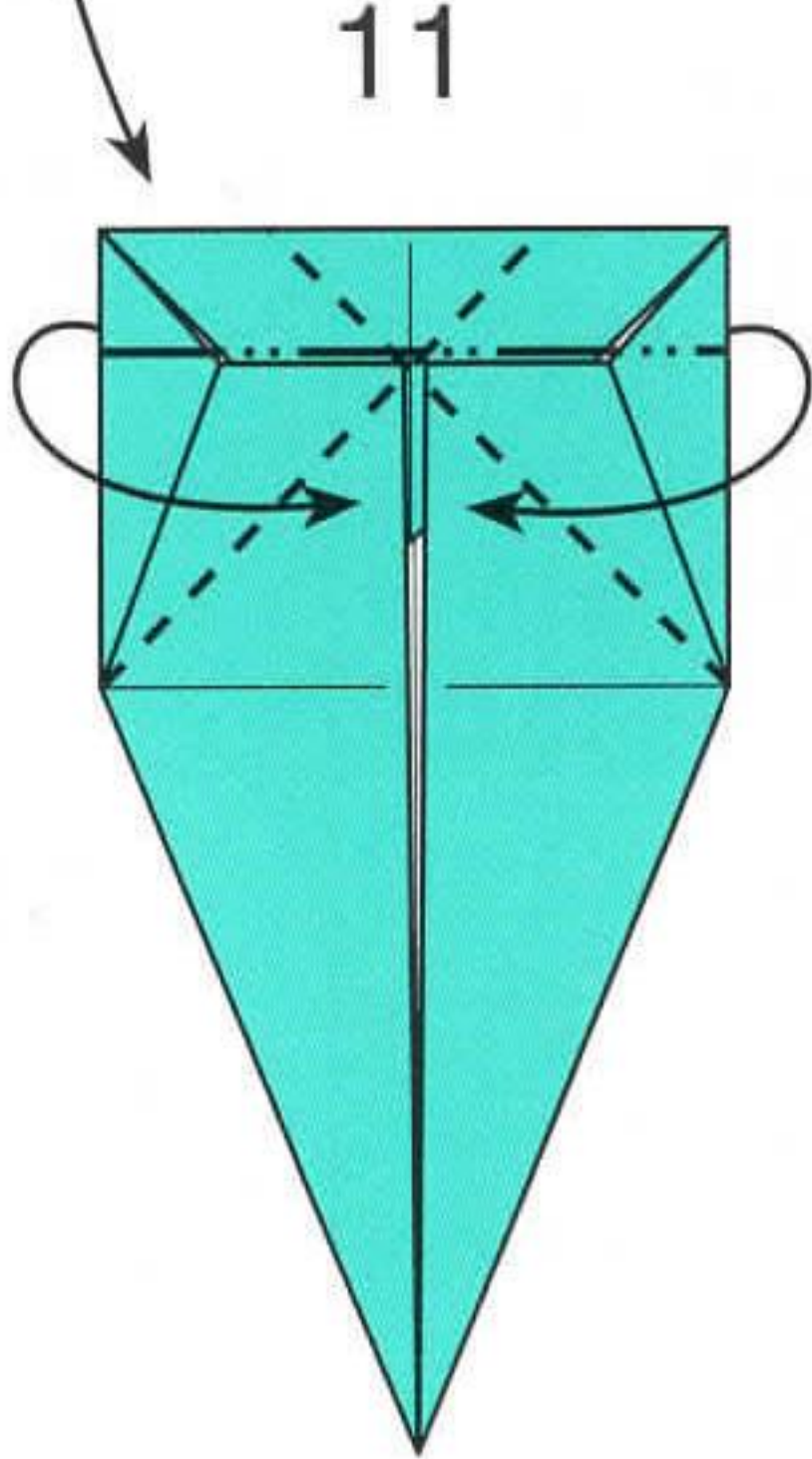
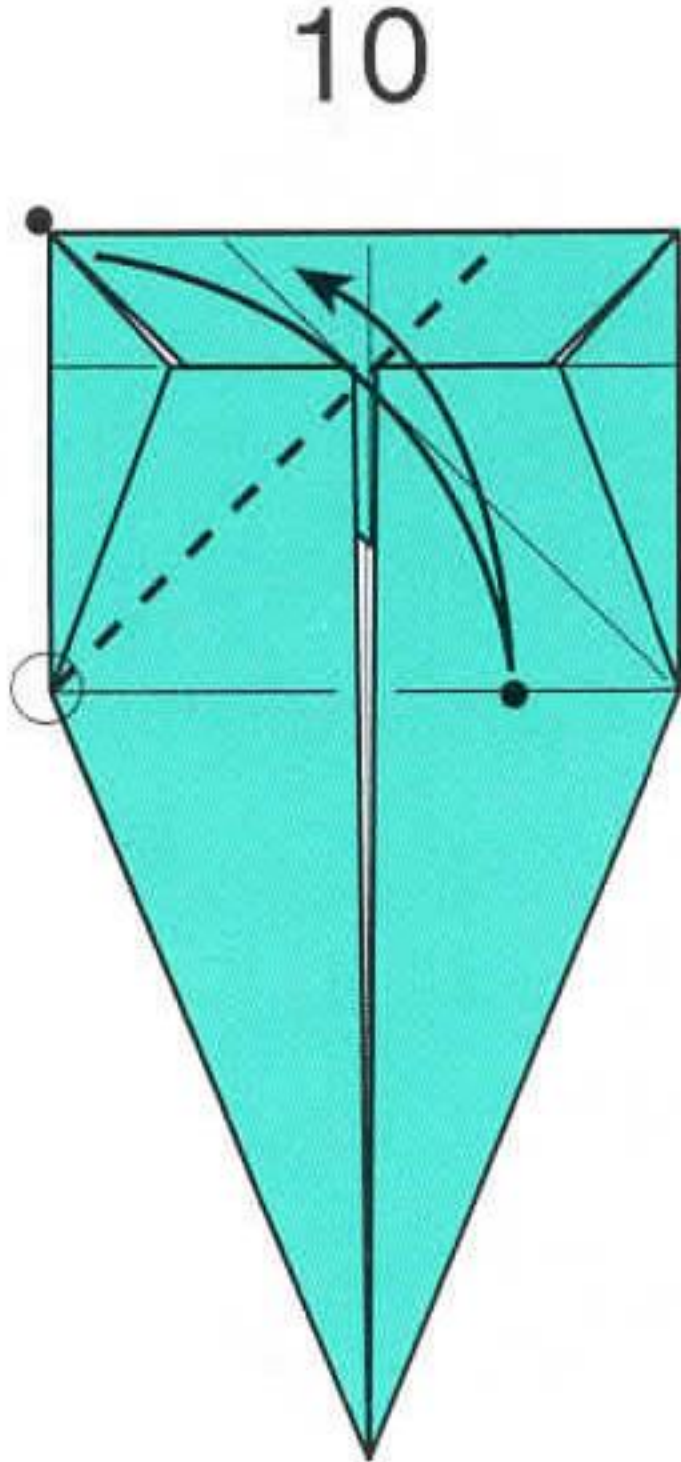
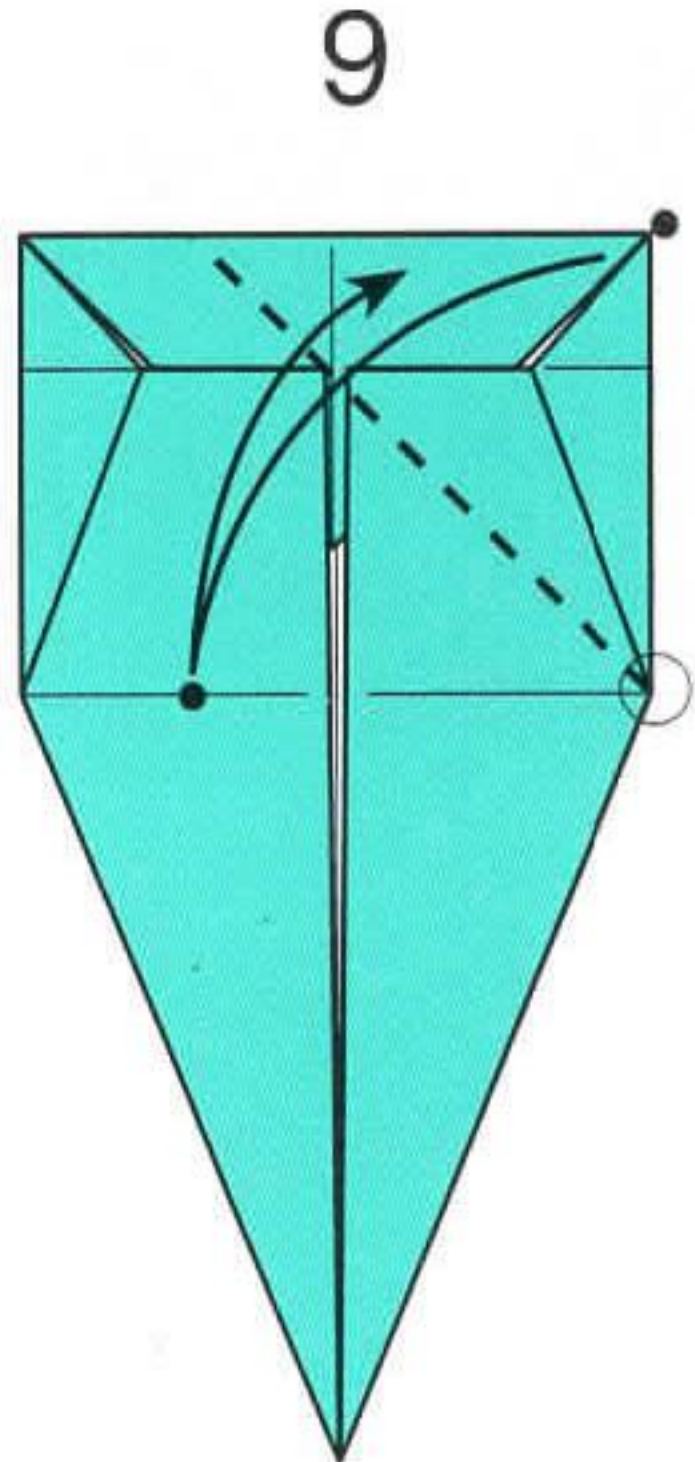
Tuck the tip under the layers.

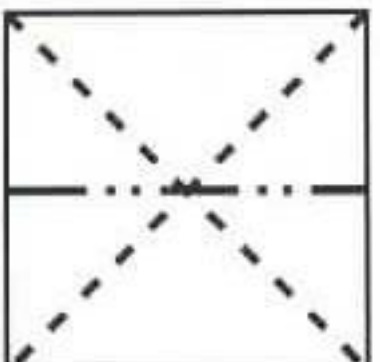


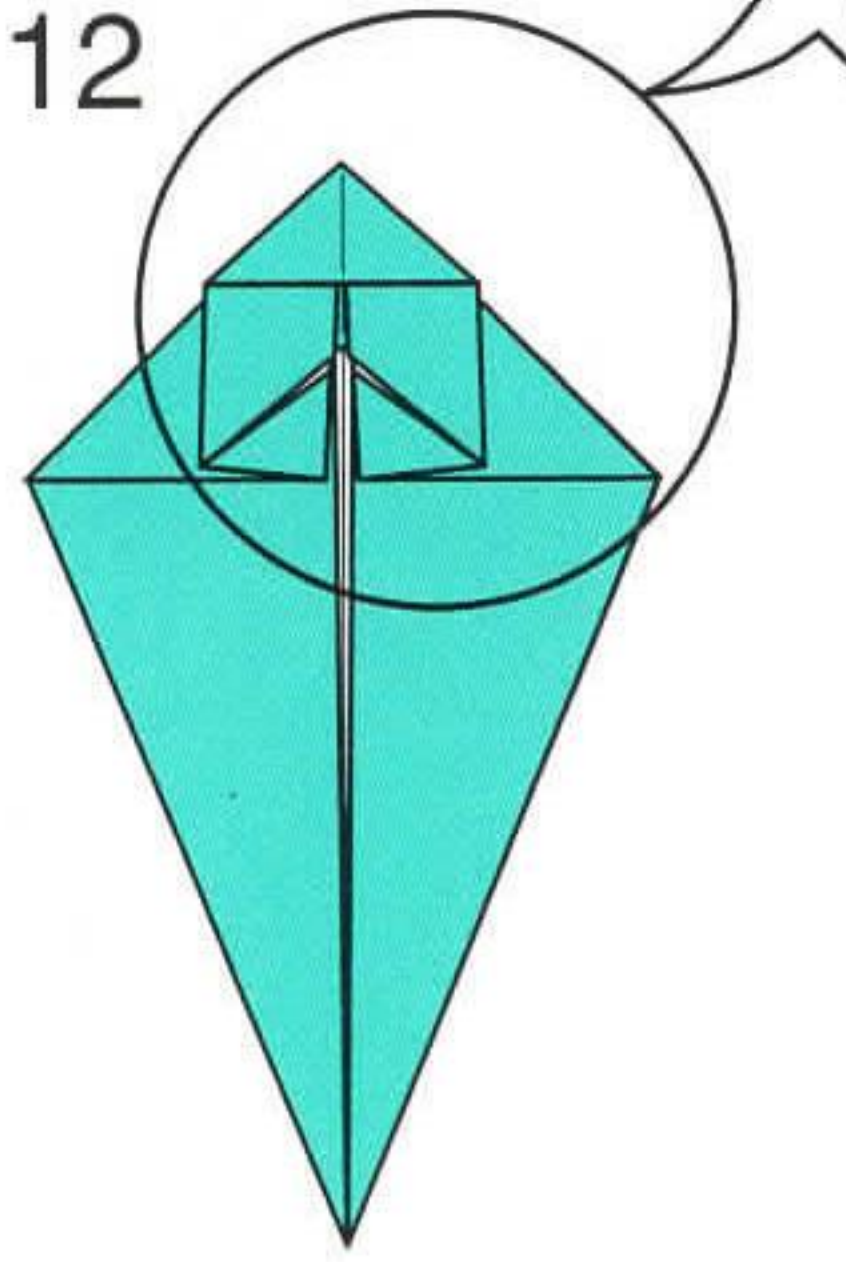
Fold along the edges.

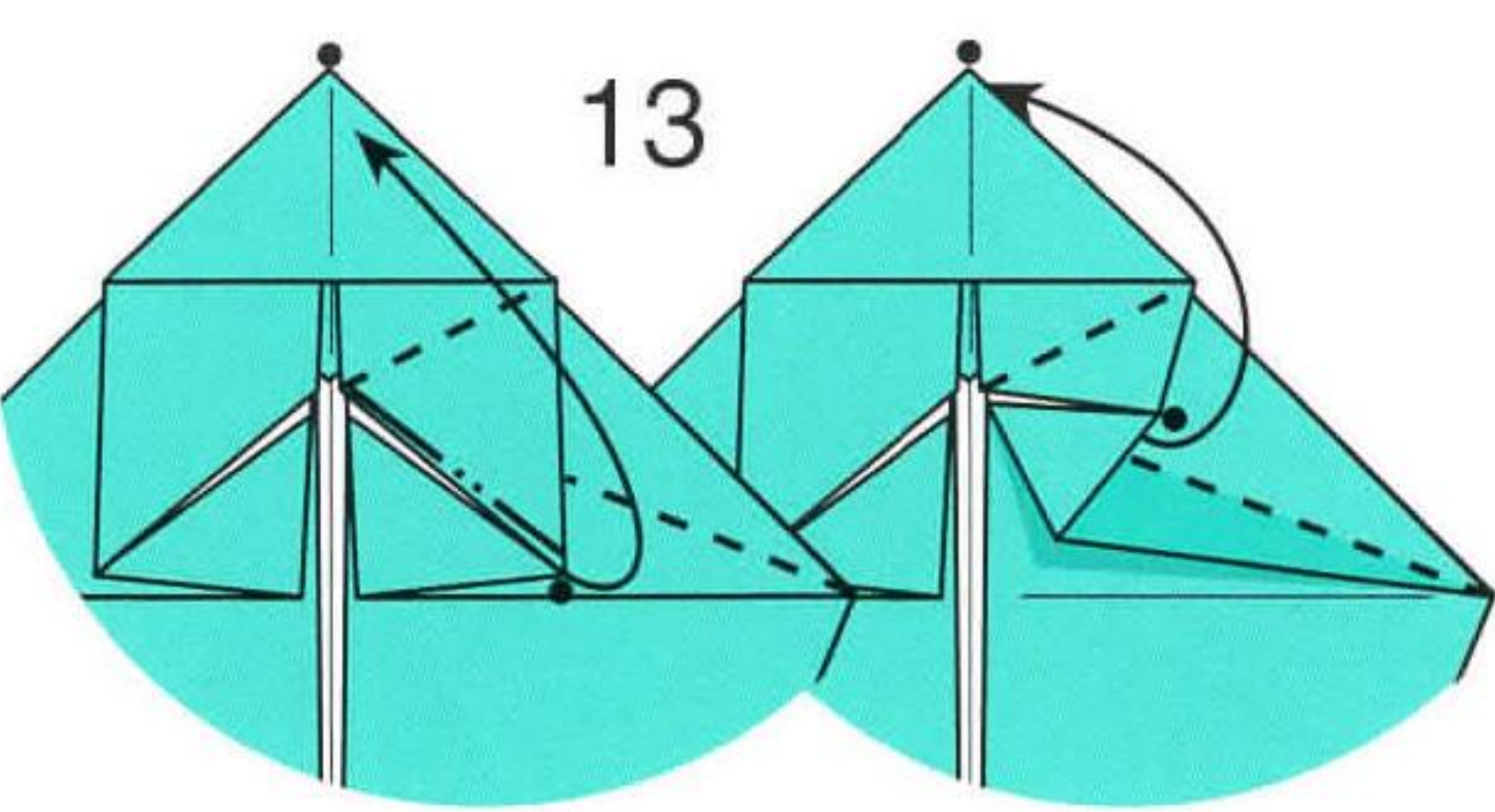


Unfold.

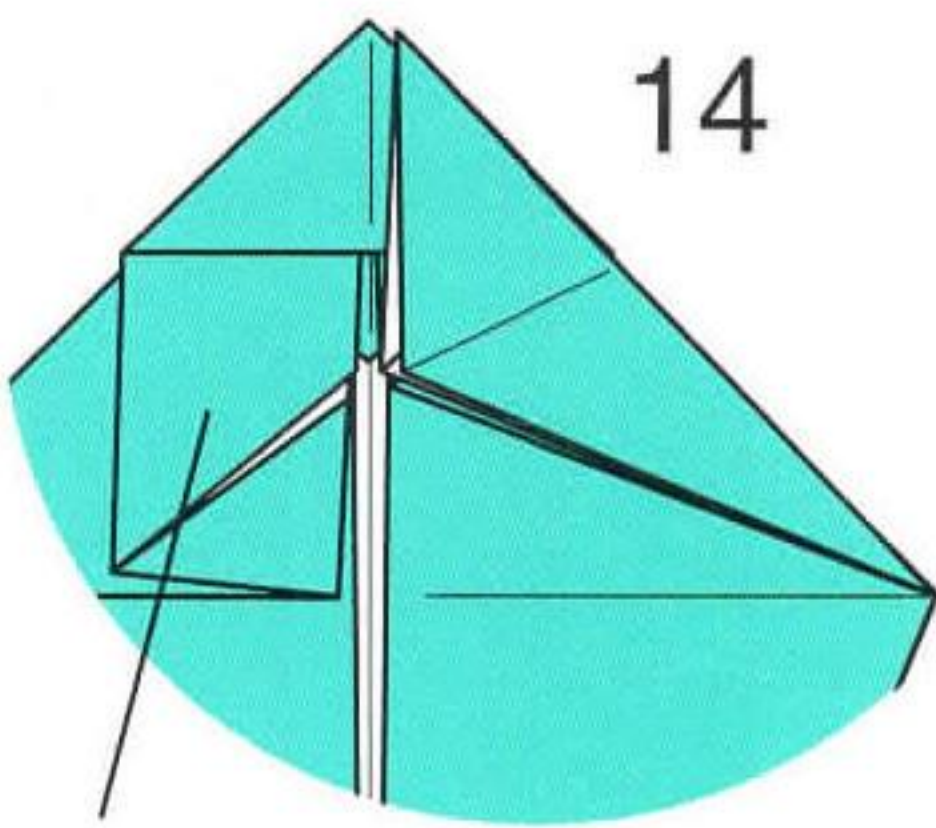



In steps 11-12, you fold like a **Water-bomb base**, which is illustrated on the left. The Water-bomb base is a halfway shape of traditional Water-bomb shown on the right.

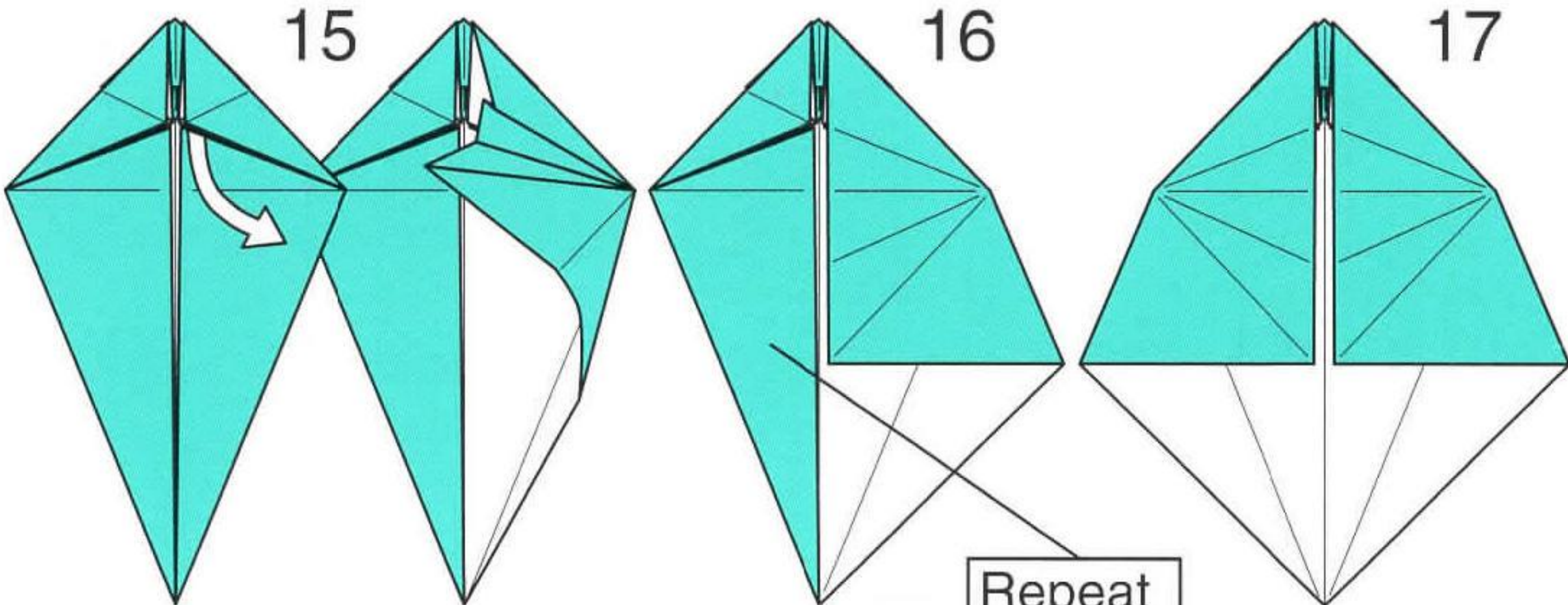




Step 13 is a kind of **rabbit ear fold**, though not a typical one. You make three new creases (two valley folds and one mountain fold) at once to make a triangular flap. Refer to the next model Squirrel for a typical swivel fold.



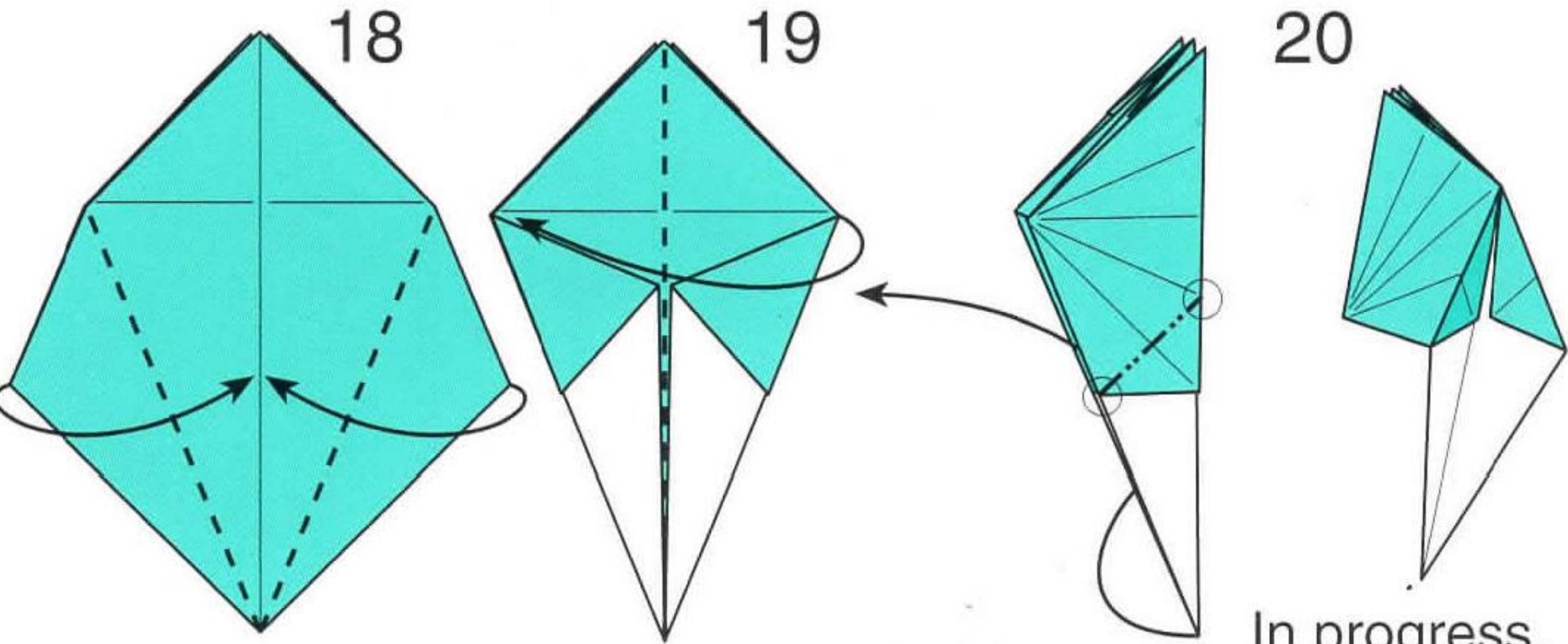
A white thick arrow as in step 15 indicates **to pull out (an inner point etc.)**. In this case, you may have to slightly unfold some creases because some layers are interlocked. This arrow sometimes indicates just to pull.



Pull out and squash.

Repeat step 15.

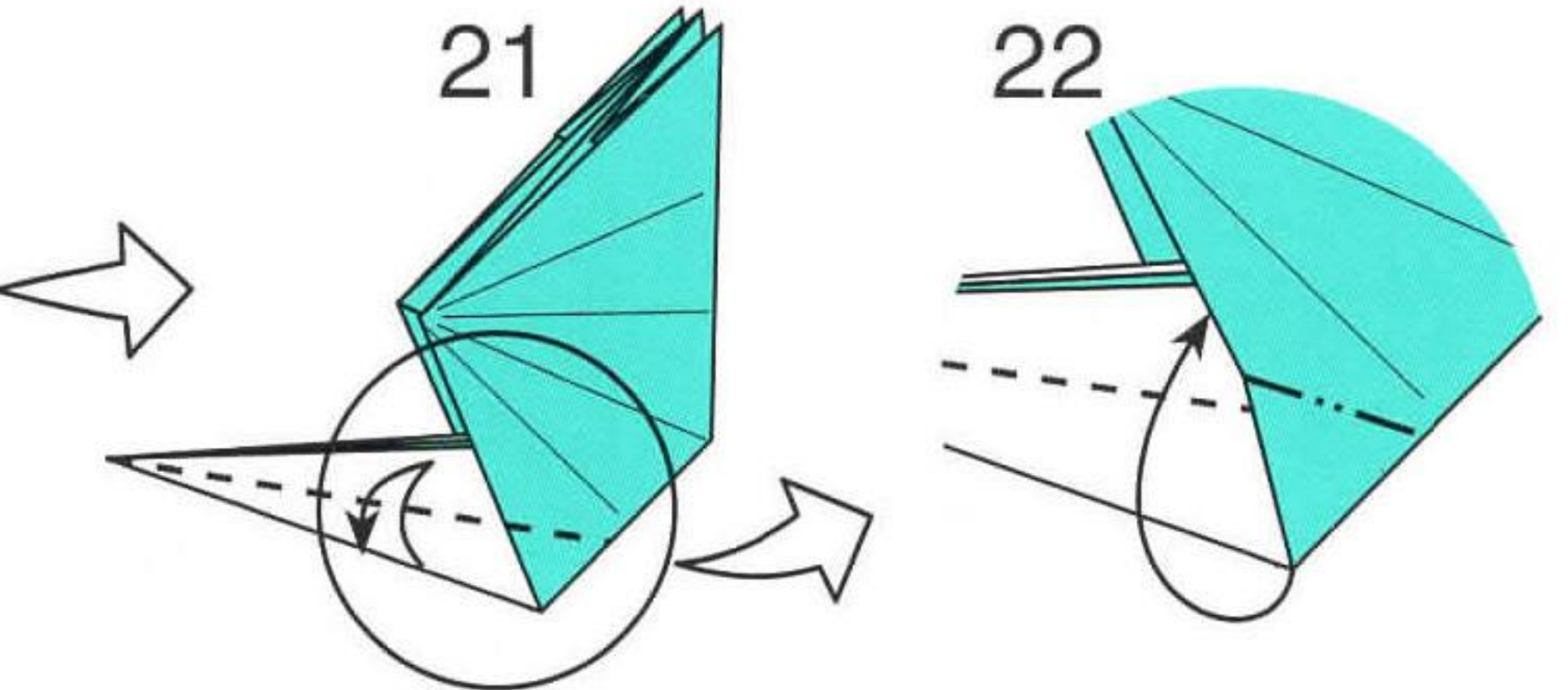
An arrow in form of a loop indicates **to turn over**. It does not change orientation.



Inside reverse-fold

In progress. Bottom-side view of step 20

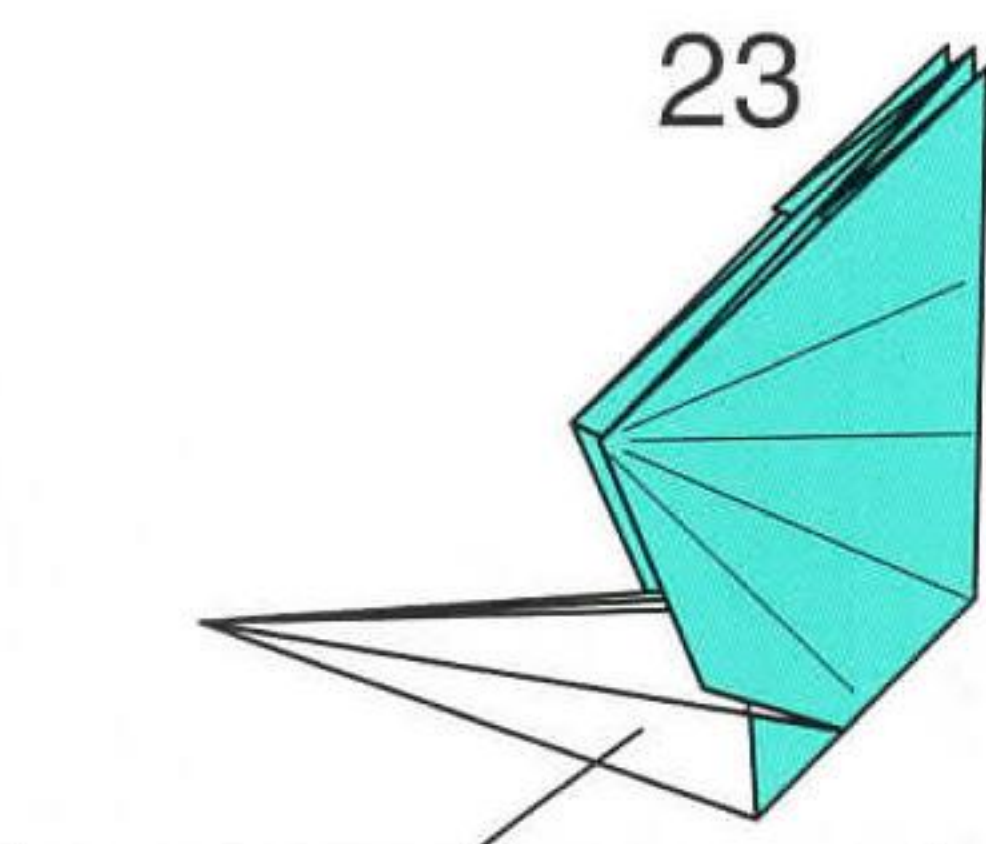
Step 20 is called an **inside reverse fold**, where you reverse the central mountain crease into valley. You can first valley-fold to make a preparatory crease as shown on the left. In this case, fold the loose raw corners at the same time.



Make a preparatory crease.

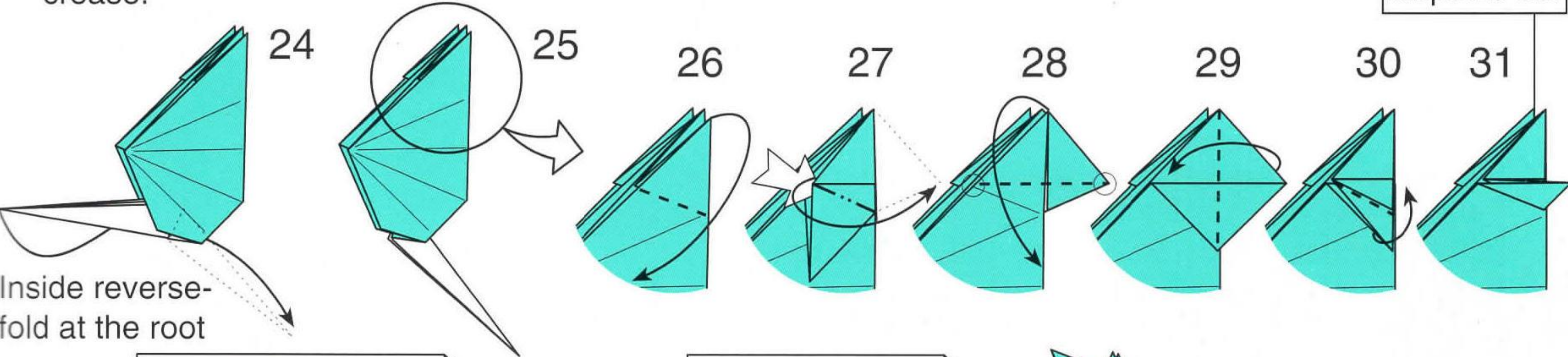
Inside reverse-fold

Step 22 may look different from step 20, but it is still an example of inside reverse fold.



Repeat steps 21-22.

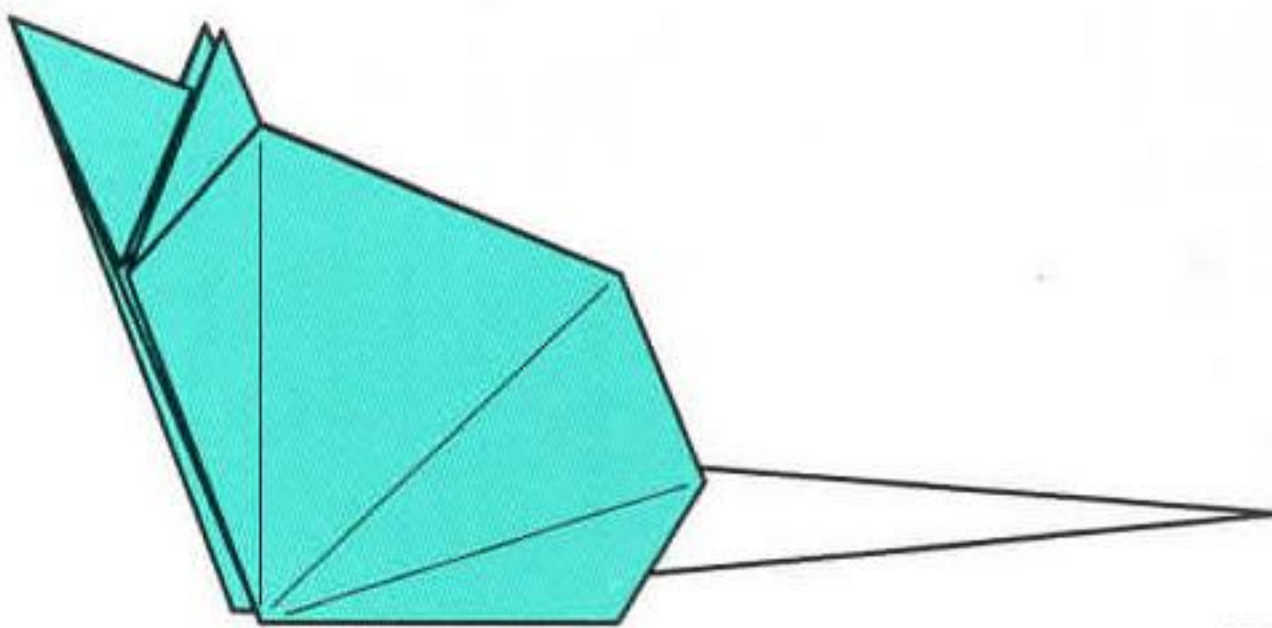
Repeat steps 26-30.



Inside reverse-fold at the root

A thin dotted line indicates an **imaginary line**, which can show a shape to-be or a hidden line.

A white arrow as in step 27 indicates **to open a pocket and squash**.

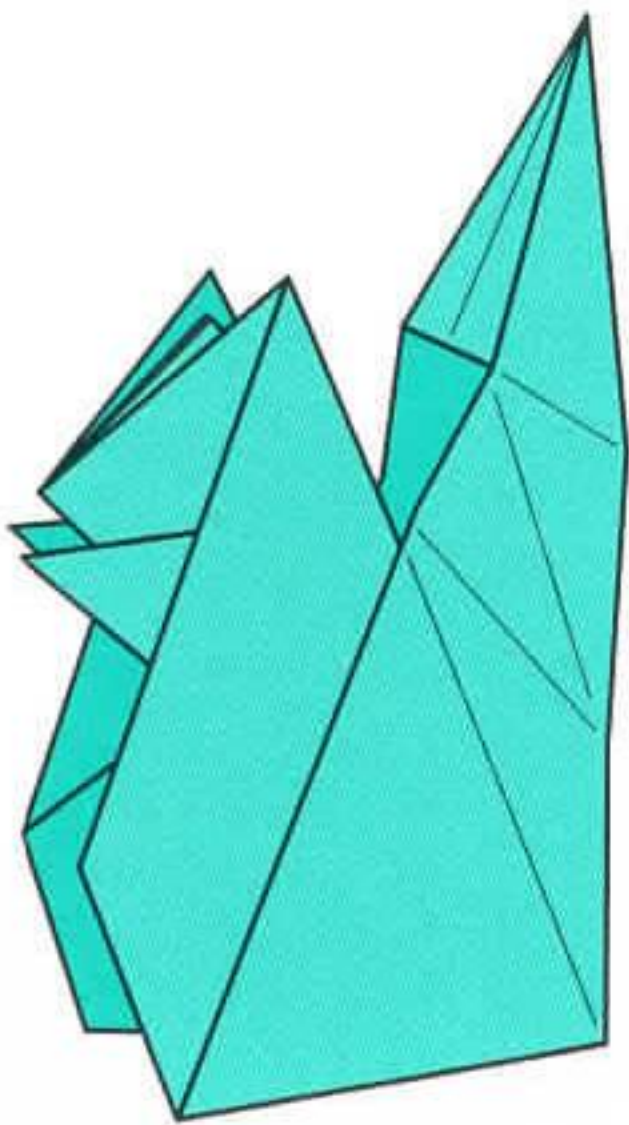


Finished.

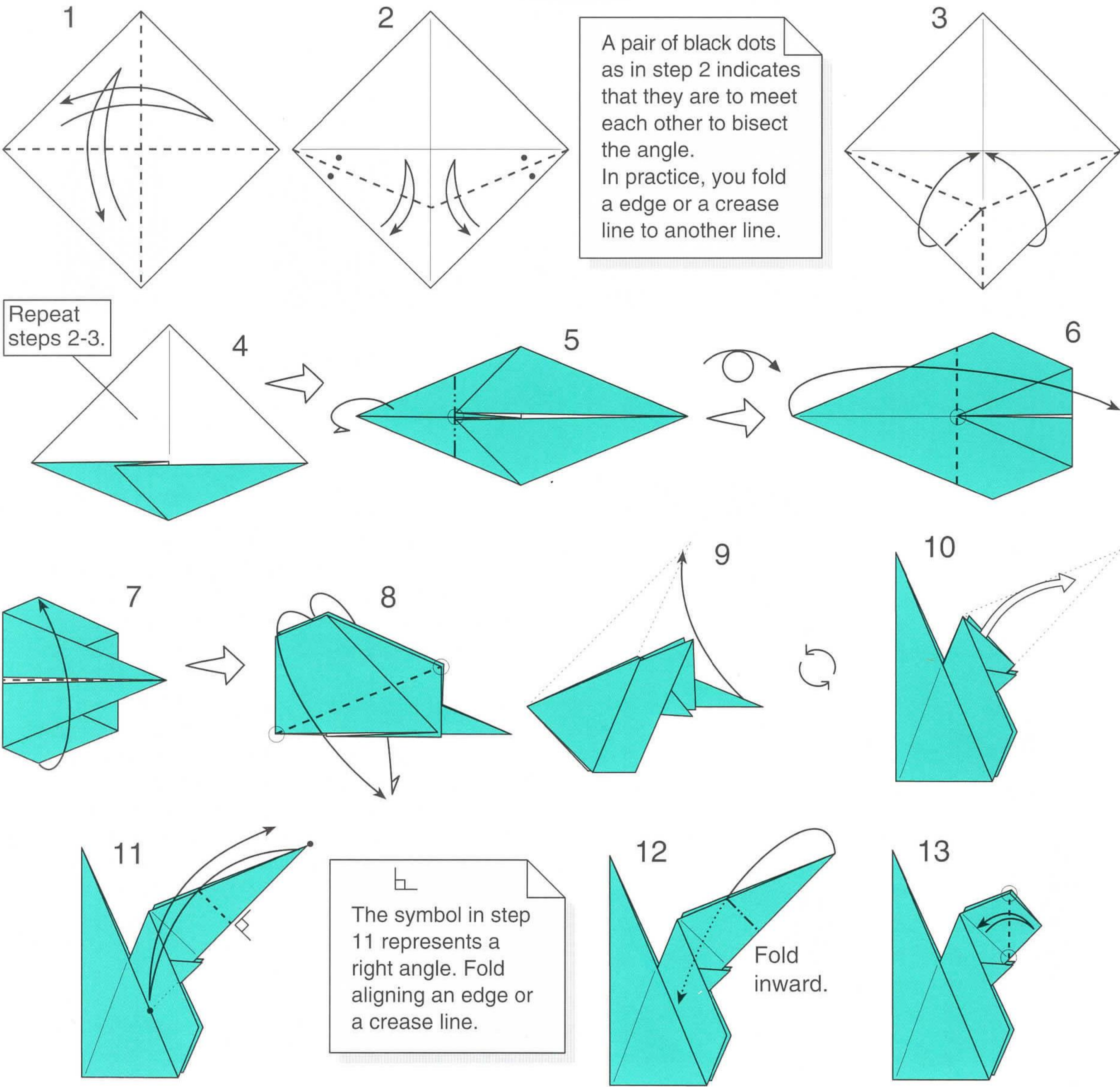
Squirrel

Theme: Base

Fold using 6" (15 cm) origami paper.

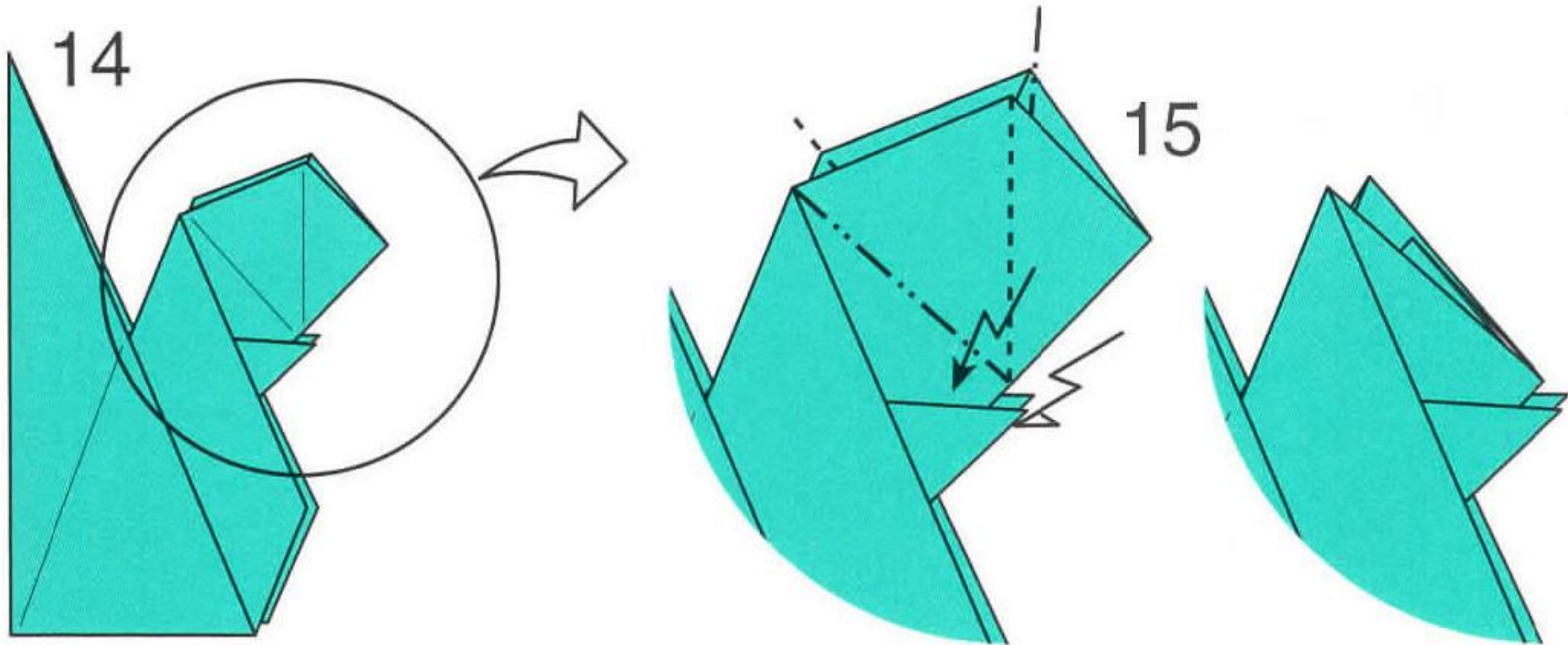


Step 5 is called a **Fish base**. And steps 3-4 show a typical **rabbit ear fold**. You can see that a Fish base consists of two rabbit ear folds.

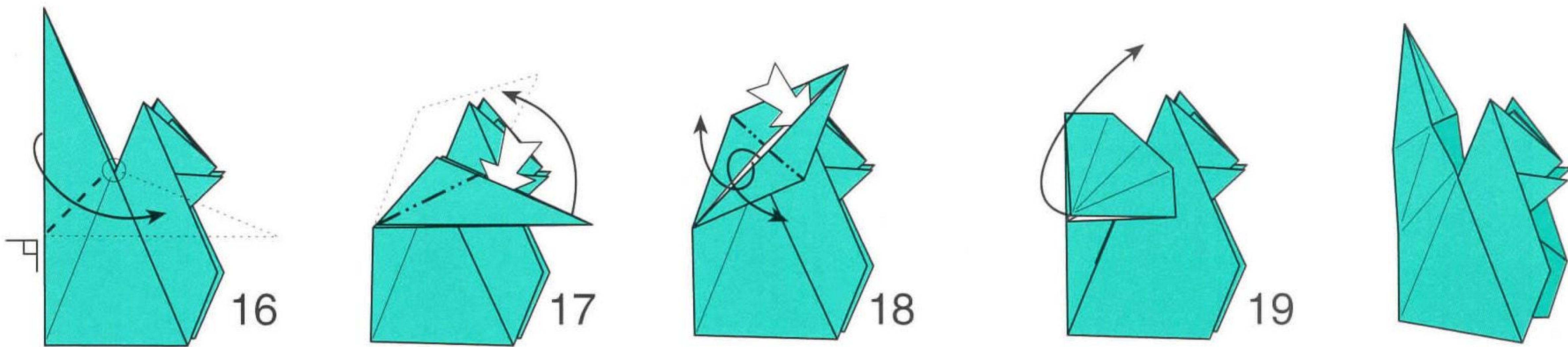


Tips: How to fold neatly (Part 1)

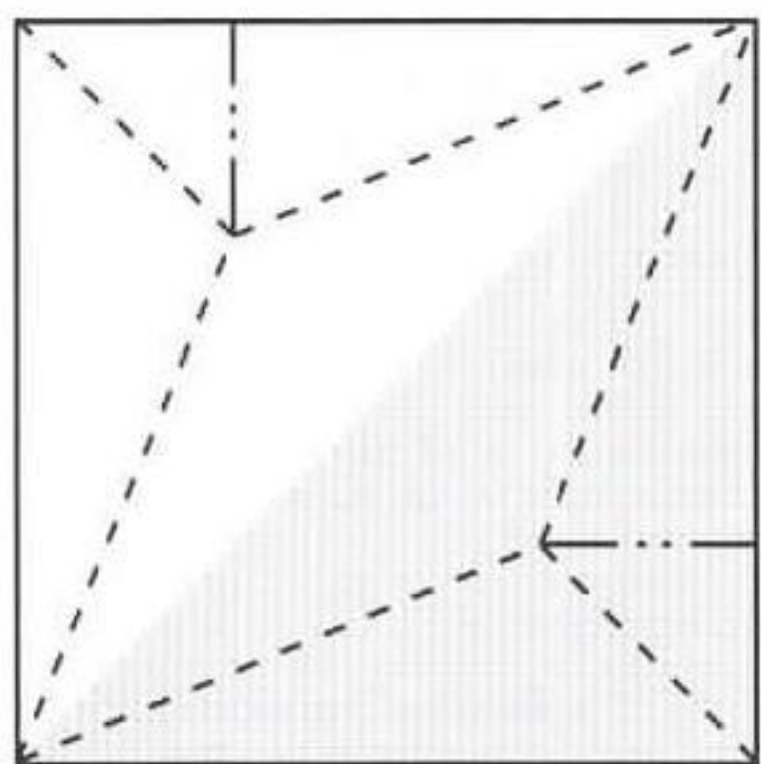
To fold origami models (at least the models in this book), you should fold accurately and firmly as a general rule. In diagrams, we usually draw layers as though they are not aligned to emphasize overlap of them. But you must fold precisely according to landmarks, which are shown as black dots or white circles, and descriptions. Moreover, unless otherwise stated, it is better to crease sharply, even using your nails, to make a good-looking model.



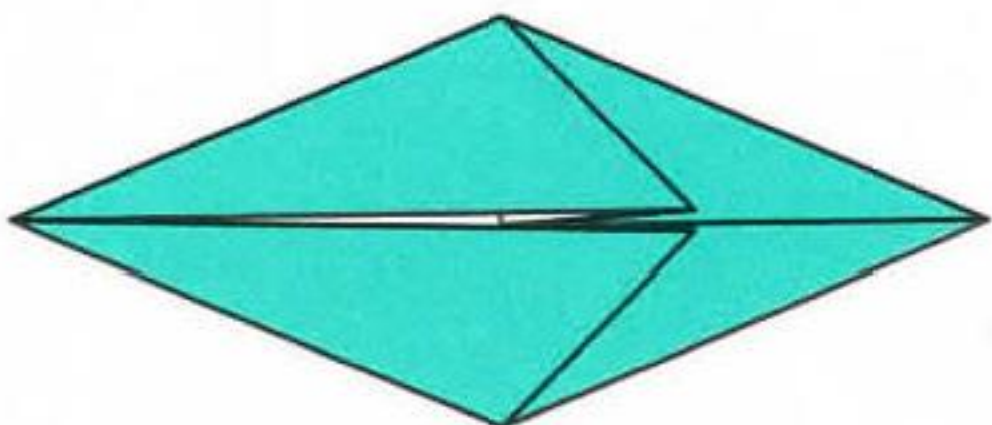
A zigzag arrow indicates **to pleat** or **to crimp**. In this case, you make angled pleats symmetrically on both layers to push the layers inward. This is sometimes called an **inside crimp**.



Squash-fold. Squash-fold. Open the tail to make it 3D. Open the body slightly to finish.



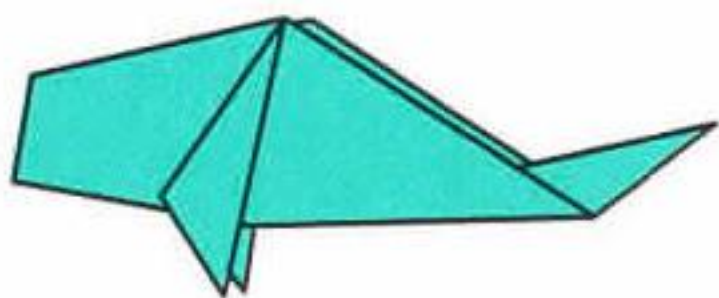
The crease pattern of a Fish base.



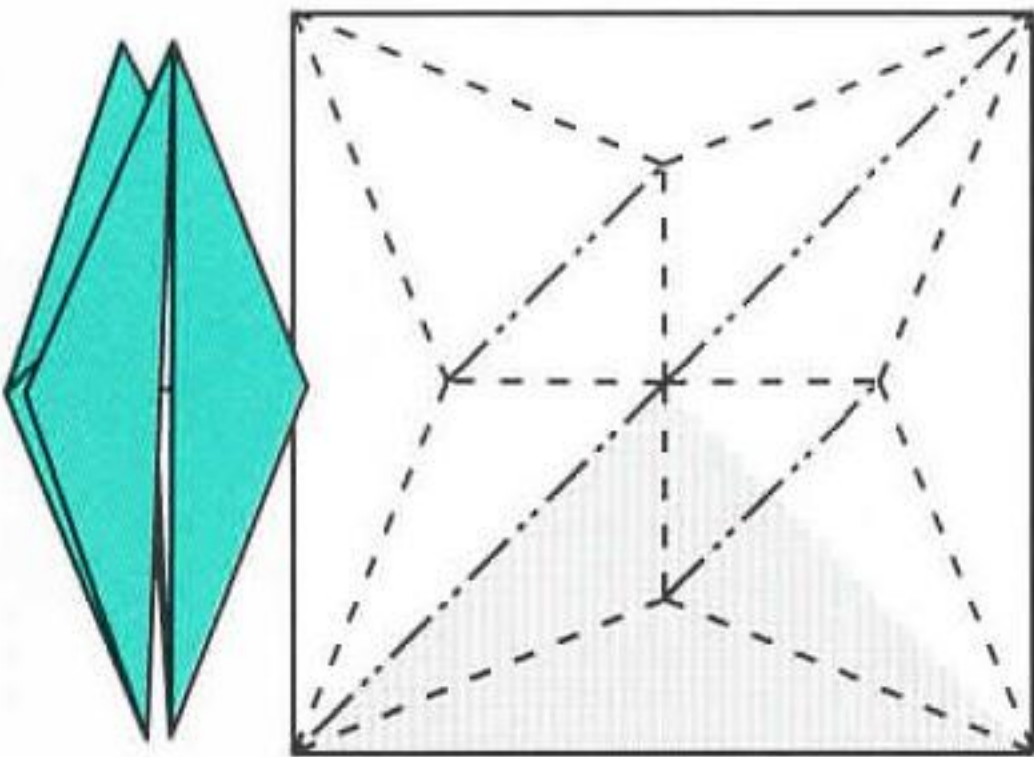
A Fish base



The tree structure of the Fish base



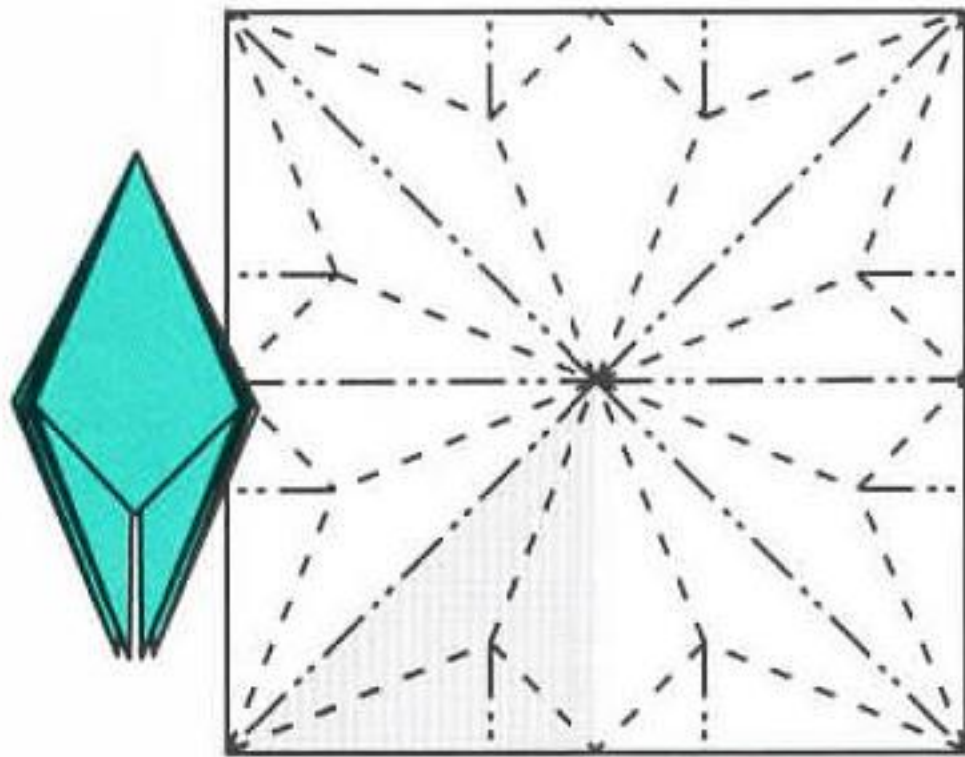
Fish (a.k.a. Carp)



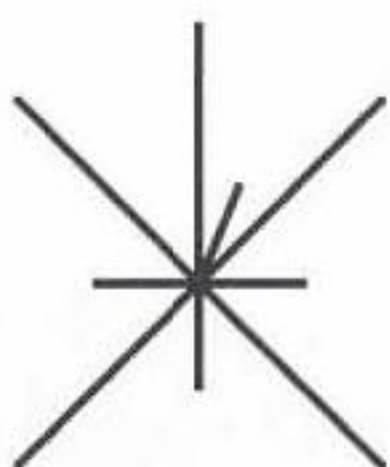
A Bird base and its crease pattern



The tree structure of the Bird base



A Frog base (a.k.a. Iris base) and its crease pattern



The tree structure of the Frog base

Base

The name Fish base comes from traditional *Fish* (also known as *Carp*). This base is characterized by two long flaps and two short ones. In *Squirrel*, I have used two short flaps for the forelegs, one long flap for the tail, and the other for the body, and omitted the hind legs. Such flap-based design is one of the basic methods of origami design.

Bases have played an important role as starting point for design of various models. For example, the *Squirrel* starts from a Fish base. However, in recent years of creative origami, similar to inside reverse folds, it may be more accurate to regard bases as just another folding technique. I have already explained a step in *Mouse* as “fold like a Water-bomb base”, which suggests that a base is a sort of fold technique.

There are about 10 important types of bases, which are described in this page and other parts of this book. The most important of all is the Bird base, which is in the same class as the Fish base, as well as the Frog base (also known as the Iris base).

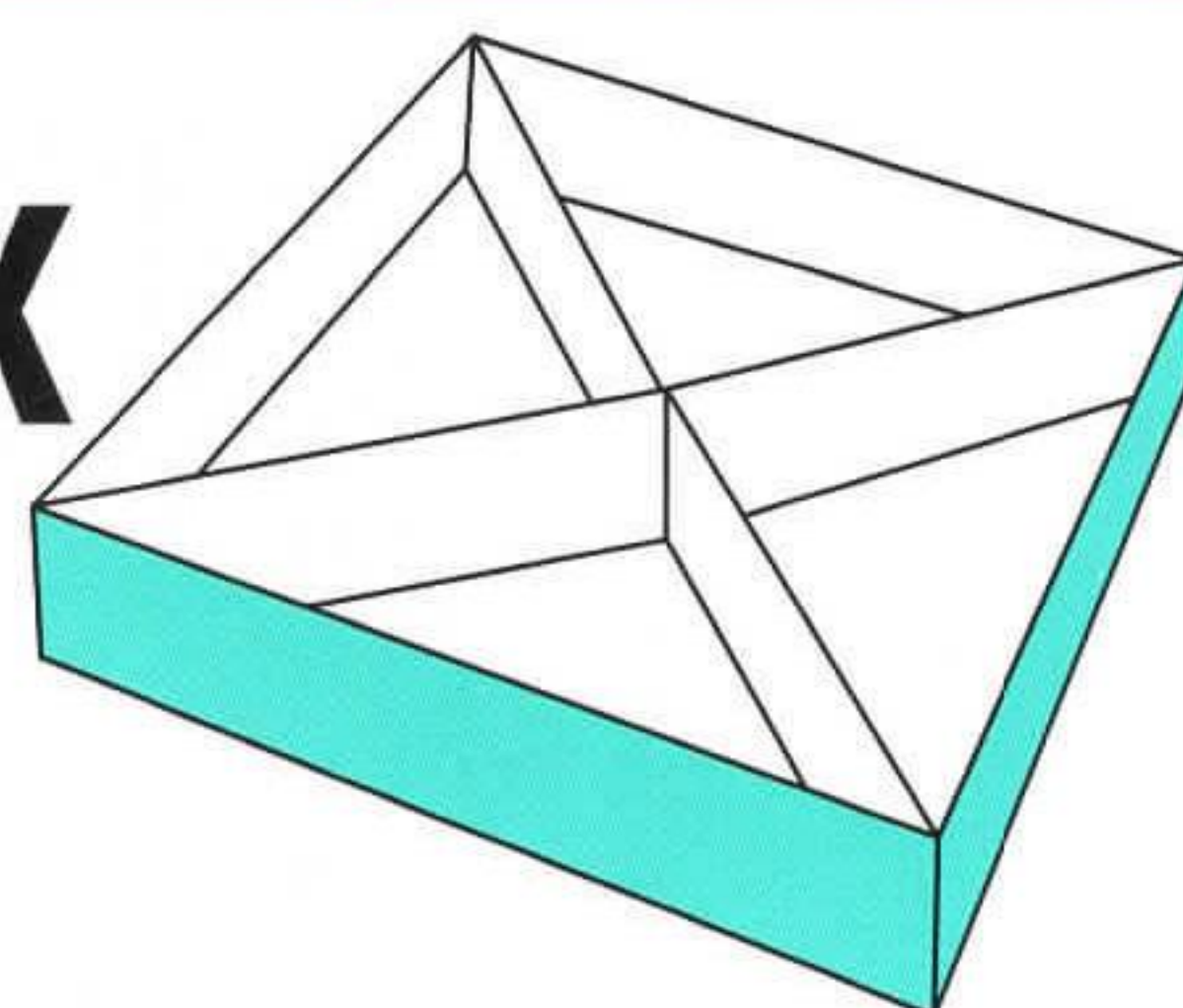
You will figure out the reason why I say they are in the same class if you look at the crease patterns, or the creases left on unfolded sheets, of the bases.

Look at the crease patterns carefully. If we cut a Fish base in half along its diagonal line, we have a unit. A Bird base consists of four units, and a Frog base eight. One can also say a Frog base is composed of four Fish bases.

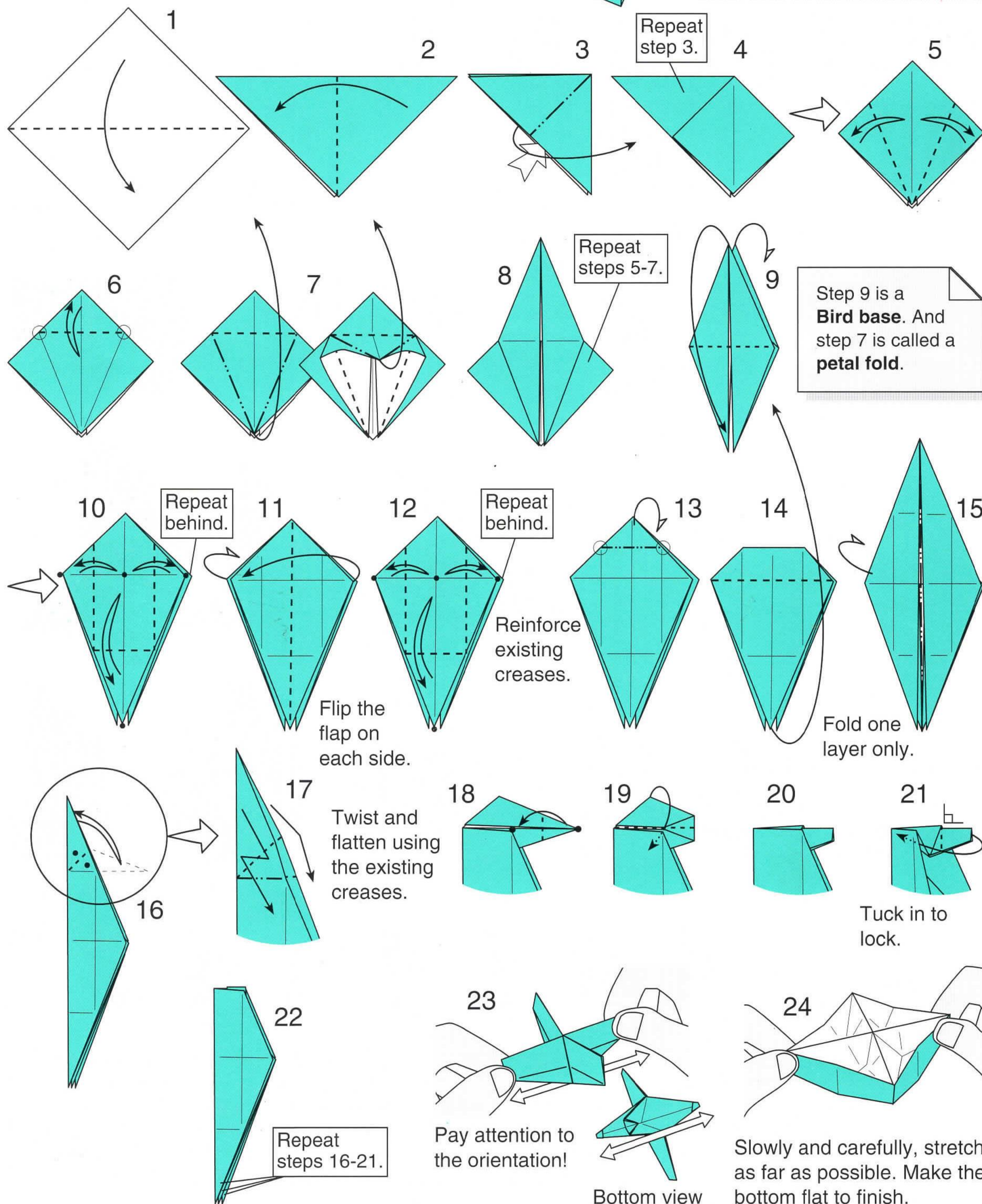
Partitioned Box

Theme: Bird base

Fold using 6" (15 cm) origami paper.

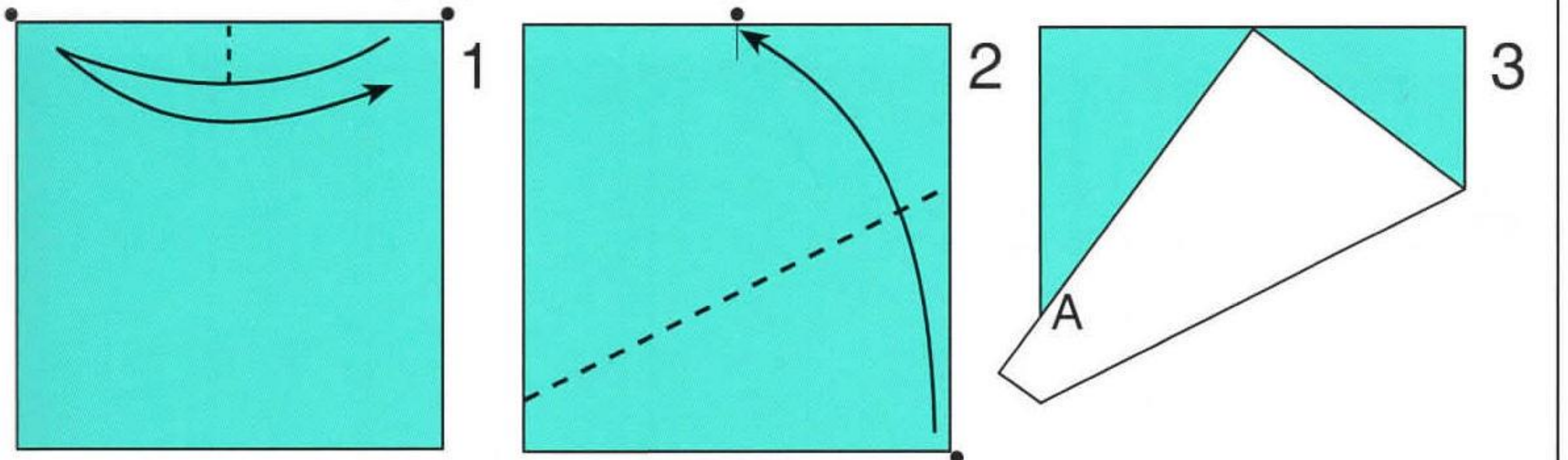


I made use of the symmetry of the Bird base to design this model. Pay attention to the orientation in the steps 13, 14, and 23. It will be also interesting to start with colored side up.



Conch

Theme: Trisection; Isosceles right triangle
Fold using 6" (15 cm) origami paper.

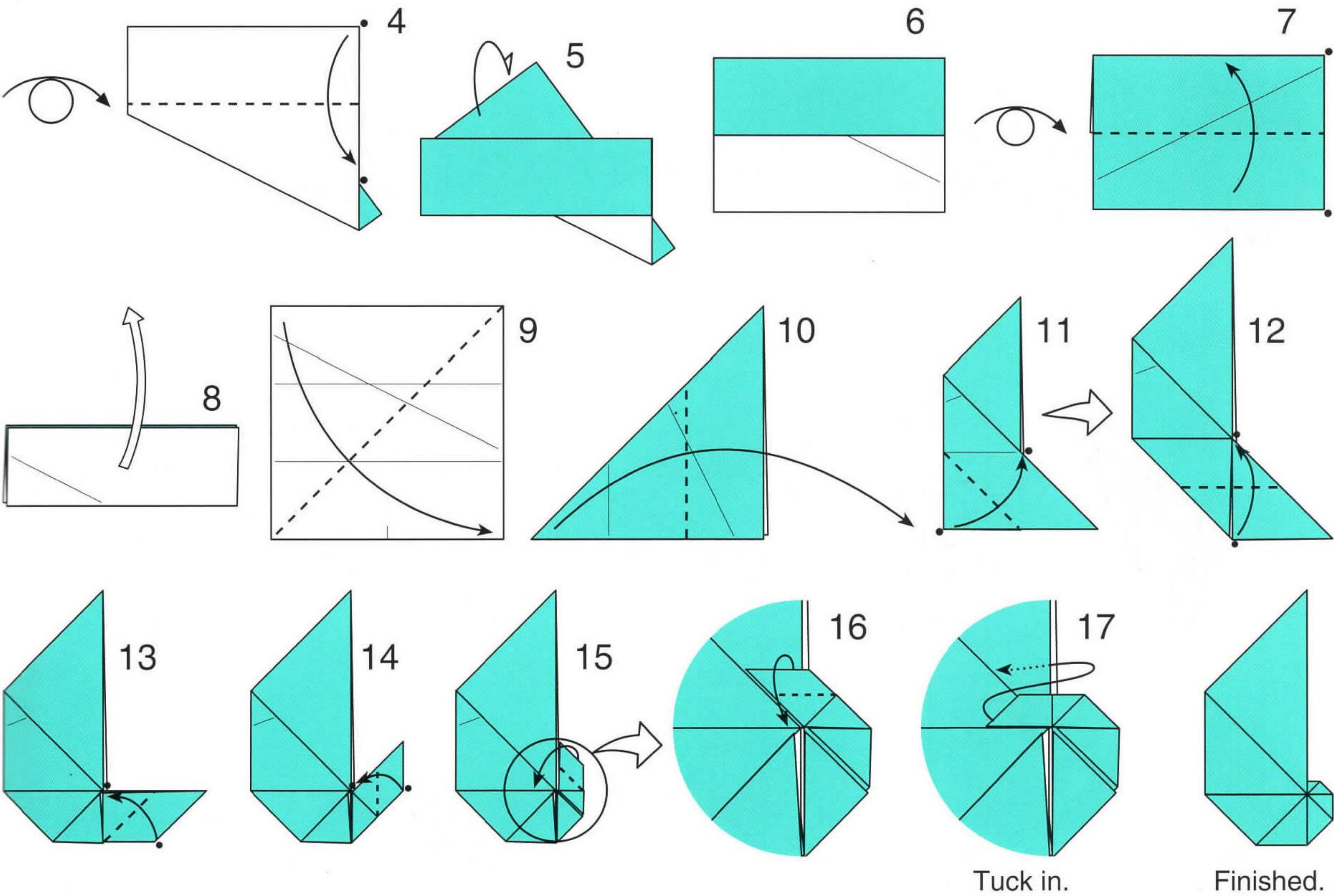
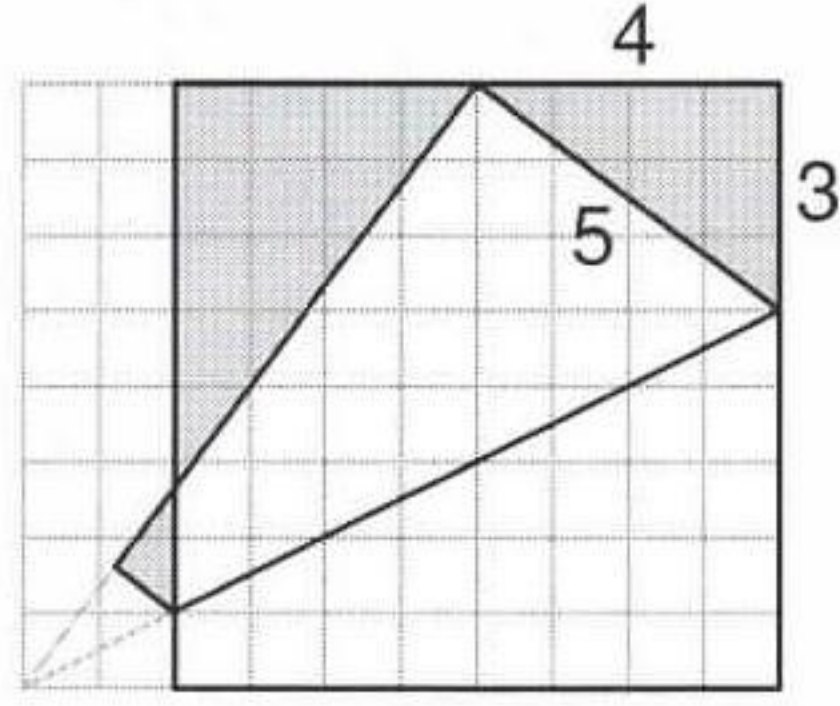


Pinch.

Trisection

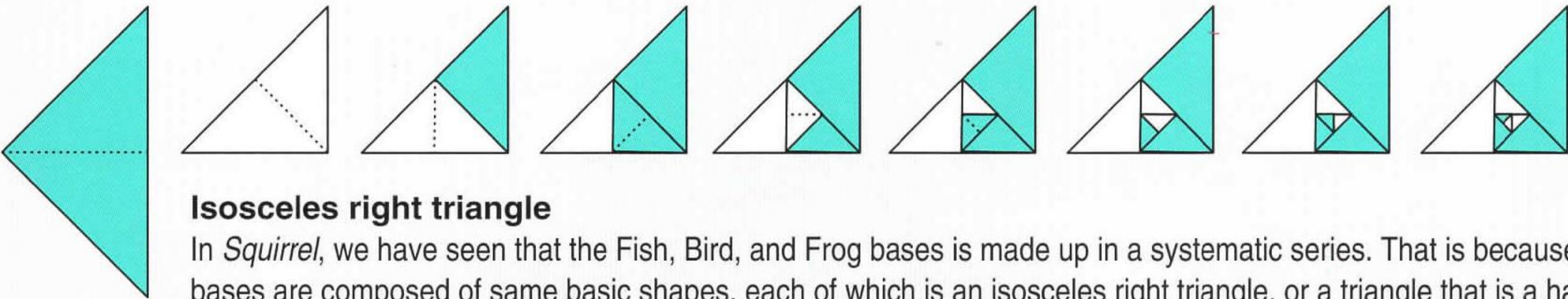
The first two steps 1-2 indicates the point that trisects the side of a square precisely, which is indicated as A. Kazuo Haga formulated this method of trisection, hence it is called Haga theorem.

The right diagram shows the key to prove the theorem. The ratio of three sides on each gray triangle is 3 : 4 : 5.



Tuck in.

Finished.



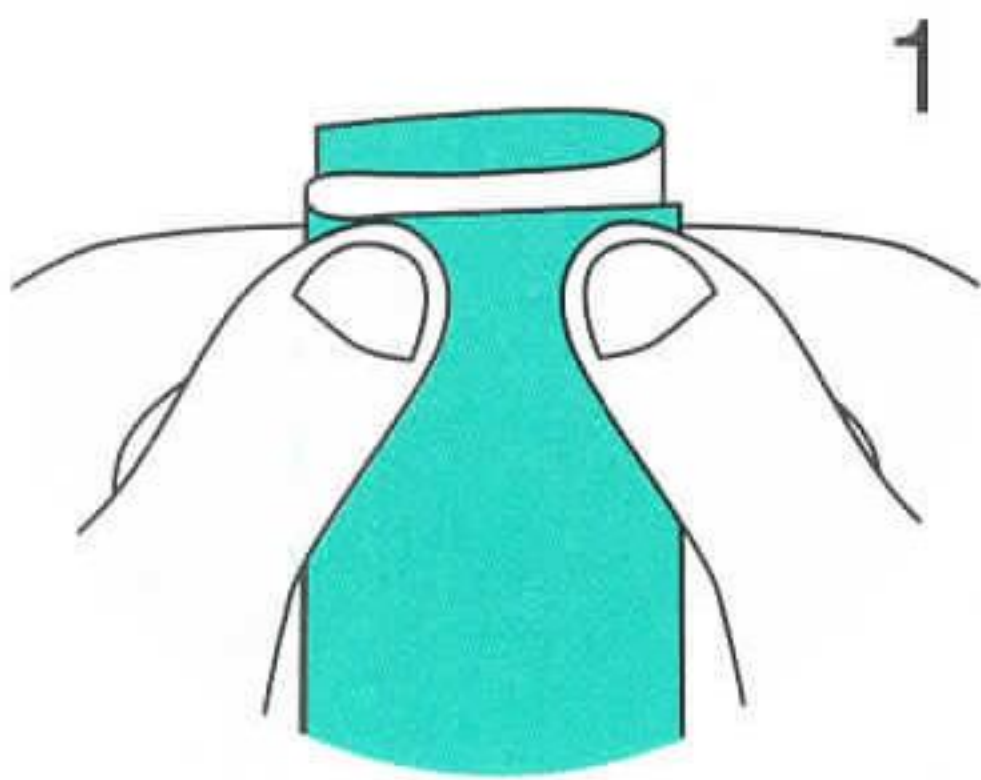
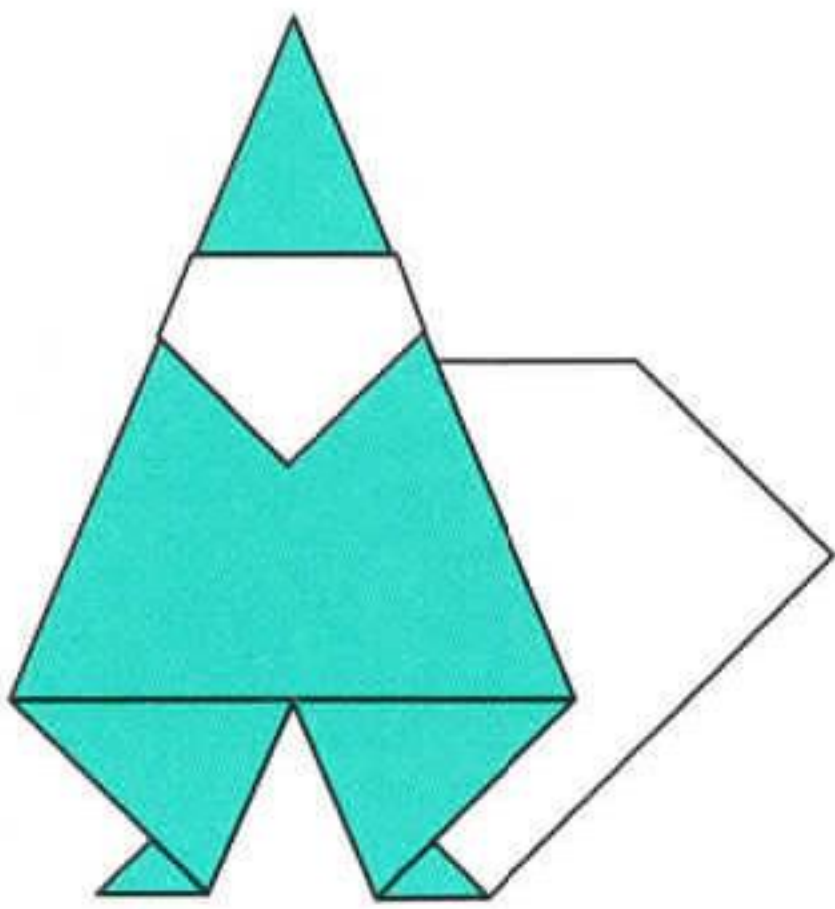
Isosceles right triangle

In *Squirrel*, we have seen that the Fish, Bird, and Frog bases is made up in a systematic series. That is because the bases are composed of same basic shapes, each of which is an isosceles right triangle, or a triangle that is a half of a square. When you divide an isosceles right triangle in two equal parts, each will be similar in proportion to the original figure. Besides the triangles, only parallelograms with ratio $1 : \sqrt{2}$ share this property. *Conch* starts with a trisection, and makes use of the property that when divided into half, it generates two parts, each similar in proportion to the original shape. The picture above also exploit this property, and it graphically represents an equation $1/2 + 1/4 + 1/8 + \dots = 1$.

Santa Claus

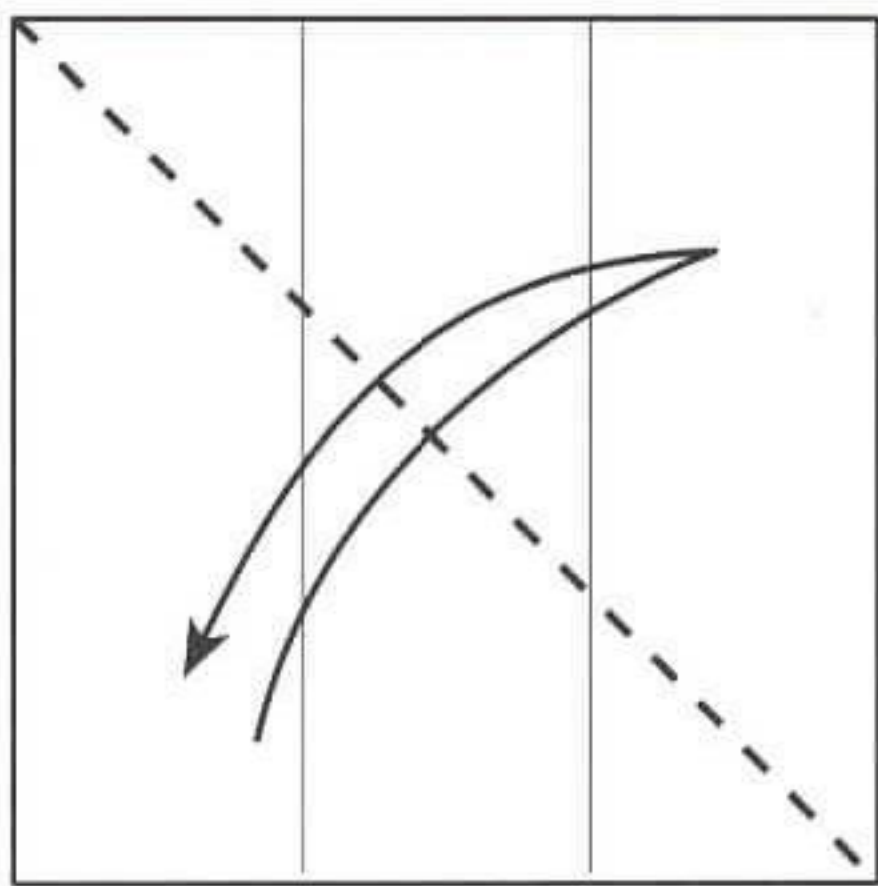
Theme: Inside-out

Fold using 6" (15 cm) origami paper.

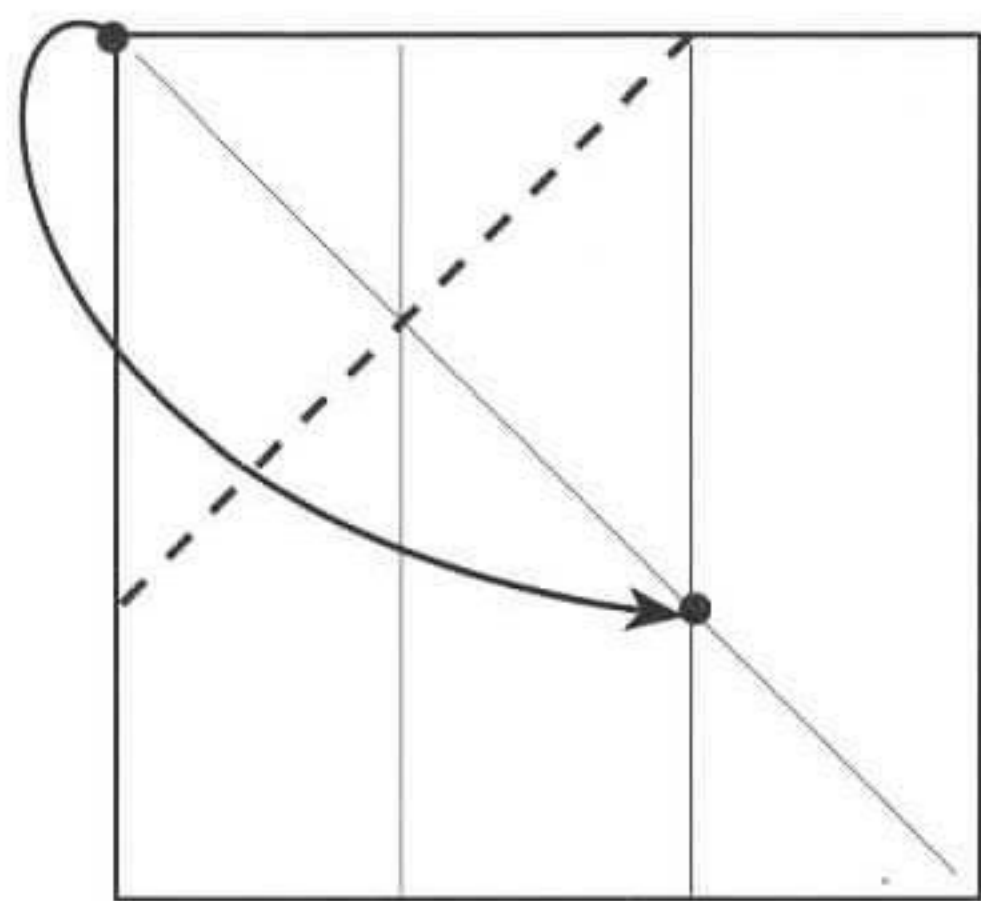


1

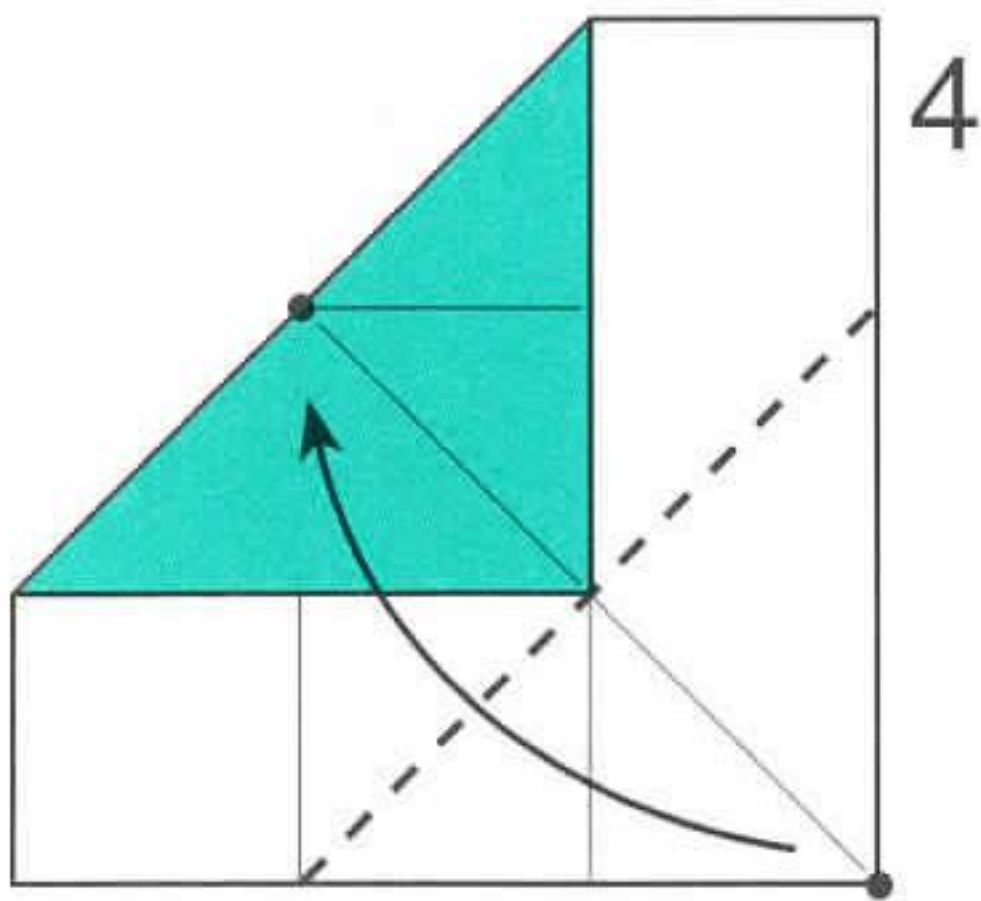
You can trisect a side by estimation as in the step 1. This is the best way if you get used to, as you will avoid the diagonal crease line.



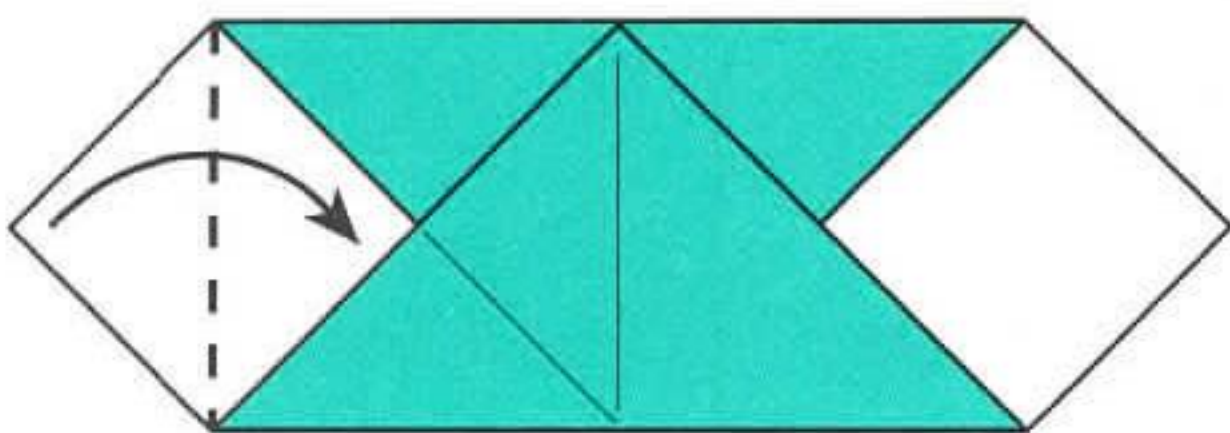
2



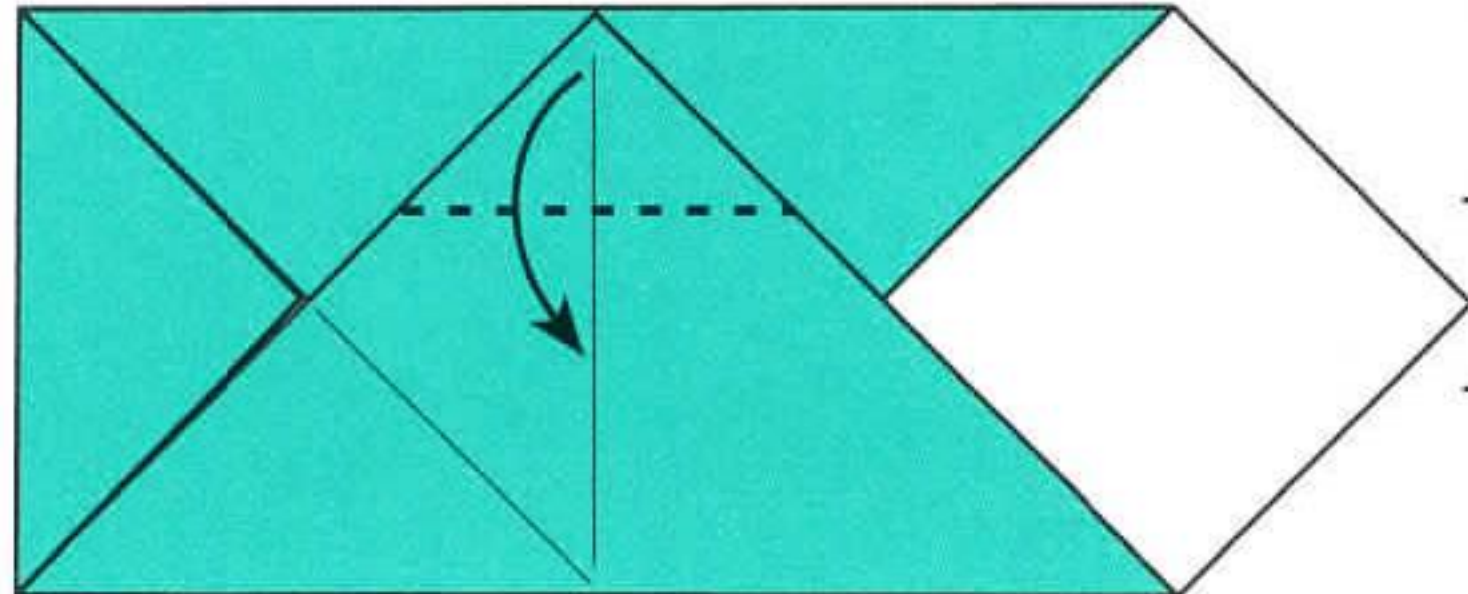
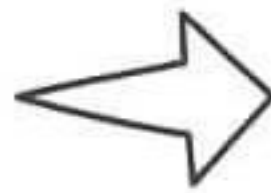
3



4

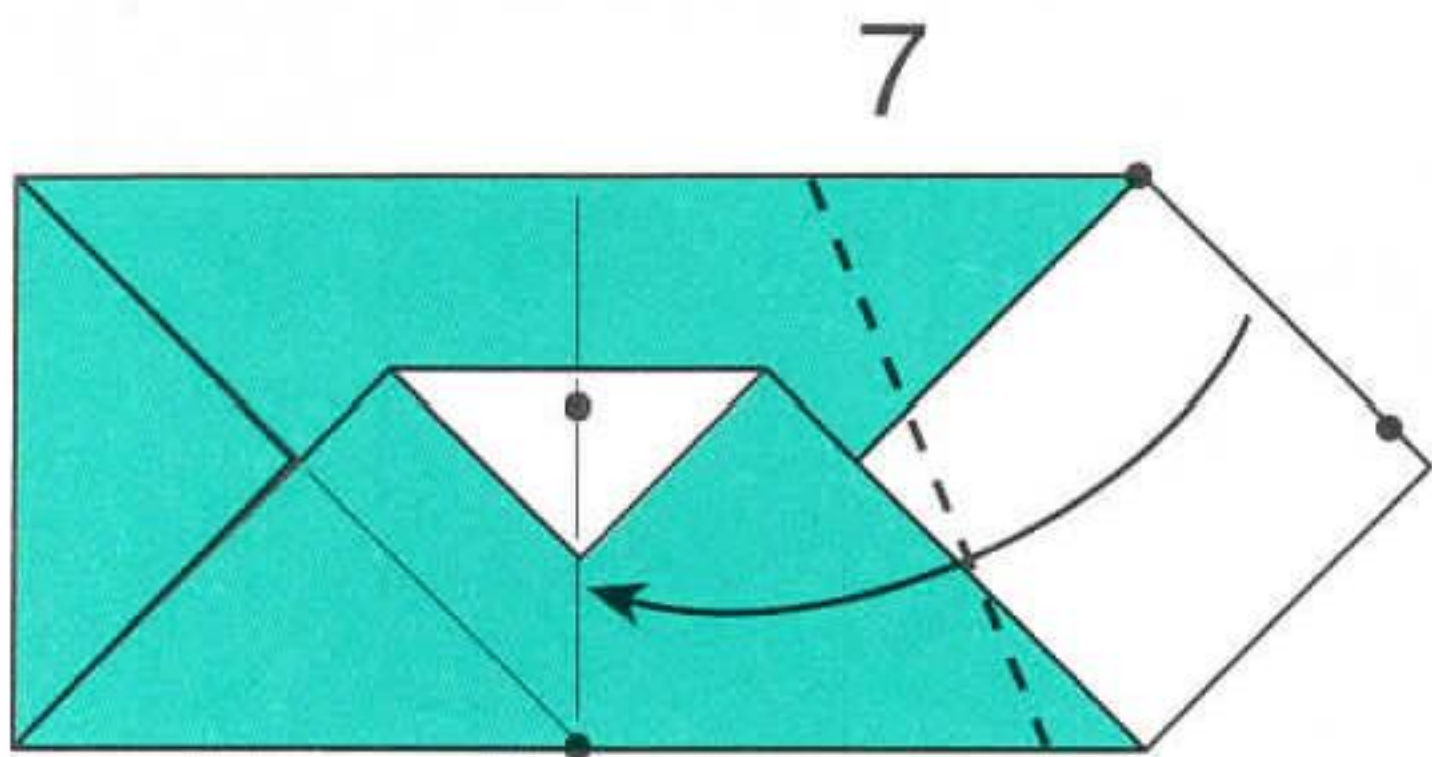


5



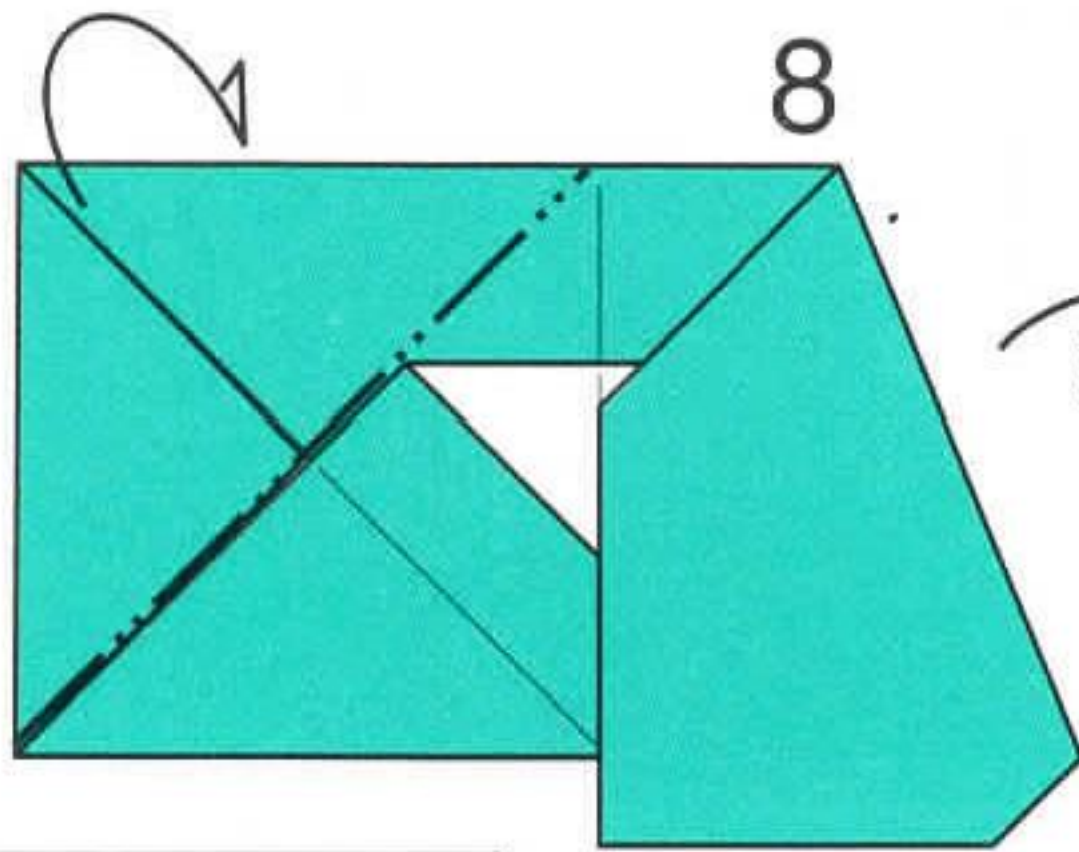
6

Approximately 1/3

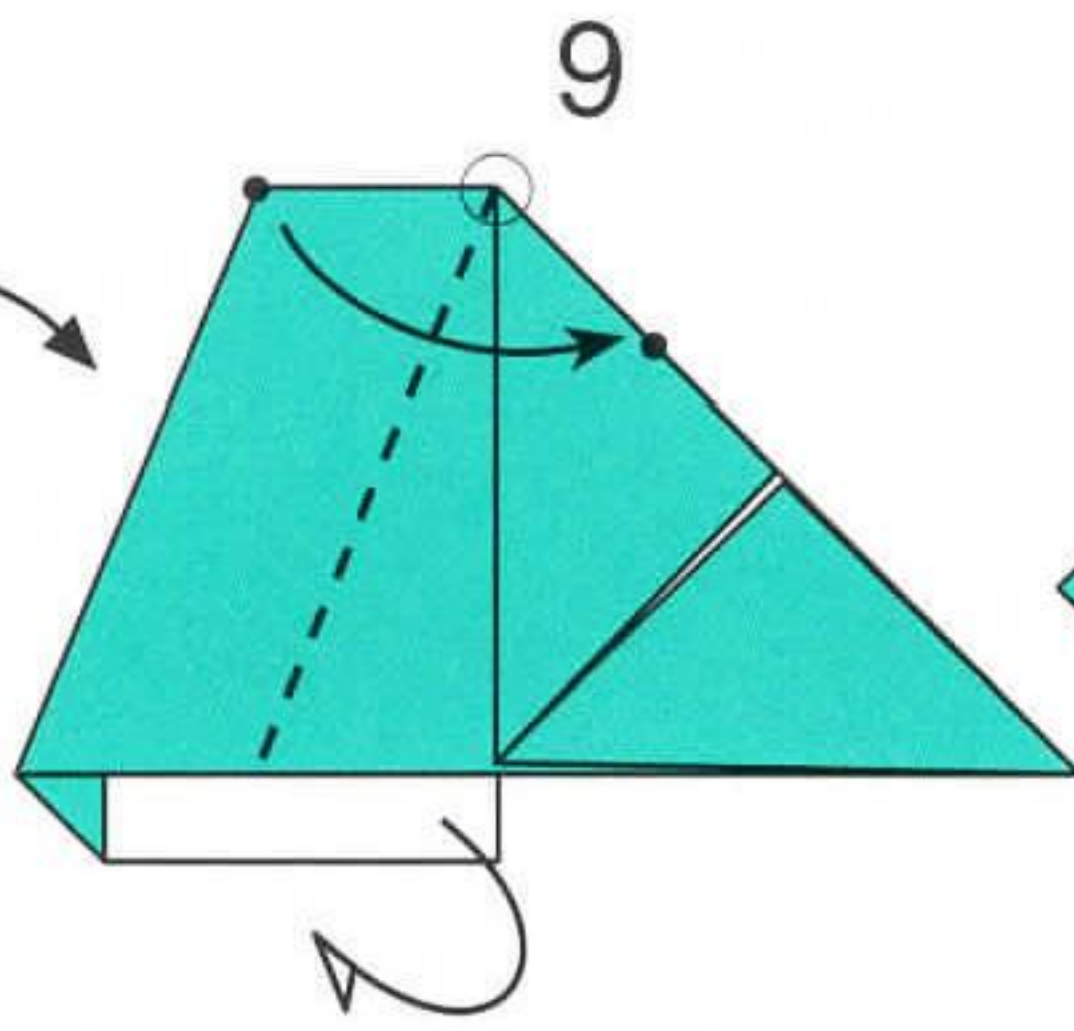
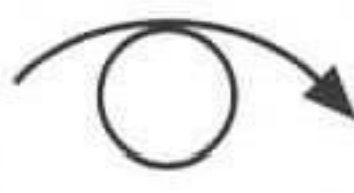


7

Fold the edge to the center line.

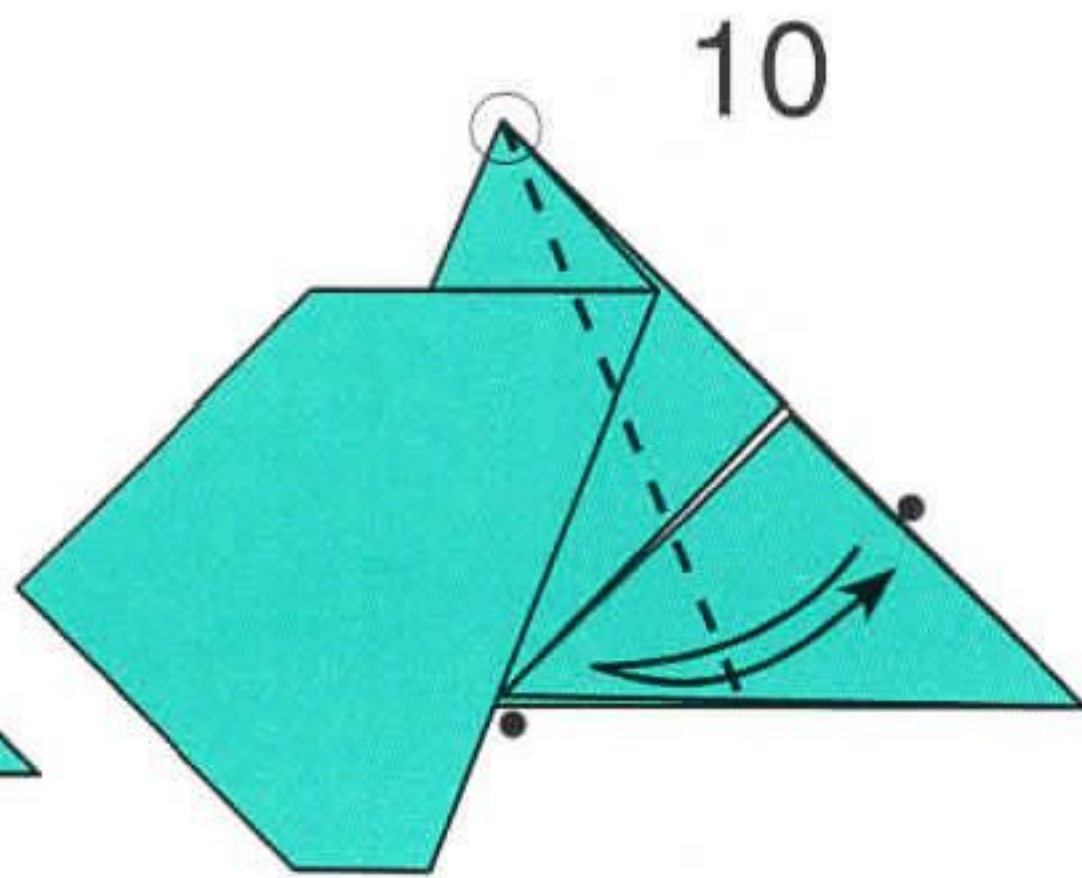


8

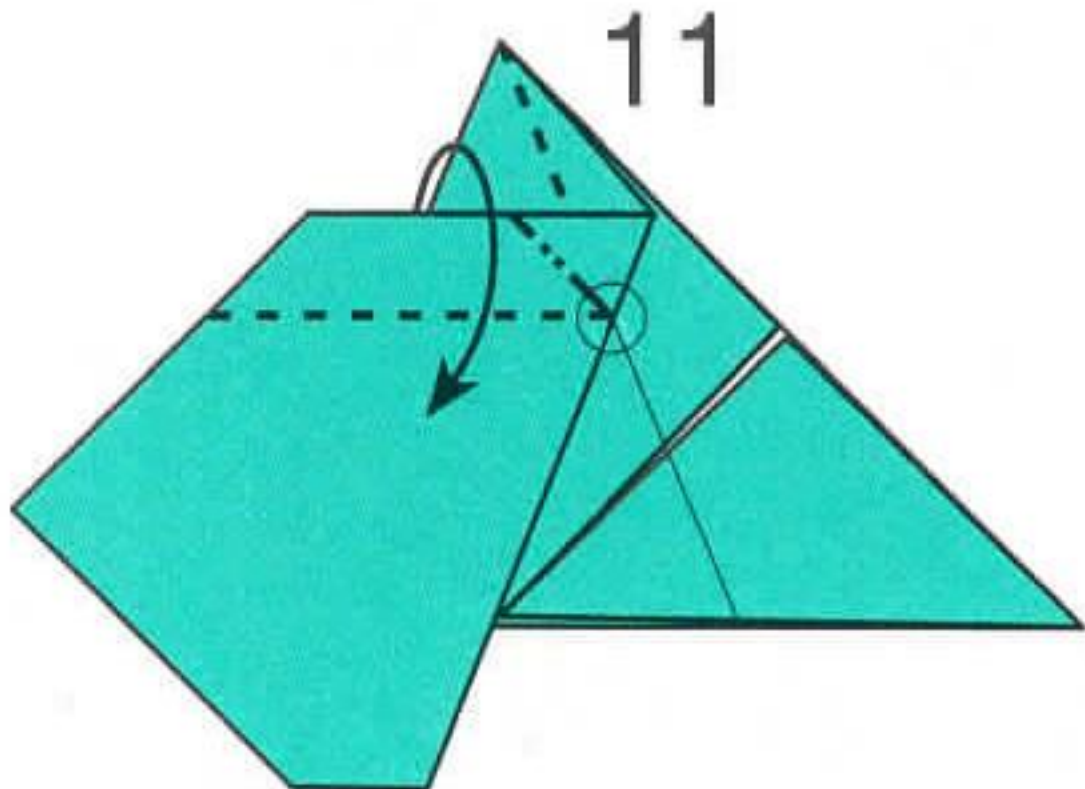


9

Fold so that the two edges align, while flipping out the bottom layer.

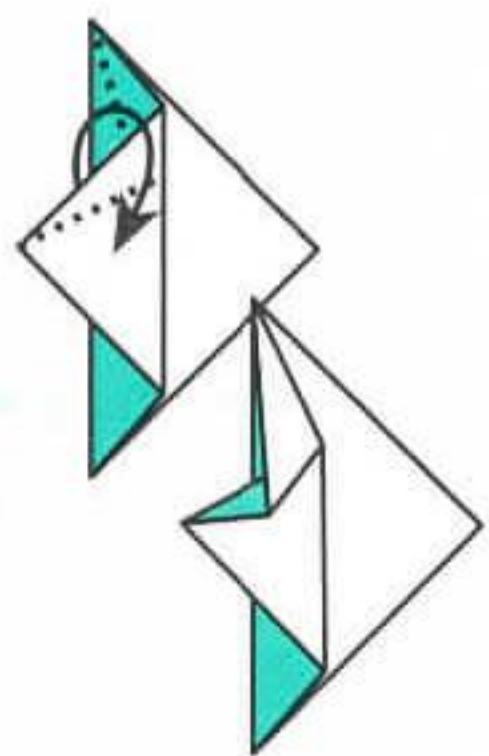


10

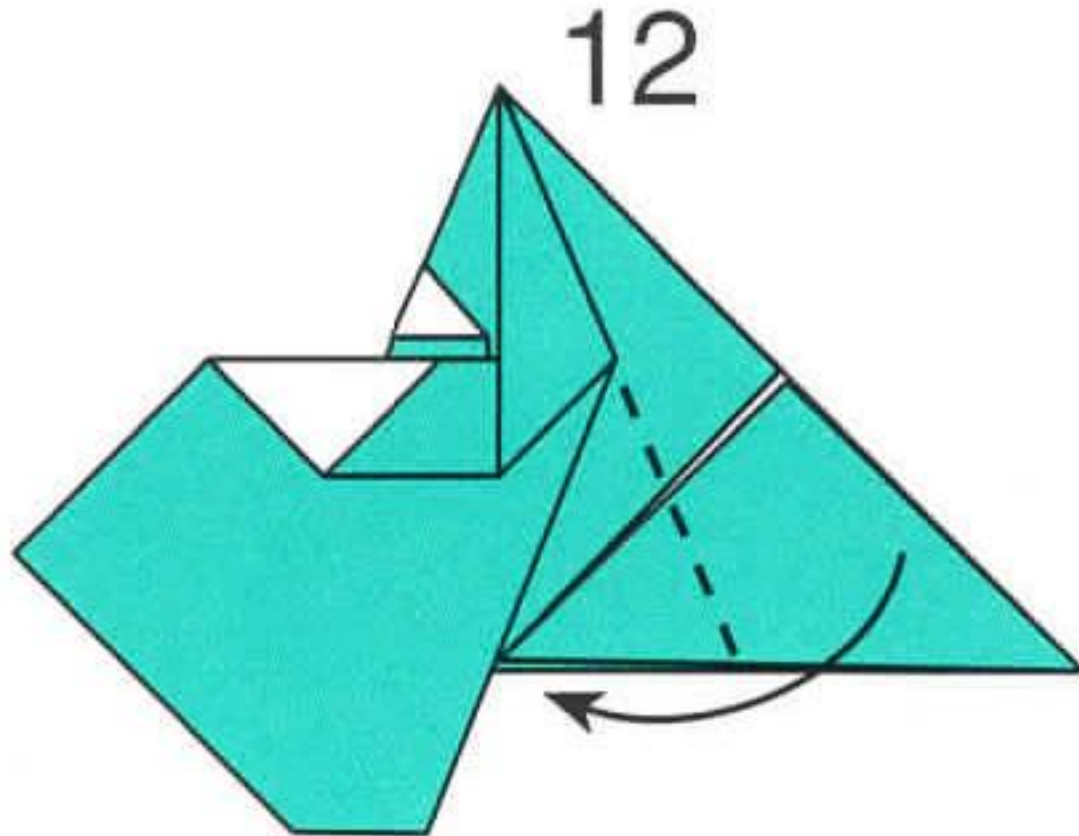


11

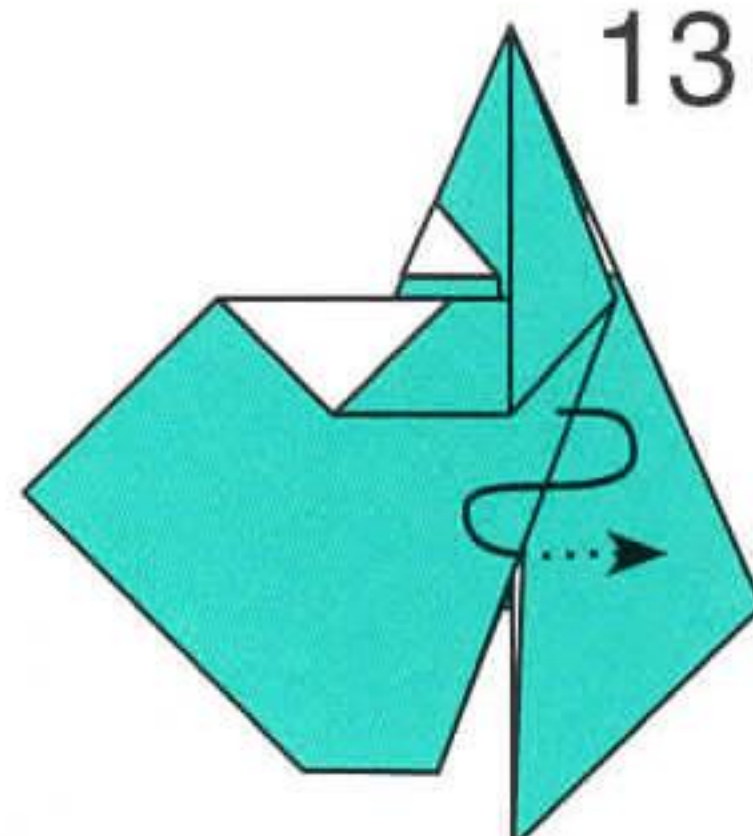
Swivel-fold



A Swivel fold is illustrated on the left. It is usually used to make an acute point.

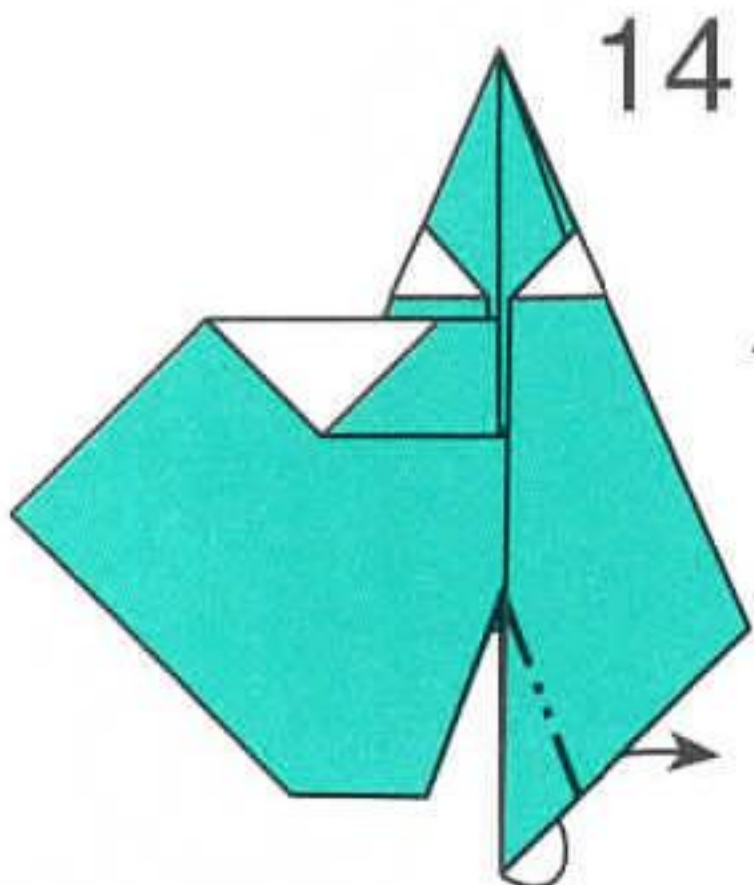


12



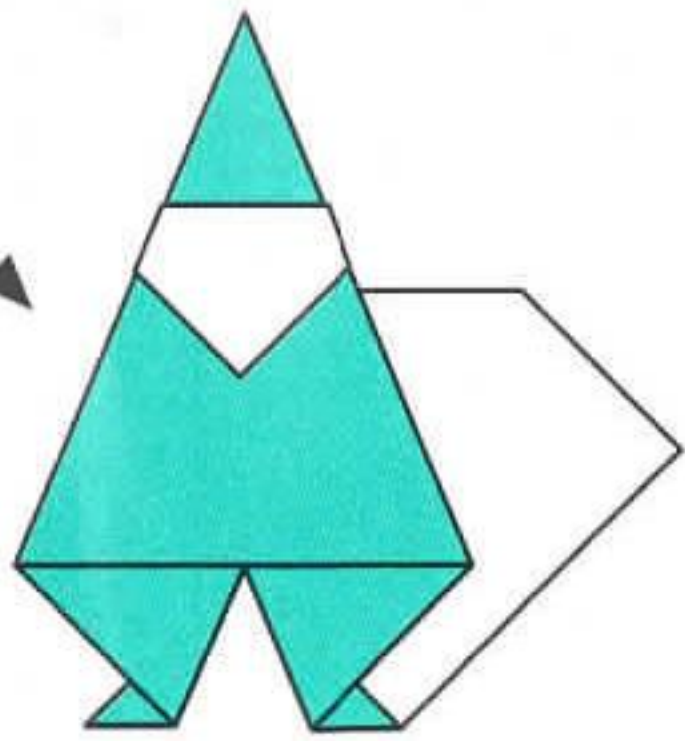
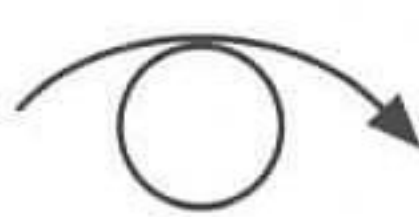
13

Tuck into the uppermost pocket to lock.



14

Inside reverse-fold

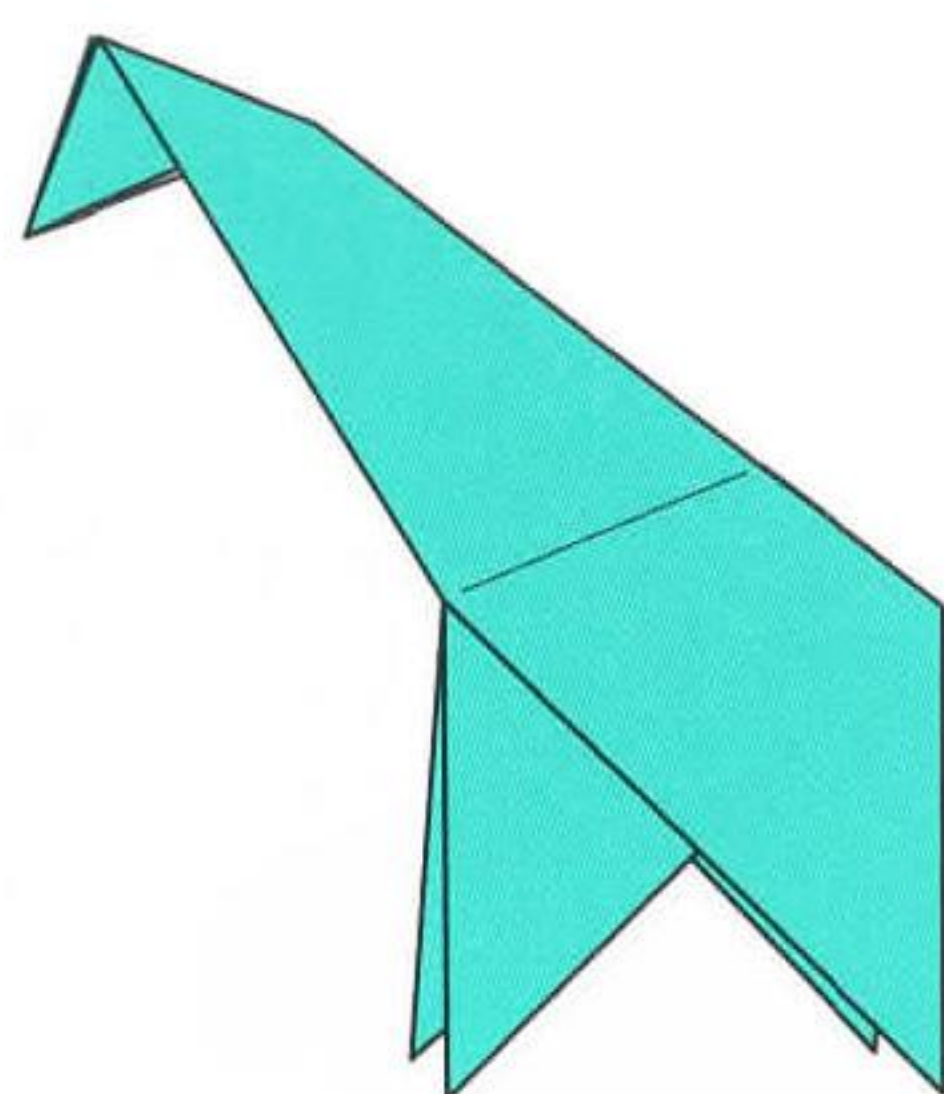


Finished.

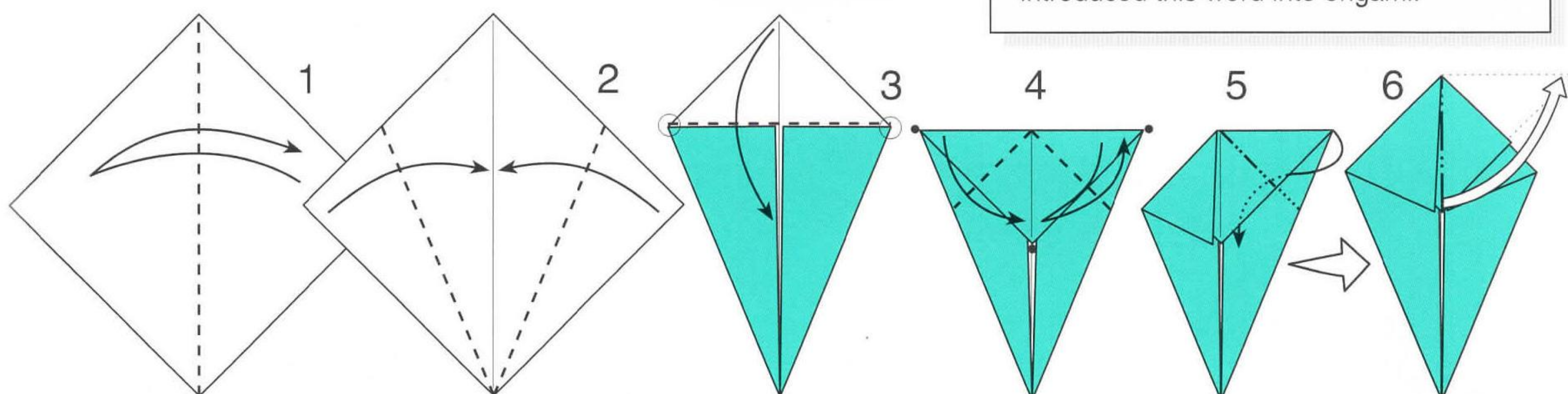
Inside-out

This model has both colored and white parts, as Mouse has a white tail. Such a technique of using different colors of each side of paper is called inside-out. Though the technique itself is not new, its name has spread out because of "Origami Inside-Out" by John Montroll, which contains only inside-out models. Note that "inside out" also means thoroughly. On the other hand, the outside surface of a Bird base is covered by only one side of paper, and the inside surface by only the other side. Such property is called one-sidedness, as coined by Kodi Husimi. It also becomes an interesting condition from a geometrical point of view.

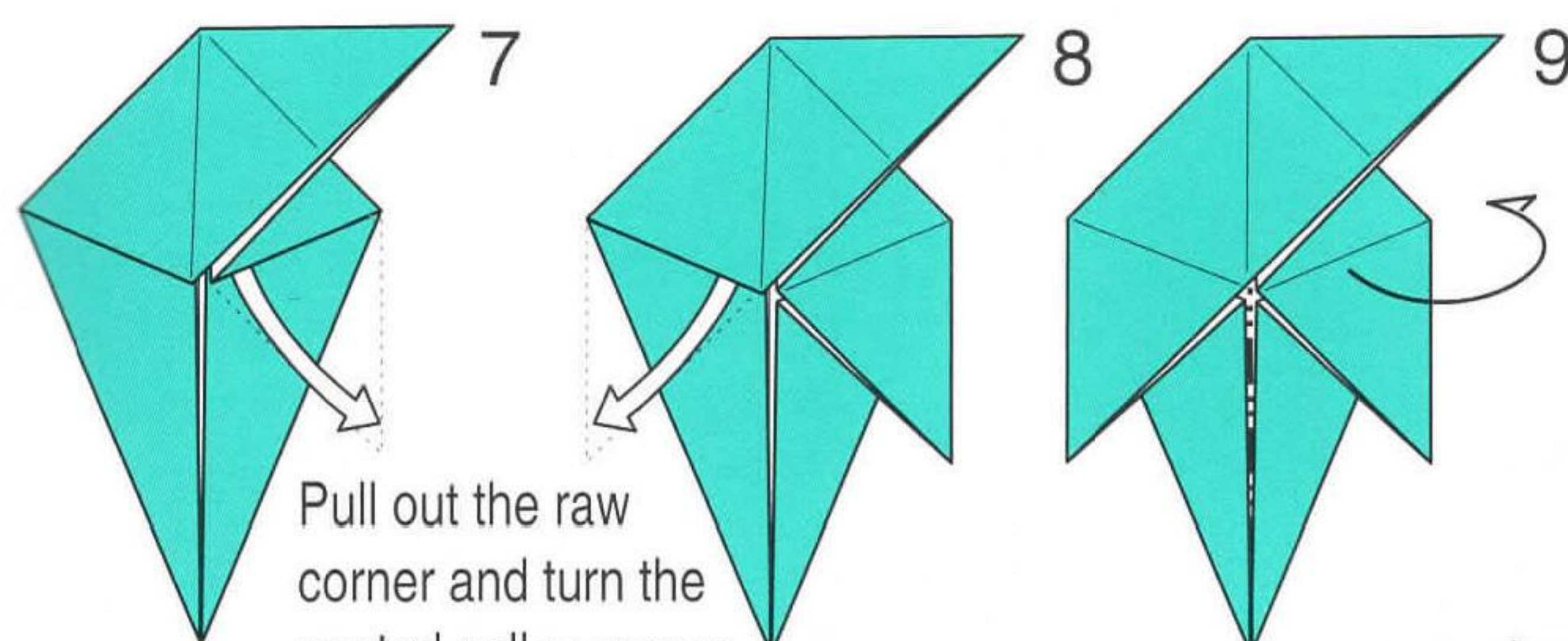
Theme: “Mitate”; Sink fold
Fold using 6” (15 cm) origami
paper.



“Mitate” is a Japanese word that means a form of expression where a simple shape is compared to another. In the case of this model, I saw a giraffe in step 9. I think the origin of origami was a game with simple shapes and imagining what it resembled like (“mitate”). Seiji Nishikawa introduced this word into origami.

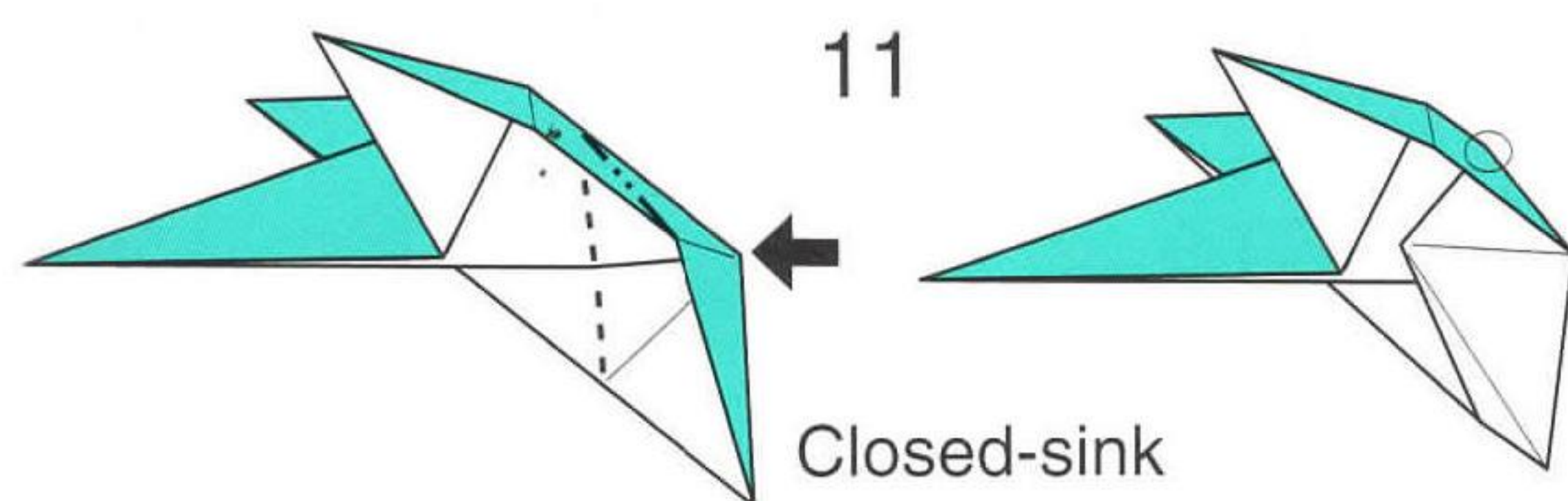
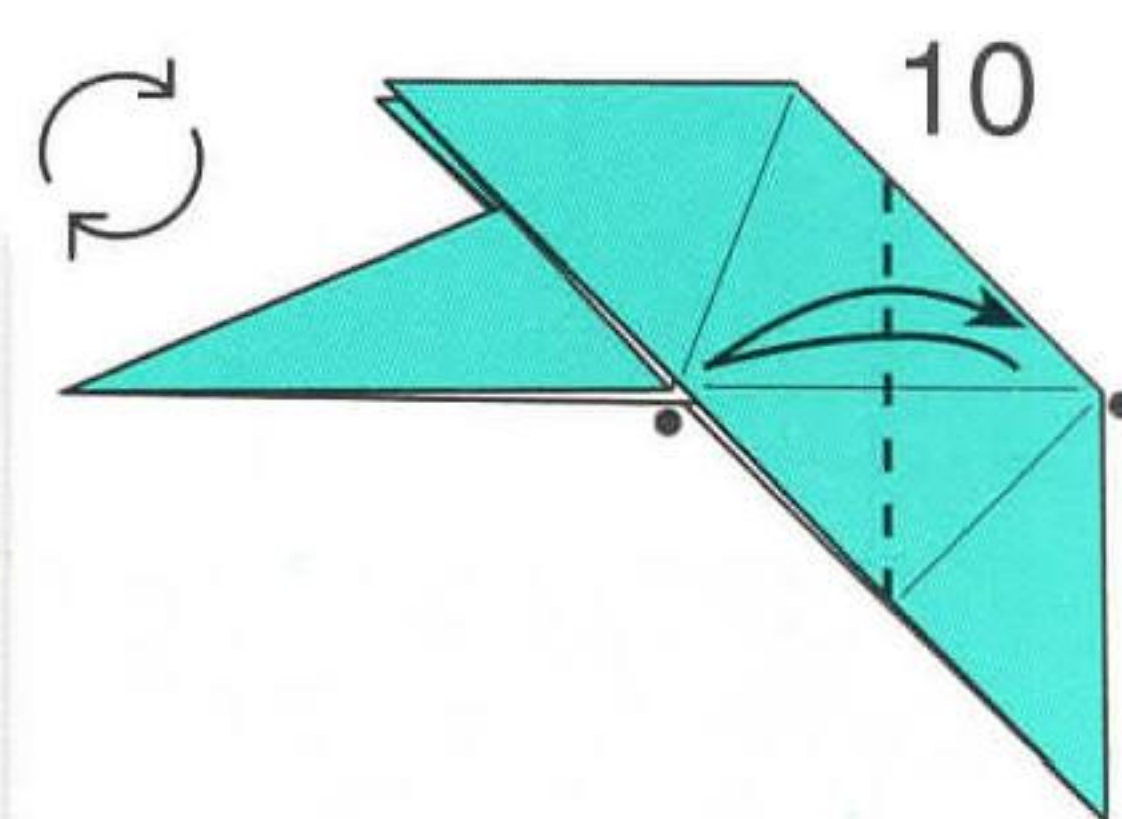
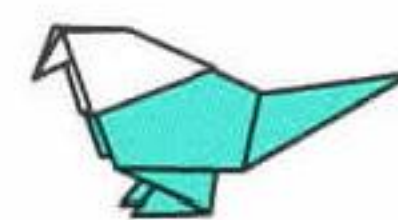


Make sure to Inside
unfold on the right. reverse-fold



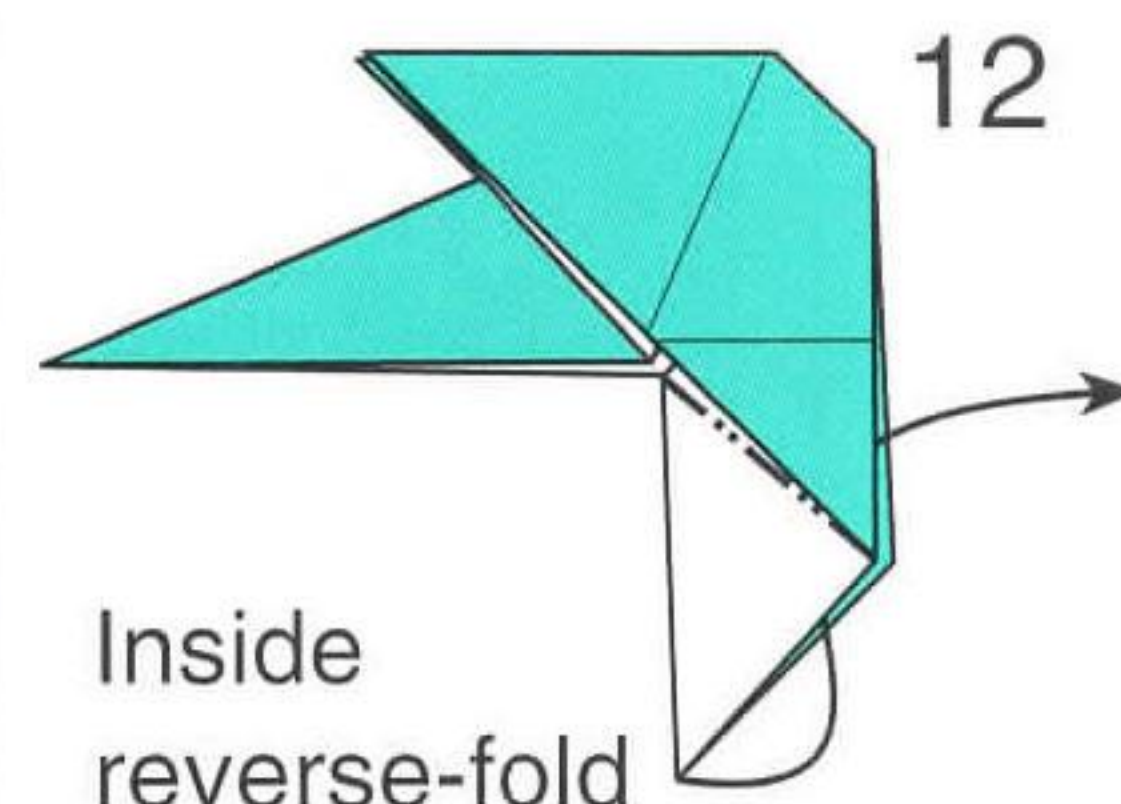
Pull out the raw corner and turn the central valley crease to mountain.

Step 9 is sometimes called a **Little-bird base**, since it is very similar to the halfway shape of the traditional *Little Bird*, shown on the right.

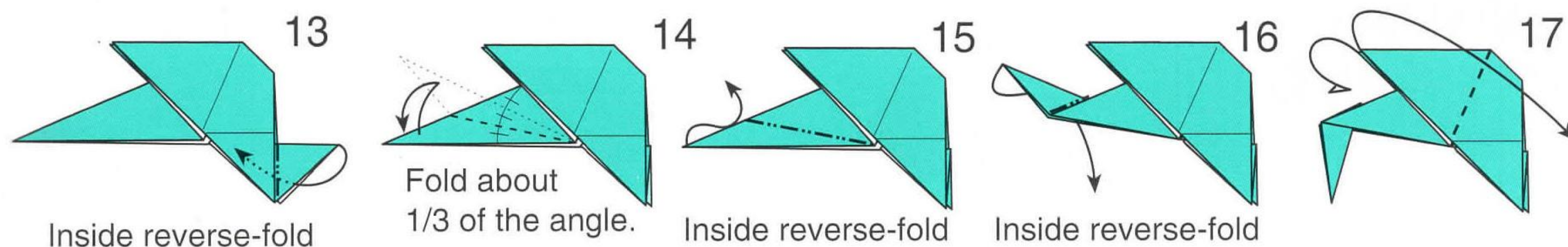


Closed-sink

← A black arrow indicates to **push in**. Step 11 is called a **sink fold**. To be precise, the step is a **closed sink** where you fold as if pushing a corner of an envelope inward. The corner indicated by the white circle in the right diagram should be locked.



Inside
reverse-fold



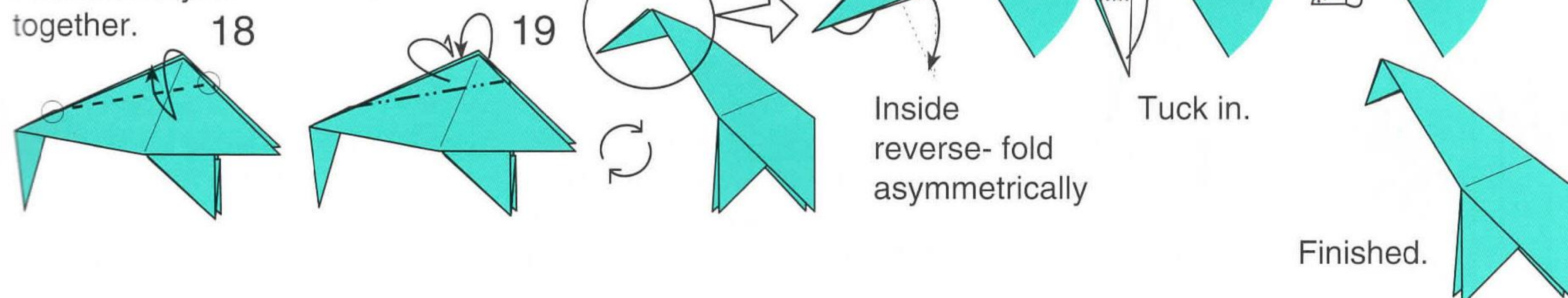
Inside reverse-fold

Fold about
 $\frac{1}{3}$ of the angle.

Inside reverse-fold

Inside reverse-fold

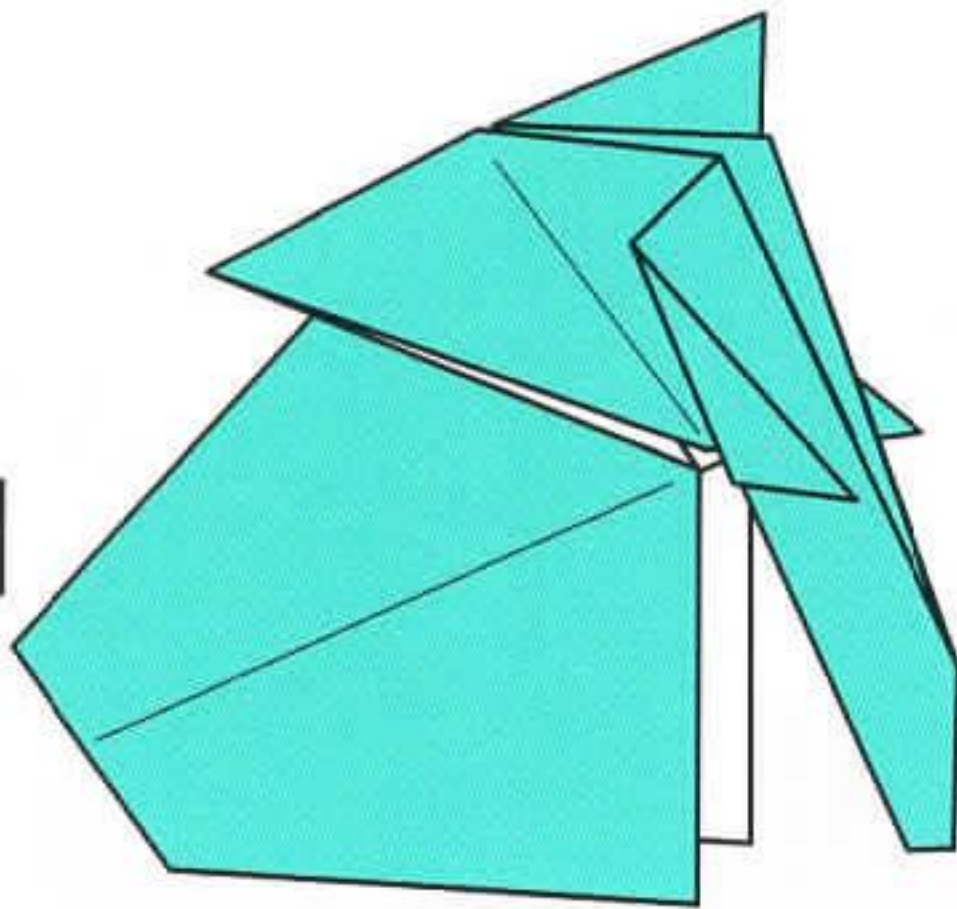
Fold both layers together. 18



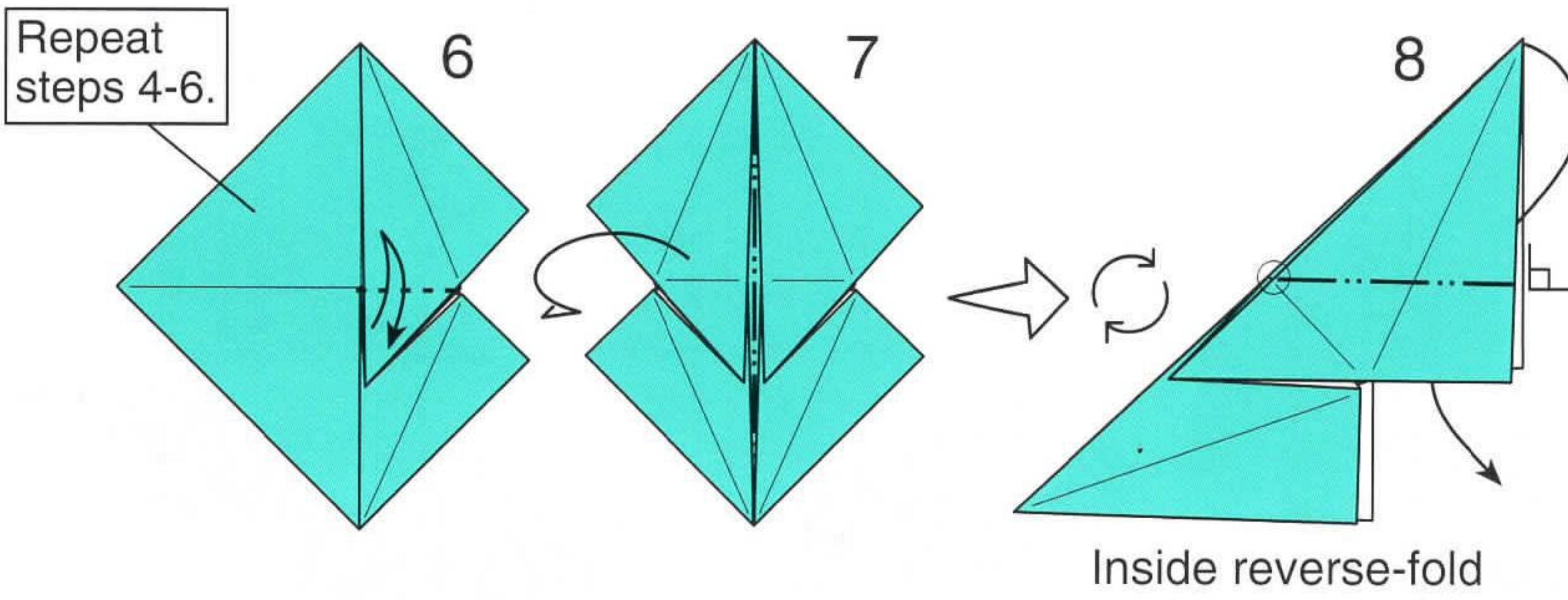
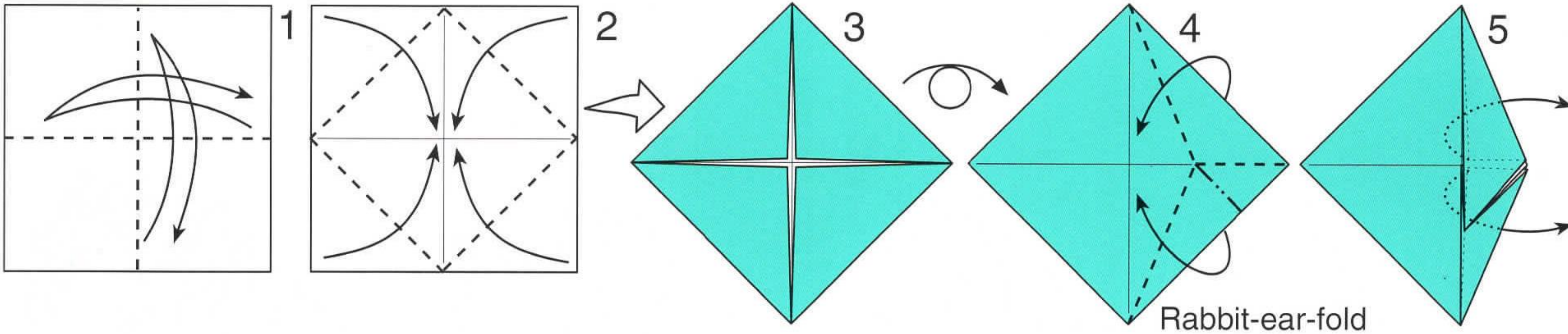
Finished.

Elephant

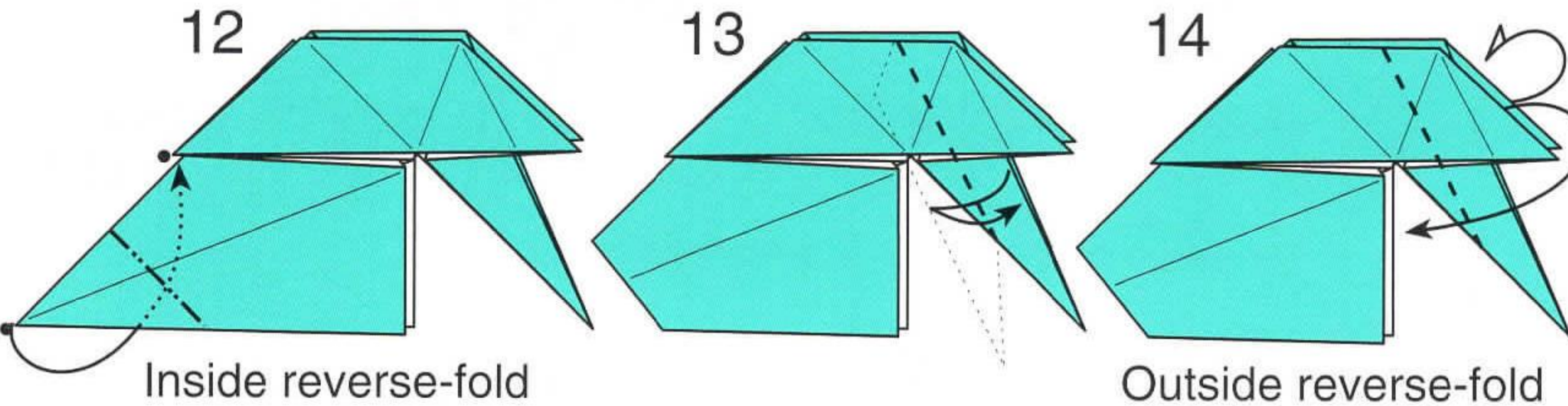
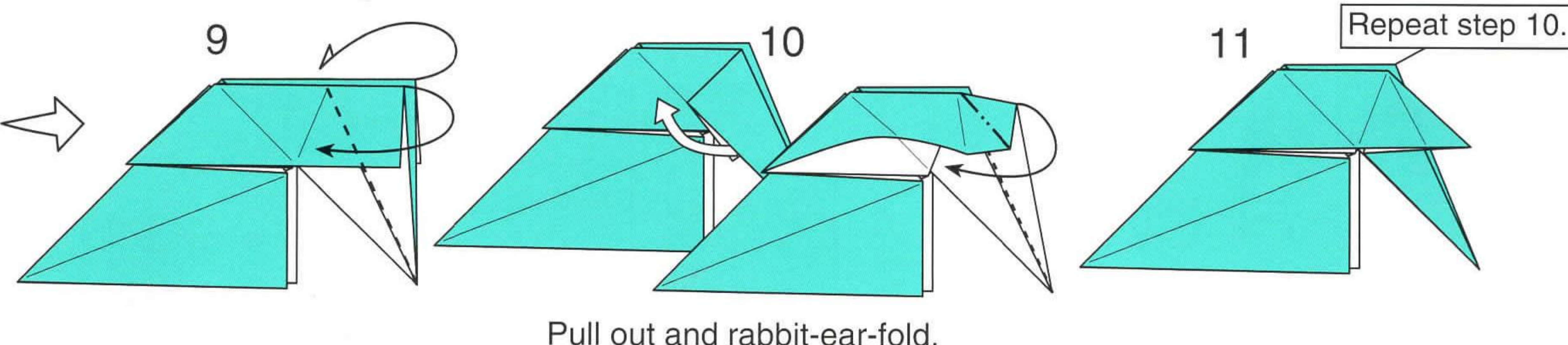
Theme: Blintz fold; Outside reverse fold
Fold using 6" (15 cm) origami paper.



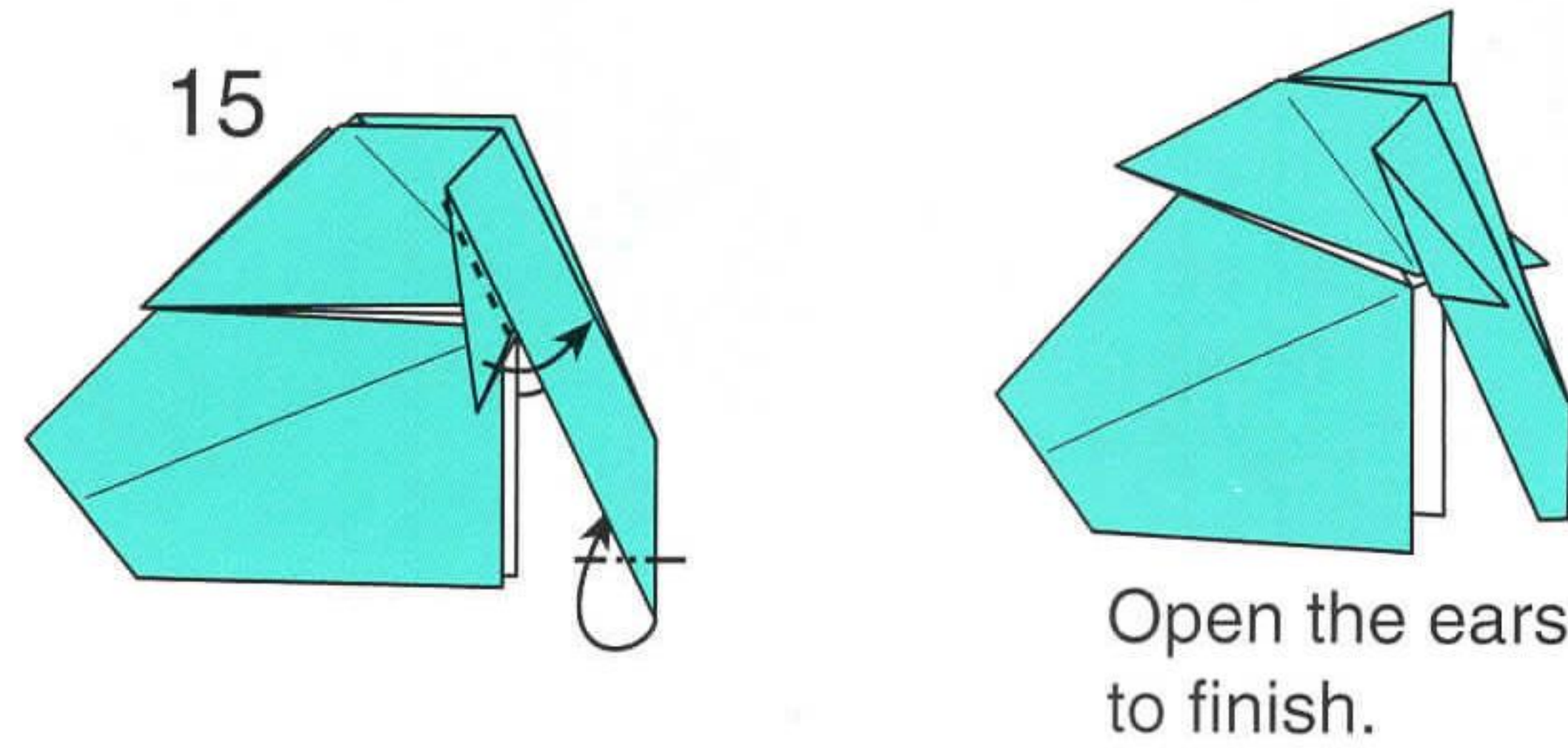
Step 2 is called a blintz fold. Since it doubles the layers of the square, this fold is often used to enhance existing bases or models.



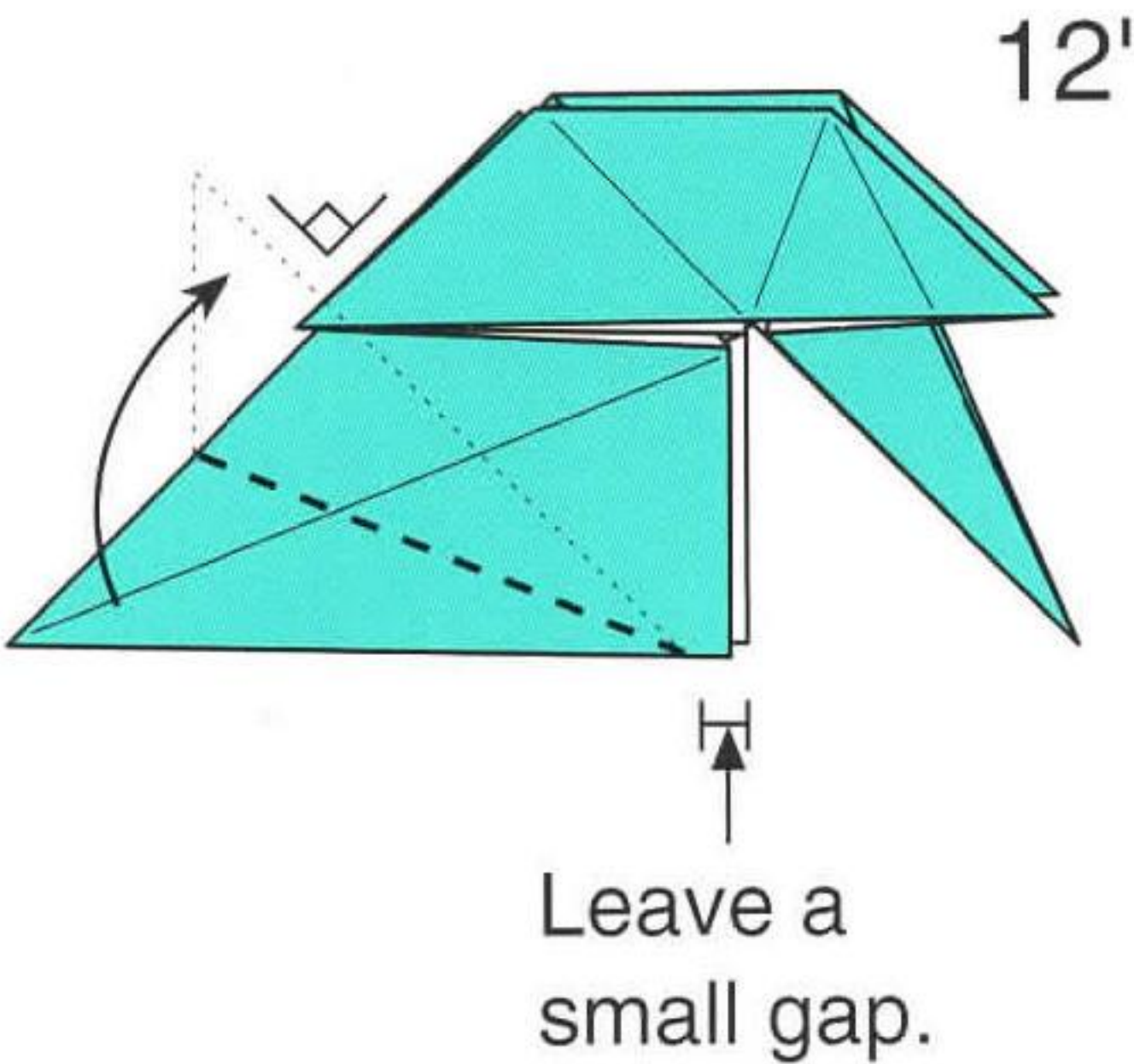
Tips: How to fold neatly (Part 2)
Make sure that all the creases intersect each other precisely at one point. For example, make a nice corner at the white circle in step 8 by folding as far as possible, pulling down as far as the reverse-folded point. A tiny gap will be amplified in course of the sequence.



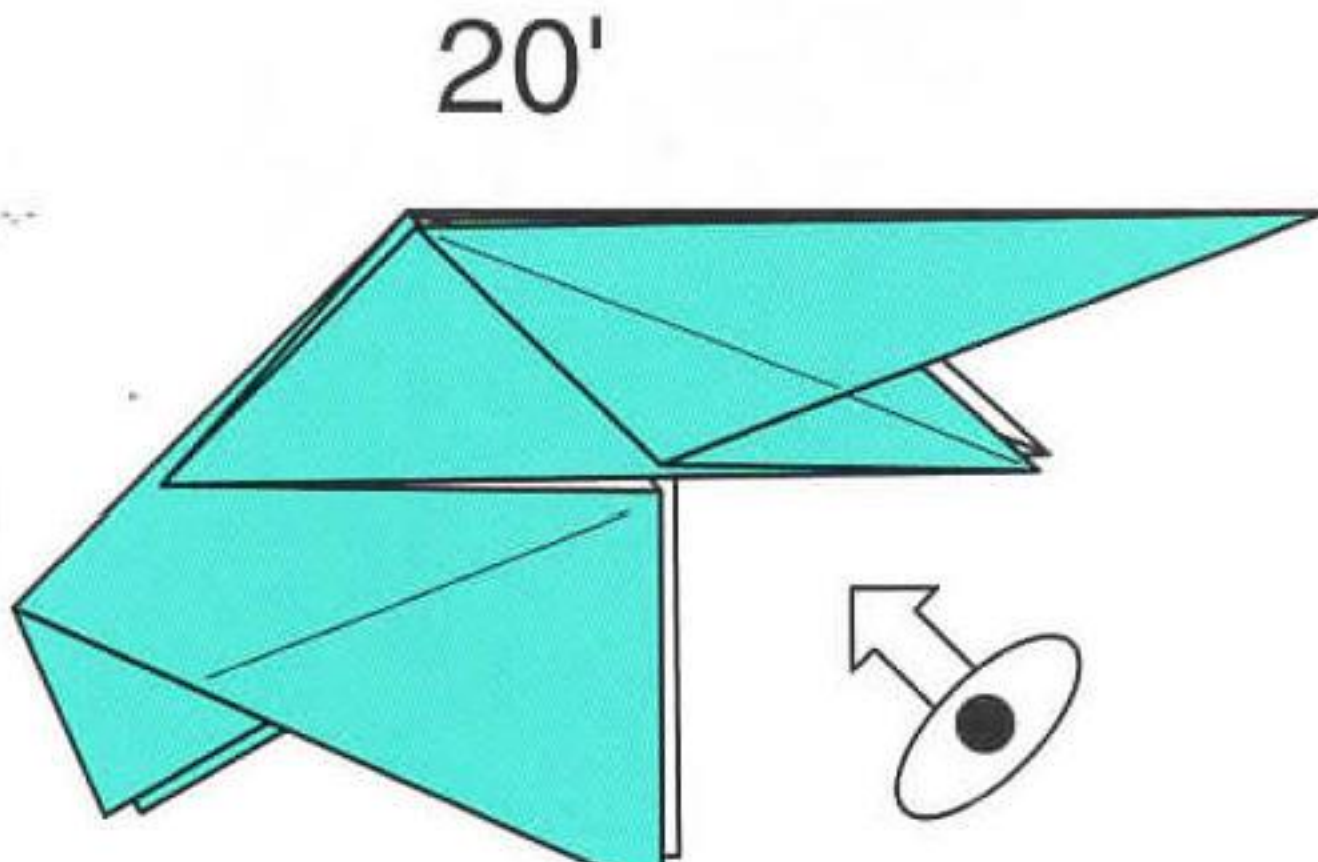
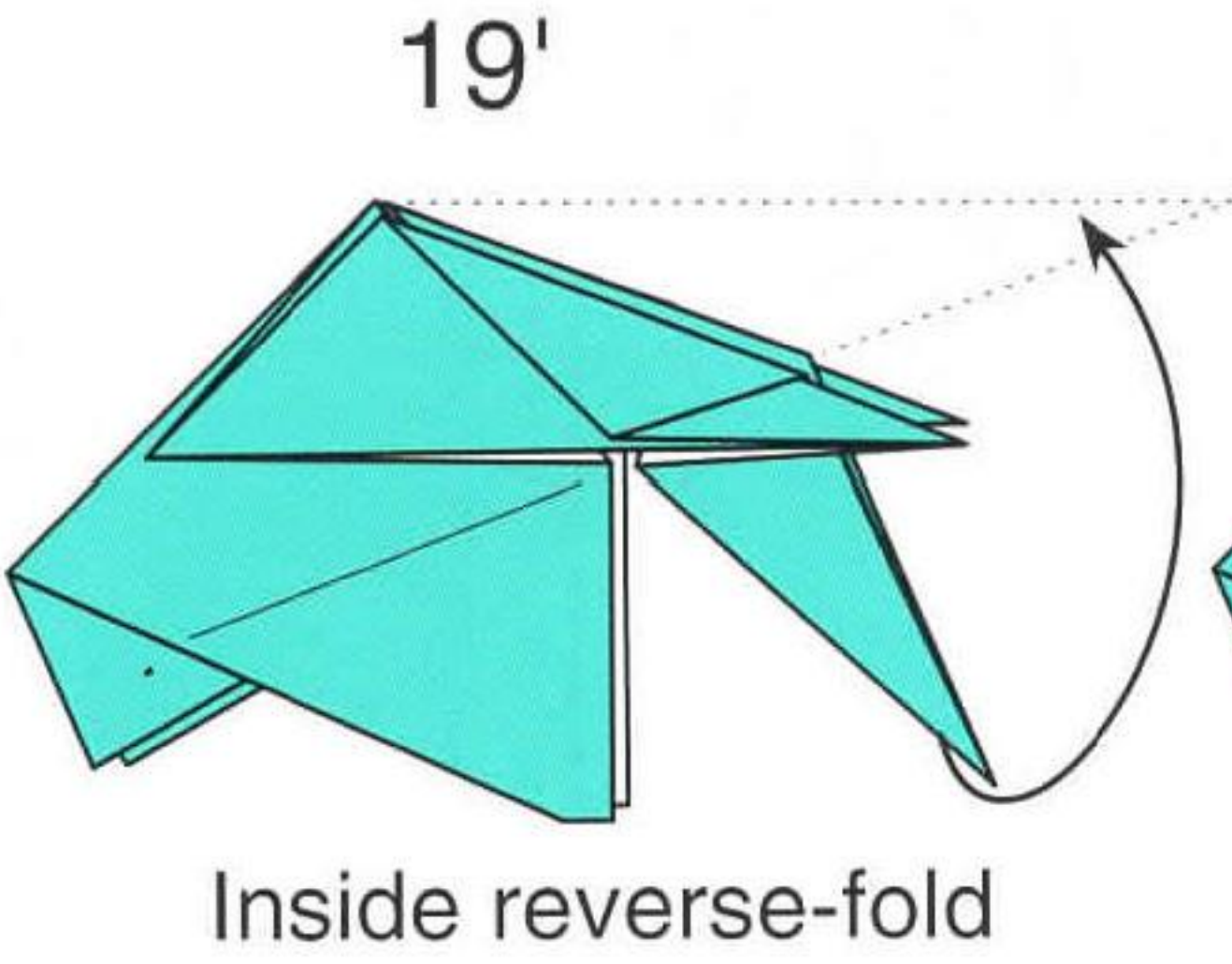
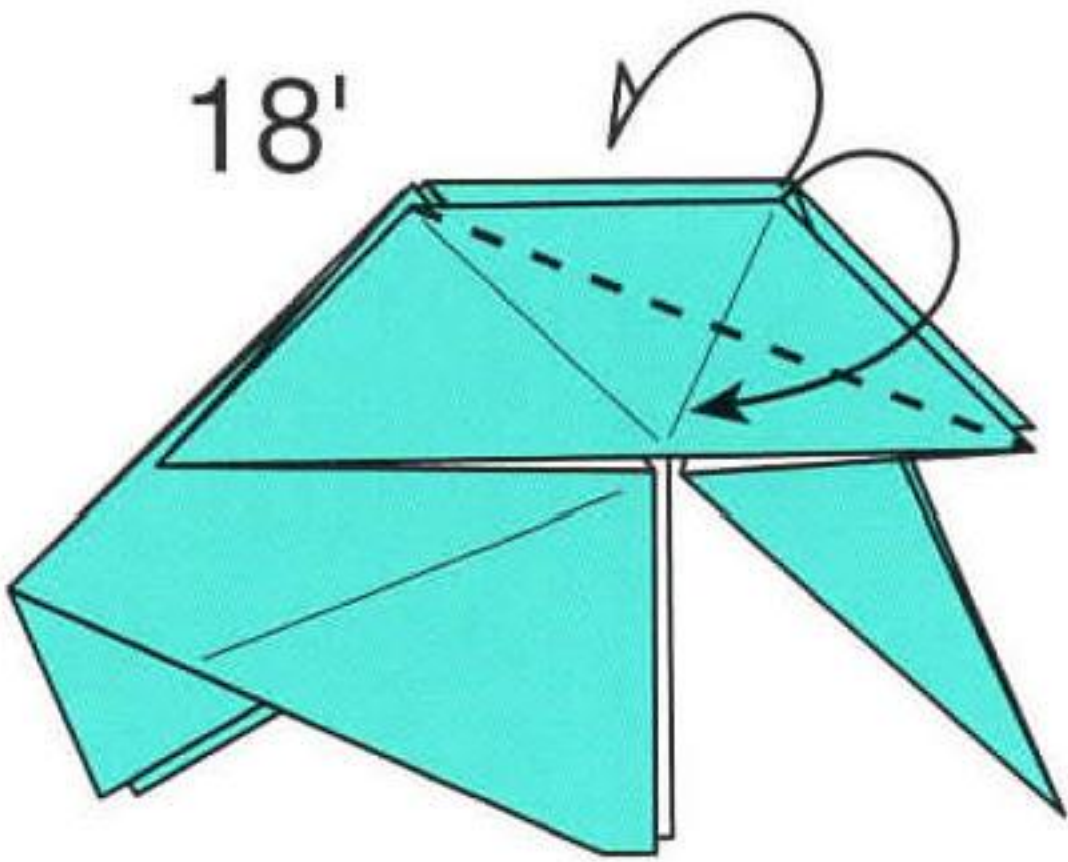
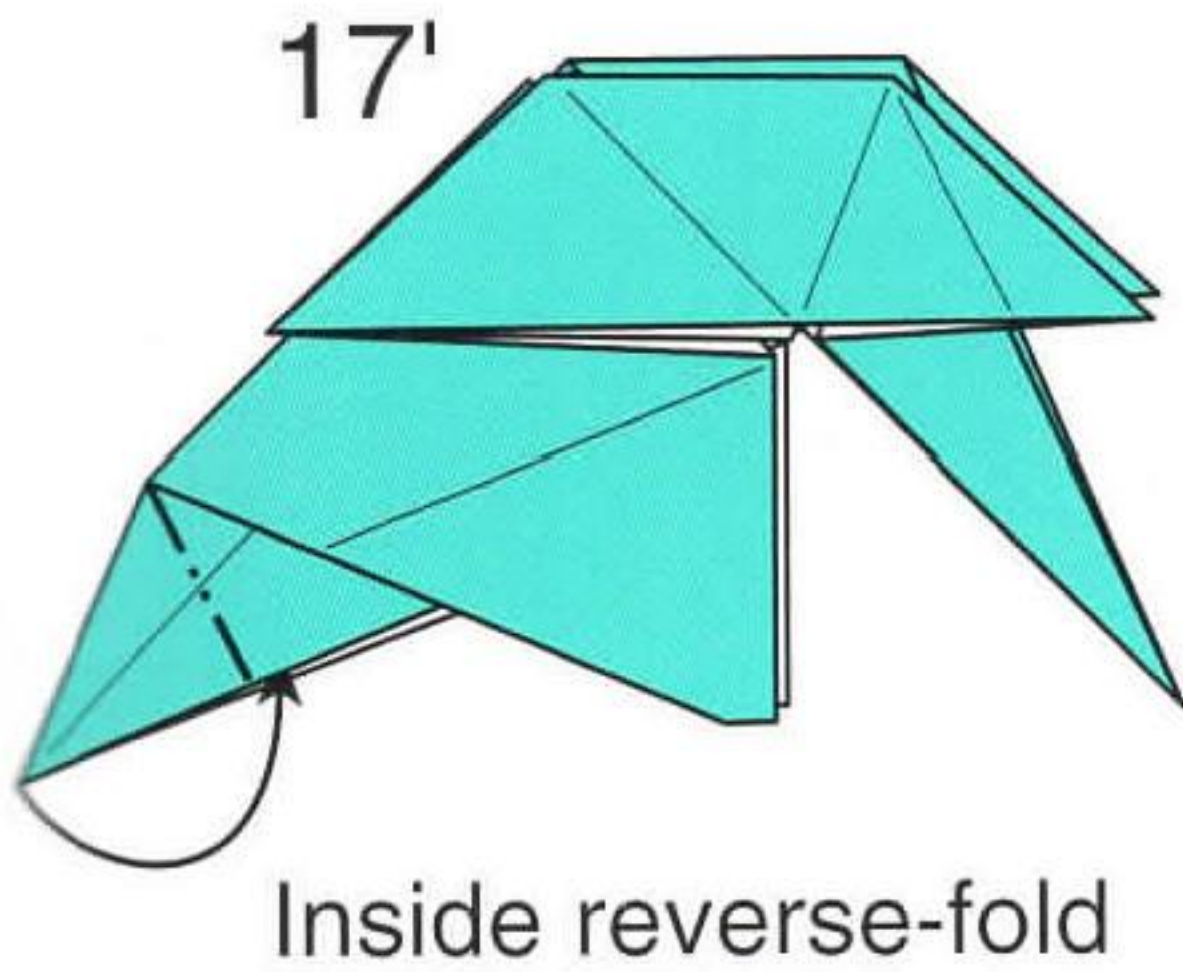
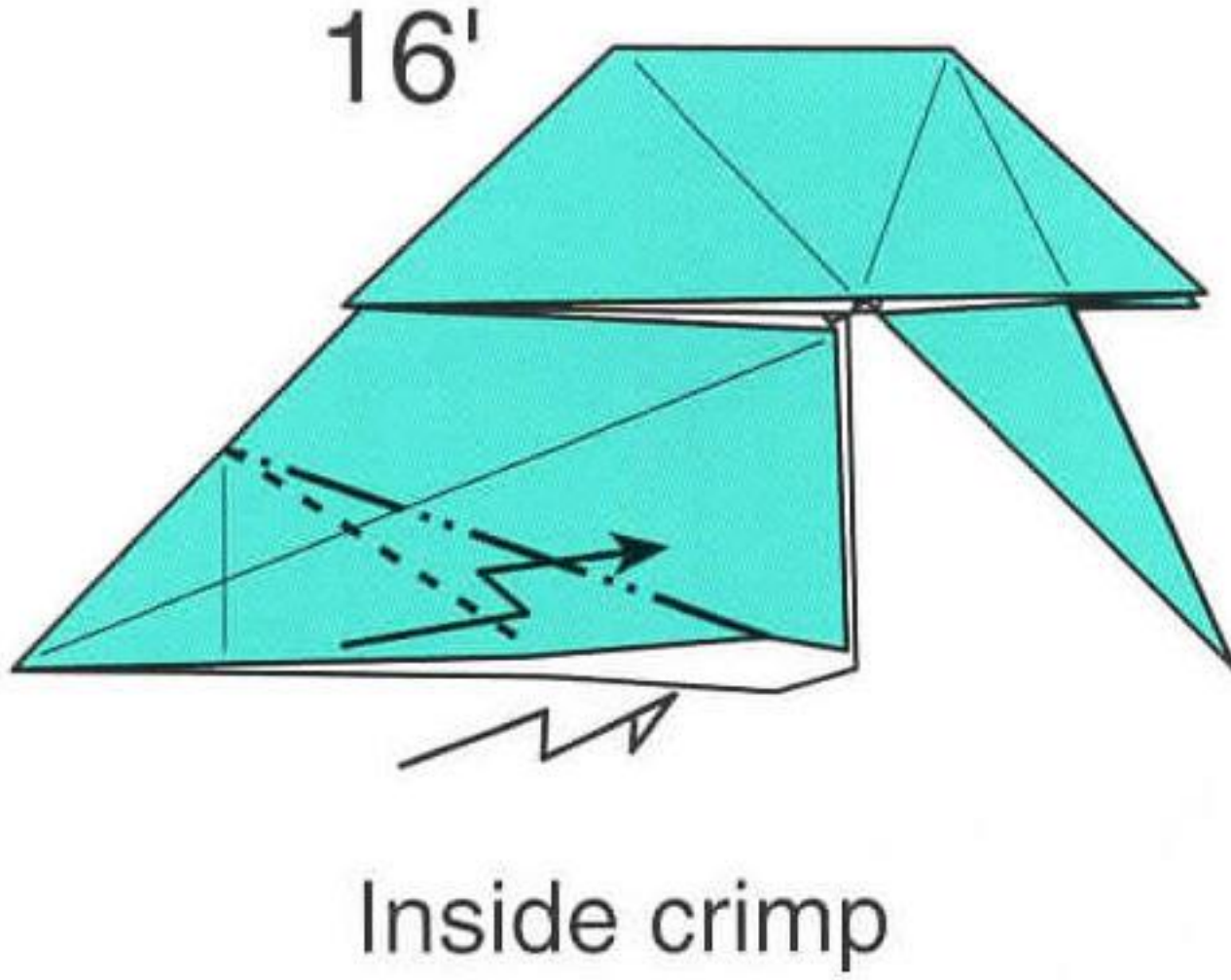
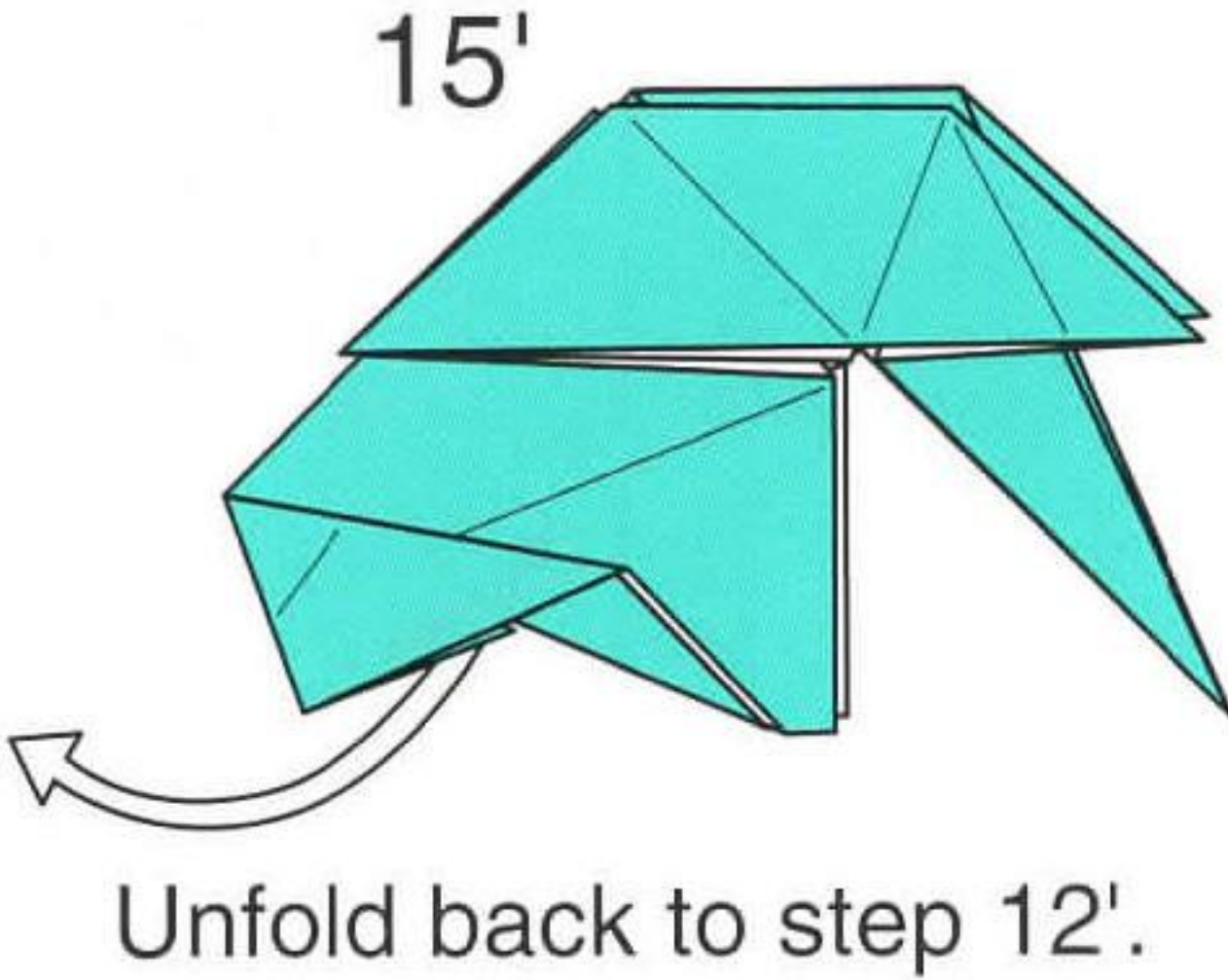
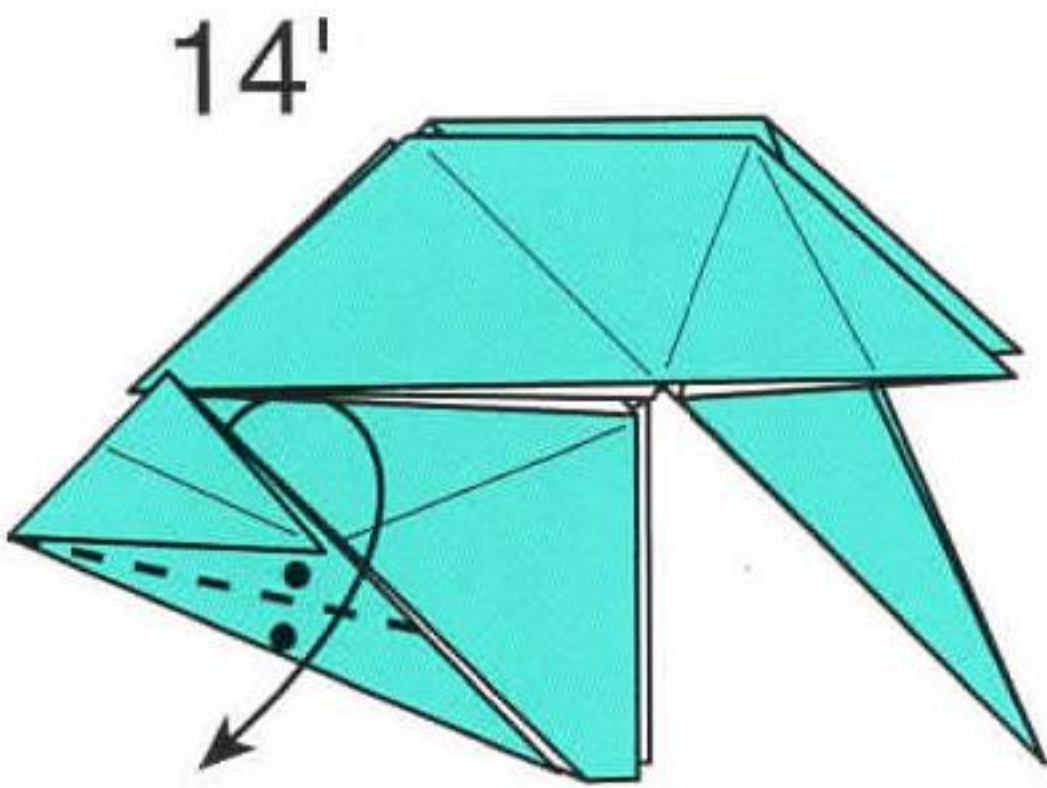
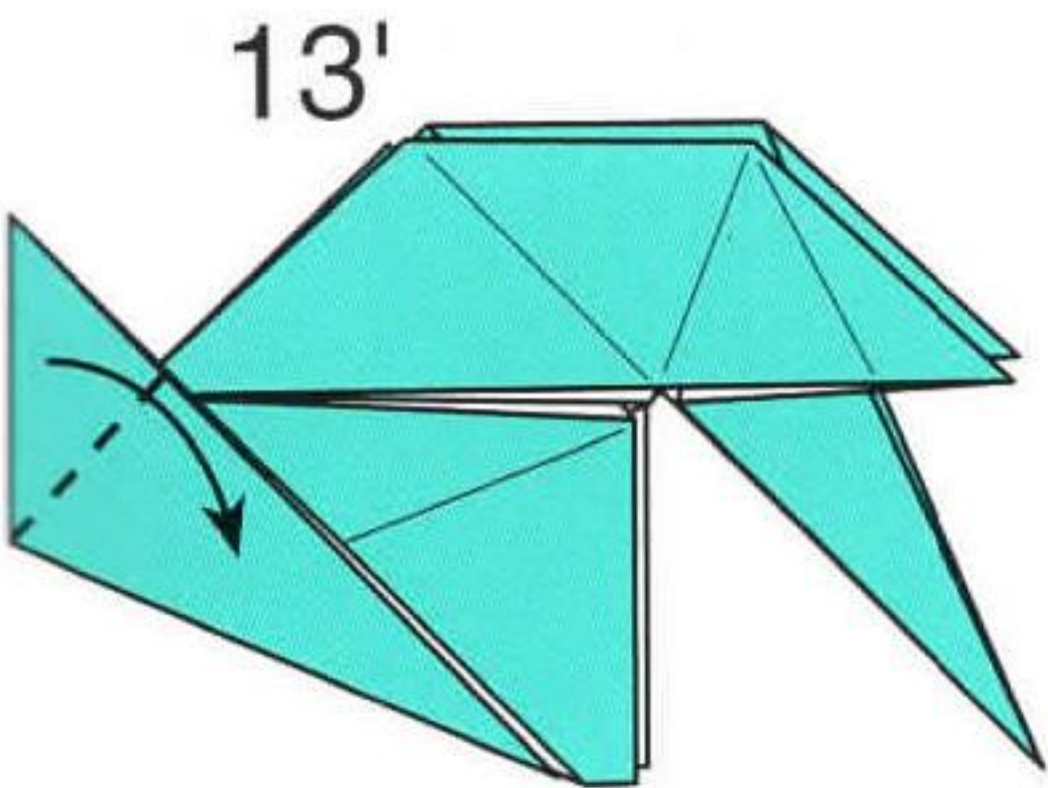
The left diagram illustrate an outside reverse fold, where you reverse the central valley crease into mountain. You can first valley-fold to make a preparatory crease, as you have done in the step 13. Also, you will have to slightly open the entire model in order to make this fold.



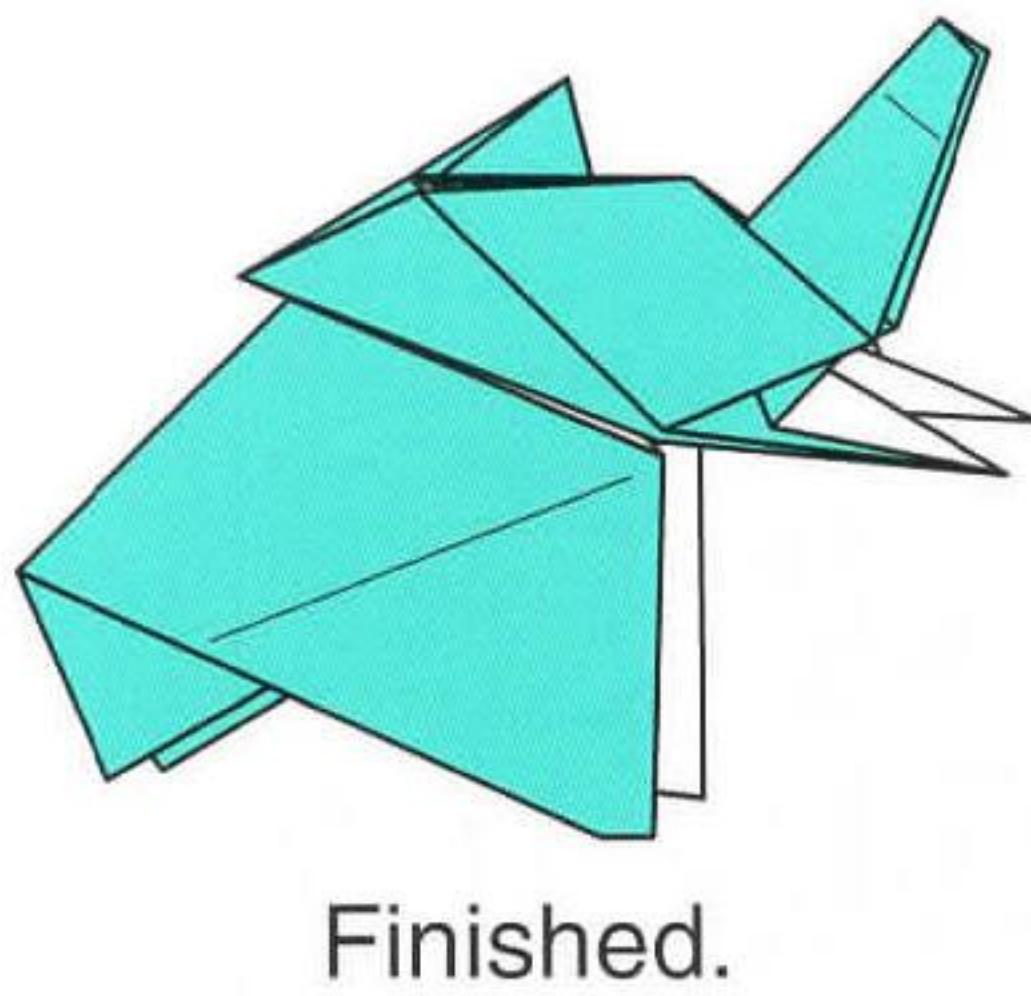
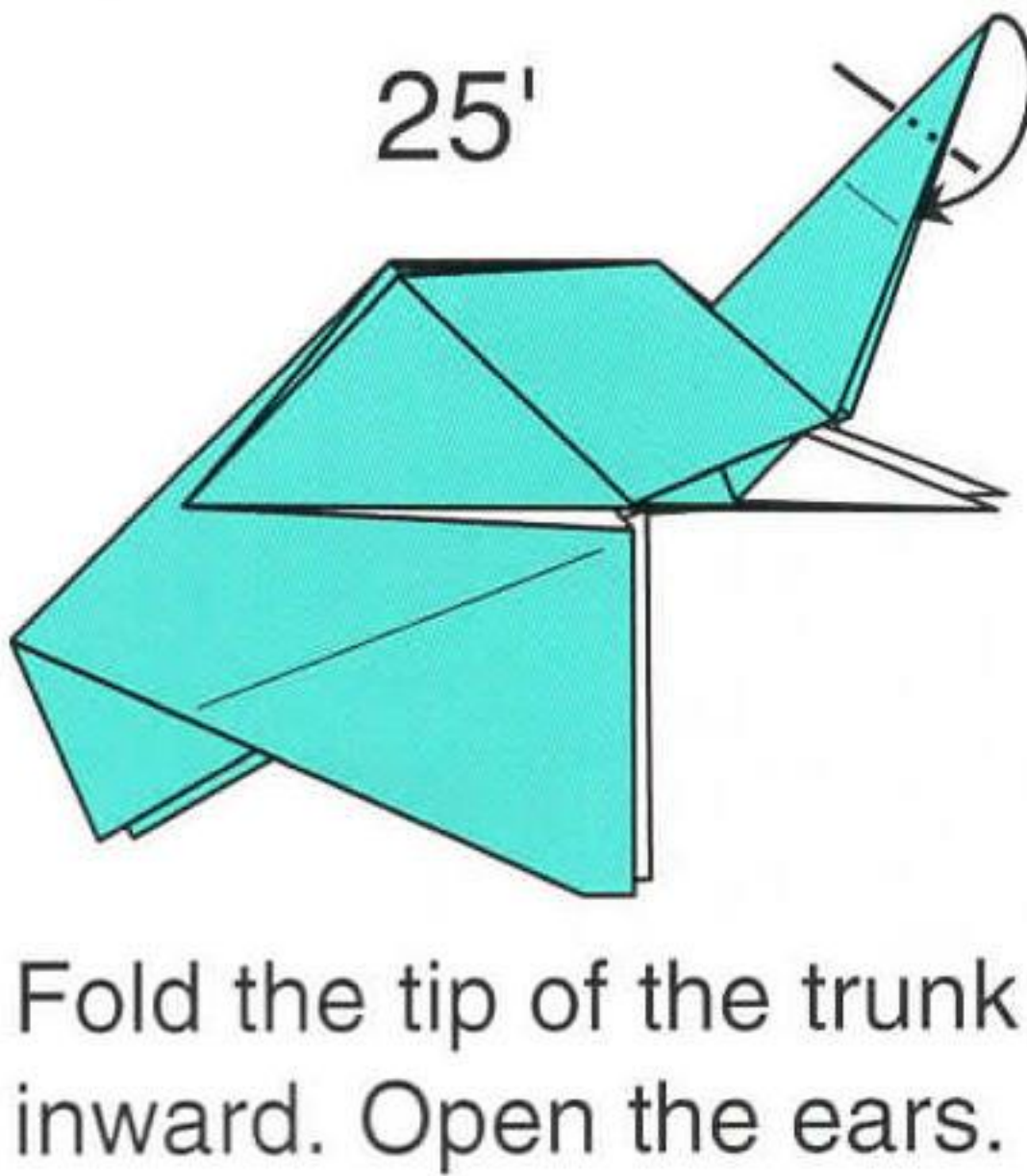
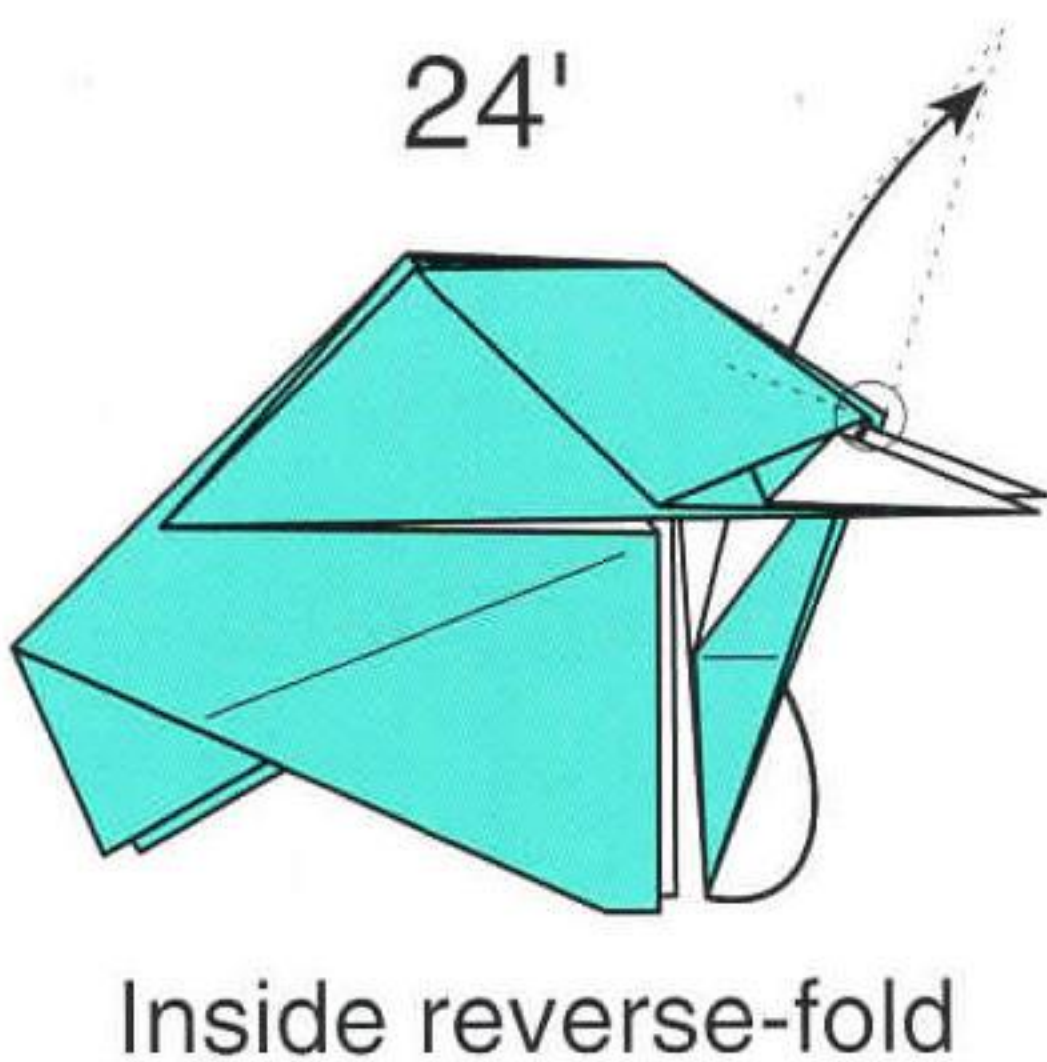
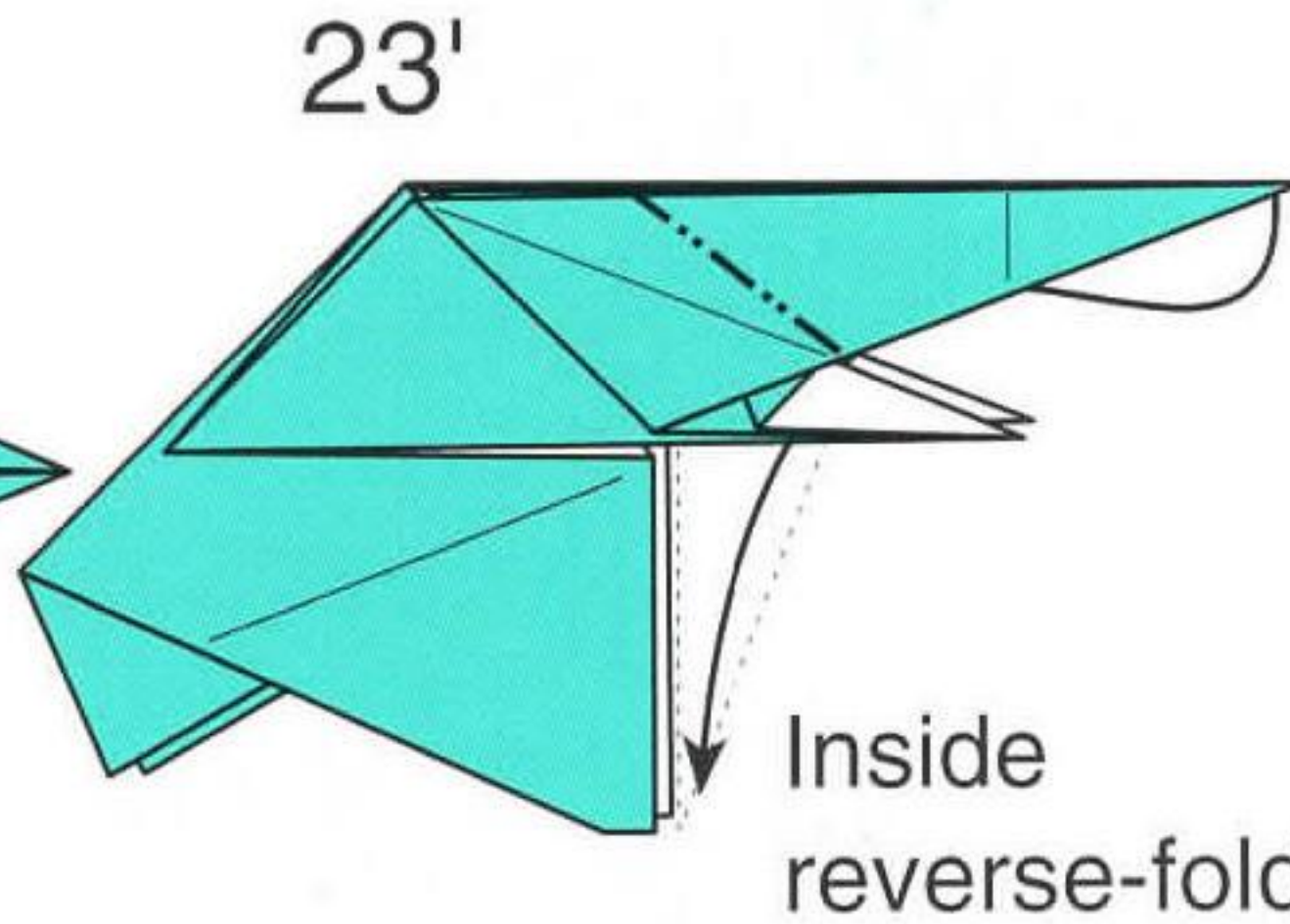
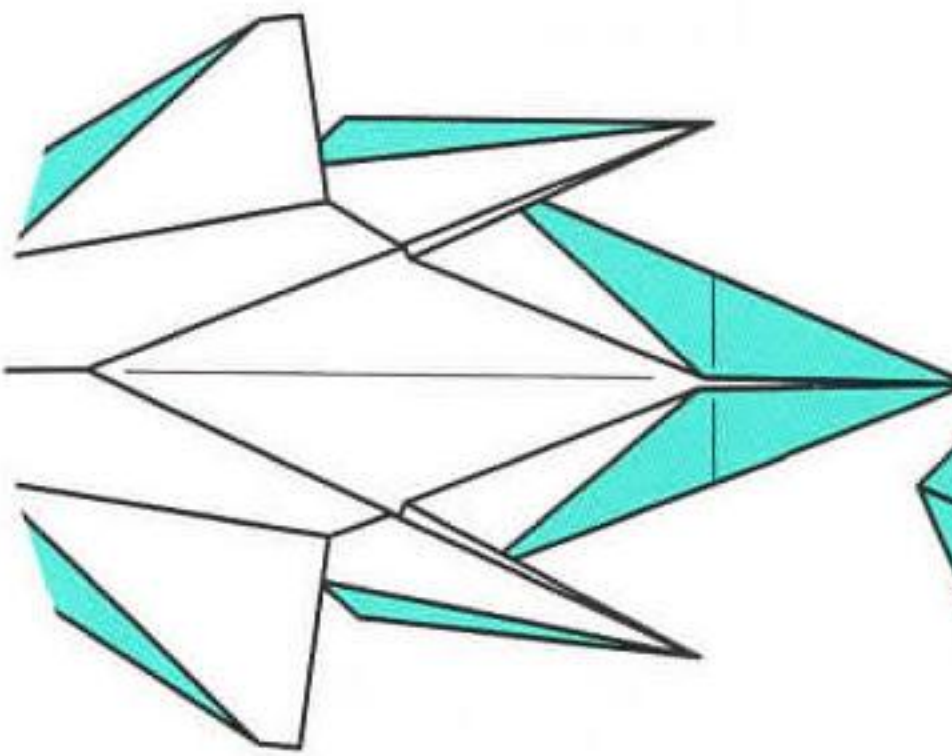
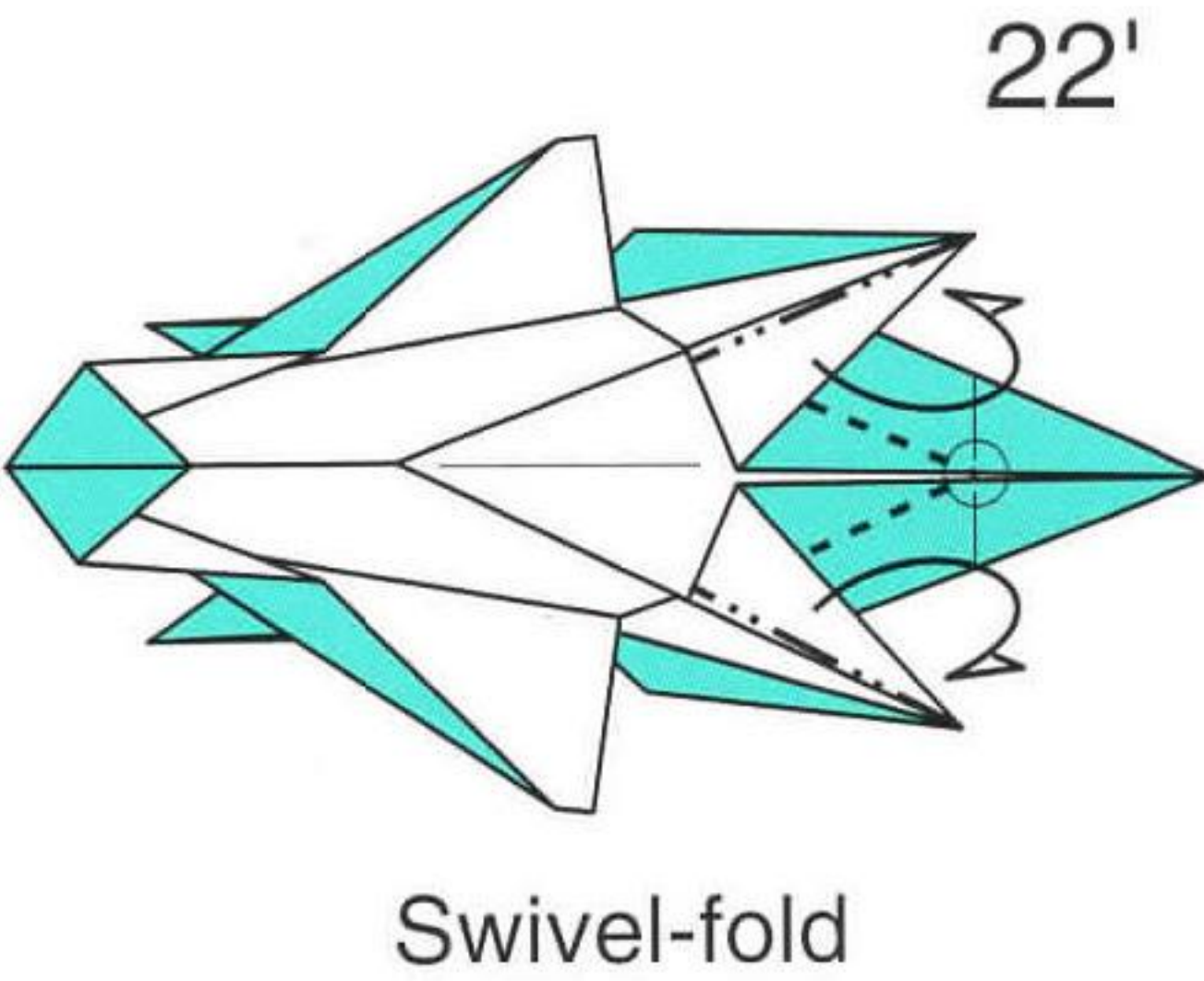
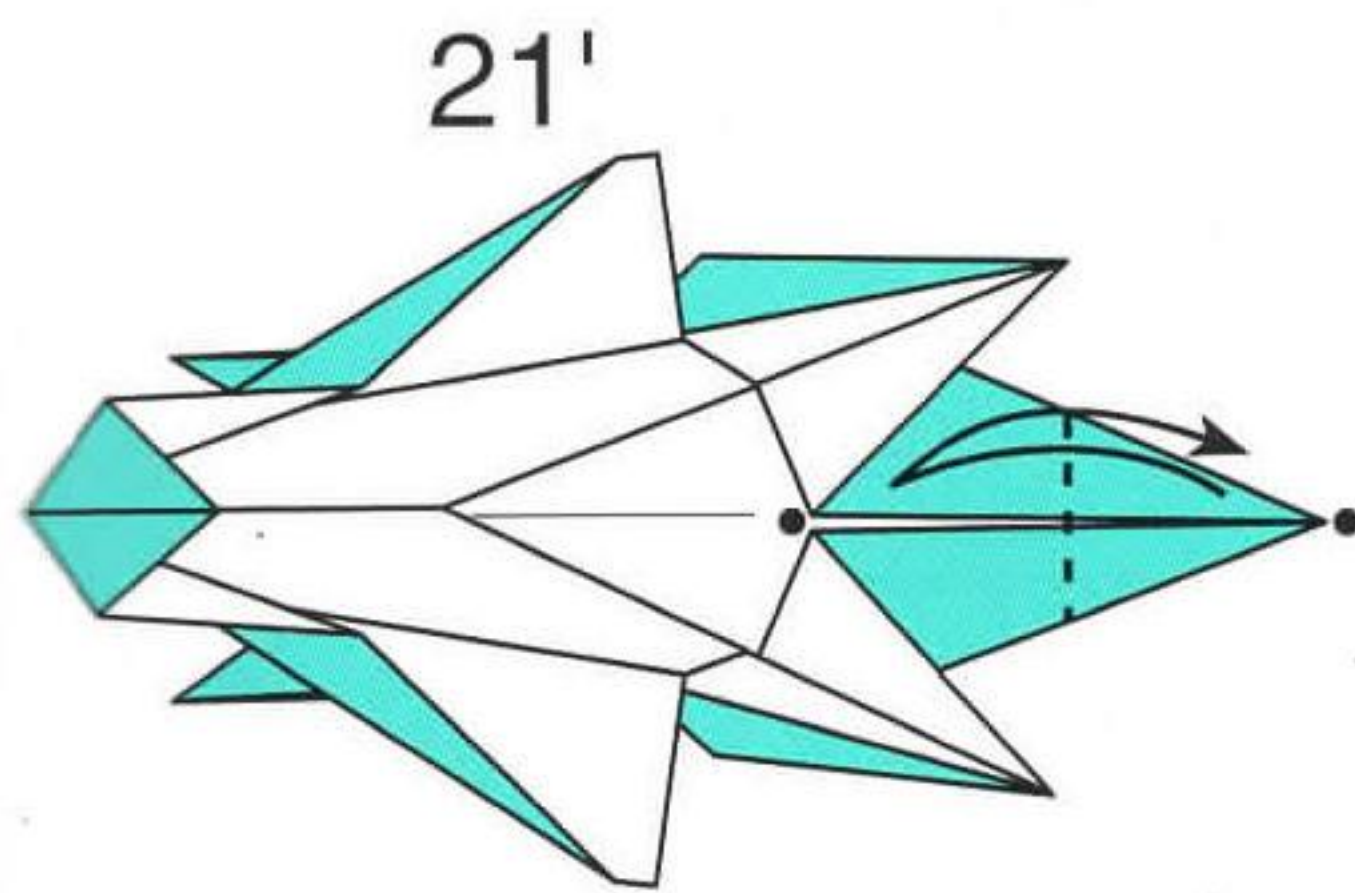
Here is a slightly modified variation.
Start from step 11.



There is no definite landmark for the step 12'. Such fold is called **judgment fold**. Though judgment is not so important with this model, a small difference sometimes results in a very different finish.



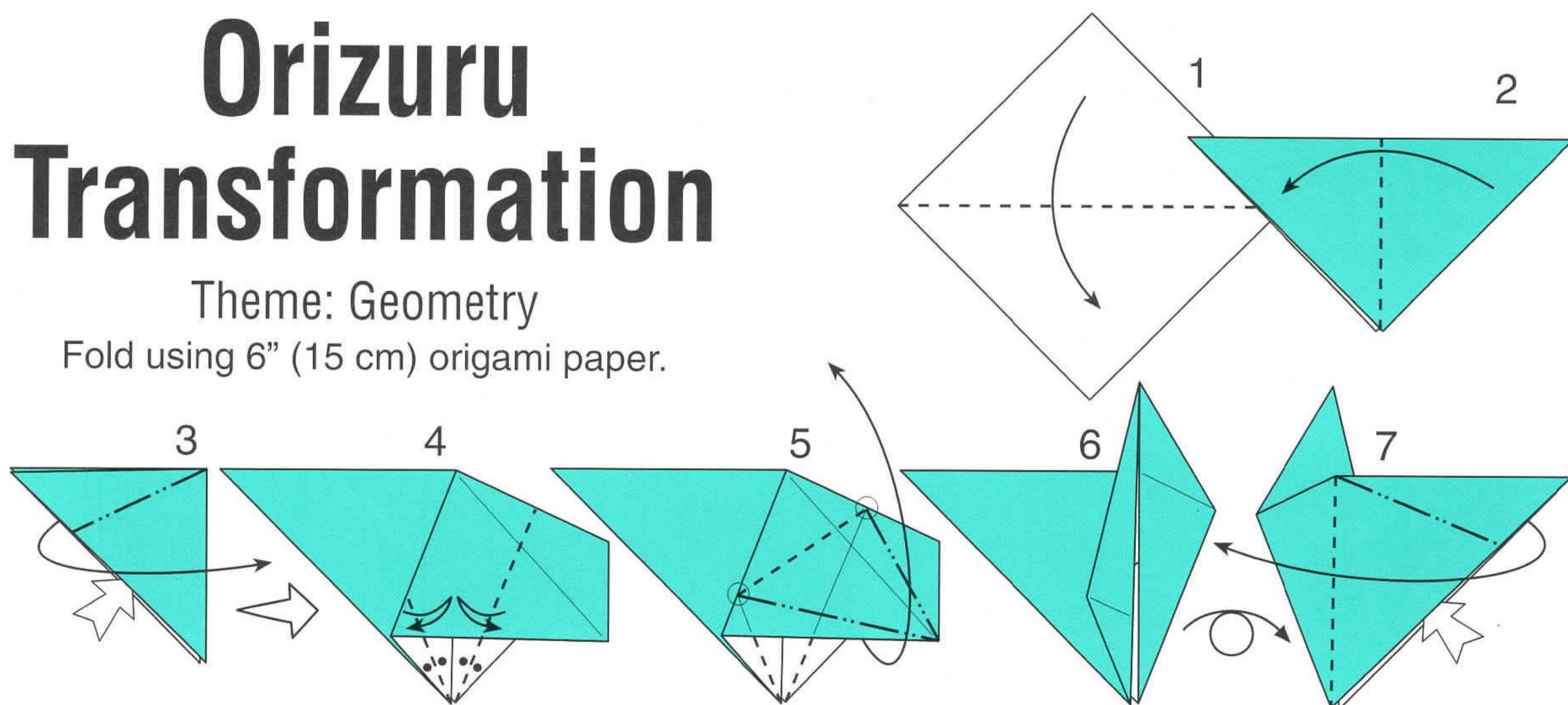
An arrow with an eye represents the viewpoint of the next diagram.



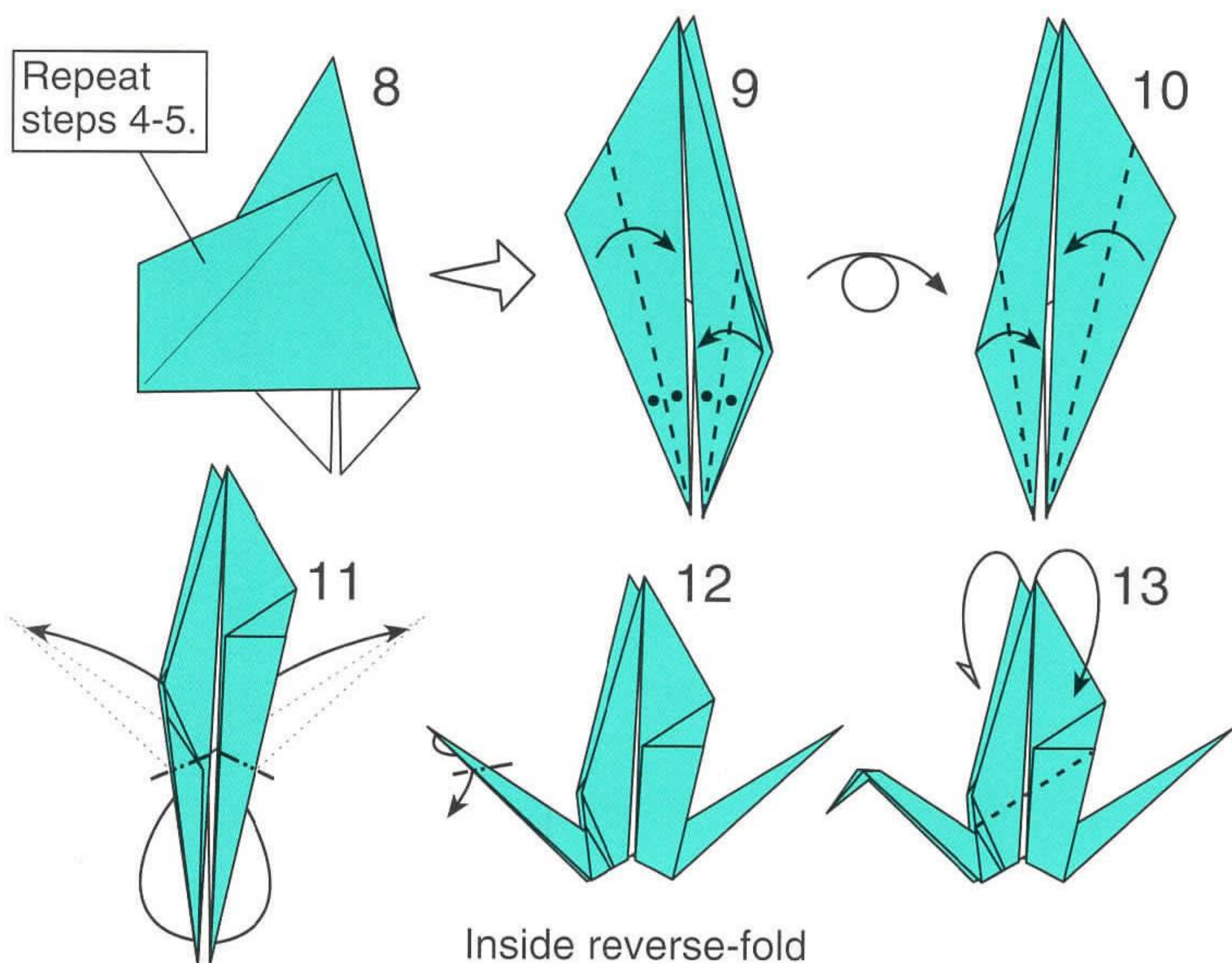
Orizuru Transformation

Theme: Geometry

Fold using 6" (15 cm) origami paper.

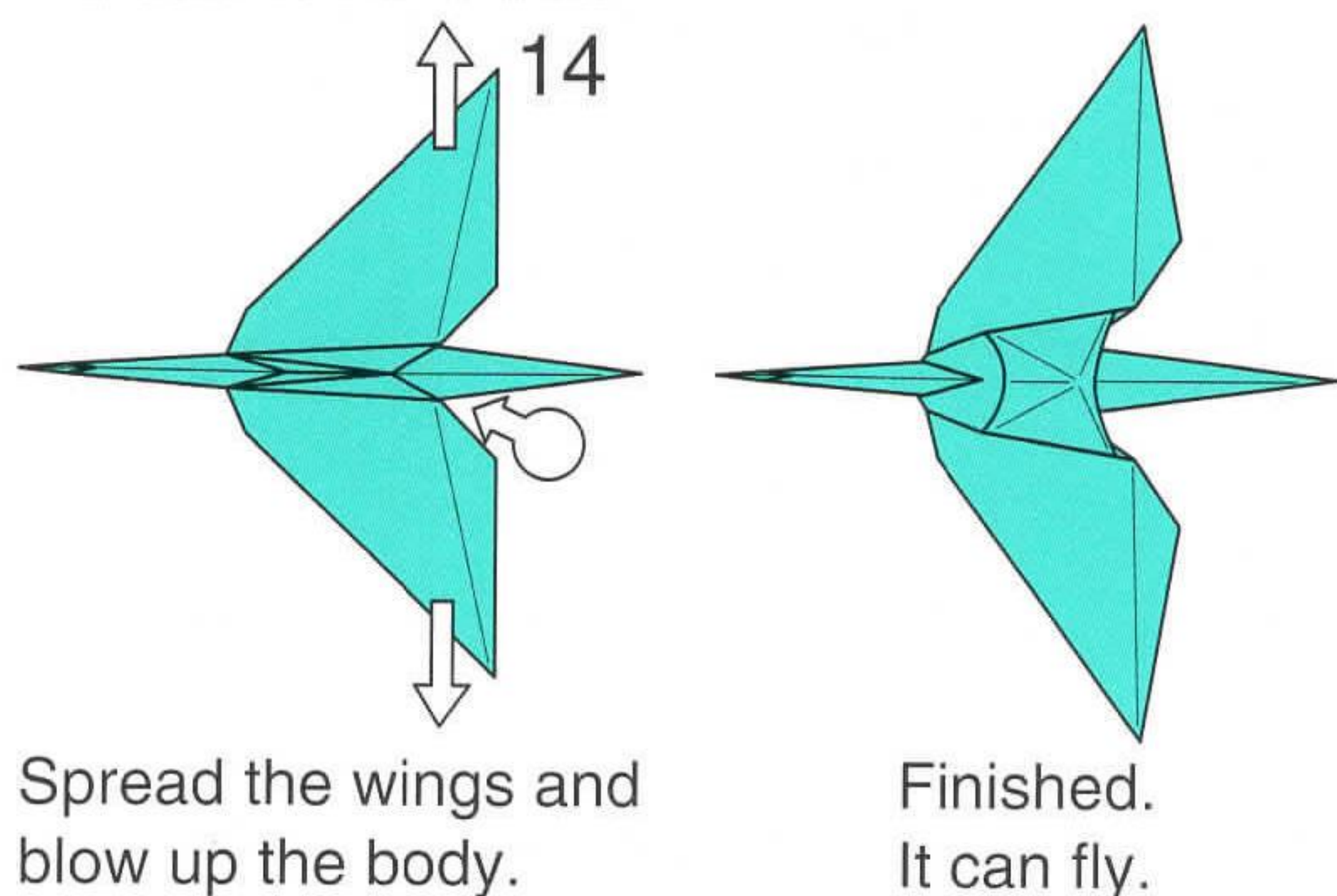


Repeat steps 4-5.



Inside reverse-fold

Inside reverse-fold



Spread the wings and blow up the body.

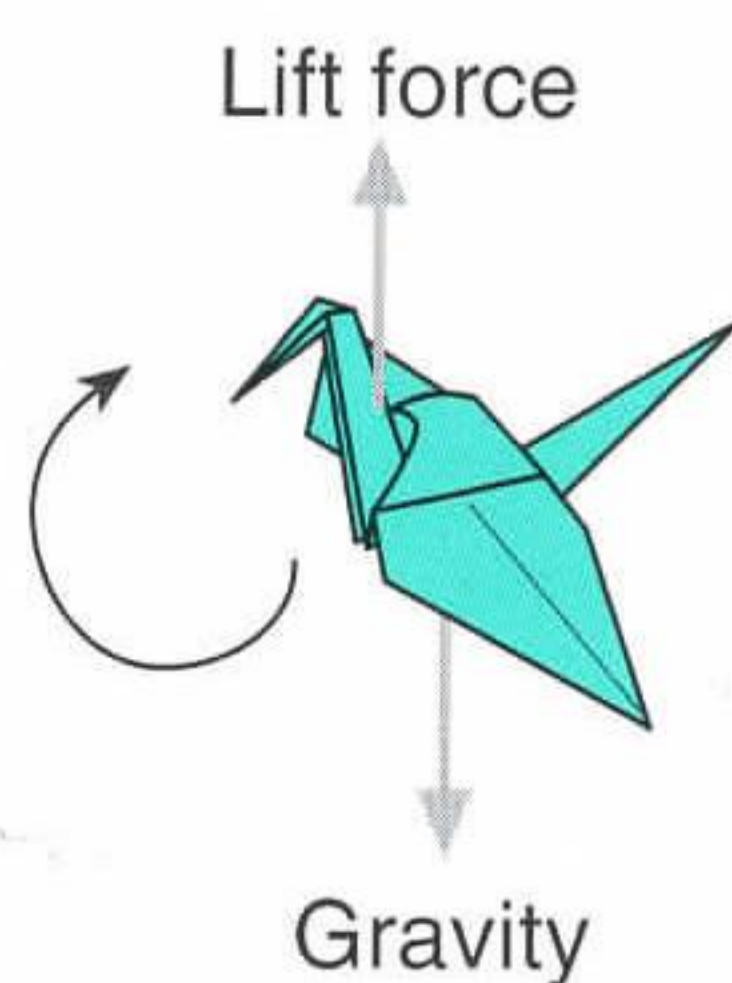
Finished.
It can fly.

Tips: How to fold neatly (Part 3)

If you bisect the angles accurately in the steps 9 and 10, you will obtain $1/8$ of a right angle or 11.25° . Good folders, however, leave a tiny gap between the edges, while making a sharp point at the tip, to avoid interference of paper at the inside reverse folds of the step 11. Origami masters will make such fine tuning almost spontaneously. They adjust folds according to thickness of paper while considering the ideal geometric form.

Make an Orizuru that can fly

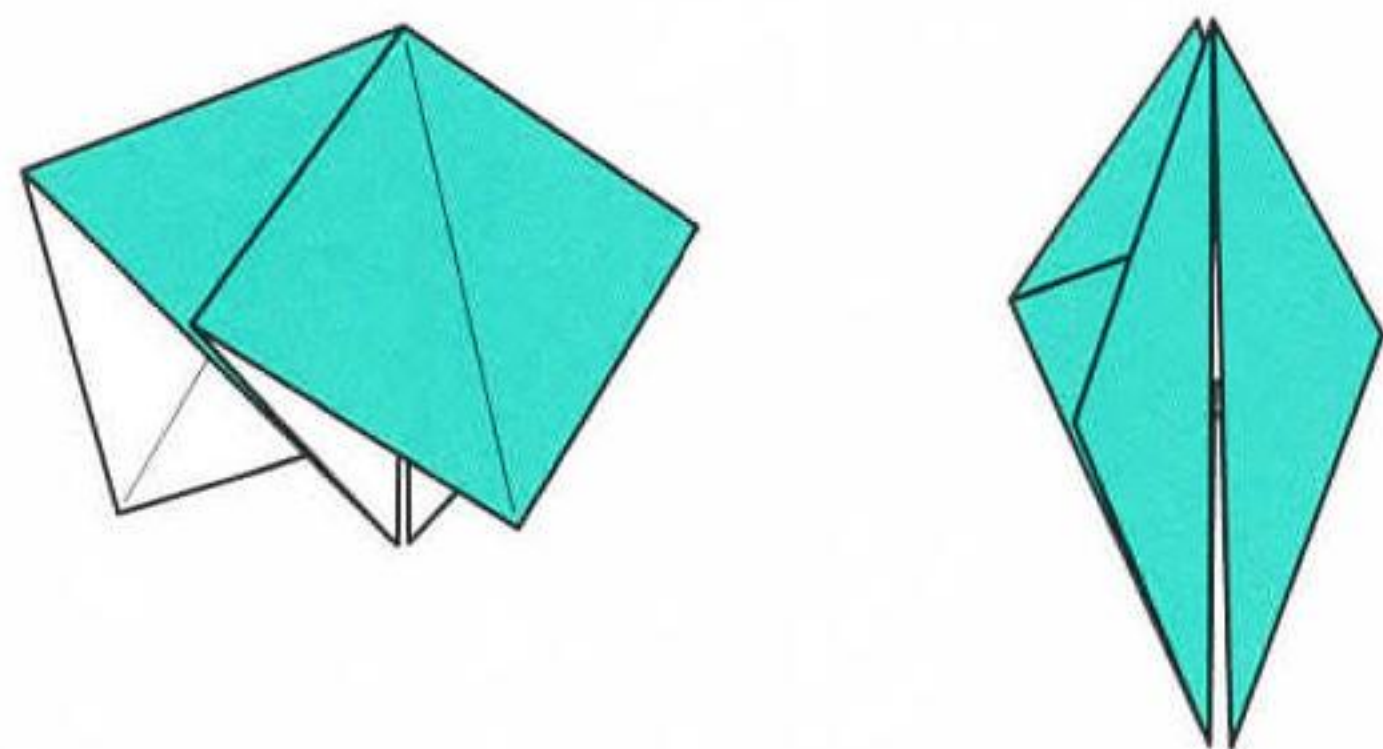
To make a traditional *Orizuru* or *Crane*, we start from a Bird base (see *Partitioned Box*) and fold as indicated in steps 9-14. But it will not fly like a paper airplane, despite of the lyrics of a popular song of '70s, *Orizuru* written by Kazumi Yasui and sung by Hiroko Chiba, that says, "fly an orizuru." It will turn upward because its center of gravity is behind the center of lift force. To be able to fly, an orizuru must have a heavier head, or sweepback wings as this model has. This transformed orizuru can fly.



An arrow with a circle as in step 14 indicates to blow up. Although you do not have to blow in this case, blowing into an orizuru has some magical meaning, according to one theory.

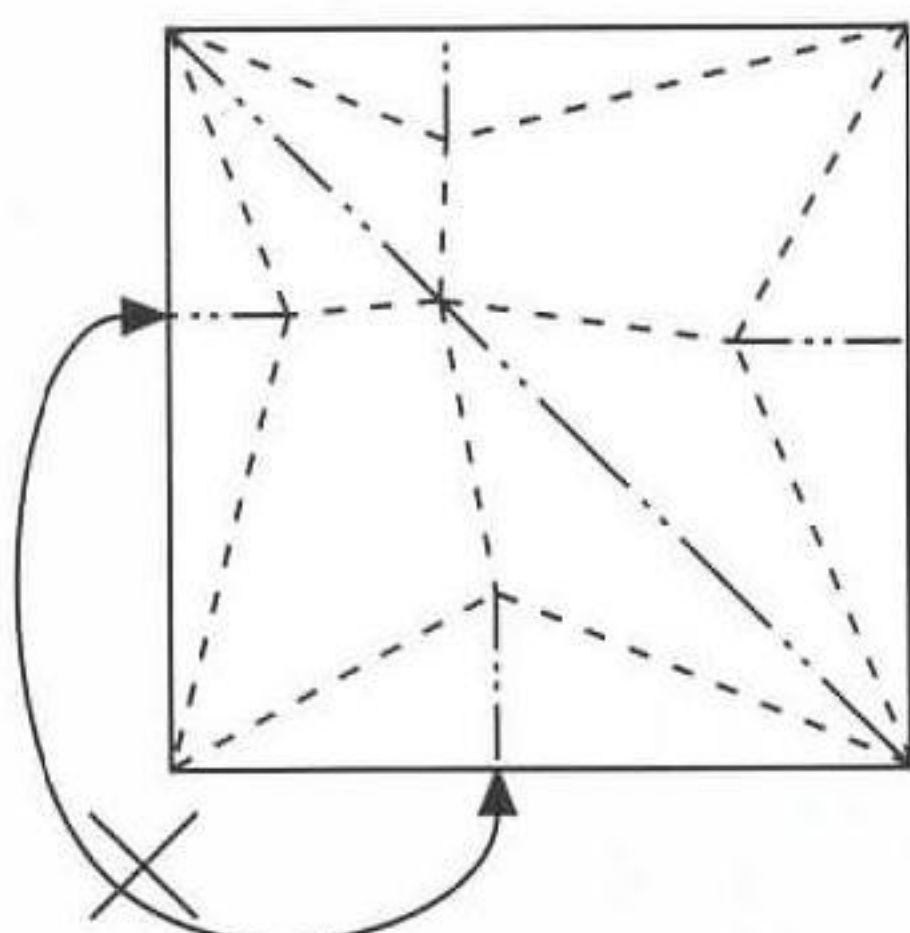
Geometry of Orizuru Transformation

In this section, I will explain the geometry of *Orizuru Transformation* referring to studies by Kodi Husimi, Jacques Justin, Toshiyuki Meguro, Toshikazu Kawasaki, and others.



You have squash-folded asymmetrically in the step 3 of this model, whereas you fold to make a square in a regular orizuru. You can squash-fold at an arbitrary angle, not only the angle specified. Moreover, you can fold in a different angle on each side, as shown on the left.

This transformation does not prevent to complete an orizuru because the transformed Bird base has the same property as the regular one. Because the base has no loose raw edge, all of the outside surface of the base is covered by one side of paper, and all of the inside covered by the other side. This property is called one-sidedness, as coined by Kodi Husimi. Also important is that the base of a wing is a single straight line. The crease pattern on the right will not make a transformed orizuru because the base of a wing will be split in two lines.

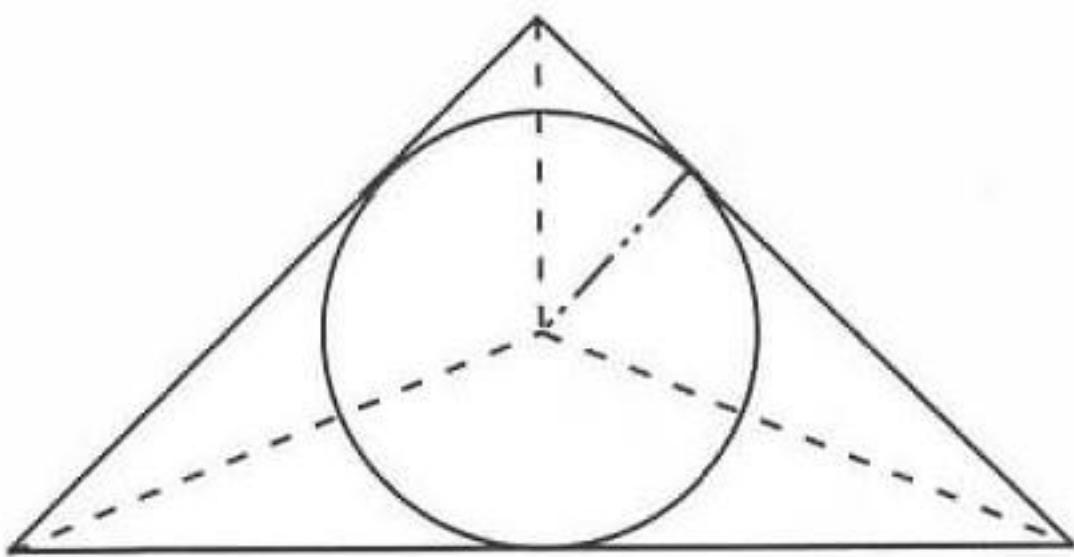
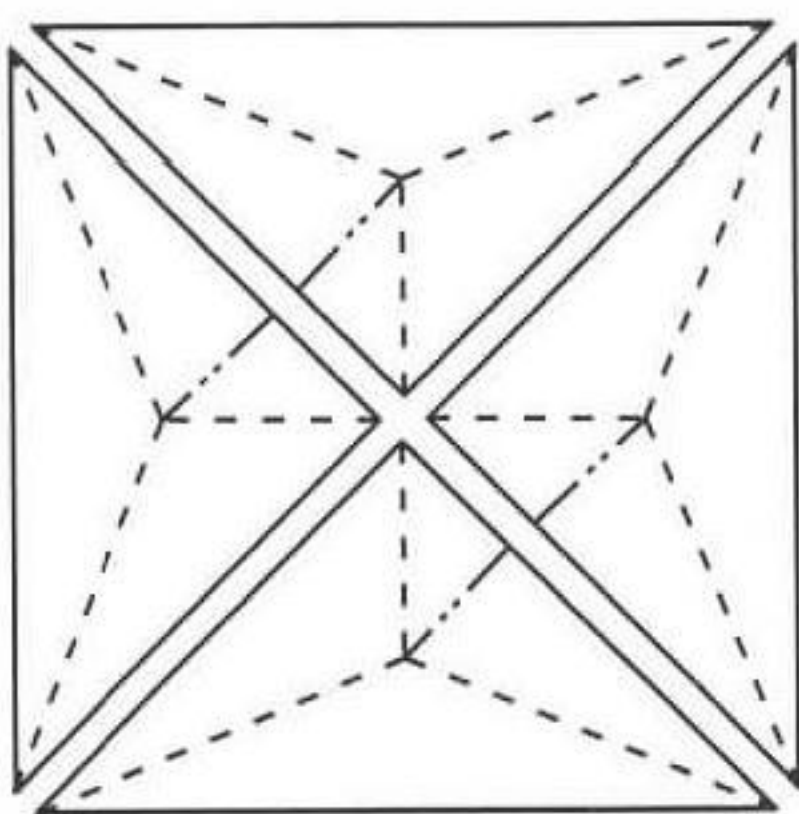


They will not match.

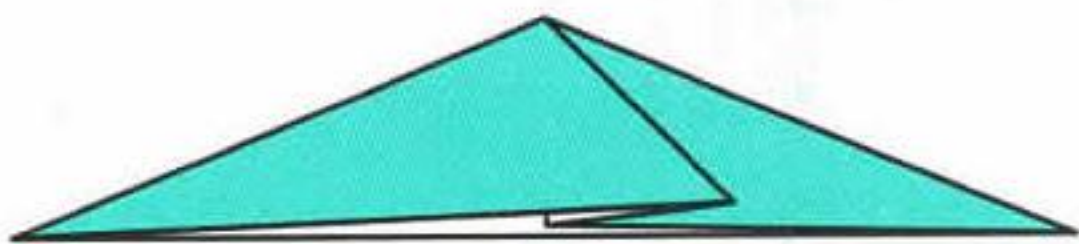
Then, what is the basic feature of the Bird base?

As we have seen in **Bases** (see *Squirrel*), a Bird base is composed of four rabbit-ear-folded isosceles right triangles, as shown on the right.

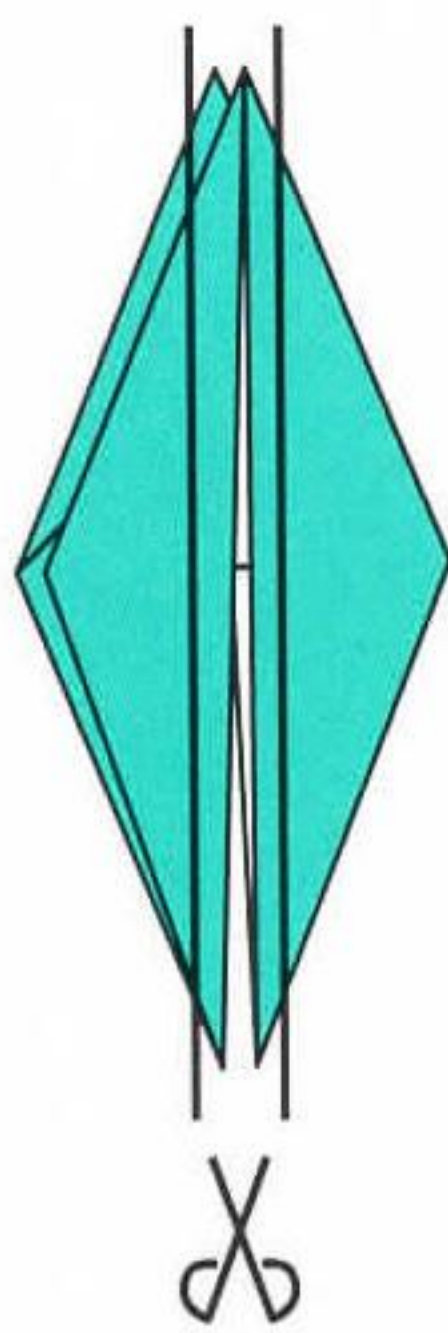
A rabbit ear fold is possible because three bisectors of angles on a triangle intersect each other at one point. The point is the **inner center**, or the center of the inscribed circle, of the triangle.



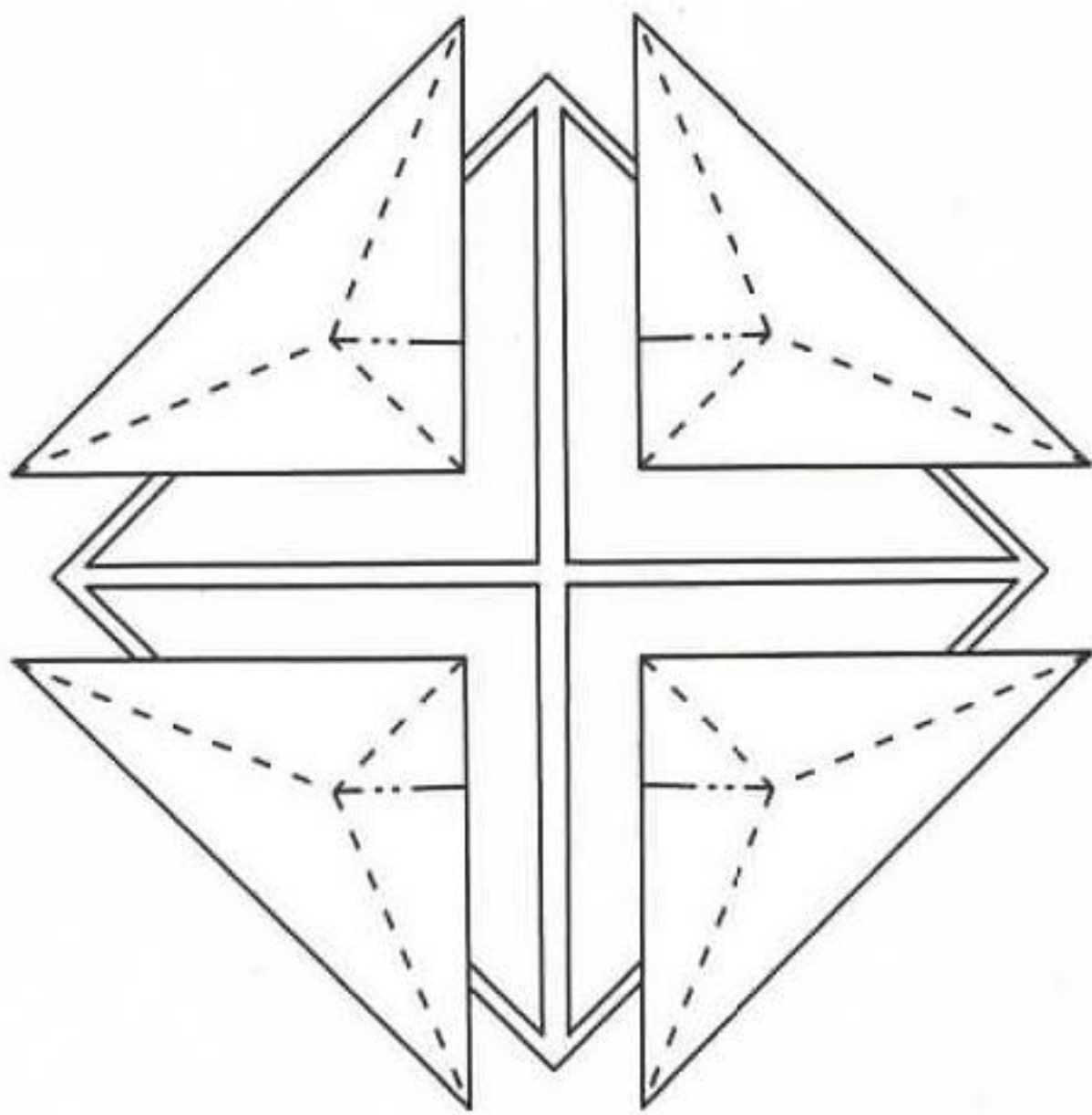
The inner center of a triangle



A rabbit ear fold



Cut.



Unfold.

Divide a regular Bird base into its basic units.

All of three edges of a triangle will be aligned with a rabbit ear fold. A Bird base has four rabbit ear folds, and all of their edges also align. Toshiyuki Meguro has demonstrated this alignment clearly in an interesting way.

Imagine you cut a Bird base along its “center line” that has some thickness. In practice, you are going to cut twice, as shown on the right, instead of cutting once with thick scissors.

When you unfold the divided parts, you will find that the square is divided into four rabbit ear folds. Remember the remaining frame, which consists of four edges and two diagonals of the square, was a single line in the Bird base.

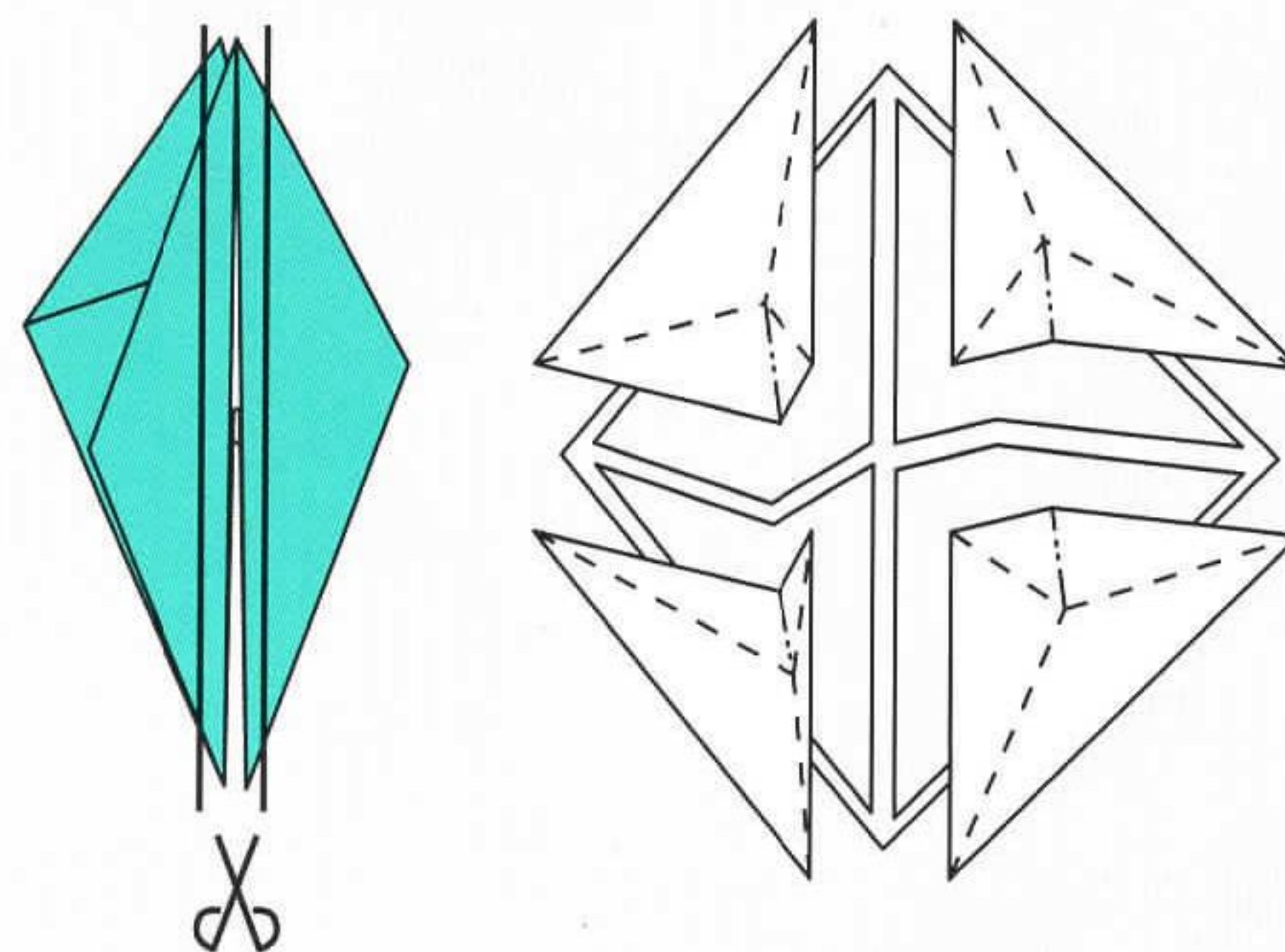
Whereas a regular Bird base consists of triangles, each of which are rabbit-ear- folded, the base of *Orizuru Transformation* consists of kite-shaped quadrangles. When I realized that each unit can be a combination of two arbitrary triangles, I still thought the units are basically triangles and called the transformation of orizuru “Tri-inner-center theorem.” But cutting a transformed Bird base along its center line reveals its essence clearly.

As you can see on the right, a base will be divided into quadrangles. And it is no surprise.

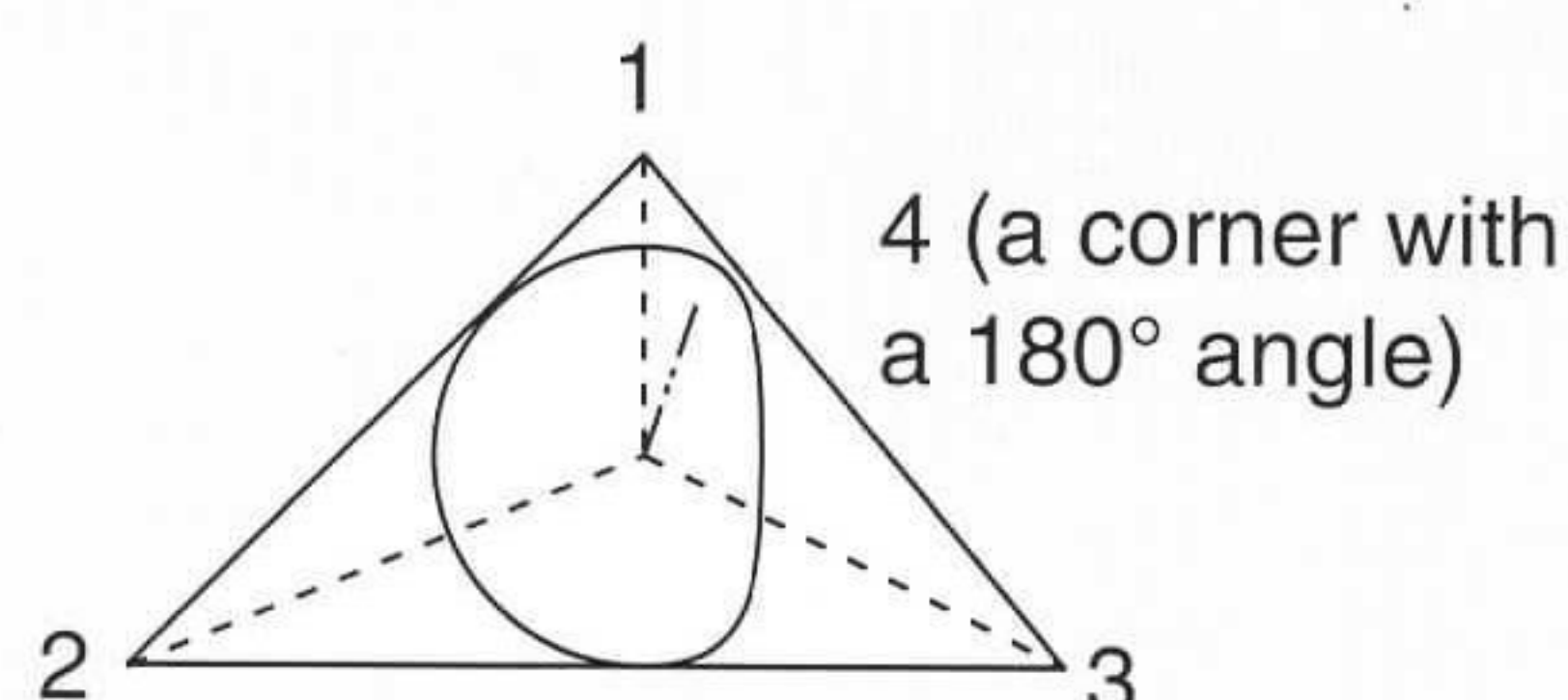
Even when you rabbit-ear-fold a triangle, you need one extra crease that is perpendicular to a side, besides three bisectors, to fold it flat. We can see the intersection of the crease and the side (the foot of the perpendicular) as fourth corner of a quadrangle, a corner with a 180° angle. Then, the Bird base consists of quadrangles, not triangles. Not all quadrangles, however, can be a unit. Four creases on a quadrangle will align the sides only if the quadrangle has an inscribed circle. If not, we need more than four creases to fold so that the sides align.

In fact, we have rabbit-ear-folded a quadrangle at the step 13 of Mouse, the first model of this book. By the way, a concave quadrangle can have an inscribed circle if the circle is tangent to two sides and two extended lines of the other sides.

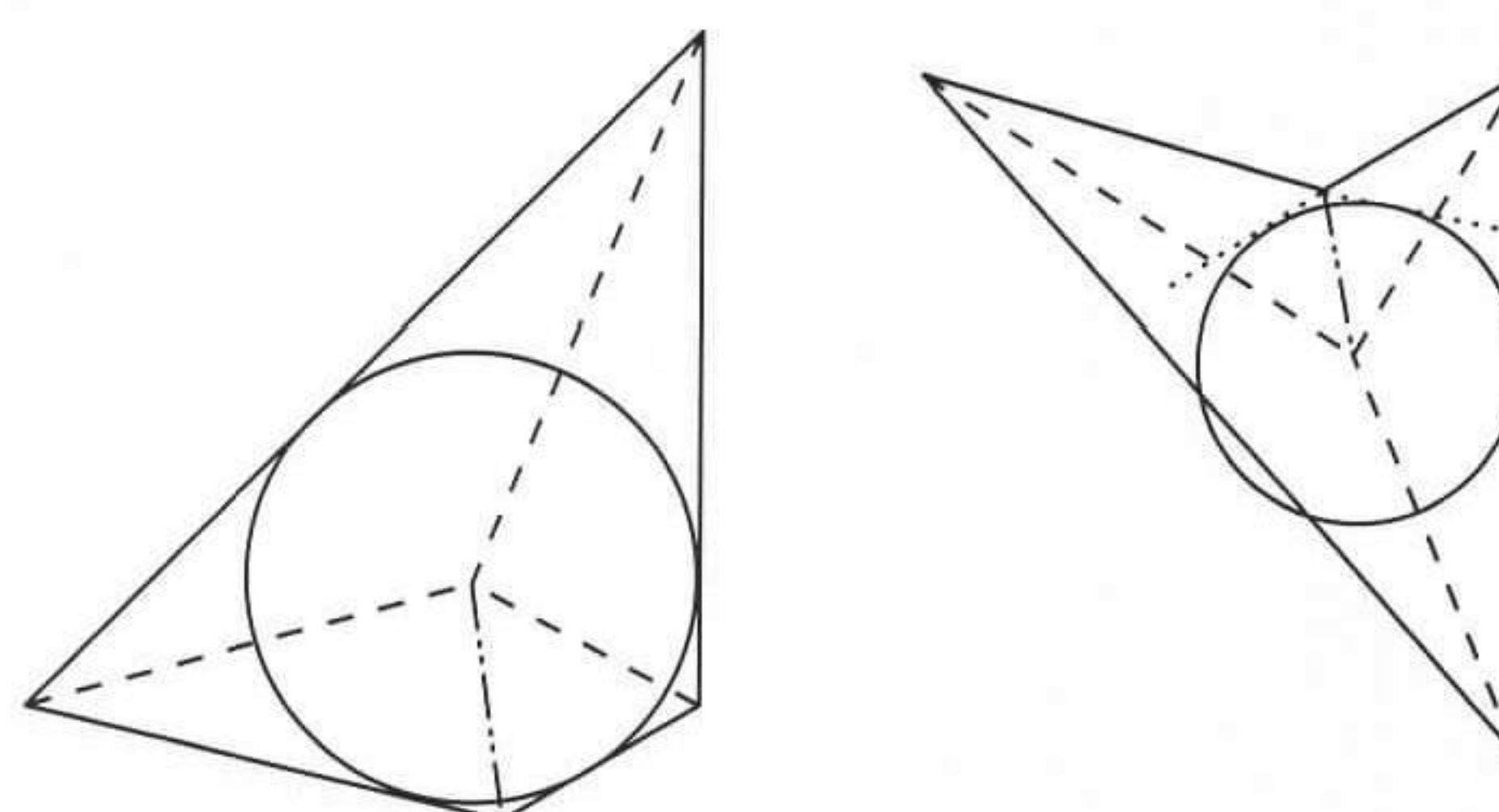
Though I did not explain here in detail, the original shape of paper can be any quadrangle, not only a square, as long as it has an inscribed circle. Toshikazu Kawasaki has proved that any quadrangle that has an inscribed circle can be divided into four quadrangles, each of which has also an inscribed circle, which can be folded to make an orizuru.



Divide a transformed Bird base into units.



In fact, a unit has four corners, hence it is a quadrangle.



A quadrangle can be rabbit-ear- folded if it has an inscribed circle.

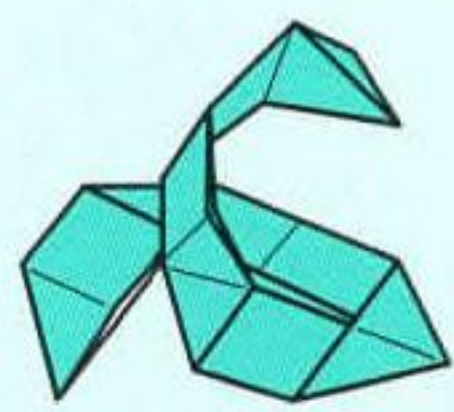
I have explained, in some detail, the transformation of orizuru that exemplifies the close relationship between origami and geometry. *Orizuru Transformation* is “fundamental” as an origami model, but its implication is by no means “fundamental.”

In other words, even a simple model conceals geometry in it. Making an origami model is a mathematical experience, even if you do not realize it.

One of the keywords here is one-sidedness. That means, when you make a Bird base, you are dividing the two sides of paper into the inside and the outside.

An avant-garde artist Genpei Akasegawa once created a can labeled inside and titled it *Canned Universe*. With this art-work, he inverted the inside and the outside, wrapping up the whole universe, except the volume of the can, “in” the can.

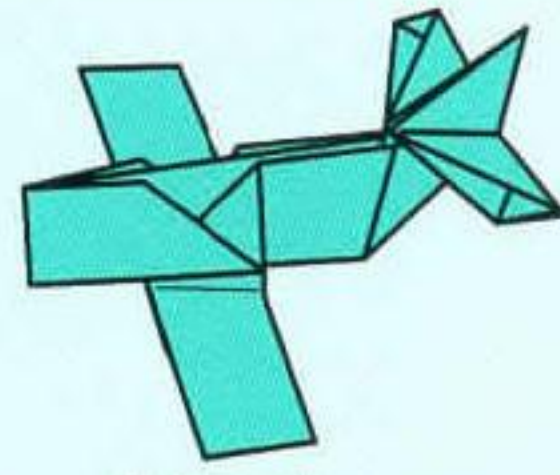
You can do the same thing with orizuru. If you make a Bird base starting with colored side up, you make a Bird base that contain the whole universe inside.



Snake

Theme: Box pleating

An example of model that is based on box-pleating or square-grid creases. This model is “longer” than the diagonal of the original square.



Airplane

Theme: Repeat on the other side

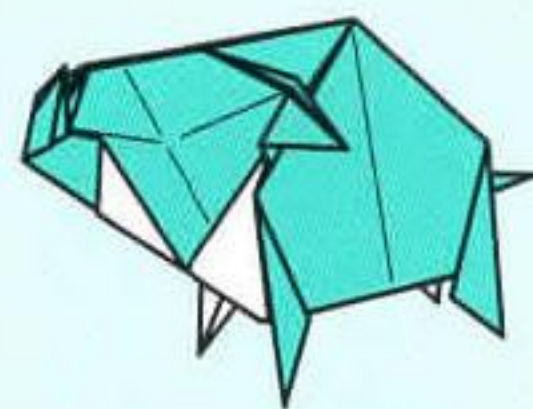
Gives you some hints about “repeat on the other side,” which is sometimes difficult to fold when following diagrams.



Samurai Helmet

Theme: Half-open

Looks into a half-open technique, which is one of the techniques to make a three-dimensional model.



Wild Boar

Theme: 22.5° and $\sqrt{2}$

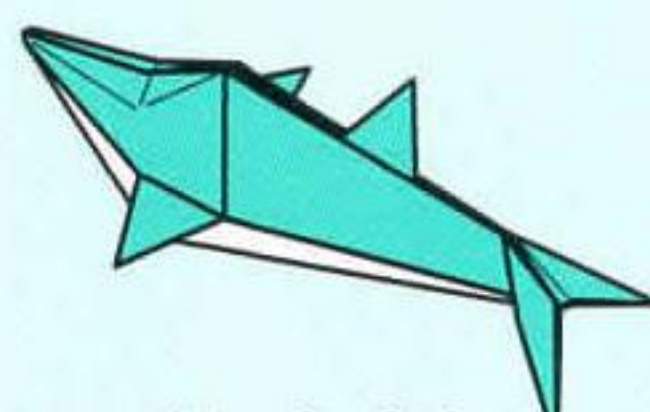
Shows significance of the 22.5° angle, which is a quarter of the right angle, and the close relation to the $\sqrt{2}$ length.

Chapter 2

Simple Models

Guest speaker: Now, that was my very simple address...

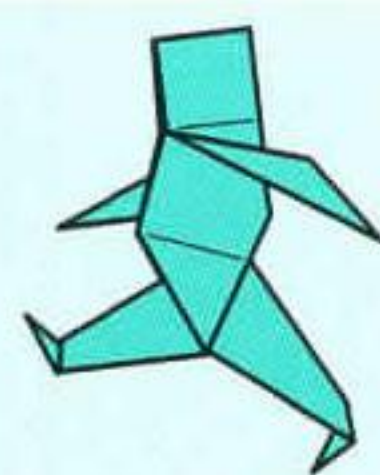
Audience: (There is nothing simple about this address.)



Dolphin

Theme: Shaping

Looks into shaping, which is another technique to make a three-dimensional model.



Human Figure

Theme: Crease pattern

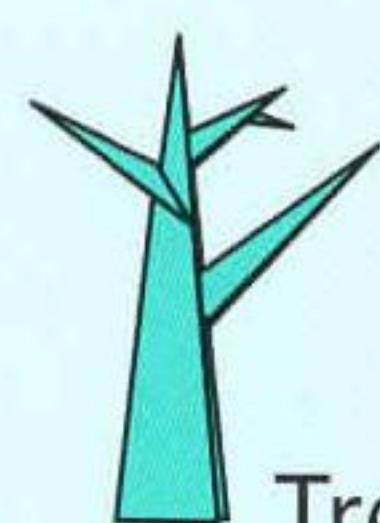
Looks into the crease pattern, which is the interesting pattern of creases observed when unfolding completely the paper.



Japanese Macaque

Theme: Crease pattern fold

Explains a fairly complex sink fold that can be folded easily with the understanding of the crease pattern.



Tree

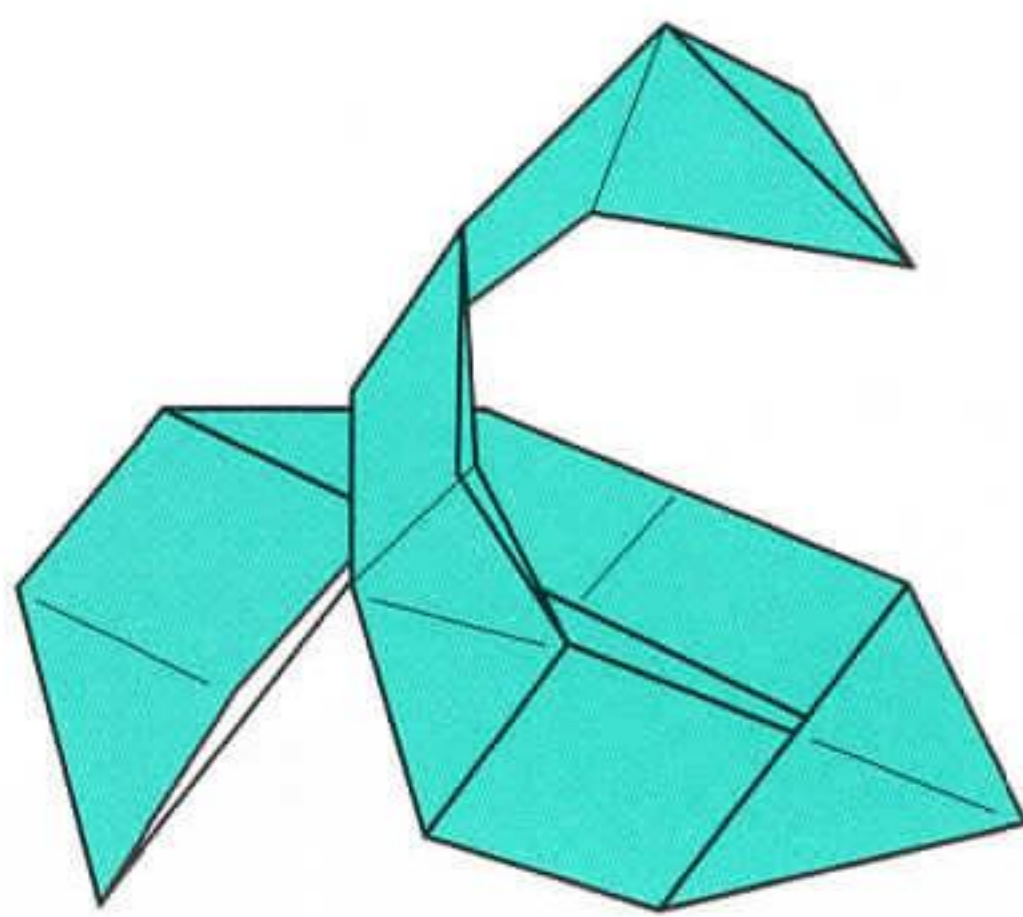
Theme: Theorem

Shows a couple of geometric theorems about flat-foldable crease patterns.

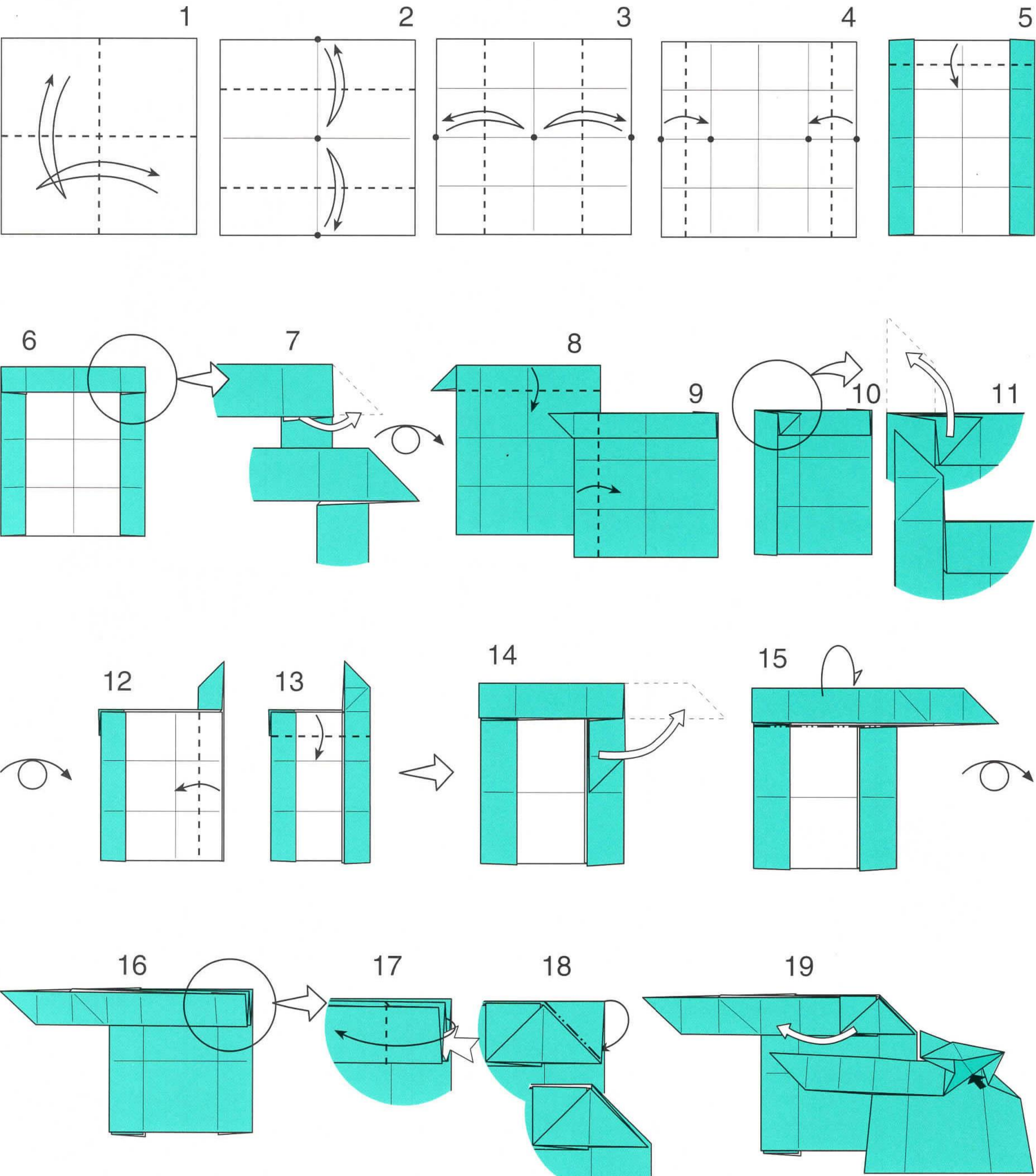
Snake

Theme: Box pleating

Fold using 6" (15 cm) origami paper.

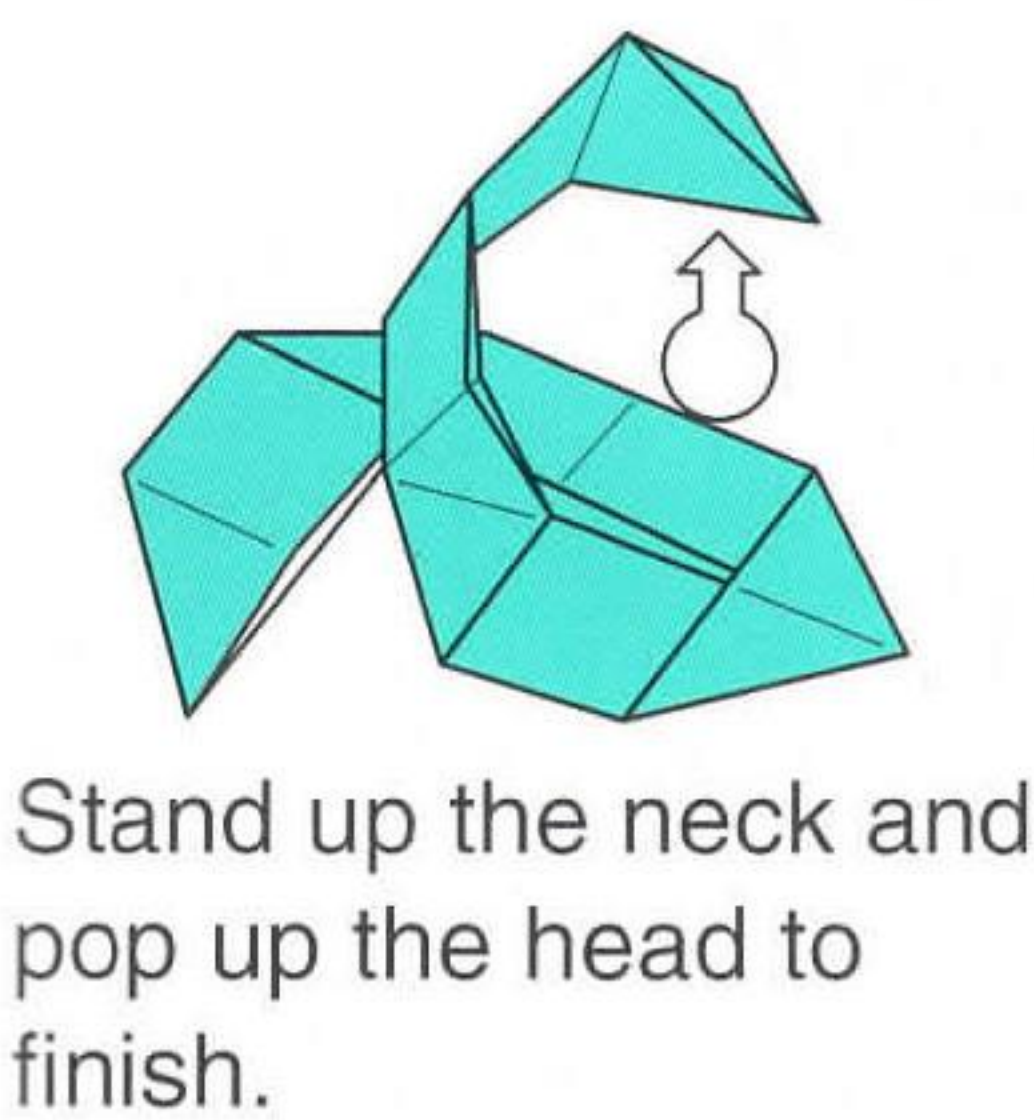
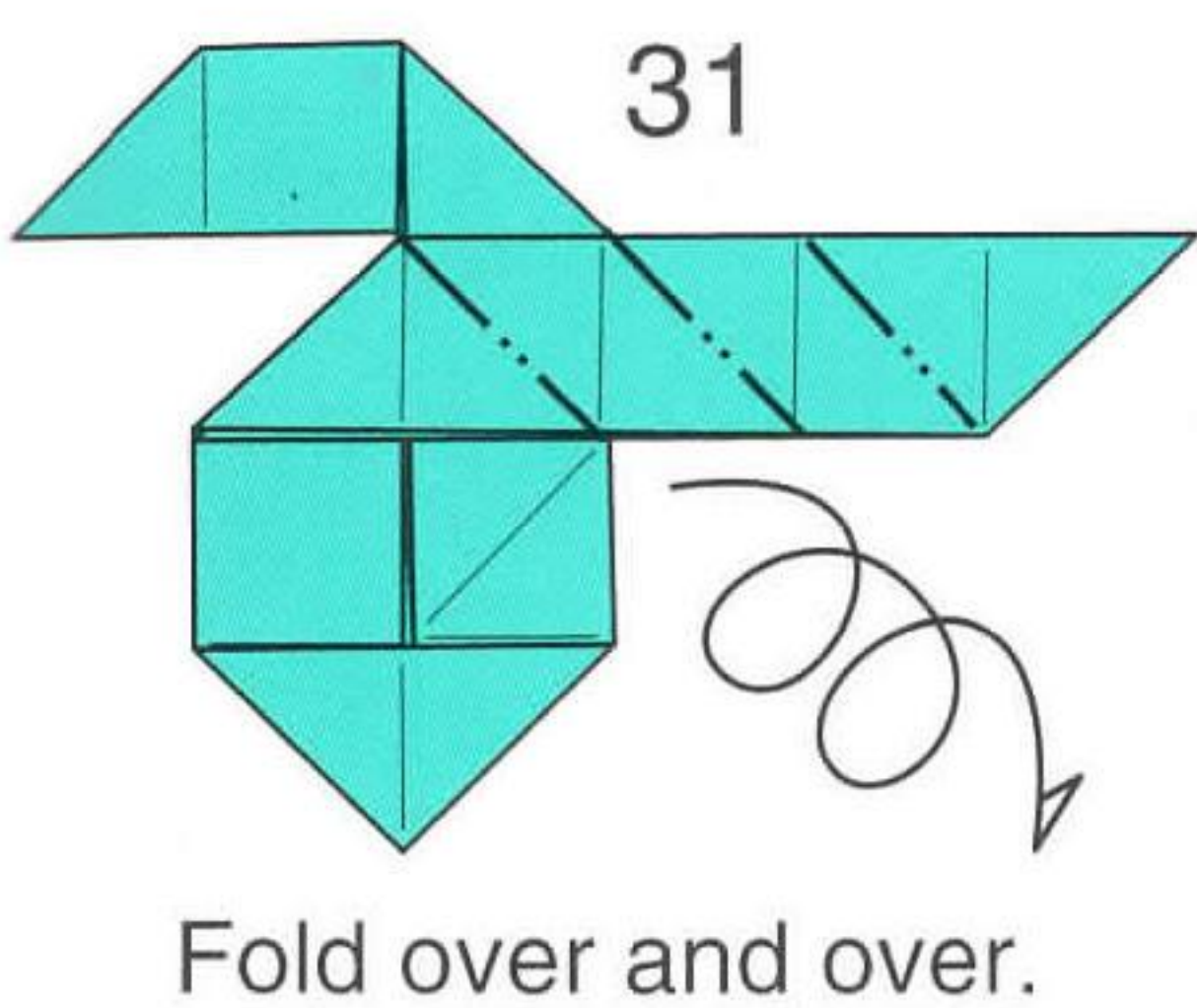
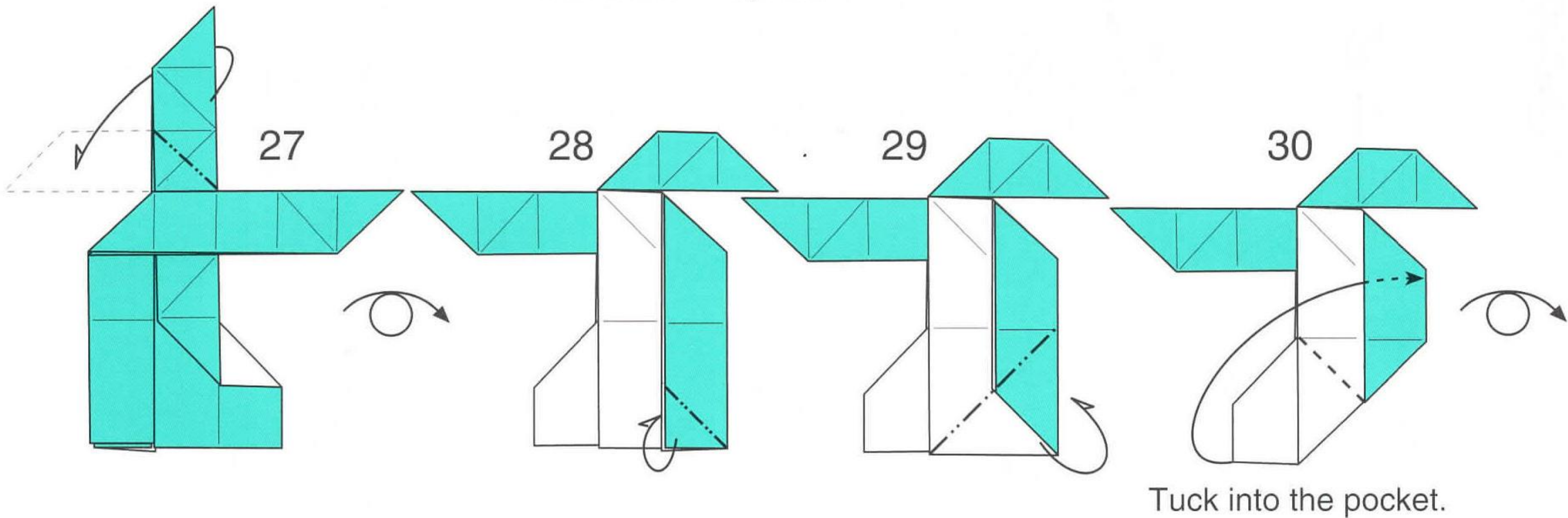
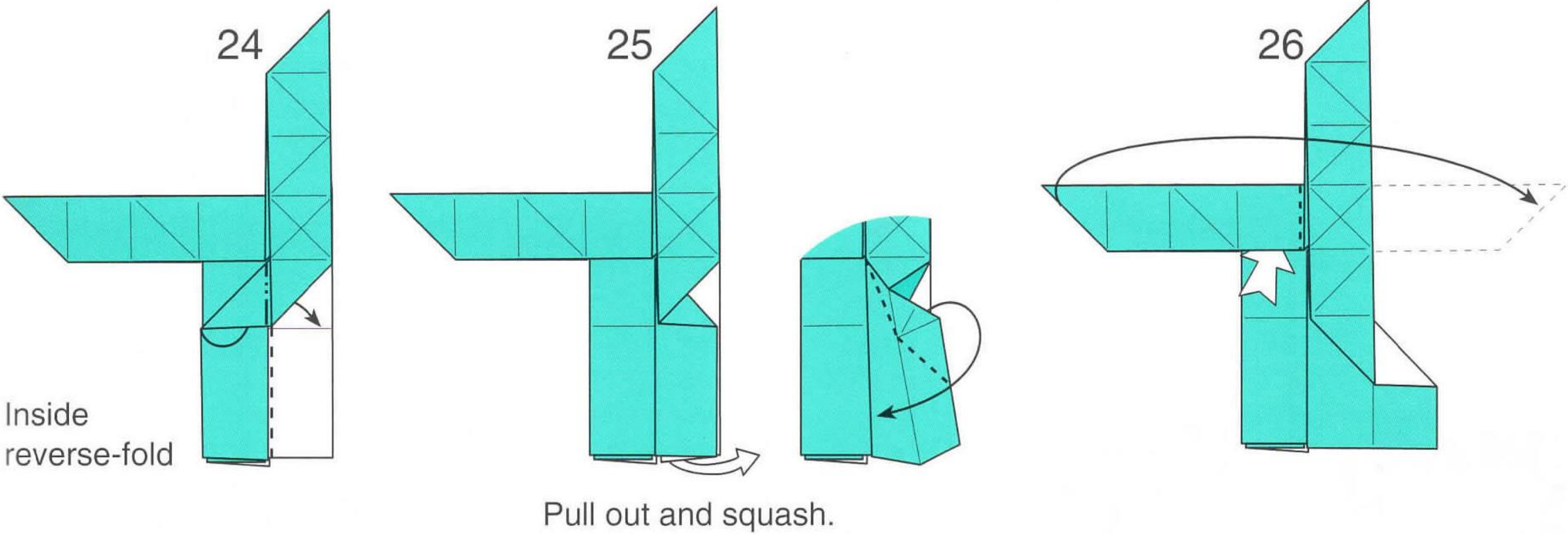
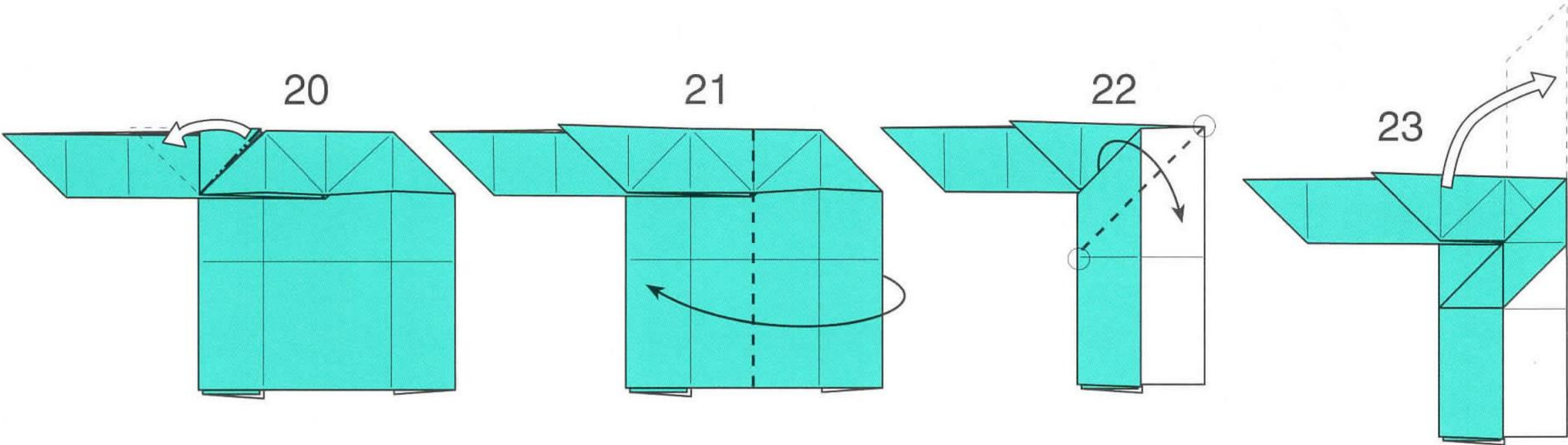


This snake is "longer" than the diagonal of the square. I got the basic idea from another origami snake designed by Masao Okamura.



Inside reverse-fold

Stretch and squash to make a trapezoid.



Box Pleating

In origami, **box pleating** are folds based on a square grid. We use box pleating to design origami models mainly for one or both of the following purposes.

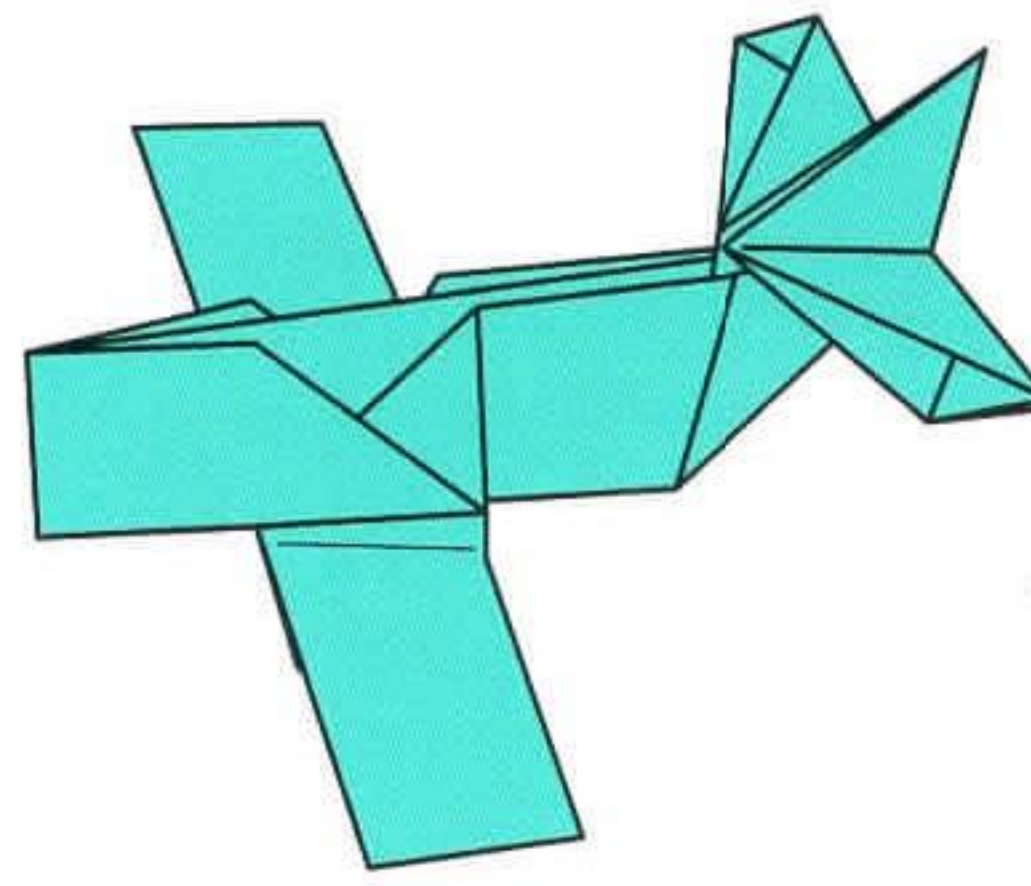
1. To isolate a point using pleats.
2. To obtain an interesting design using shades of pleats.

The use in Snake is a typical example of the former. An example of the latter is that of Peacock in **Complex Models**. Among the techniques (or structures) of controlling lengths of points with box pleat, the most basic fold is a squash fold to make a trapezoid, as in steps 19- 20. While this model is based on the 8 x 8 grid, much more complex design can be achieved with the 16 x 16 or finer grid.

Airplane

Theme: Repeat on the other side

Fold using 6" (15 cm) origami paper.



In step 17, you are required to repeat the previous ten steps. You may get stuck with such a long “repeat on the other side” sequence in the diagram because:

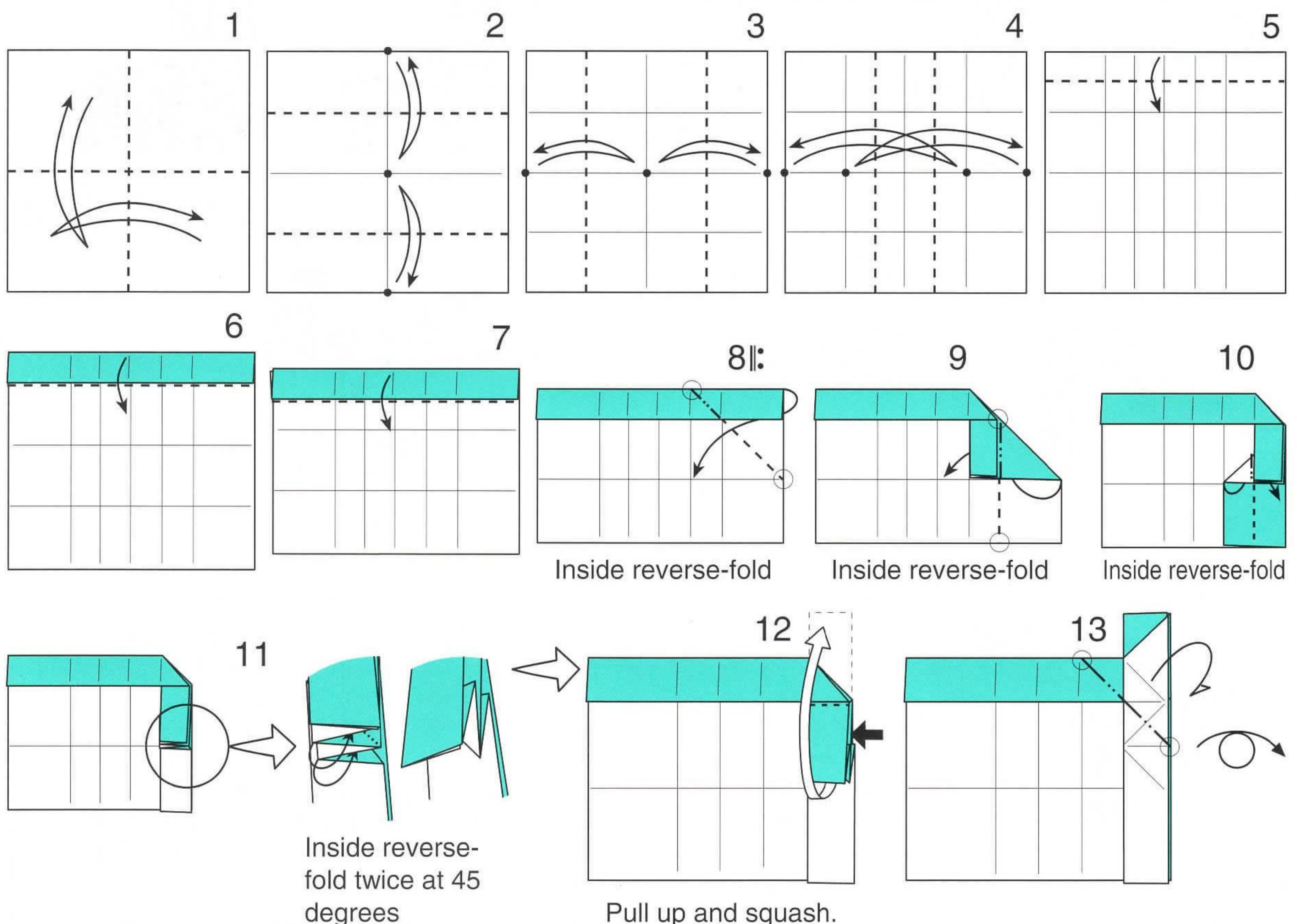
1. the sequence is not exactly the same but becomes a mirrored image, and
2. one side is already folded but the other is not, so they are not exactly mirrored images.

One can say the repeating sequence should be shown explicitly or in a smarter way in a diagram. But I challenge you to repeat a long sequence here. Some models in this book have even longer repeating sequences. Such diagrams may be unfriendly, but, in my opinion, folding based on mirrored images is a good exercise for your brain. However, I suggest two ways to manage a “repeat on the other side” sequence.

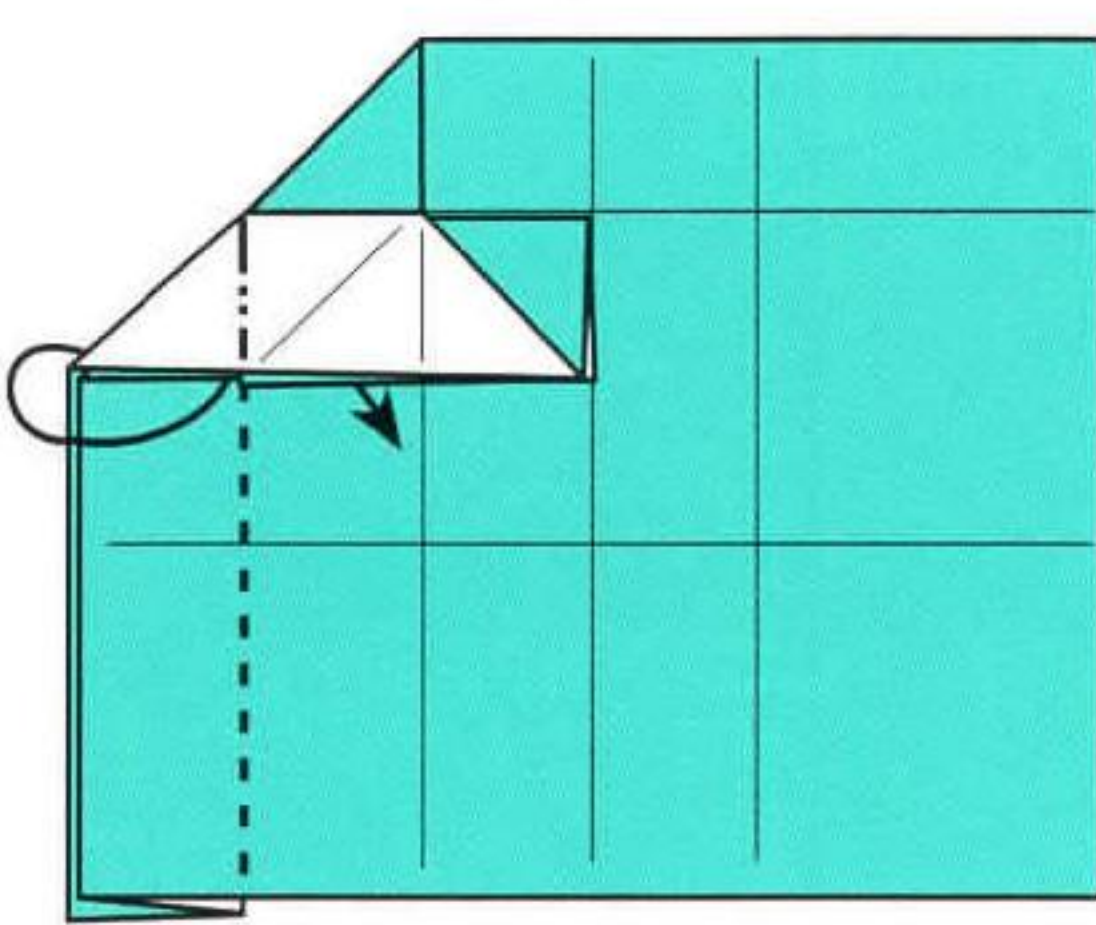
Two ways to manage a “repeat on the other side” sequence

1. Fold both sides at each step.
For example, inside reverse-fold on both sides at step 8. It is, however, sometimes impossible.
Note that I added the repeat sign used in the music notation (starts with ||: and ends with :||) for long repeating steps in this book to show you where to start and where to stop.

2. Fold and unfold on one side, then fold the other.
For example, fold through step 17, unfold back to step 7, and fold on the other side. You will fold twice on one side, once as preparation for the more difficult side, where you must fold the mirrored image. It will be much easier to fold the second time because you already have all the creases.

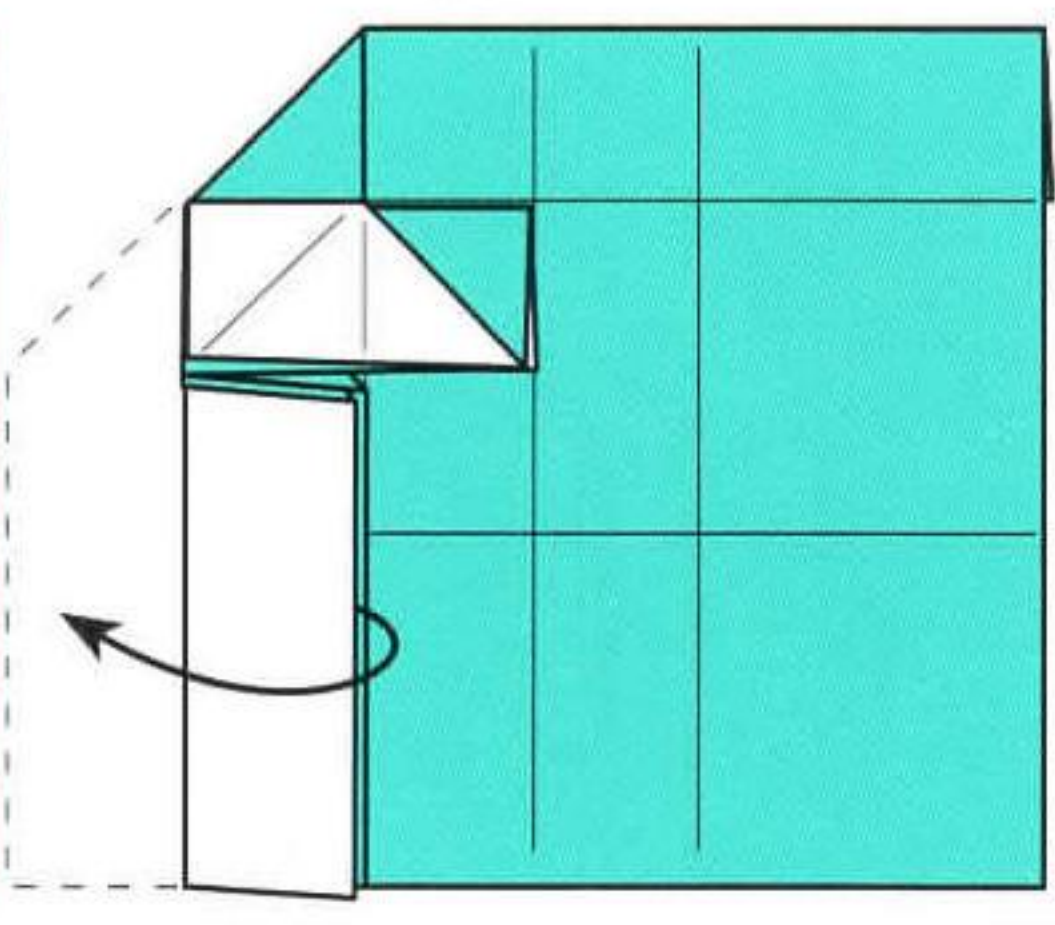


14



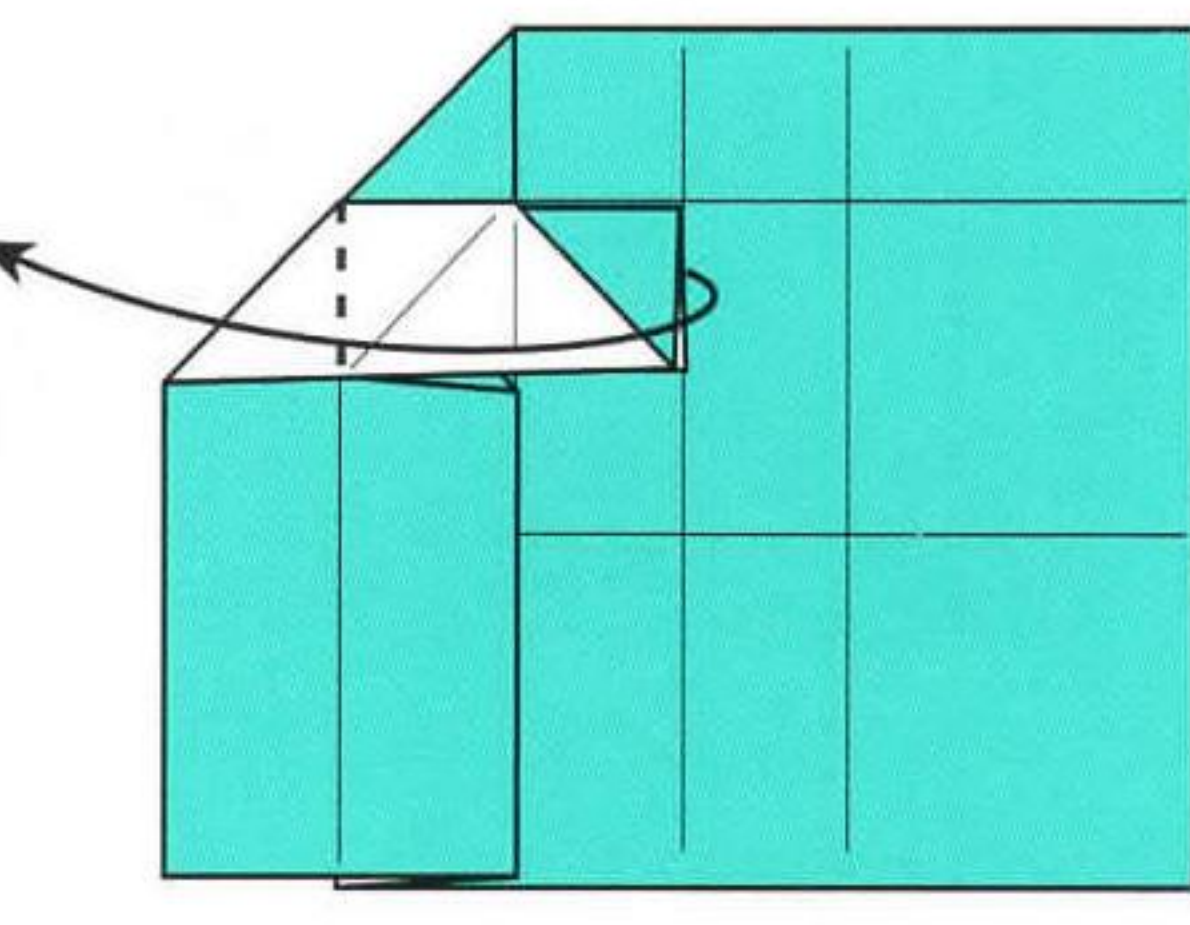
Inside reverse-fold

15

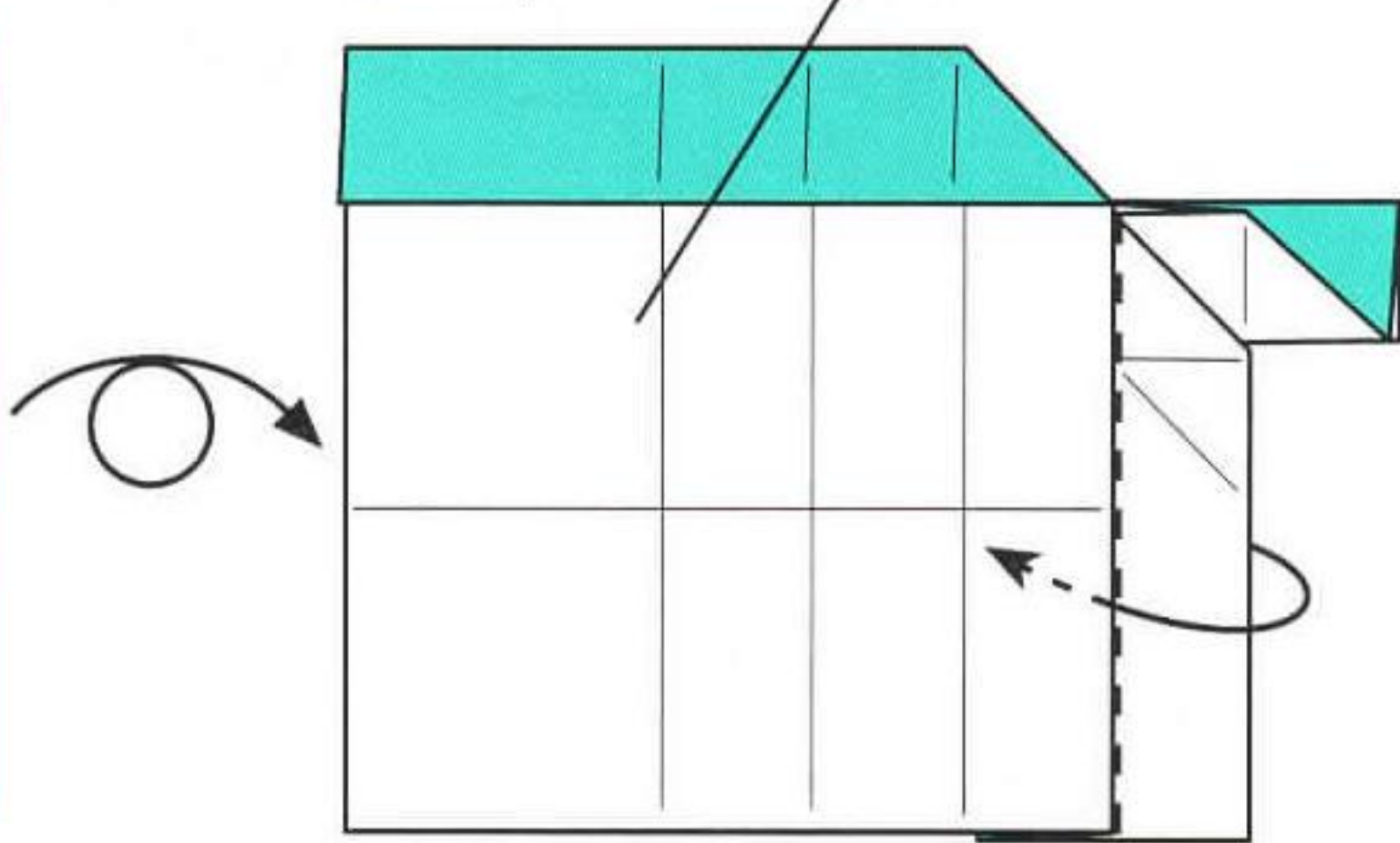


Unwrap one layer.

16



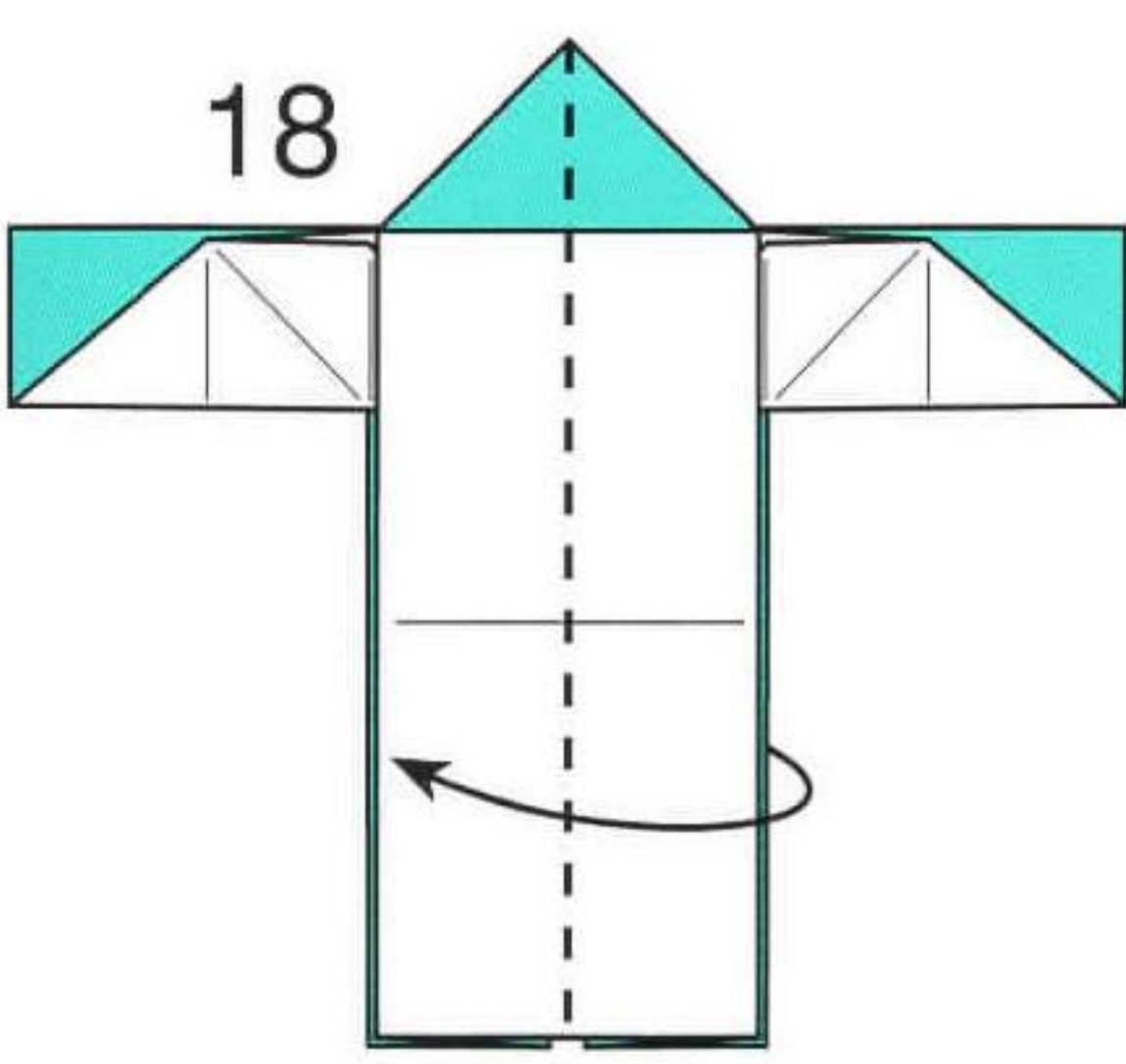
17: ||



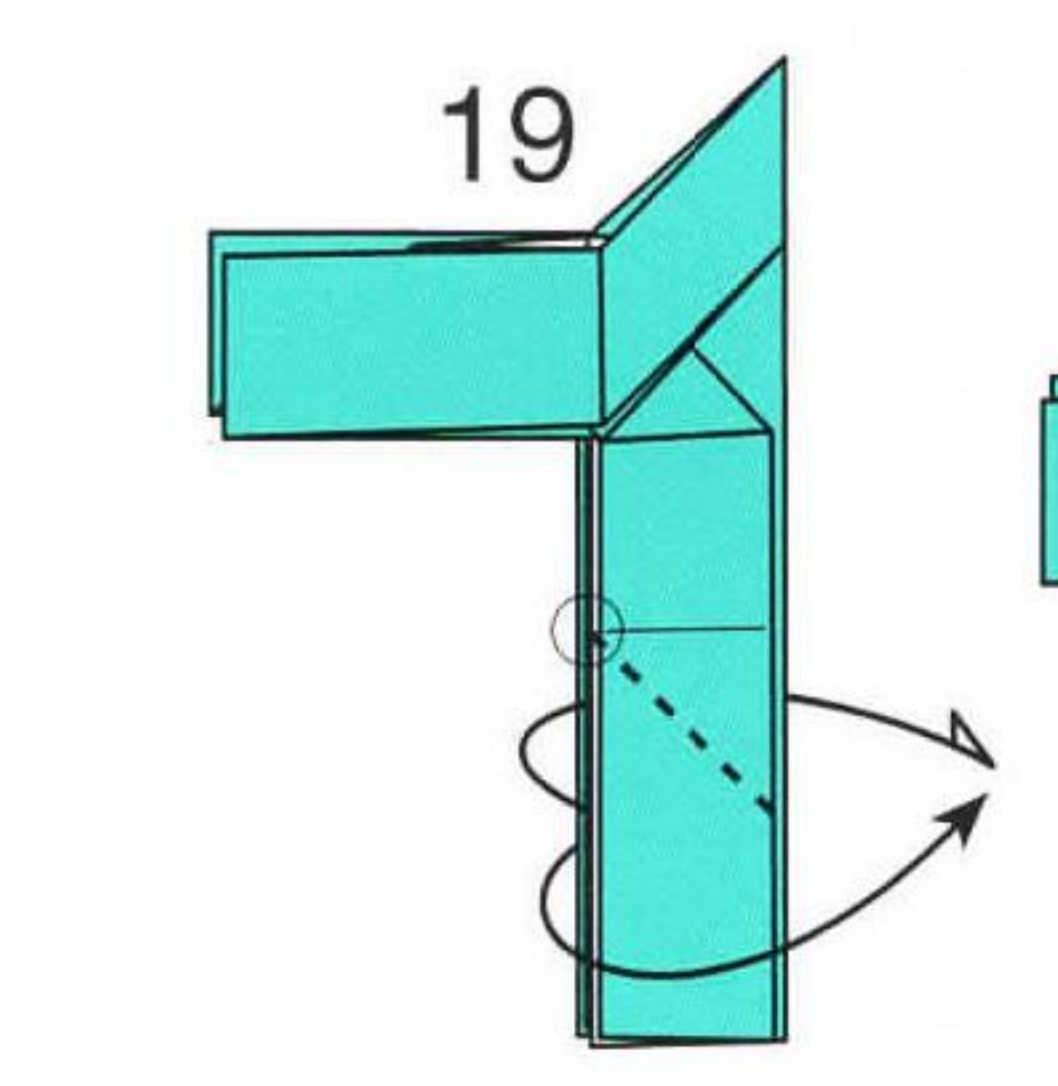
Repeat steps 8-17.

Tuck under the top layer.

18

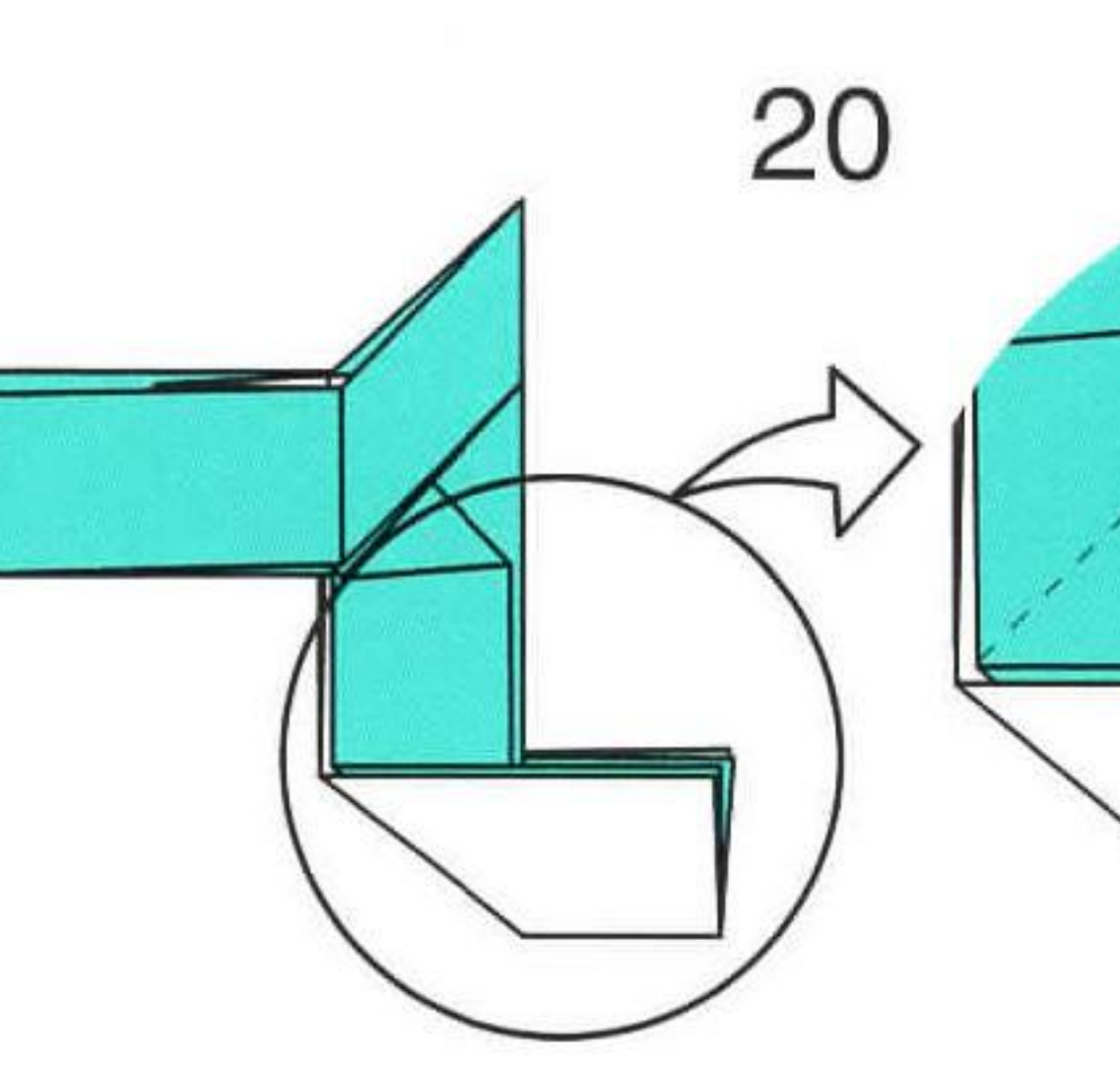


19

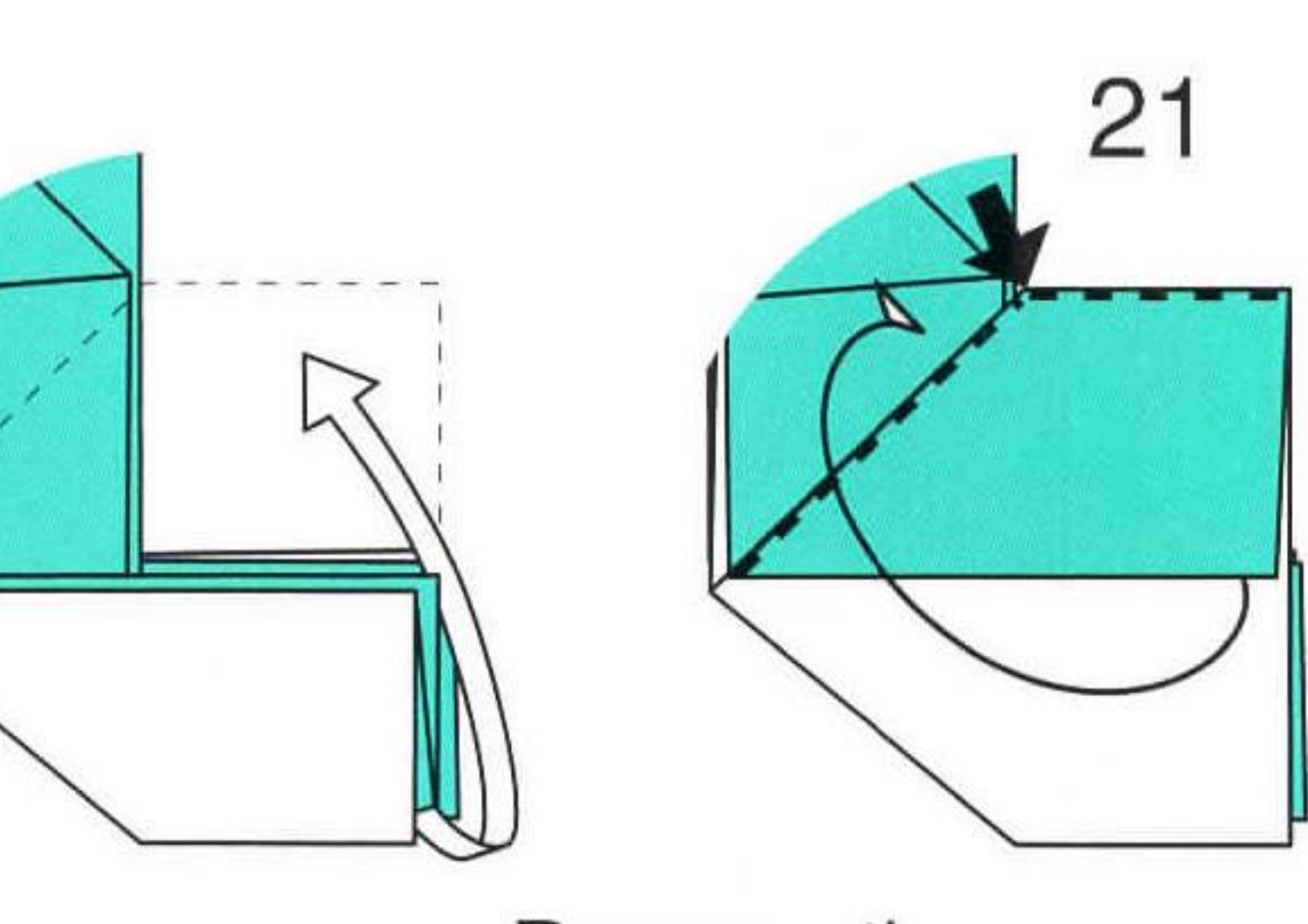


Outside reverse-fold

20

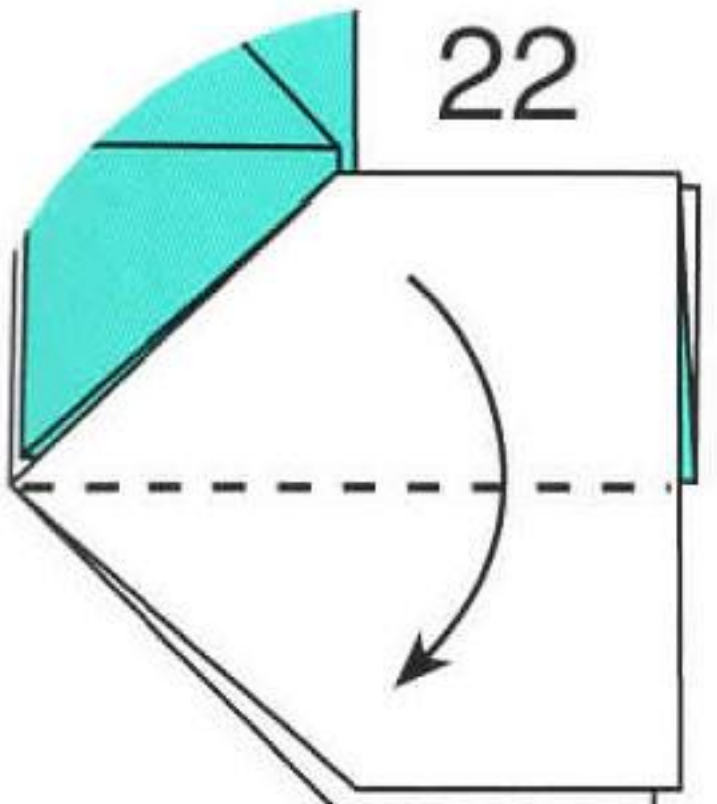


21

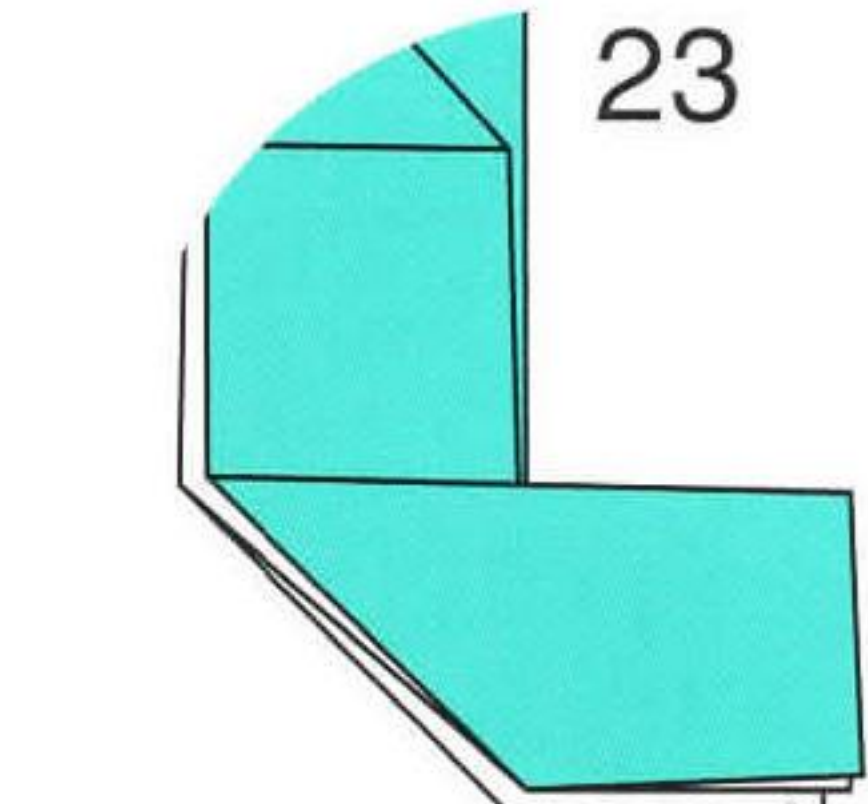


Reverse the mountain creases into valley. (You will have to slightly open the entire model.)

22

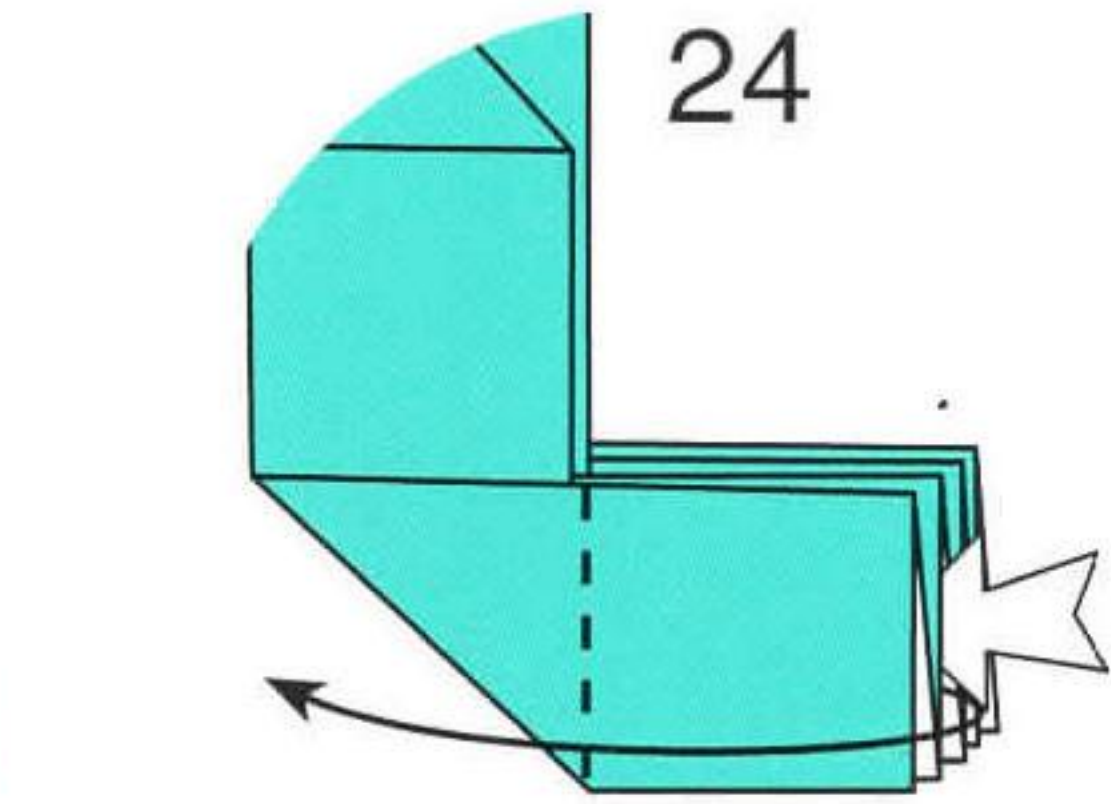


23

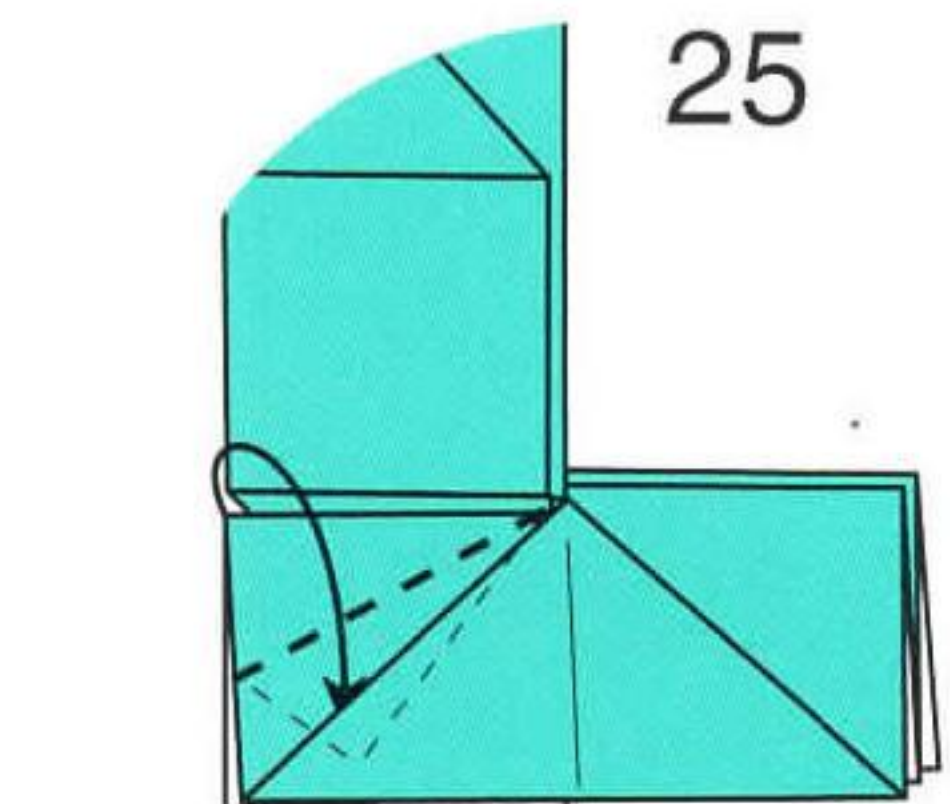


Repeat steps 20-22.

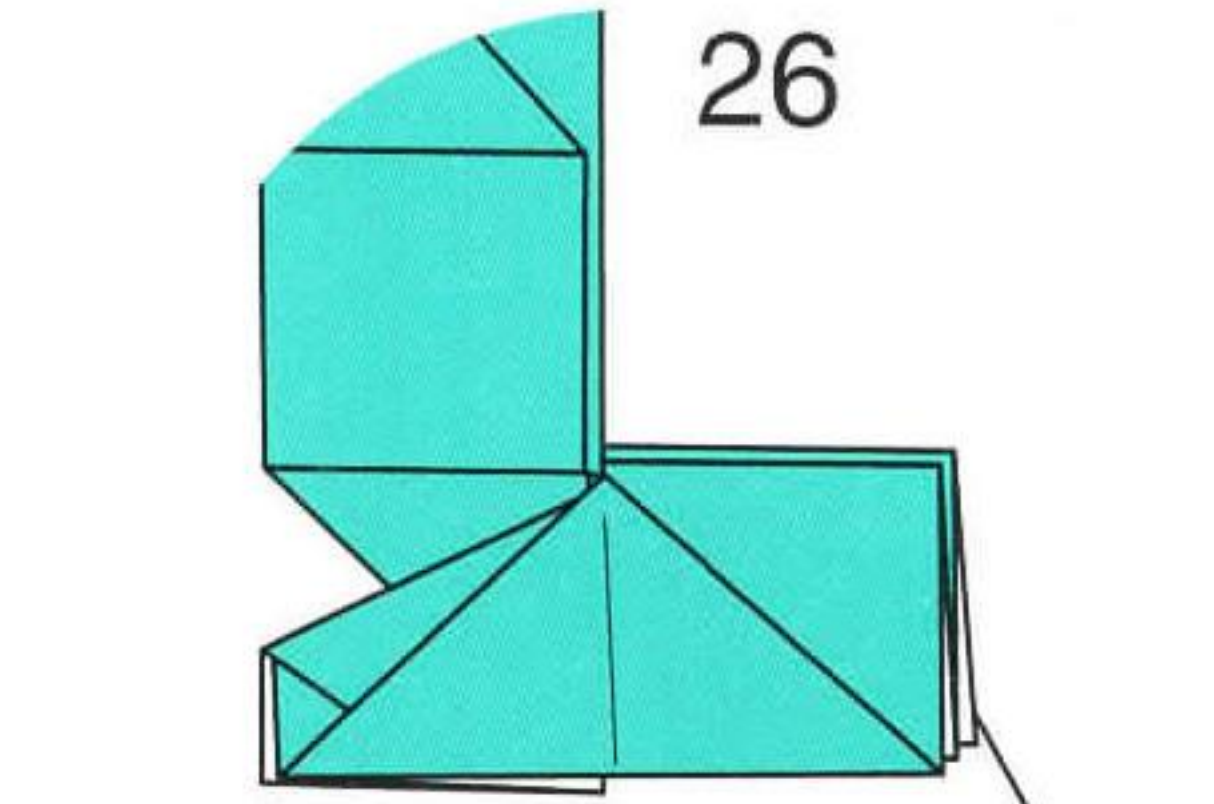
24



25

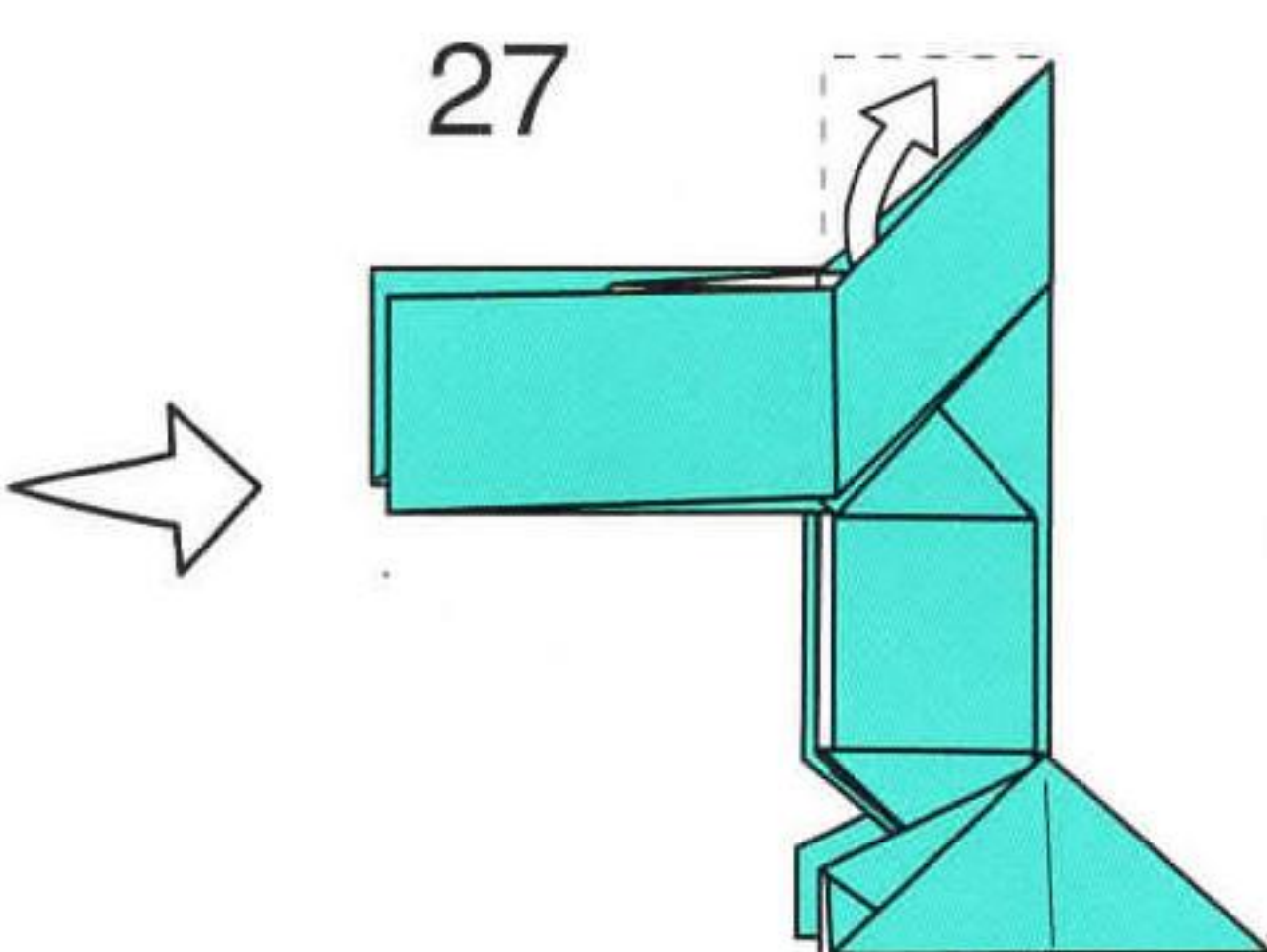


26

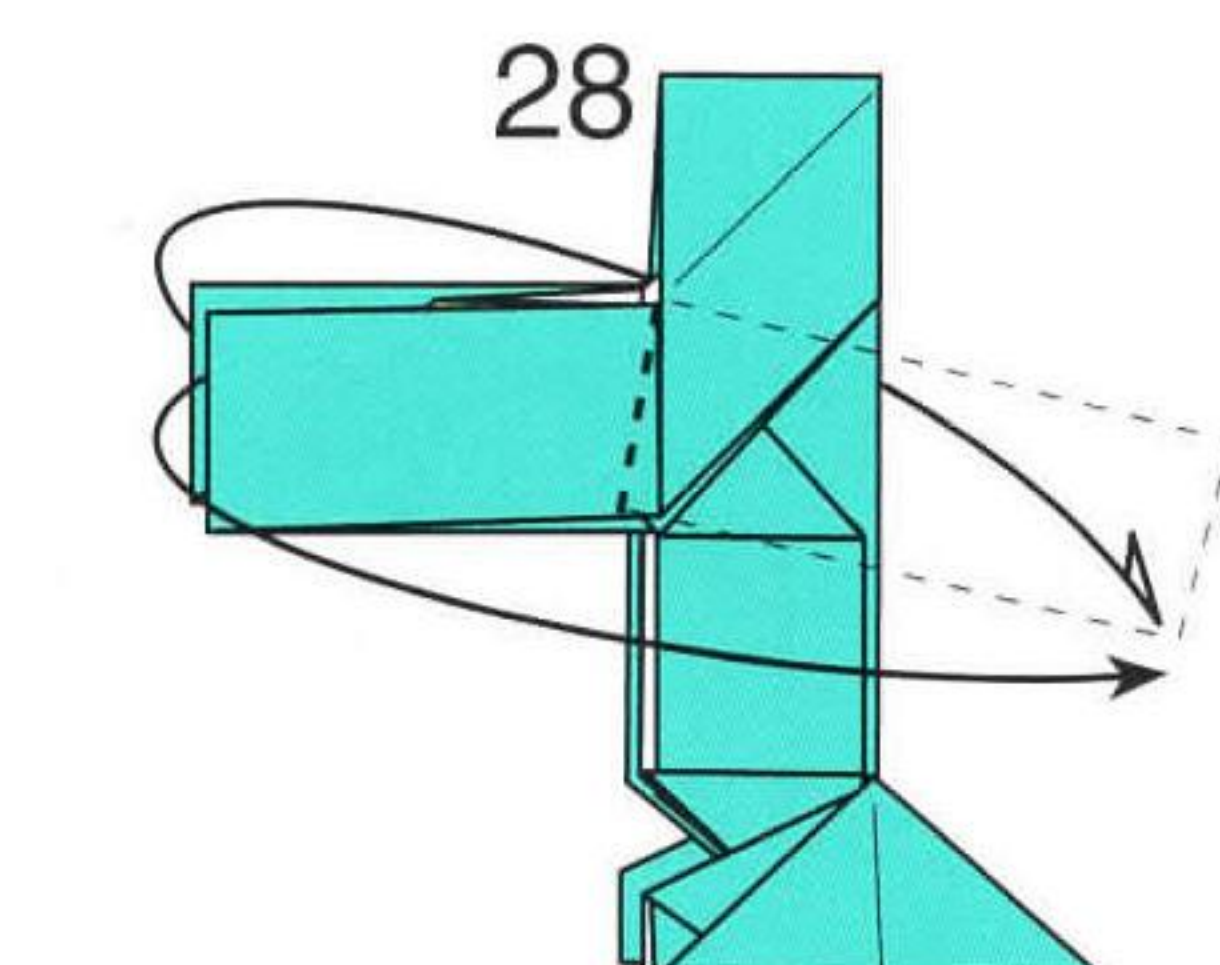


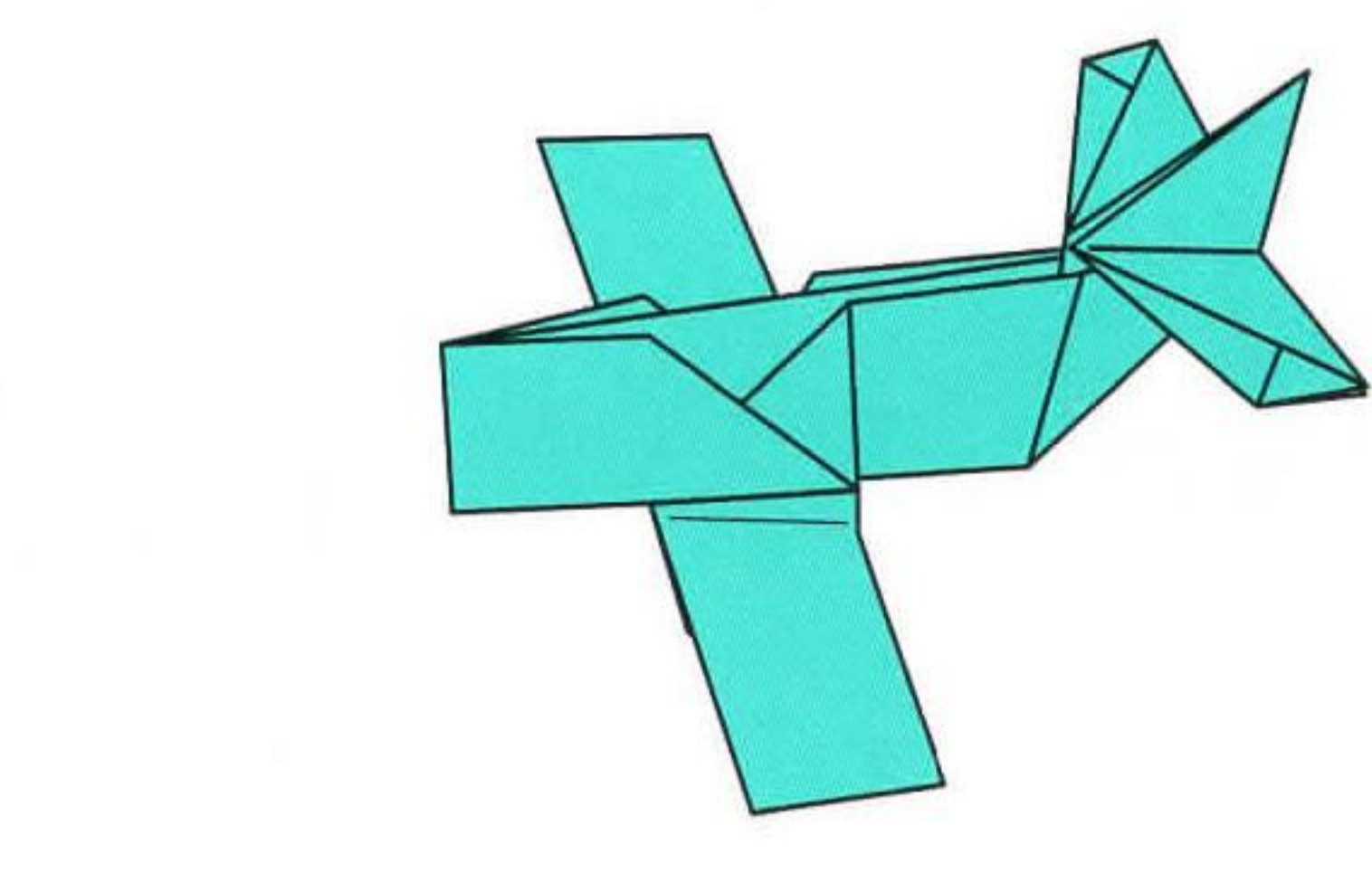
Repeat steps 24-25.

27

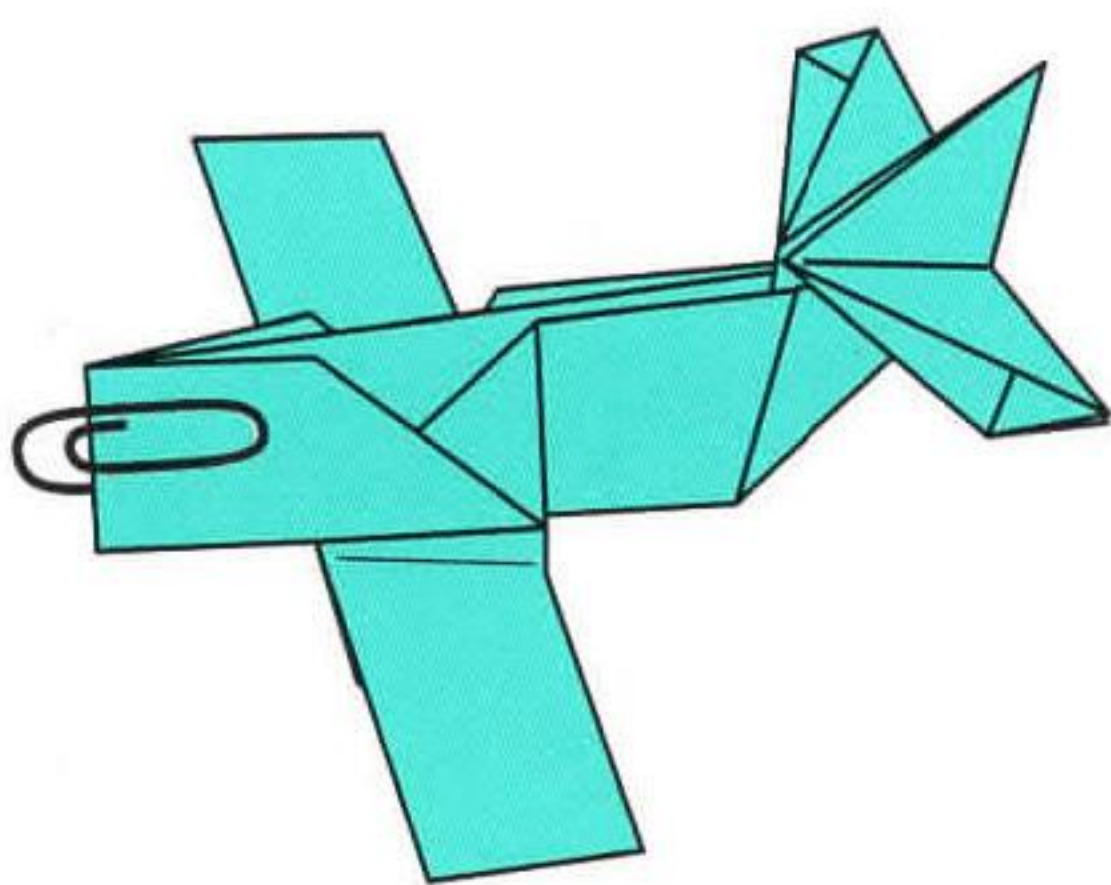


28





Finished.



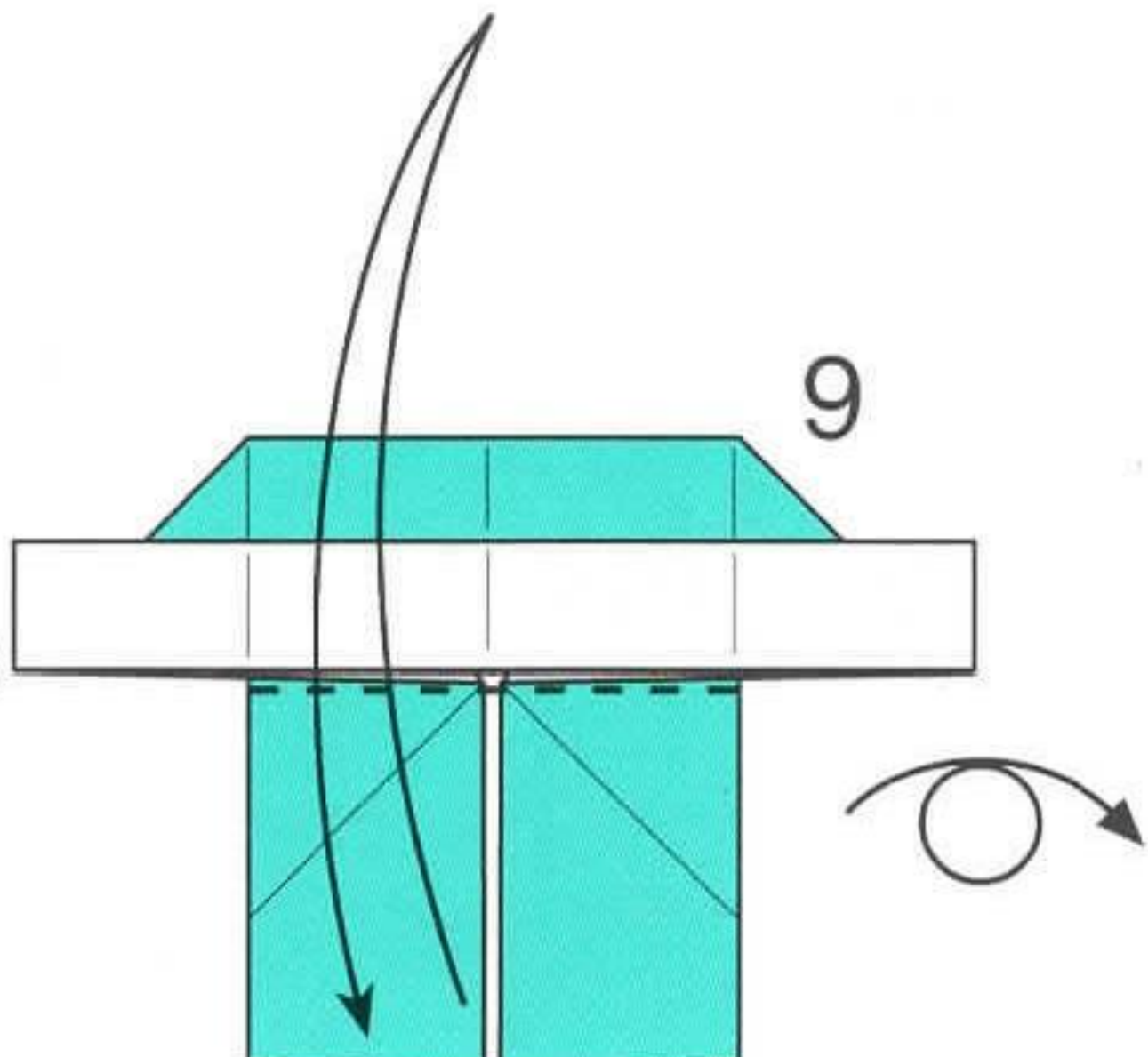
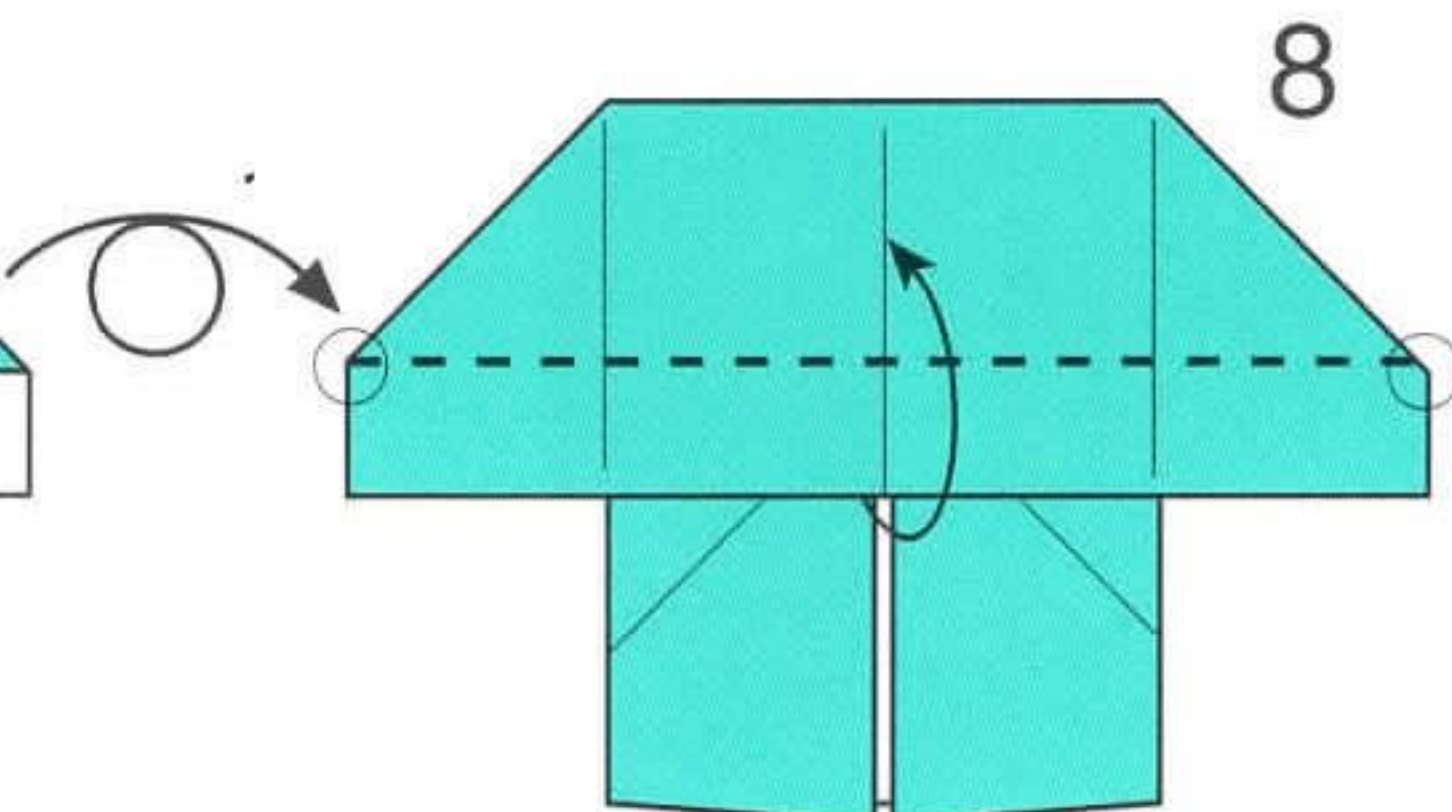
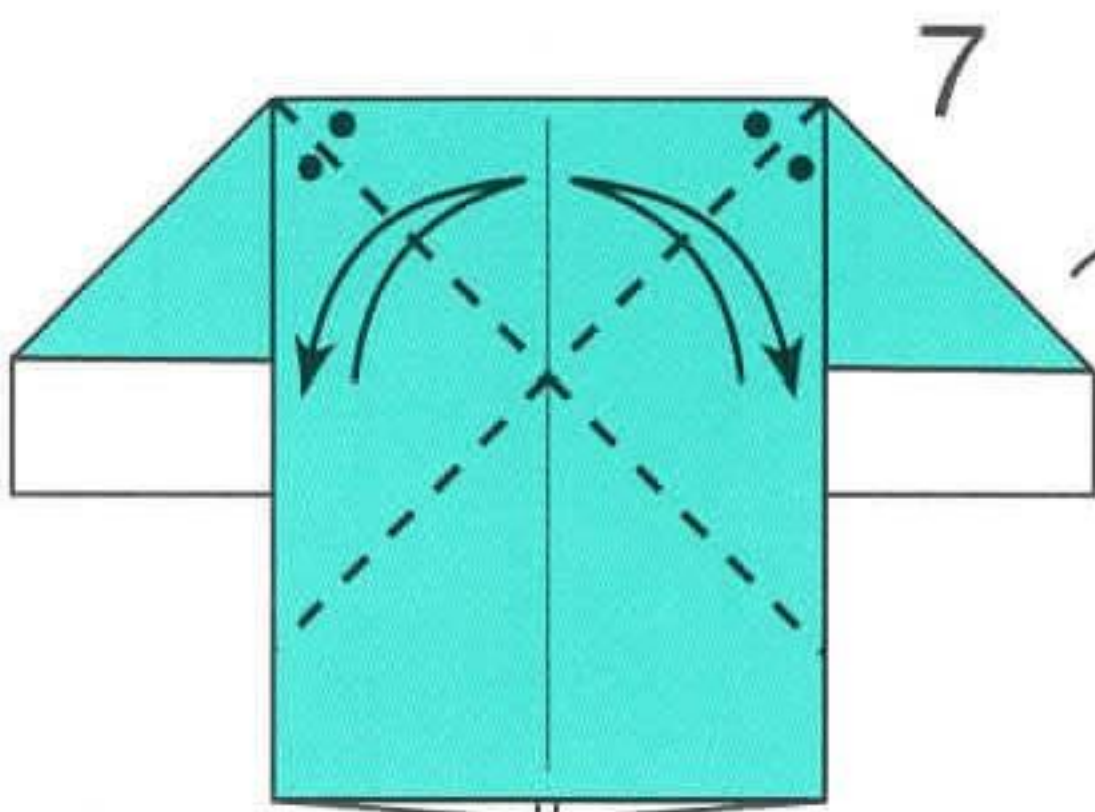
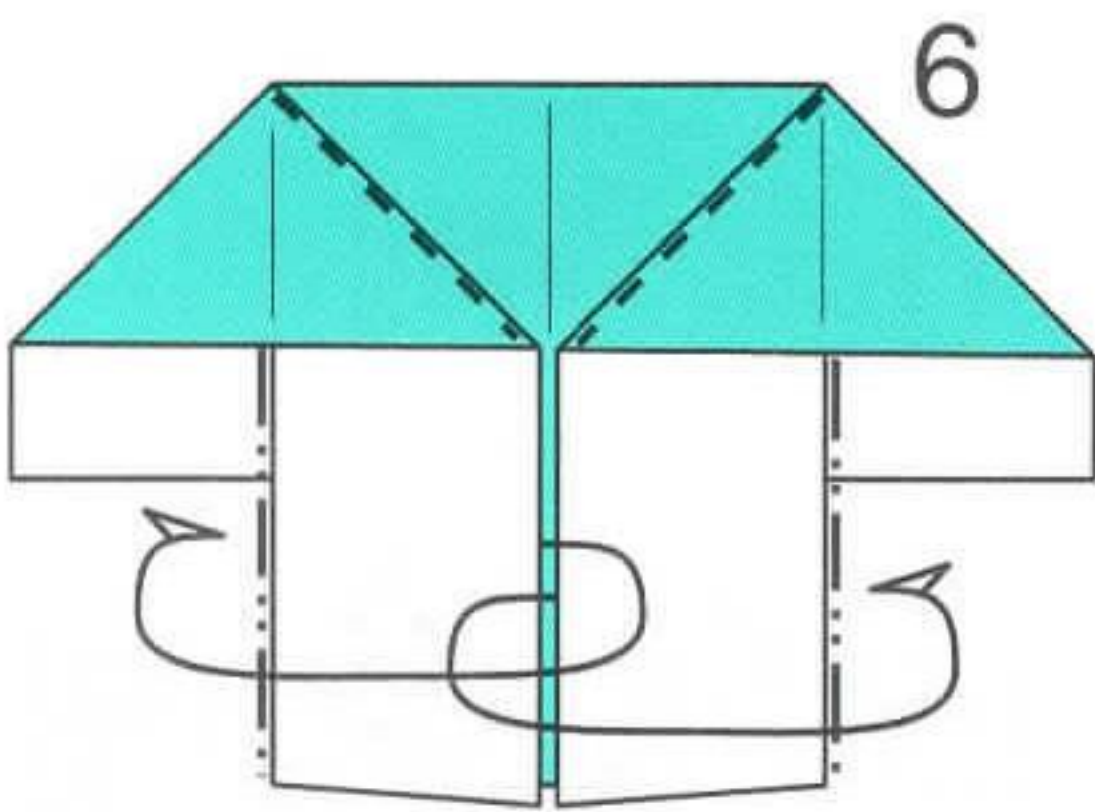
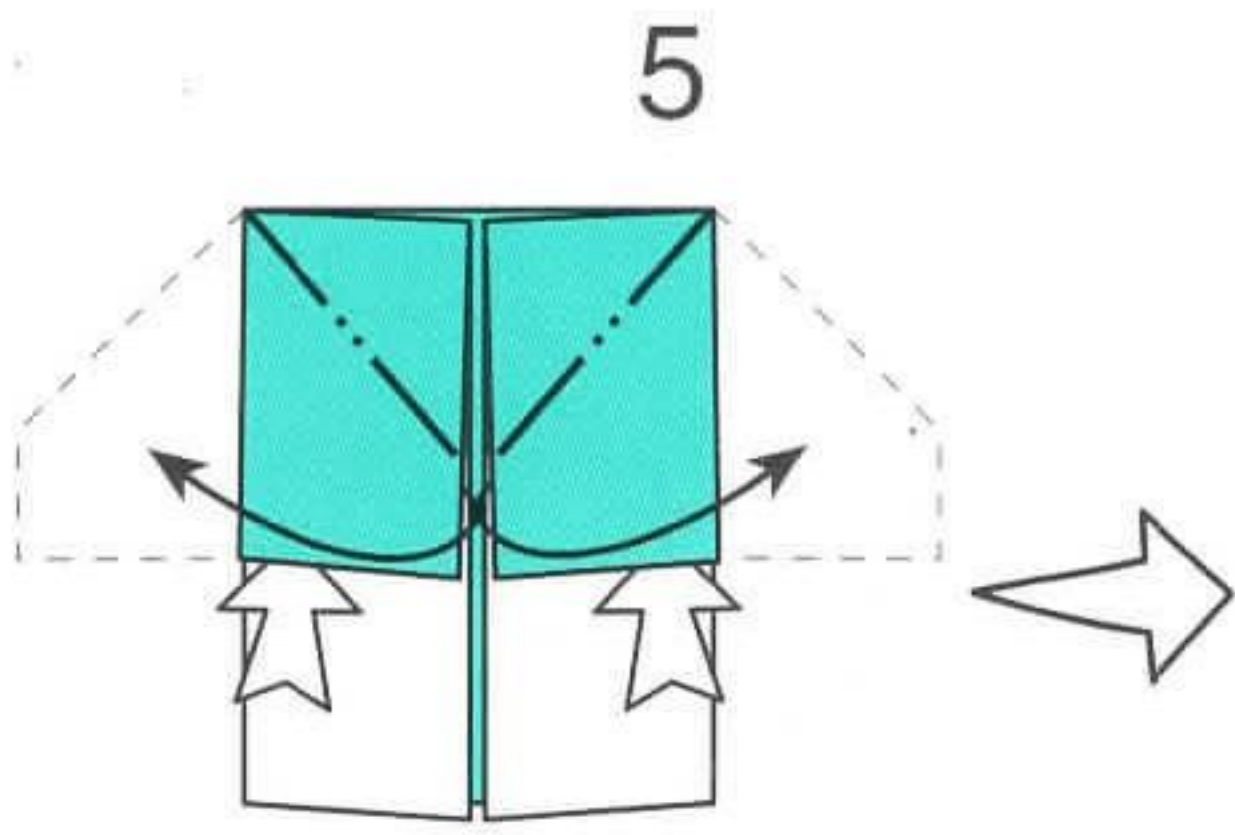
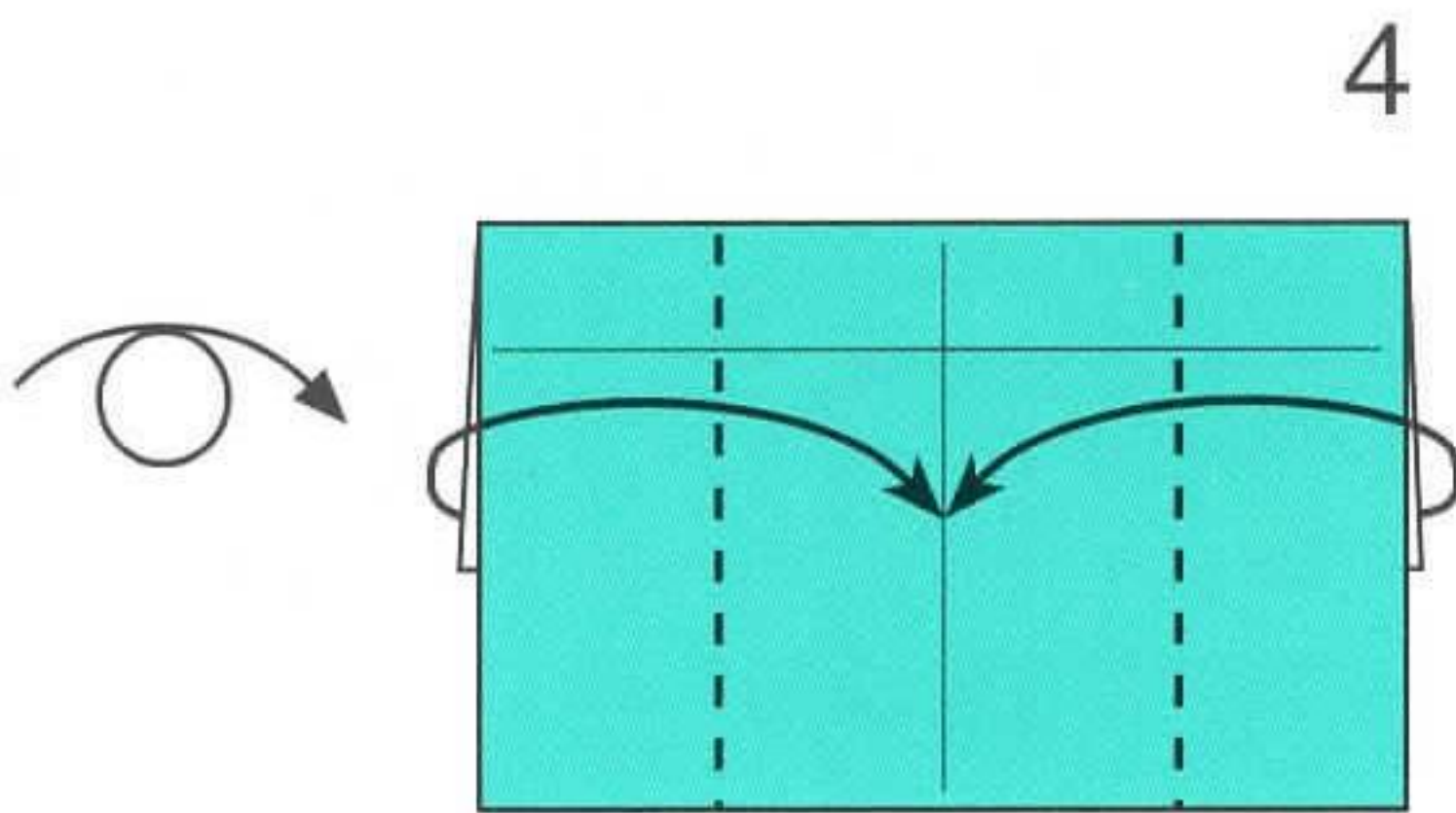
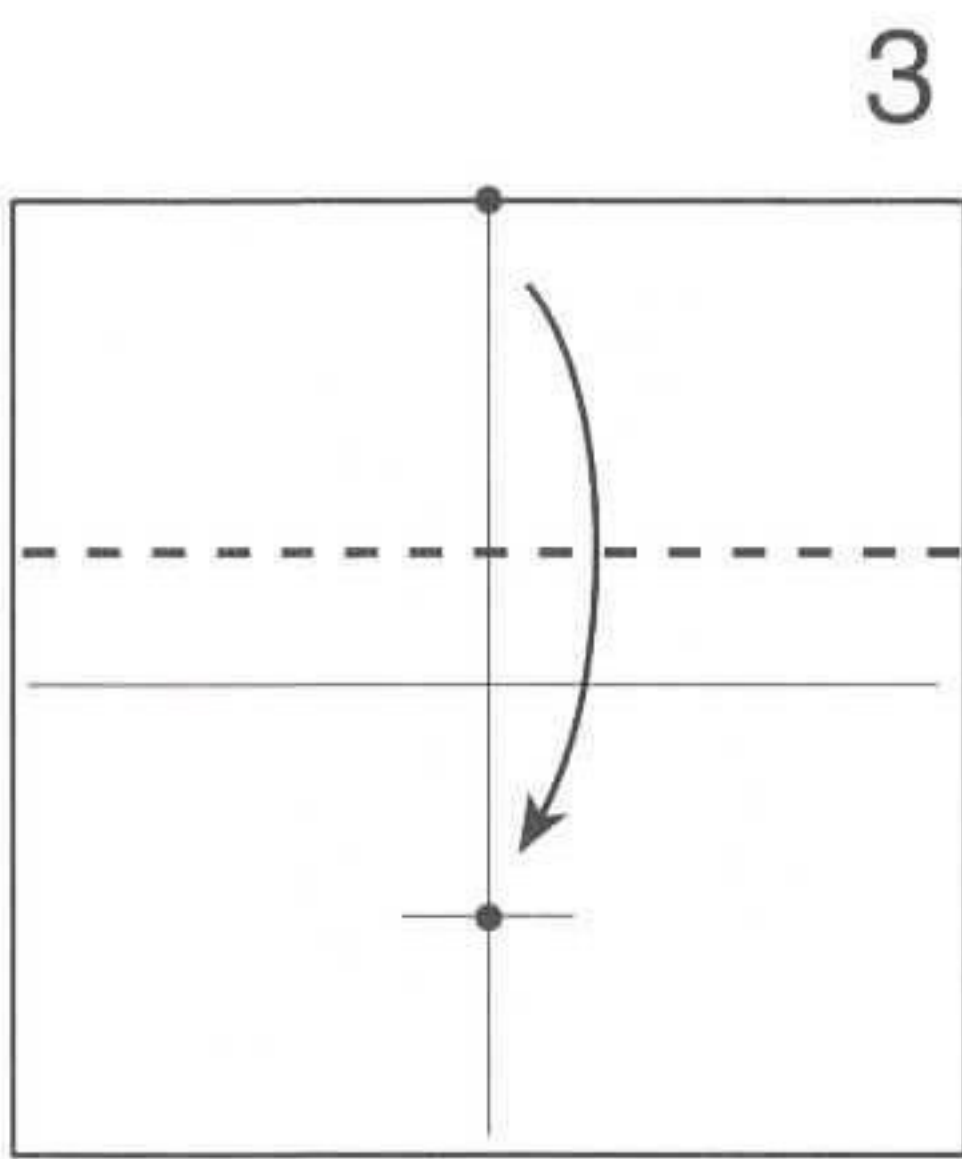
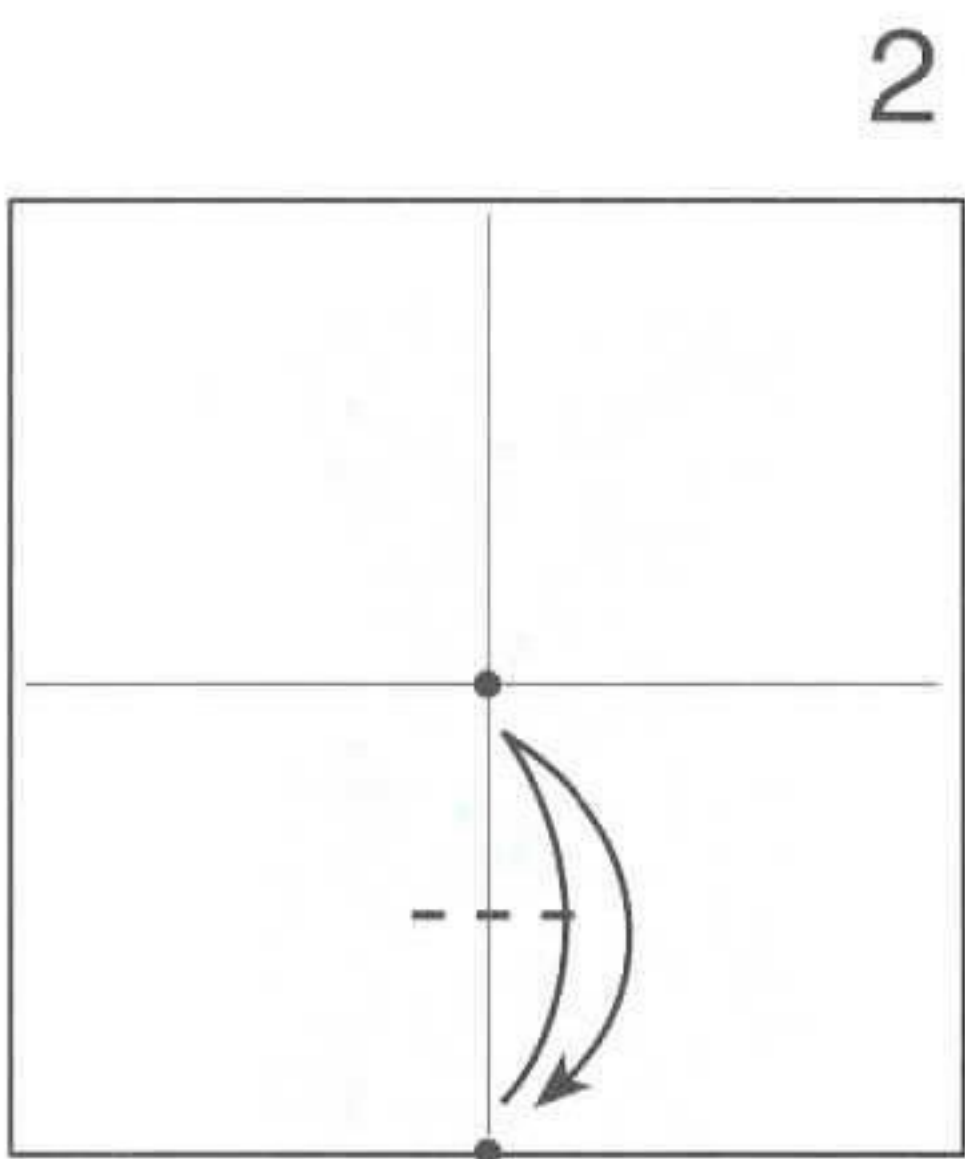
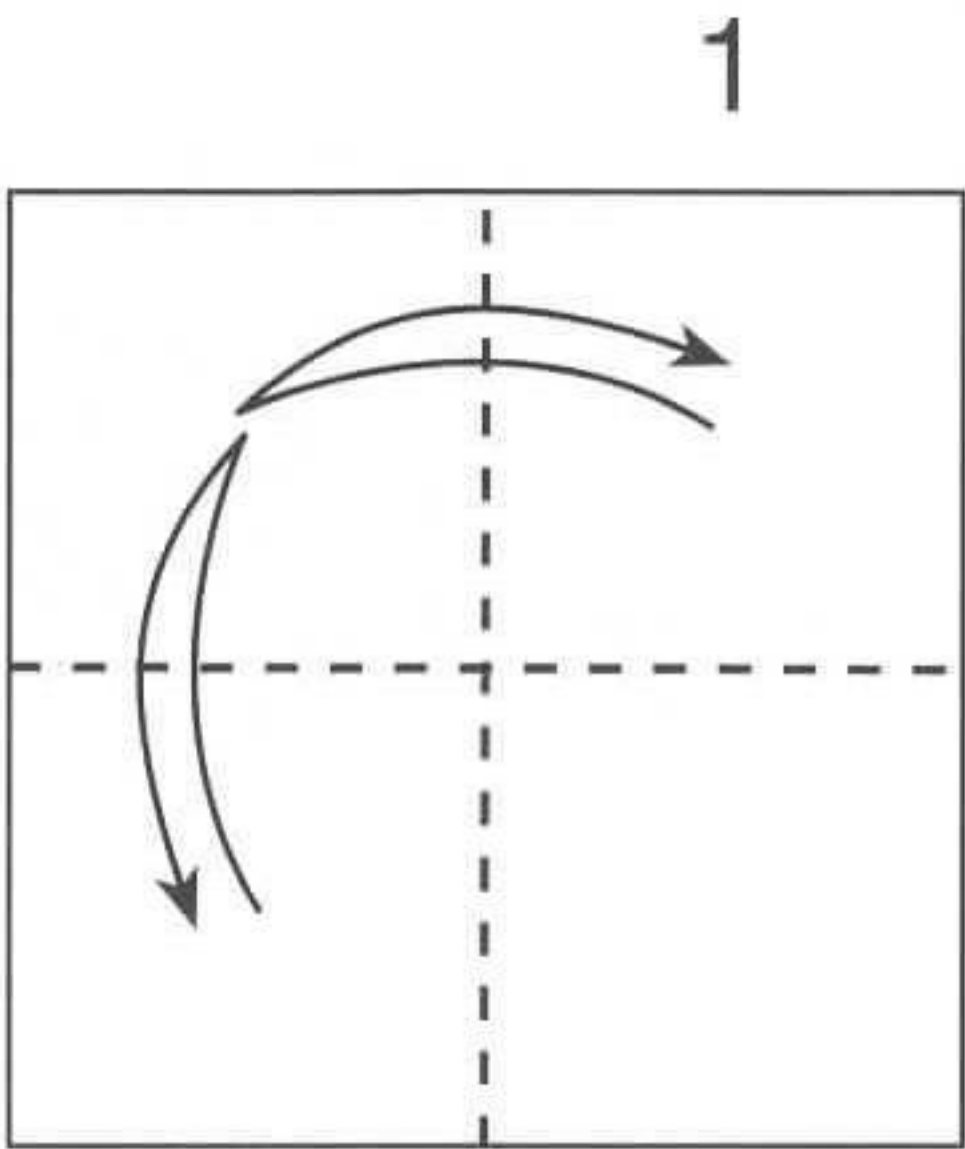
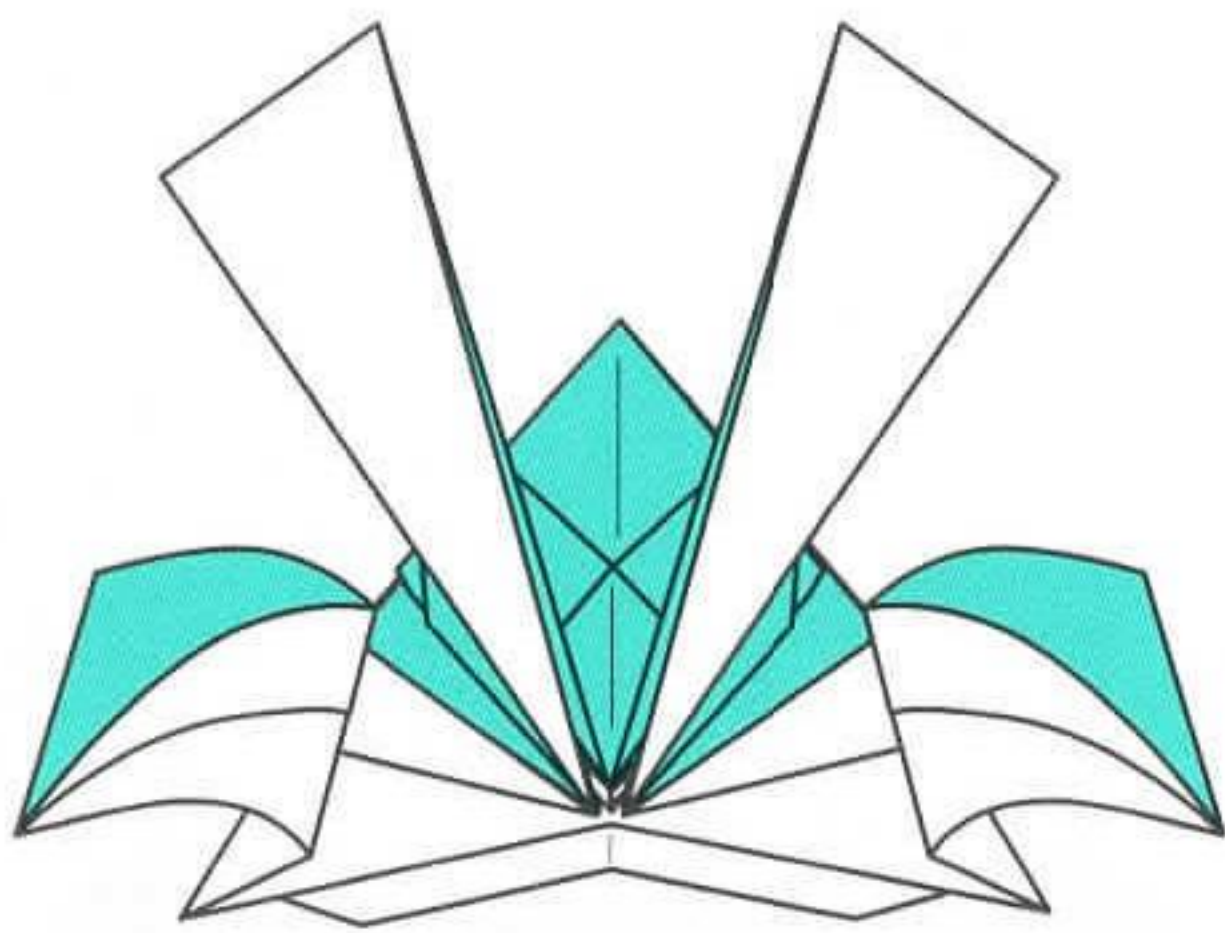
When folded using a sheet of 6" (15 cm) regular origami paper, this model will fly with a paper clip on the nose, although without great flight performance.

There are some origami models that you can play with, such as models that move (either passively by your action or actively with force of unfolding creases) or make sounds. This book does not present such models, but it contains a couple of model that can fly. They are typical examples of action origami.

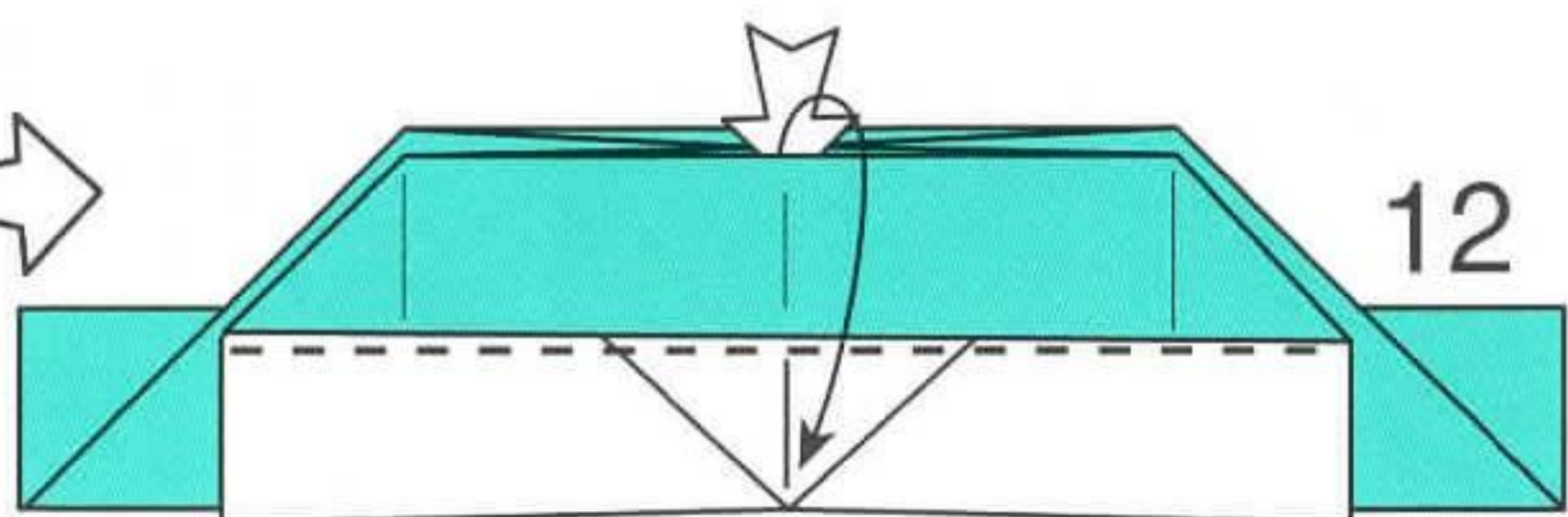
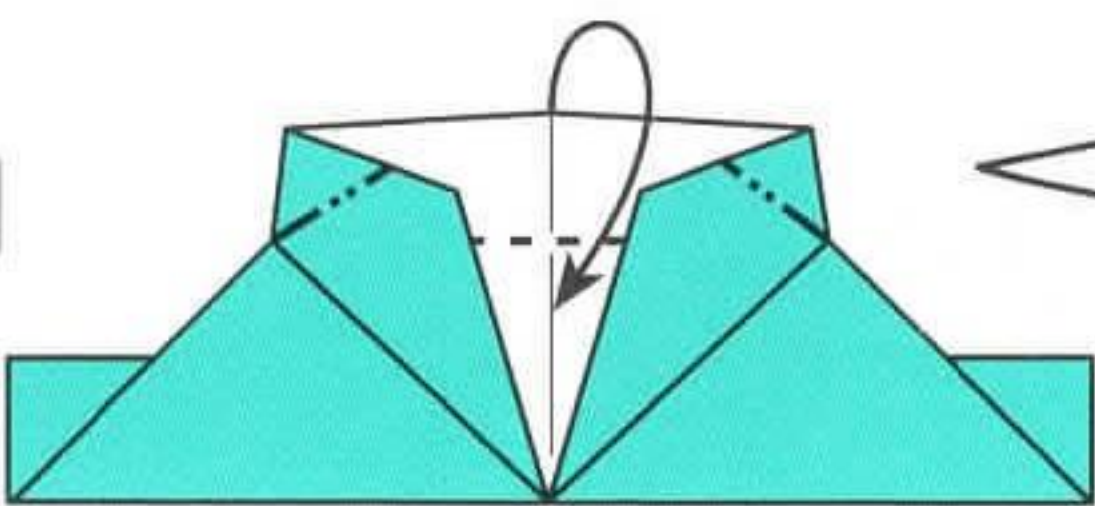
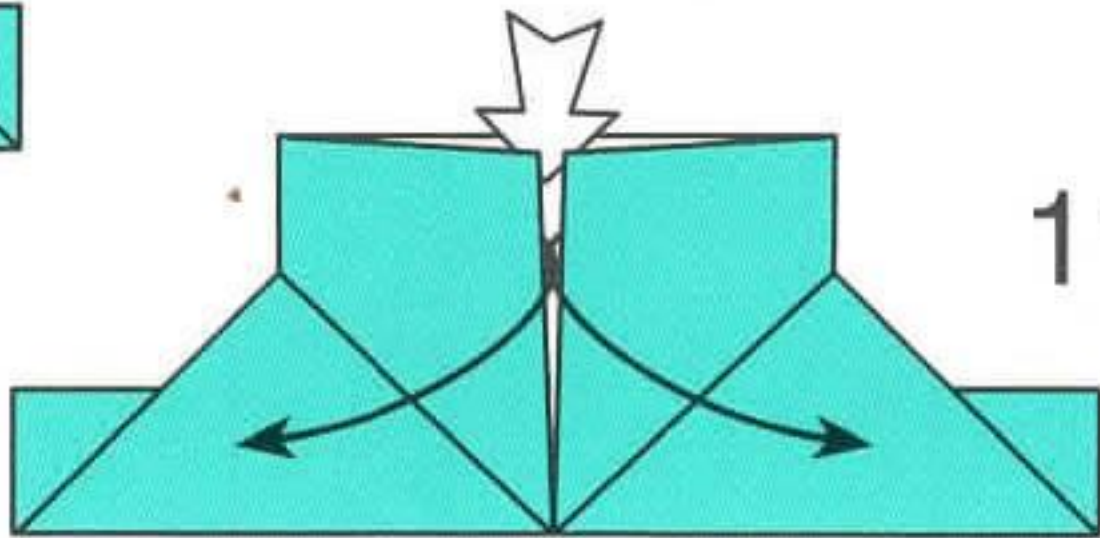
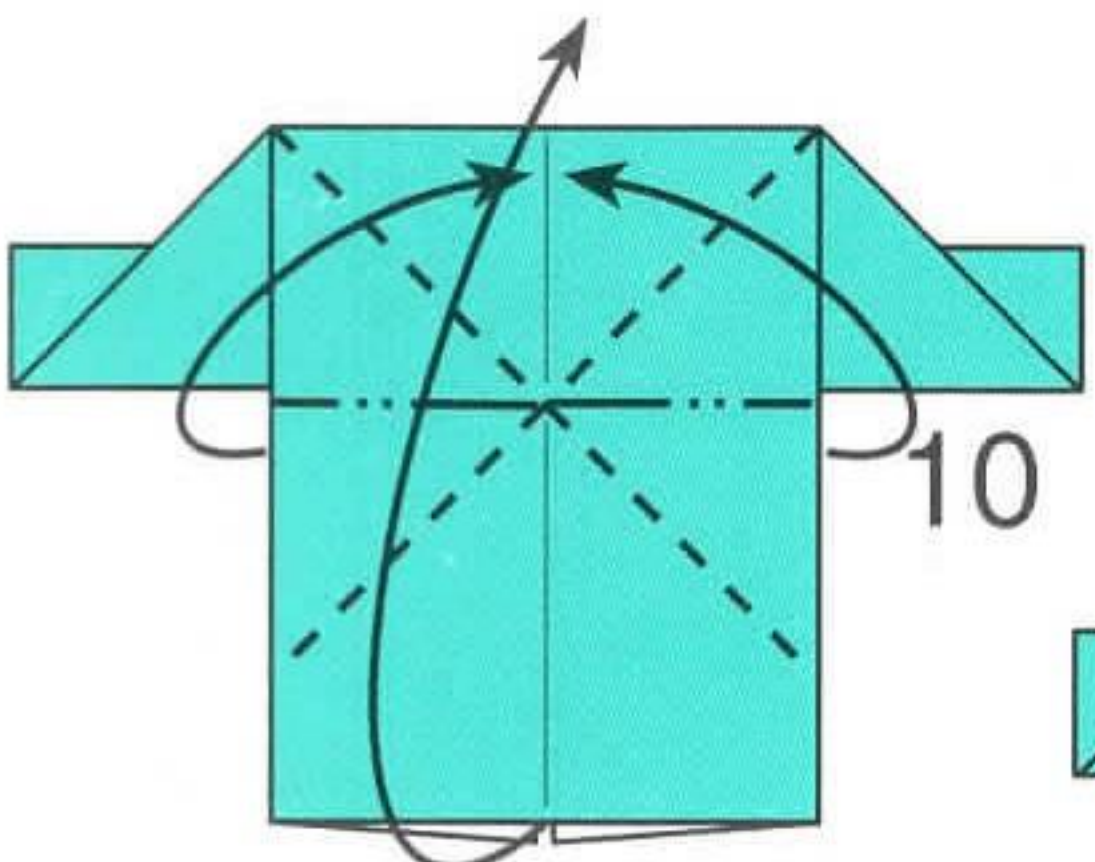
Samurai Helmet

Theme: Half-open

Fold using 6" (15 cm) origami paper.



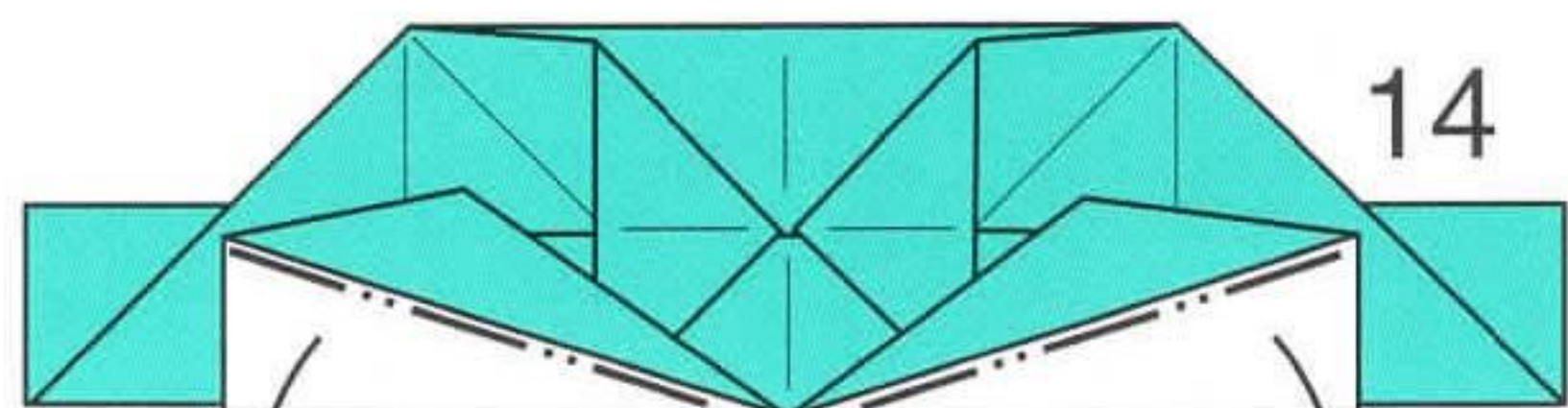
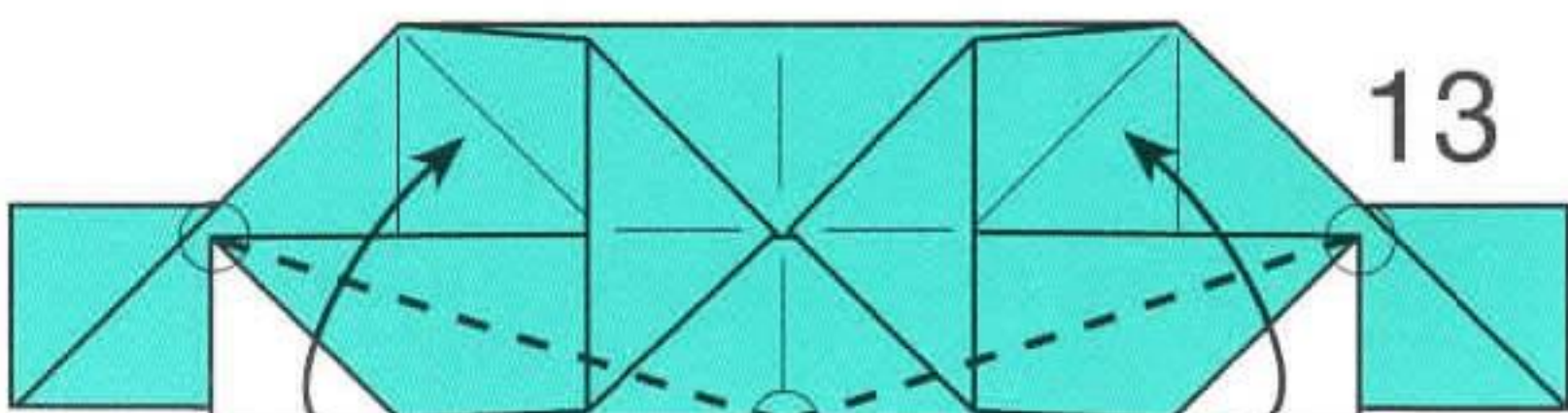
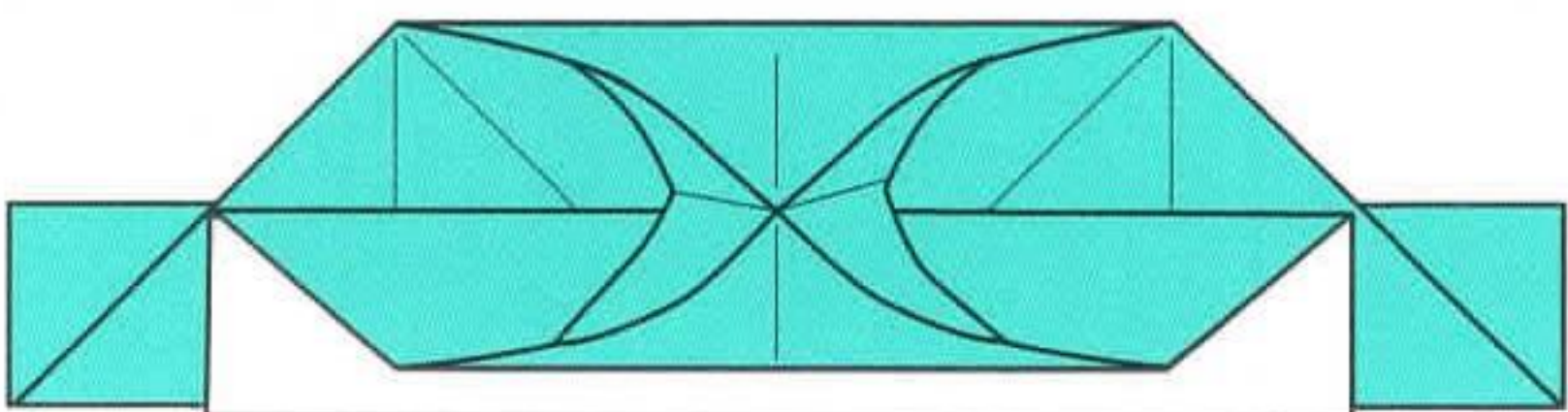
Reverse the mountain creases into valley and valley into mountain.



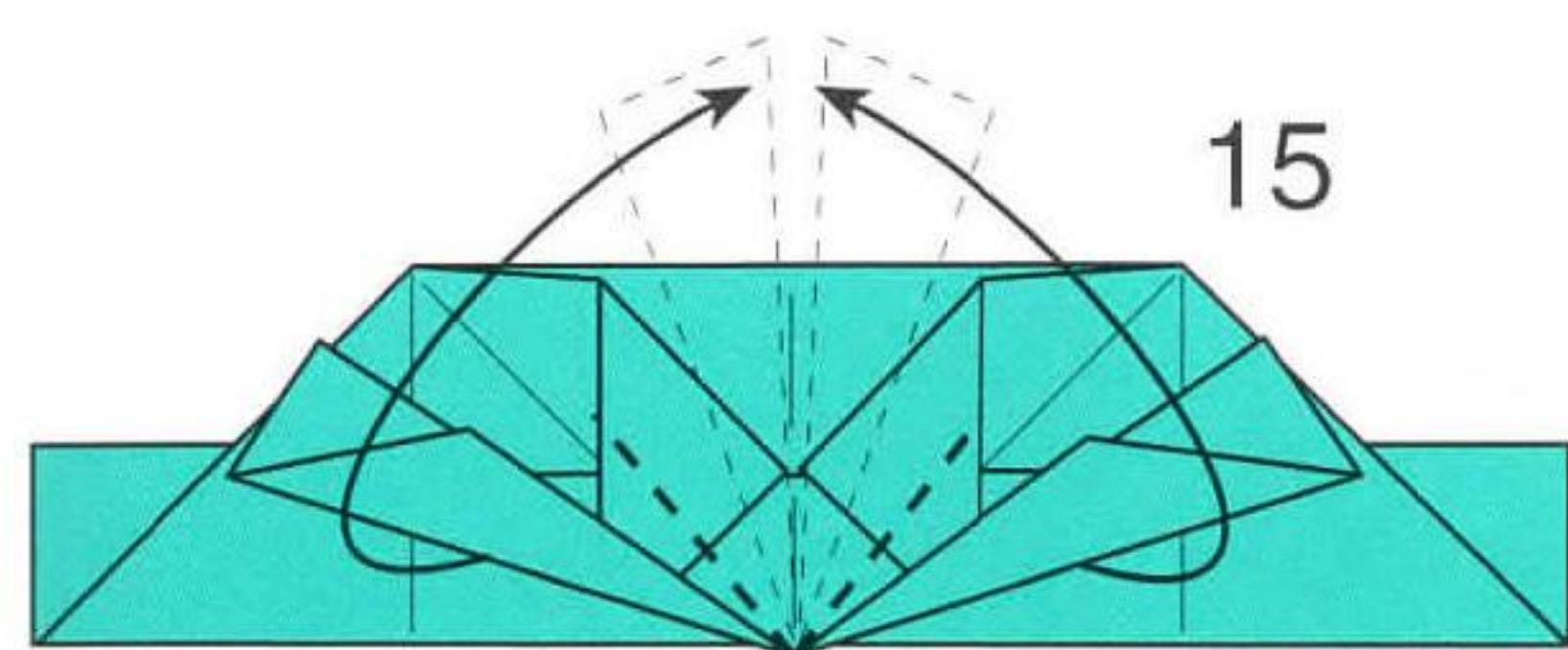
Fold like a Water-bomb base using existing creases.

Open,

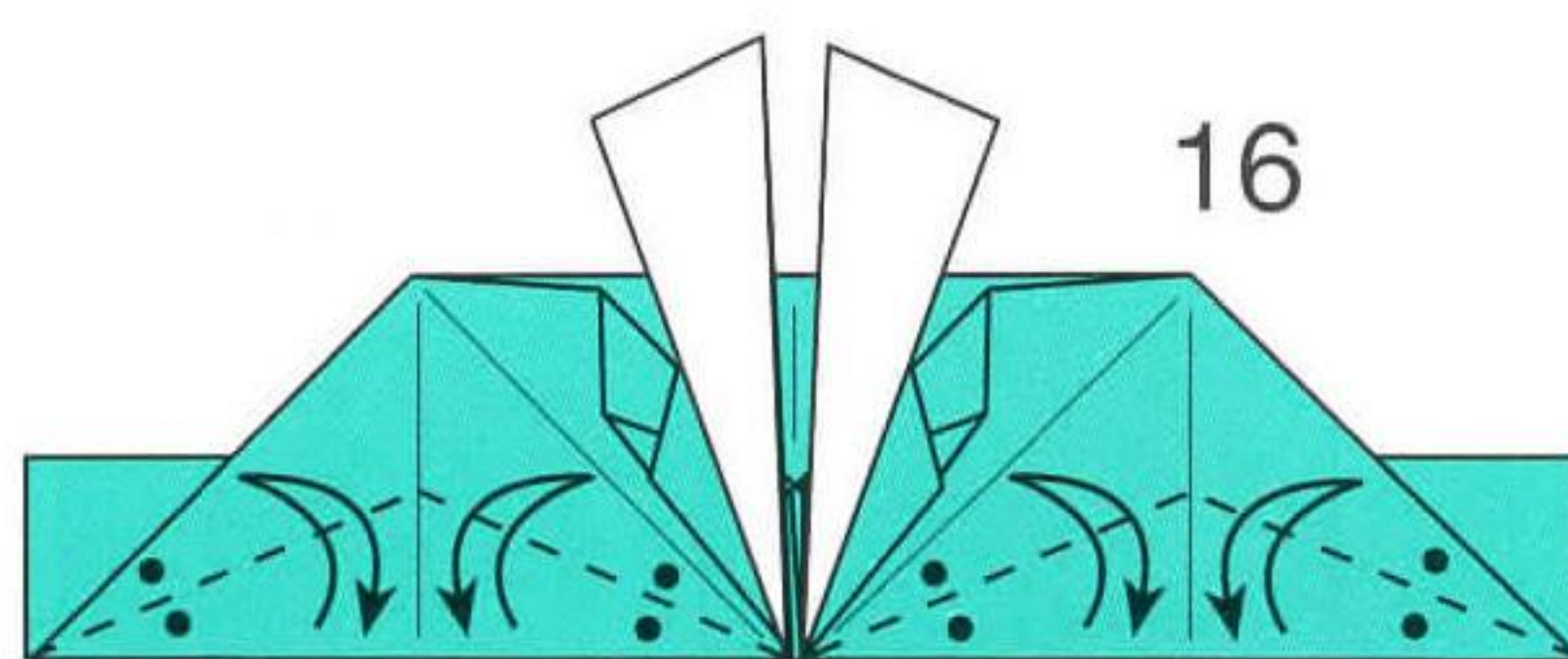
and squash.



In progress.

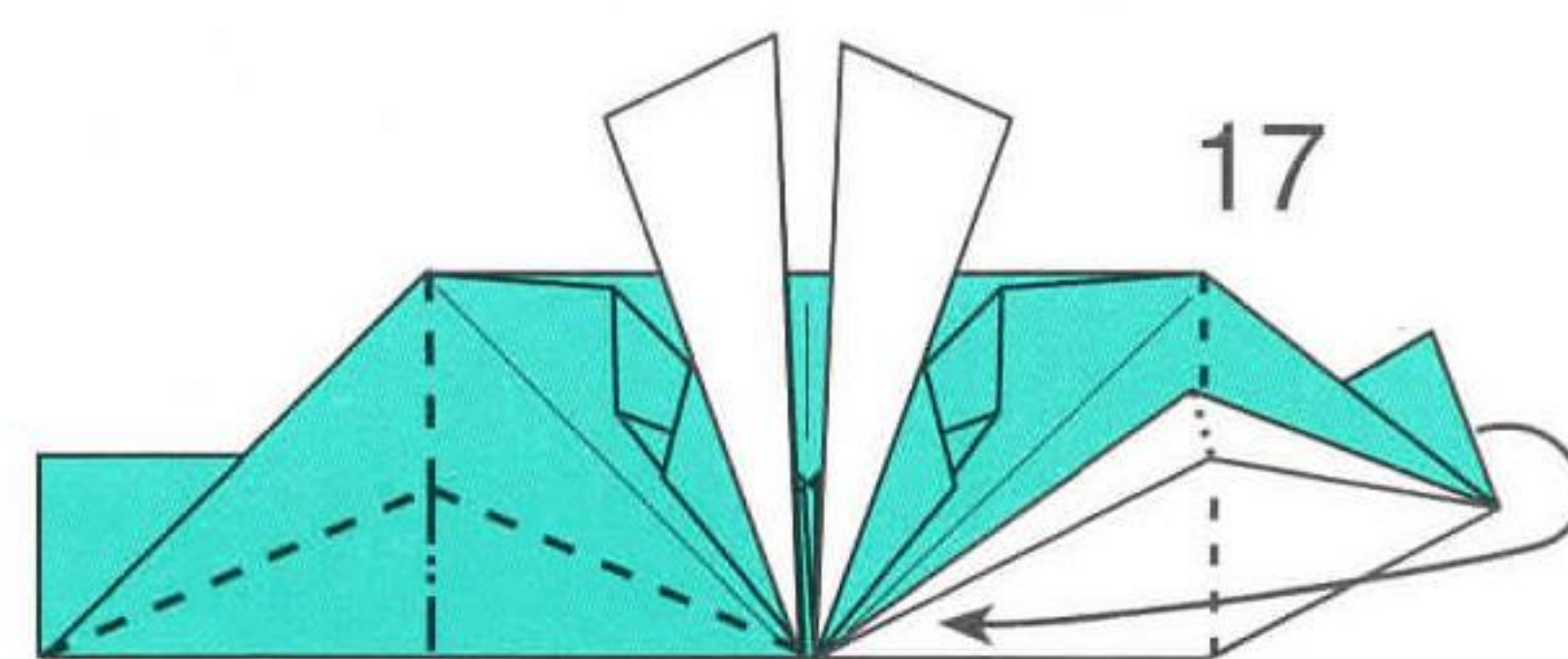


15



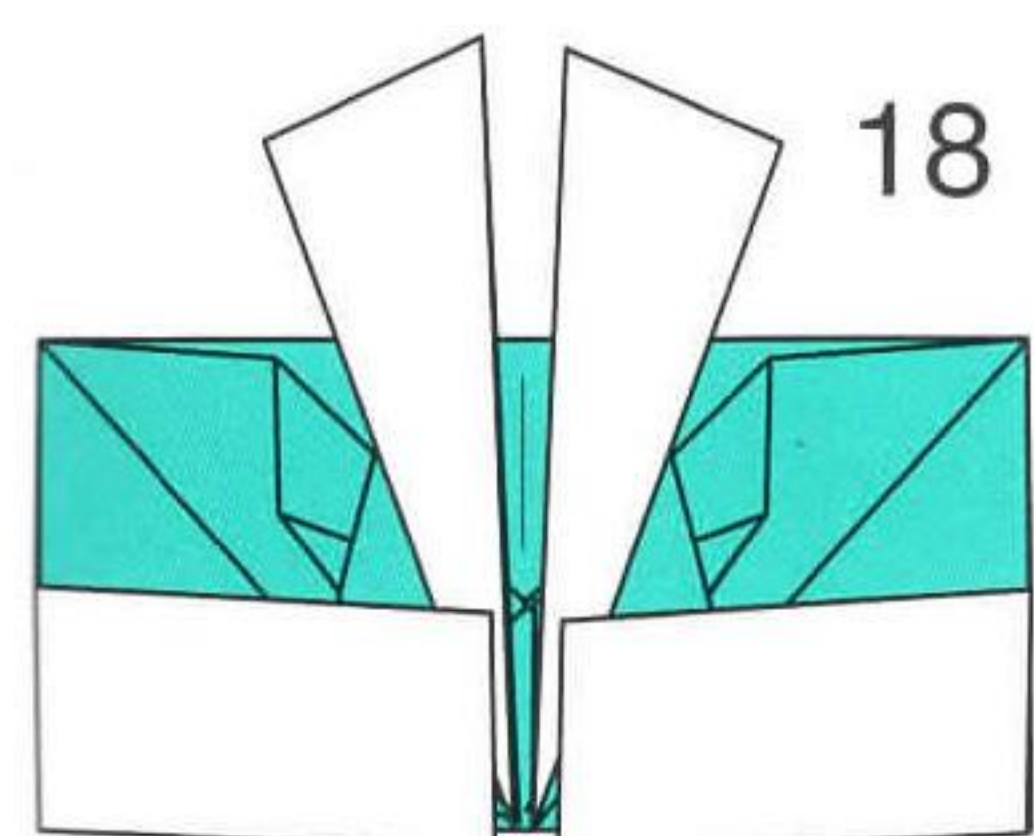
16

Fold and unfold the top layer only (the model will not lie flat).

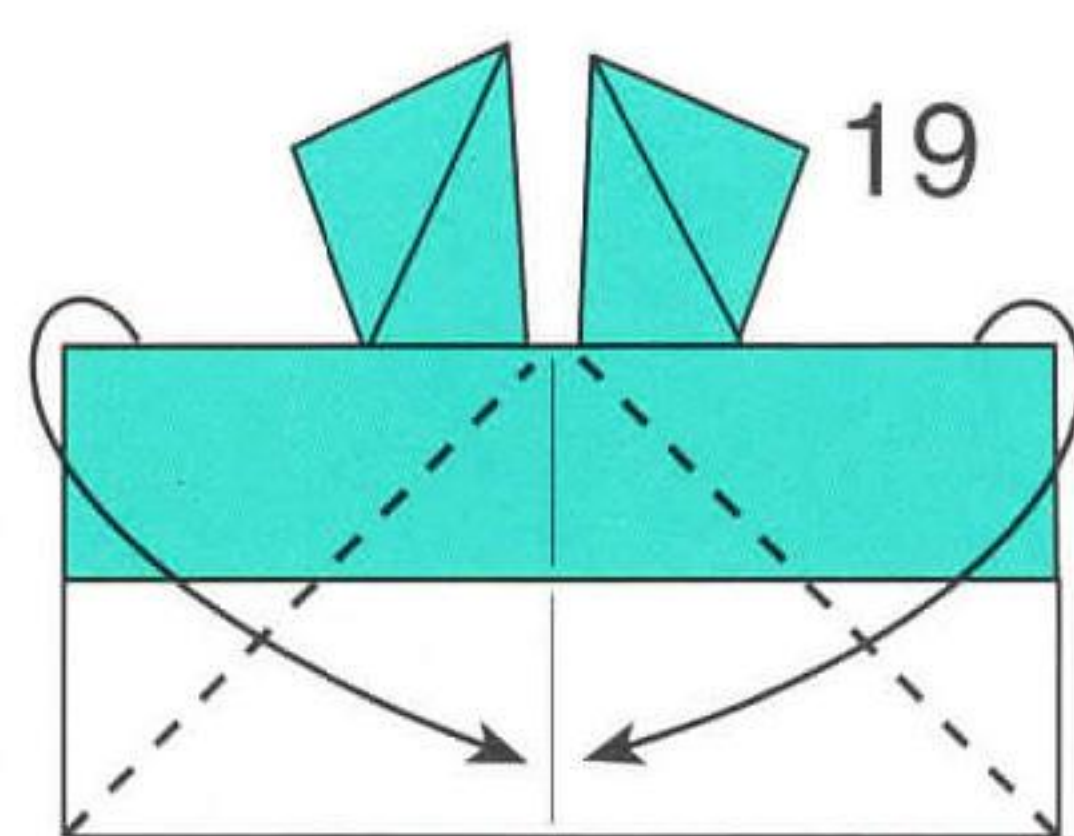


17

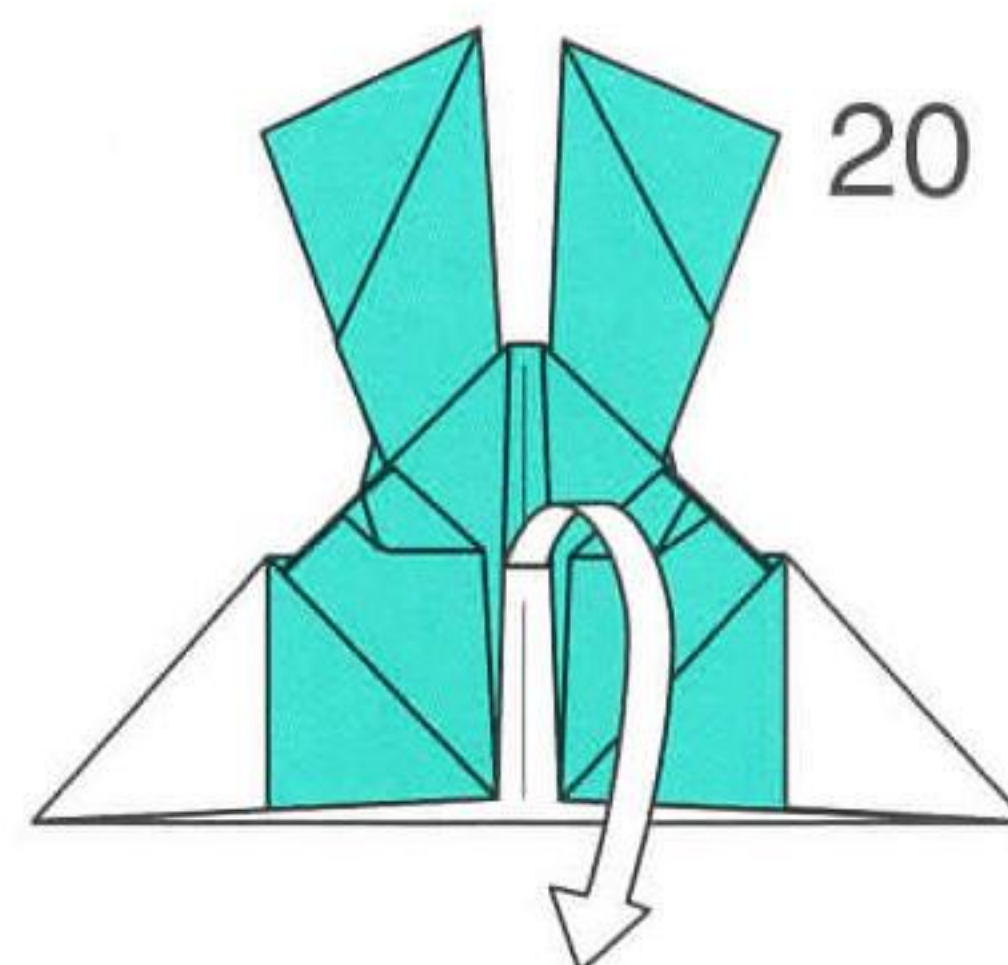
Fold like a half Bird-base using the creases made in step 16.



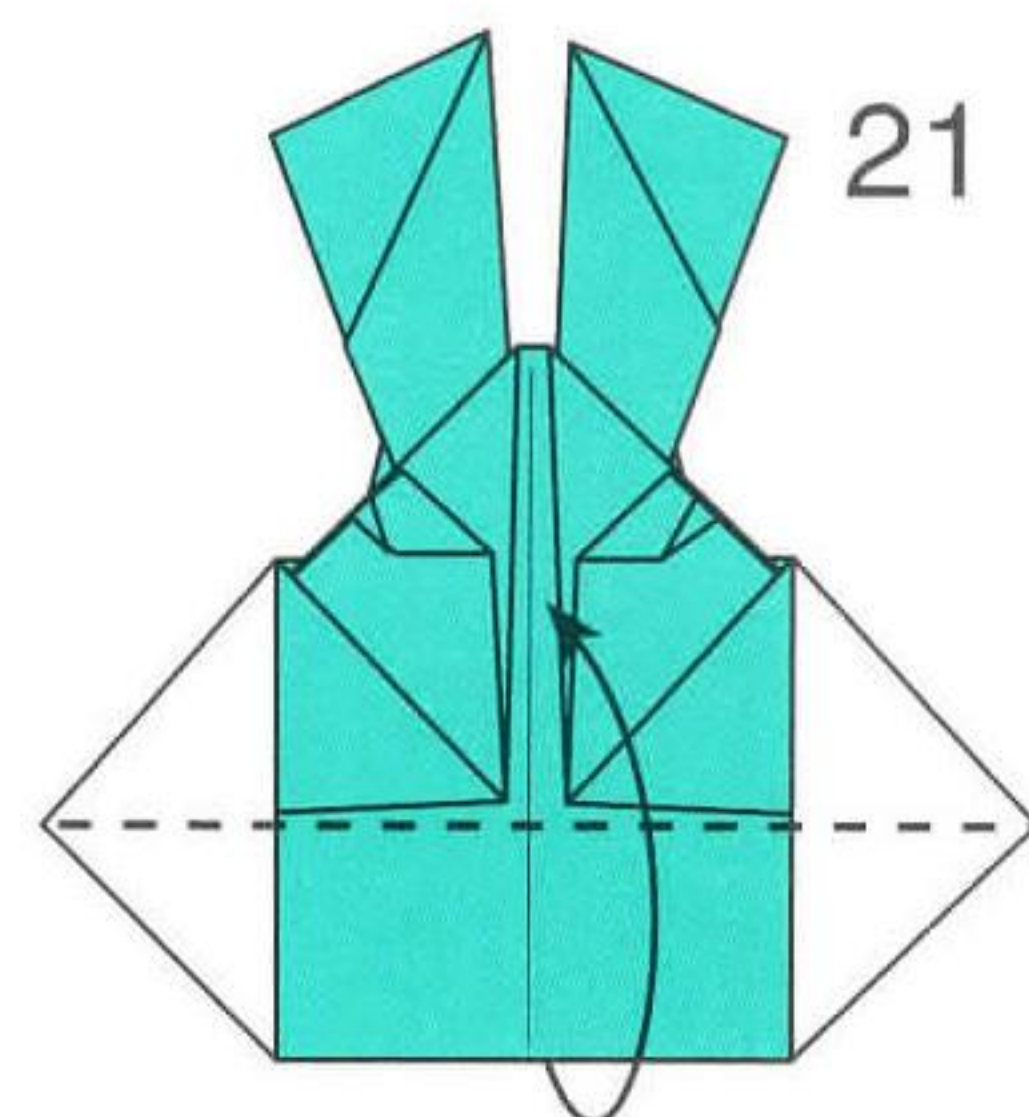
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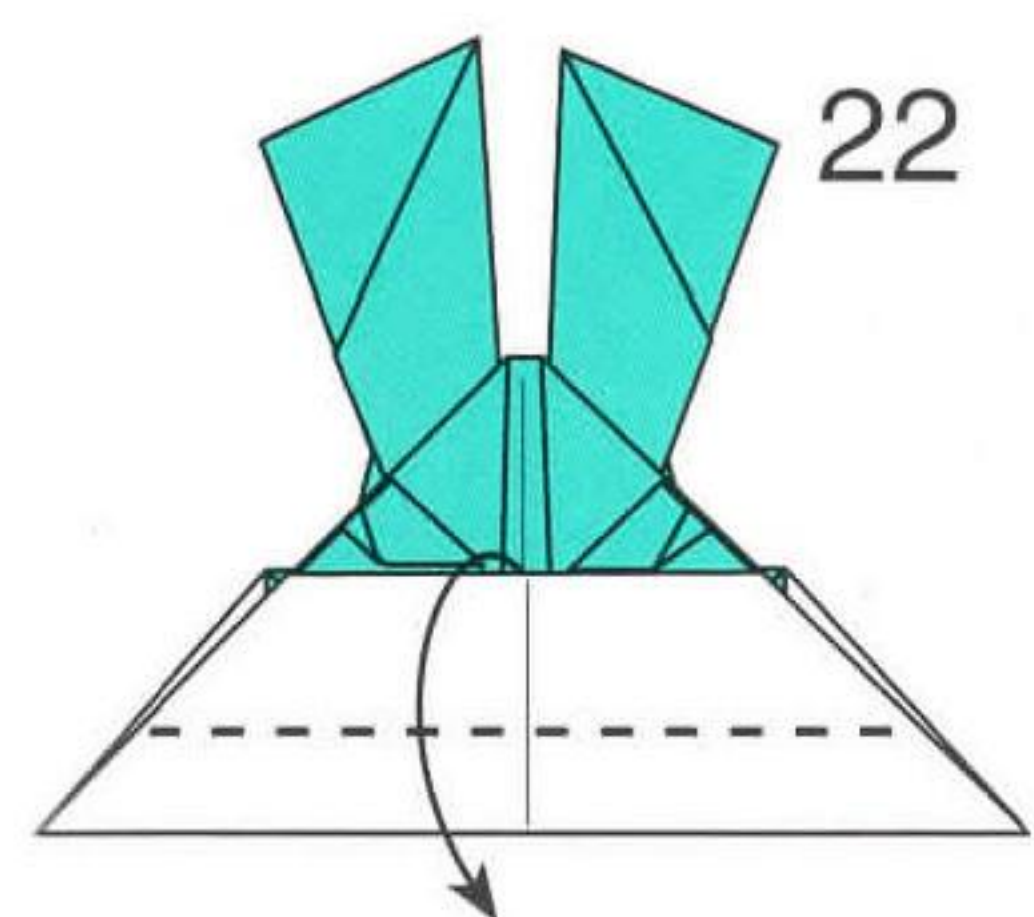
19



20

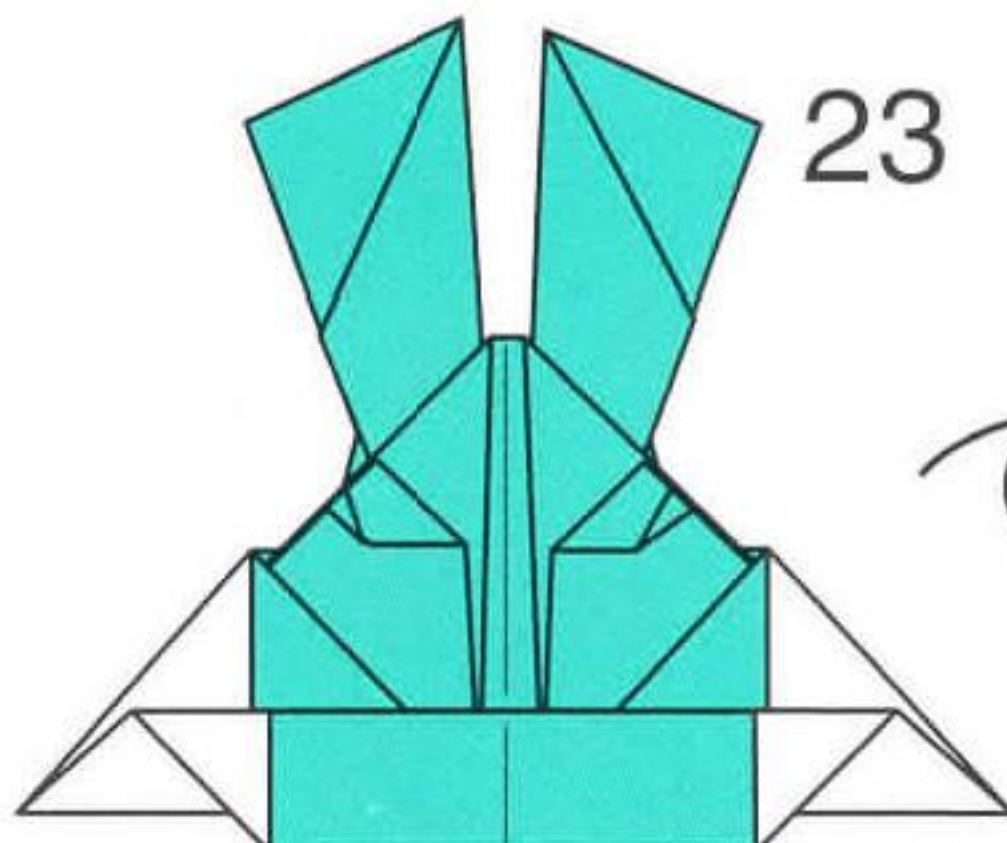


21

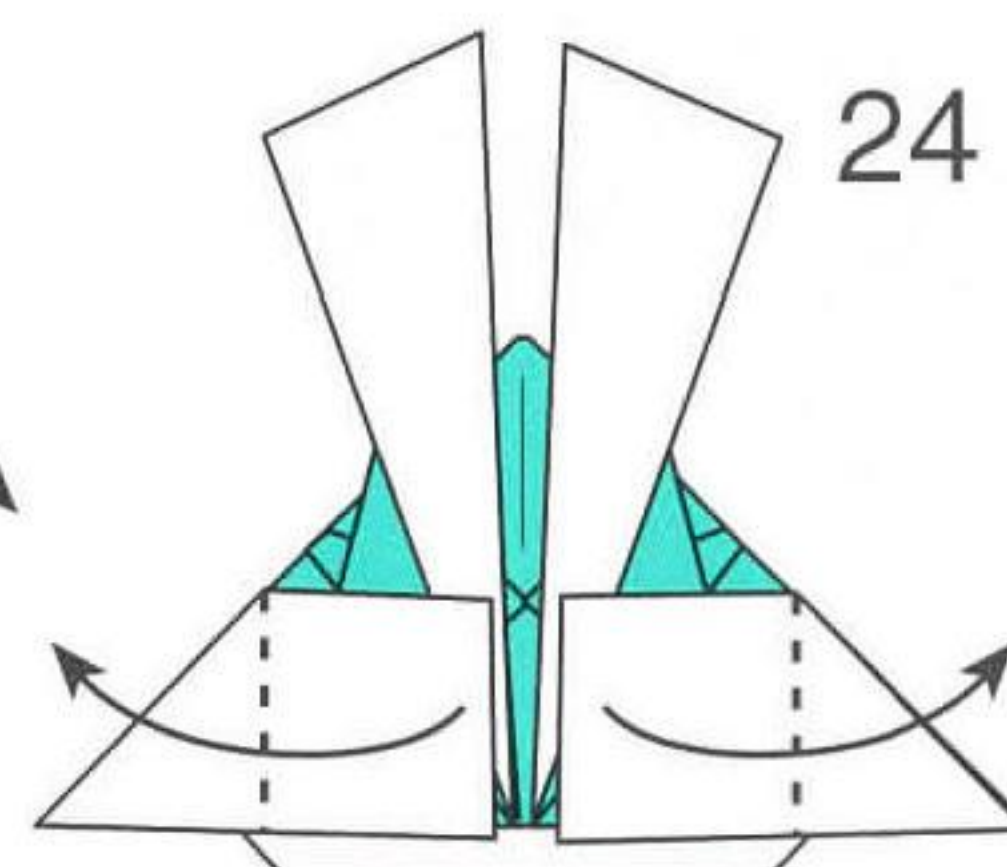
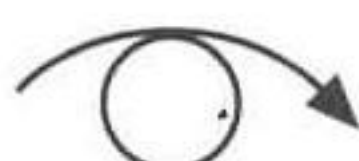


22

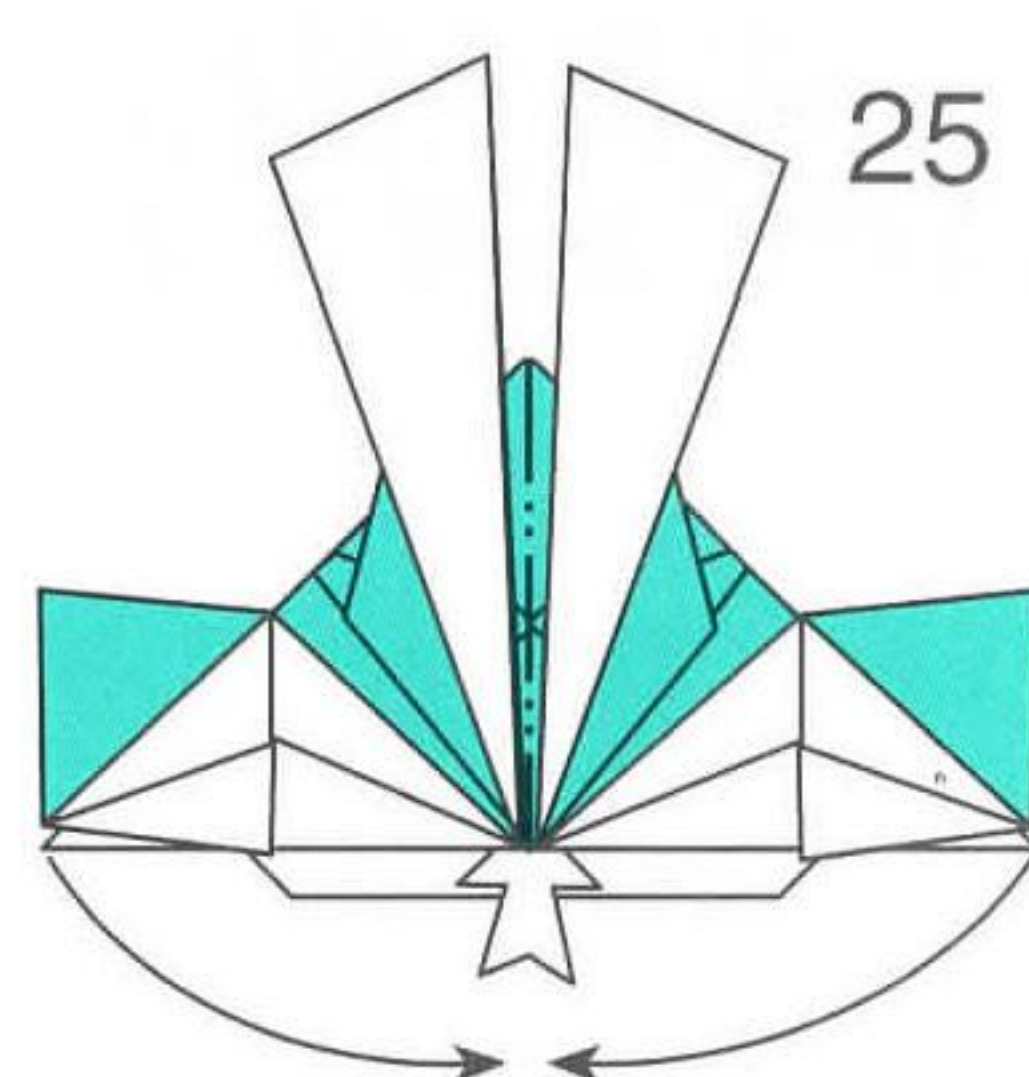
about 3
about 2



23

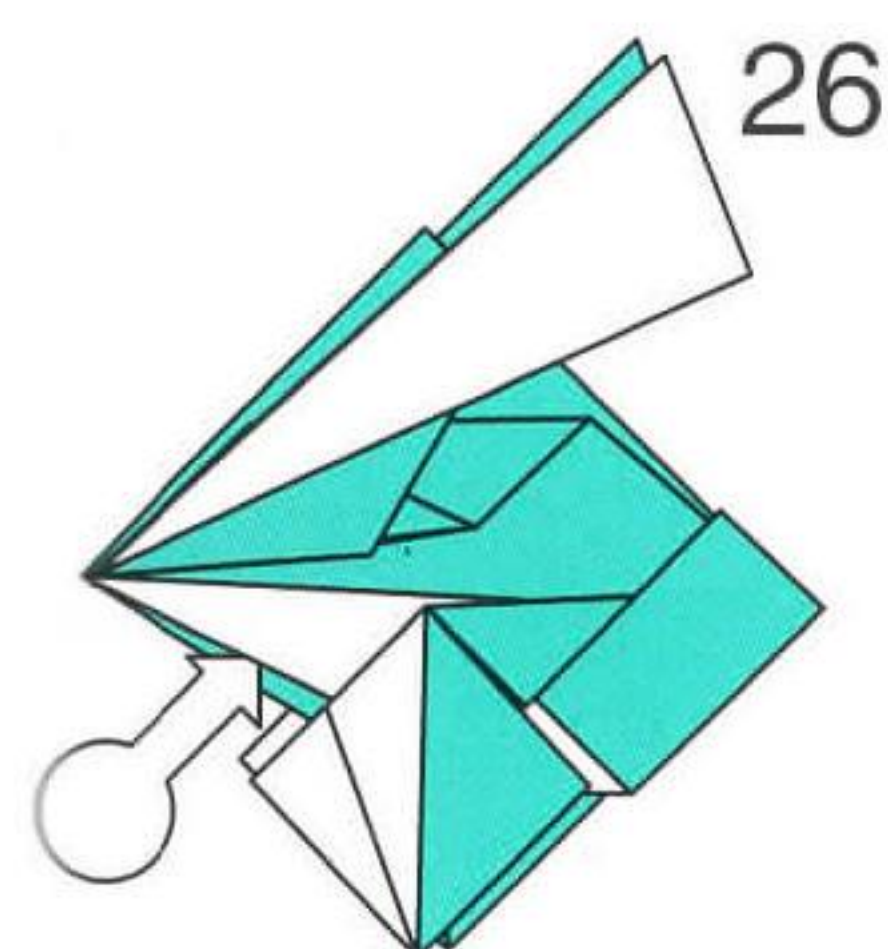


24

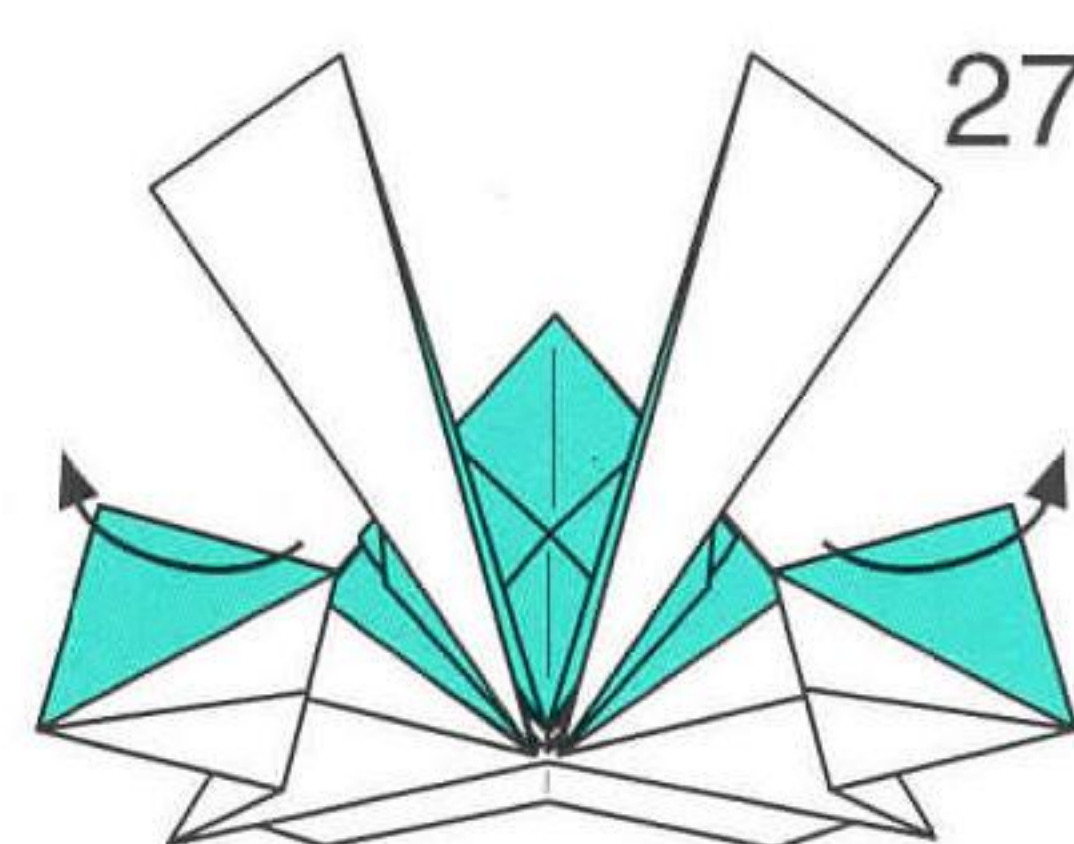


25

Open the model and squash to the side.



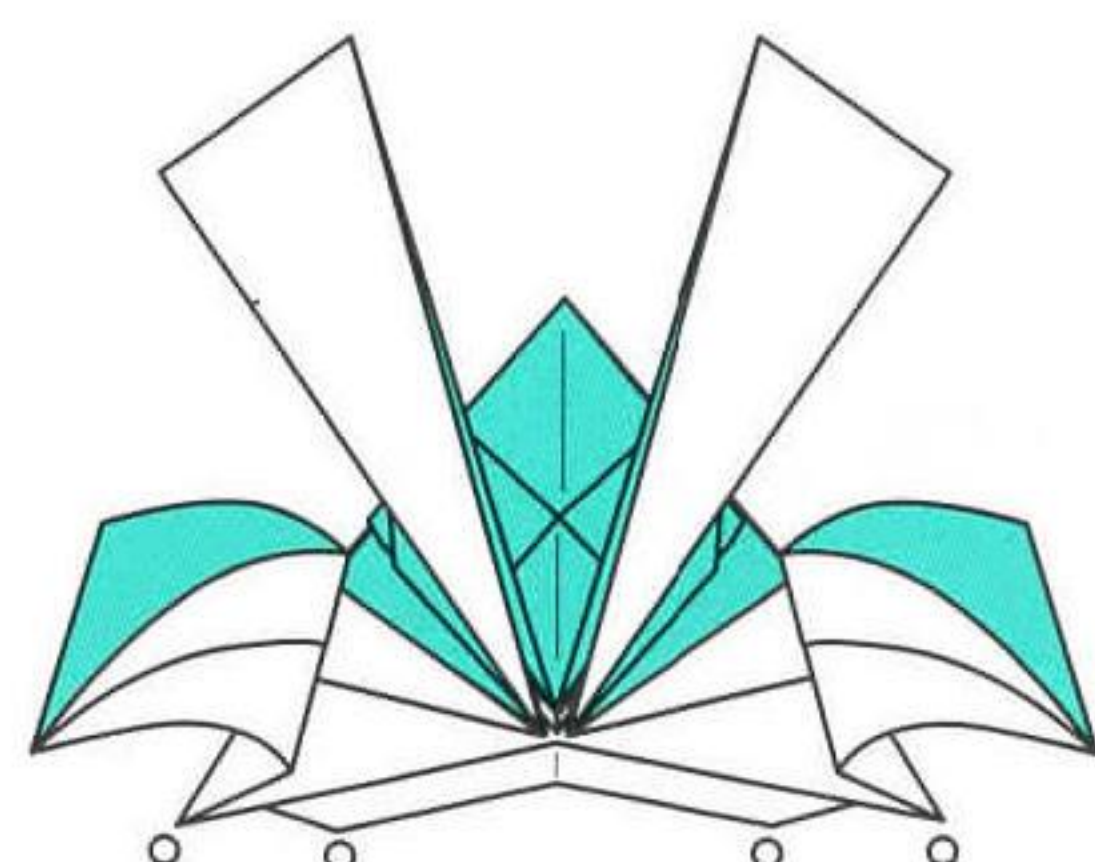
26



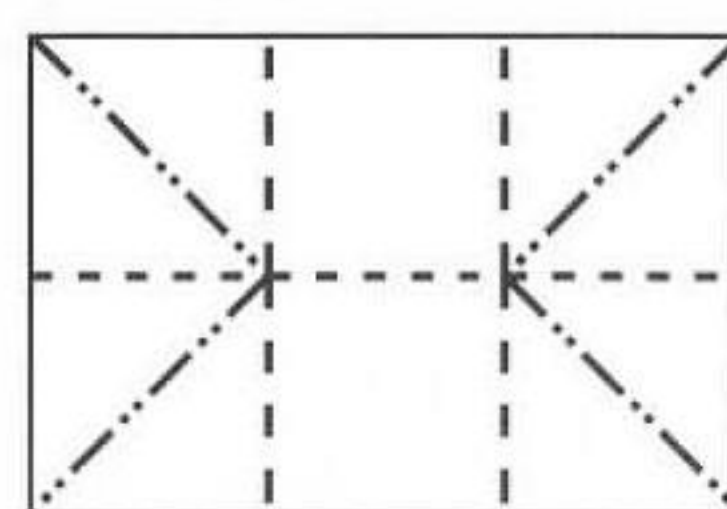
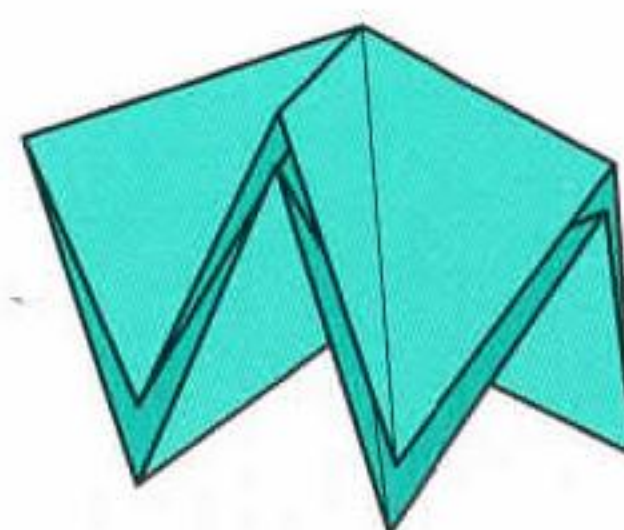
27

Curl the ears.

Open to make the model 3D.



Finished. The model should stand on the four points.



Tridacna

Half-open

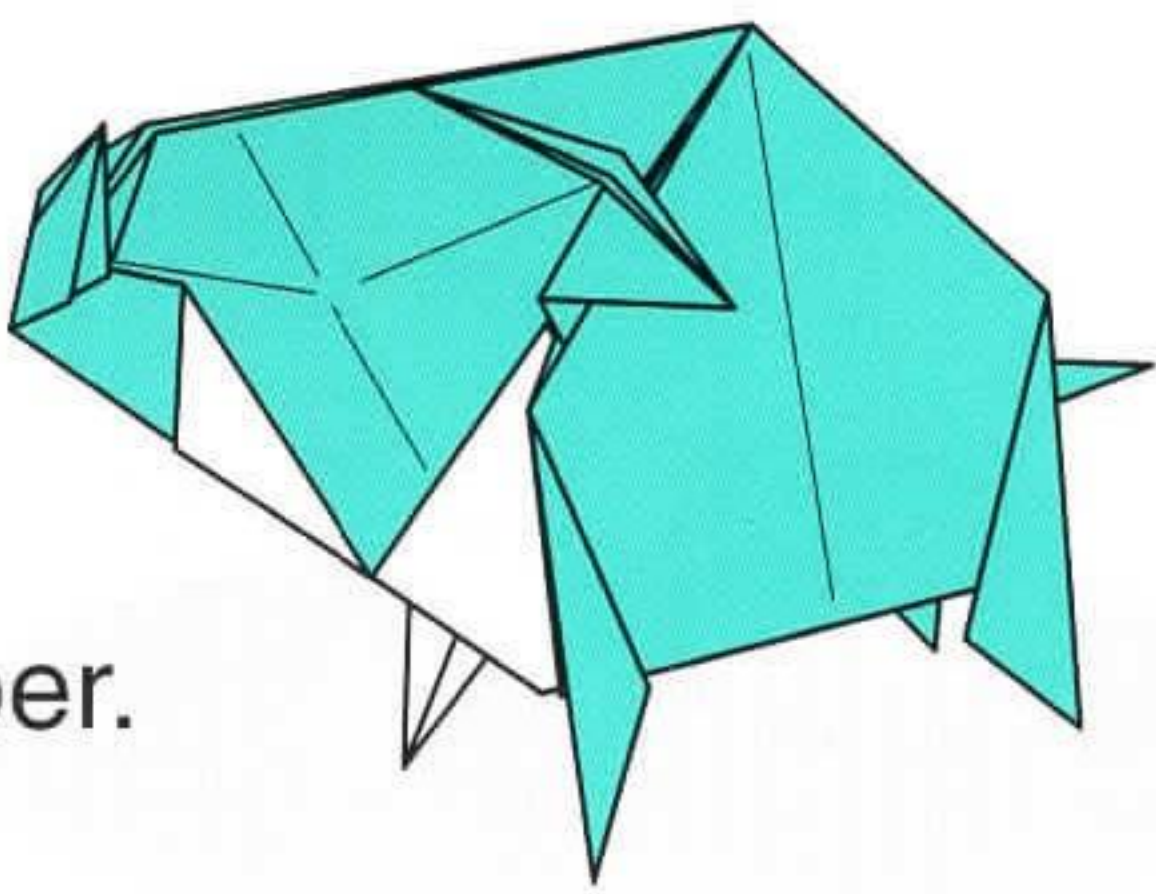
This Samurai Helmet is three-dimensional model, and basically a quadrangle pyramid without a bottom. Of course, helmets do not have a bottom.

Such technique of making 3D models can be called **half-open**.

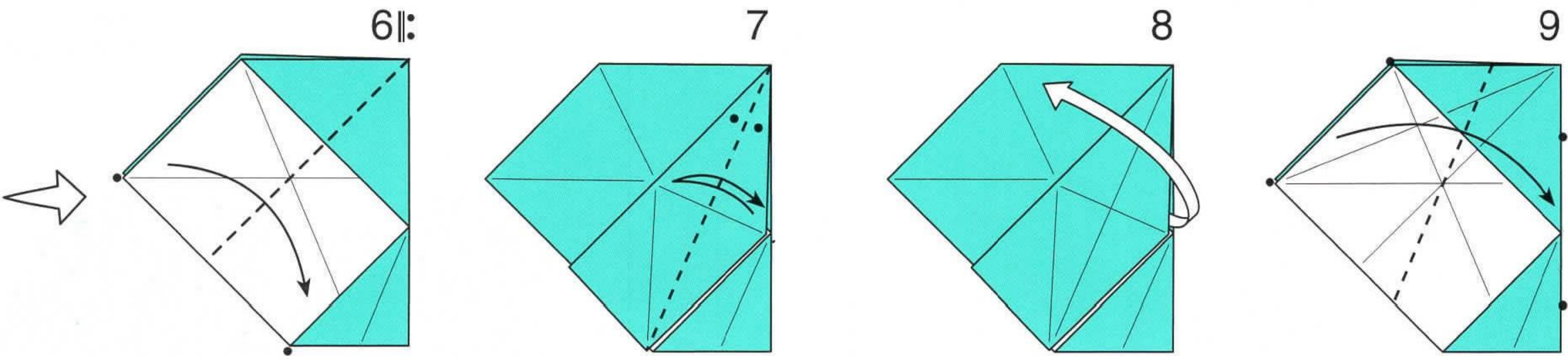
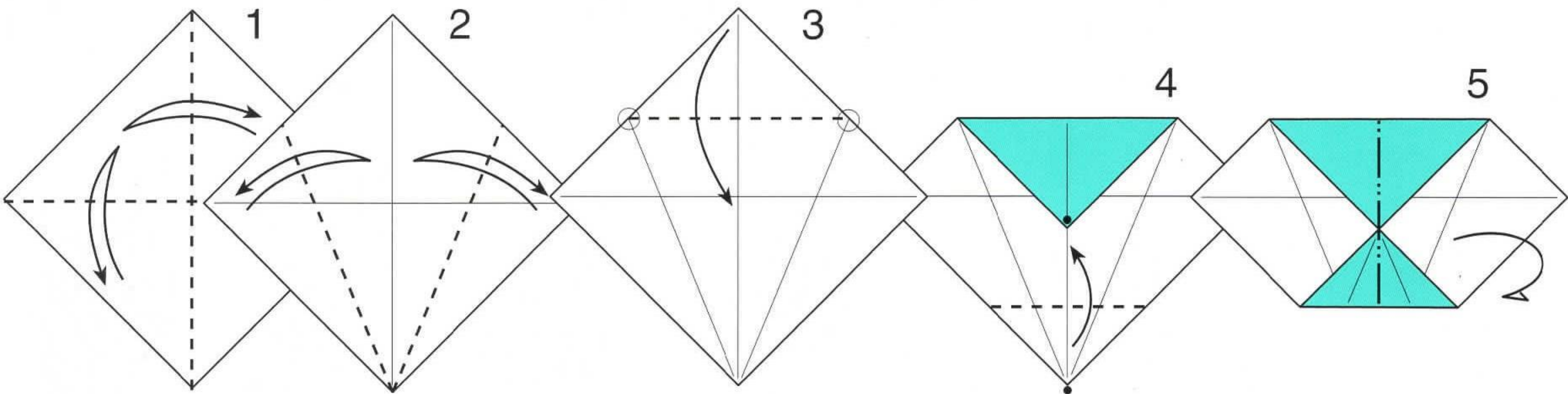
Kunihiko Kasahara makes use of this technique in the most pure form and calls it **half-open folding**. My Tridacna on the left, folded from a 3 : 2 rectangle, is another example of model using half-open folding.

Wild Boar

Theme: 22.5° and $\sqrt{2}$
Fold using 6" (15 cm) origami paper.

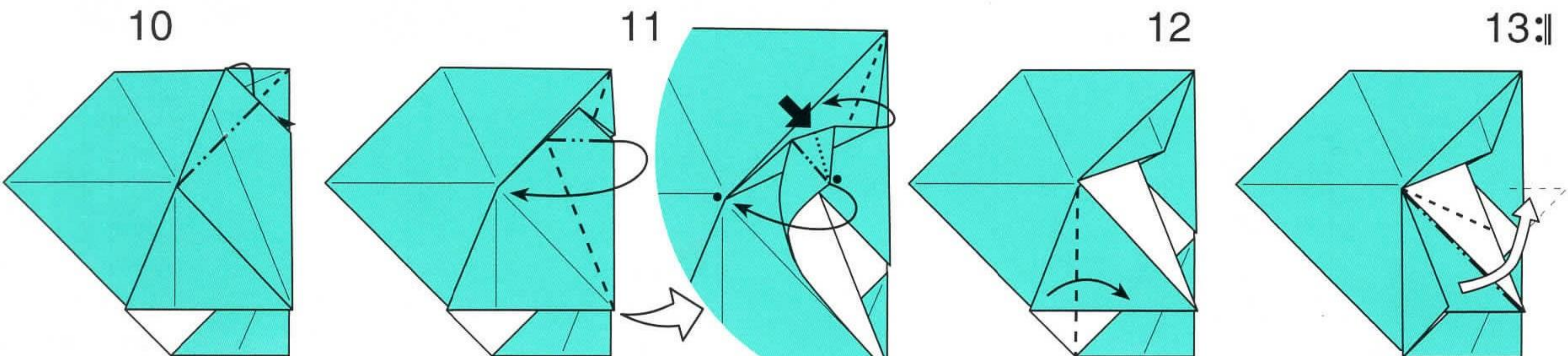


One of the basic angles in origami is 22.5°, which is a quarter of the right angle. This model is based on this angle, as all the creases intersect each other at an angle of 22.5° or its multiples.



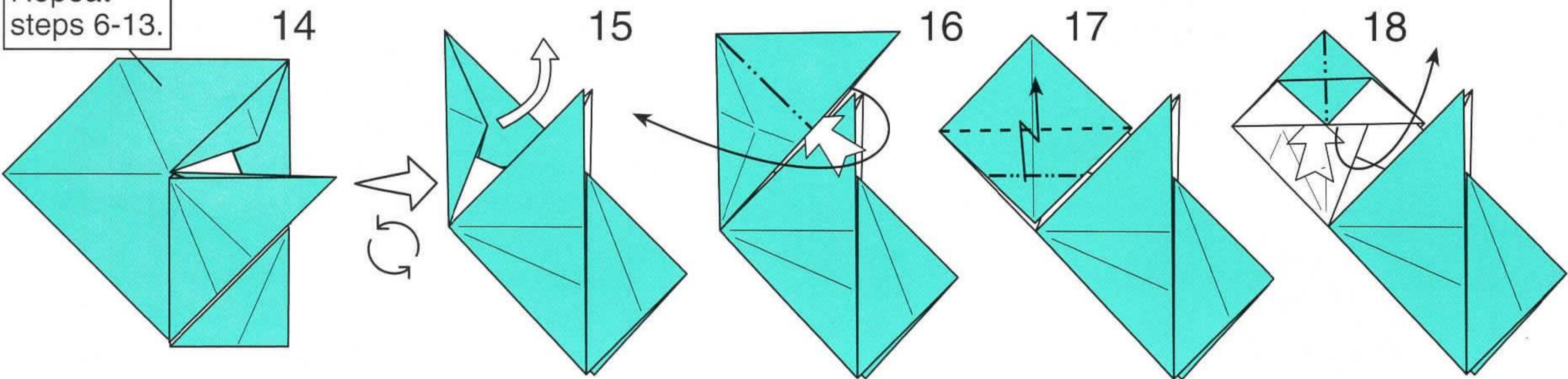
Unfold back to step 6.

Fold edge-to-edge.



Inside reverse-fold

Repeat steps 6-13.



Pull out the corner carefully, paying attention not to tear the paper.

19

20

21

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

Finished.

Lift the nose to face forward.

1

2

3

4

5

$\sqrt{2}$
1
22.5°

22.5° and $\sqrt{2}$

If you pay close attention to this model, you will notice that all the creases intersect each other at an angle of 22.5° or its multiples. You will find a lot of triangles such as those shown on the left.

The 22.5° angle, which is a quarter of the right angle, is the most common angle in origami. Being familiar with these five types of triangles is helpful to fold neatly. For example, you bisect triangle 3 to make triangles 2 in step 34, and you make triangle 5 in steps 35-36. Note that triangles 1 and 2 are the most basic as the other three are composed of those two.

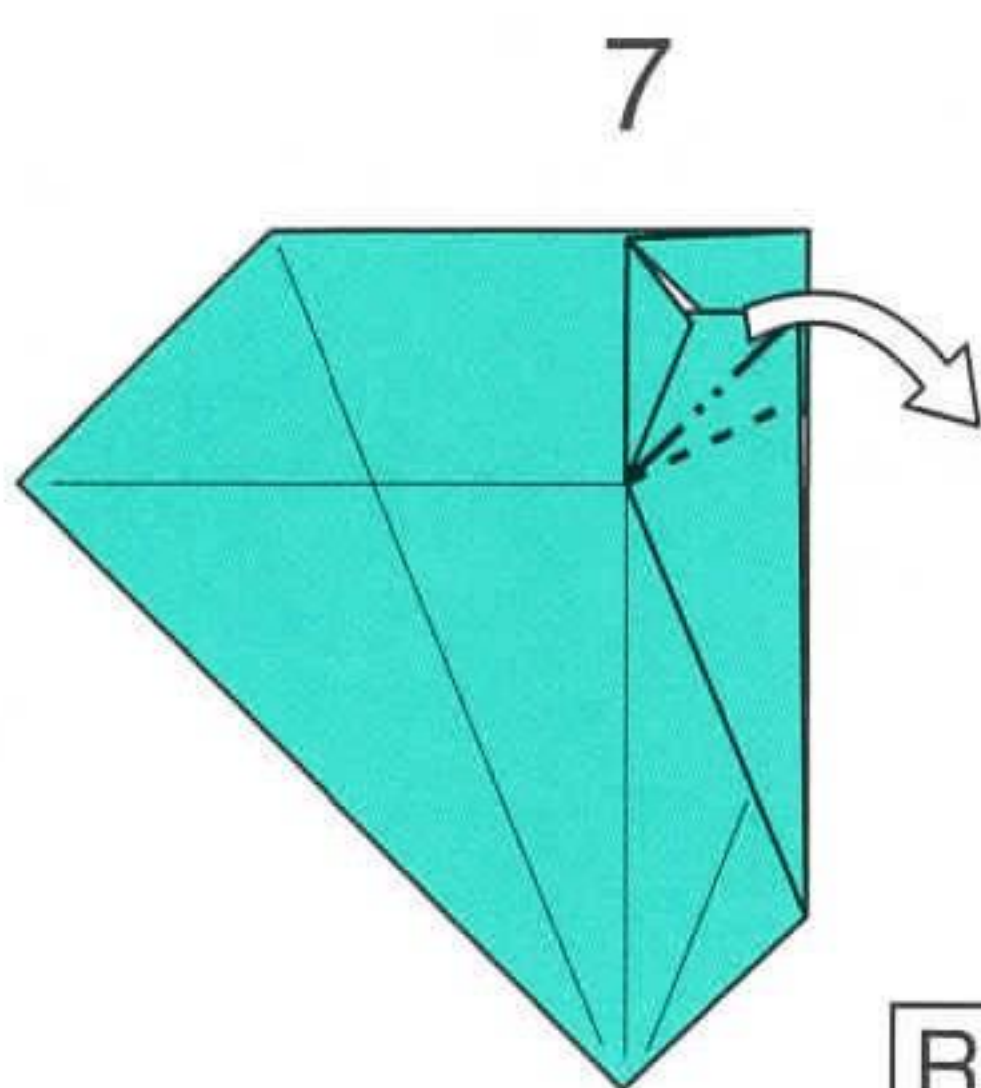
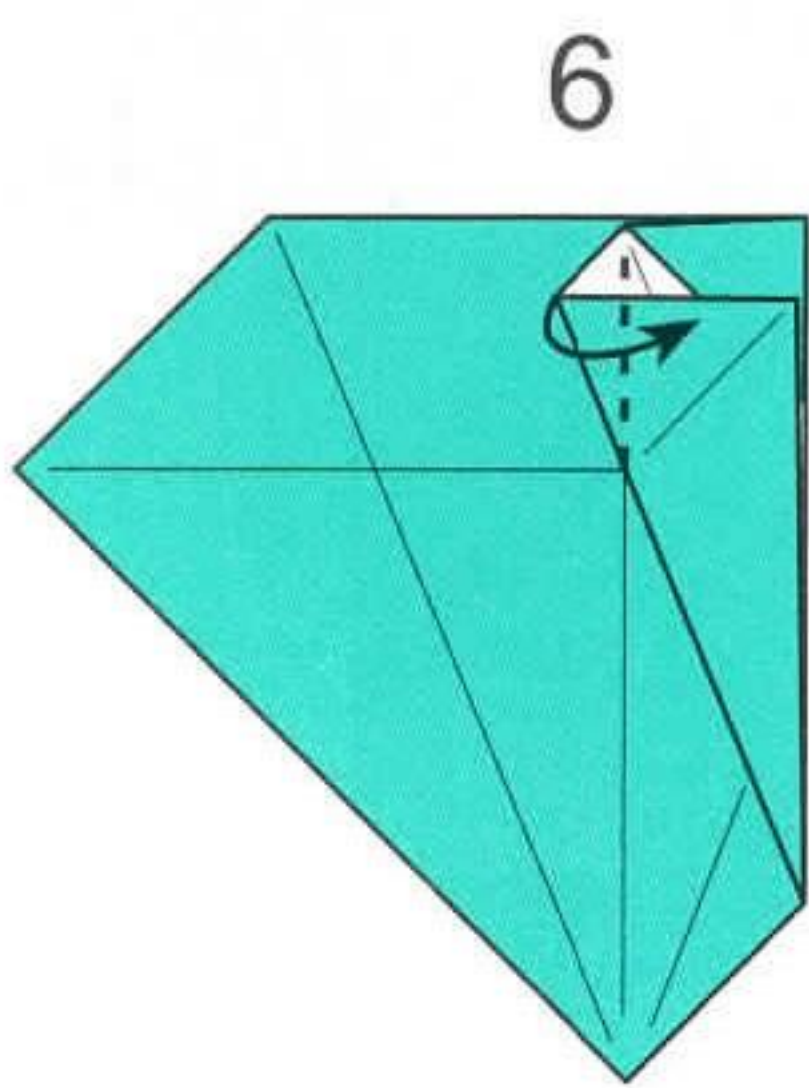
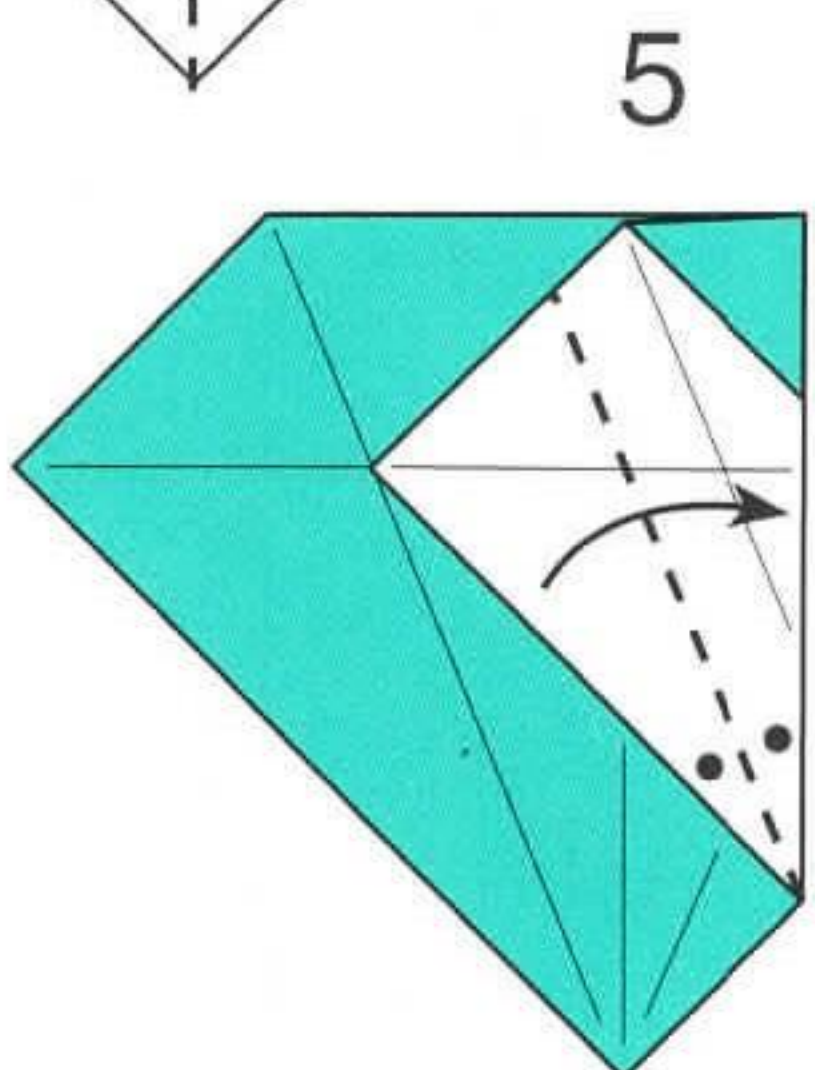
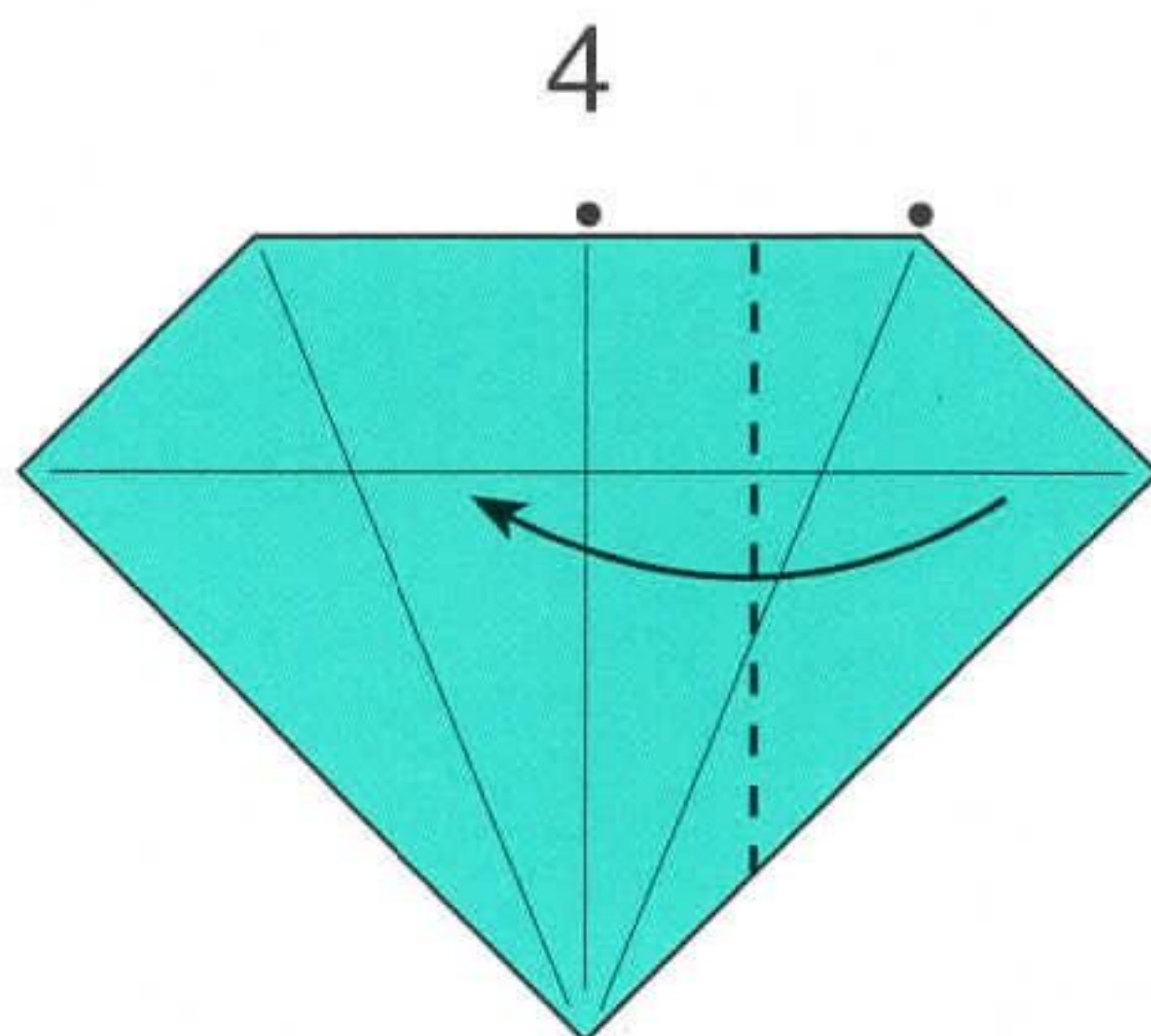
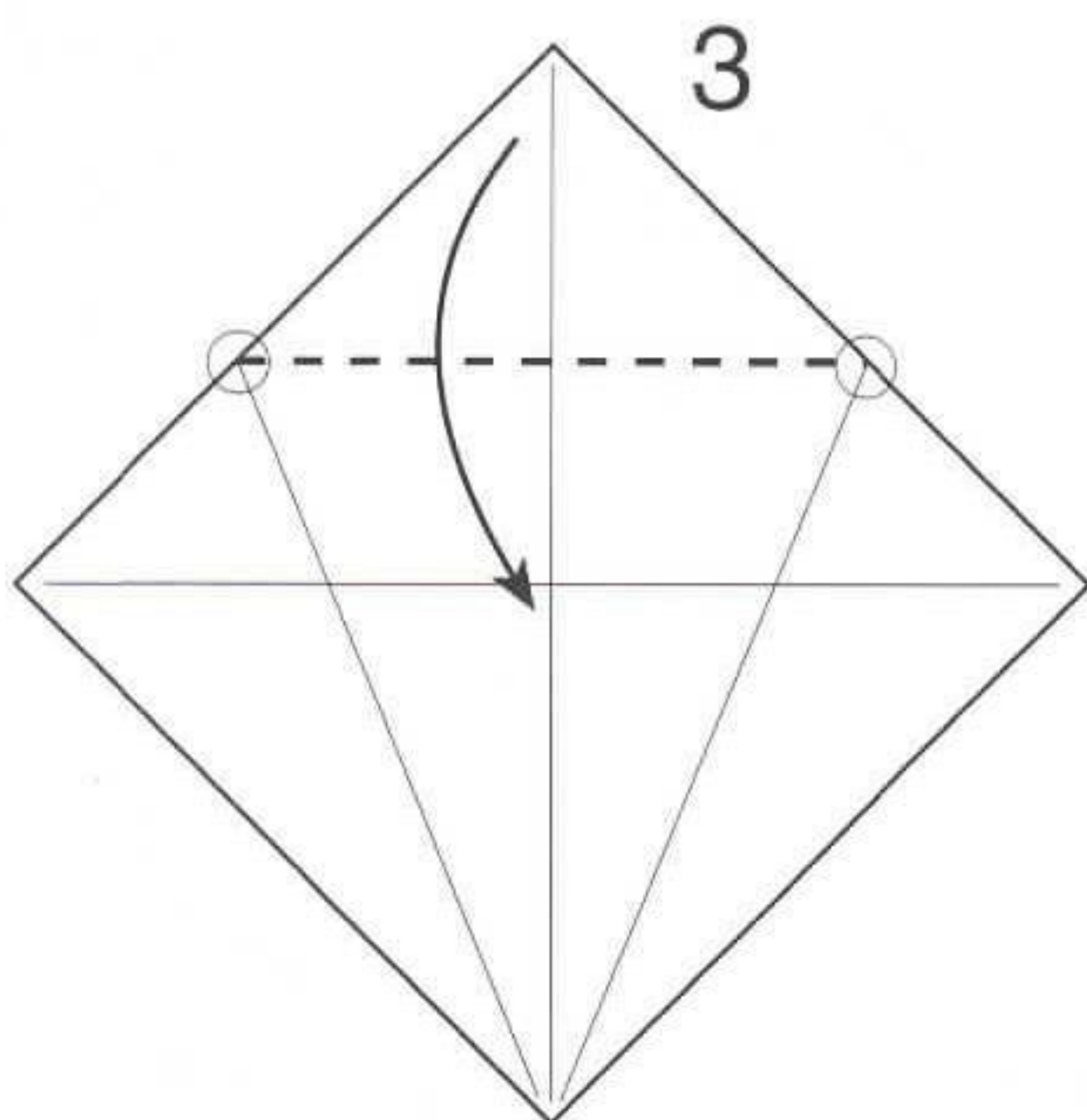
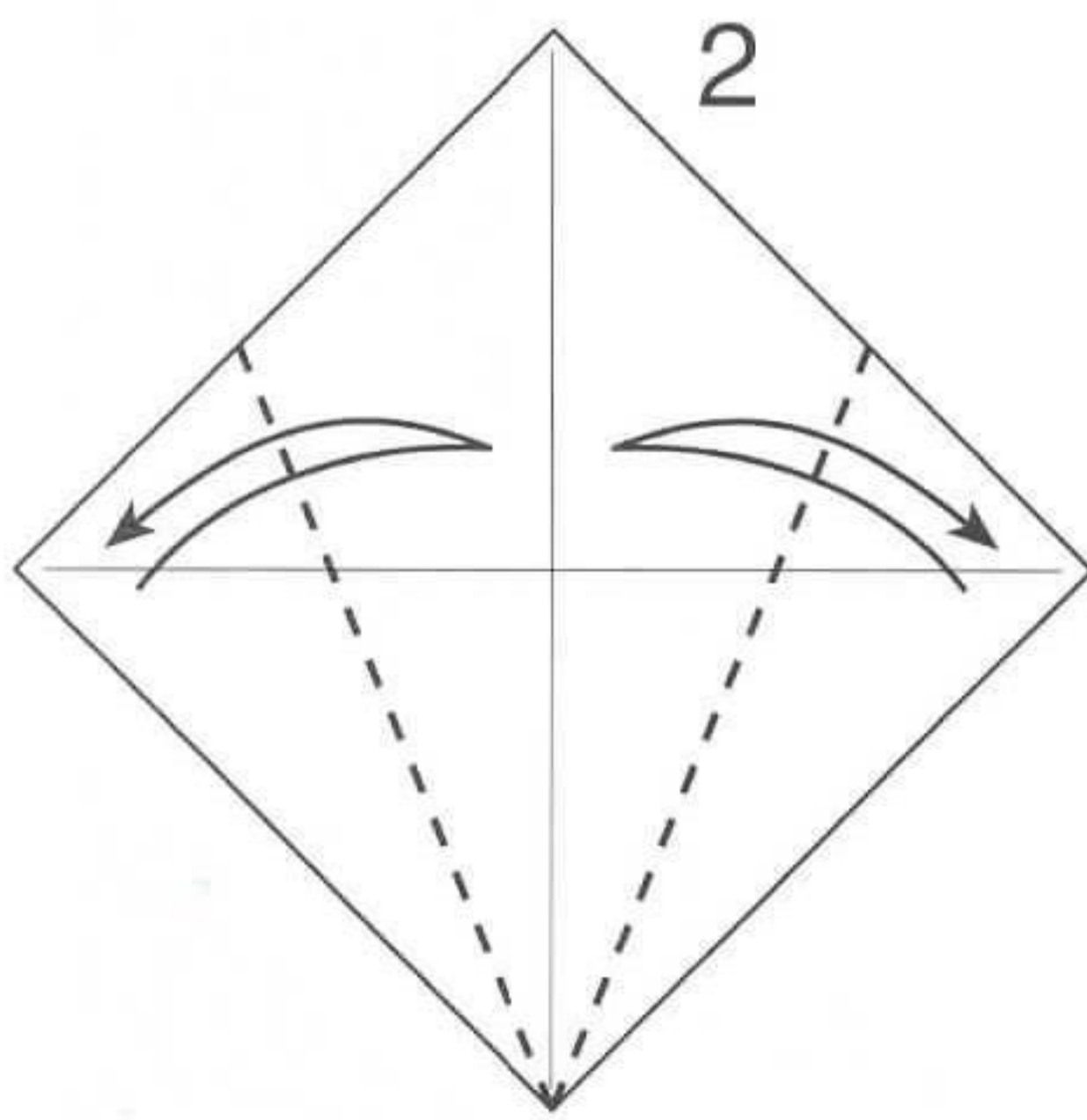
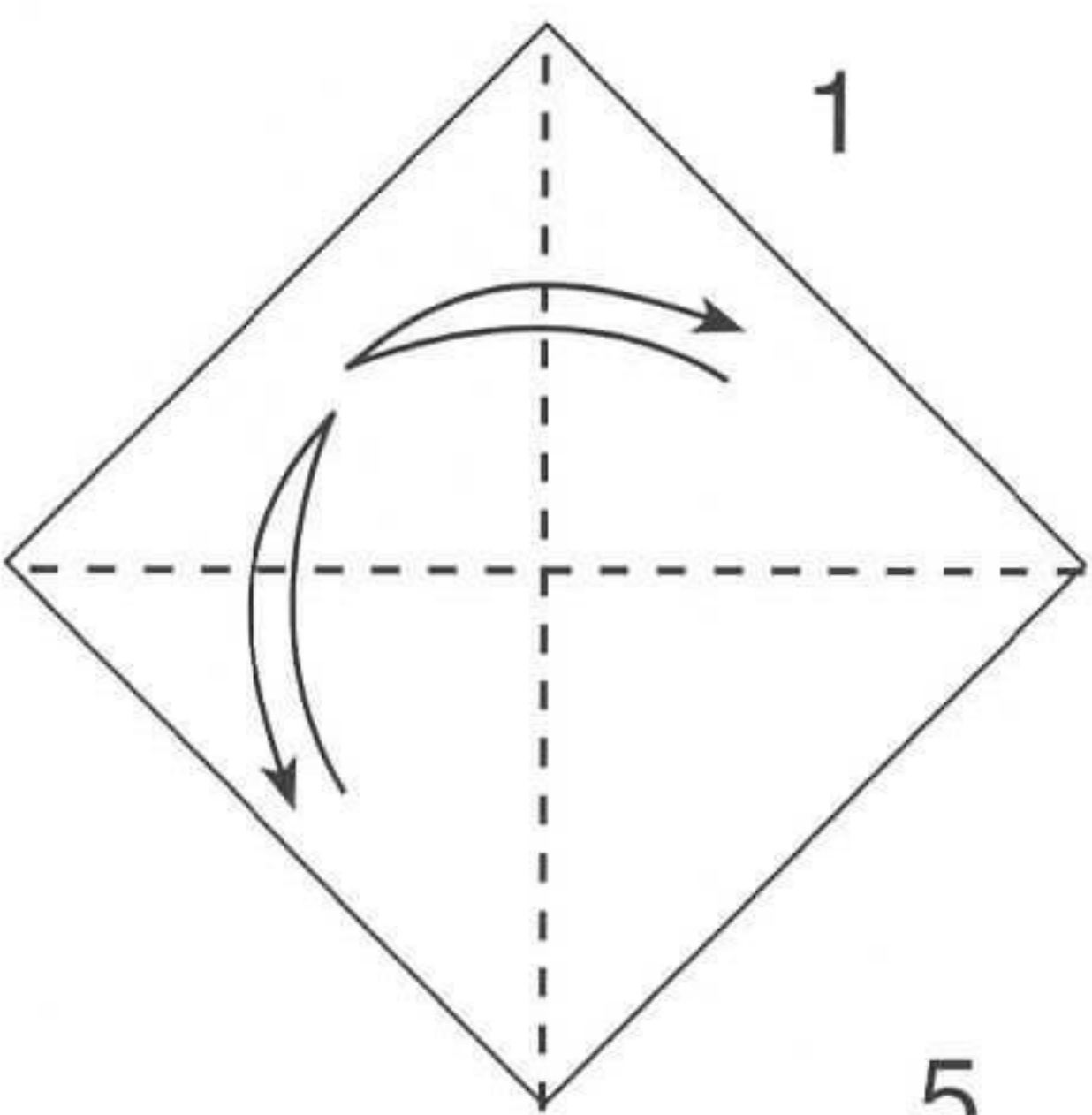
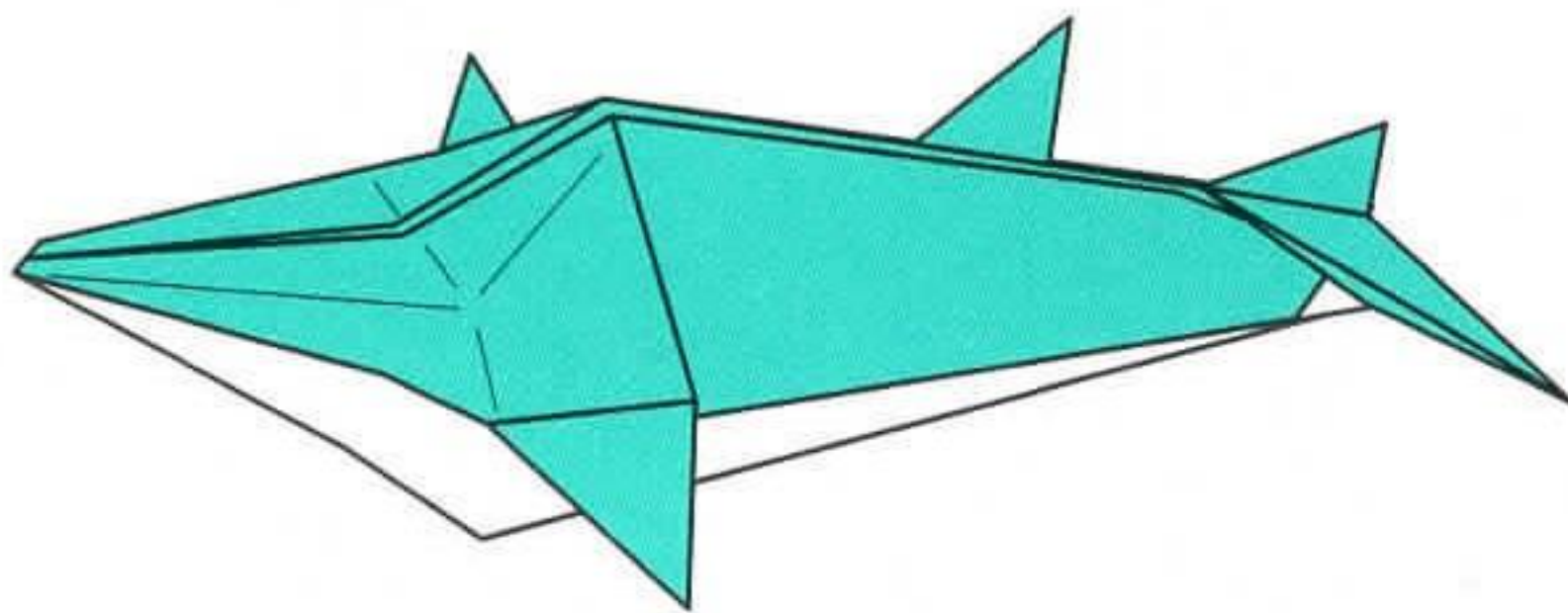
The 22.5° angle closely relates to $\sqrt{2}$ (=1.414...). One example of such relationship is shown on the left. The 22.5° crease line in a square divides the side into 1 : $\sqrt{2}$.

Simple Models 37

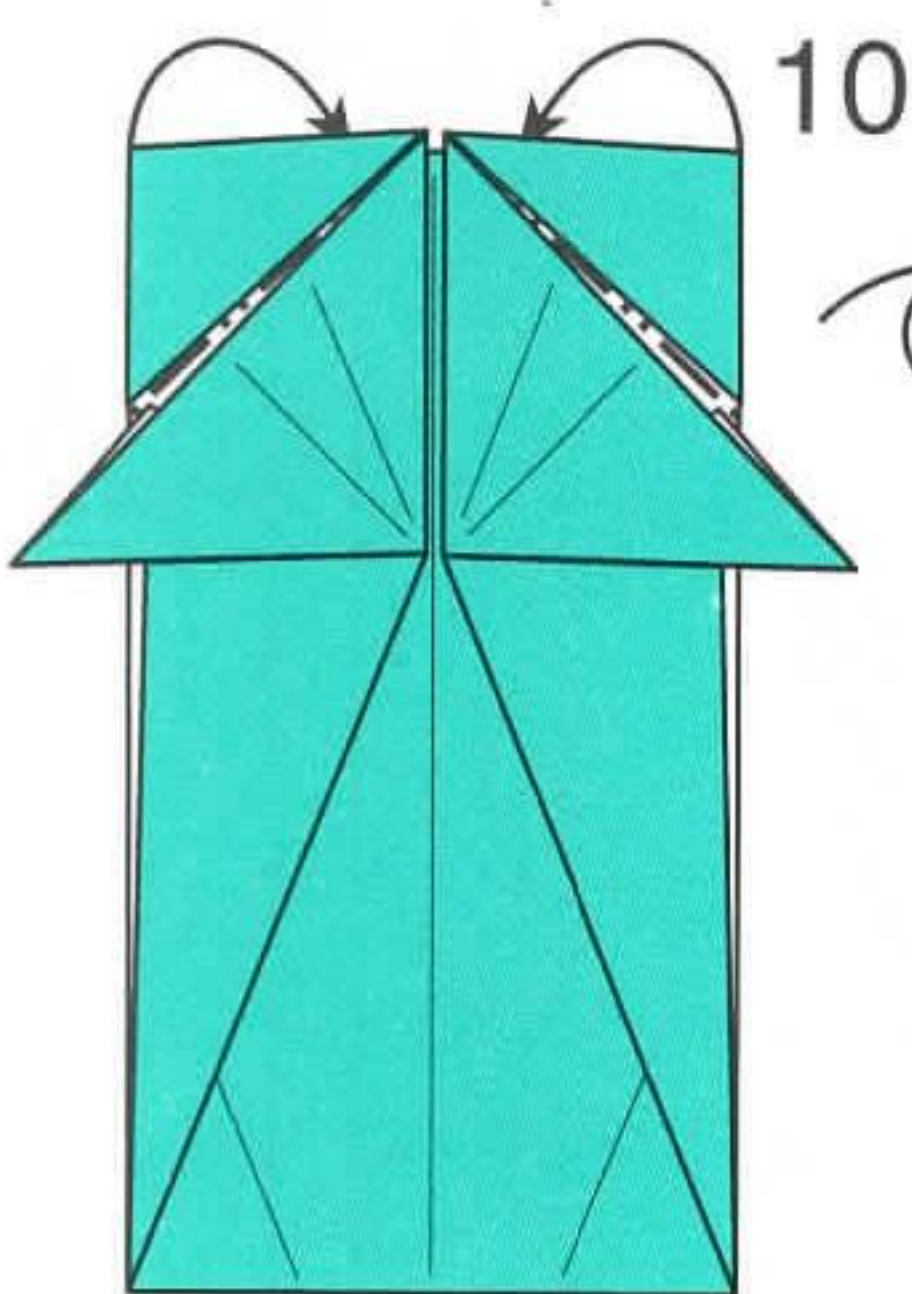
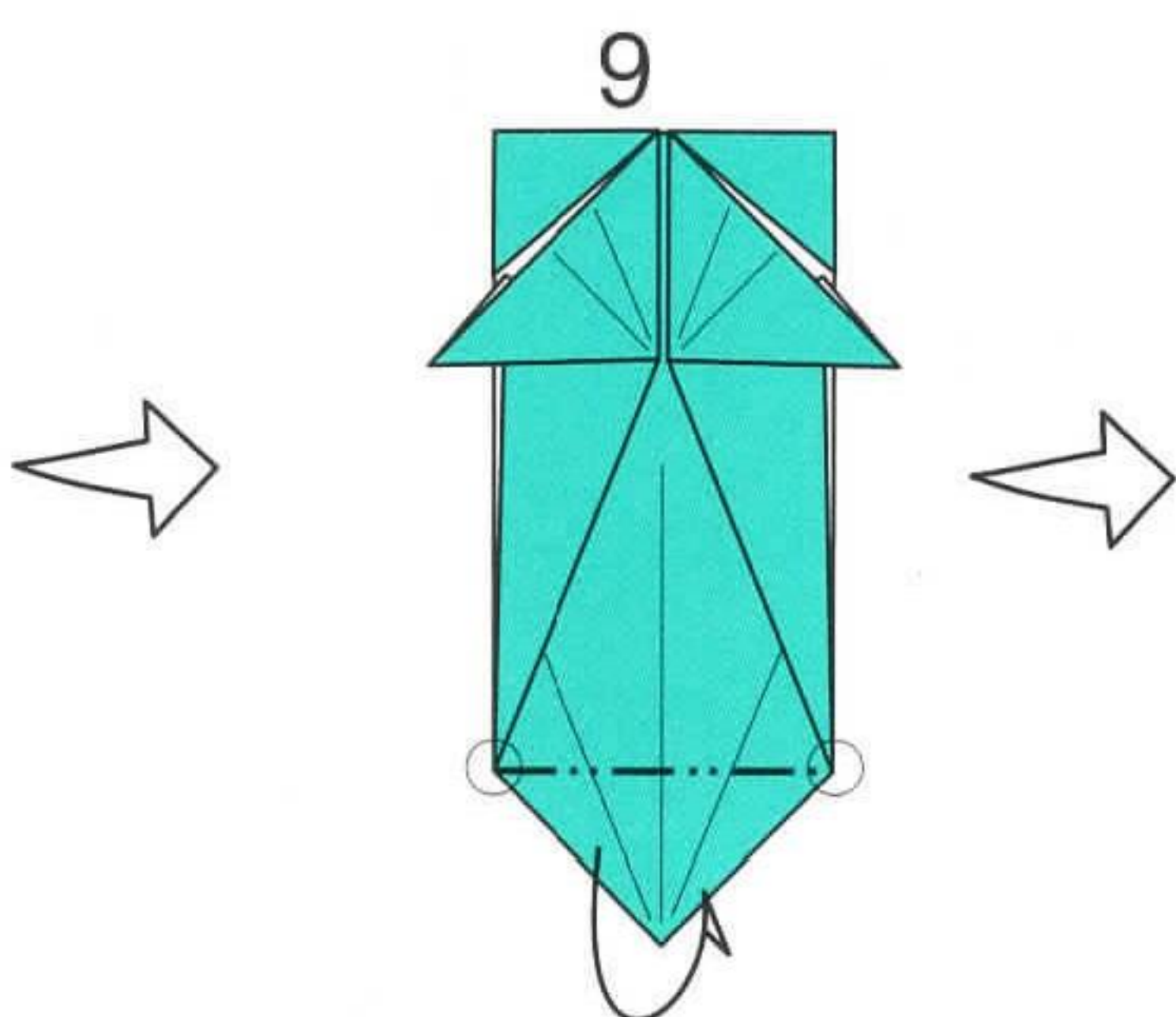
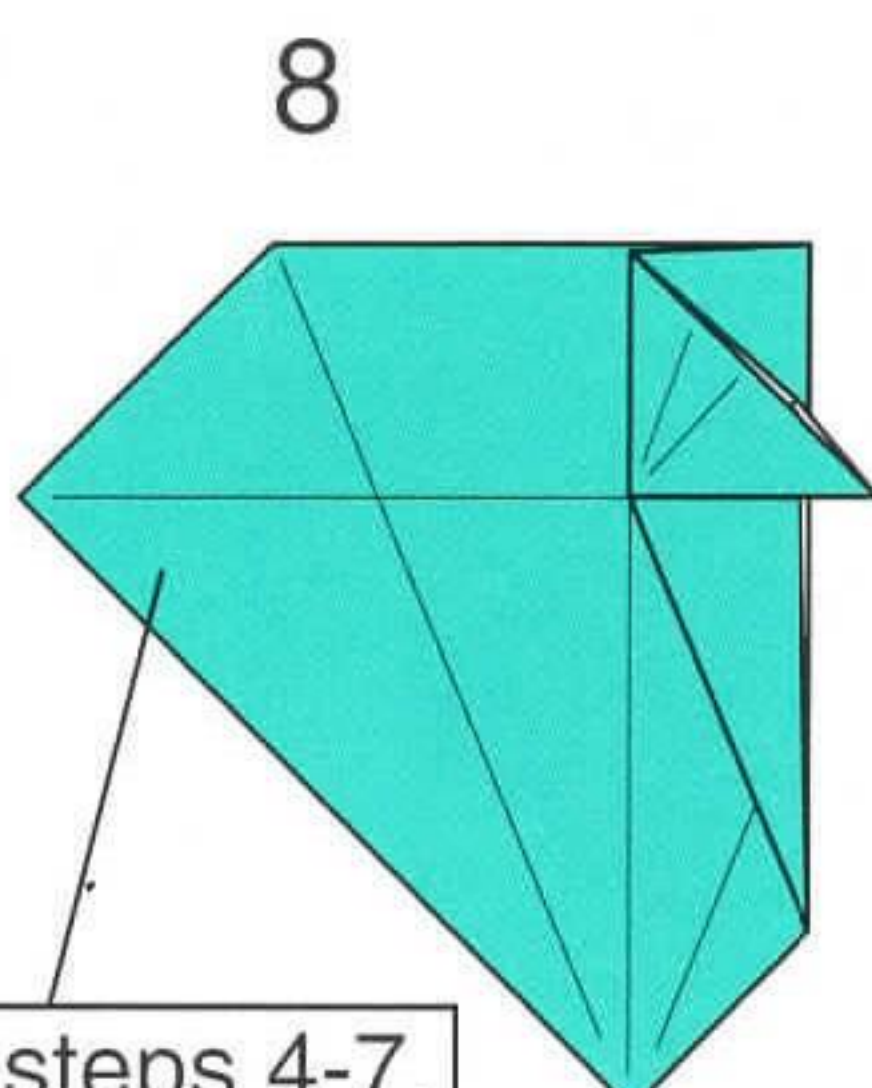
Dolphin

Theme: Shaping

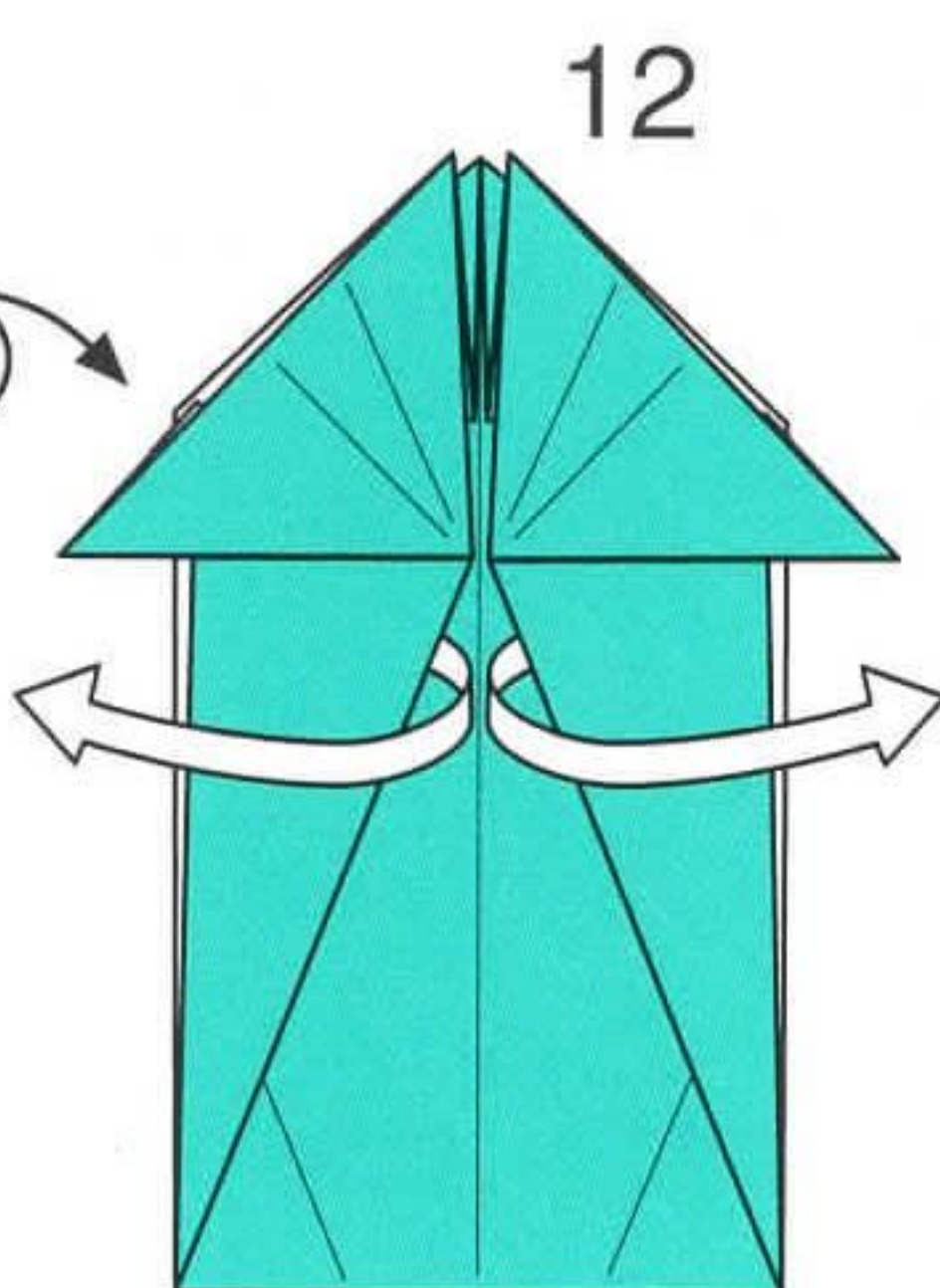
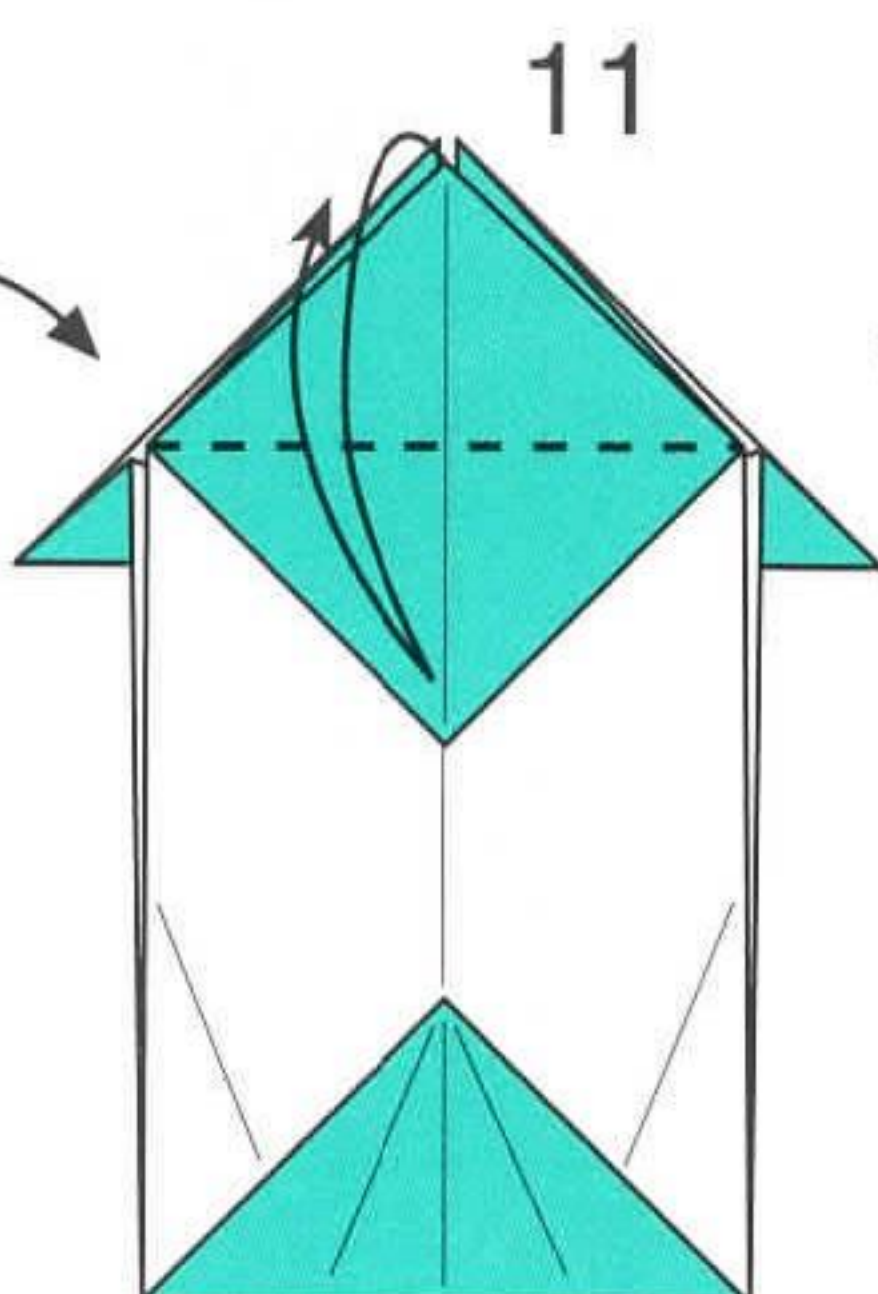
Fold using 6" (15 cm) origami paper.



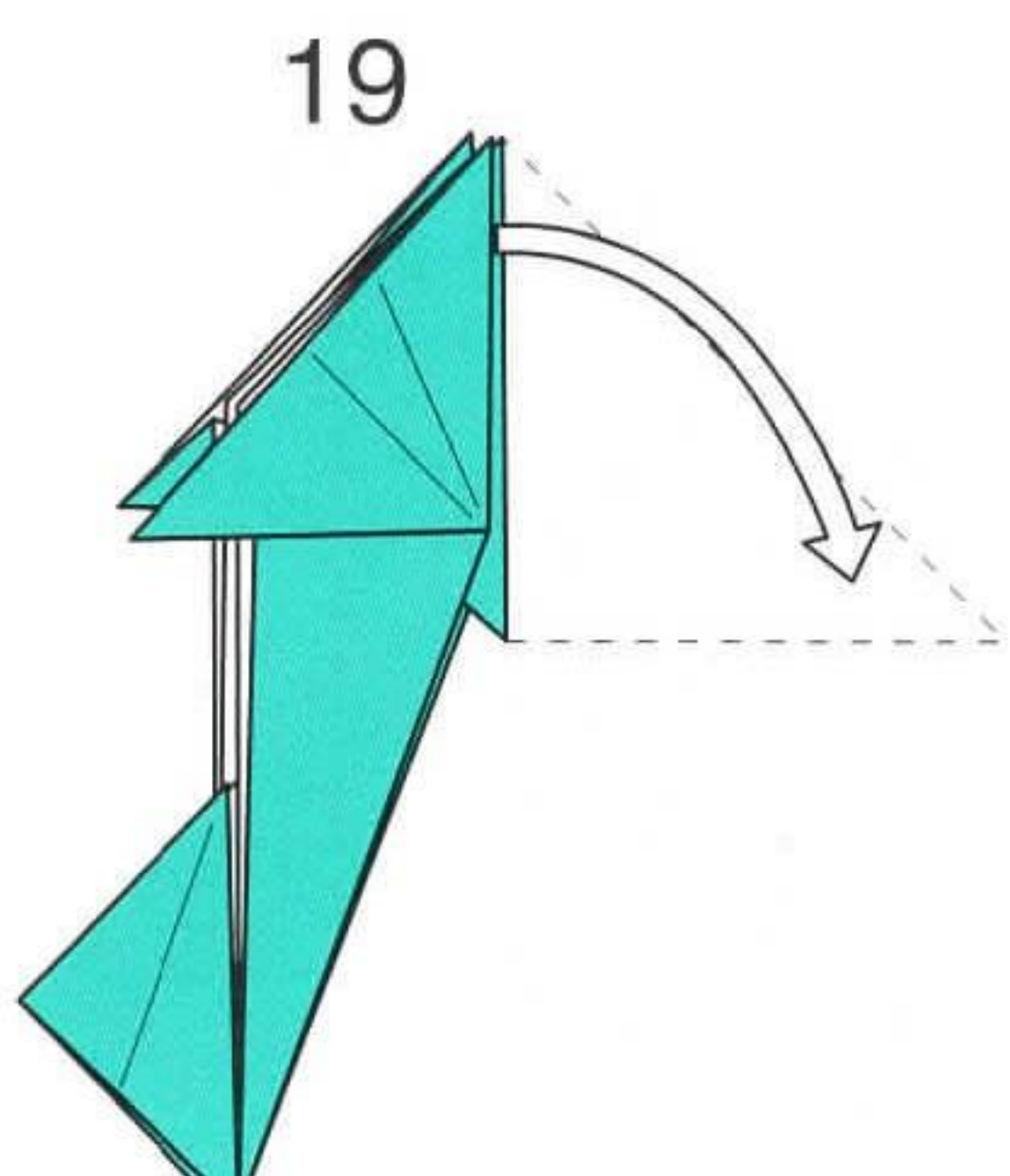
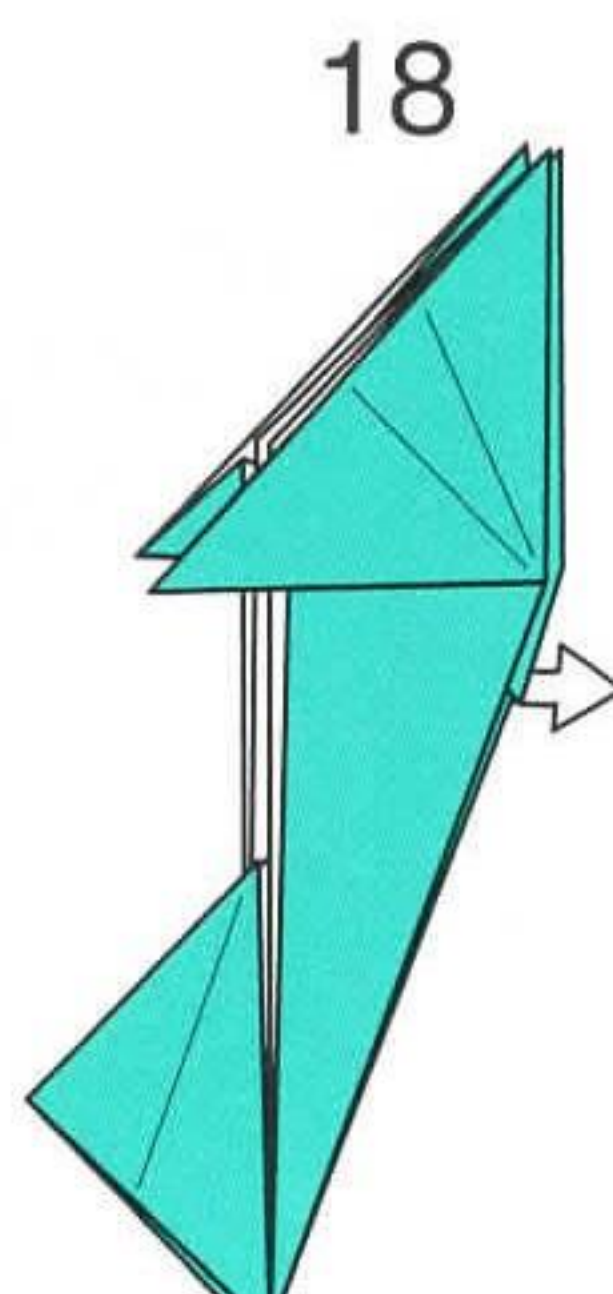
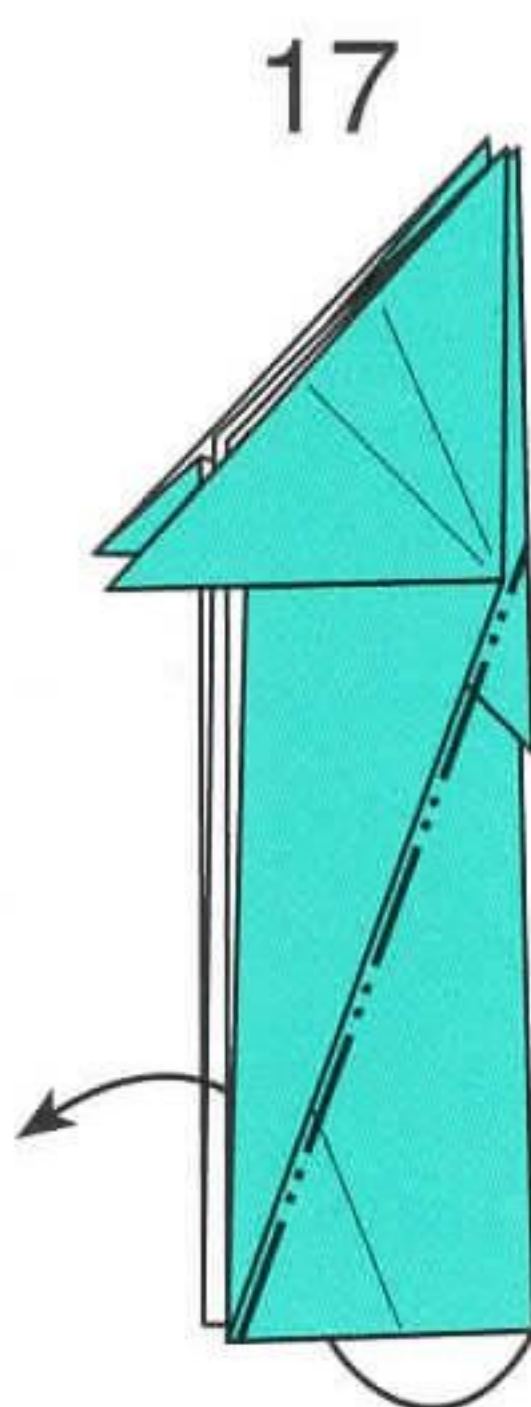
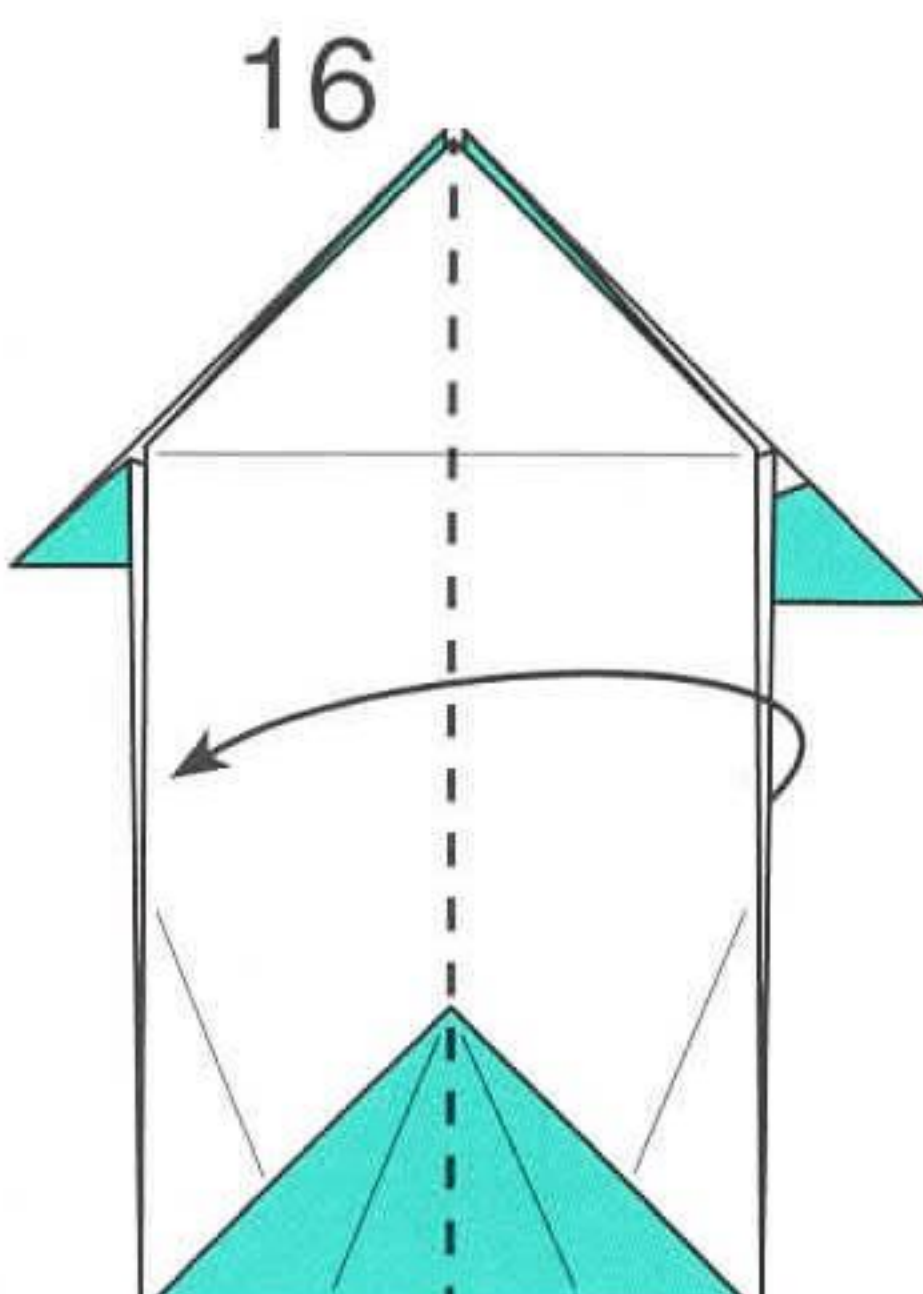
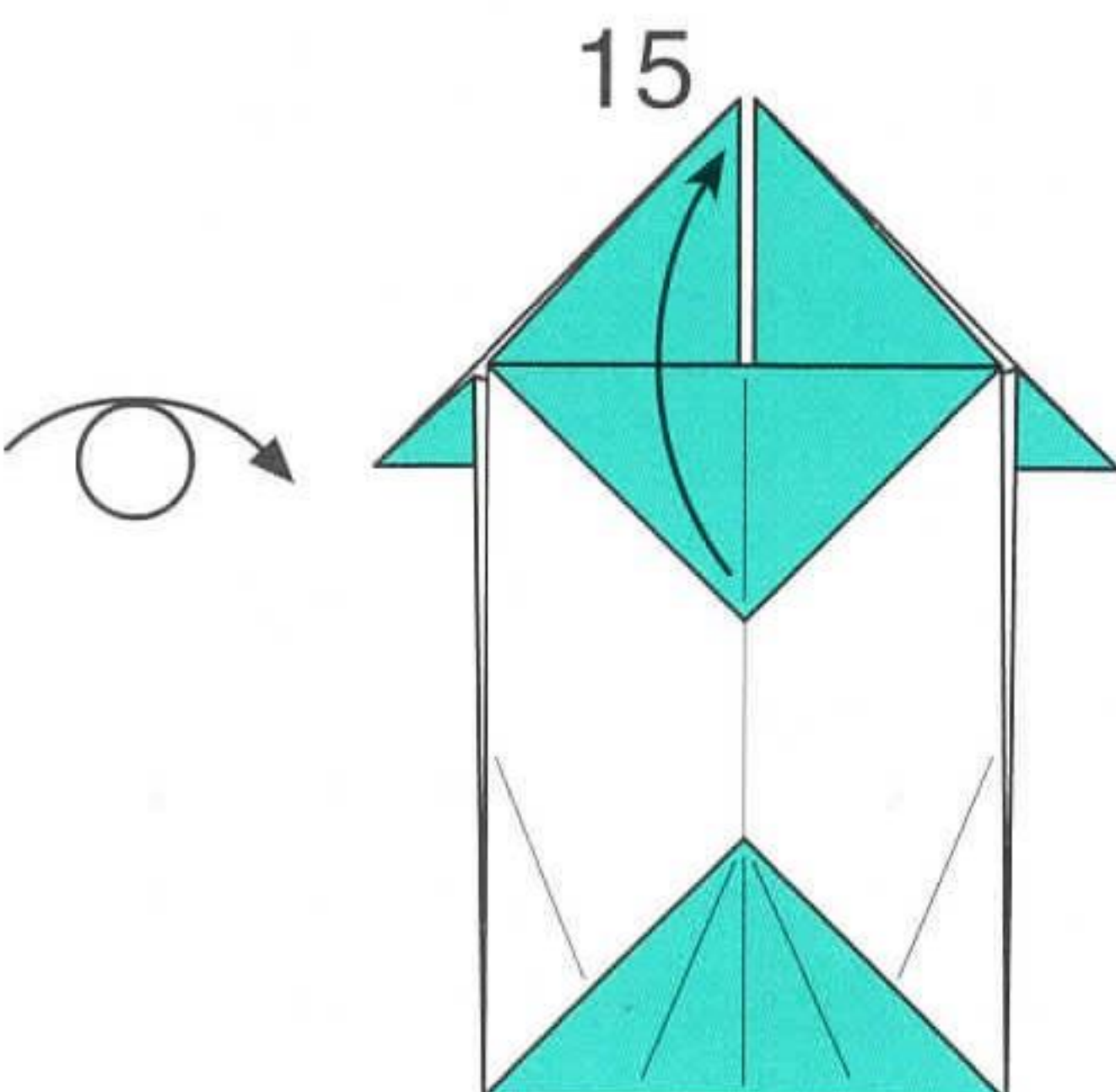
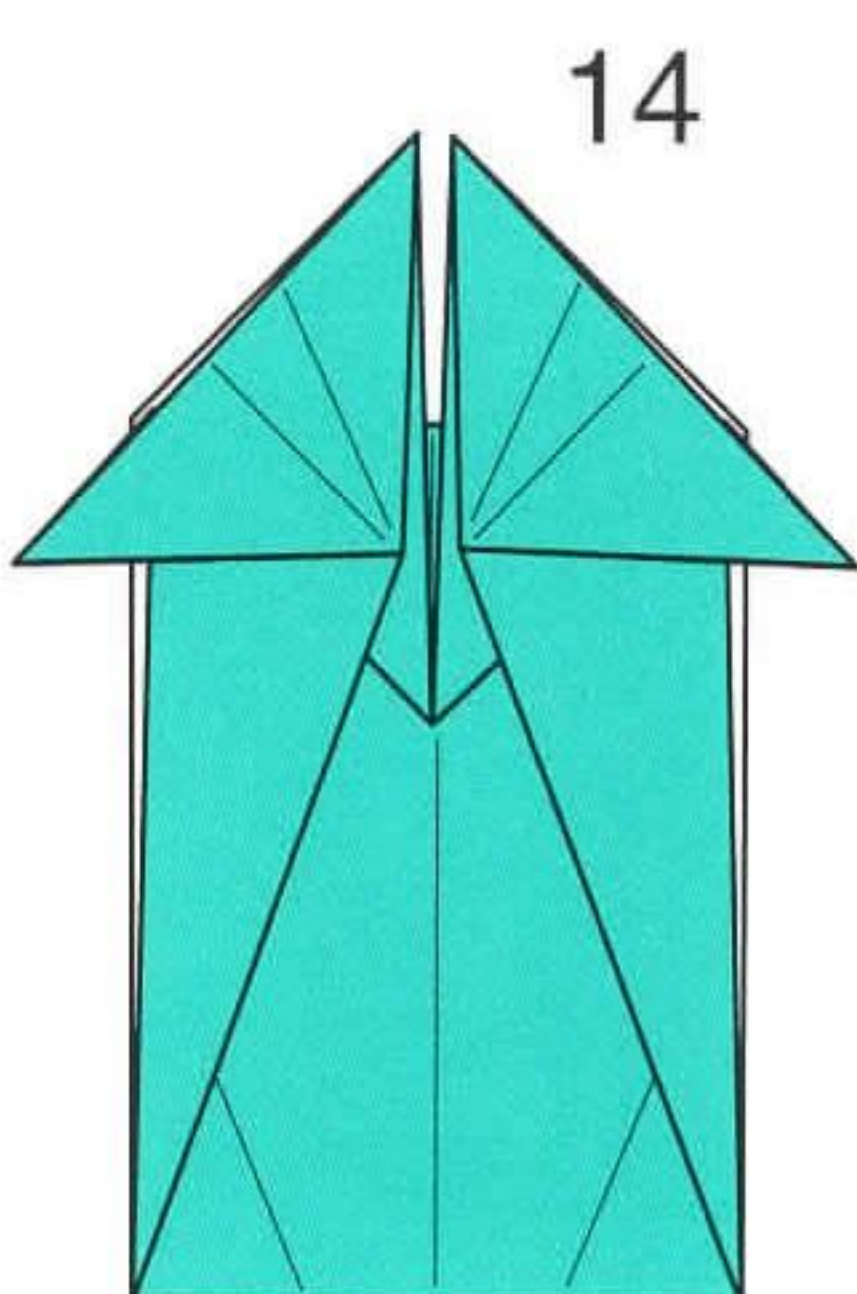
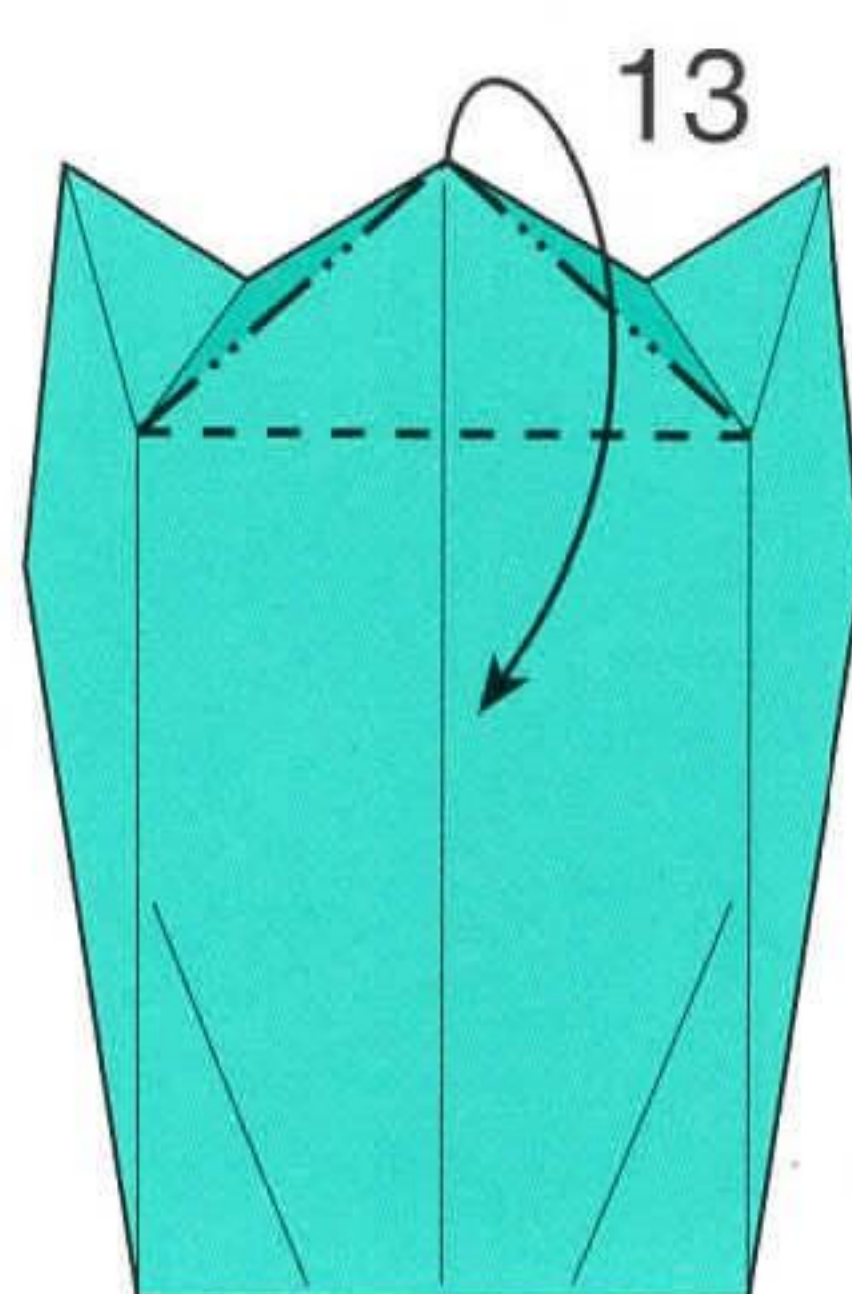
Repeat steps 4-7.



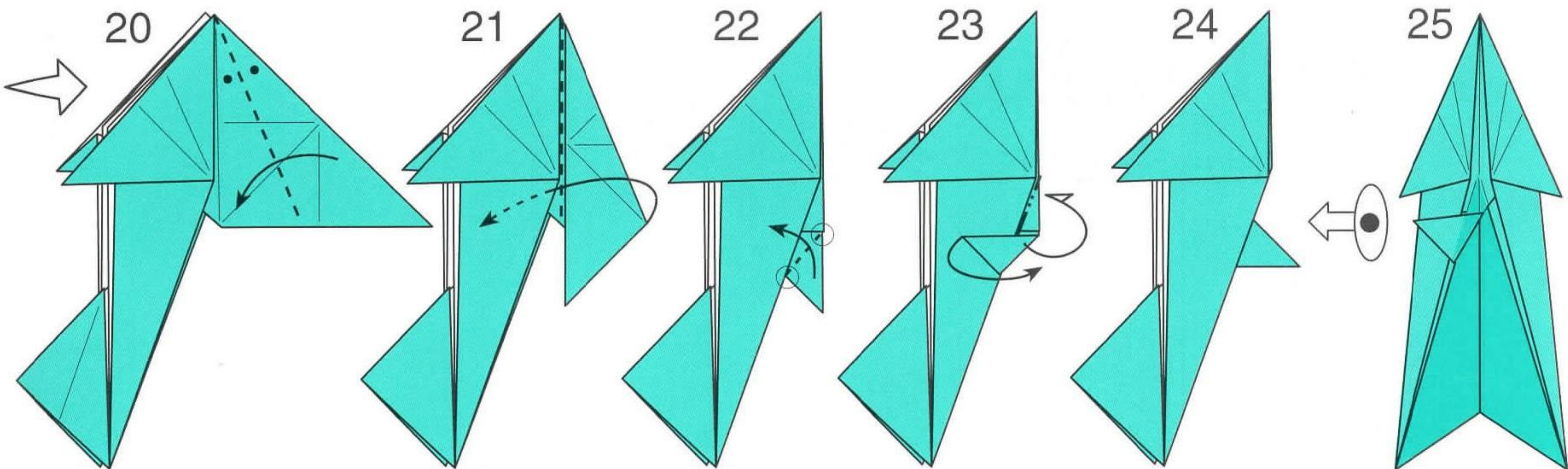
Inside reverse-fold



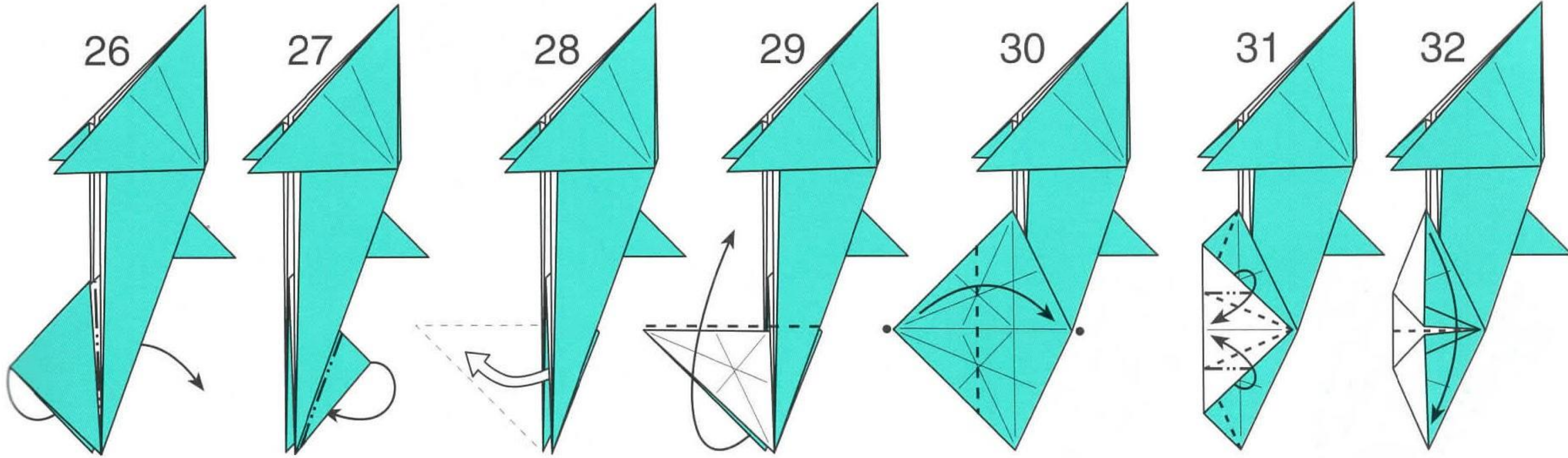
Open the model partially.



Inside reverse-fold



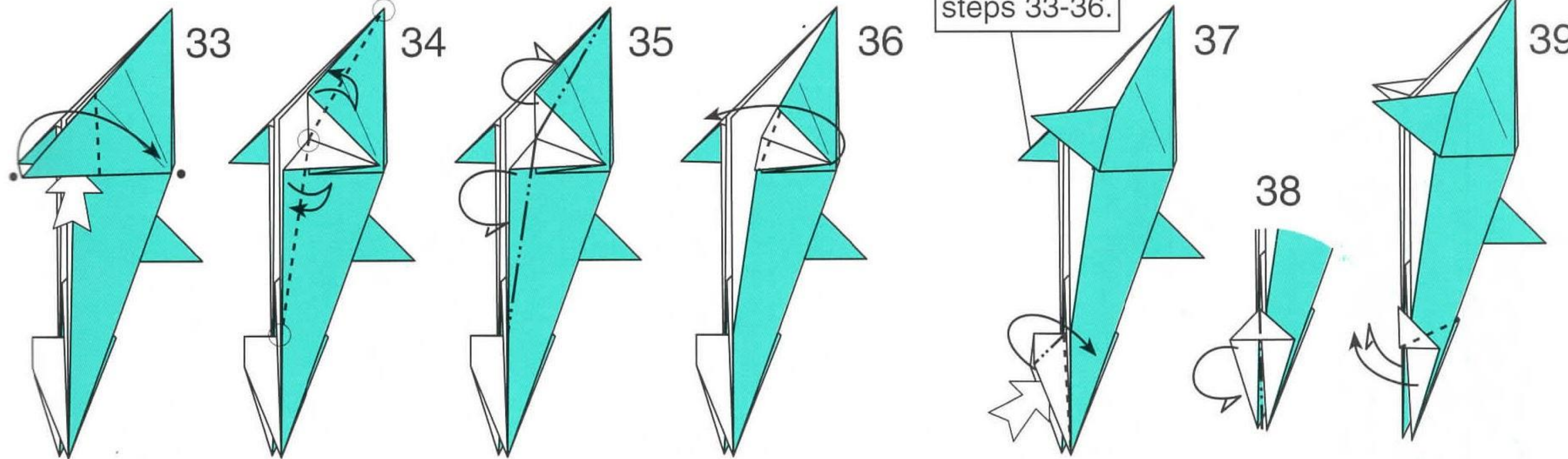
Tuck the small flap into the center pocket.



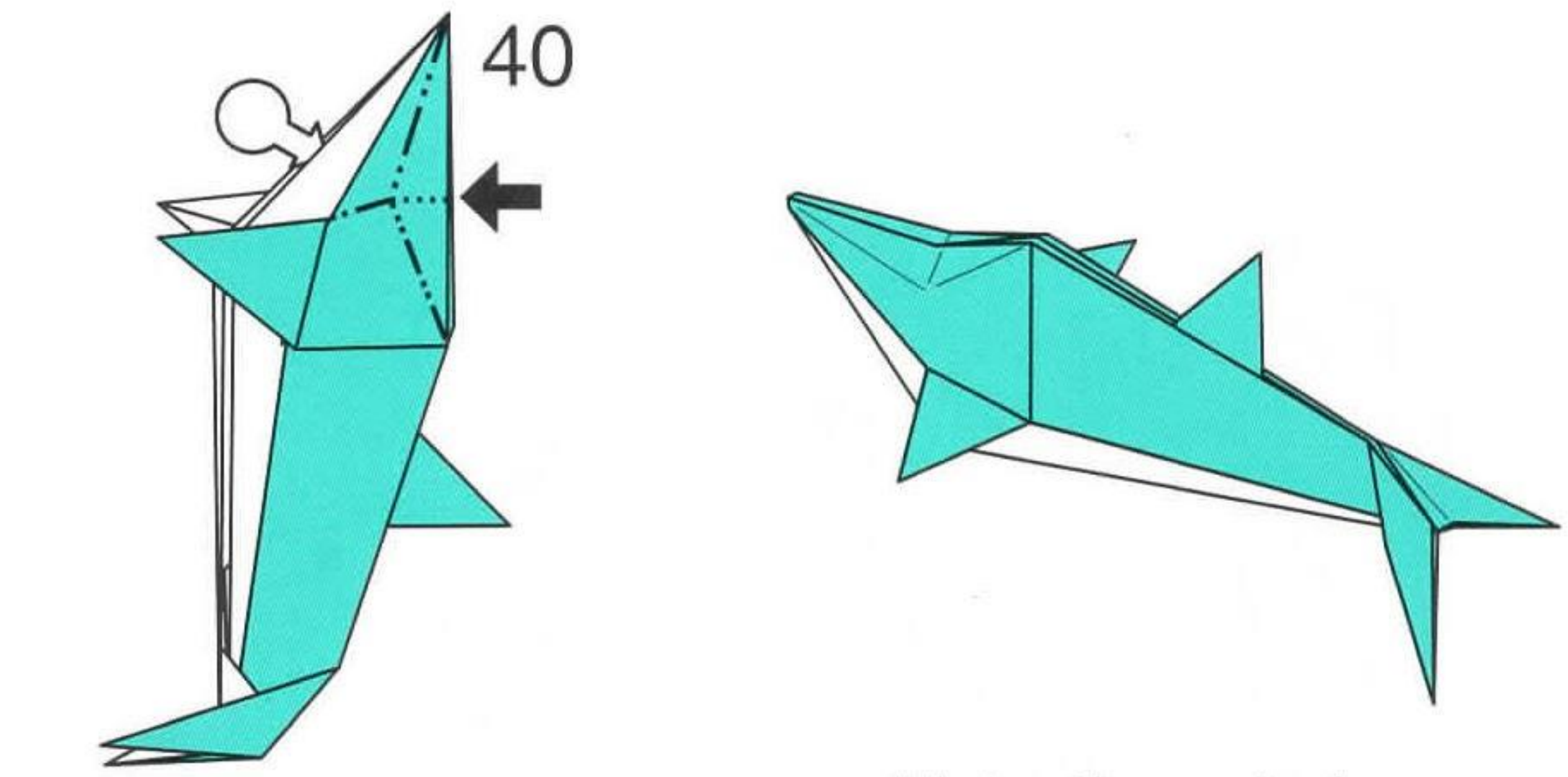
Inside reverse-fold

Inside reverse-fold

Swivel-fold



Repeat steps 33-36.



Using existing creases, pinch the head to make it 3D.

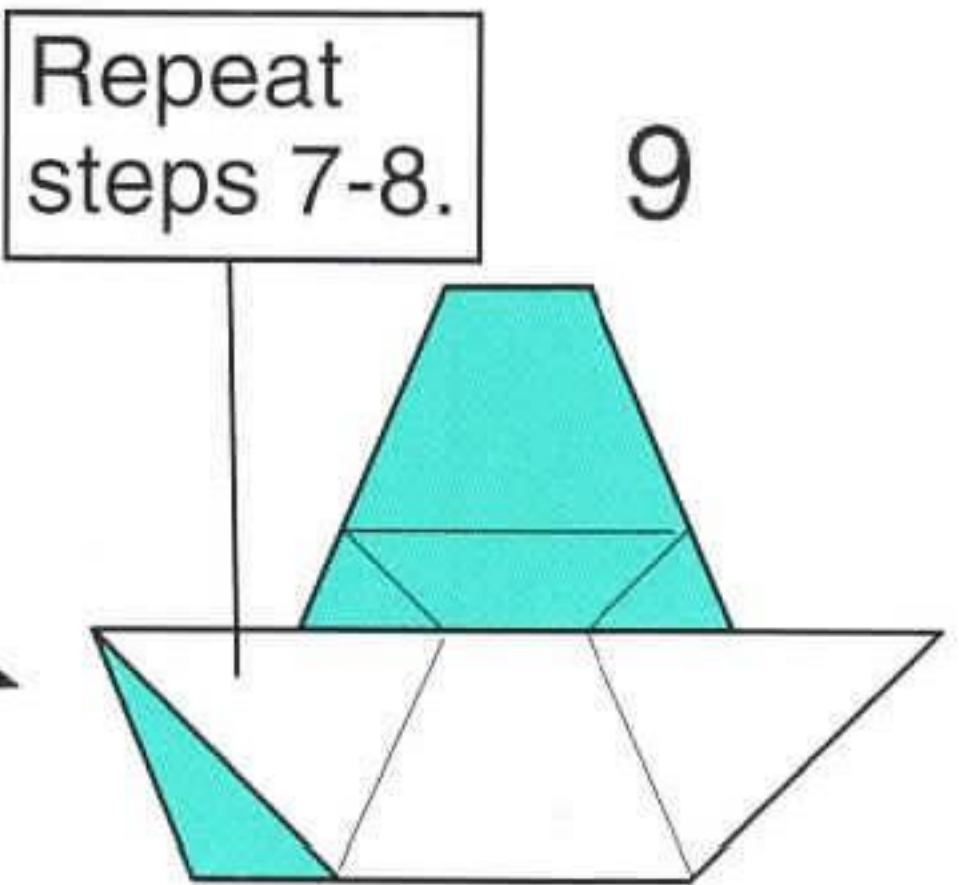
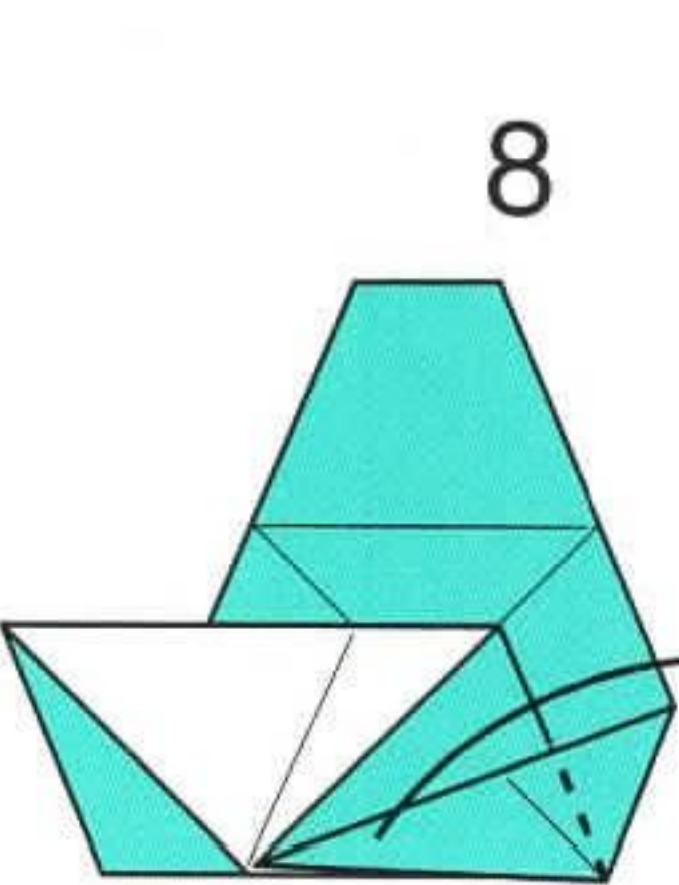
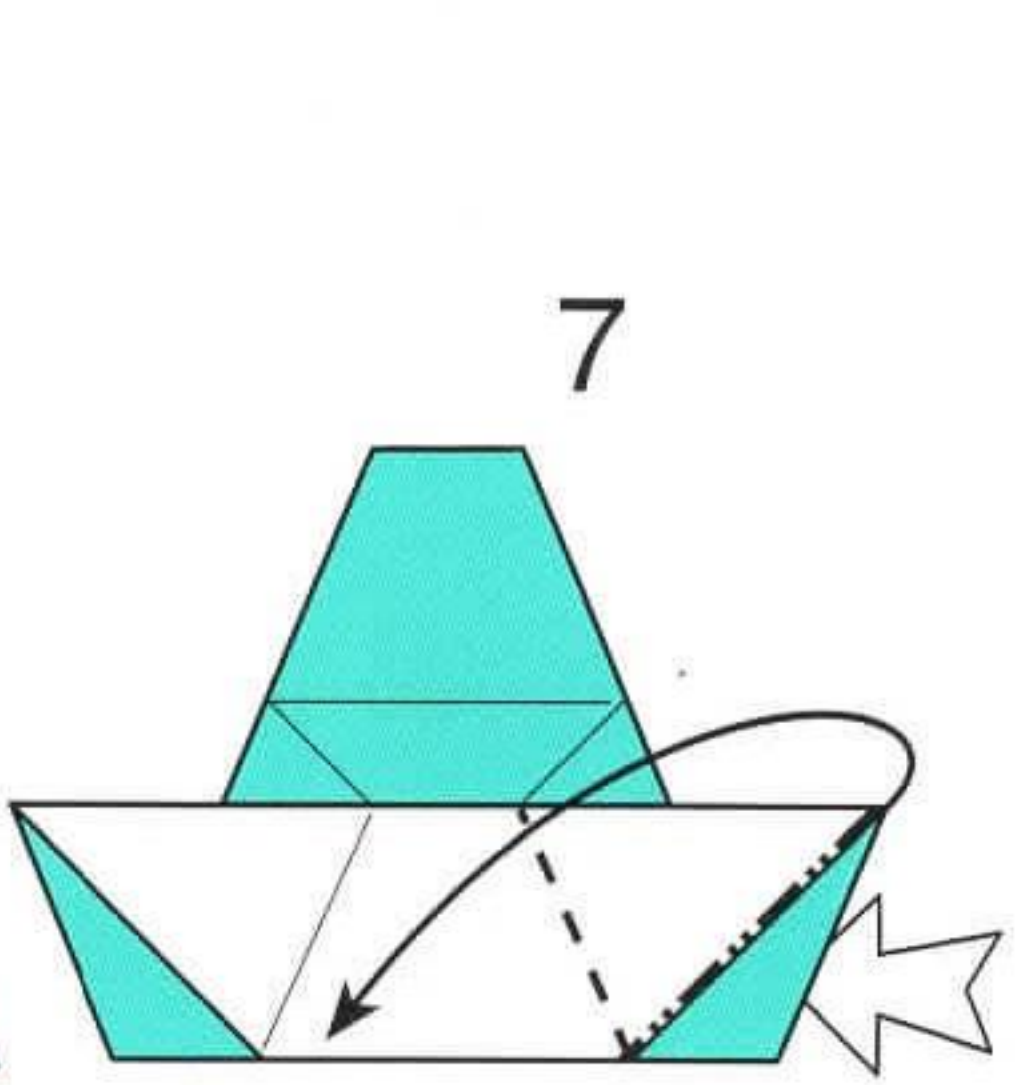
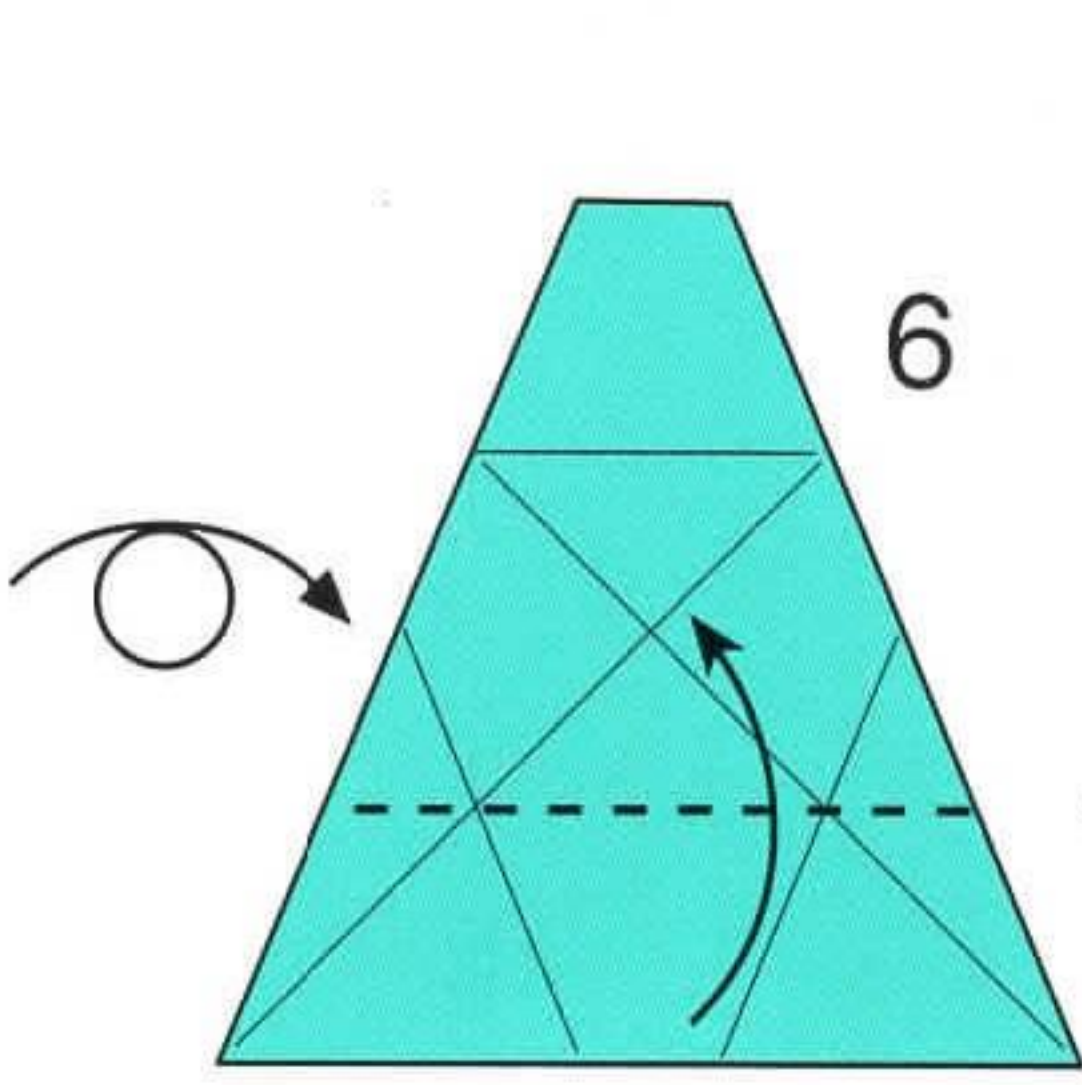
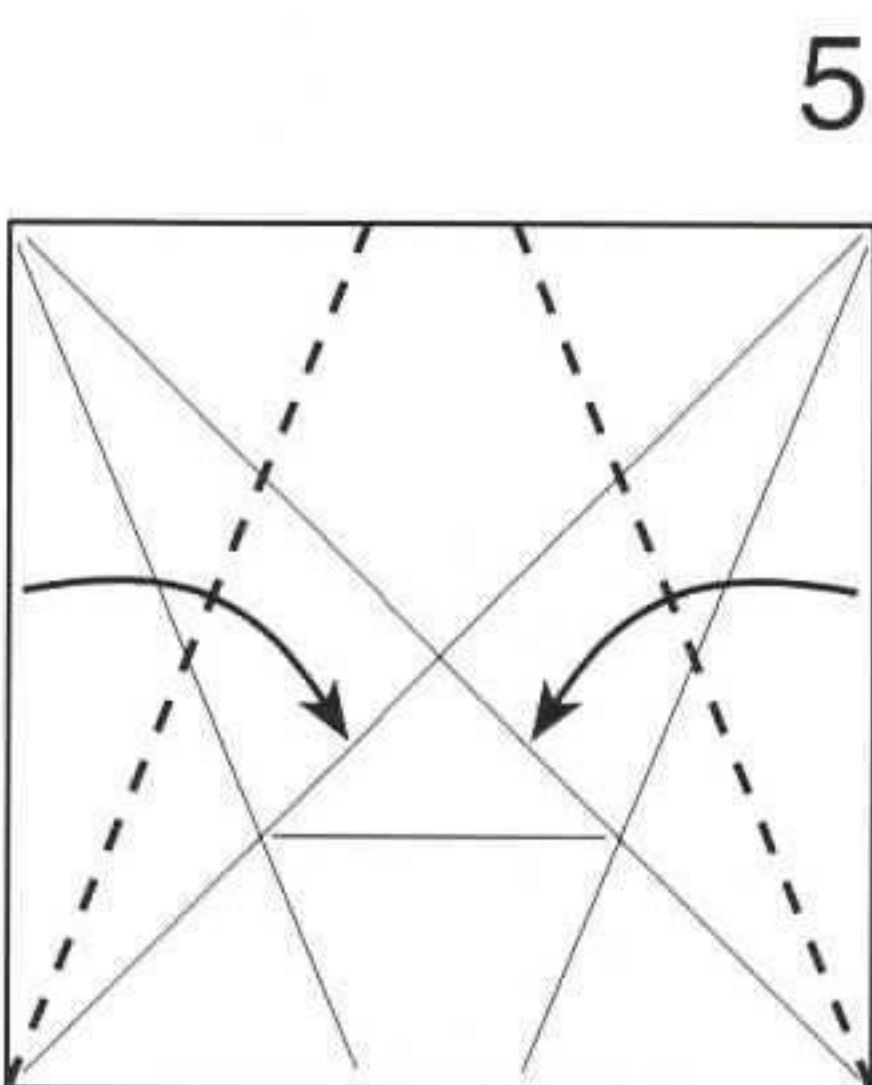
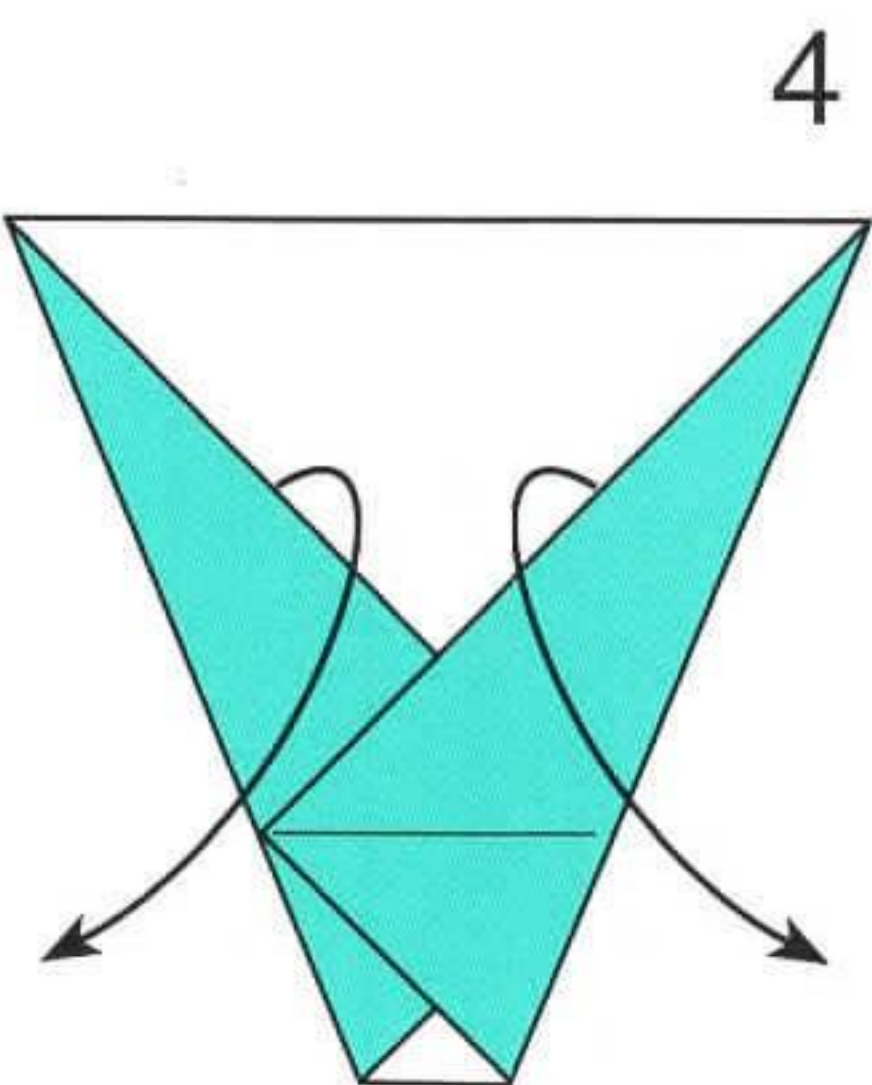
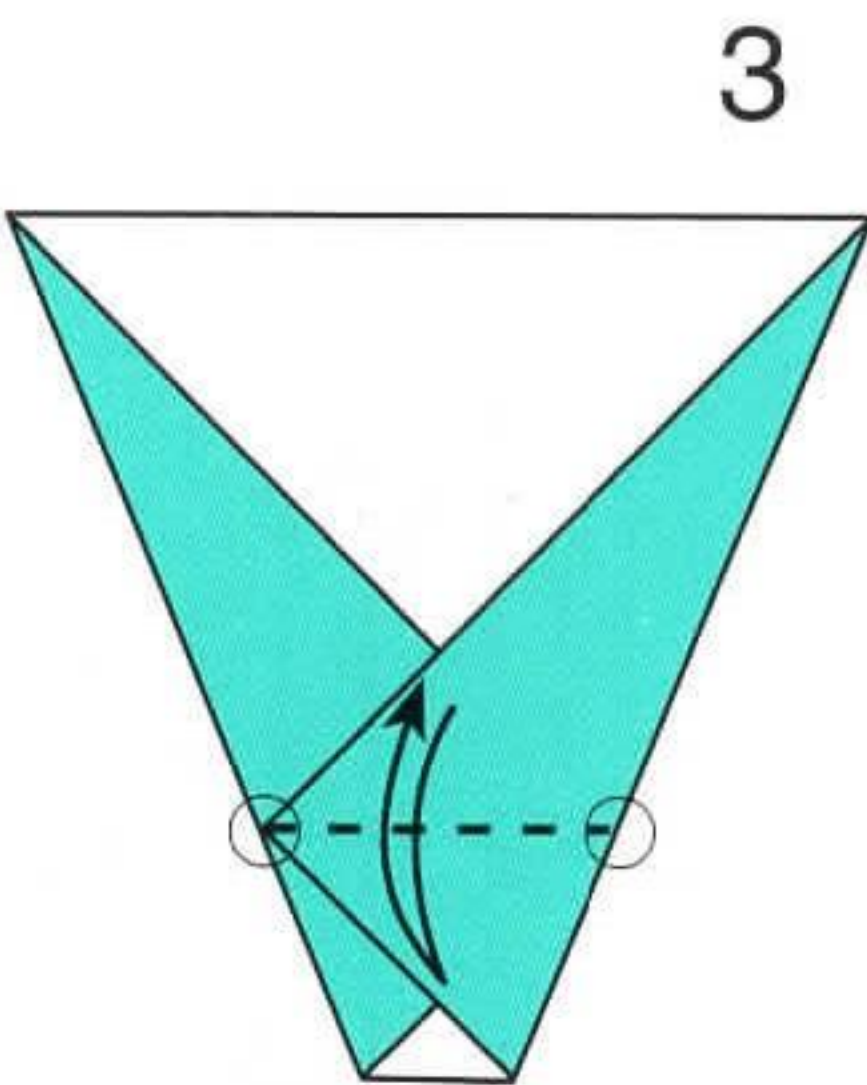
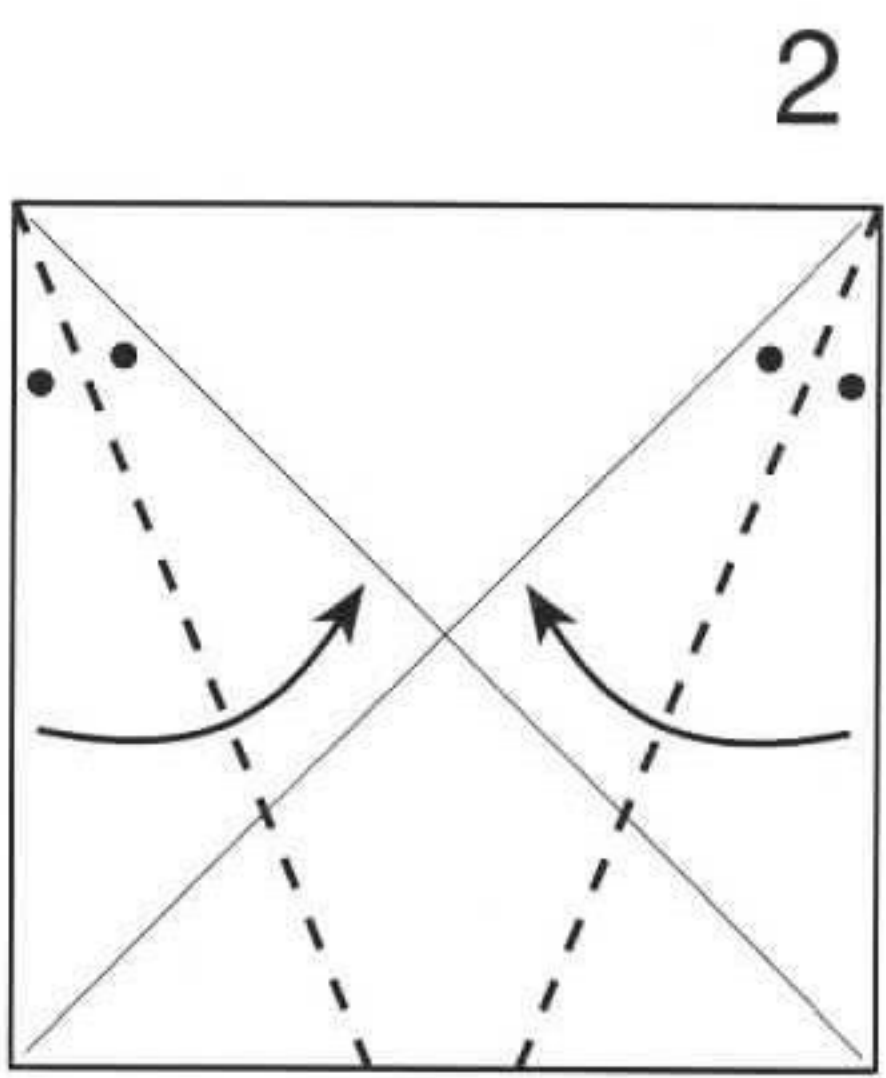
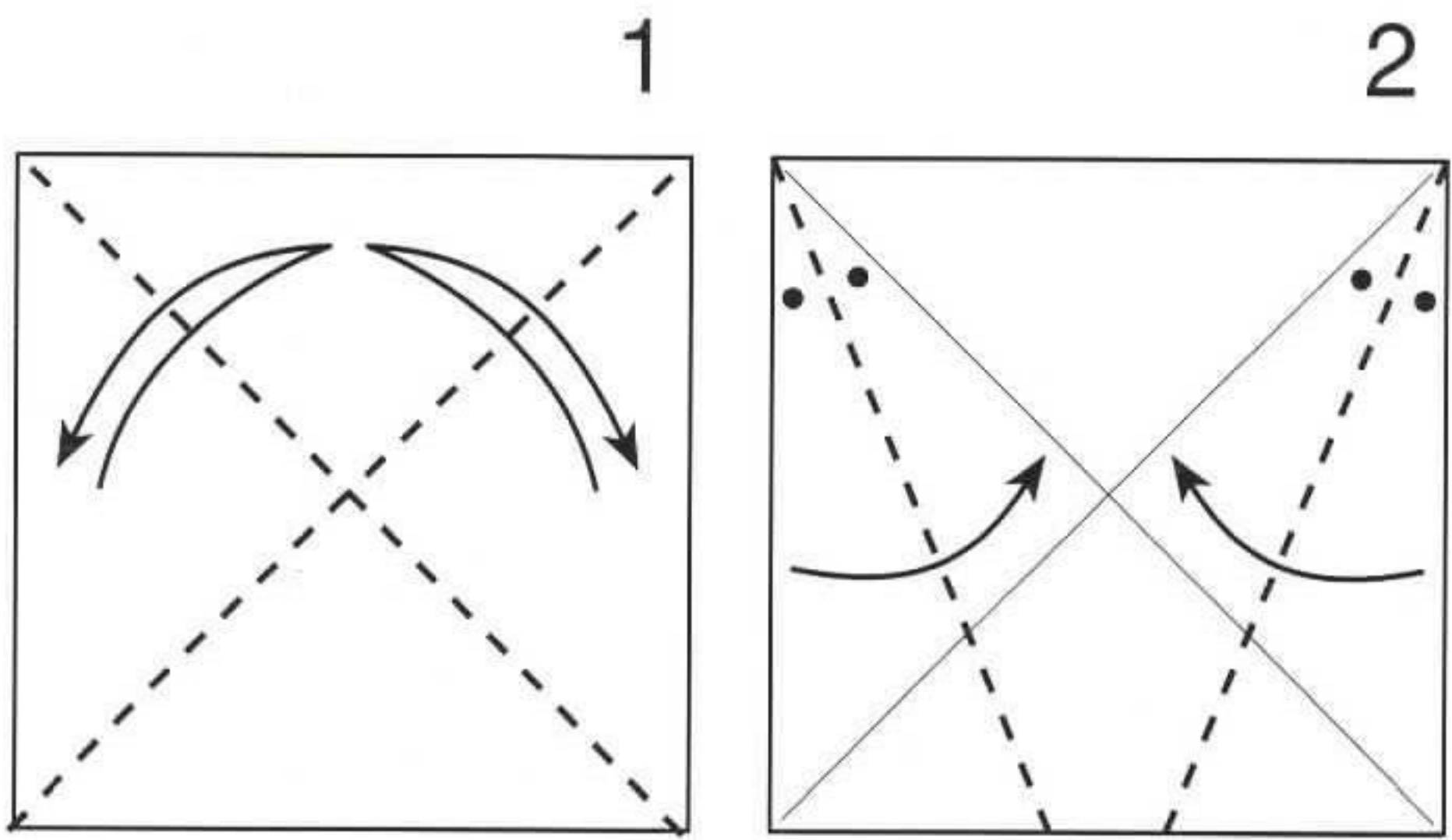
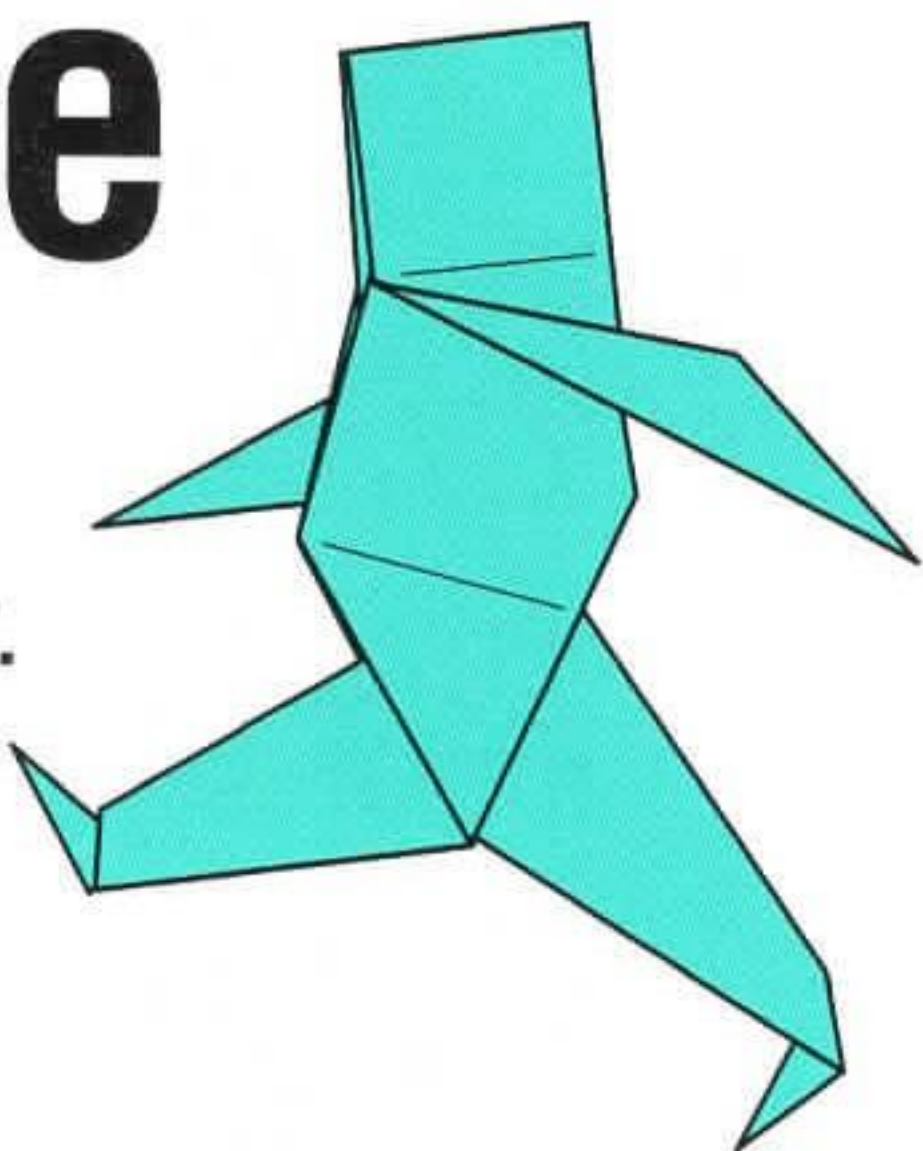
Make the anterior and tail fins almost horizontal to finish.

Shaping in origami

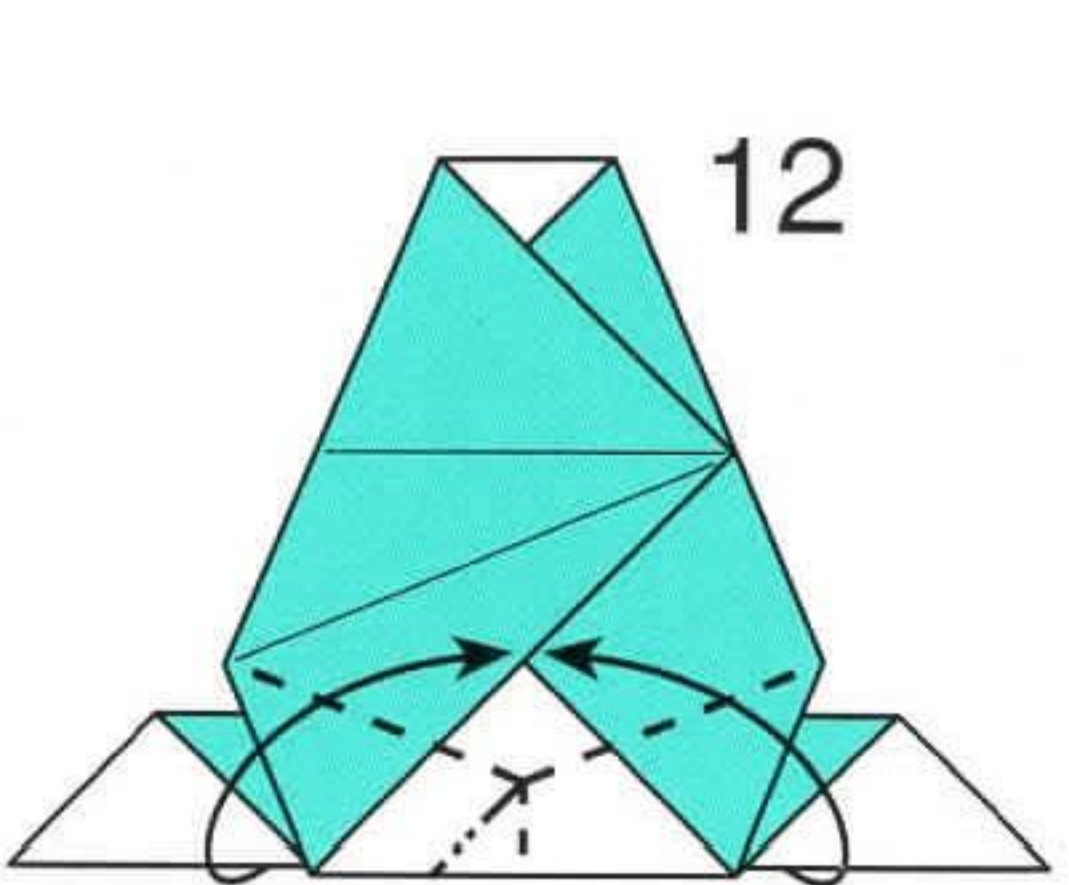
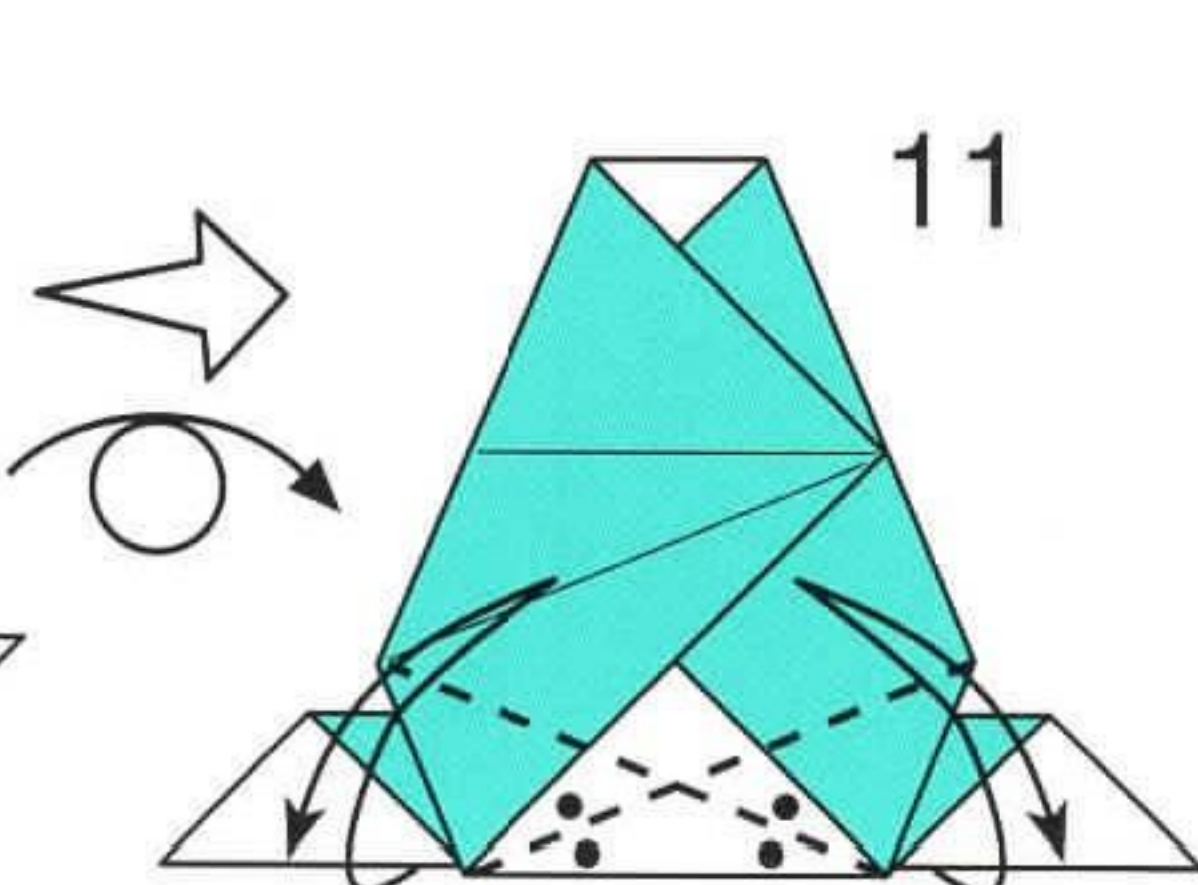
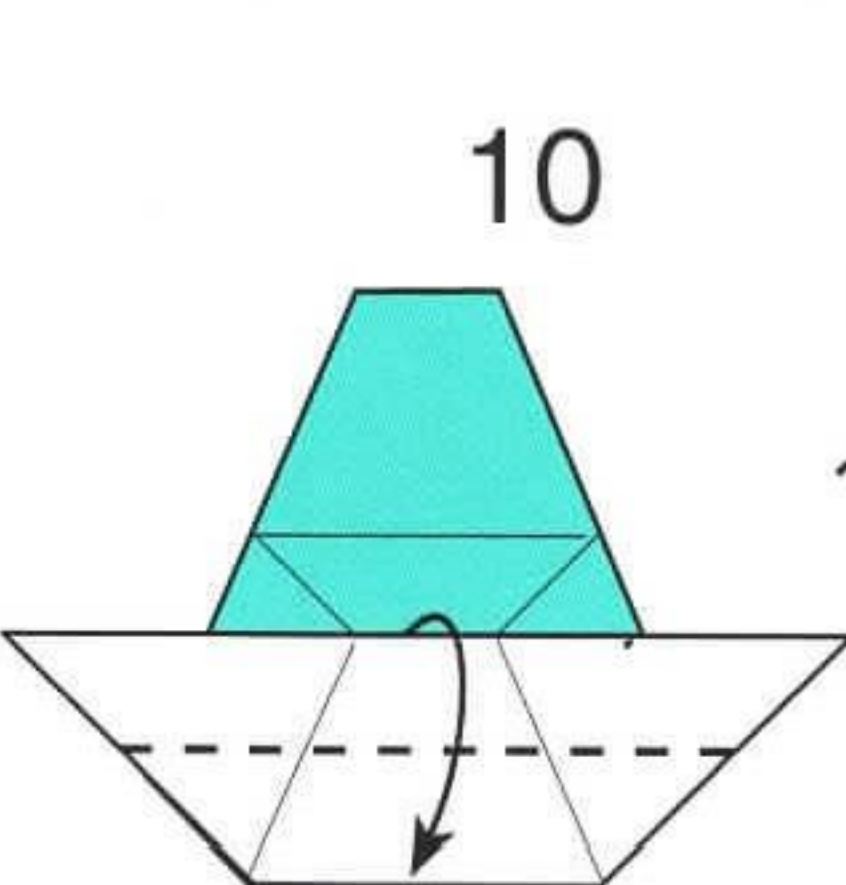
Pushing in and popping up, as with the head of this model, are techniques used to fold three-dimensional models. In this case, it is rather an extension of **half-open** folding and because of clear landmarks it is easy to fold. Akira Yoshizawa, the father of modern origami, enhanced this technique to delicate craftsmanship. He also developed a technique called **wet folding**, where we damp the paper and fold before it dries to obtain stable curved surfaces. Though, I personally have very little experiences with that technique.

Human Figure

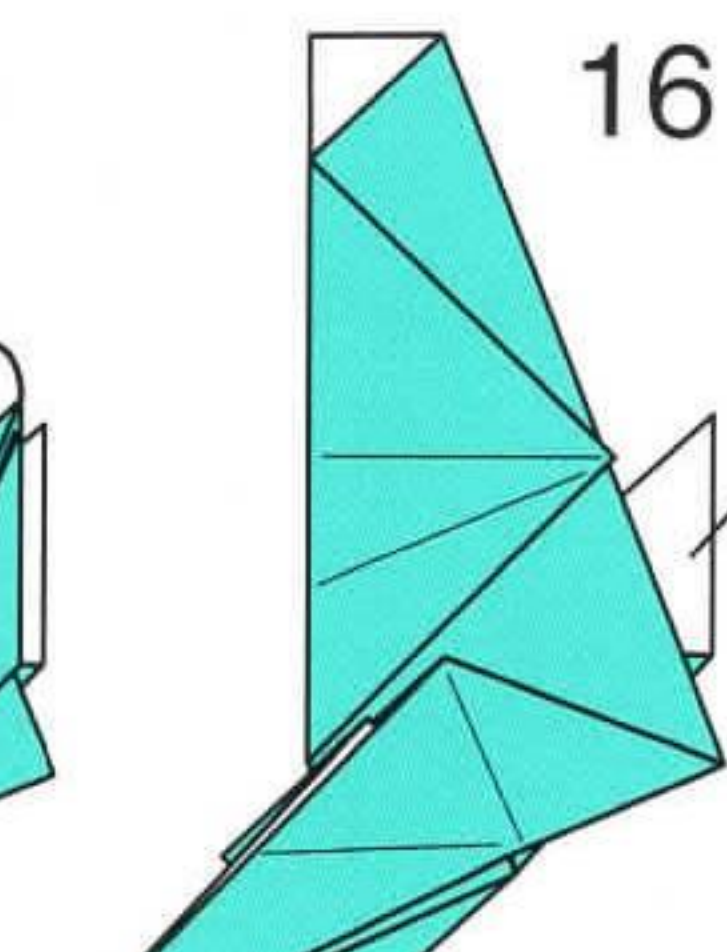
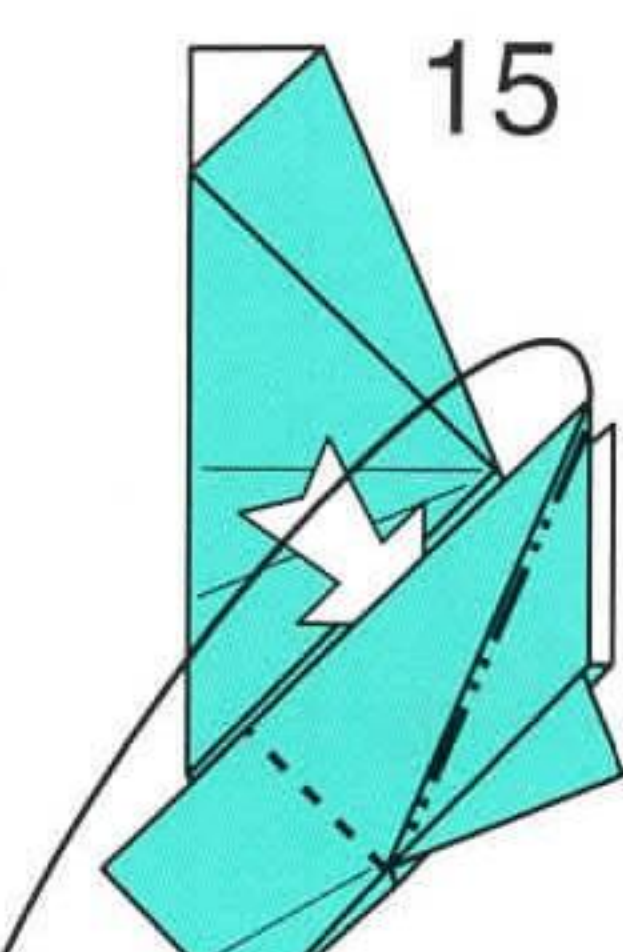
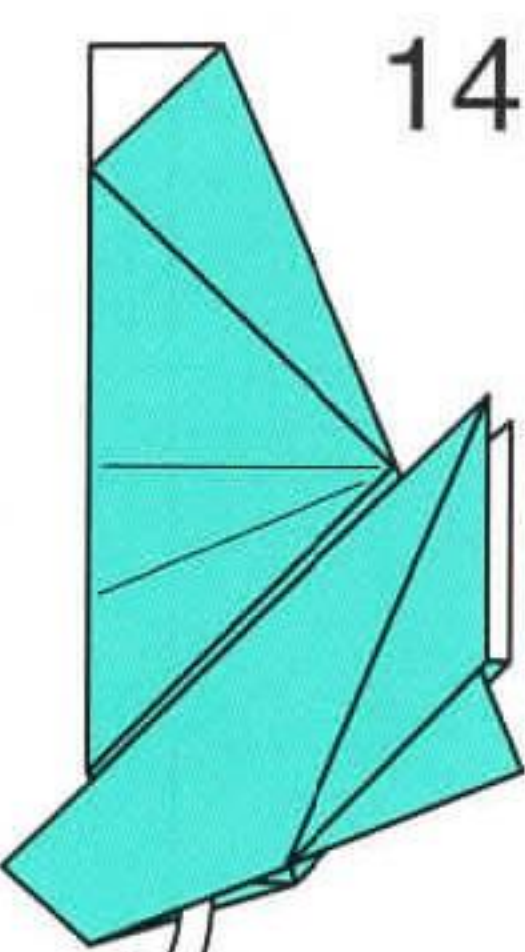
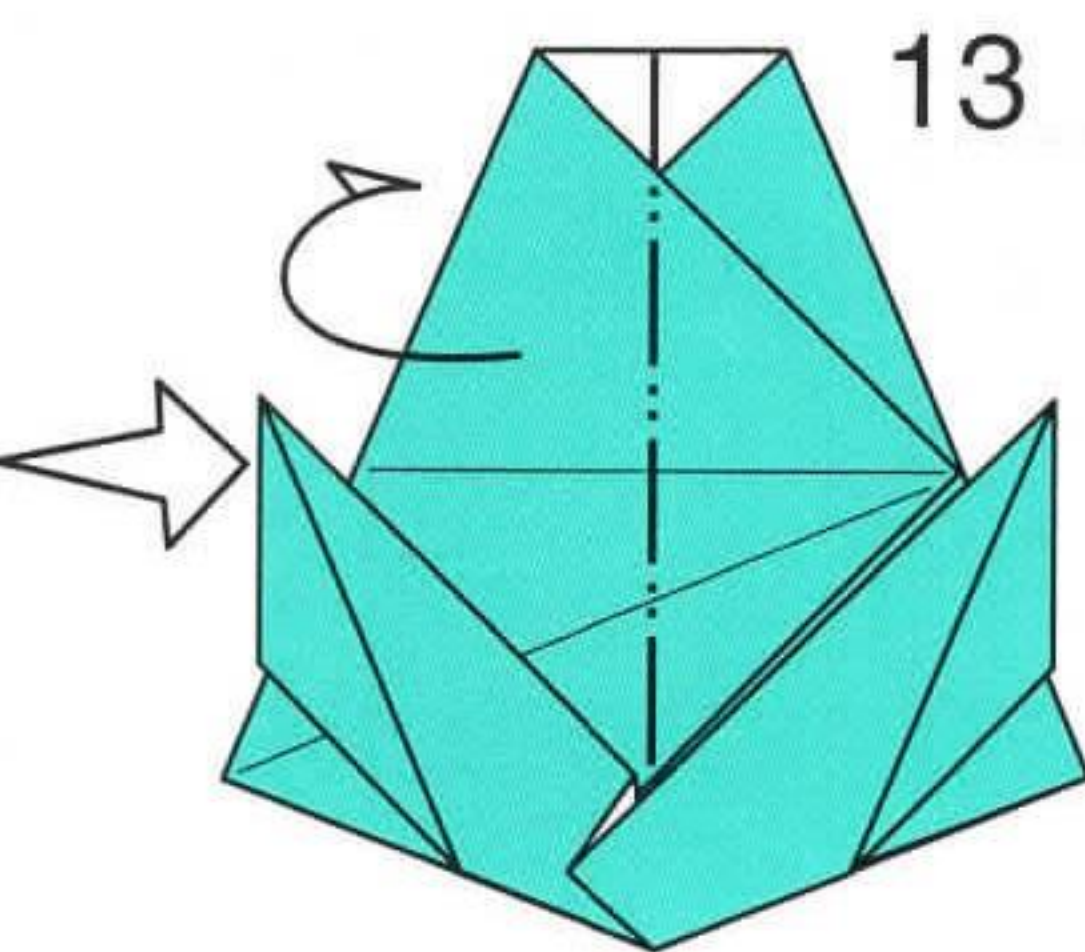
Theme: Crease pattern
Fold using 6" (15 cm) origami paper.



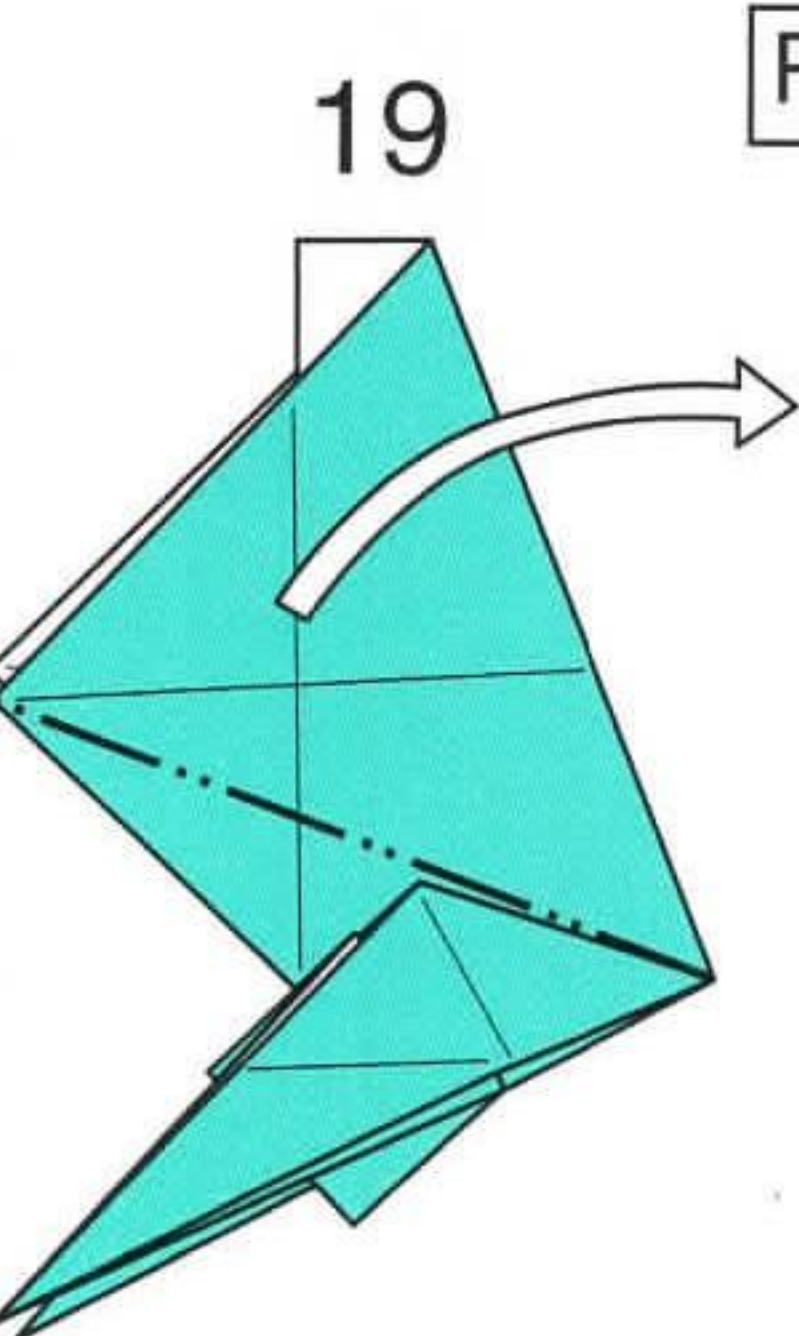
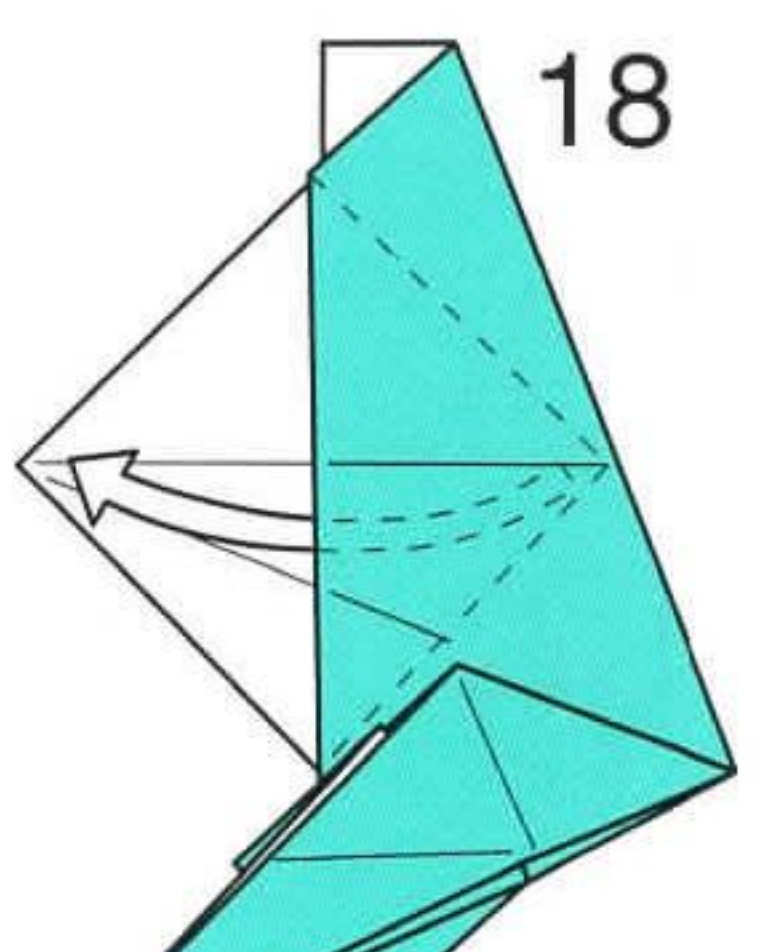
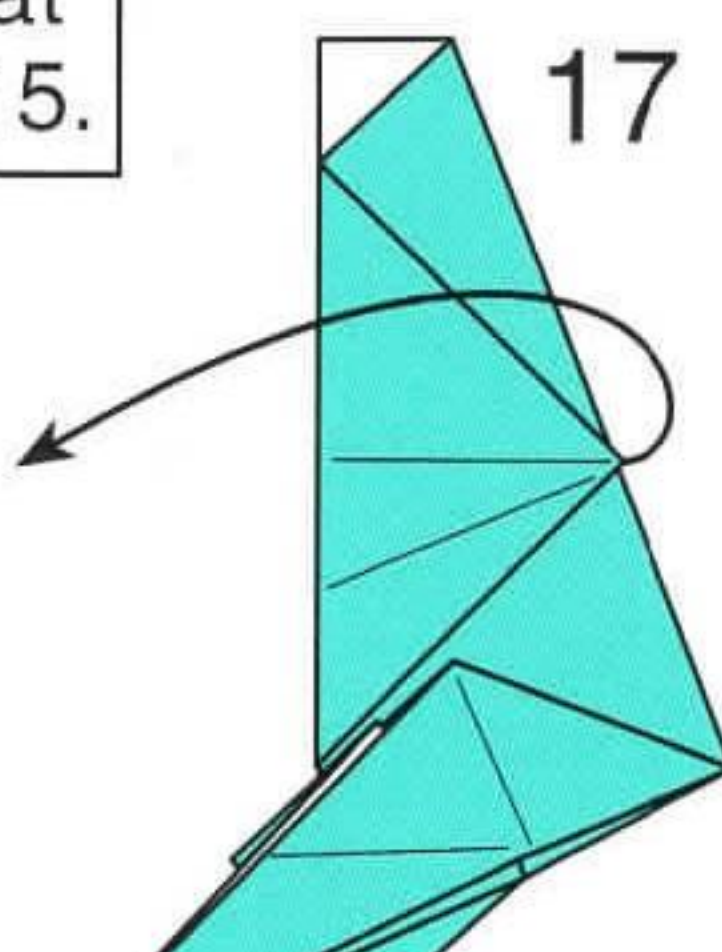
Repeat steps 7-8.



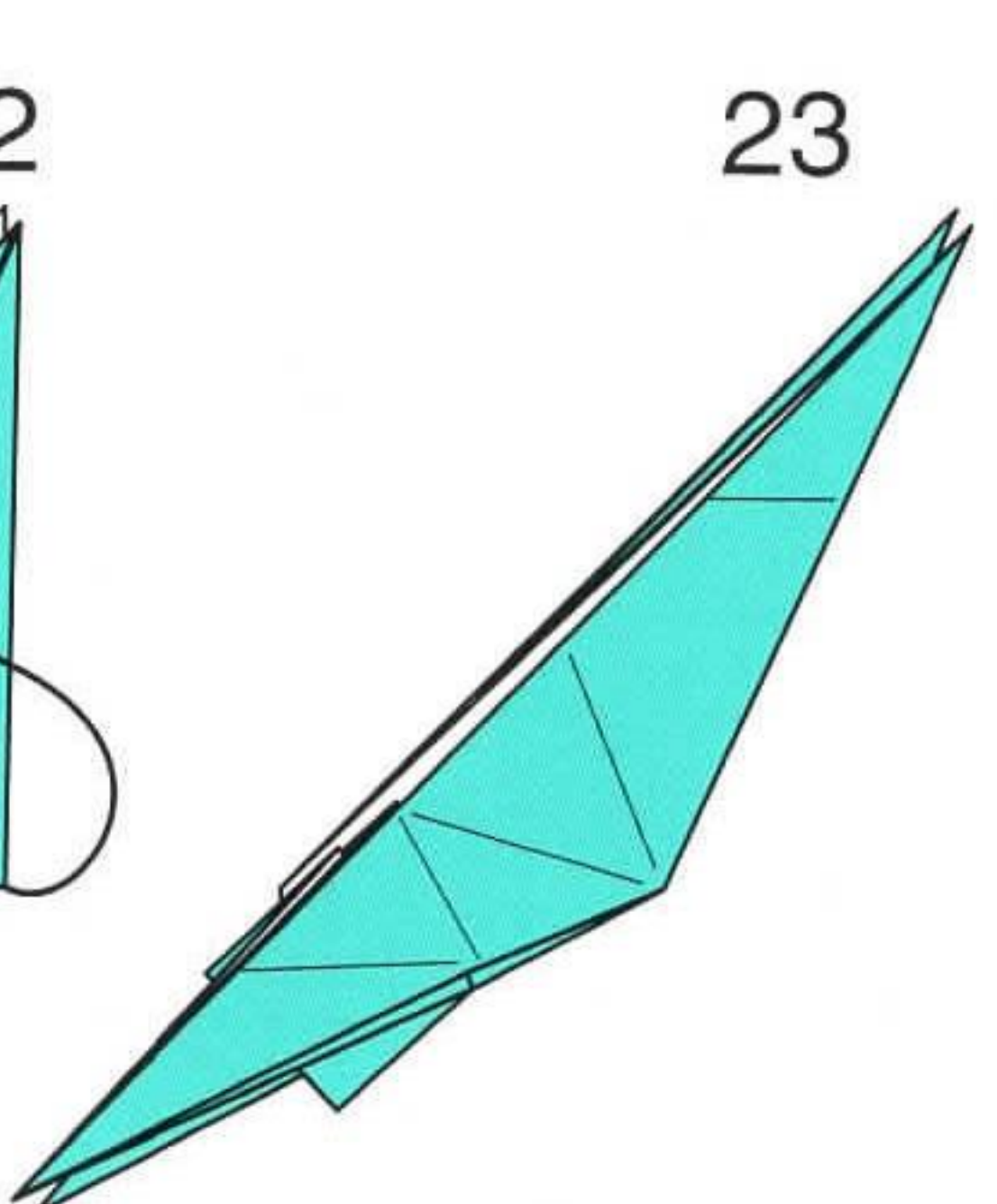
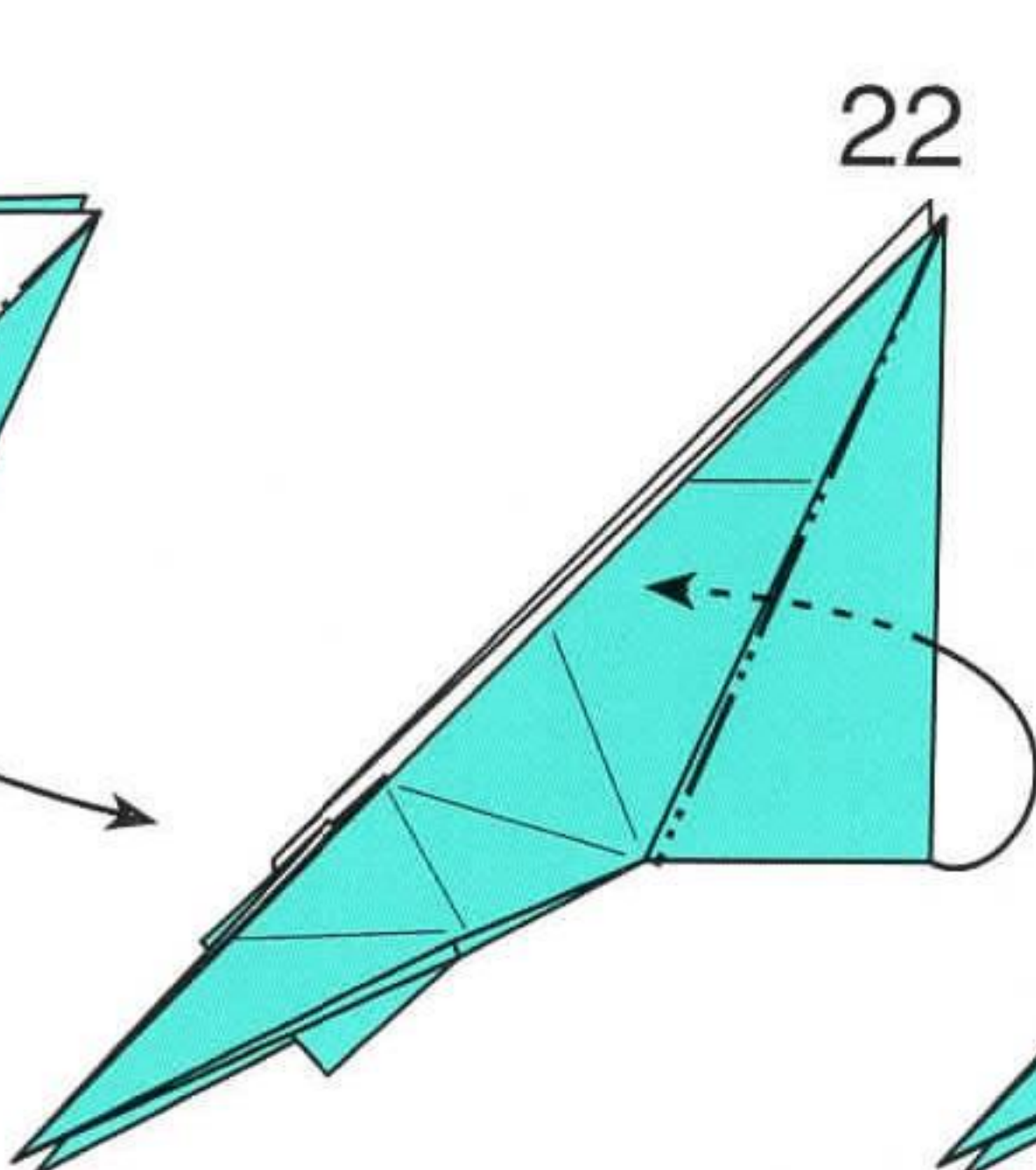
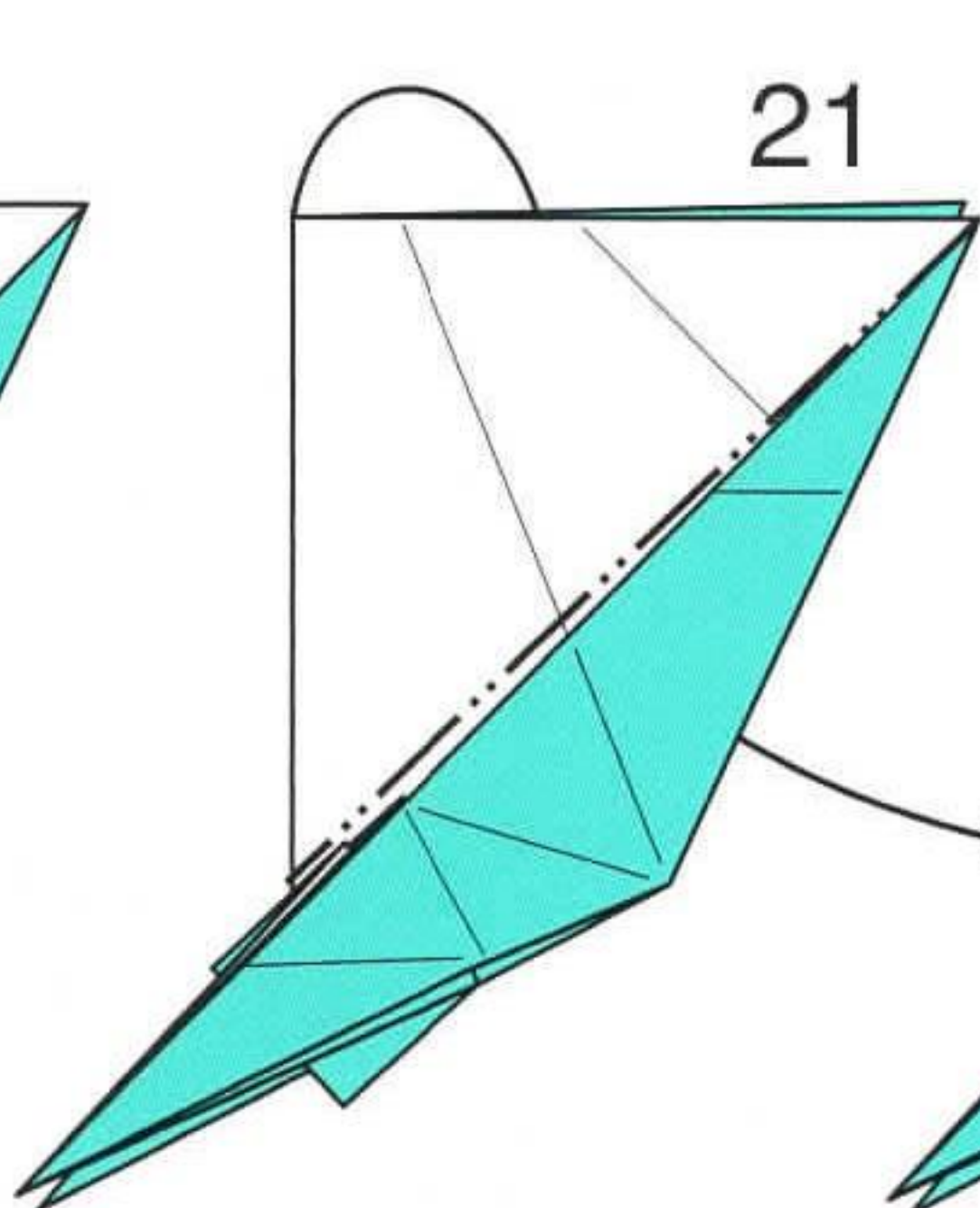
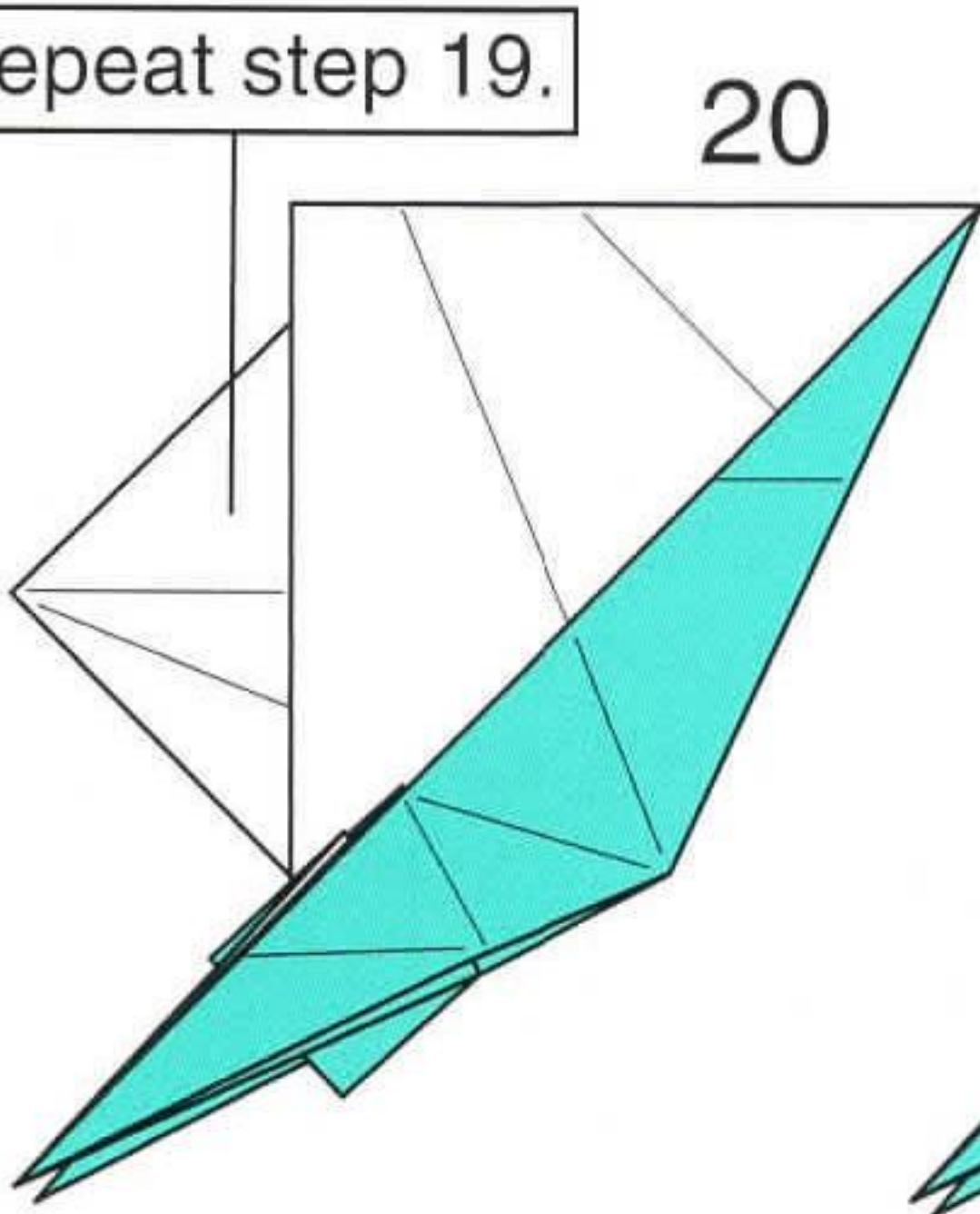
Rabbit ear fold.



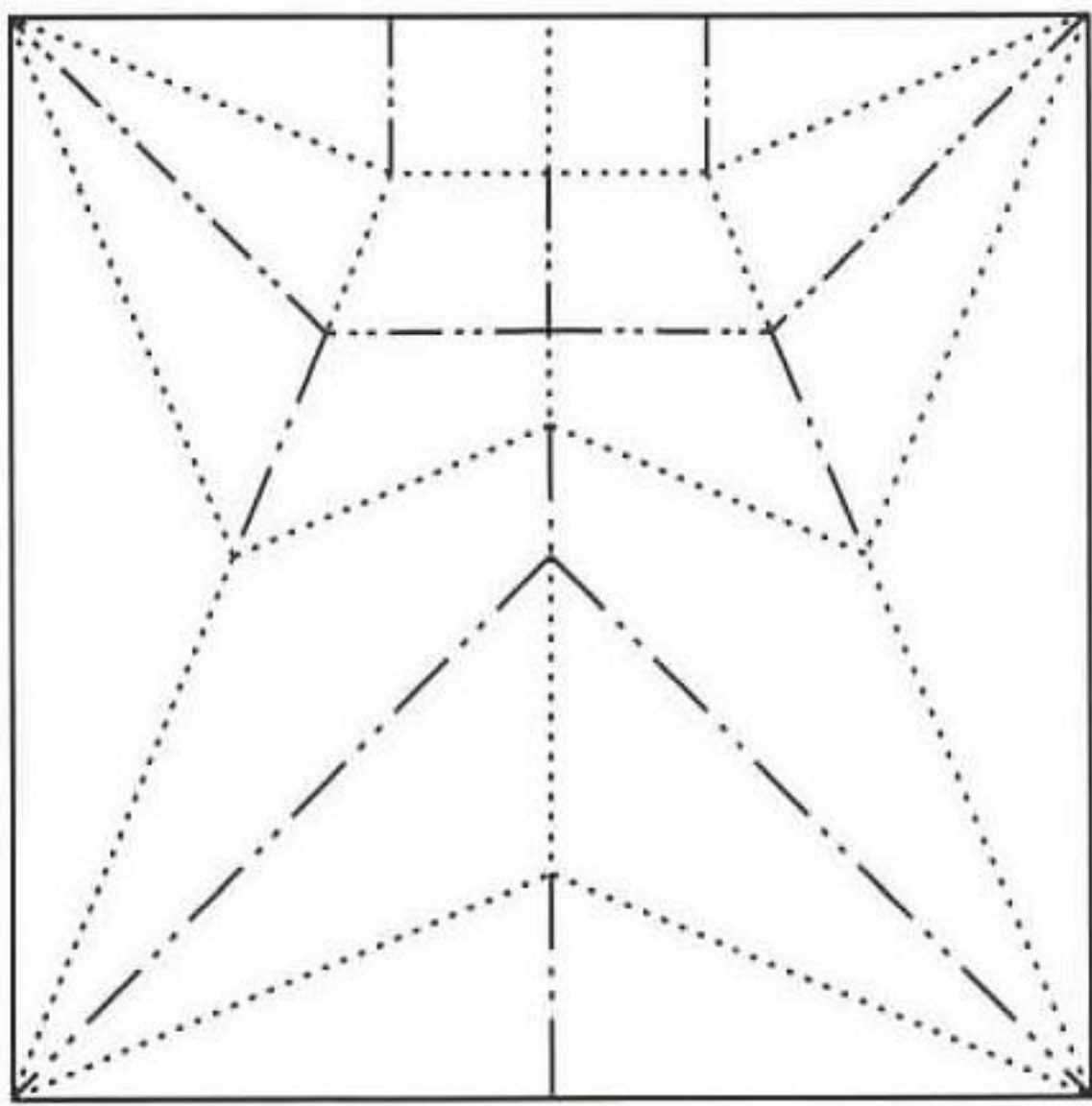
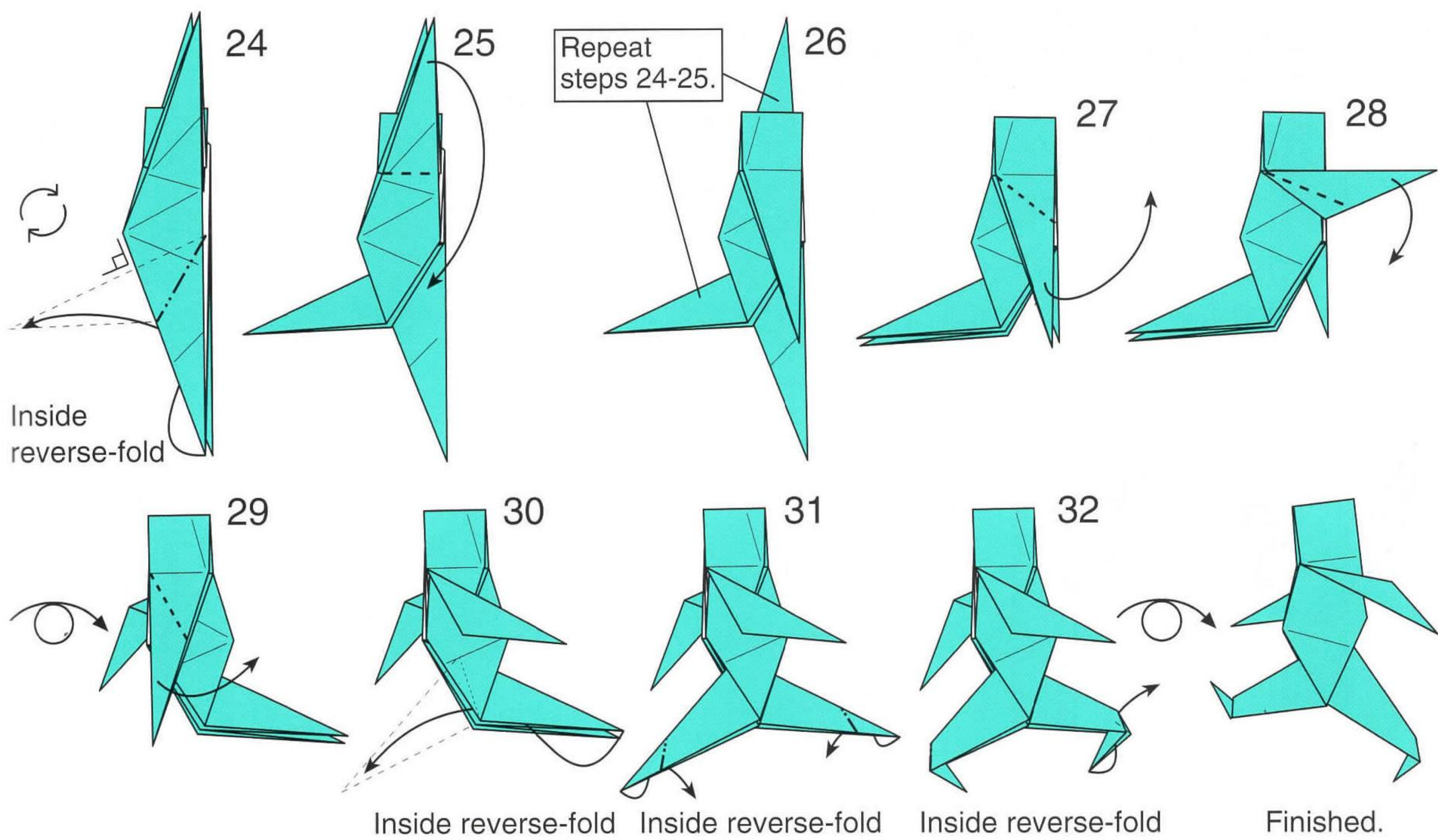
Repeat step 15.



Repeat step 19.



Inside reverse-fold Inside reverse-fold



Crease pattern

If you stop folding at step 23 and unfold completely, you will see on the white side of the paper the creases as shown on the left. Such creases, as well as those shown in the **Base** section, is called **crease pattern**.

Although I designed this model a long ago, I came up with this rather tricky sequence through step 23 only when I started writing this book. Noboru Miyajima once created diagrams of this model, but his sequence was far different from mine. My old sequence was also different. I basically pre-creased everything, and collapsed in one step.

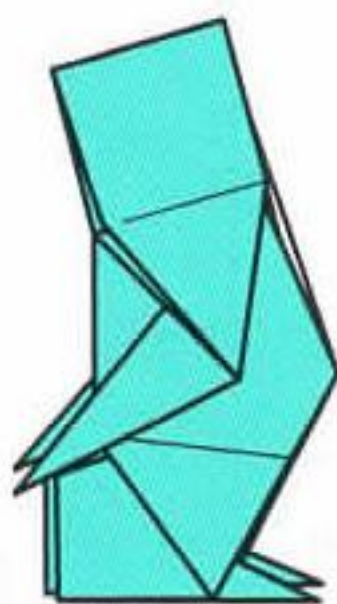
When I taught this model, I sometimes distributed a sheet on which the crease pattern was printed and told to collapse according to the lines.

You must be an expert to fold a complex model just from its crease pattern. Moreover, when you fold from the crease pattern, you cannot enjoy the sequence as a story composed by the designer. But this model is an excellent puzzle, when you are supposed to fold the model only from its crease pattern.

In other words, a crease pattern can document a model, in a different way from what can be done using the diagrams.

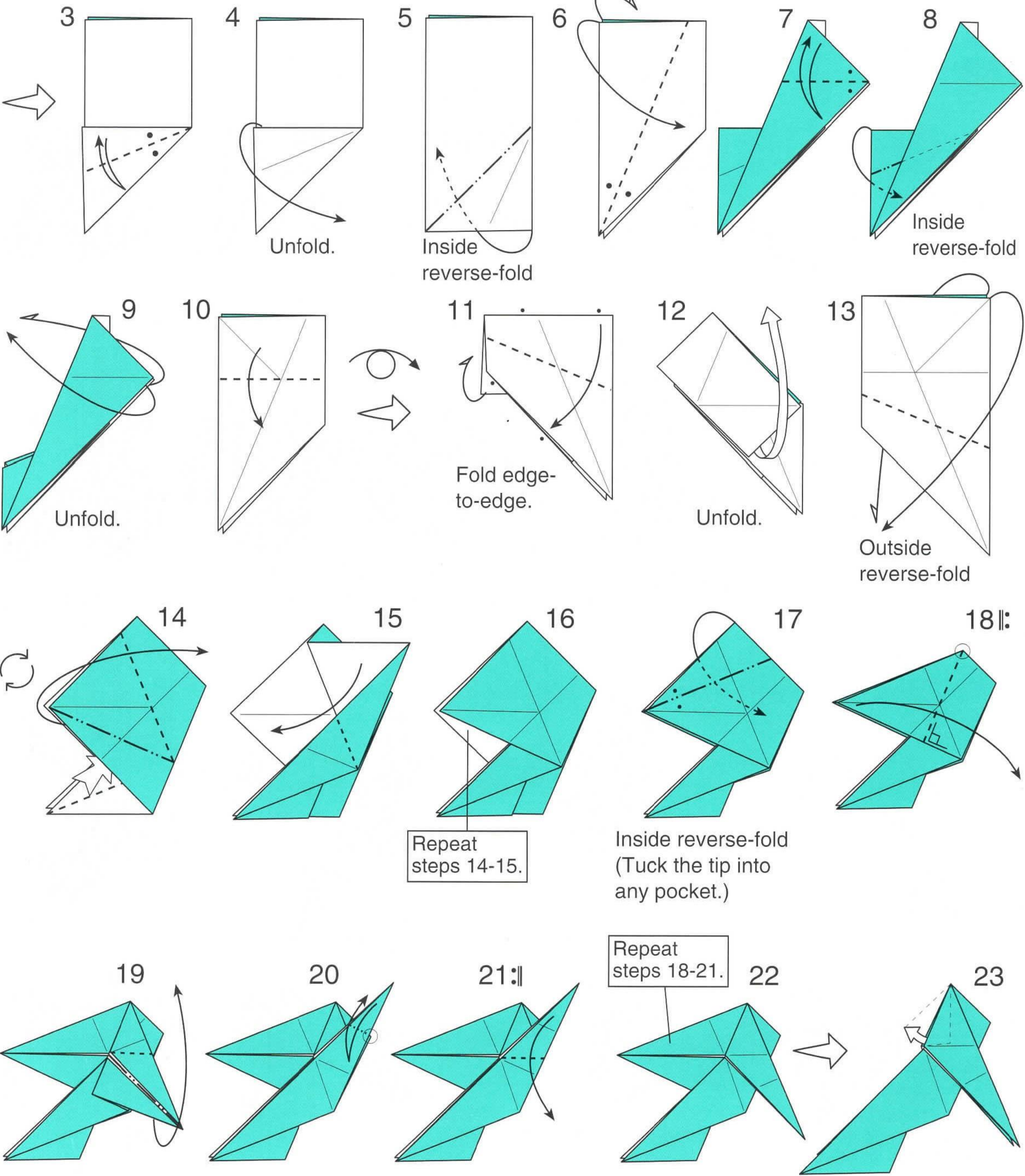
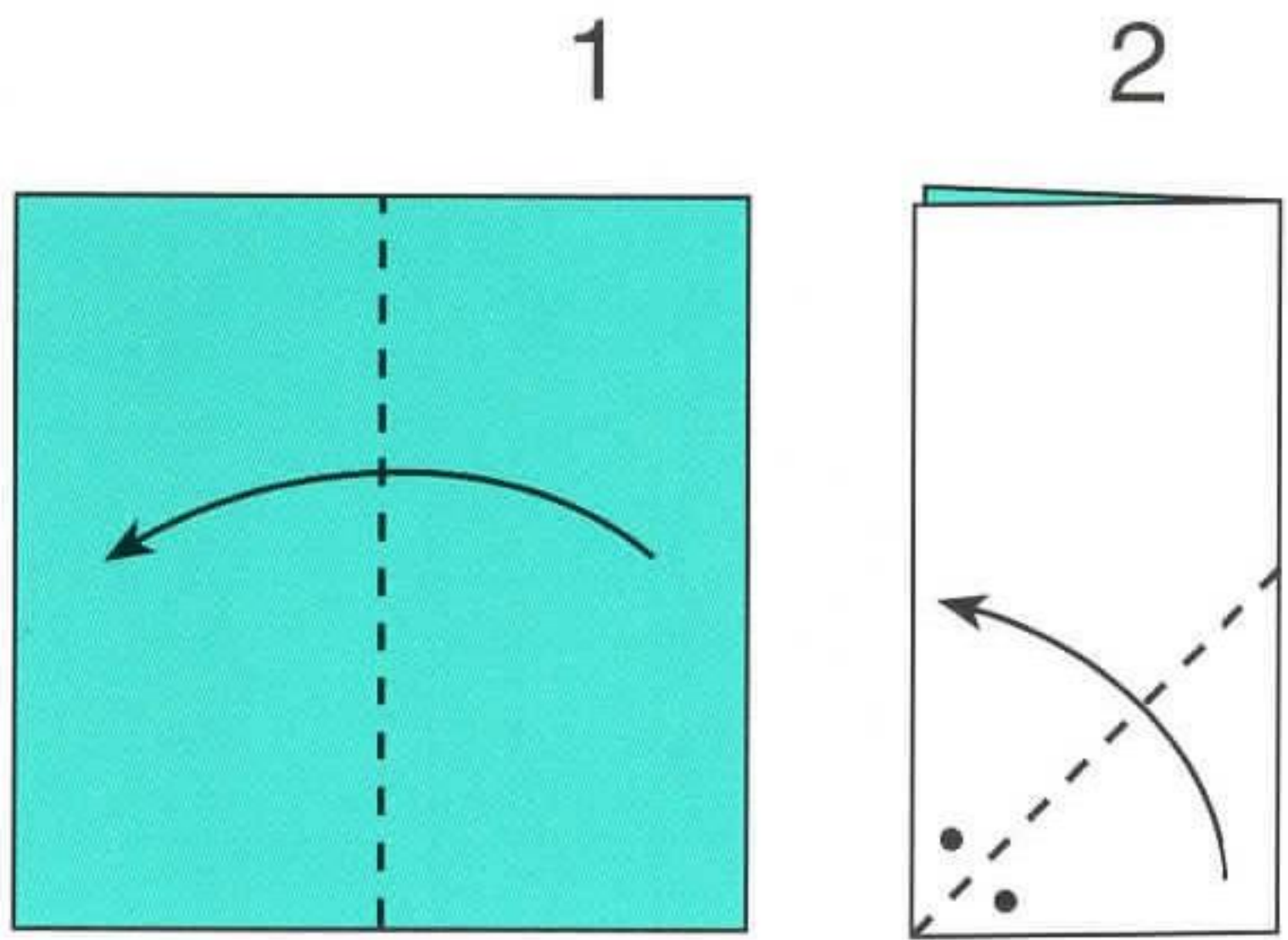
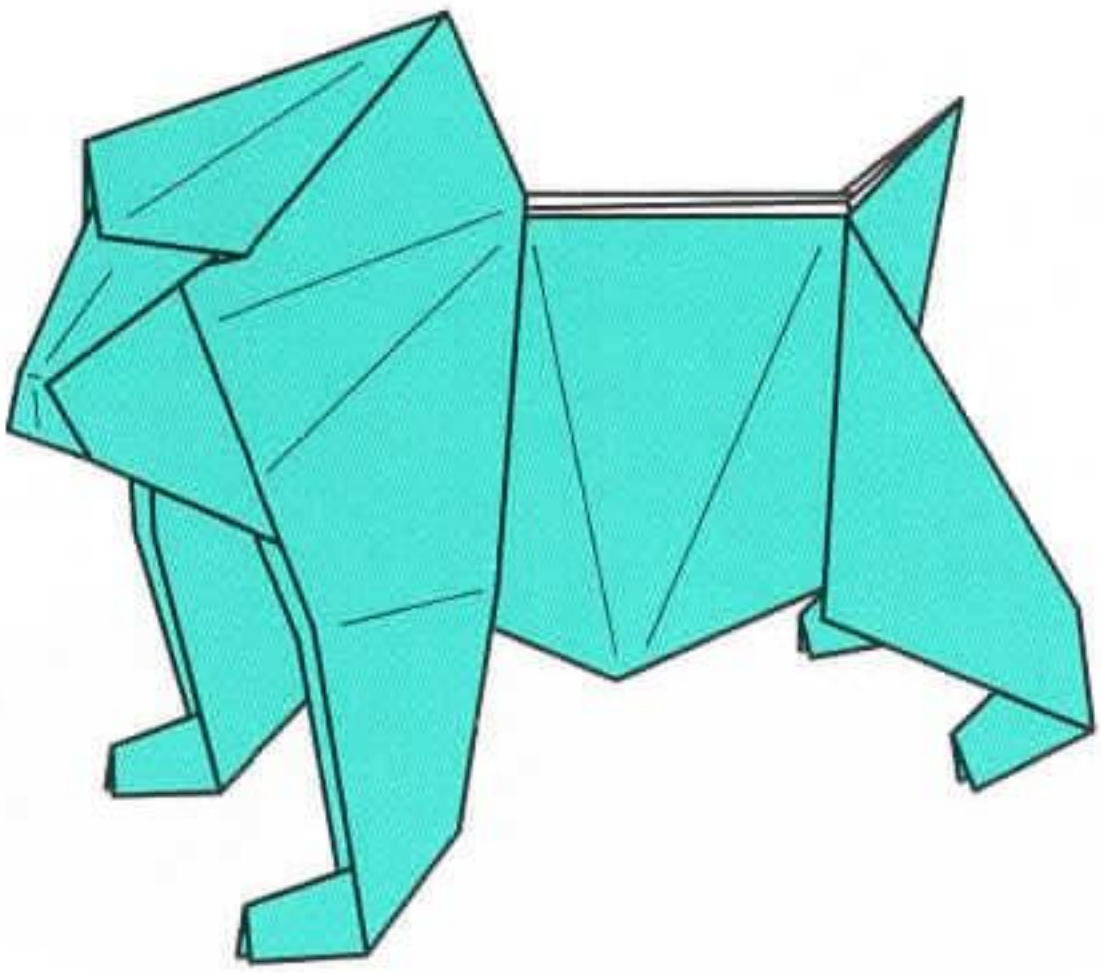
In addition, as explained later in the book, one can examine the construction of the model using the crease pattern before actually folding it. Such a crease pattern usually does not contain detailed creases.

The pattern for this model has especially few creases. That means, you can pose this human figure as you like. Please find your favorite pose. My favorite is the sitting-on-the-knees pose, as shown on the right. To fold it, mountain-fold the arms in the other direction than in step 28 so that the hands will rest on the knees, and inside reverse-fold the legs twice. For the first inside-reverse fold deeper than in step 24.



Japanese Macaque

Theme: Crease pattern fold
Fold using 6" (15 cm) origami paper.



24

Repeat step 24.

26

27

28

Outside reverse-fold

Outside reverse-fold

Pull down the long flap while holding the tip folded in step 27.

Repeat steps 28-29.

29

30

31

32

45°

Rabbit-ear-fold

Unfold back to step 30.

Steps 33-34 show a kind of sink fold, which I would call **crease pattern fold**. To fold it, you must understand the crease pattern in the circle.

33

34

35

Open the model partially.

Push in using the creases made in step 31, while folding like a Bird base.

Inside reverse-fold

36

37

38

39

Parallel.

Inside reverse-fold

Inside reverse-fold

40

41

42

43

Finished.

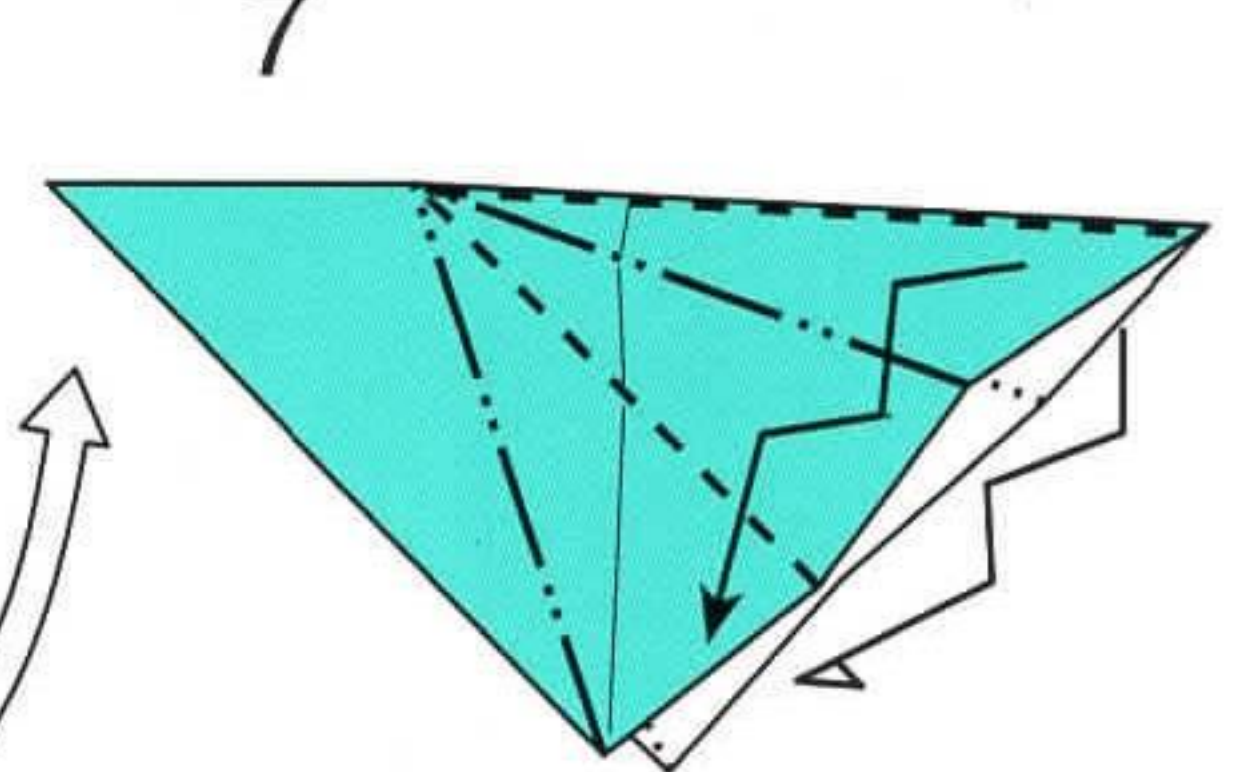
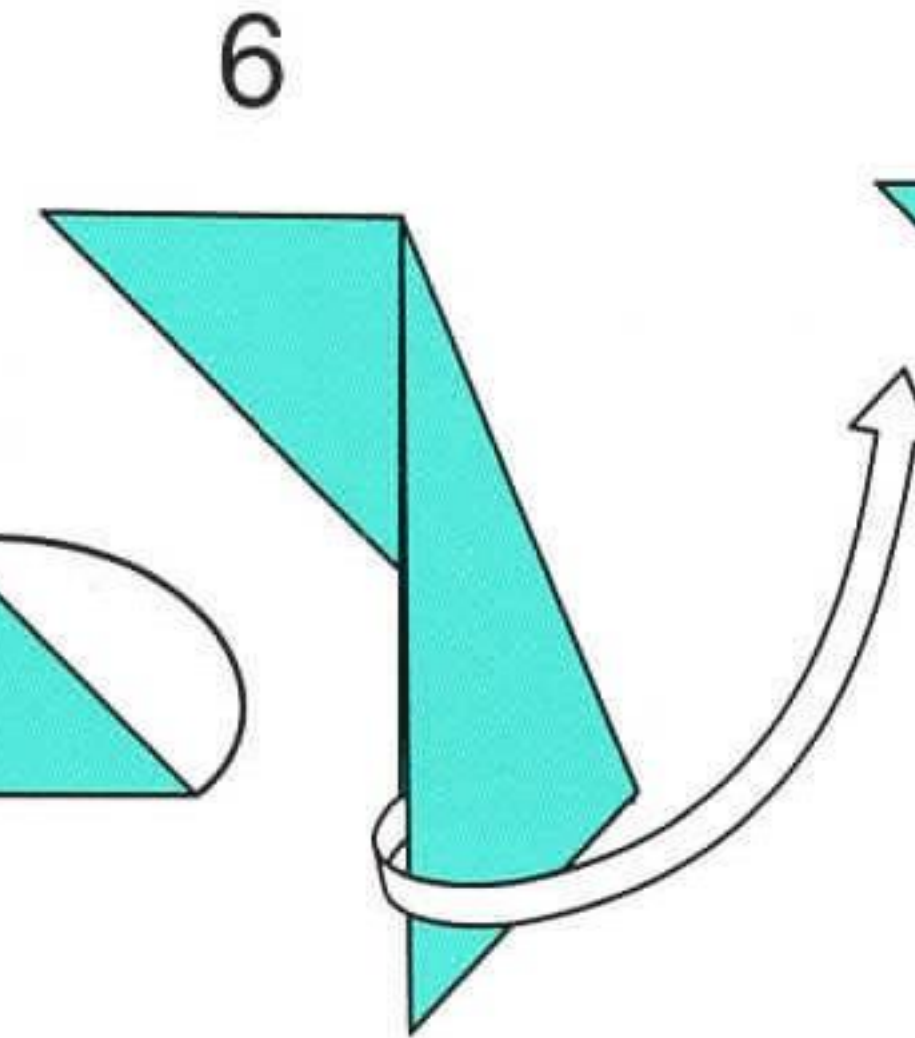
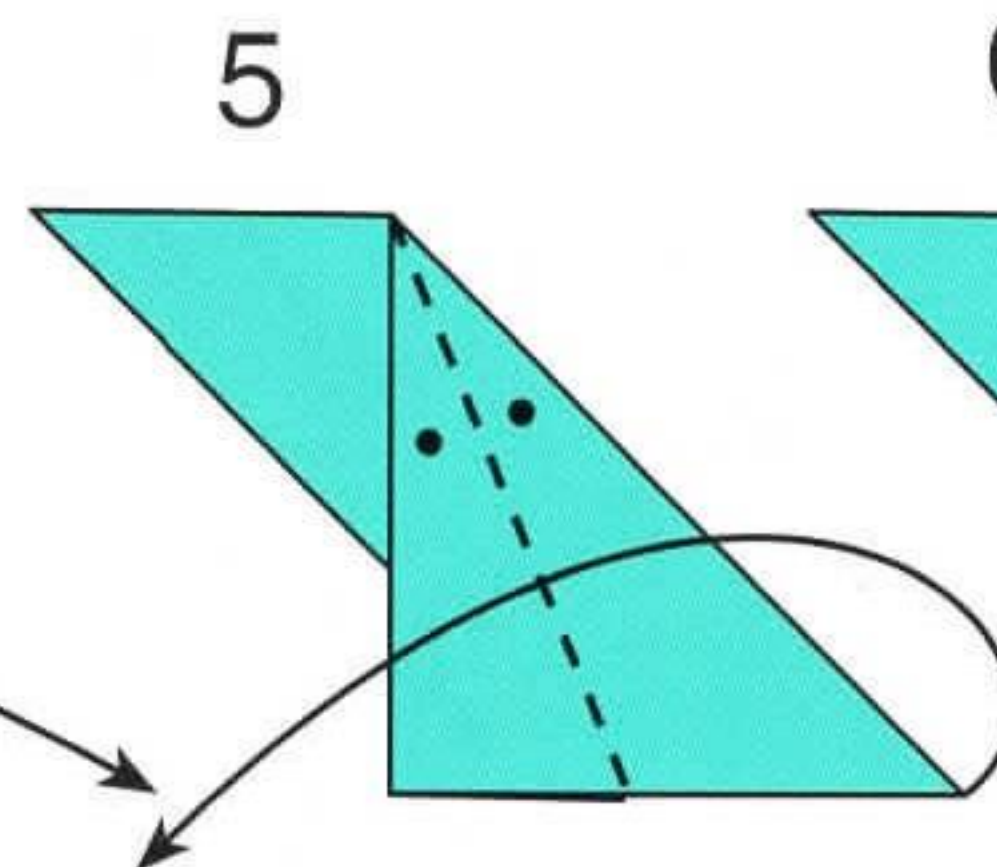
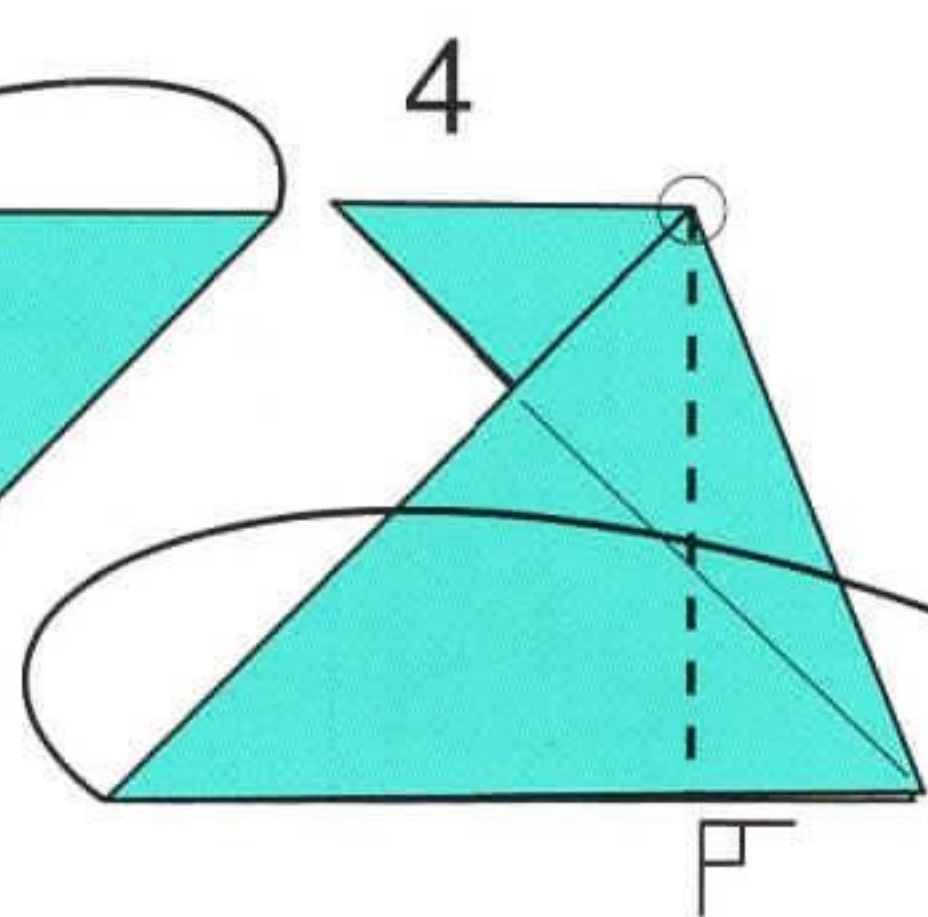
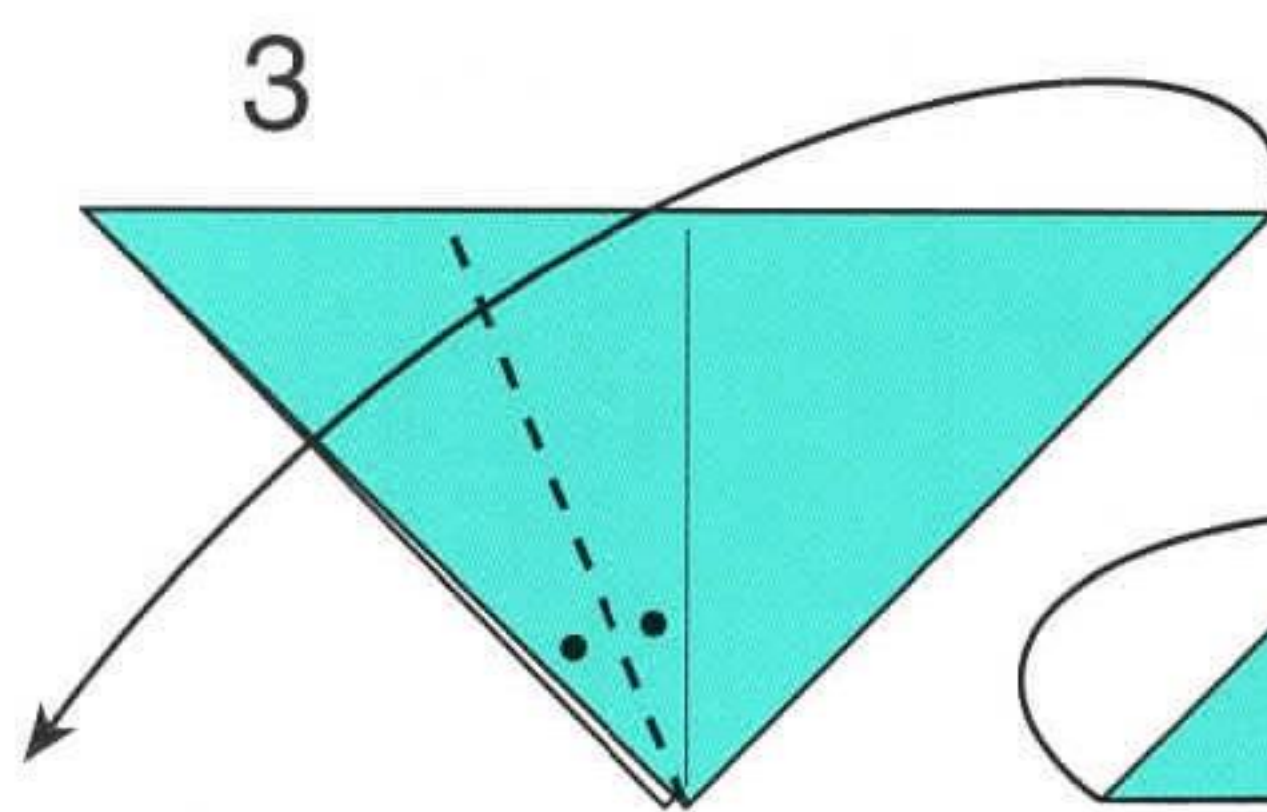
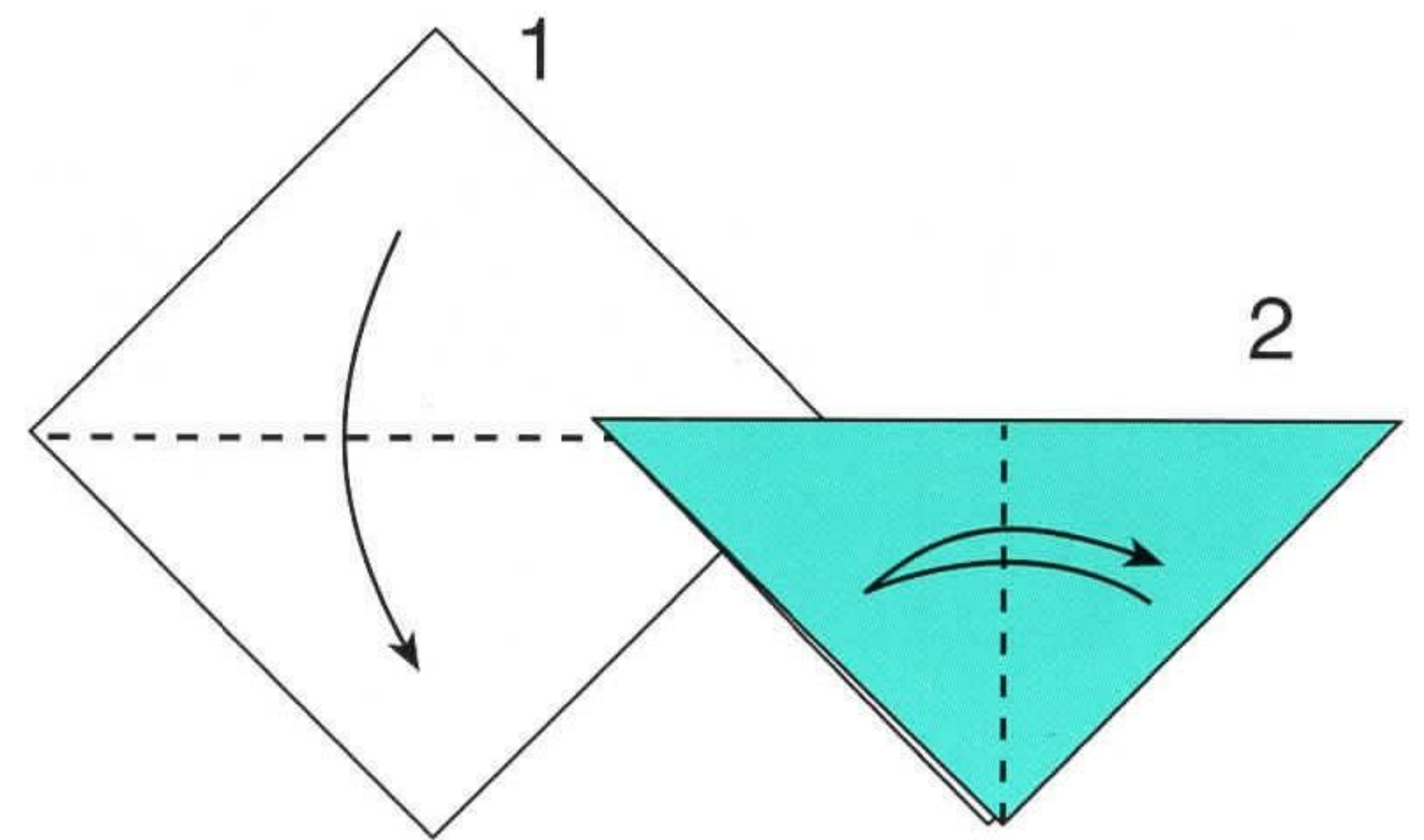
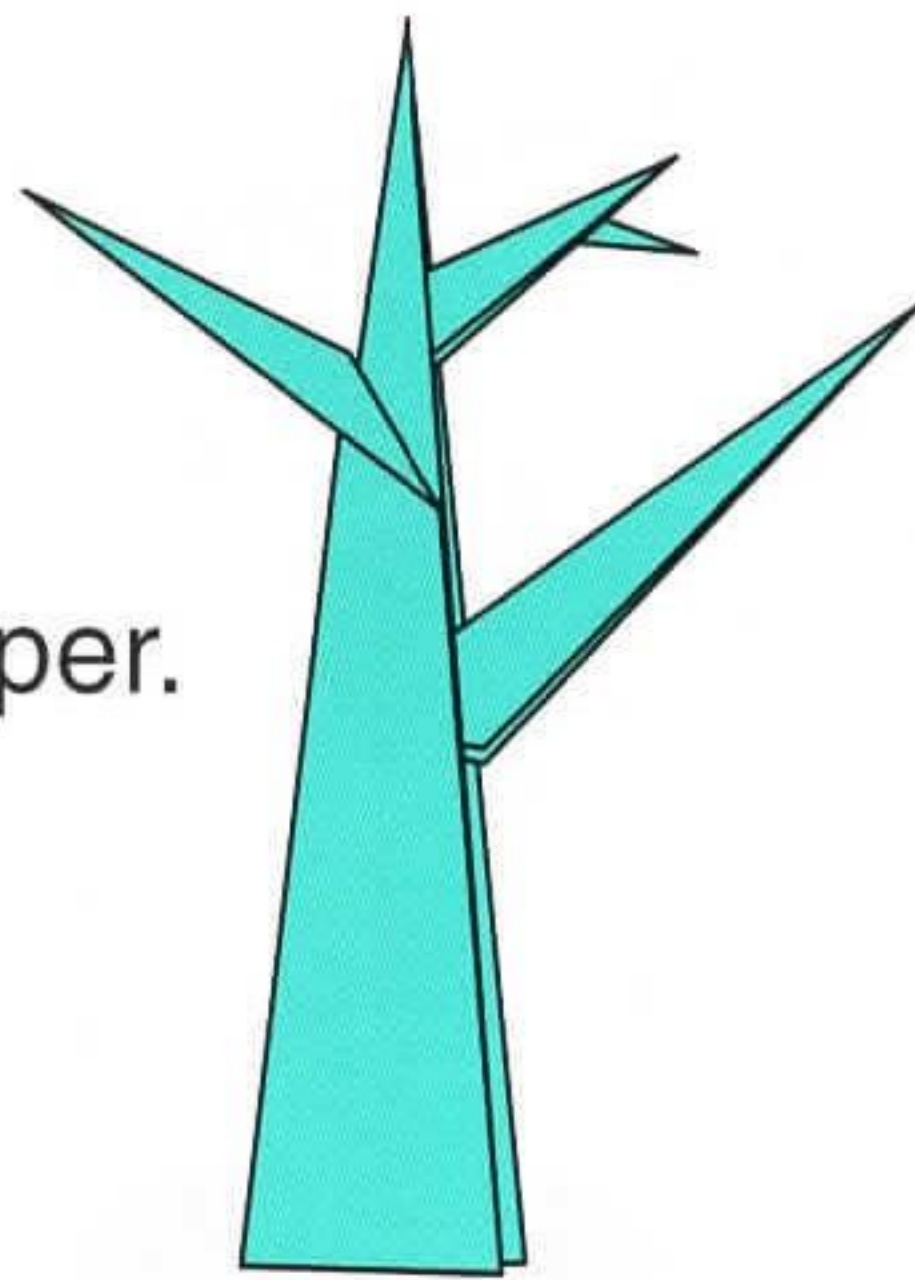
Reinforce the creases at the bases of arms.

Push the tip of the nose a little.

Tree

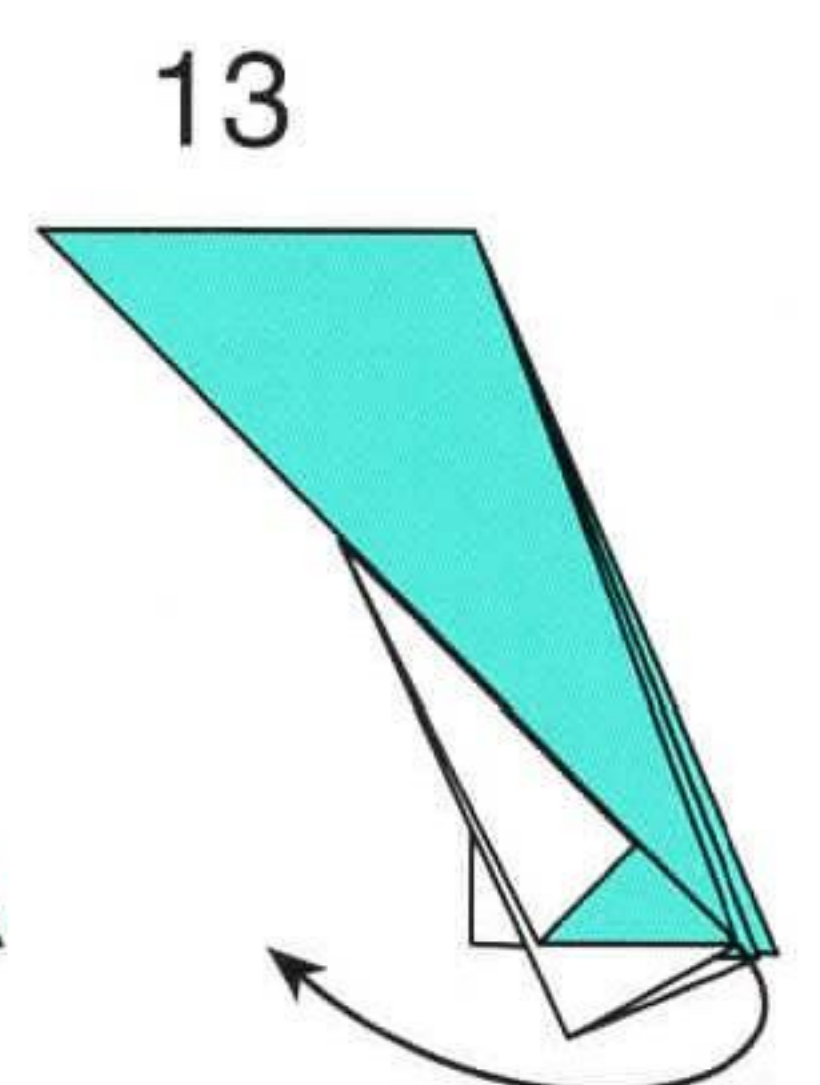
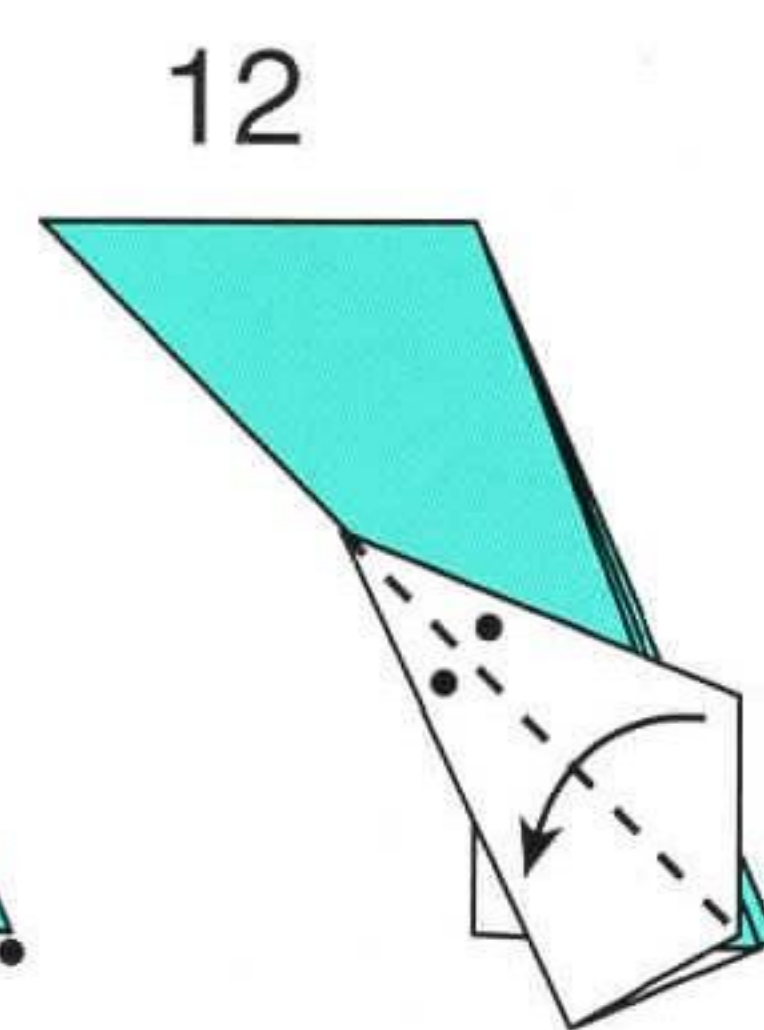
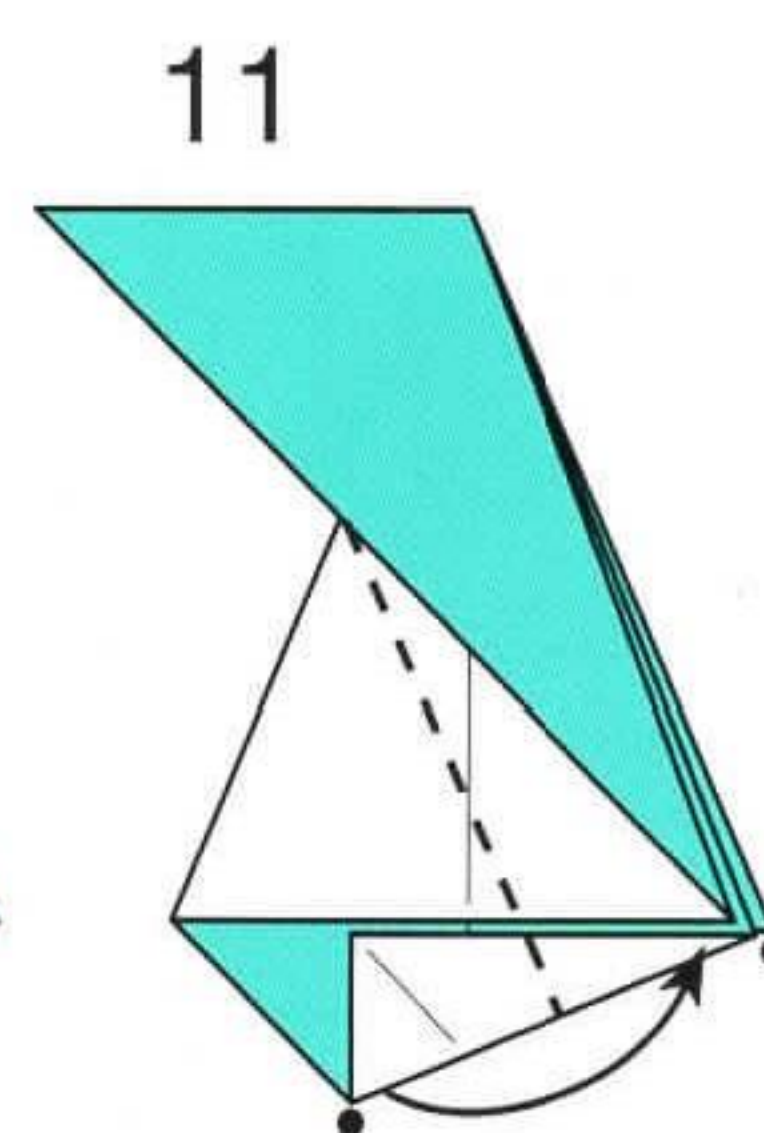
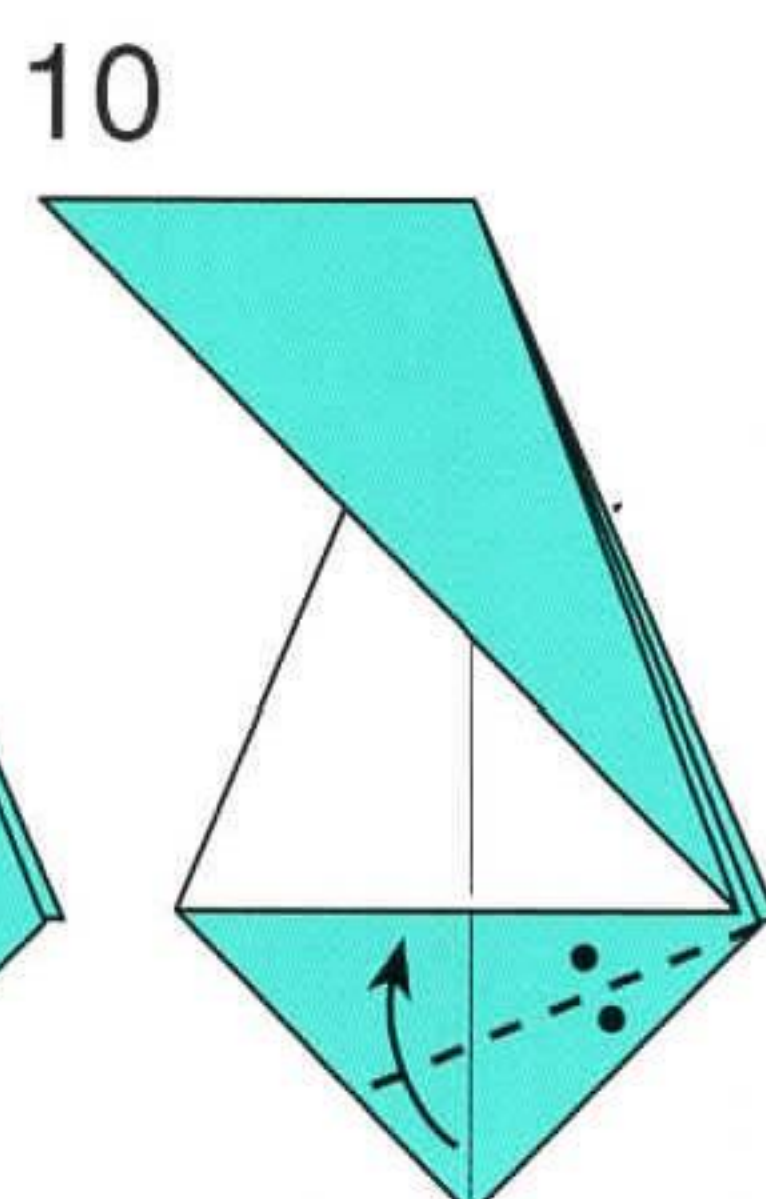
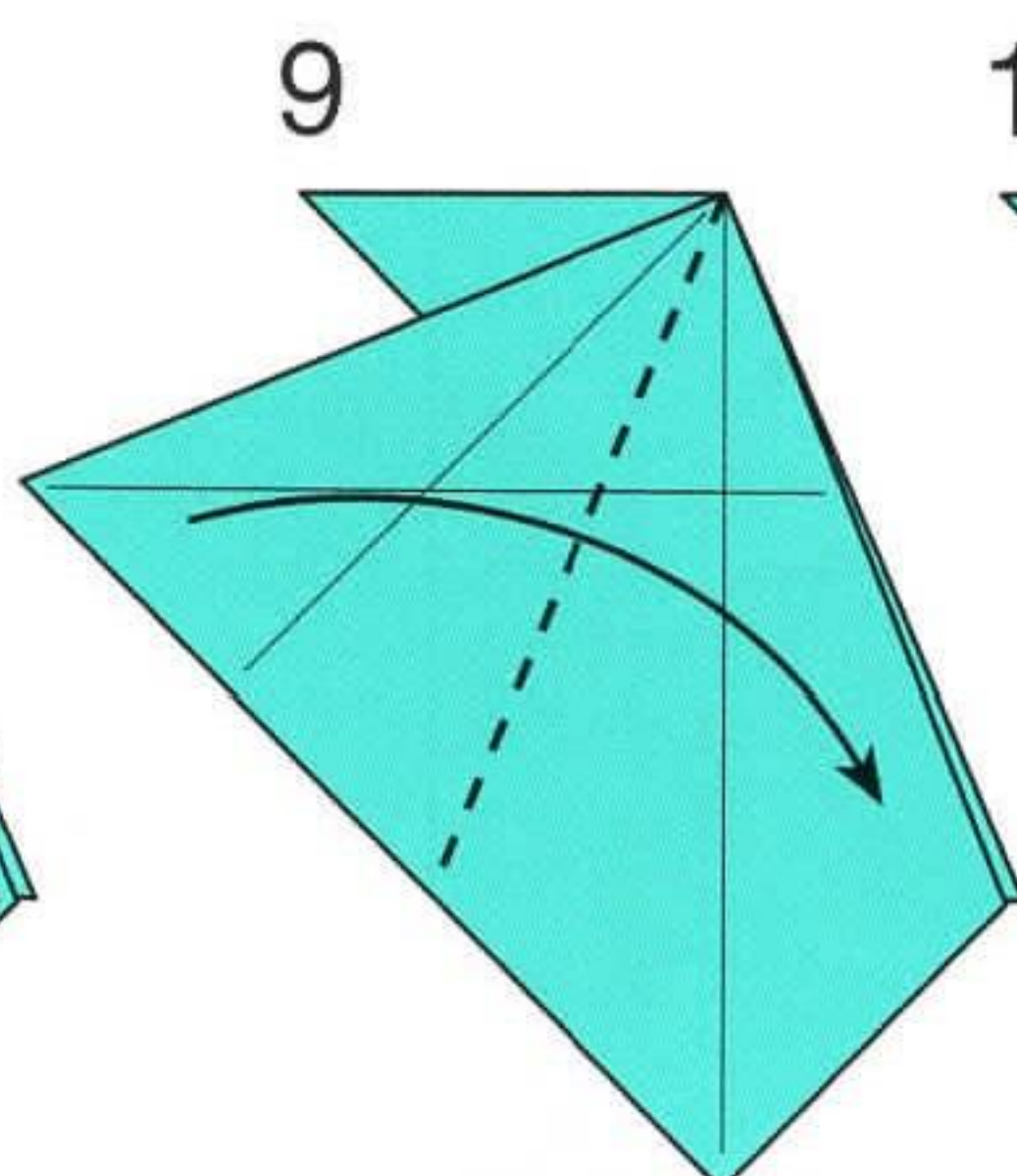
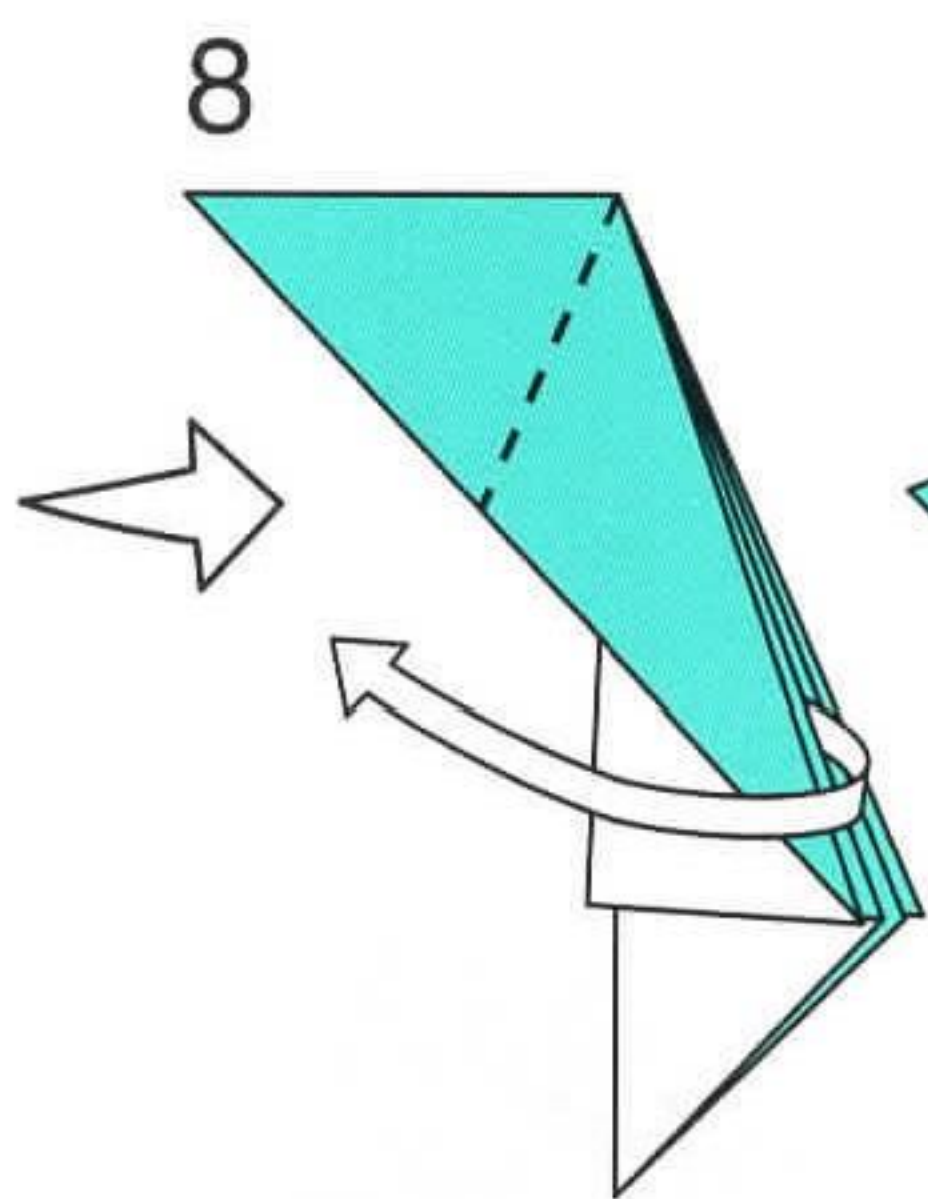
Theme: Theorem

Fold using 6" (15 cm) origami paper.

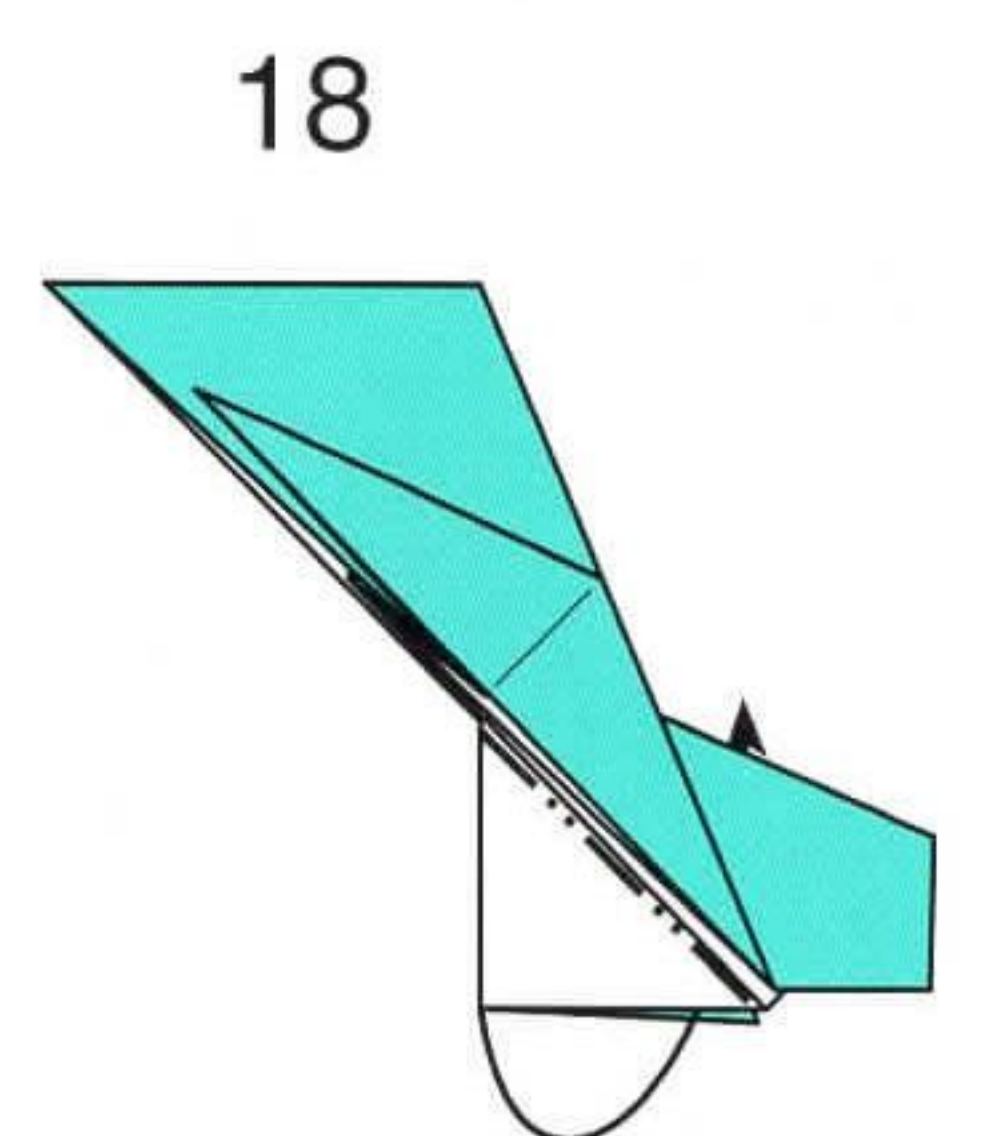
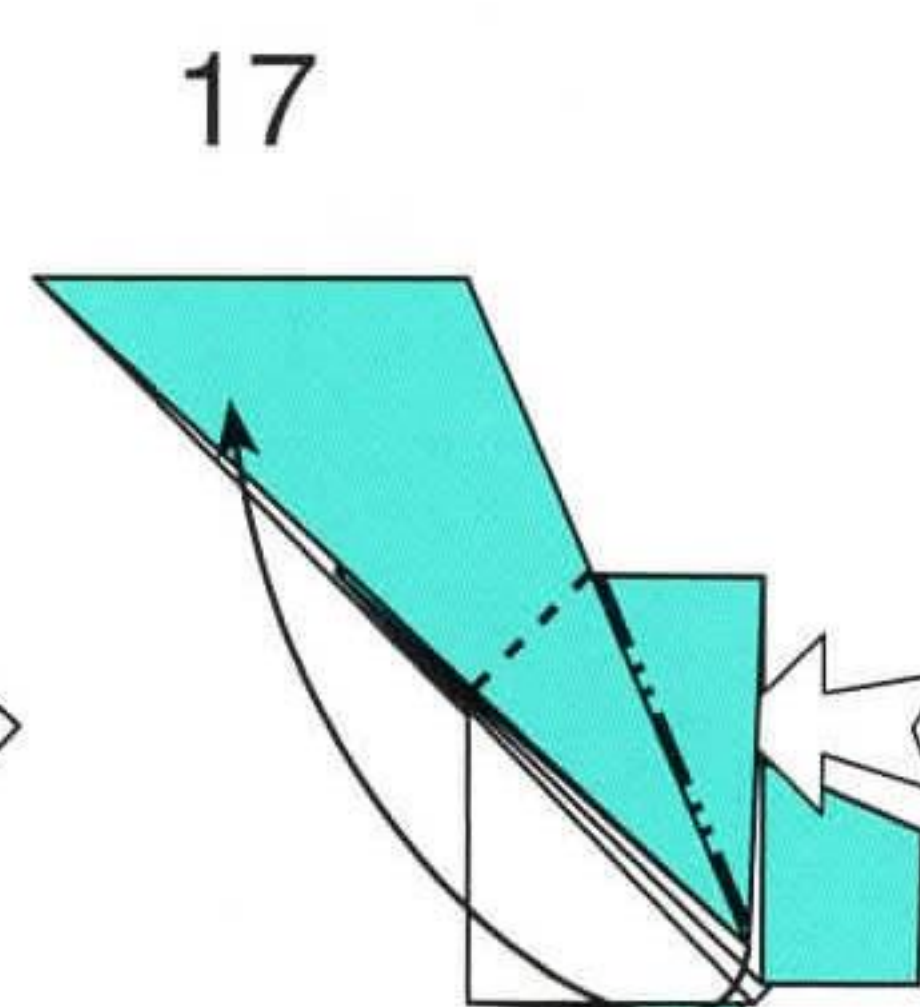
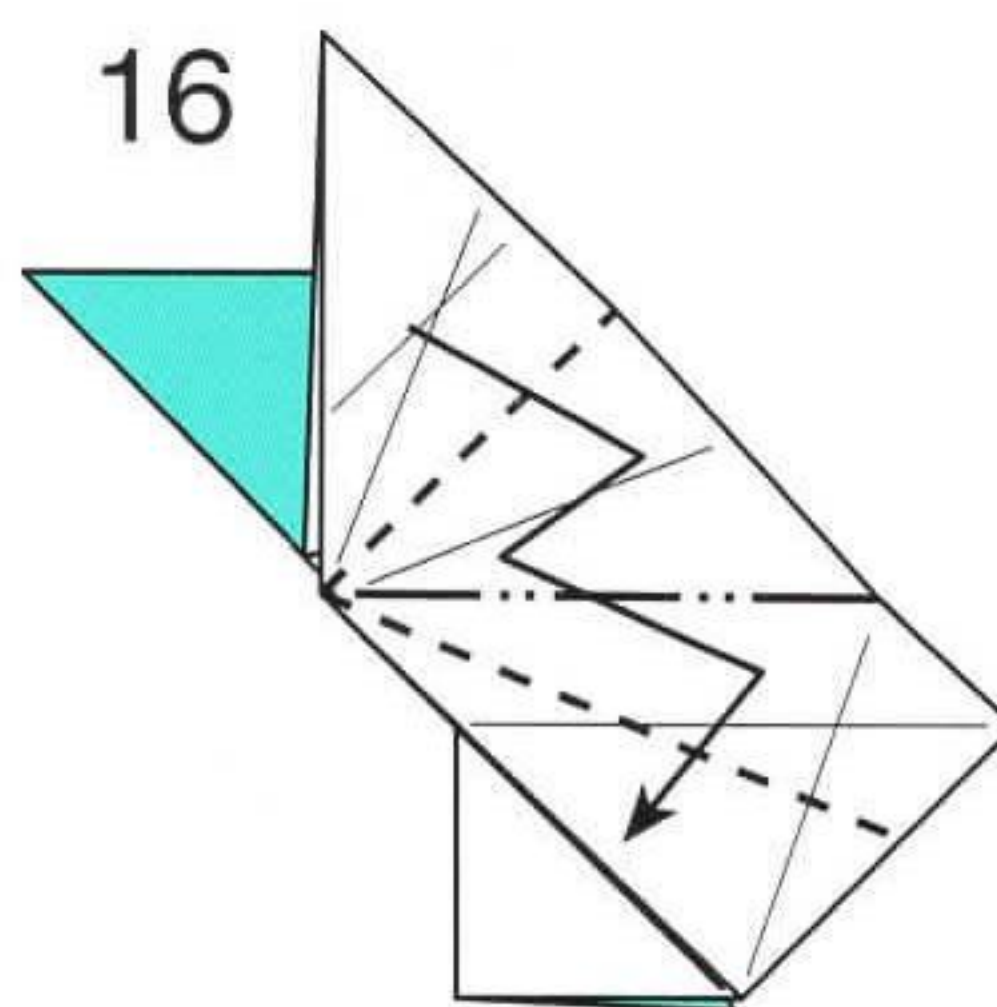
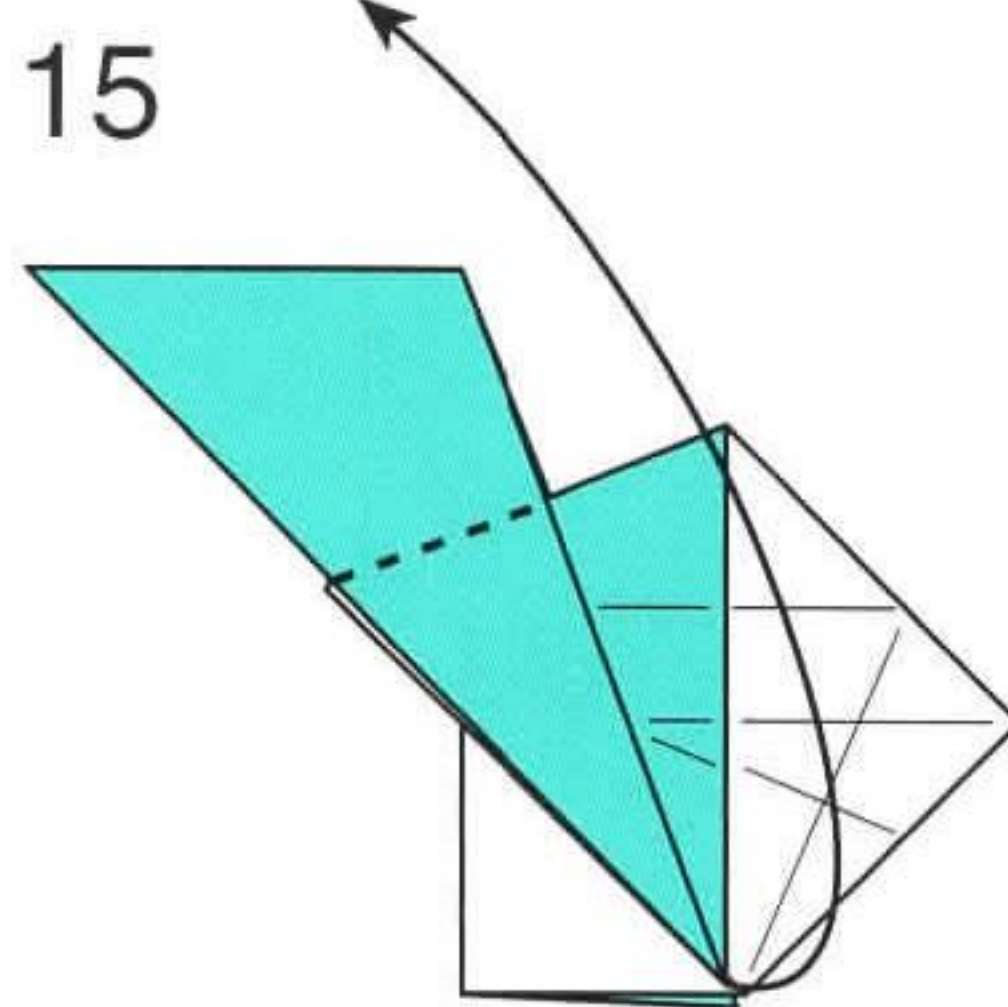
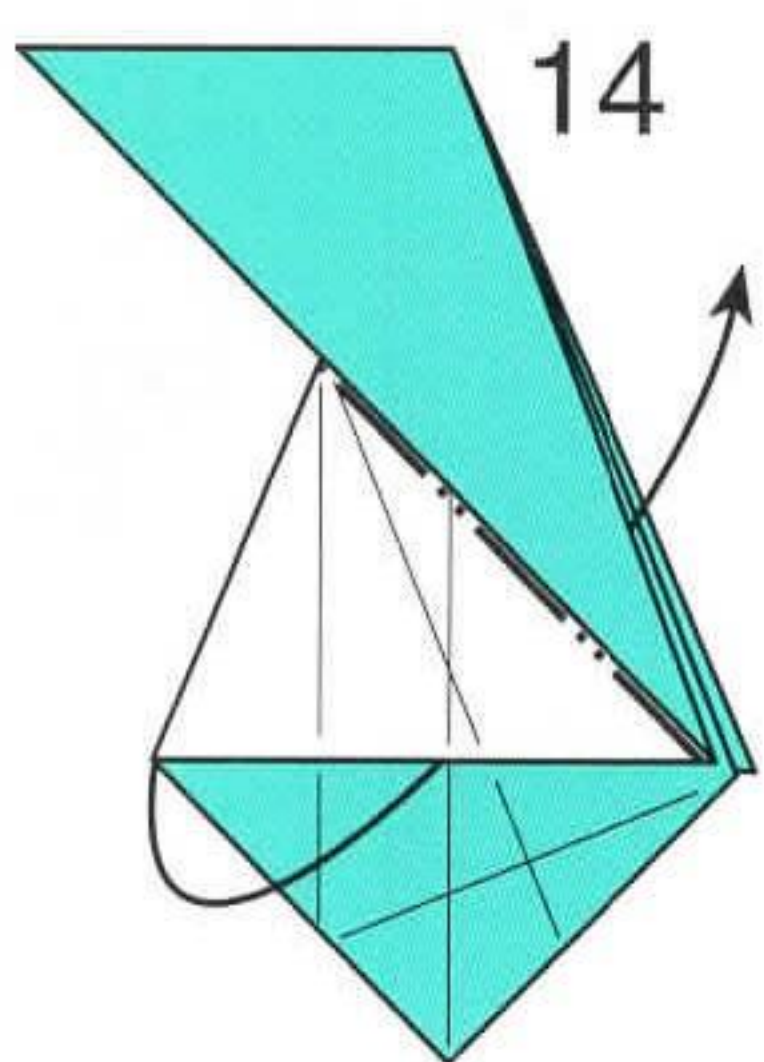


Pleat like a fan.

Unfold back to step 3.

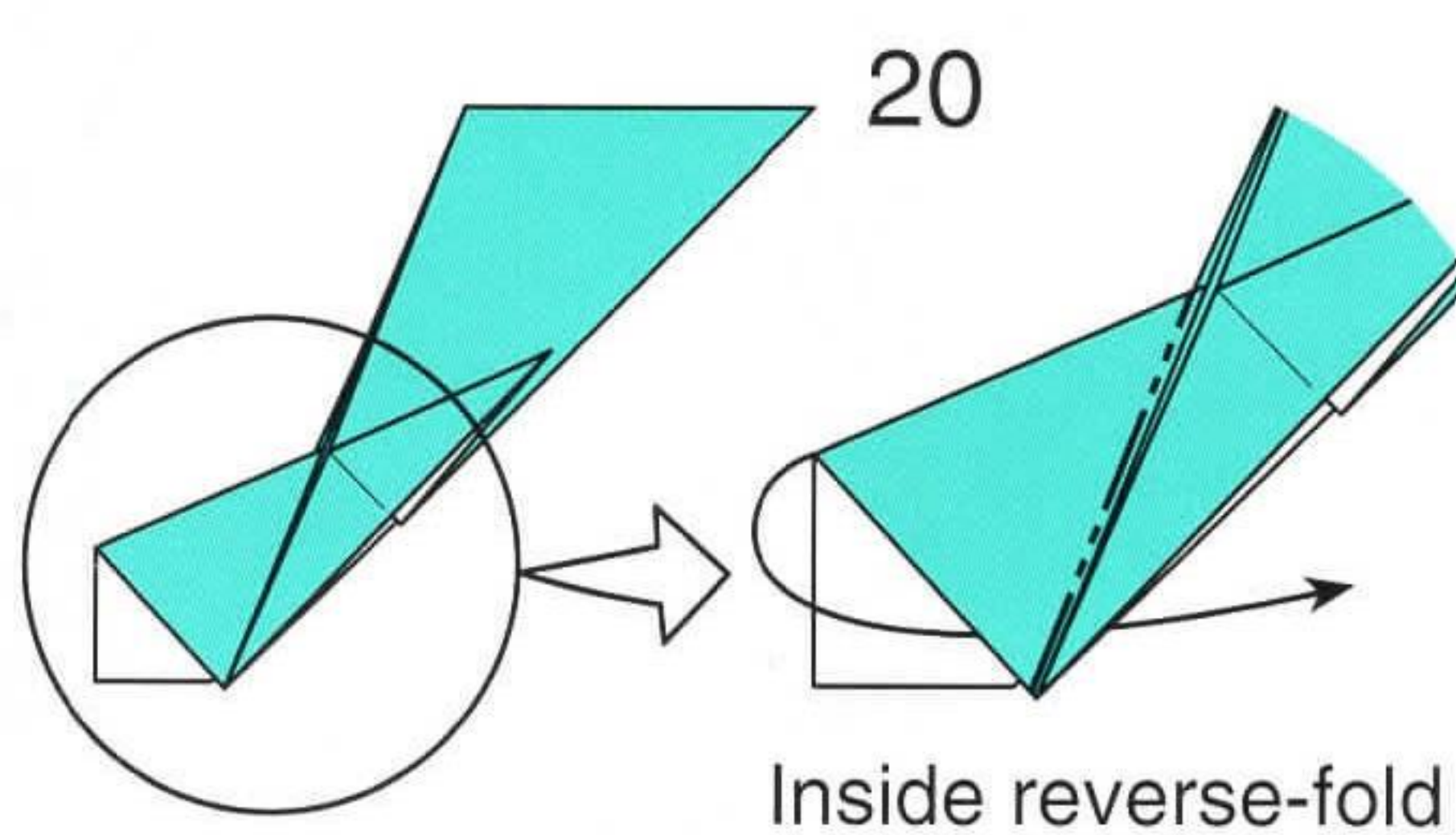
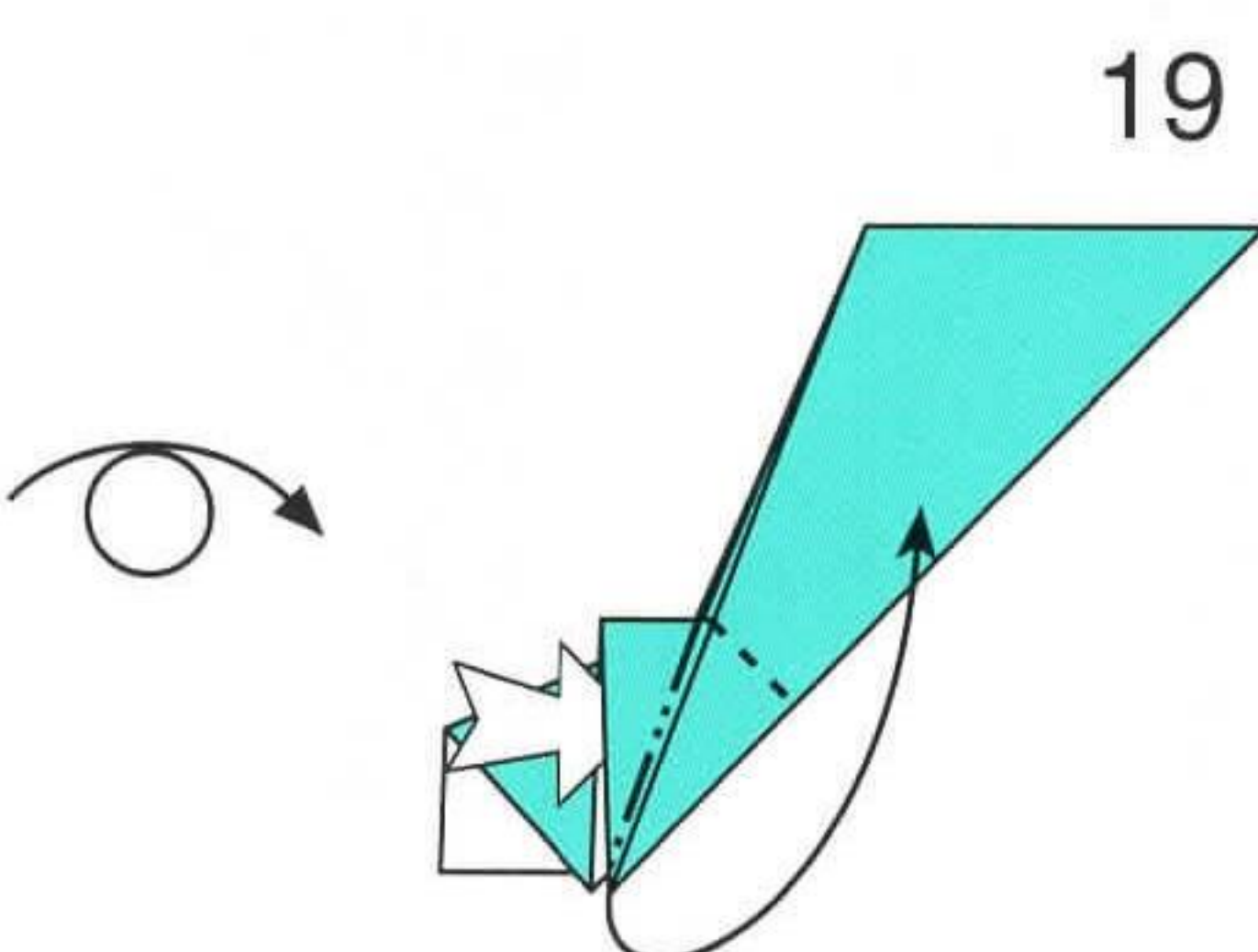


Unfold back to step 10.

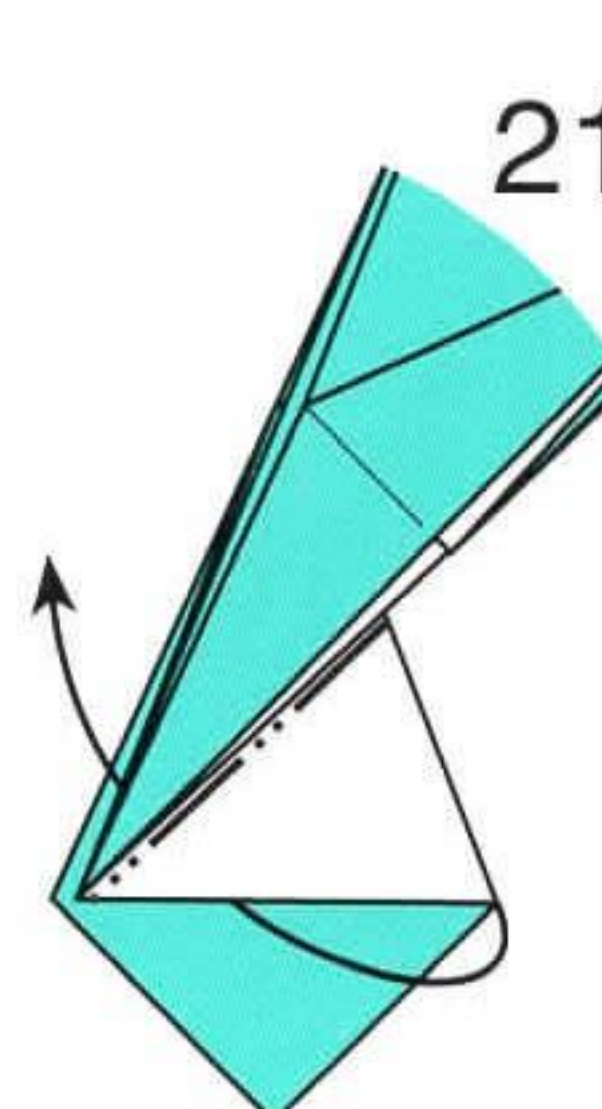


Inside reverse-fold

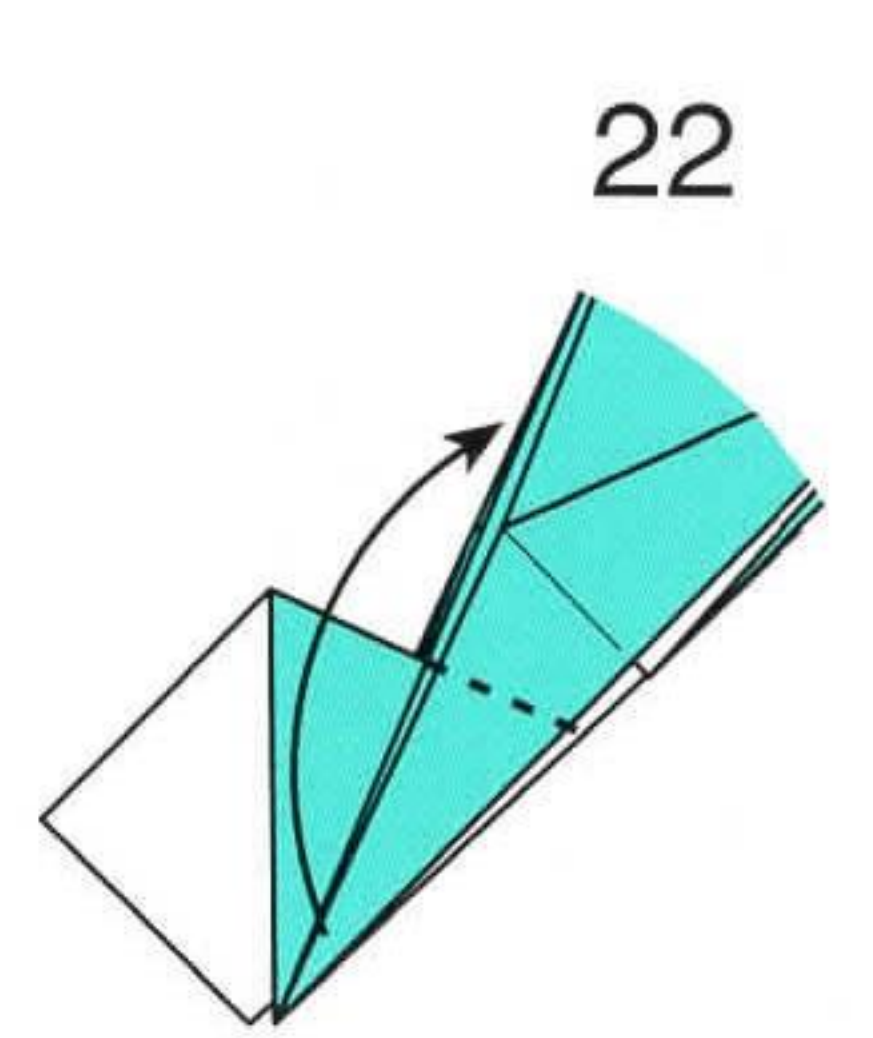
Inside reverse-fold

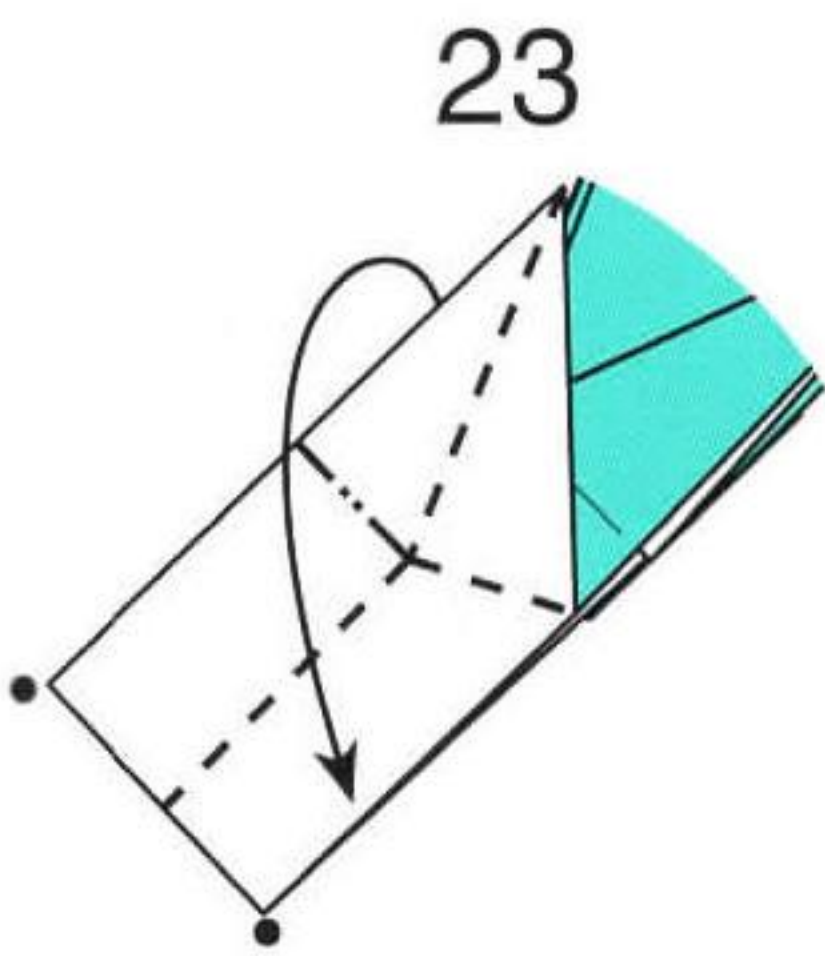


Inside reverse-fold

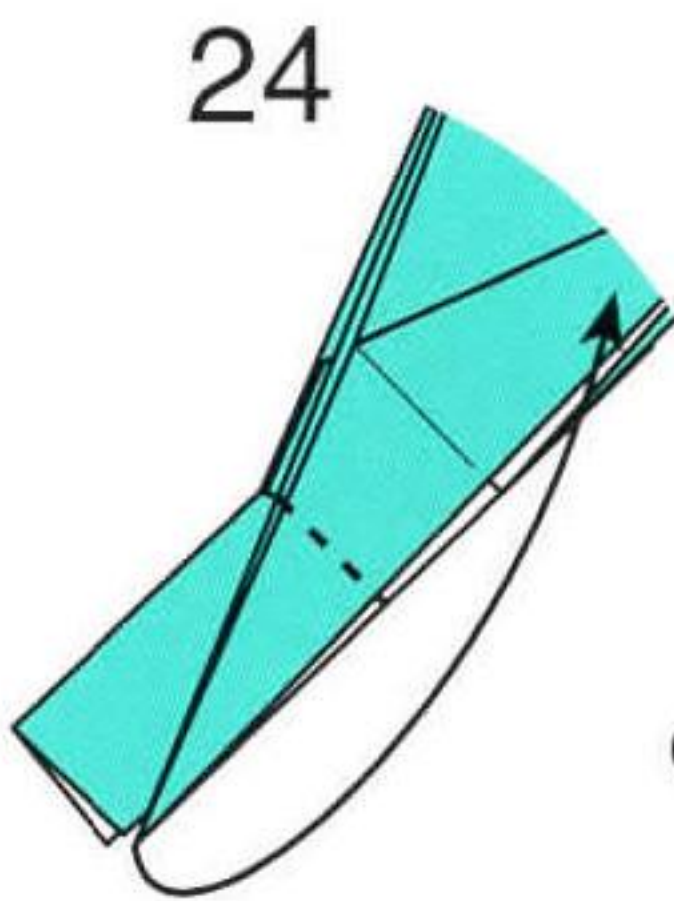


Inside reverse-fold

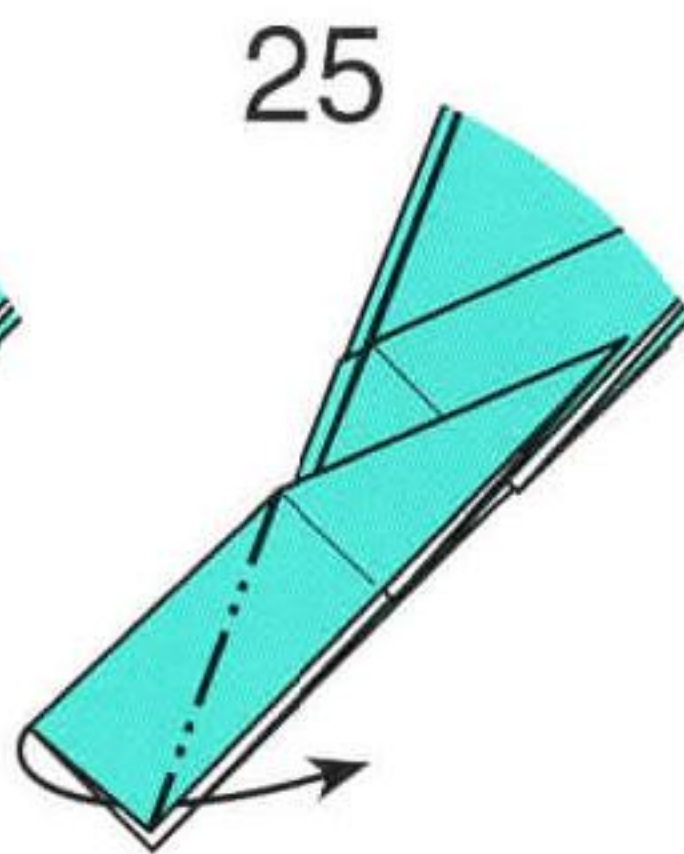




23

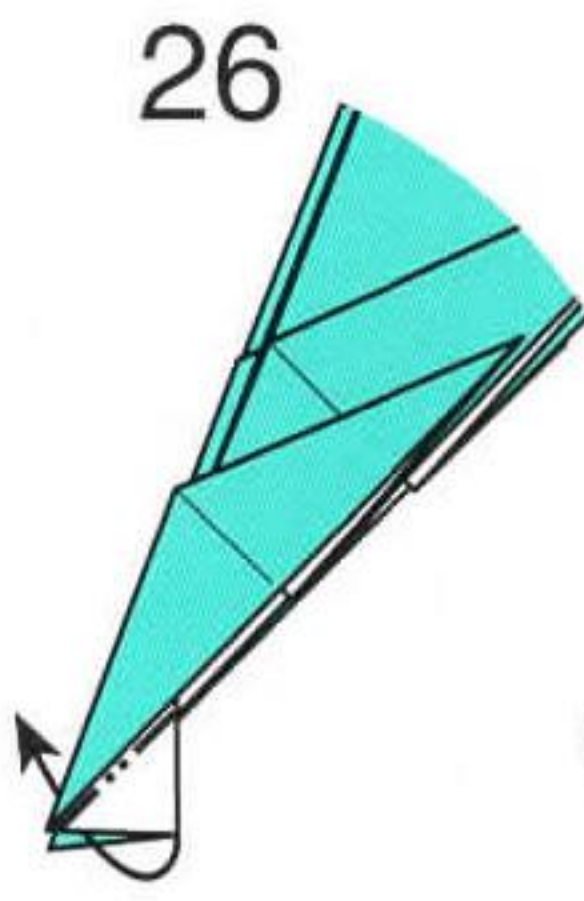


24



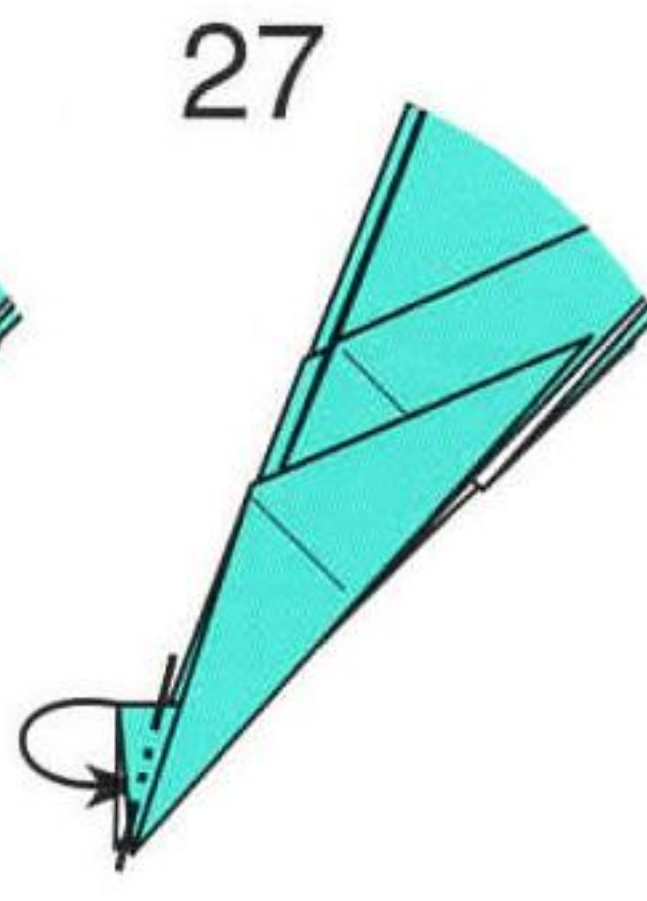
25

Inside
reverse-fold



26

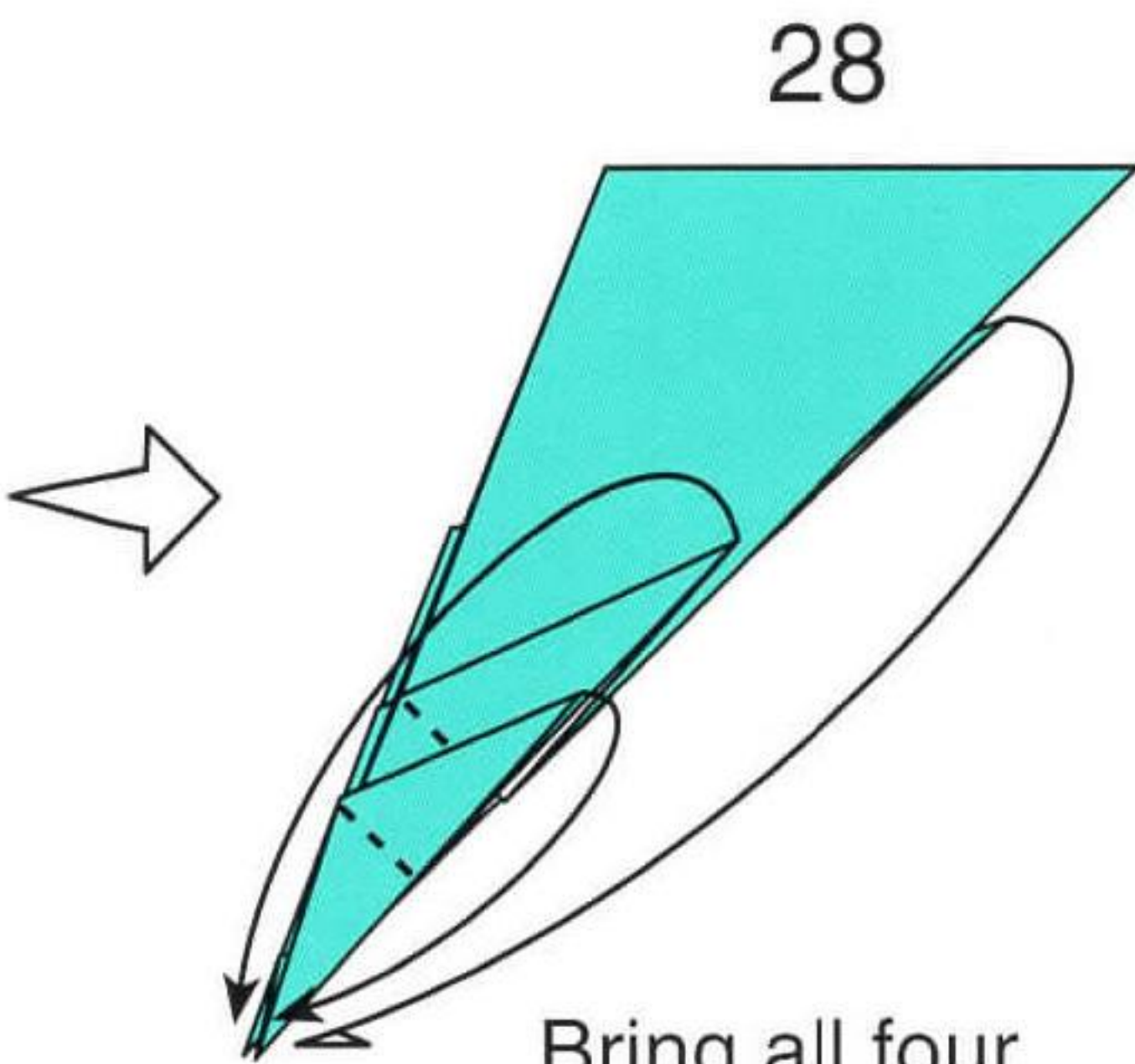
Inside
reverse-fold



27

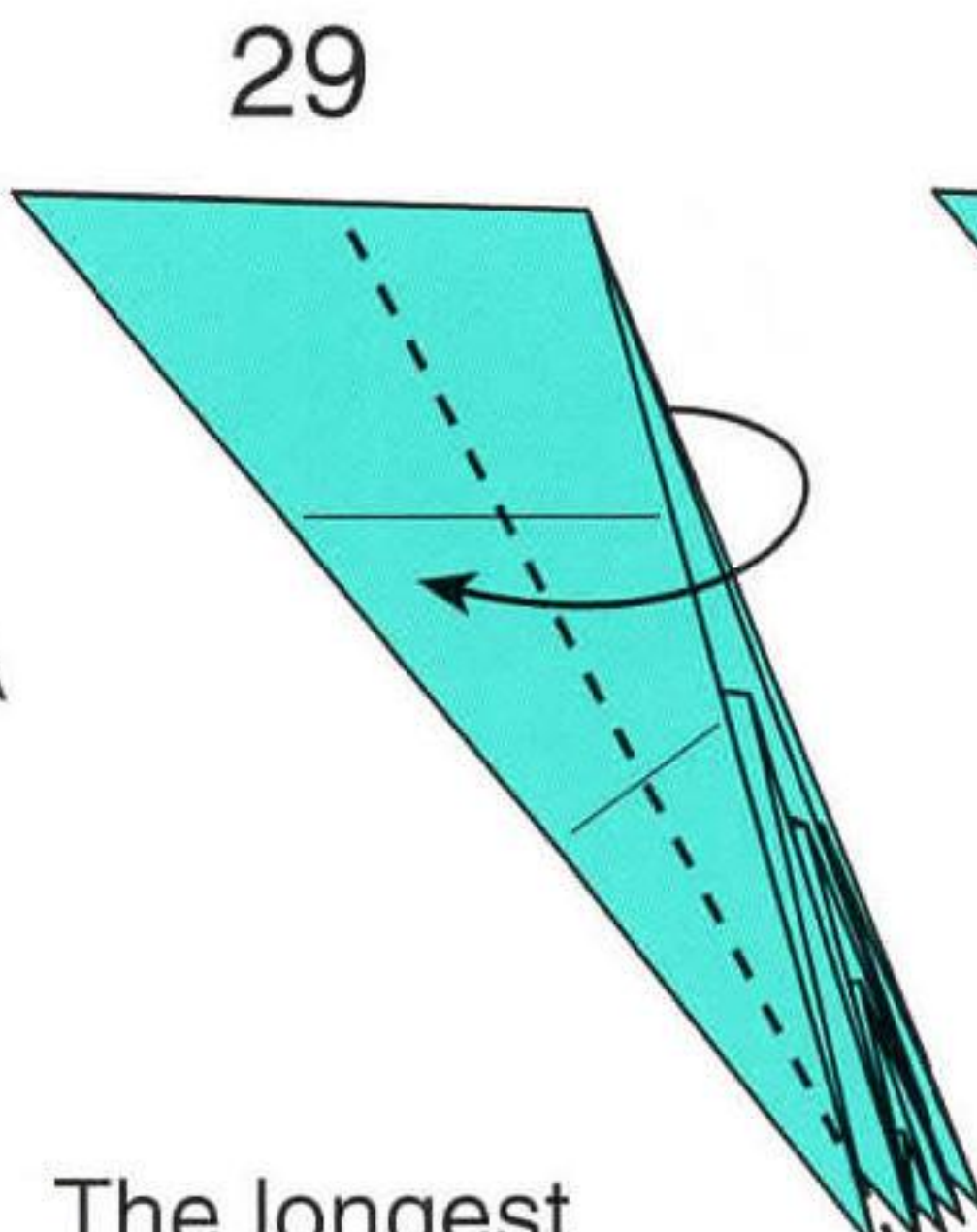
Inside
reverse-fold

The white part in step 23 has the same shape as that in step 16, though they are mirror images. That means, you can repeat steps 16-22 instead of step 23, and continue repeating as many times as you want to make smaller branches. Such "infinitely foldable structure," also seen in *Conch* and other models later in the book, is one of the interesting aspect of the geometry of origami.



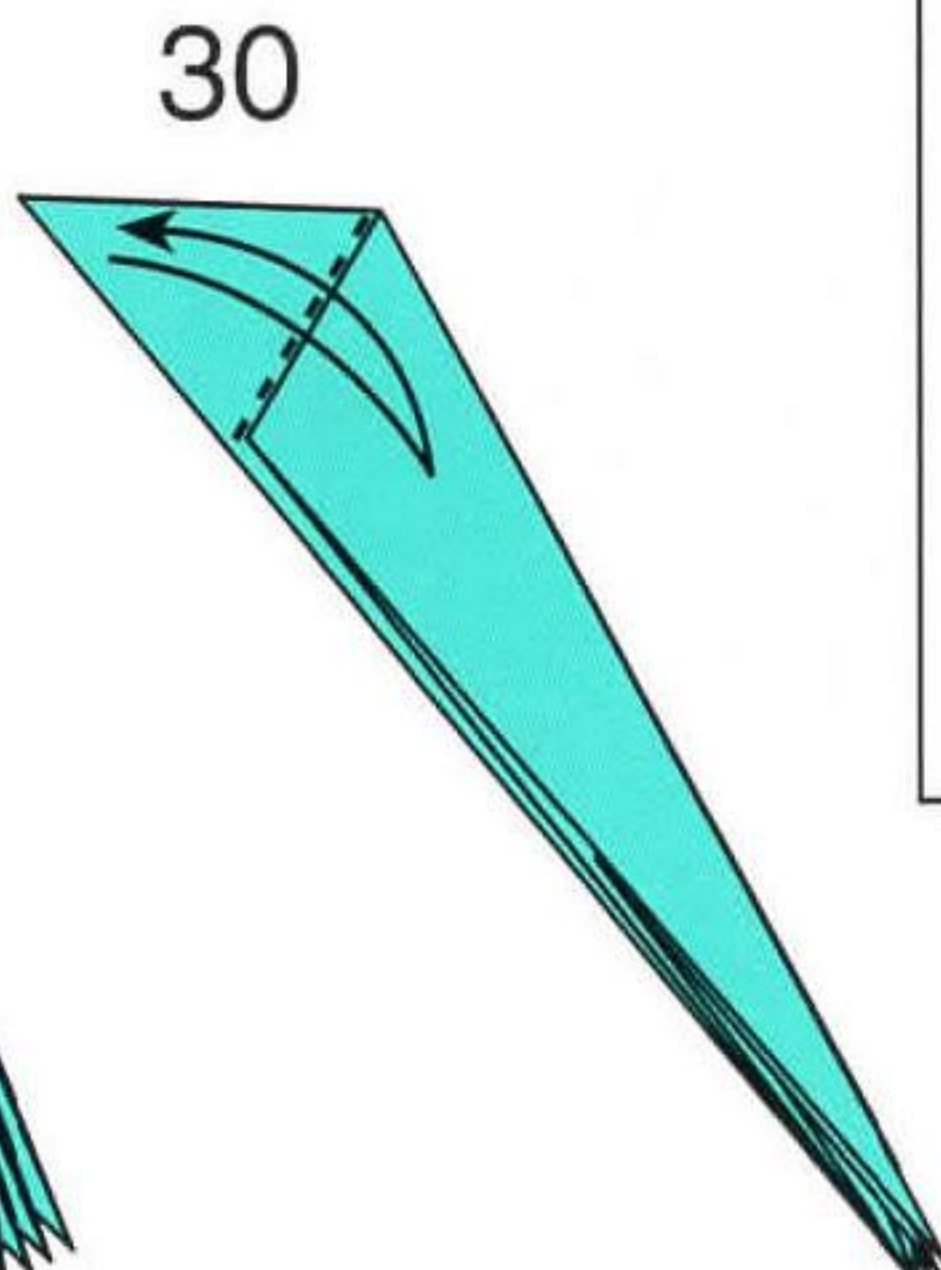
28

Bring all four
points together.

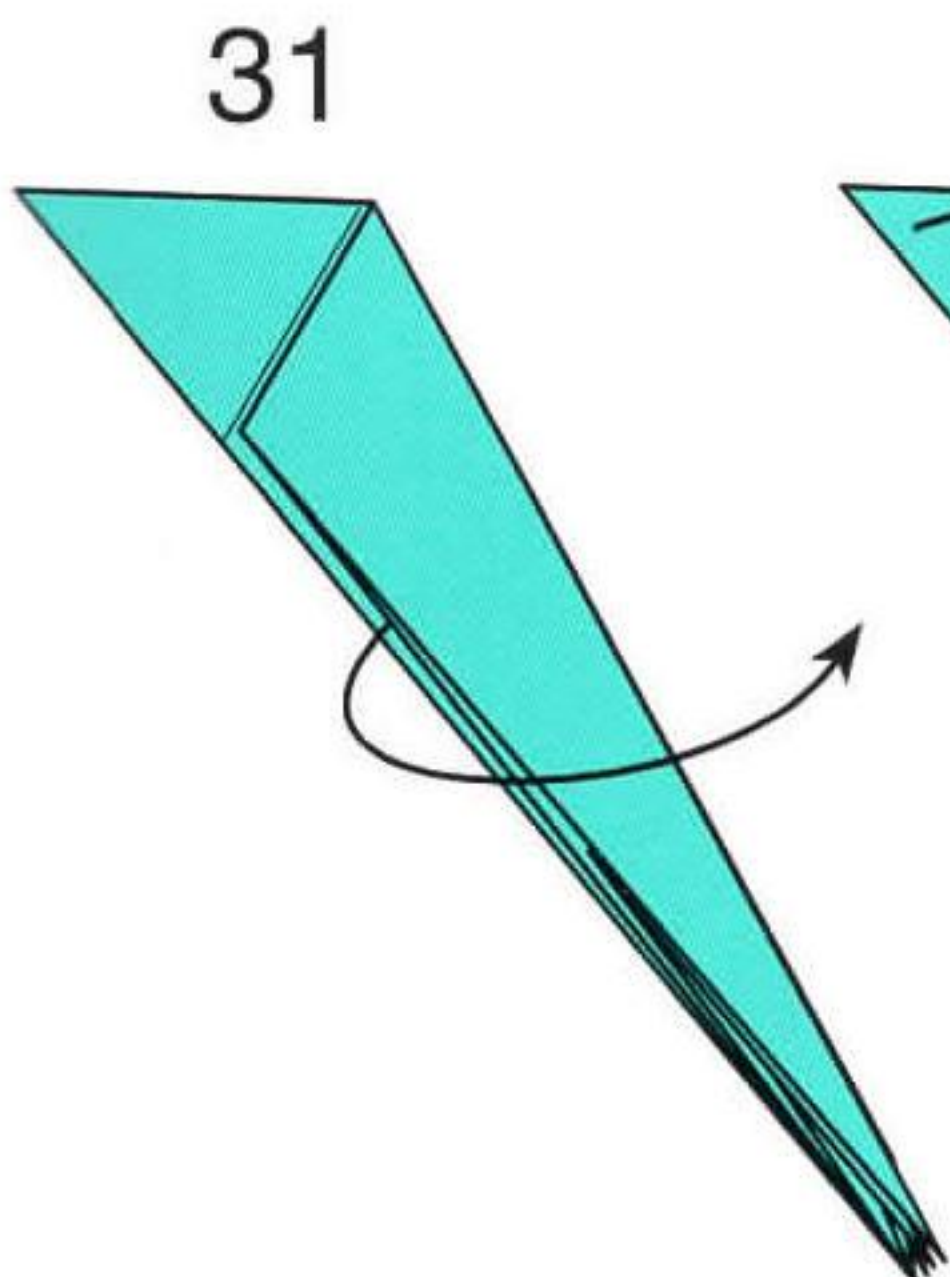


29

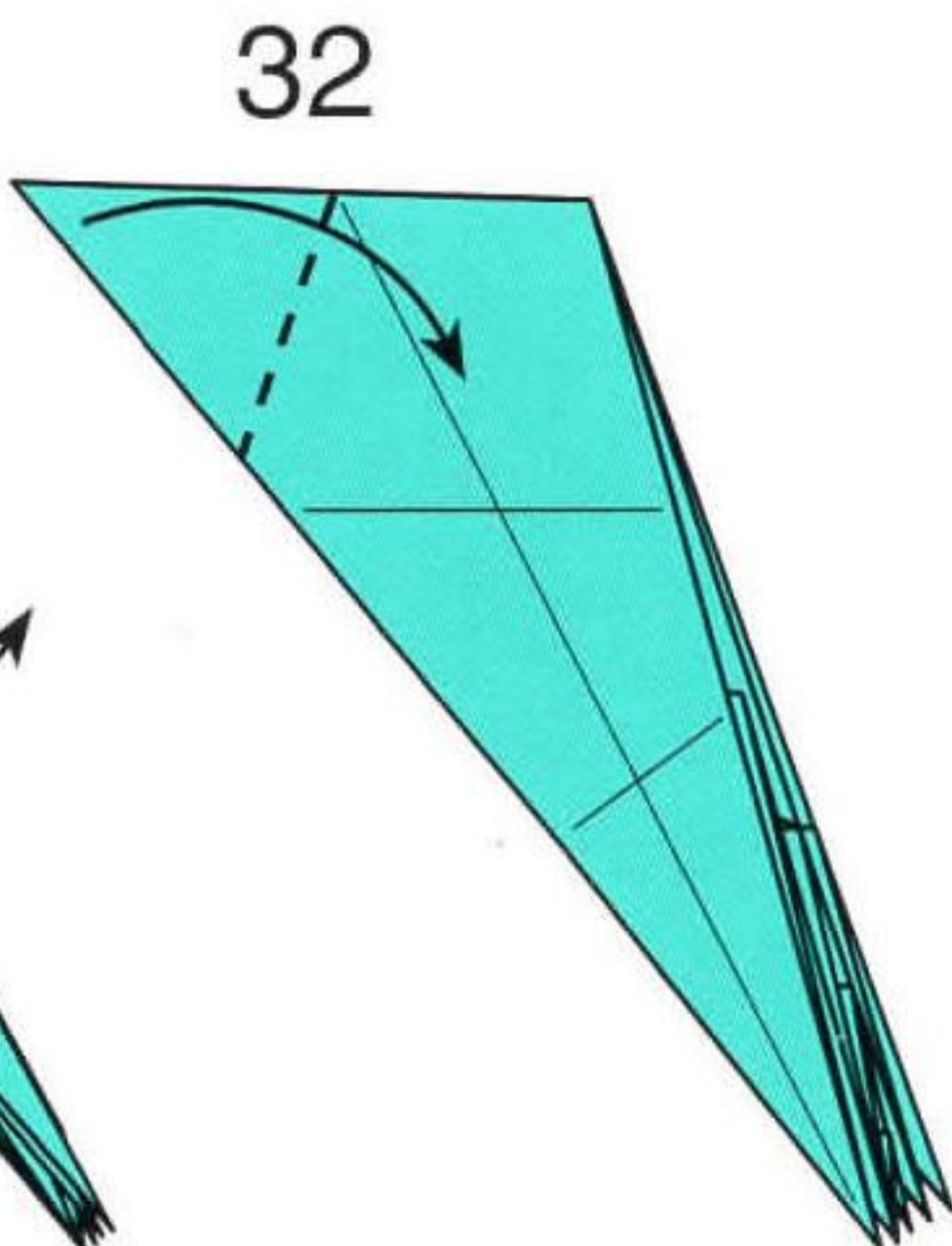
The longest
branch is on top.



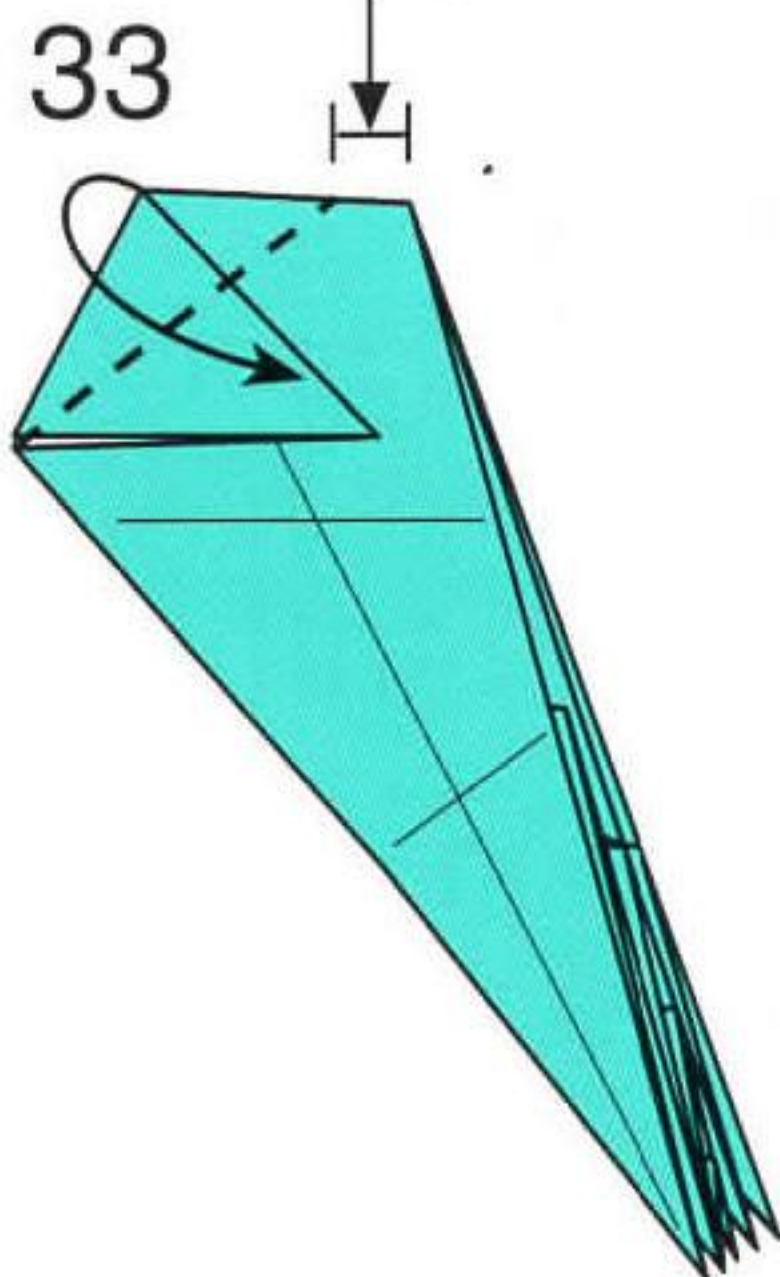
30



31

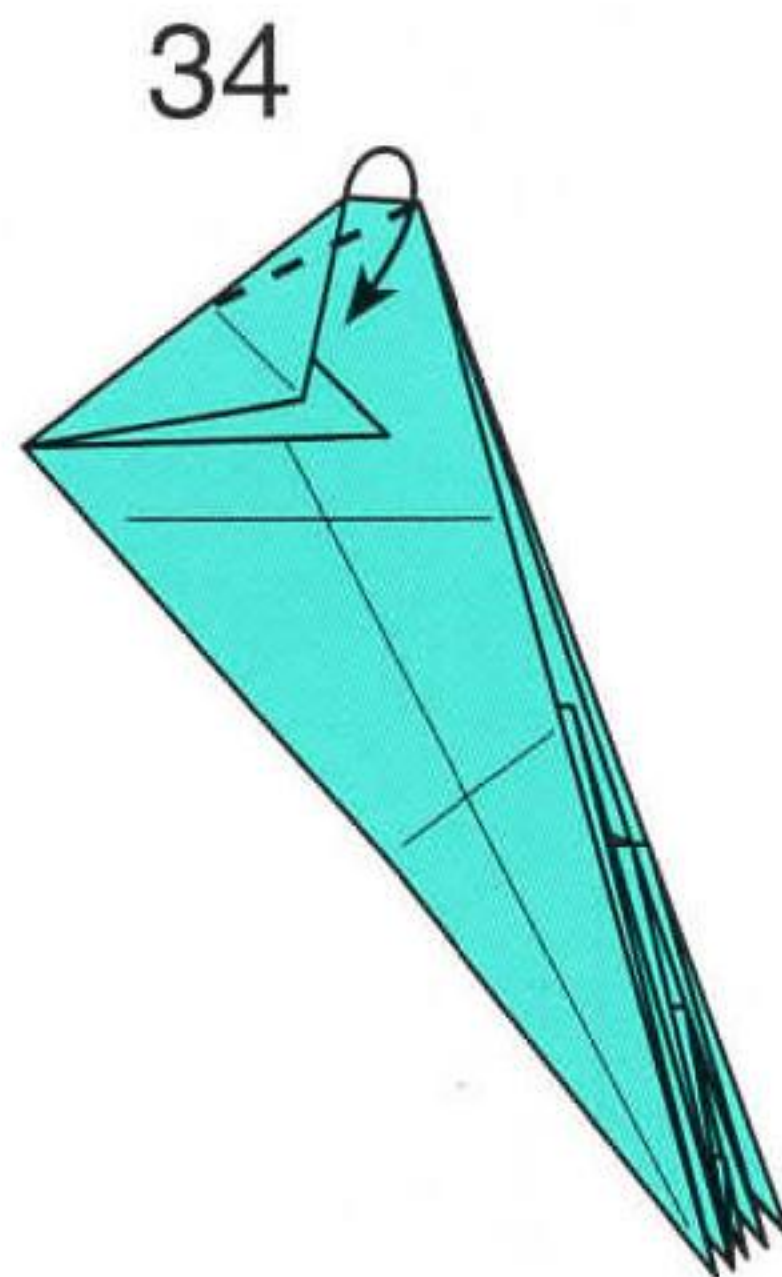


32

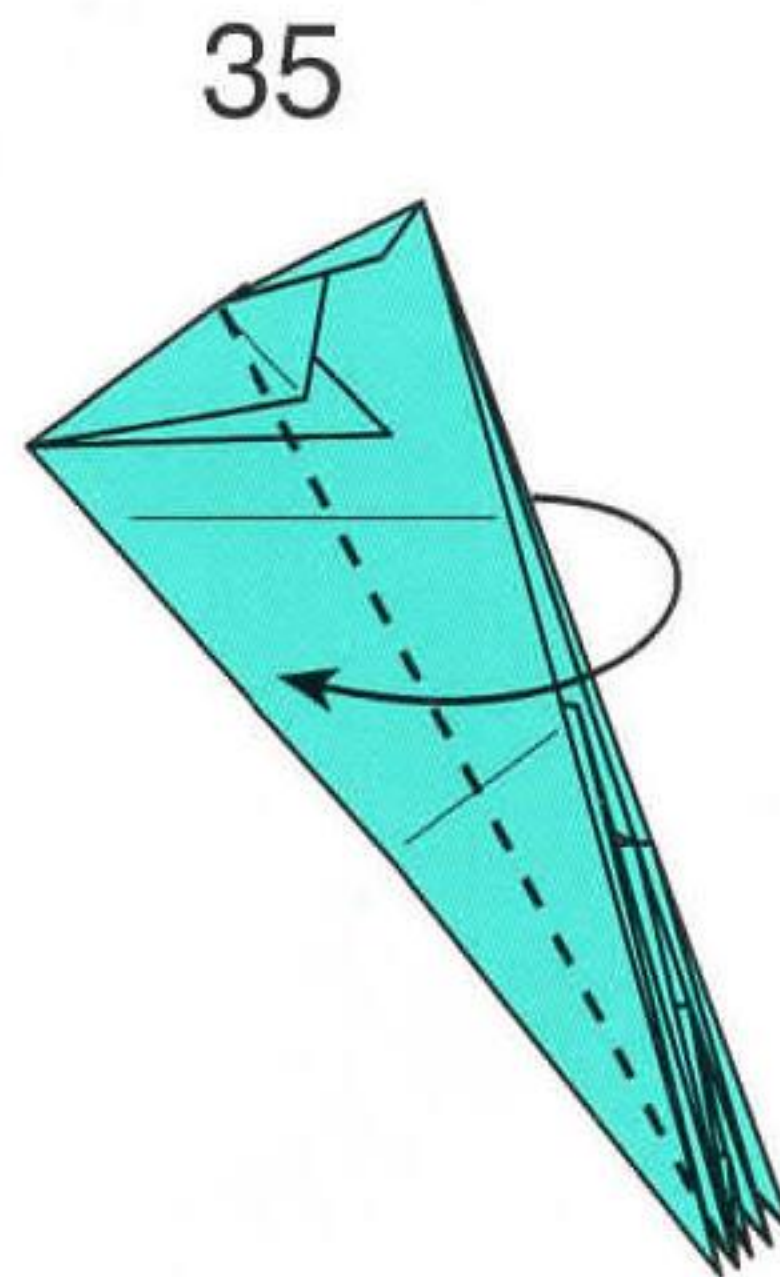


33

Leave a
small gap.

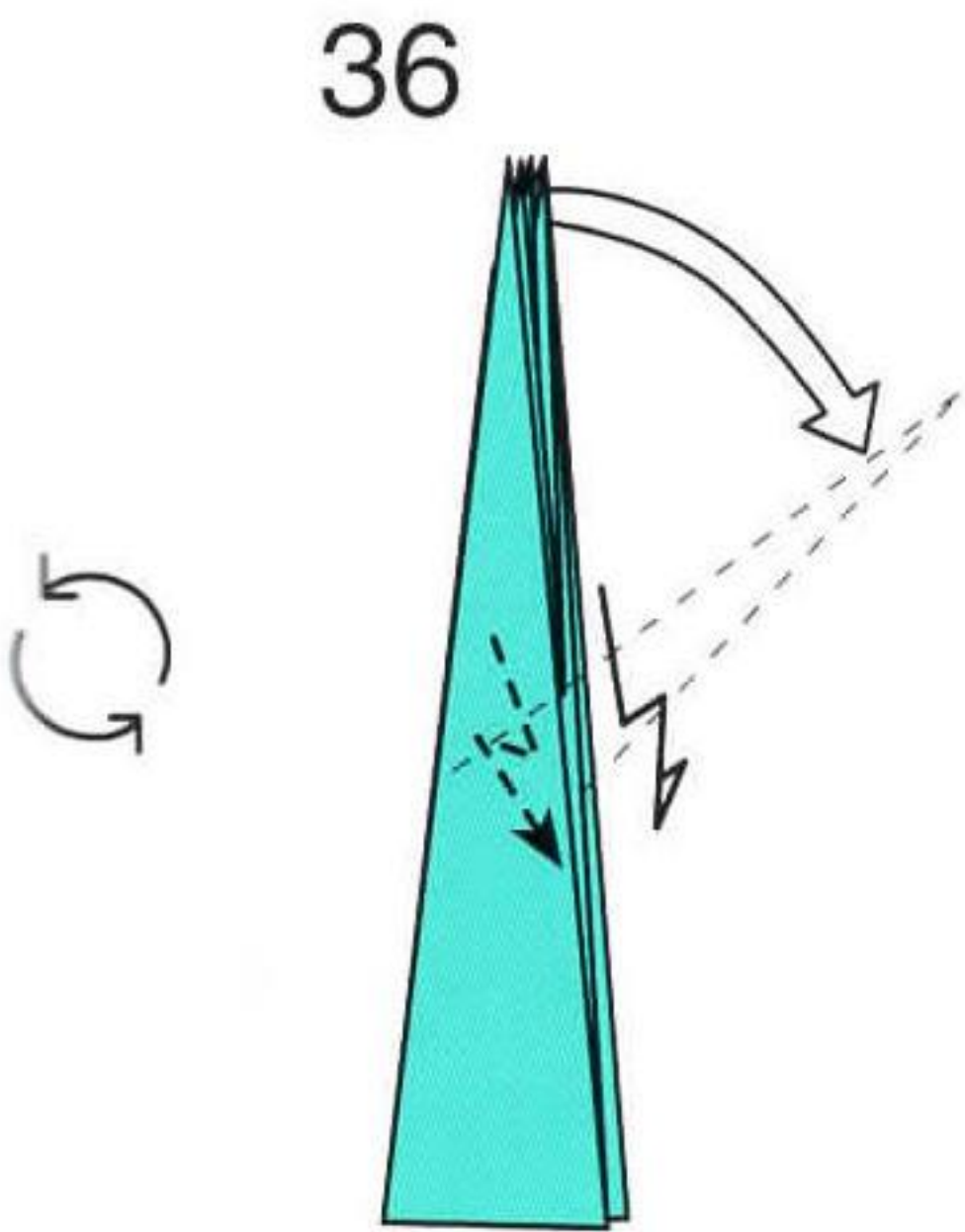


34



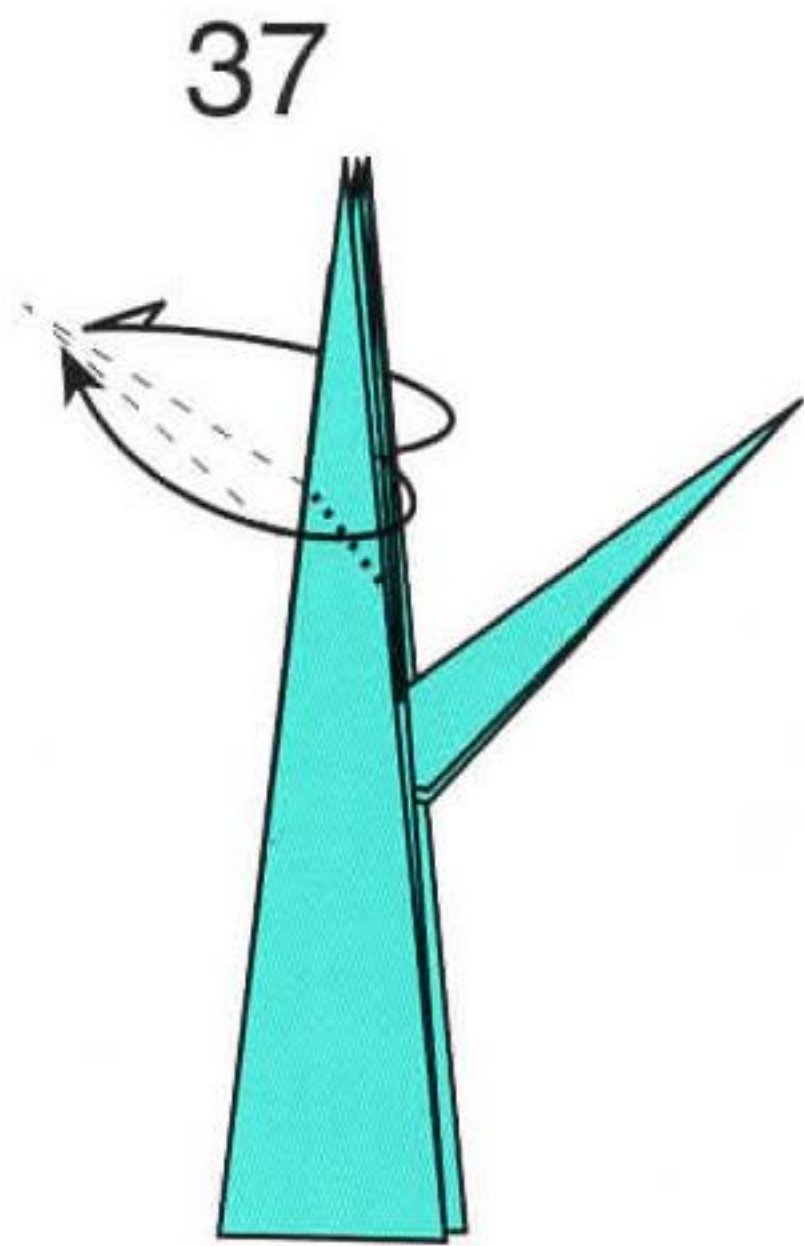
35

The model should be
an isosceles triangle
when folded in step 35.



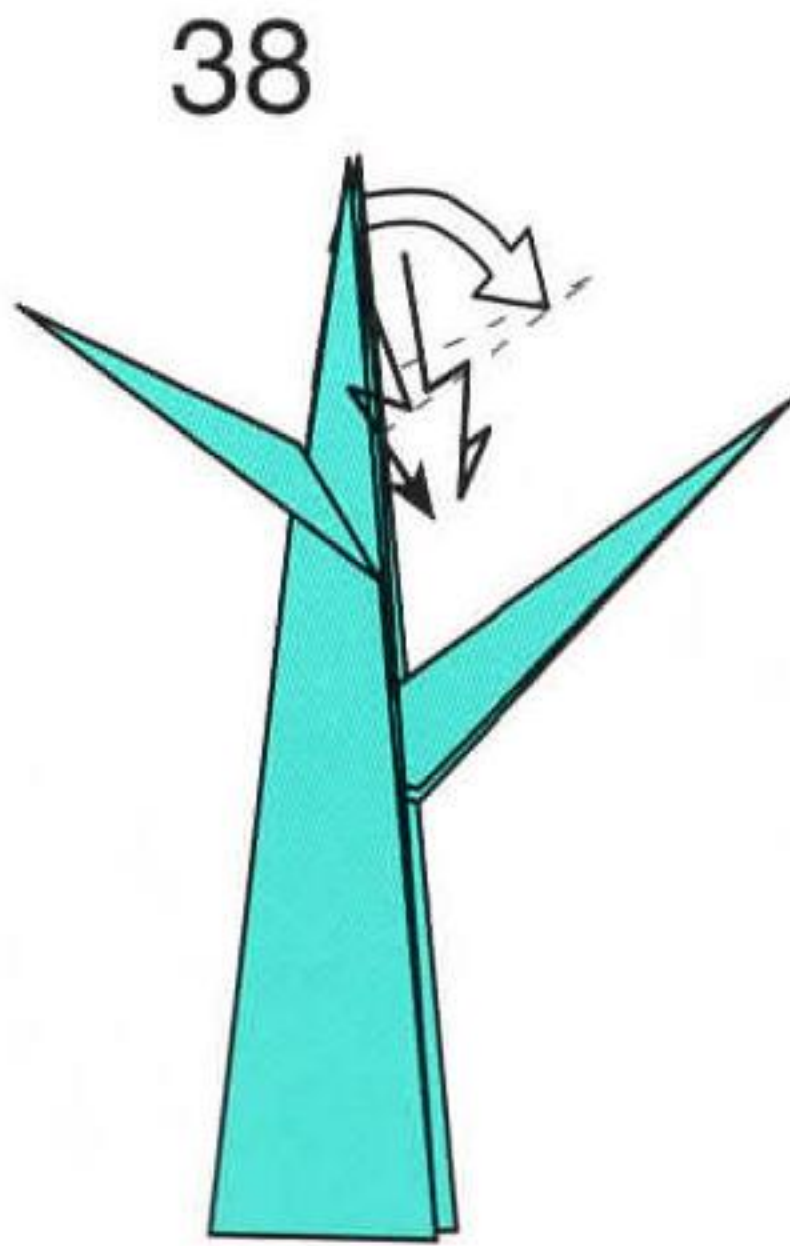
36

Crimp at the root of
the branch.



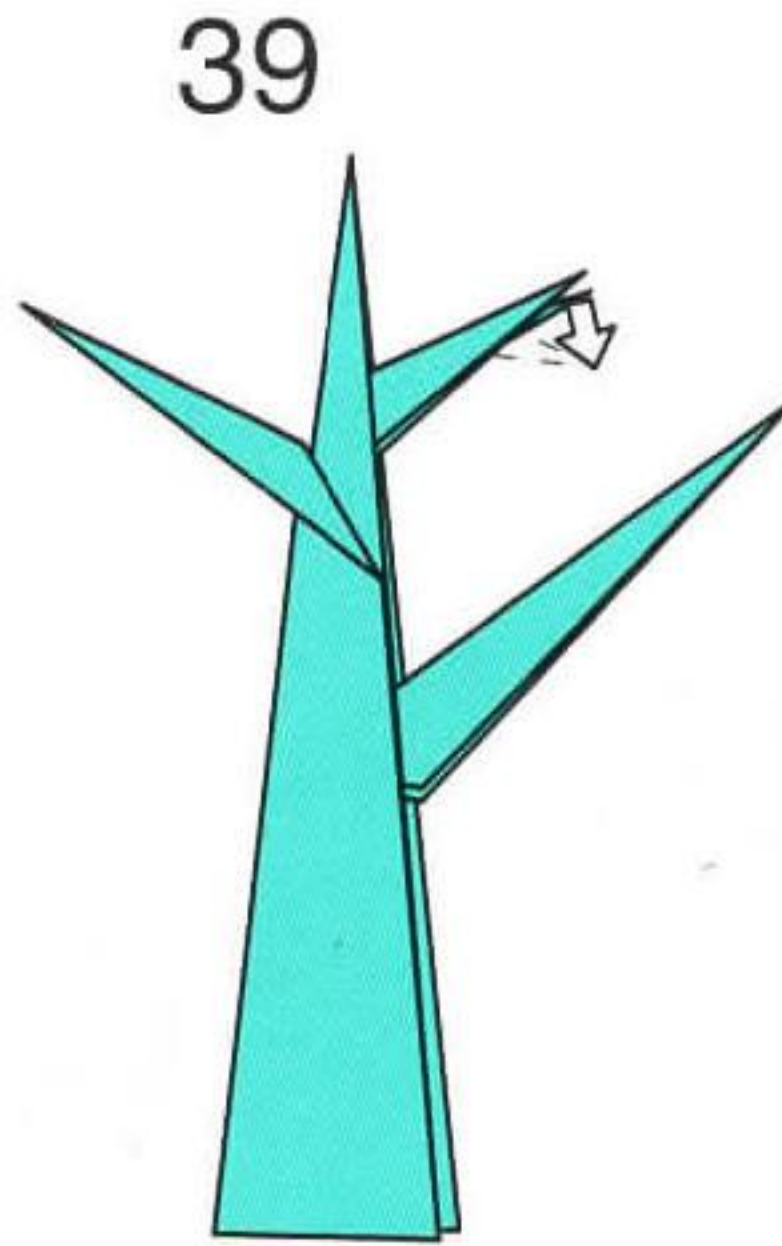
37

Outside reverse-fold

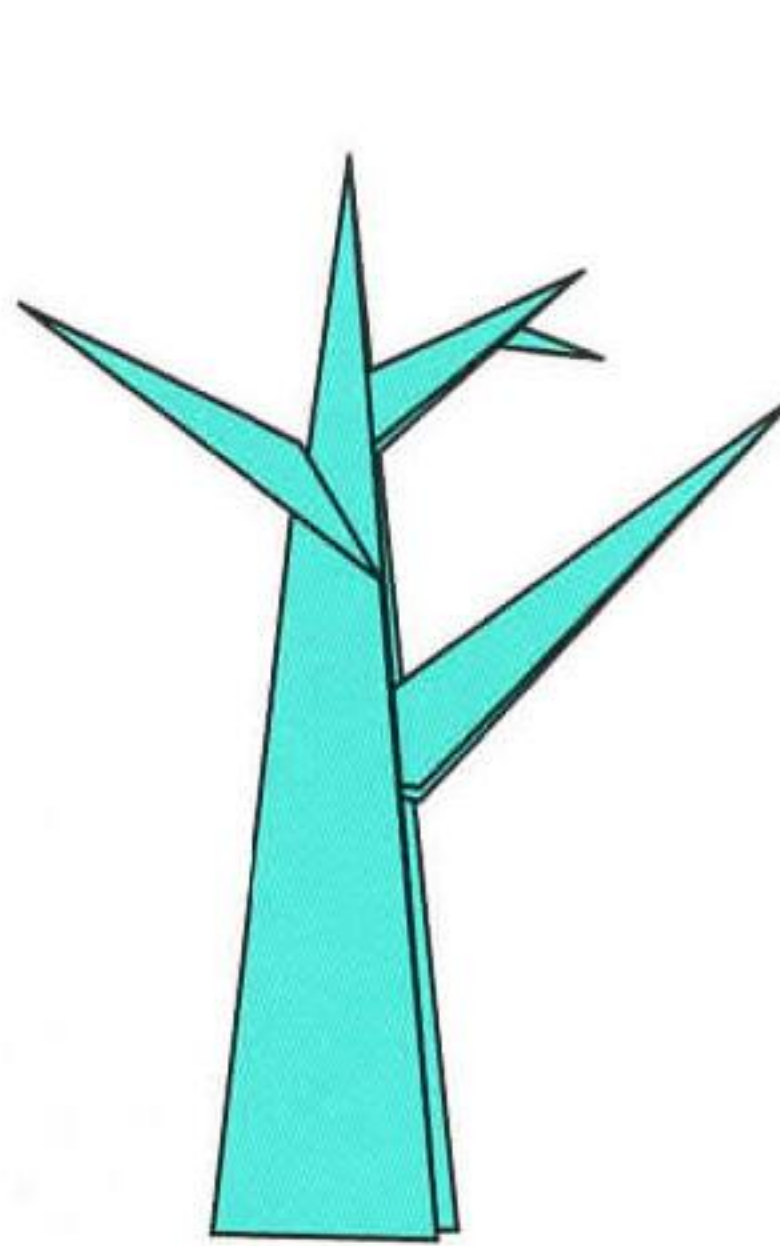


38

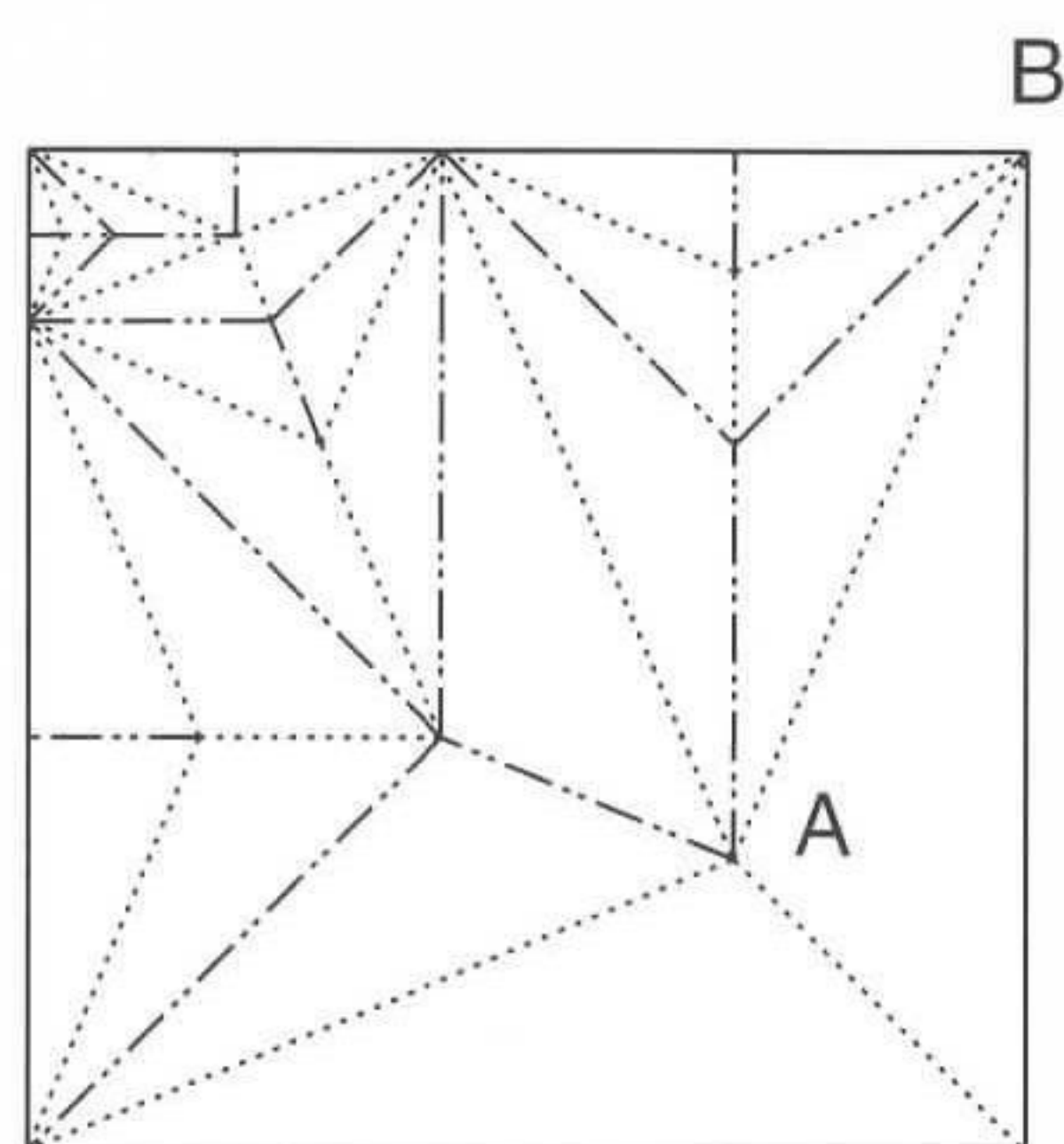
Crimp at the root of
the branch.



39



Finished. Make
the model stand
by itself.



Theorems about creases

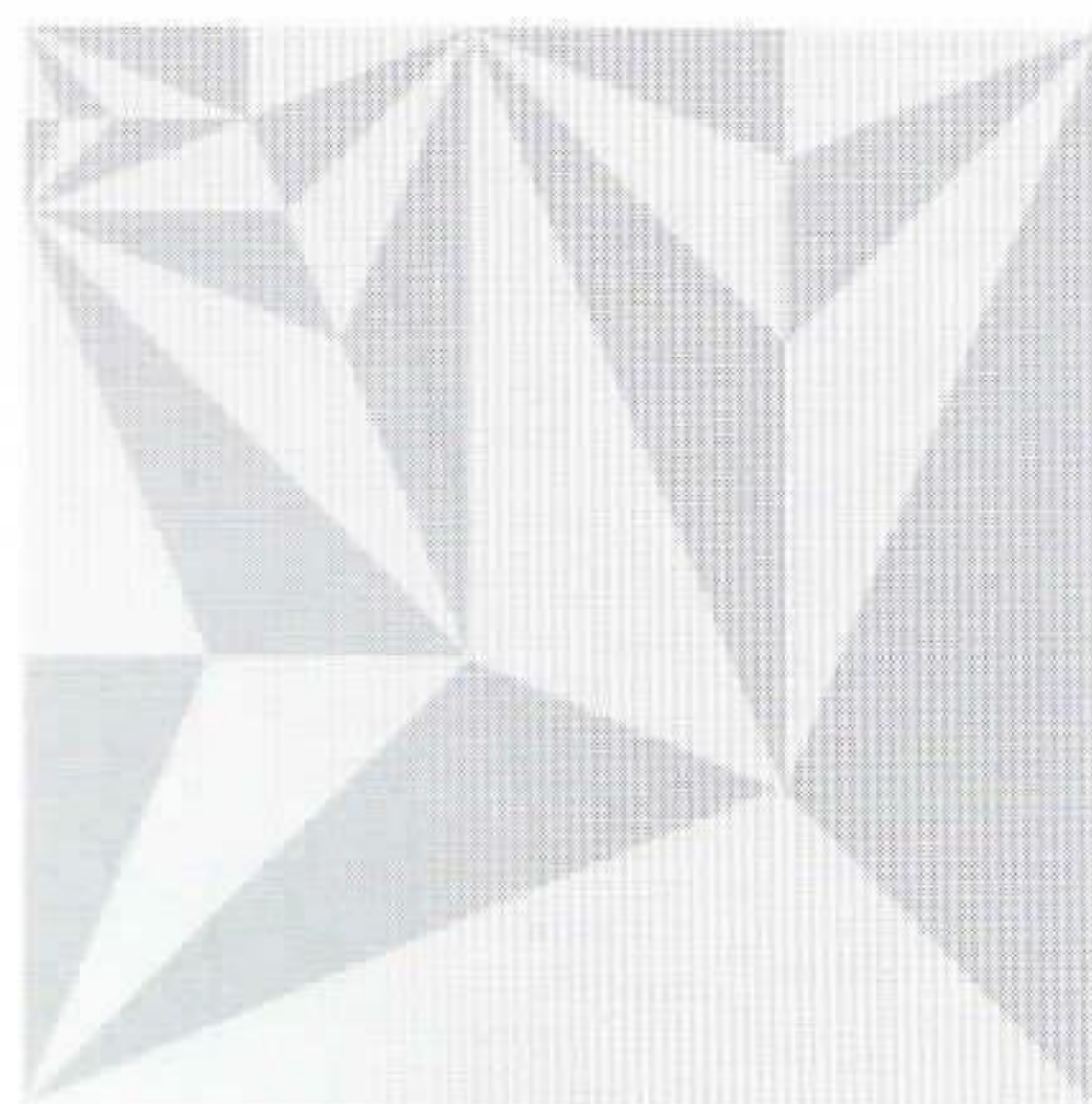
If you unfold *Tree* in step 30, you will see on the white side of the paper the crease pattern shown on the left. Note that the model was folded flat with these creases. Using this crease pattern as an example, let's examine some of the general features of flat-foldable creases.

Pay attention to the "corners" where mountain and valley creases meet. (Ignore those on the edges of the sheet for now.) You may find that:

1. The difference between the number of mountain and valley creases is always 2. (Maekawa Theorem)
2. If you add all angles between creases, one by one with alternate signs, the sum is always 0. (Kawasaki Theorem)

For example, look at the point A in the crease pattern. It has 2 mountain and 4 valley creases, so the difference is 2. The angles between the creases counter-clockwise from the right are 67.5° , 22.5° , 22.5° , 45° , 45° , and 67.5° . $67.5 - 22.5 + 22.5 - 45 + 45 - 67.5 = 0$.

Though not all corners that satisfy these theorems are flat-foldable, all flat-foldable corners satisfy both of them. This is true not only in regular patterns like this but also patterns of crumpled and flattened sheets.

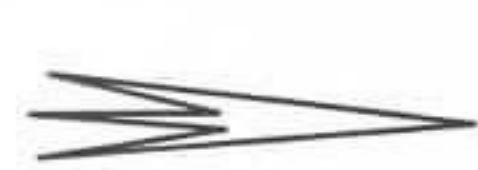


We can prove, from the Maekawa theorem, that any corner has an even number of creases. And that any crease pattern requires only two colors to paint the areas surrounded by the creases. One color represents all the areas facing up when folded, and the other all areas facing down.

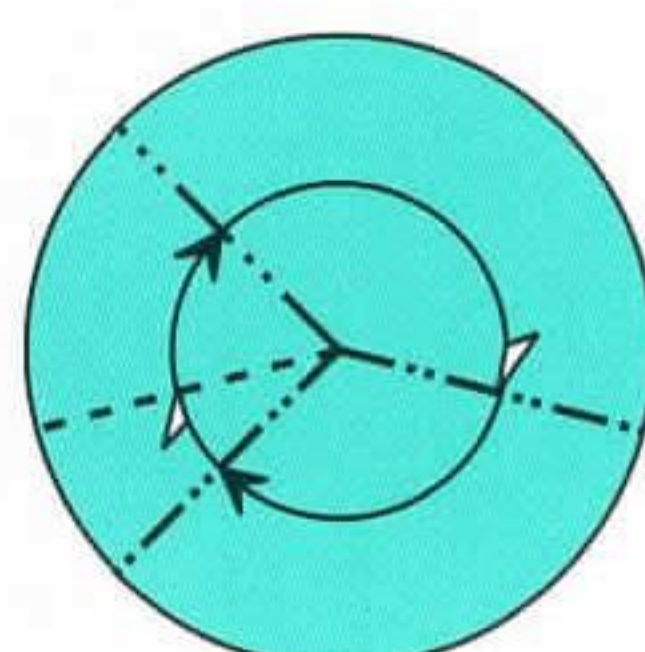
If the model has one-sidedness (see *Orizuru Transformation*), as in this crease pattern, the corners on the edges also satisfy both of the theorems. For example, look at the point B. You can easily see that the Kawasaki theorem is satisfied. Now, imagine that the two edges fuse into one valley crease when folded, and the Maekawa theorem is also satisfied.

Keys to prove the theorems

Calculate the sum of interior angles of the polygon.



Mountain = 360°
Valley = 0°



In the next section...

That concludes **fundamental models** and **simple models**. There is, however, no objective standards for complexity levels in origami, and you may think the models presented so far are not simple, as they are accompanied with complicated theories. In fact, they are not necessarily easier to fold than those in **intermediate models**.

Before we step forward to **intermediate models**, I want to introduce some models that break the "basic rules" of origami.

The "basic rule" is described as "one square sheet without cuts." Such origami is often thought to be "genuine" as in the title of this book.

However, there are many truly origami-like designs that are folded from shapes other than a square, with more than one sheet, or with cuts.

These models make us rethink about "authenticity" in origami.

Chapter 3

Varieties of Origami

"There is nothing in this world constant, but inconstancy."

Jonathan Swift



Hina dolls

Theme: Multi-piece

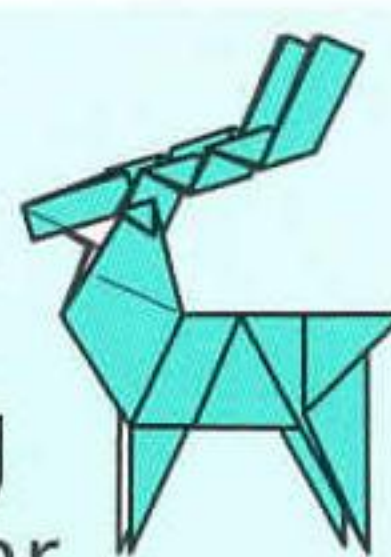
An example of model that is folded using multiple sheets. The purpose of this model is to use multiple colors.



Fujiyama
Module

Theme: Modular

An example of modular origami, in which a lot of simple modules are assembled mainly into geometric shapes.



Tea-bag
Reindeer

Theme: Irregular shape

Introduces a model folded using a sheet with an extremely odd shape. Origami paper does not have to be square.



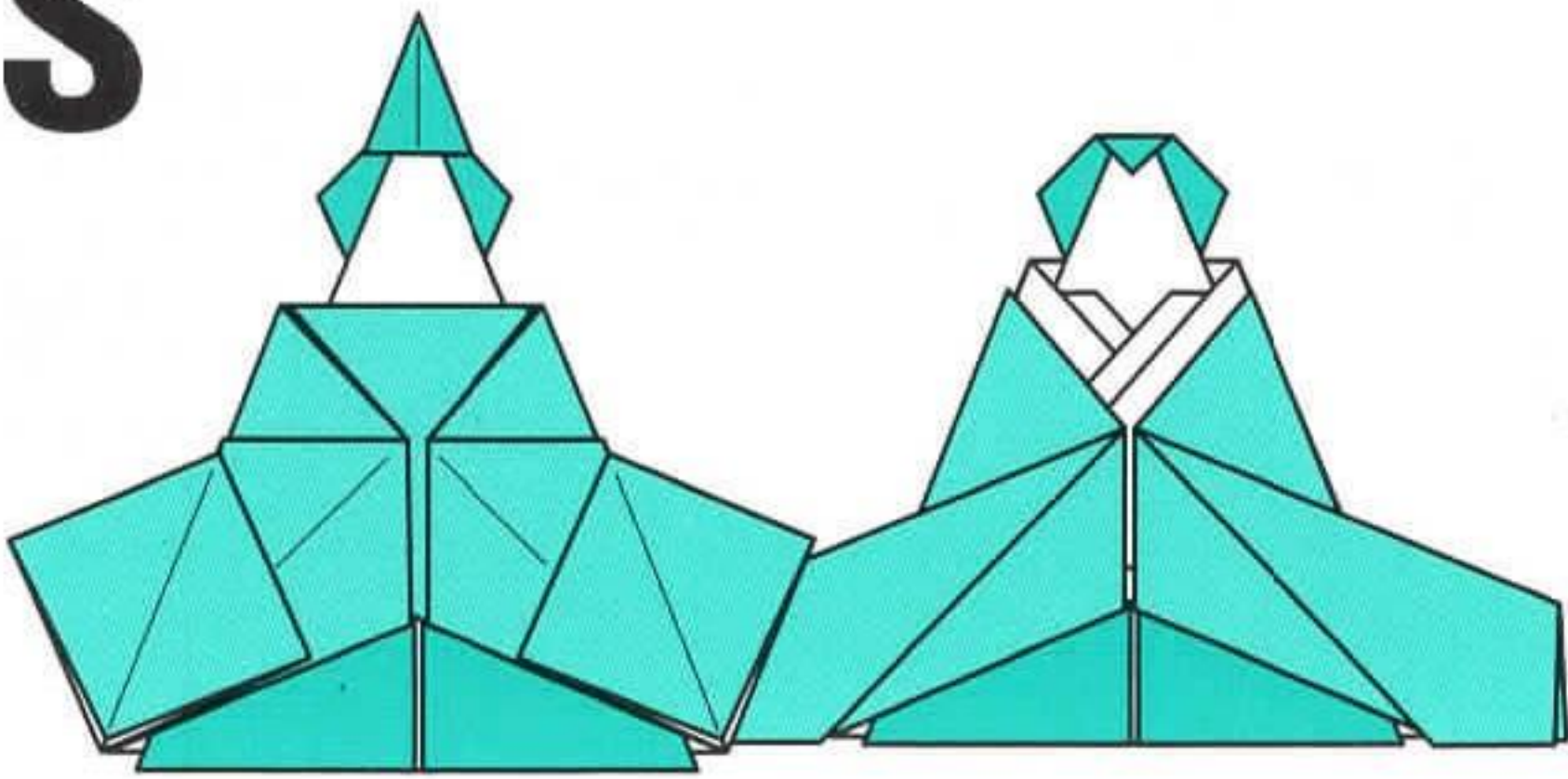
Connected
Cranes, Kotobuki

Theme: Cut

Some models are more origami than kirigami or paper-craft, even though they are folded with cuts.

Hina dolls

Theme: Multi-piece
Fold using 6" (15 cm)
origami paper.



This model breaks the rule of "one sheet" in "one square sheet without cuts."

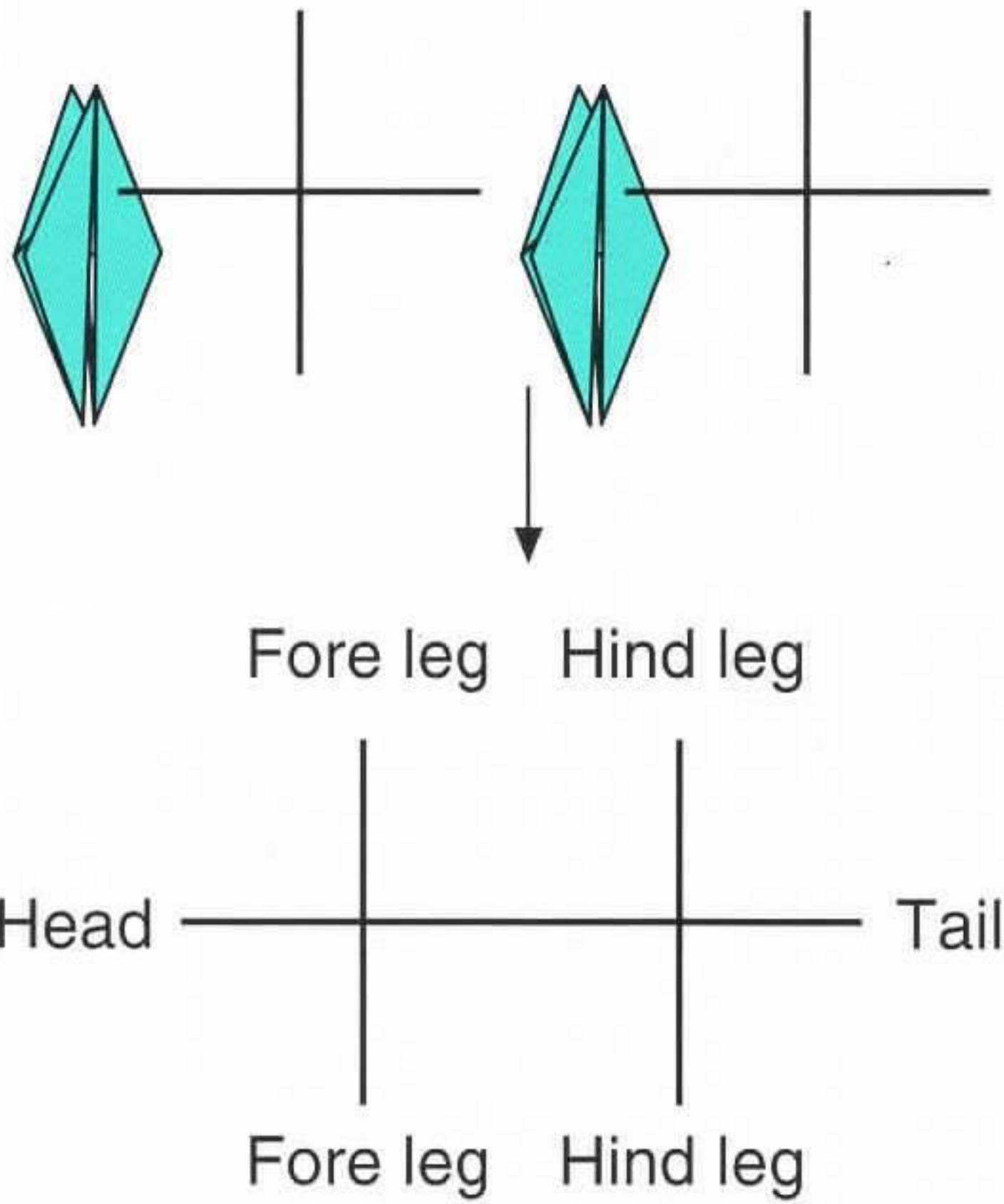
A Bird base has four long flaps, which are not enough to make, say, a quadruped animal that has a head, a tail, and four legs.

One solution for this situation is to combine two Bird bases, as shown on the right. Although it expands the possibility of design without introducing difficult steps, it is not likely to offer puzzle-like twists. Generally speaking, however, using multiple sheets is not necessarily boring.

When we use multiple sheets, we can obtain not only more flaps but also more colors. Even with one sheet, we can use two colors. Using the inside-out technique, as in Santa Claus, we can use the colors of each side of the sheet. But with multiple sheets, we can use more than two colors.

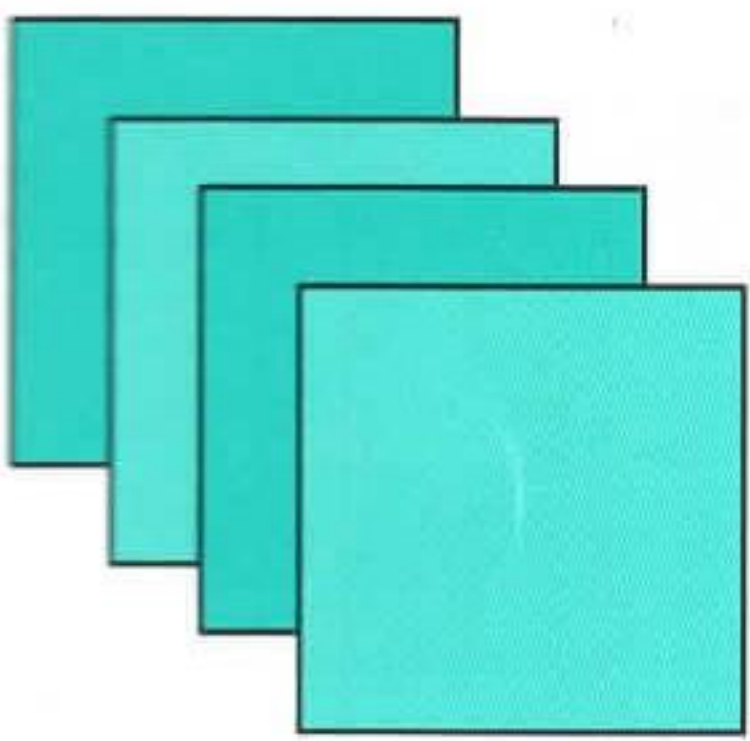
This model is based on such idea. At the same time, I wanted to use as little colors as possible. So, I used a limited number of colors by making hair and hakama (Japanese traditional trousers) with one sheet.

Speaking of colors, we sometimes use decorated or painted paper. It is interesting to fold using such paper, especially for simple models, because we often get surprised with unexpected patterns appearing on finished models. A pair of artists Cochae explores a new genre of such origami called "graphic origami."

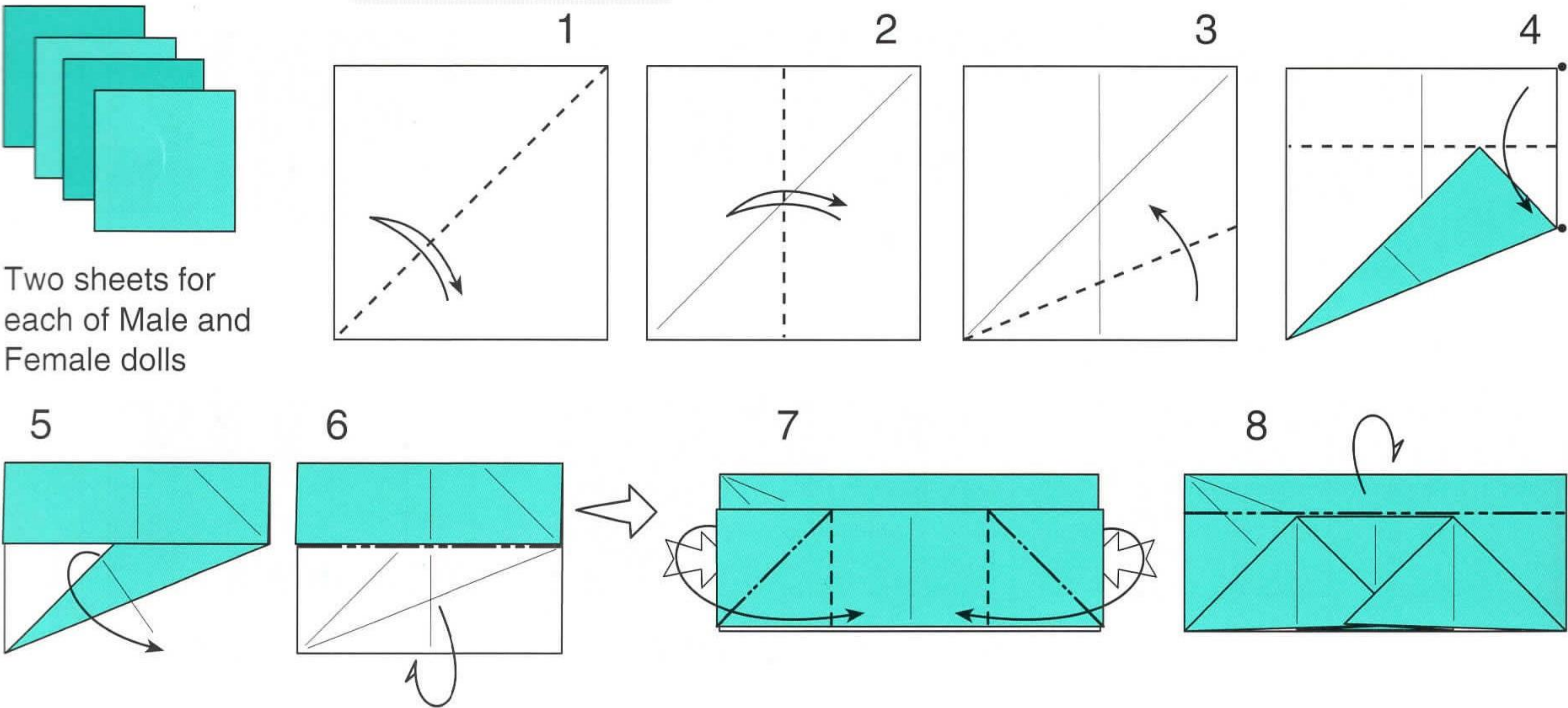


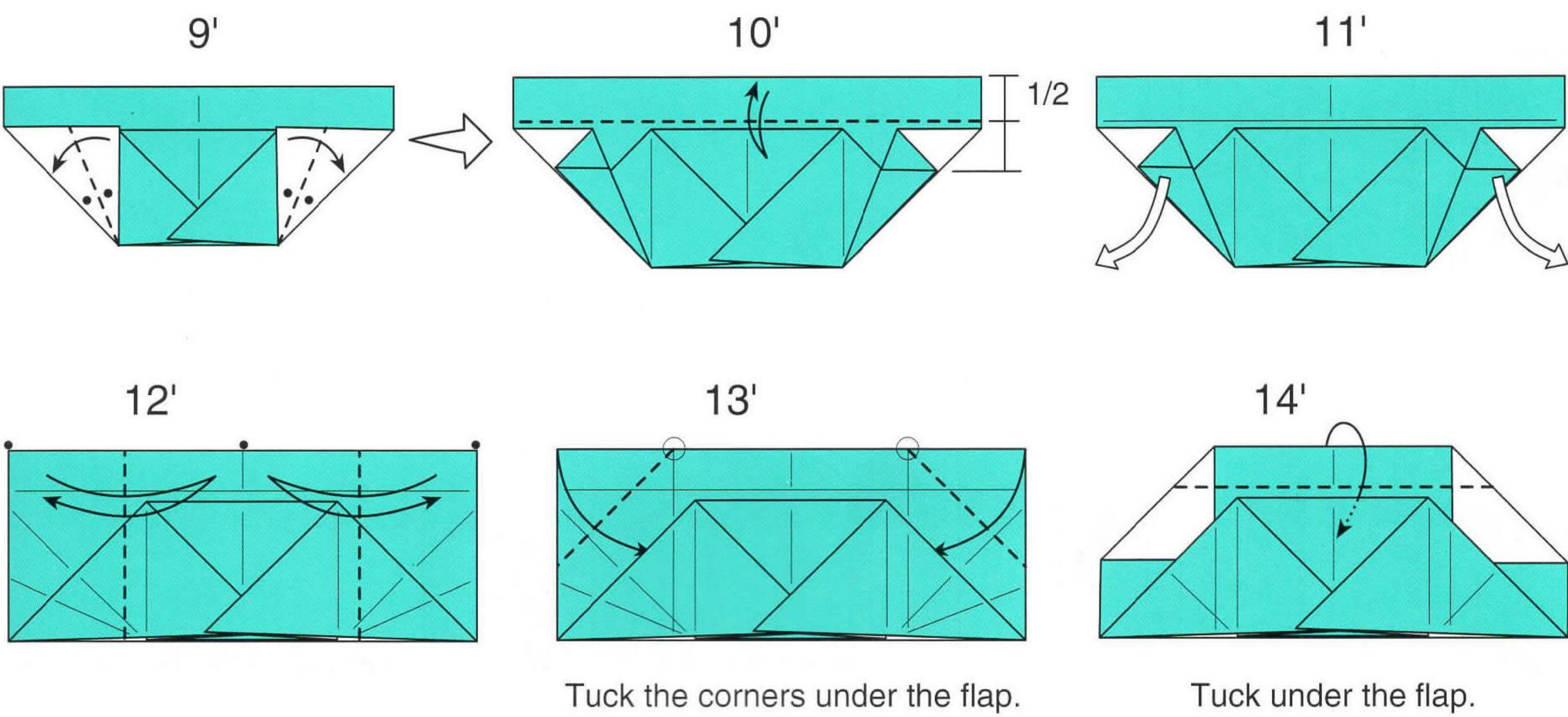
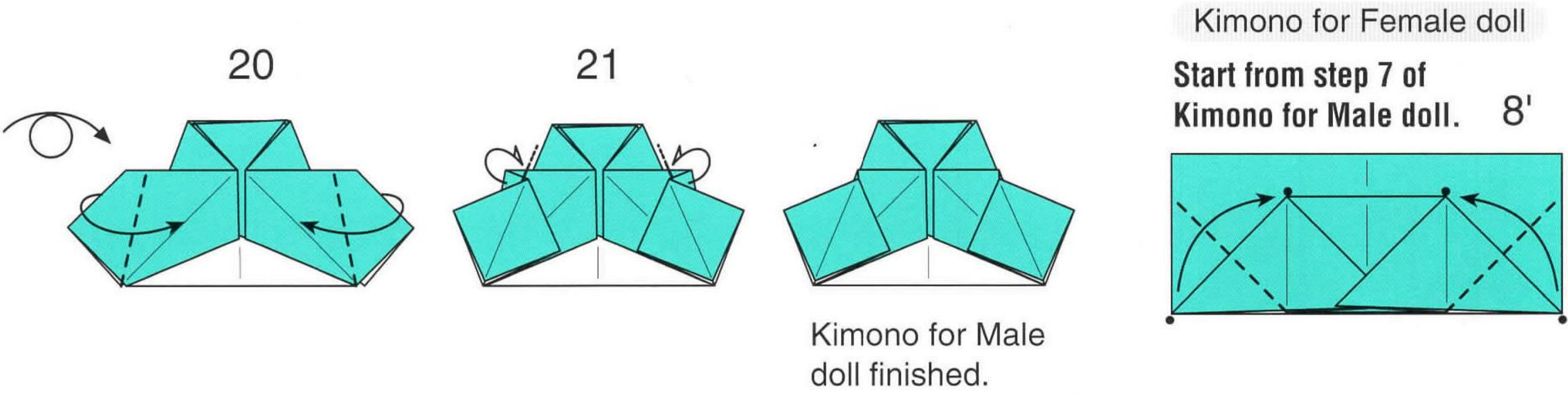
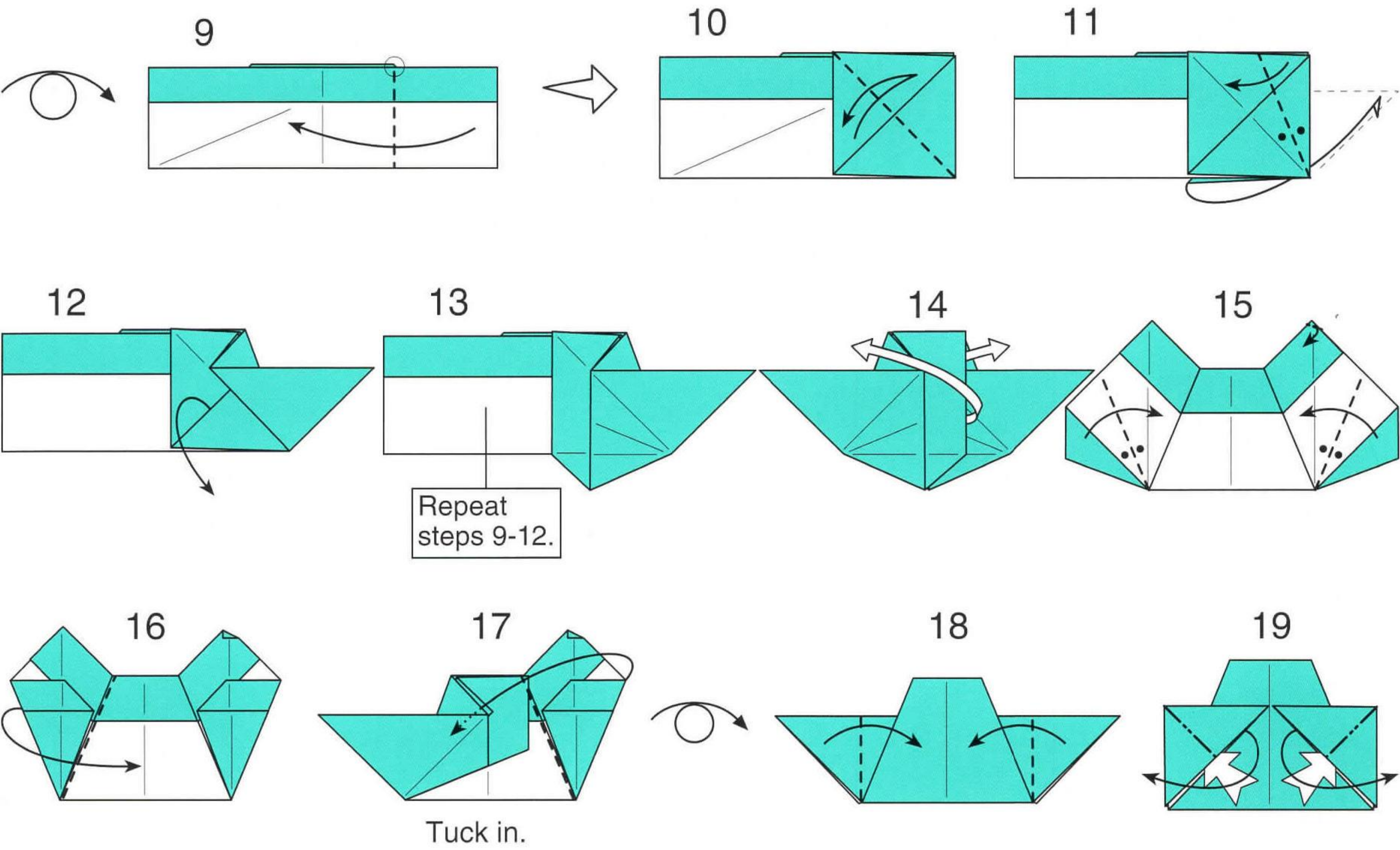
Designing a quadruped animal using two Bird bases.

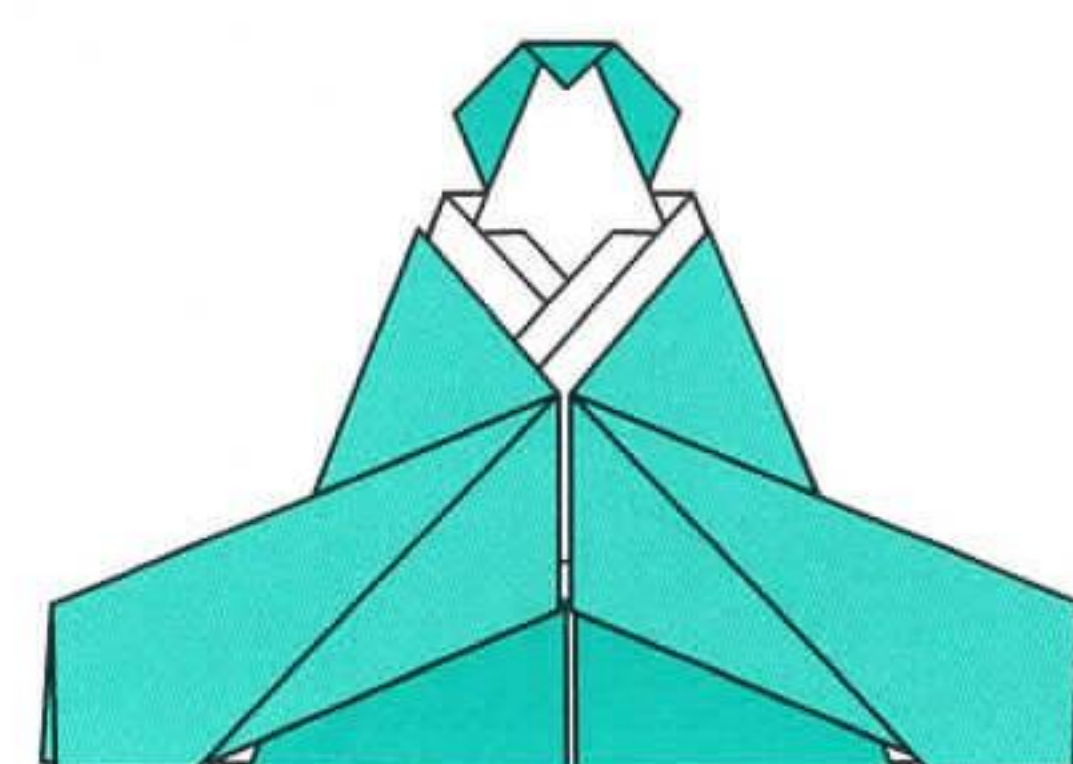
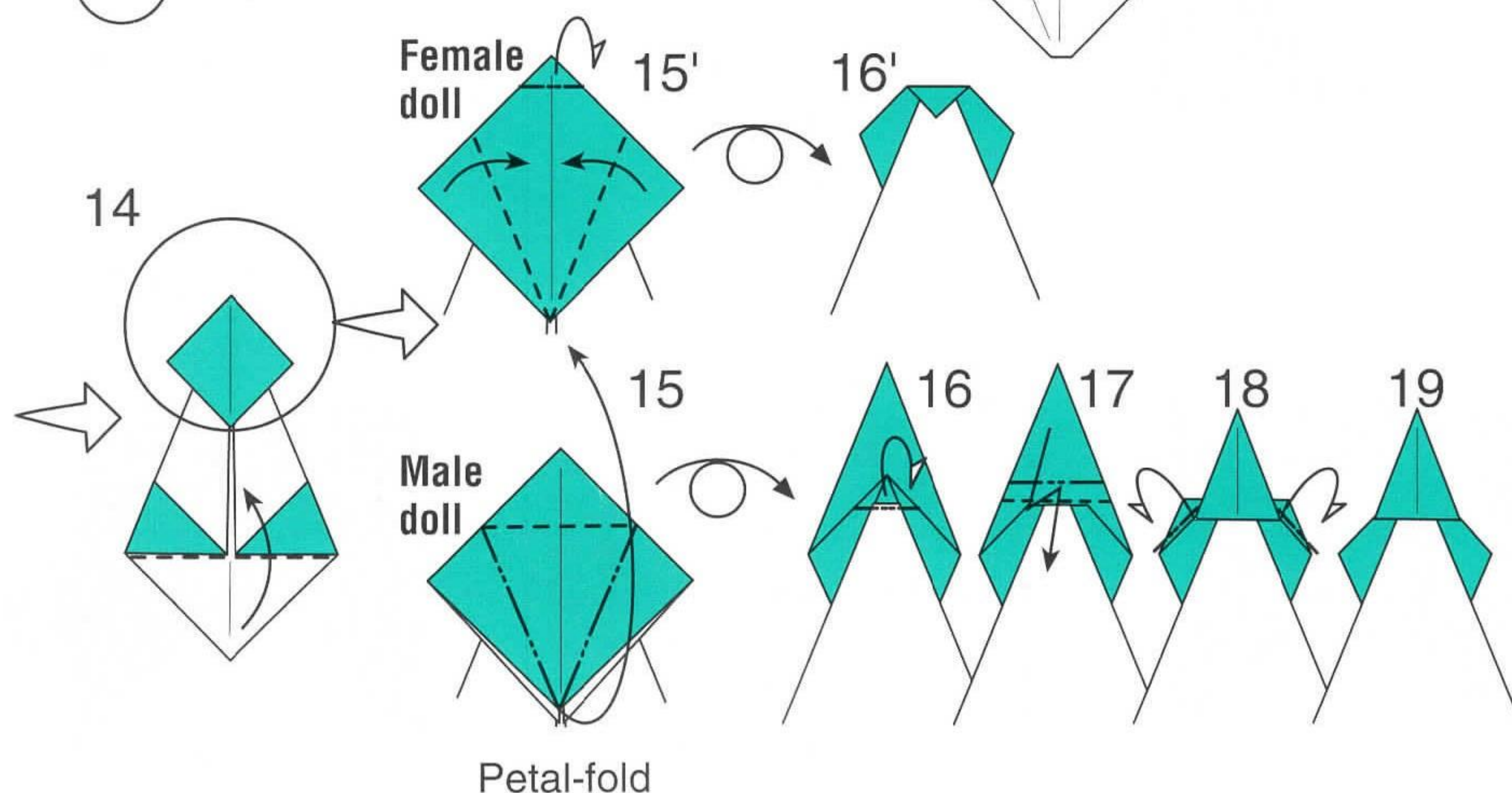
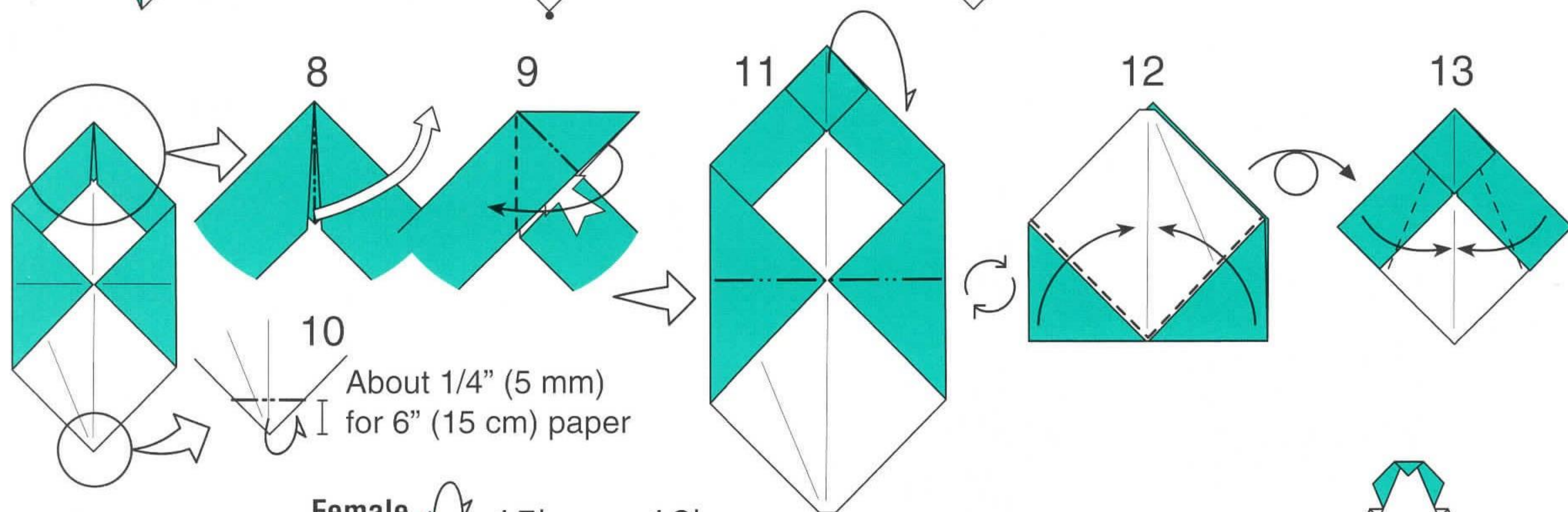
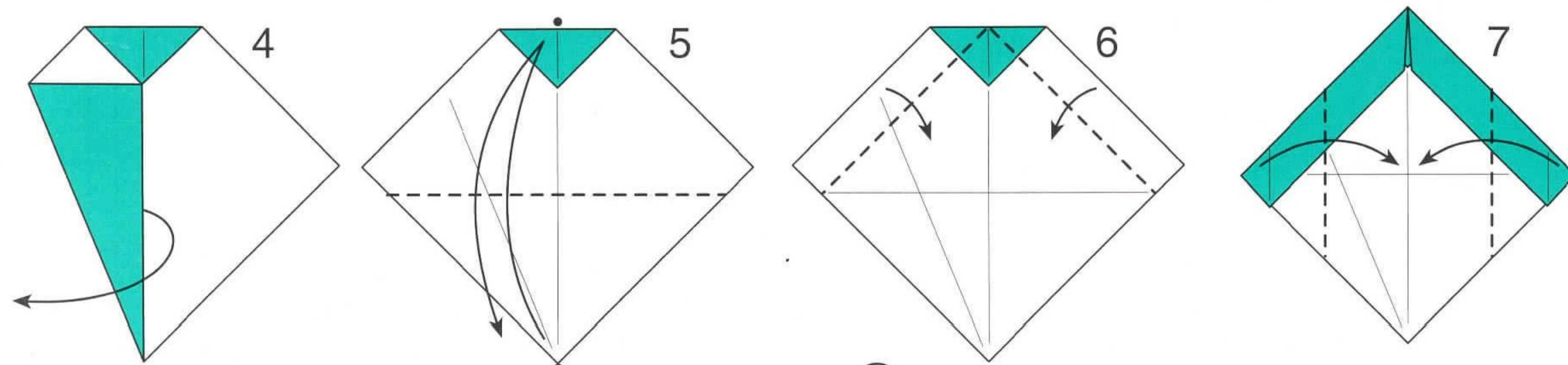
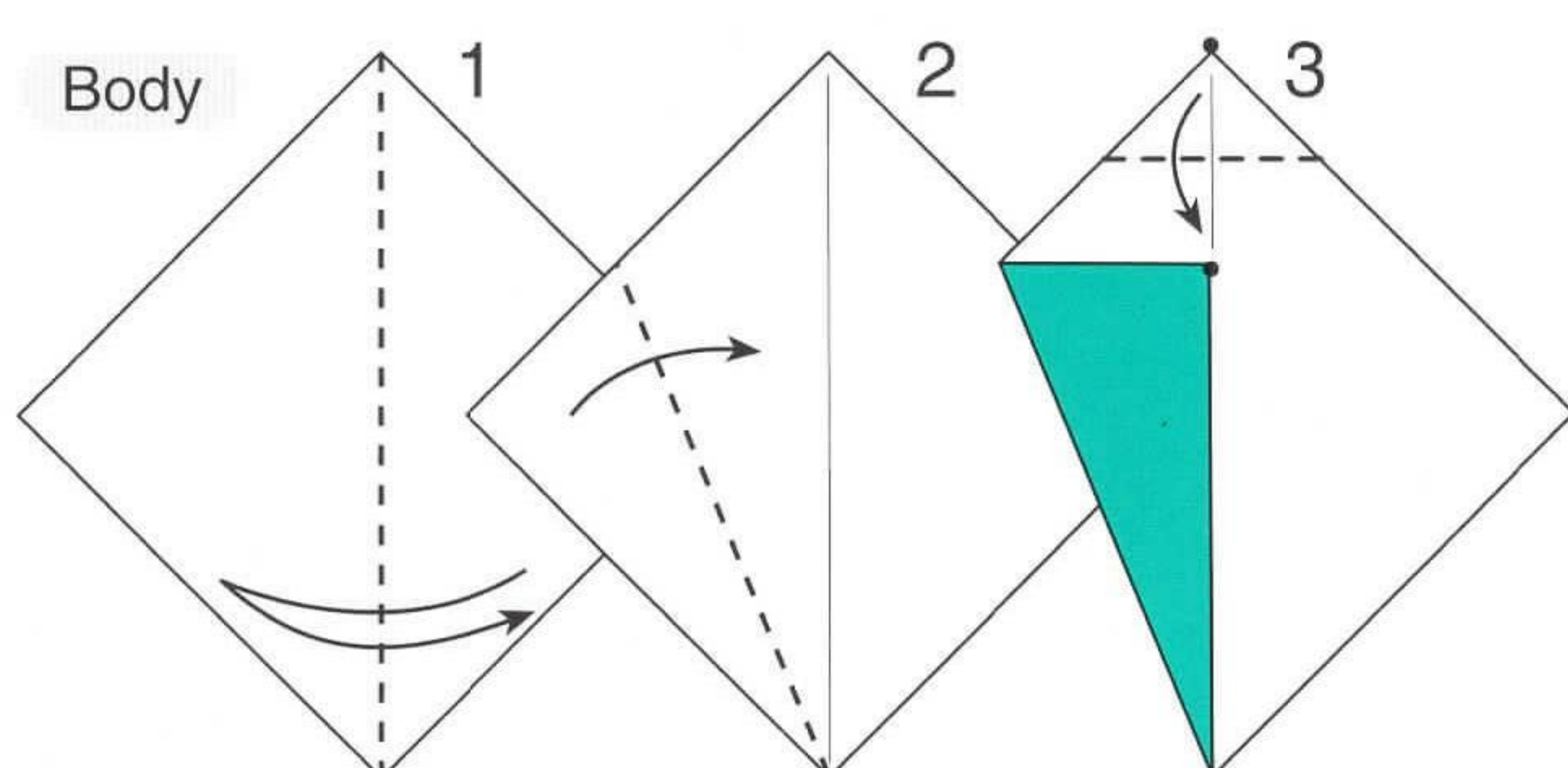
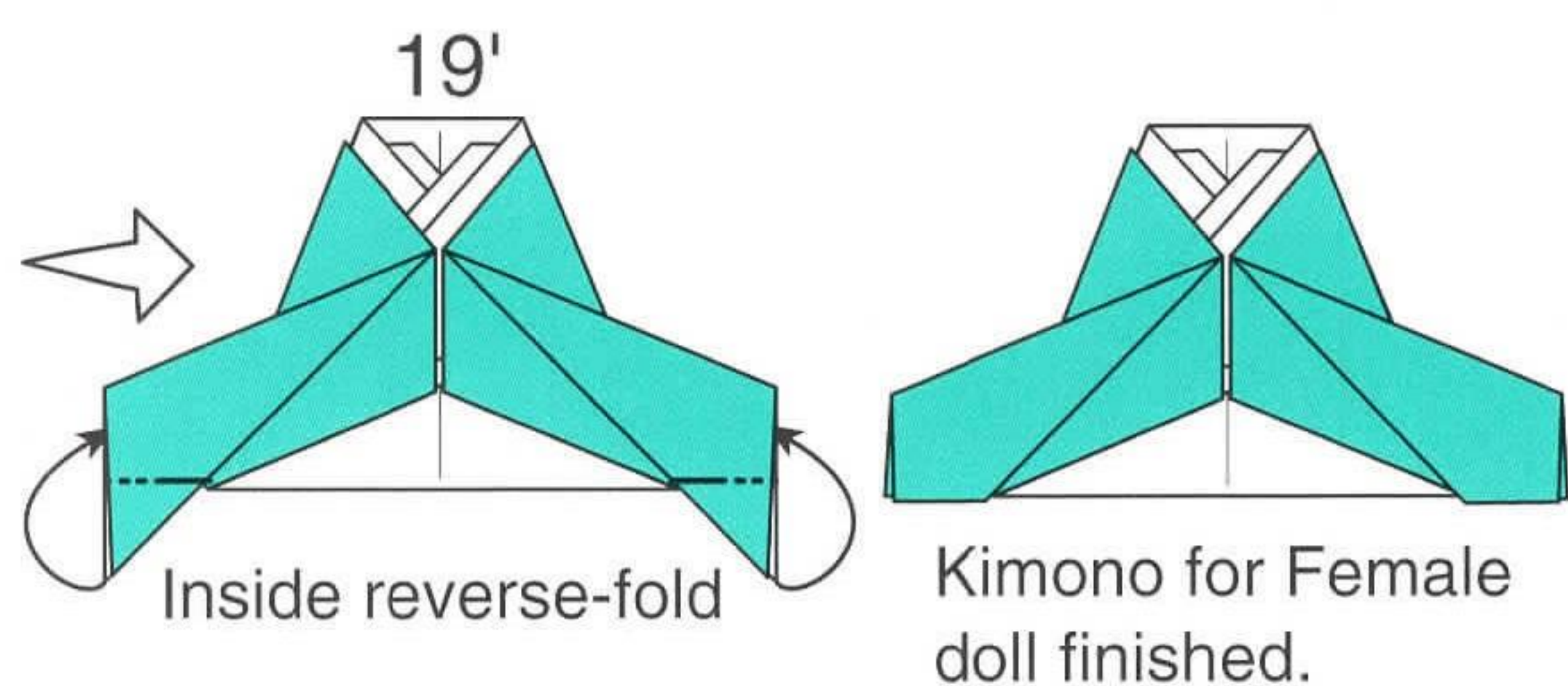
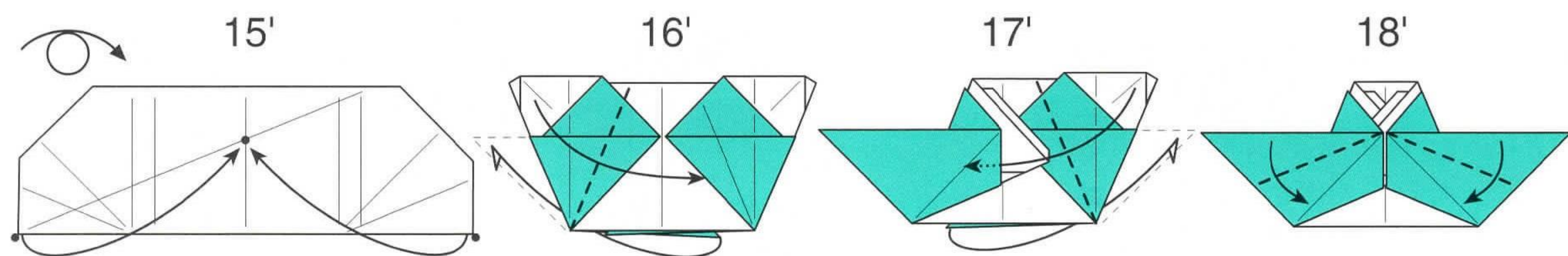
Kimono for Male doll



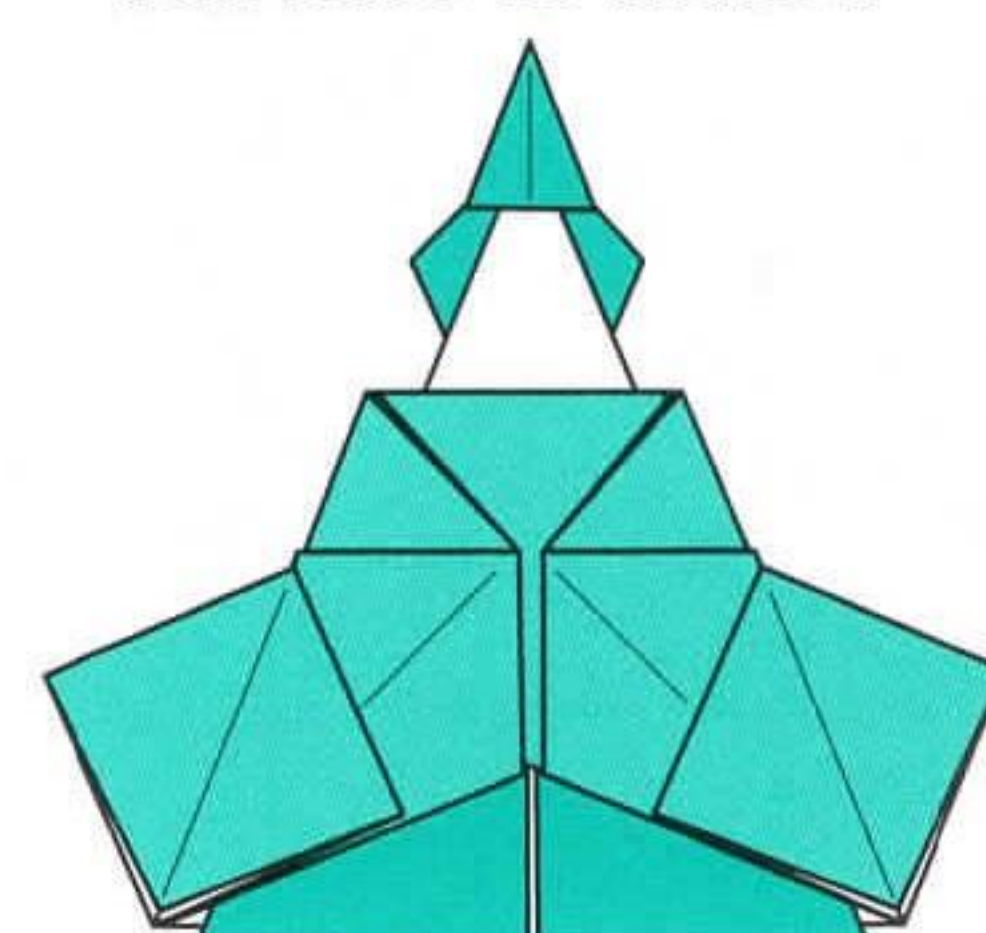
Two sheets for each of Male and Female dolls







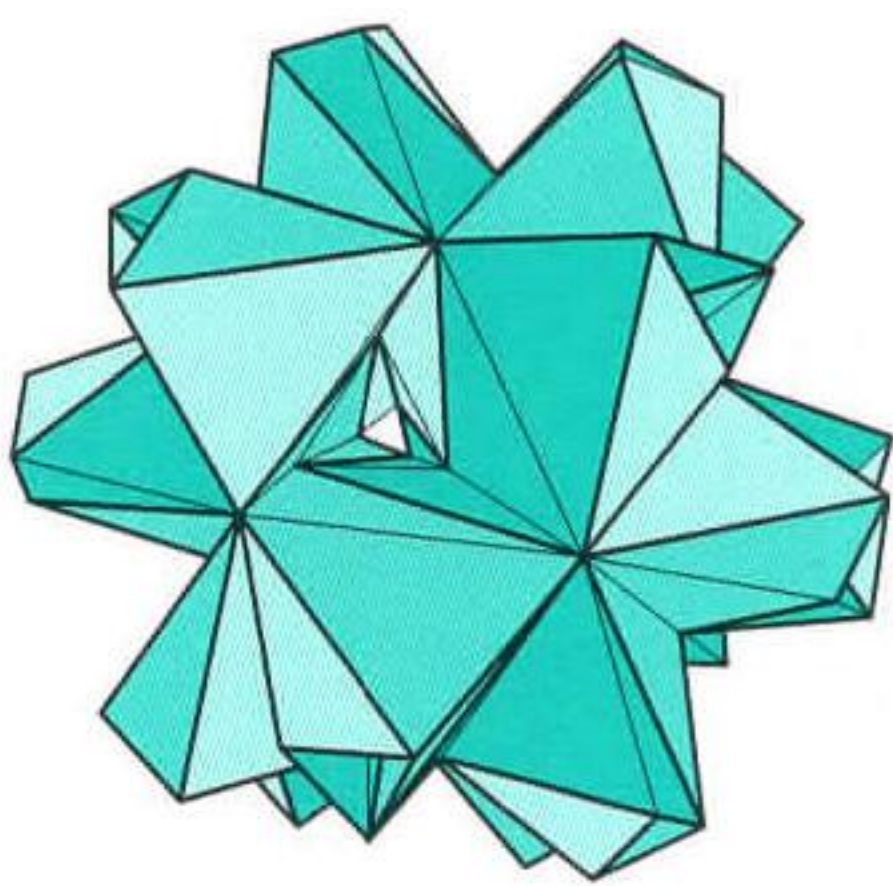
Assembly with Kimono to finish.



Fujiyama Module

Theme: Modular

Fold using 6" (15 cm) origami paper cut into eight equal parts.



This model is an example of **modular origami**, where we use more sheets than “one square sheet without cuts.”

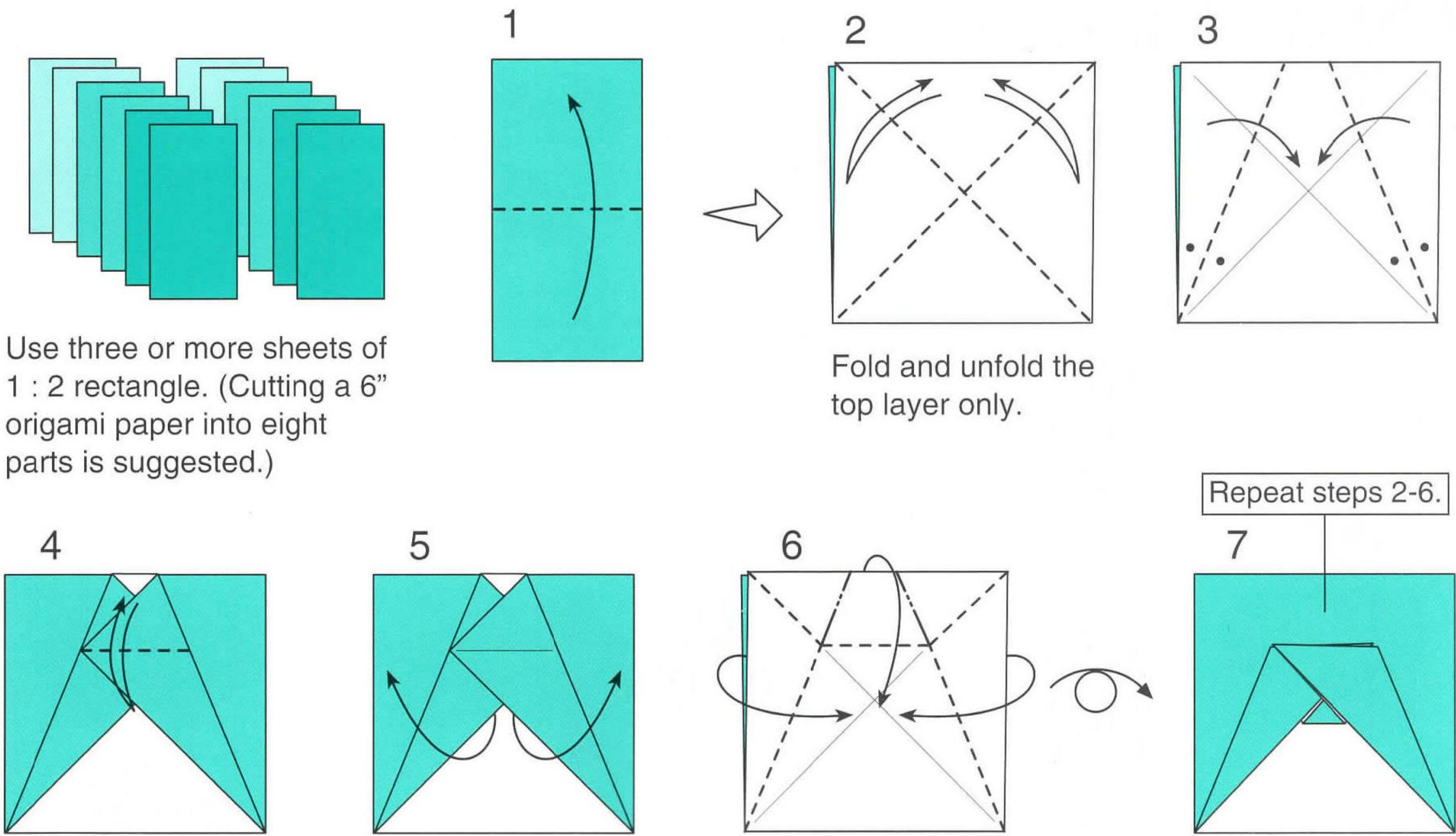
Modular Origami

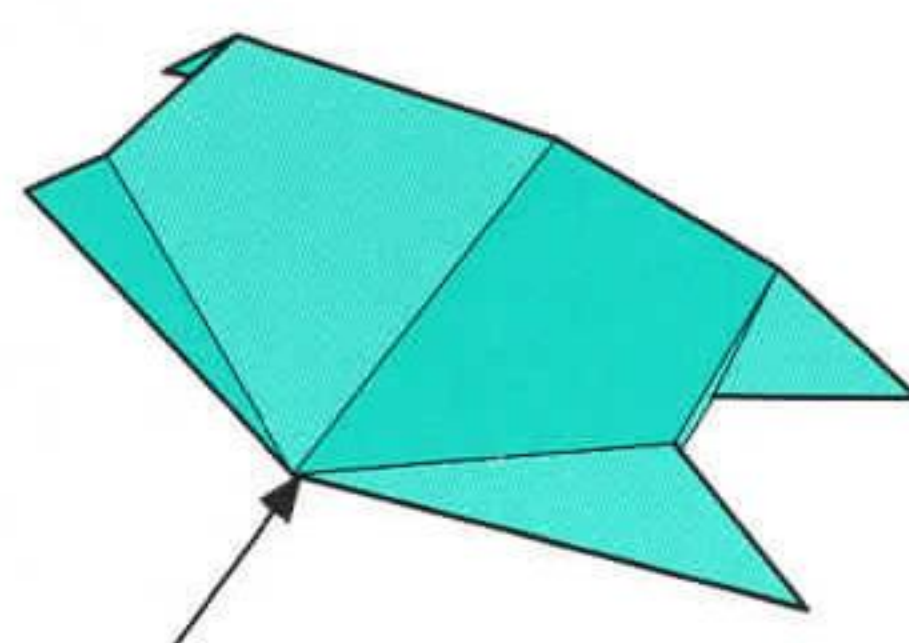
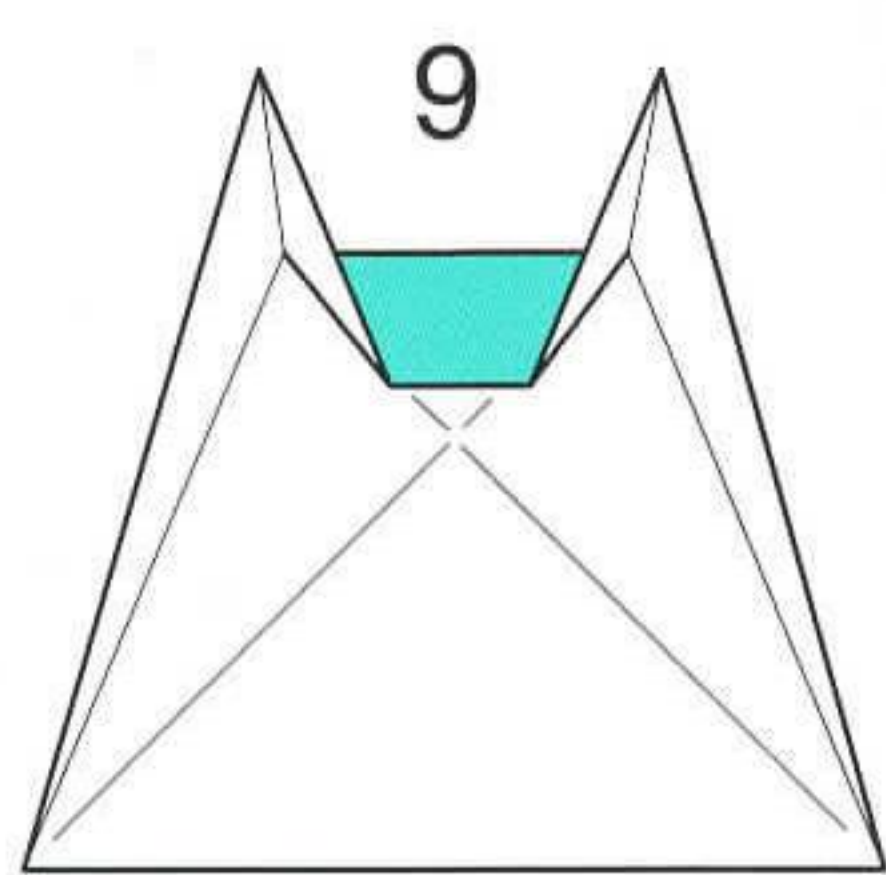
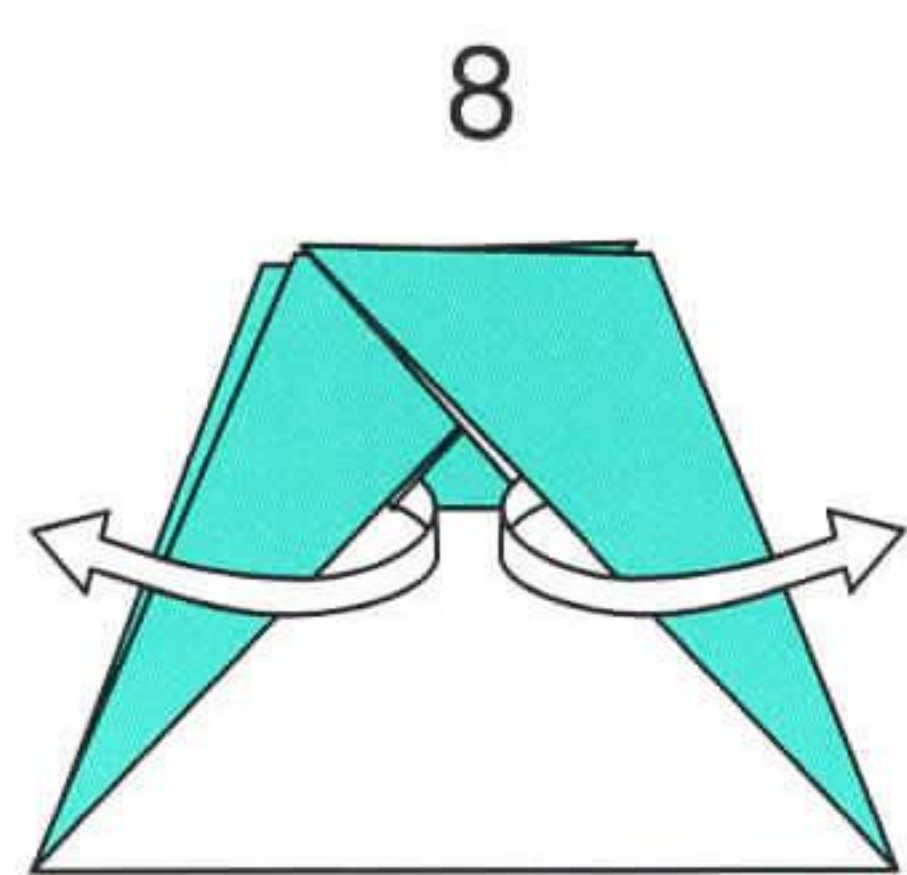
Modular Origami is a kind of multi-piece origami.

Many people have been creating a number of models of various shapes, each of which is usually assembled from identical modules. Although there are some traditional modular model such as the *Kusudama* (decorative ball), the notion of modular origami was first introduced by Kunihiro Kasahara who was interested in diverse variations of *Color Box* designed by Mitsunobu Sonobe. Besides using multiple sheets, typical modular models have the following features.

1. Each module is relatively simple.
2. No glue is required to assemble.
3. No new fold is required to assemble.
4. Modules can be assembled in different ways.

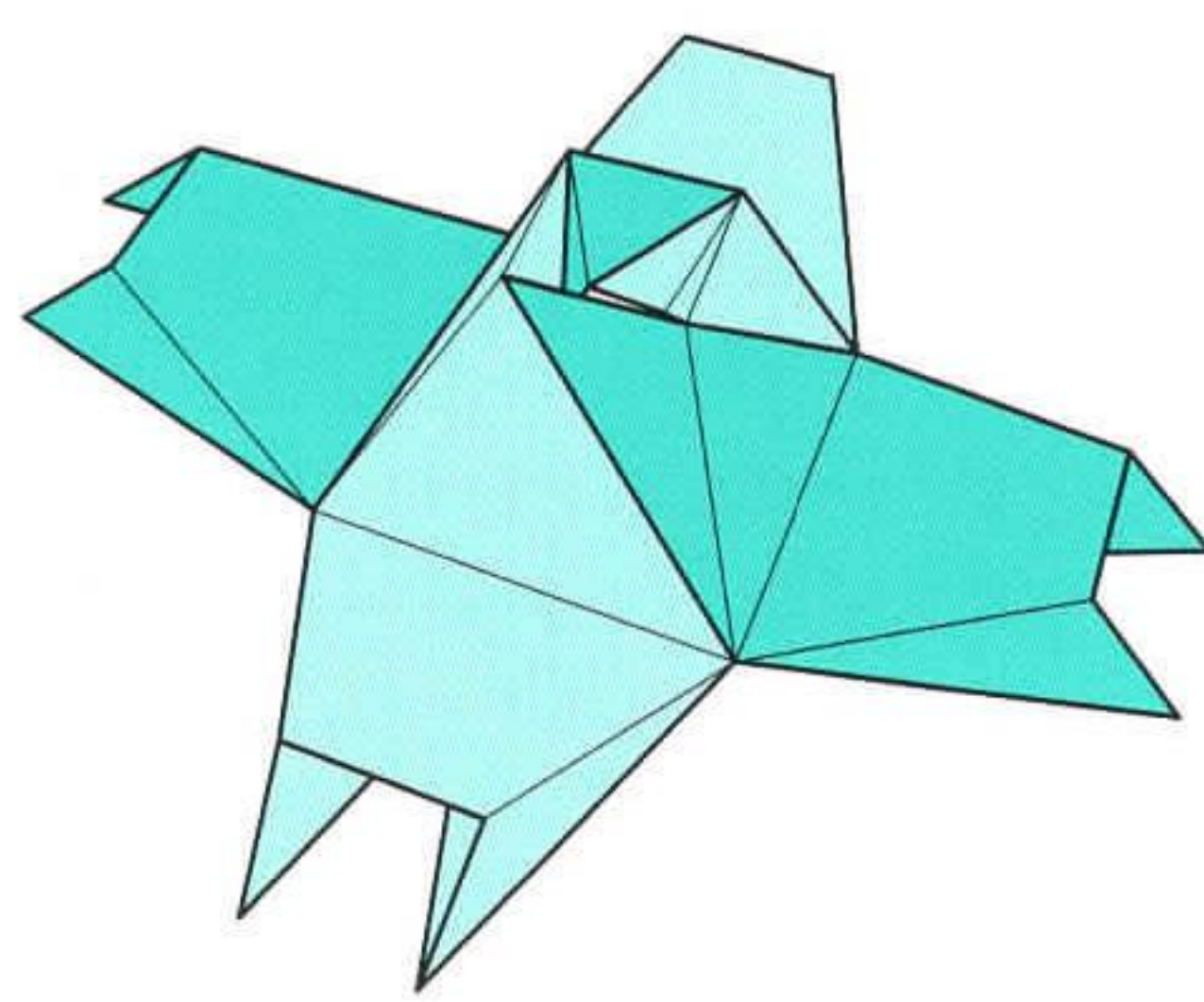
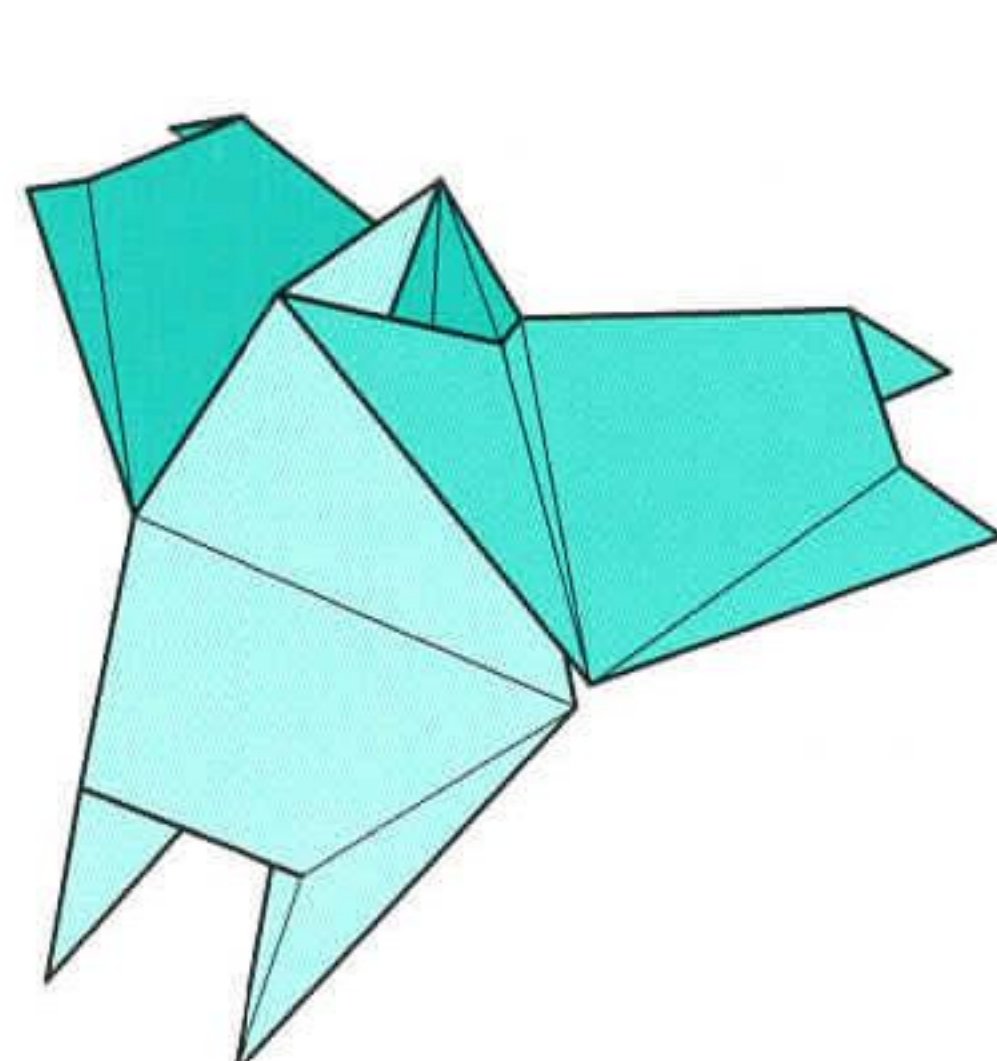
This model *Fujiyama Module* has all the features above. The most common way to assemble modules is to tuck a flap of a module into a pocket of another. But in this model, a half-open flap is wrapped over by another. It is sometimes puzzling to assemble in this way because the model tends to fall apart in the course of assembly, though it gets stable when completely assembled.



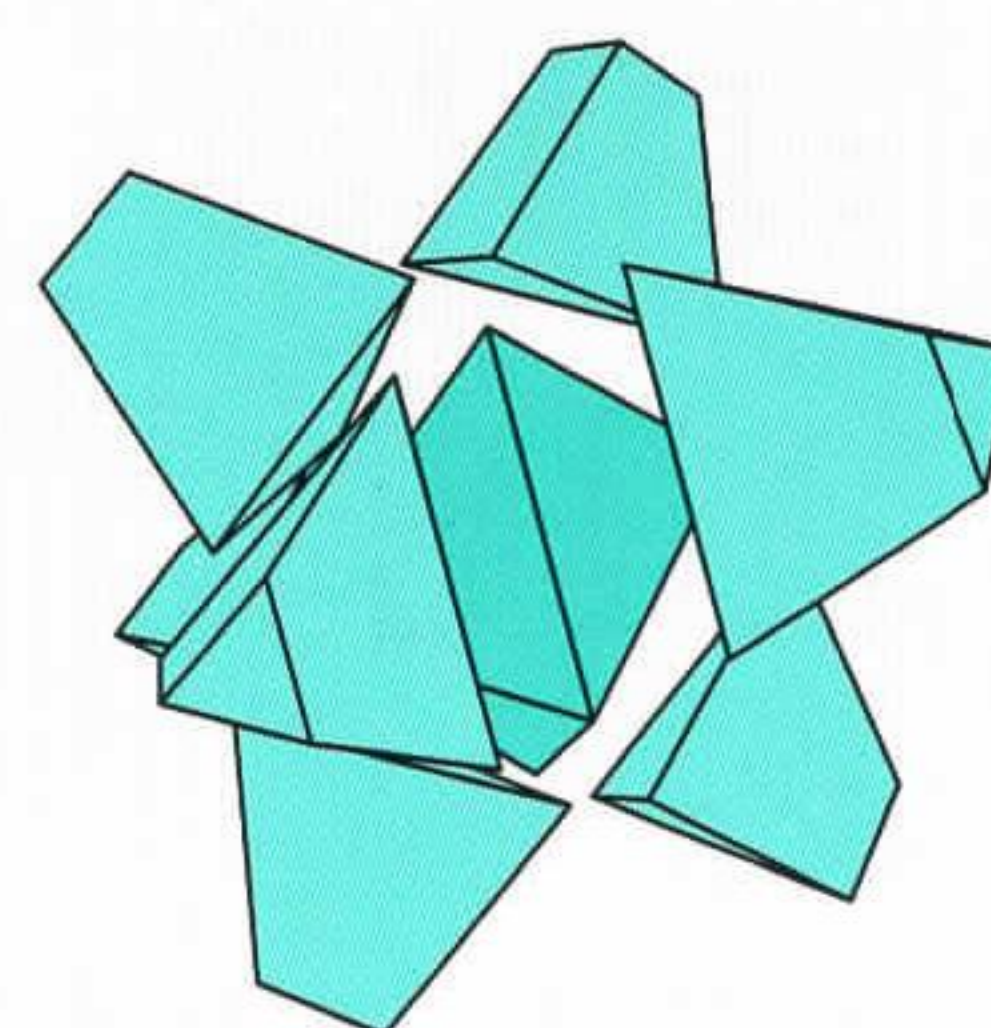


You may have to reverse this crease into mountain in some assembled models.

Finished.



Basic assembly



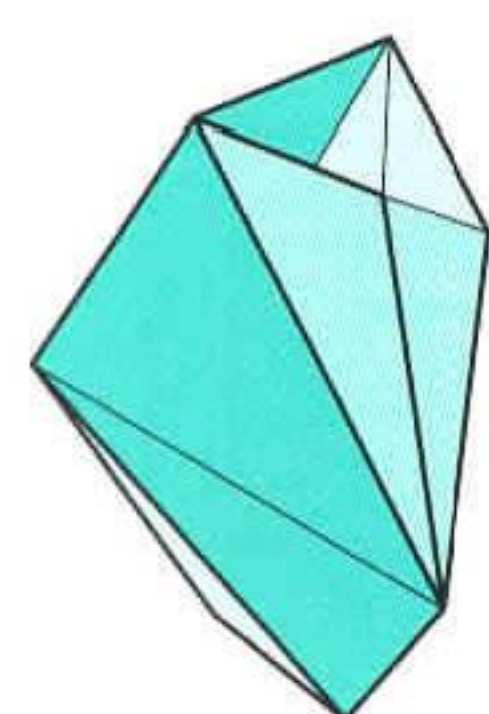
The structure of 12-piece #2 (a regular octahedron)

To grasp the structures, imagine adding a pyramidal frustum to each face of a polyhedron whose faces are equilateral triangles, squares, or other polygons (see also *Chick* in **Complex Models**).

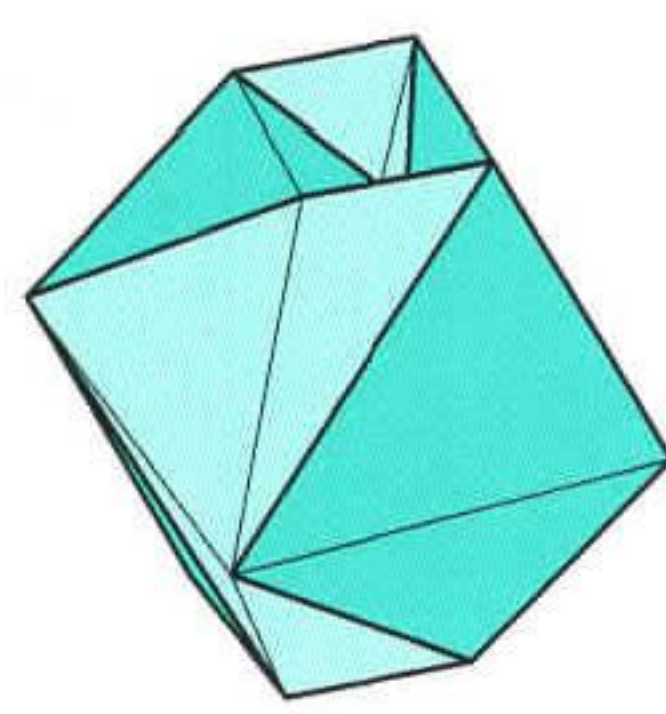
In addition, think about the symmetry of colors.

Note that the stability of the some assembled models varies depending on the stacking order of the layers.

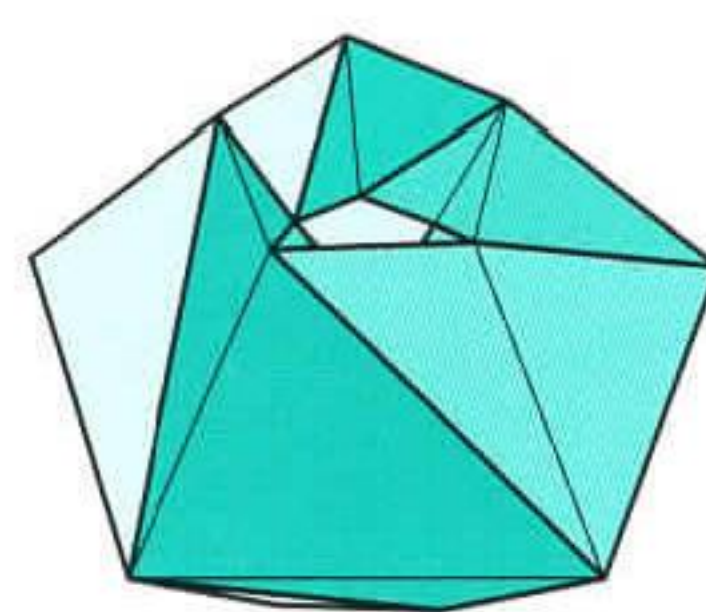
Although 15 variations of assembled models are shown below, other combinations with 11, 13-23, 25-29, 31 and more pieces are also possible. Regardless of the number of modules, all faces of the underlying polyhedron are flat.



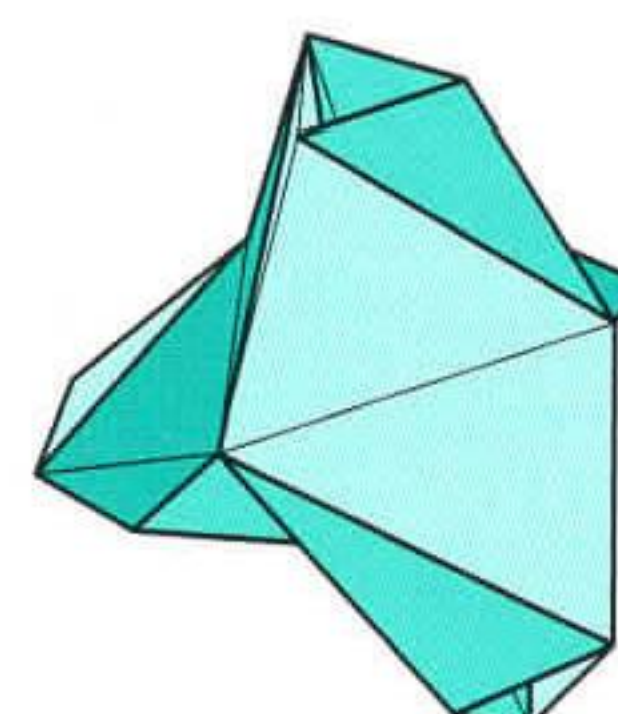
3-piece



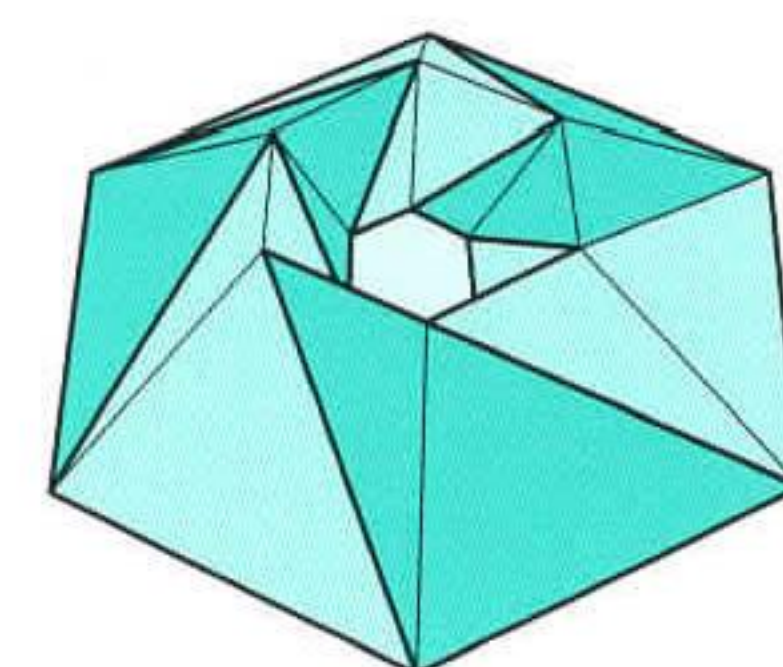
4-piece



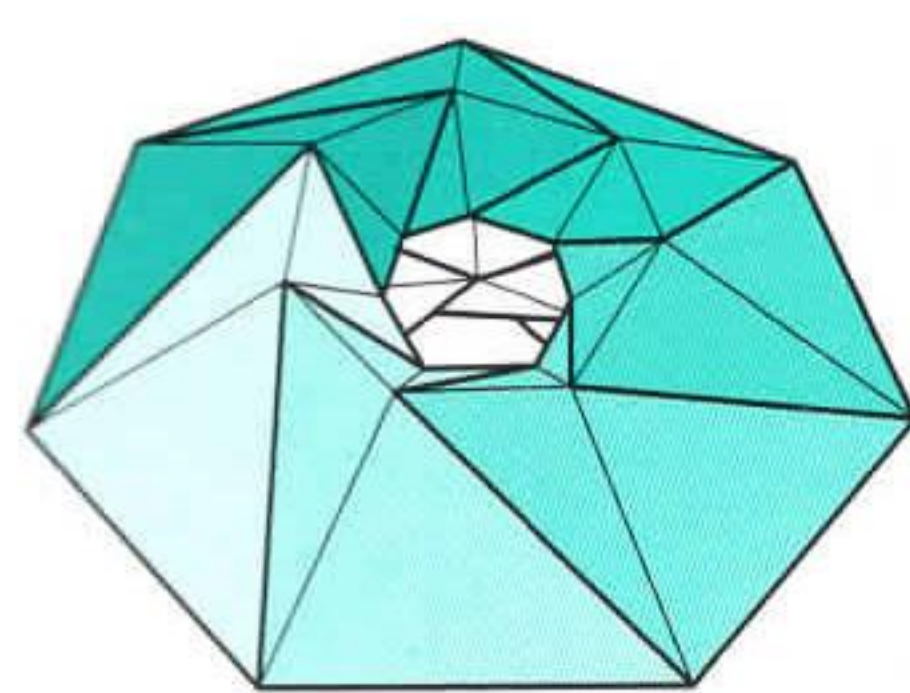
5-piece



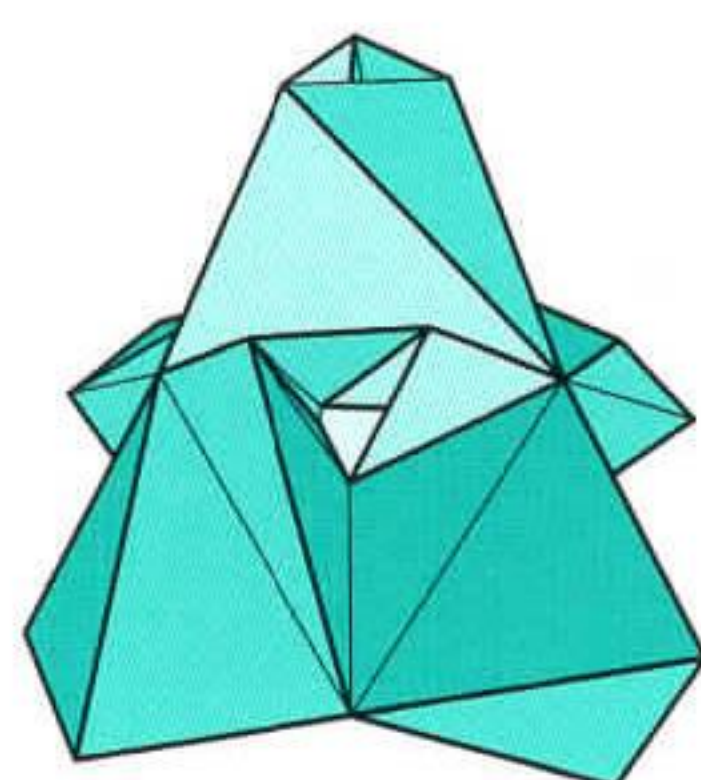
6-piece #1



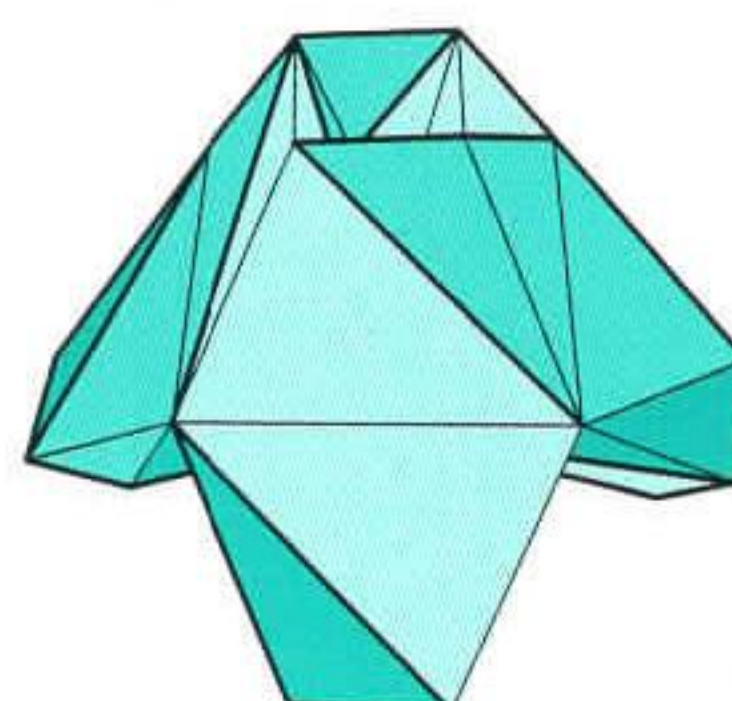
6-piece #2 (not stable)



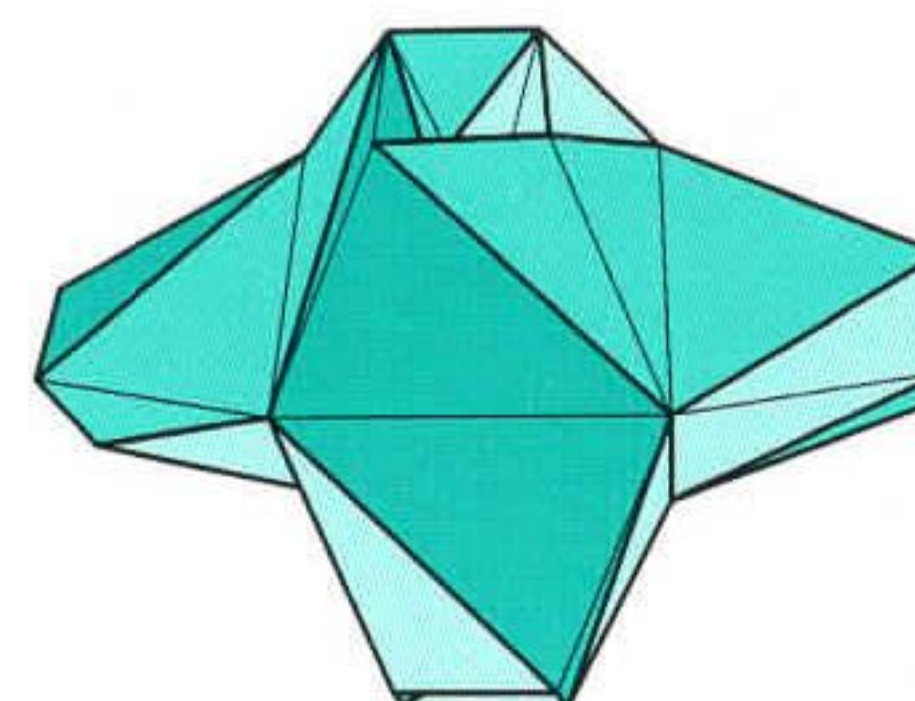
7-piece (not stable)



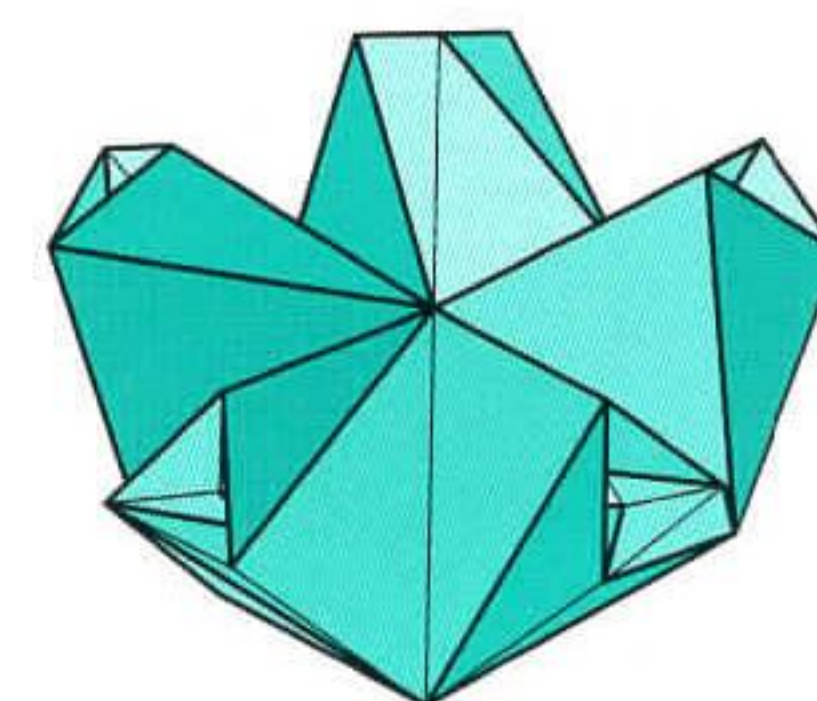
8-piece



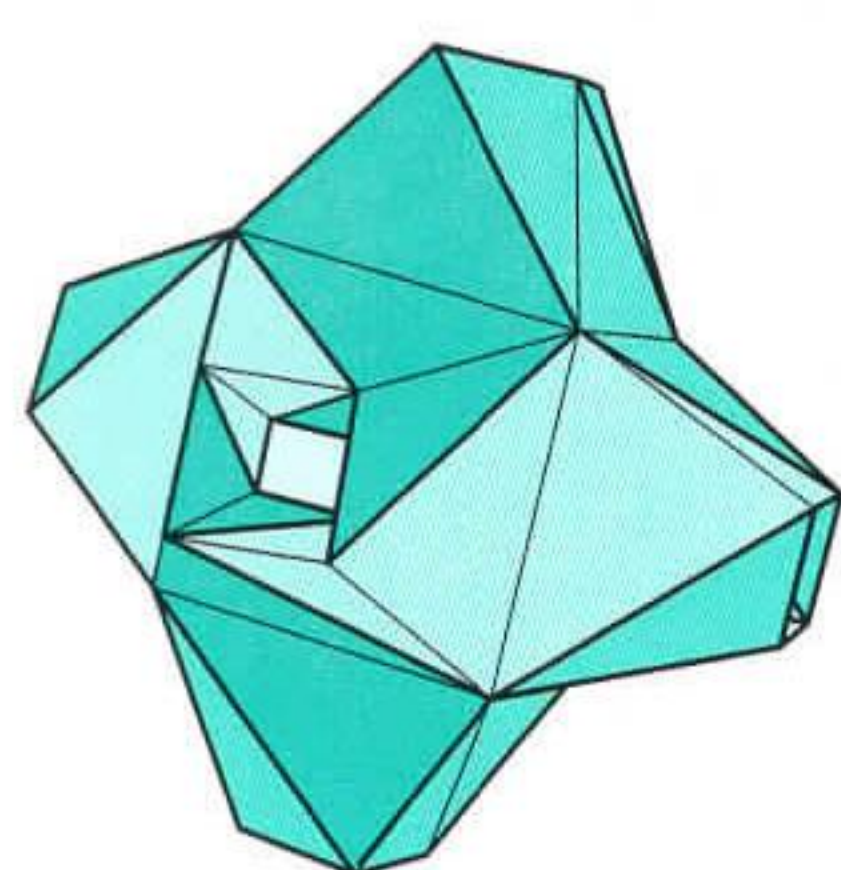
9-piece #1



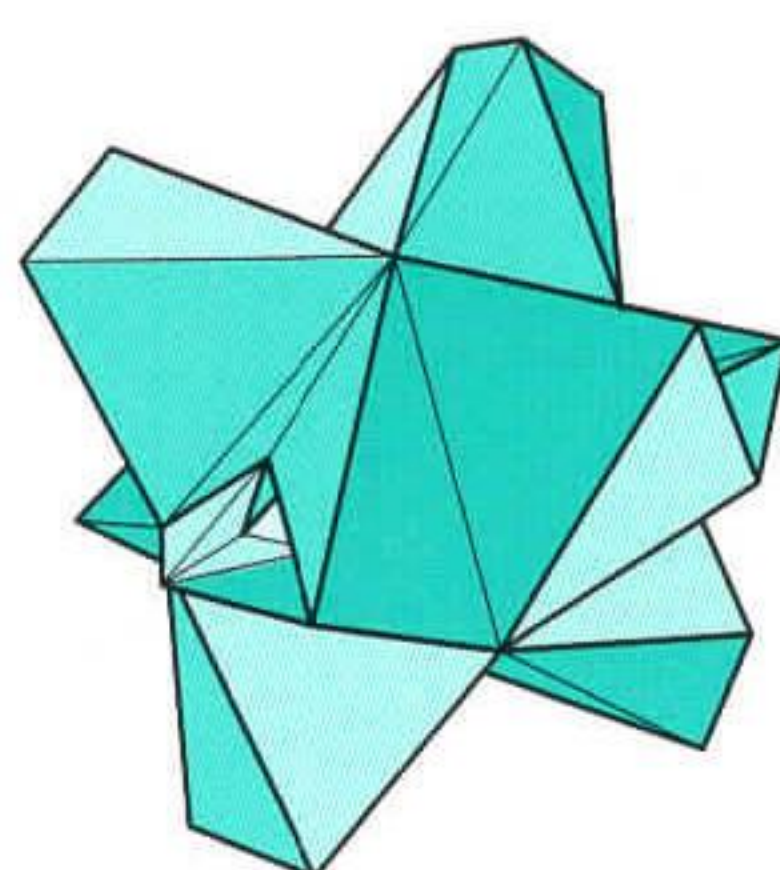
9-piece #2



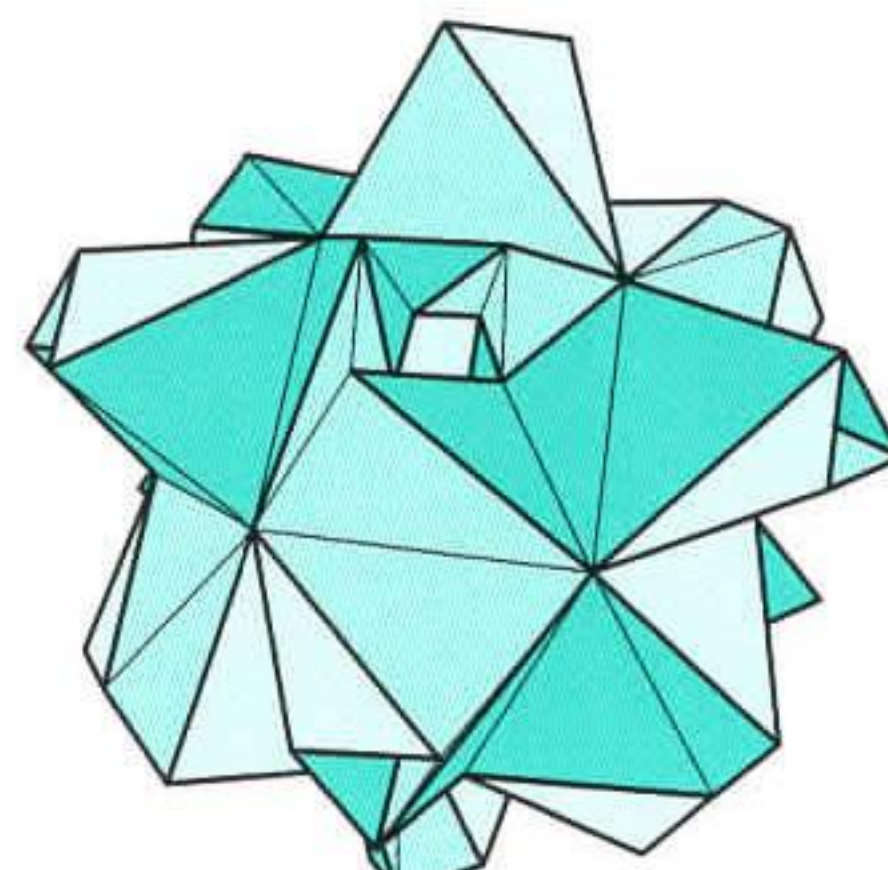
10-piece



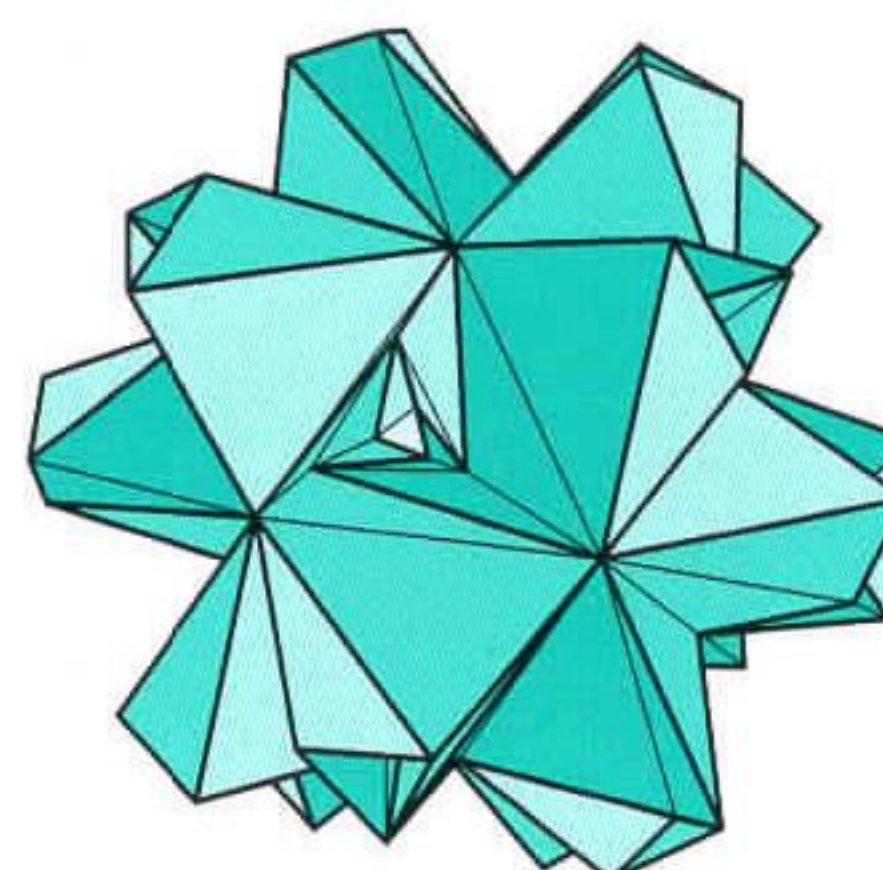
12-piece #1



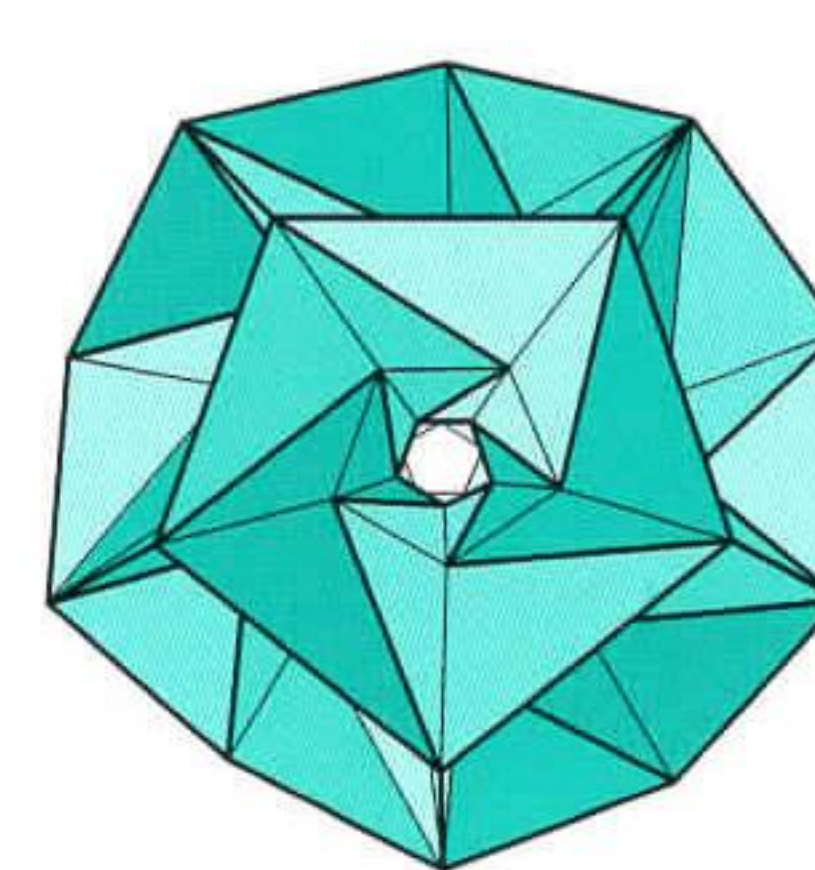
12-piece #2



24-piece



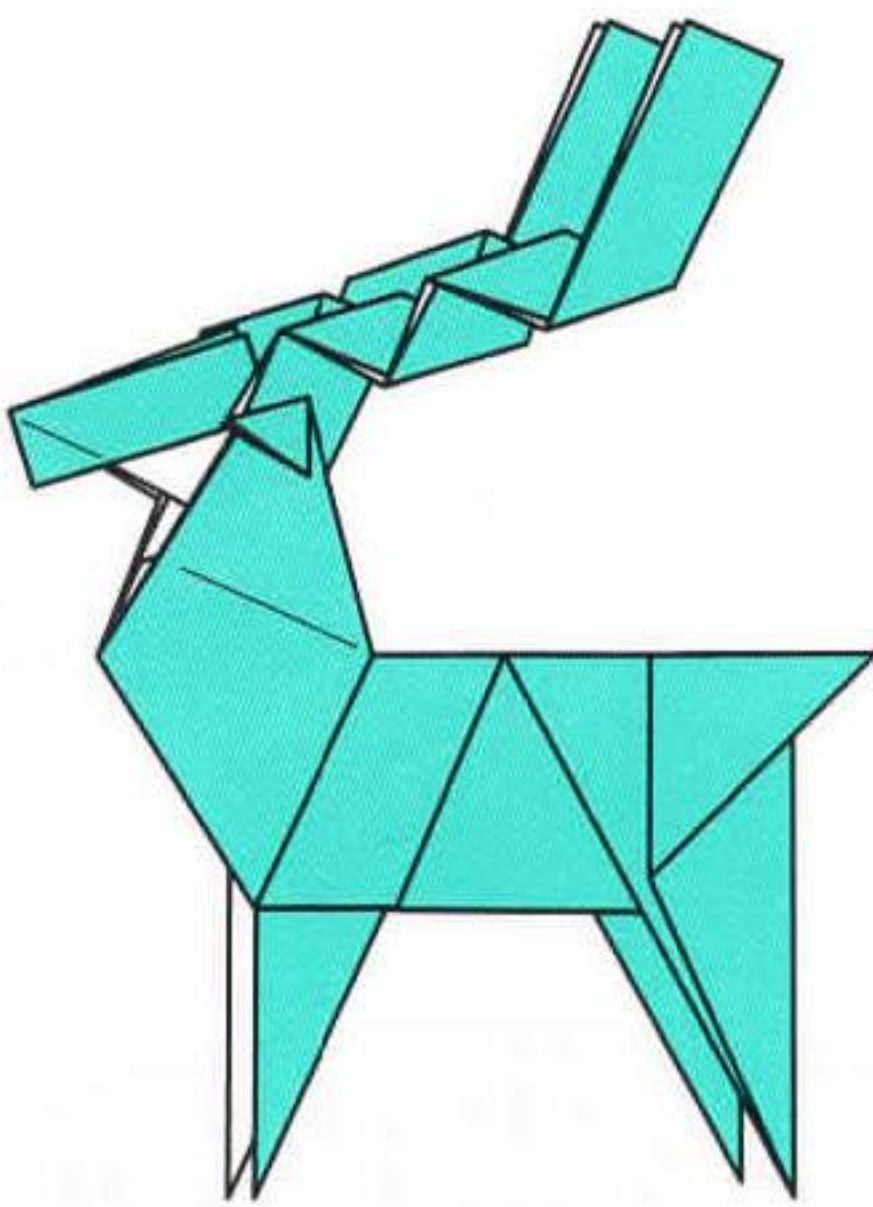
30-piece



30-piece #2 (reversed; not stable)

Tea-bag Reindeer

Theme: Irregular shape
Fold using a tea-bag envelope.



This model starts from nowhere near the “square” required in “one square sheet without cuts.”

Shapes of paper

Why square is regarded as a special shape in origami?
There had been several discussions on a Web BBS several years ago, and here is the summary.

- * History
There is a enormous repertory of models that start from a square, including *Orizuru* (crane).
Square origami paper has been commercialized and is now wide-spread.
Obeying the rule leads to development of techniques, challenge, and unexpectedness.
- * Simplicity
Square is easy to make (and cut).
Square is easy to describe.
Square seems to be a tabula rasa in origami, as it resembles to almost nothing.
- * Perfection
Square is regarded as a prototypical shape. Square is regarded as a natural shape.
- * Other geometric features
Square is “symmetric” in a broad sense, because of its repeating structure and other reasons.
Square has two types of axis of symmetry, a diagonal and a perpendicular bisectors, both of which offers different “expressions.”

There are so many various factors that I do not dare to come to a conclusion. But I am sure square will continue dominating origami.

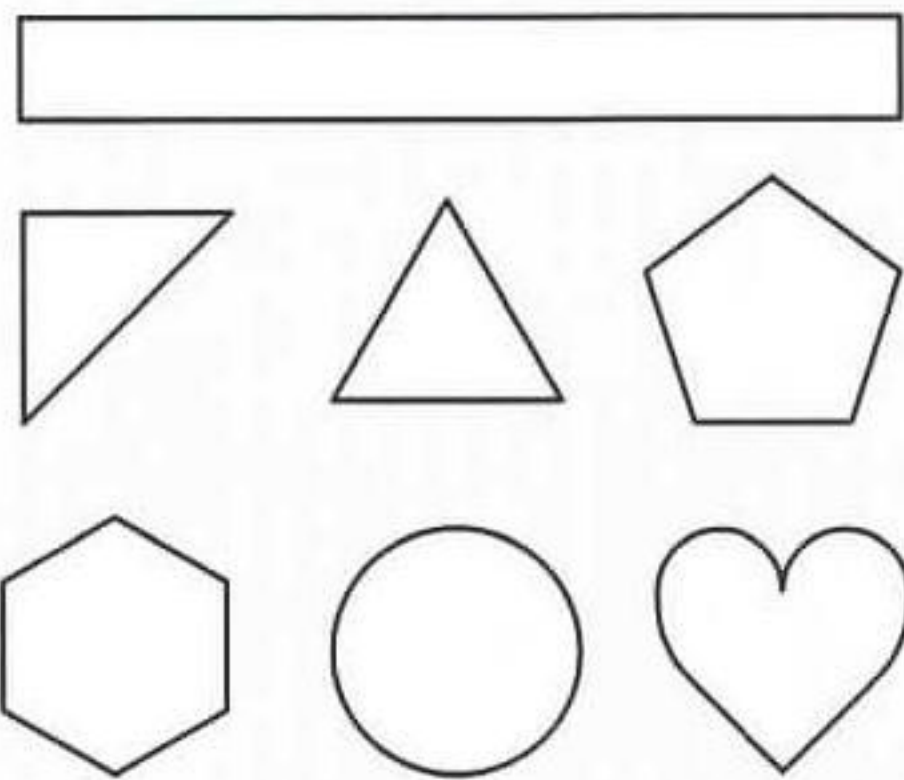
However, as I said at the beginning of this book, many sheets of paper around us are not square.

The most common shape worldwide is the rectangle with 1.414... ($\sim\sqrt{2}$) : 1 aspect ratio, which is also called silver ratio. This shape has been standardized because the ratio of its half shape is the same. This property is also useful in origami. Some traditional models such as airplanes and boxes start from that or similar rectangles. One can say that the silver rectangle is a close relative of the square, because the length of the long side is the same of the diagonal of a square whose sides are equal to the short side.

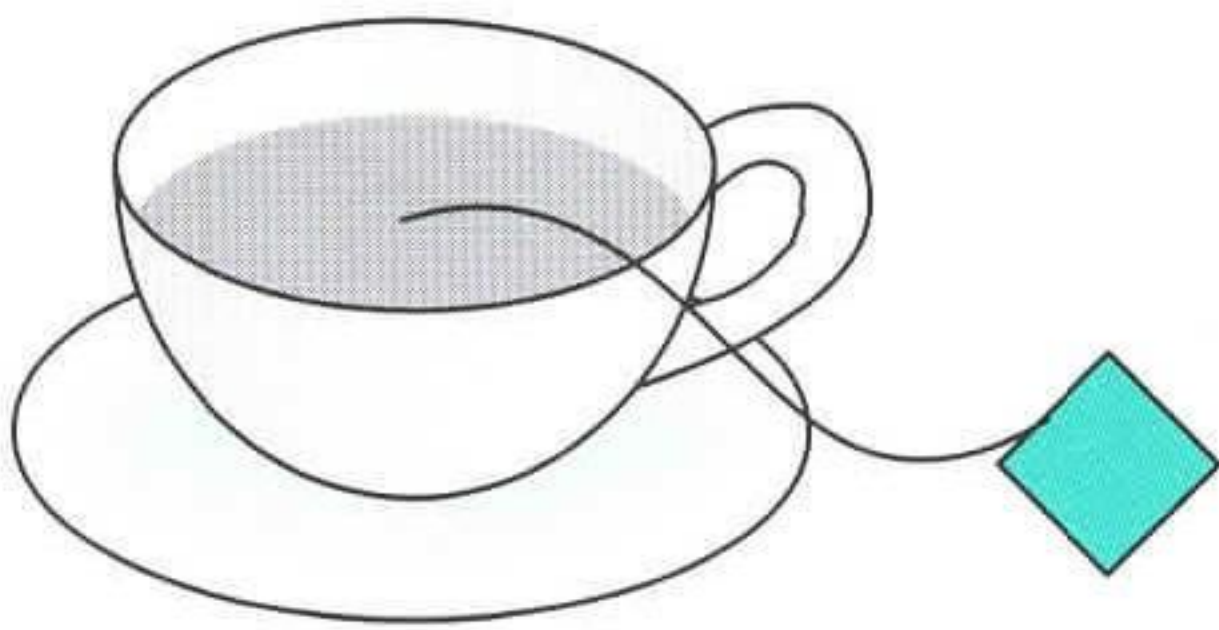
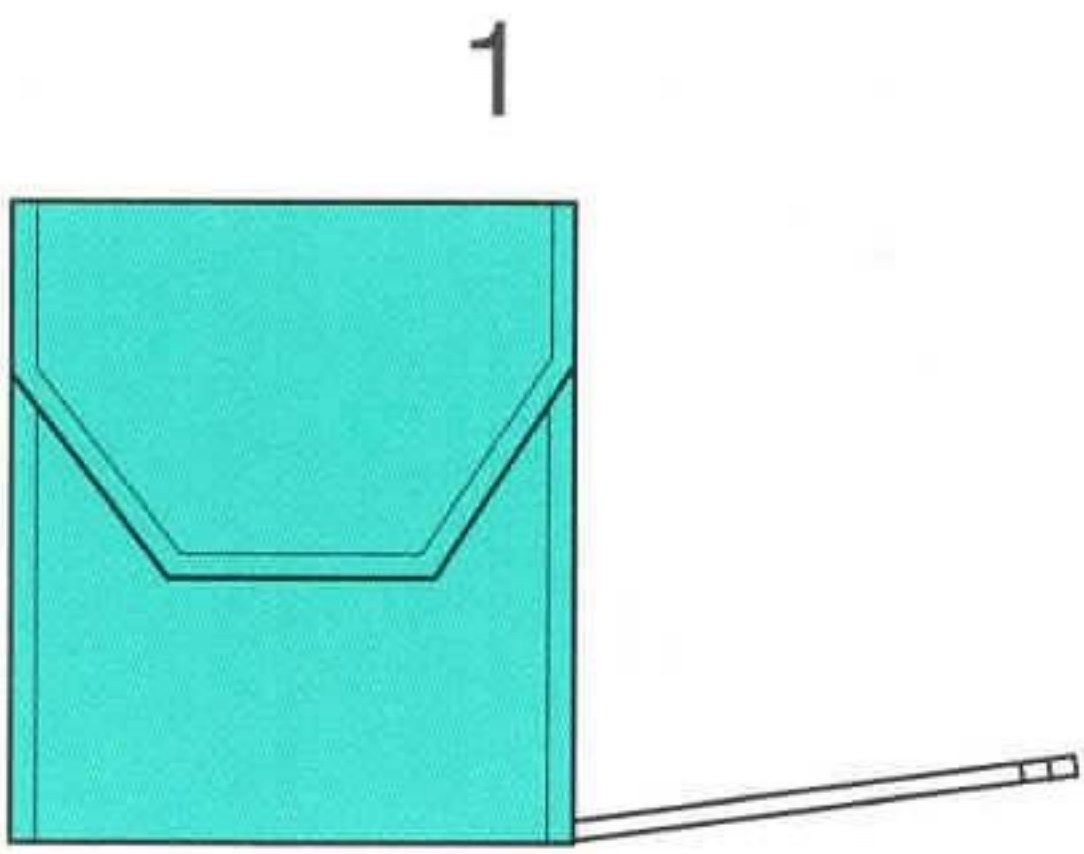
Besides the rectangle, various shapes such as a rectangle with the golden ratio or 1 : 1.618..., a tape, and all kinds of polygon can be used in origami. Bank notes, with ratio of about 1 : 2, are also common in origami. In short, sheets of any shape can be used in origami as long as the main method of design is folding.

Silver rectangle 1
1.414..

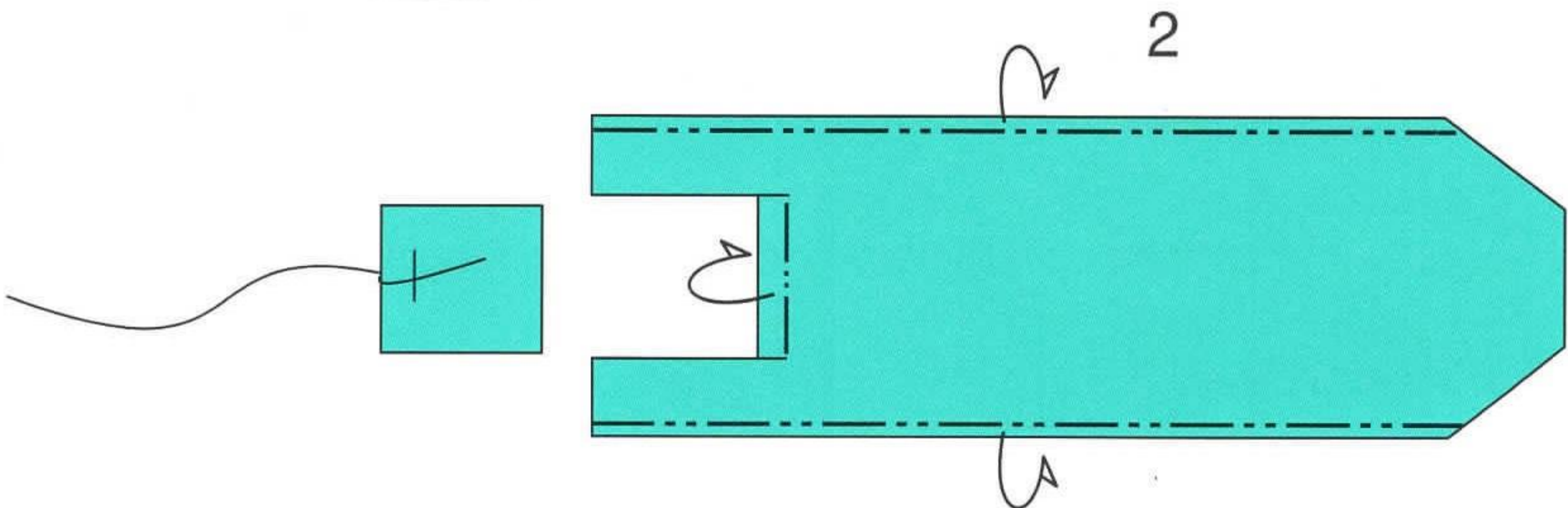
Golden rectangle 1
1.618..



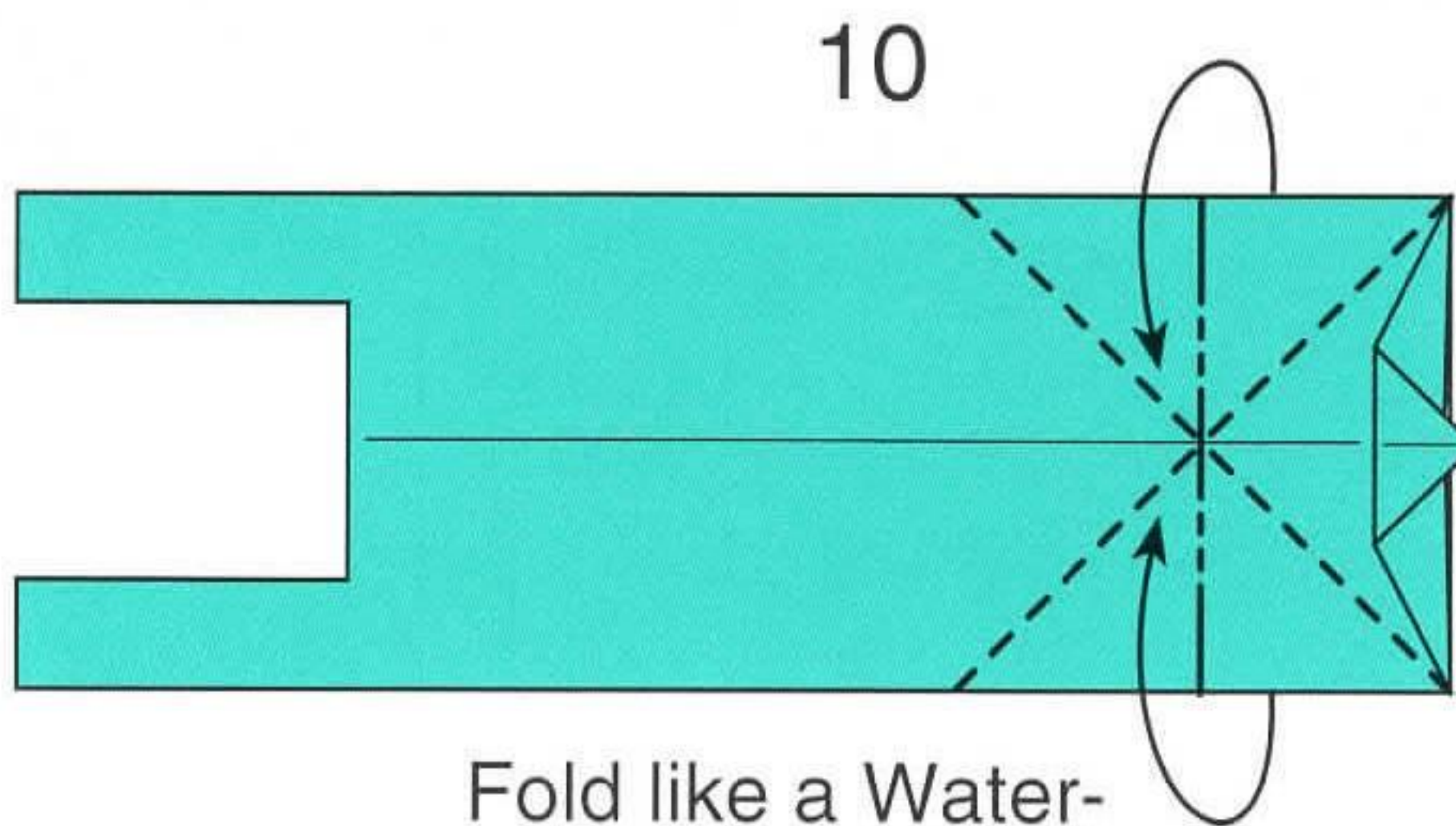
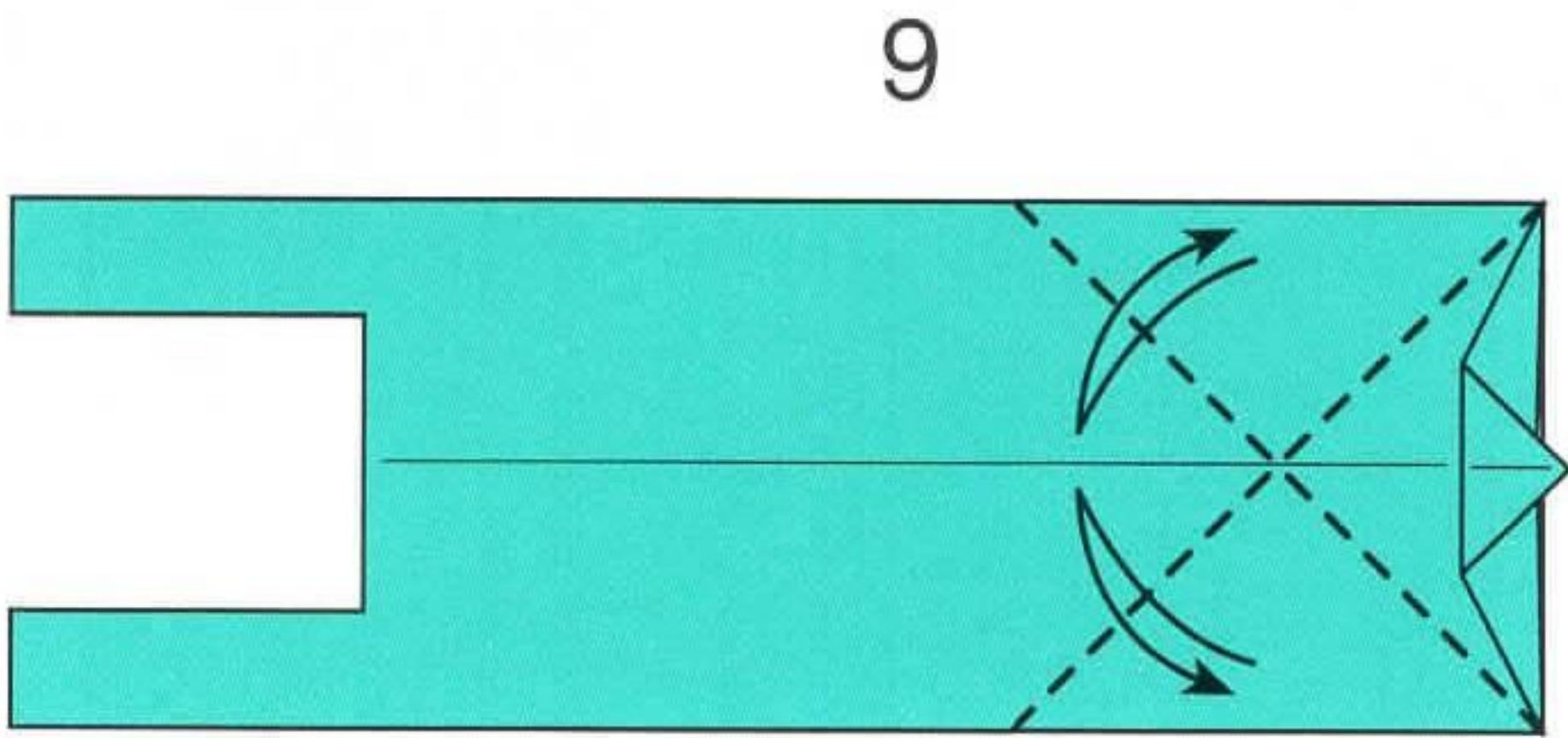
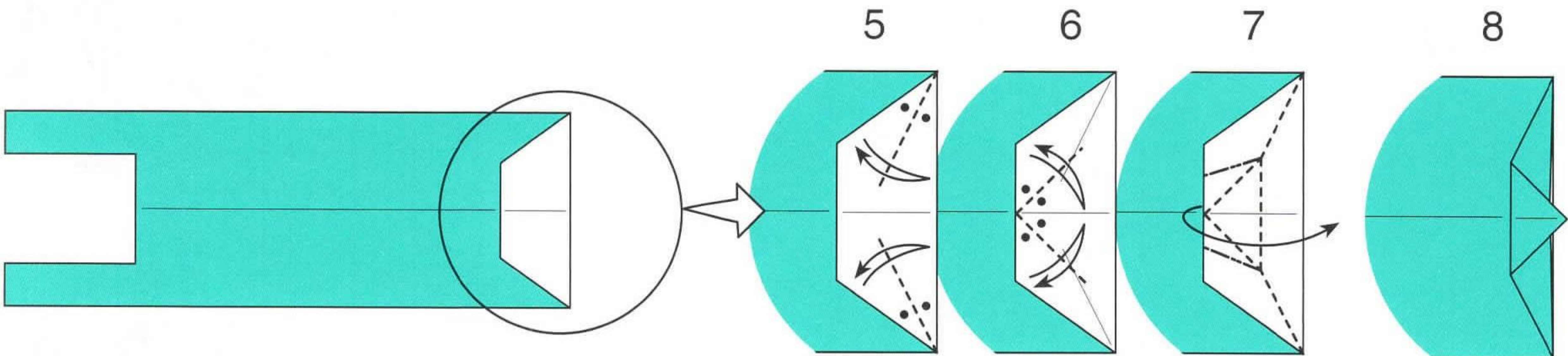
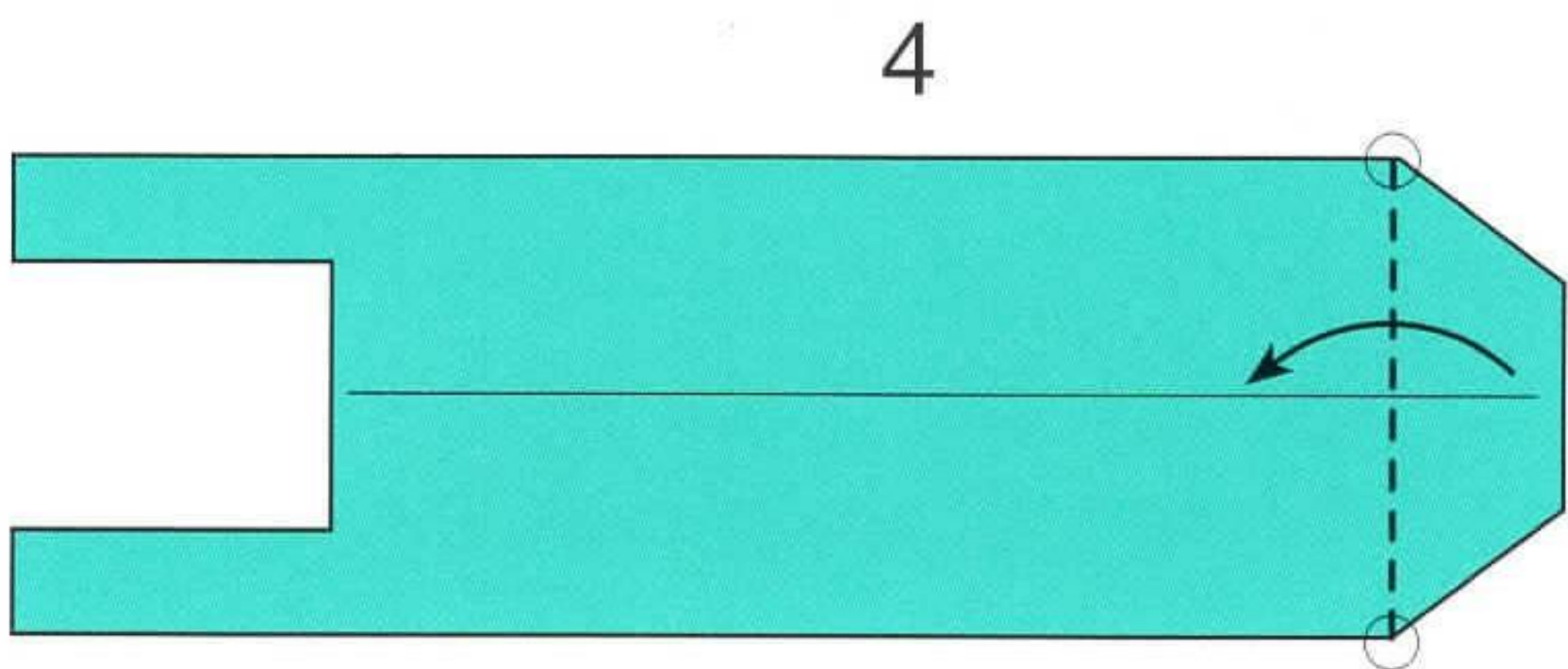
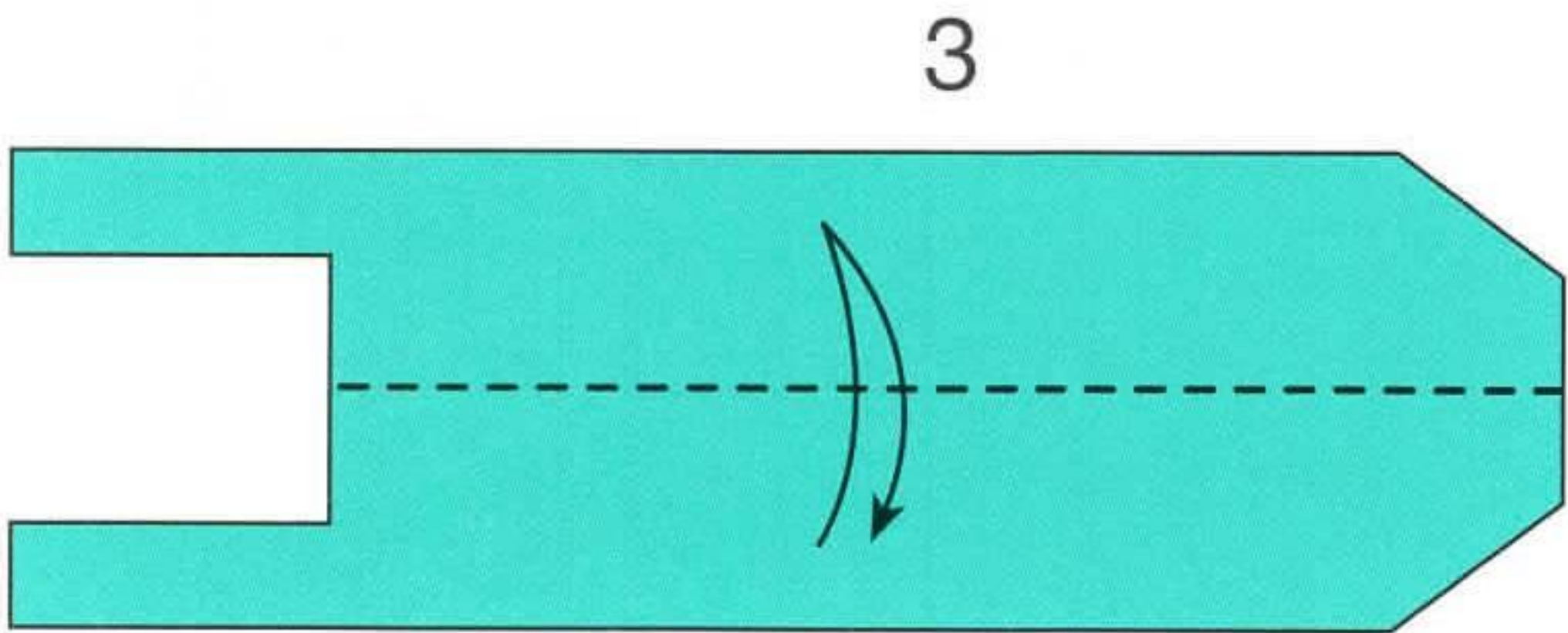
Various shapes



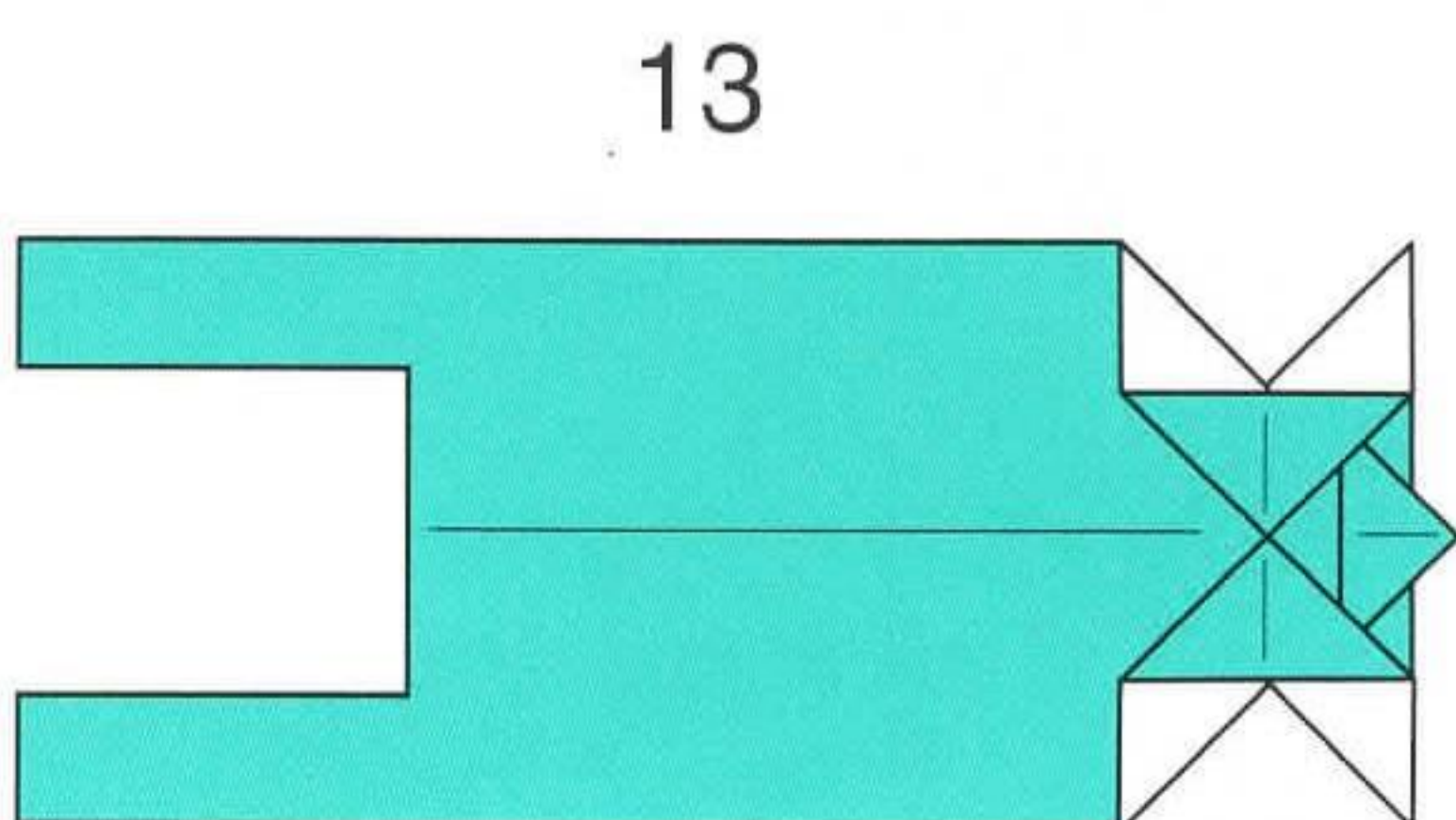
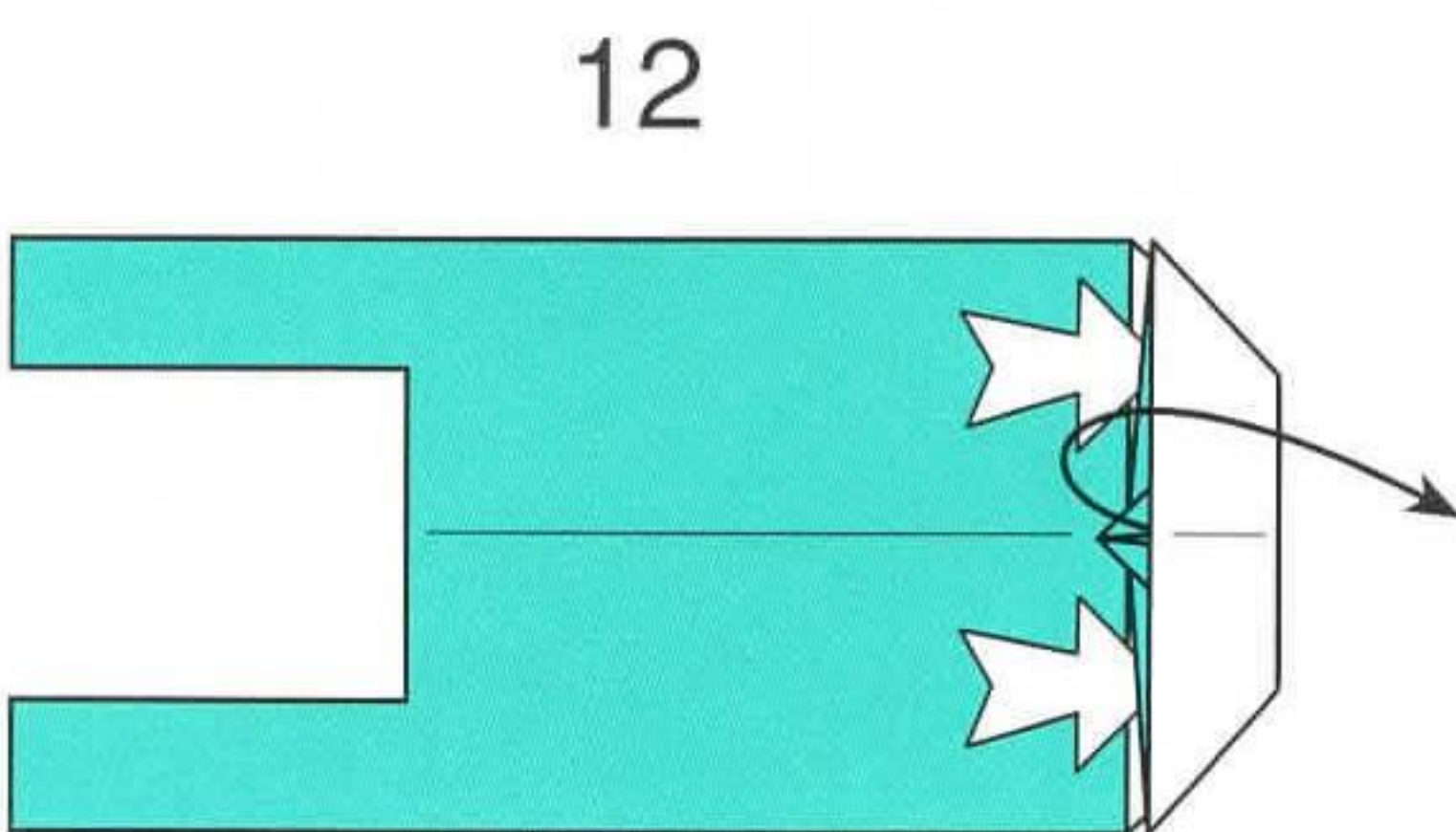
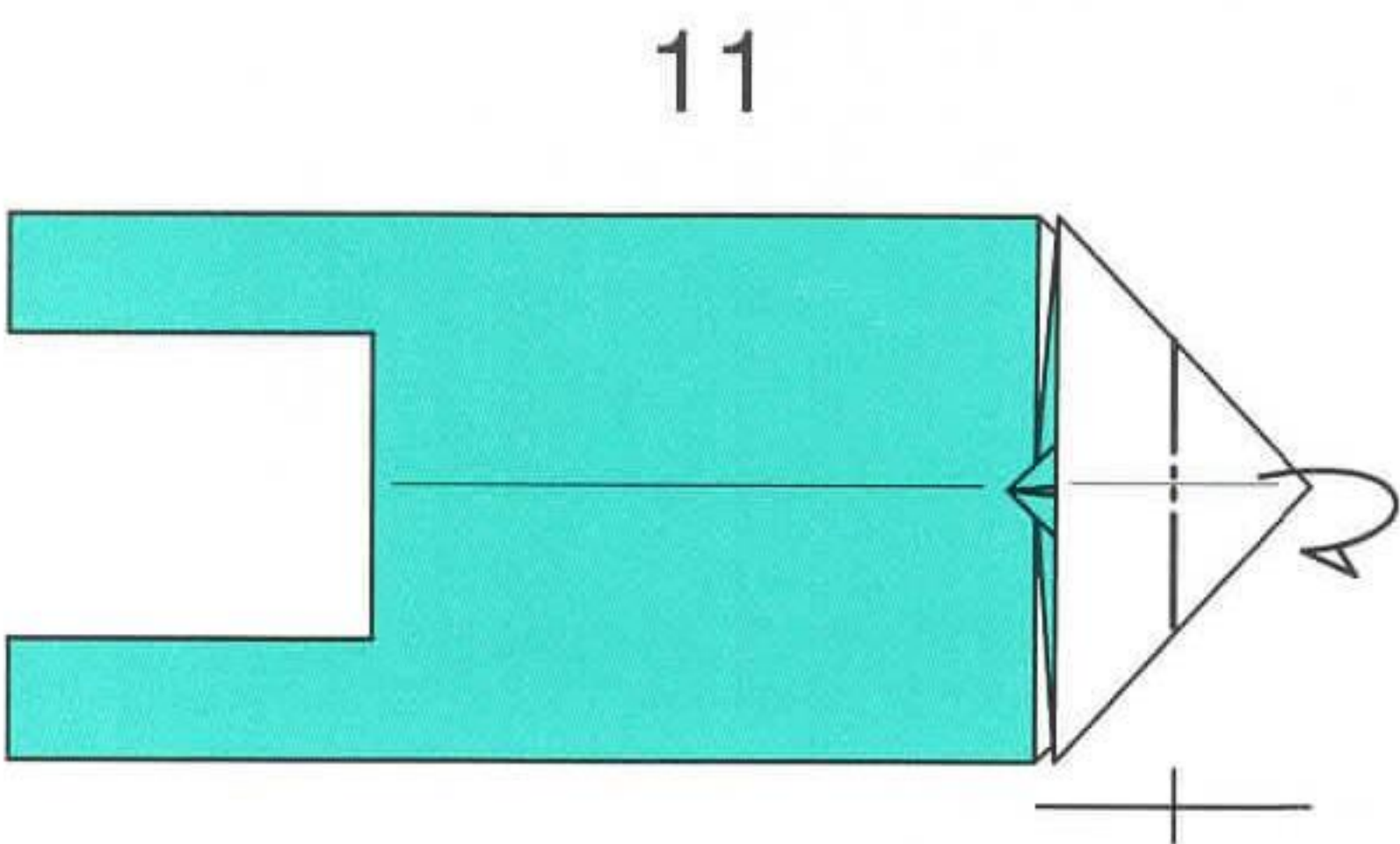
Open a tea-bag envelope from the bottom with a toothpick.

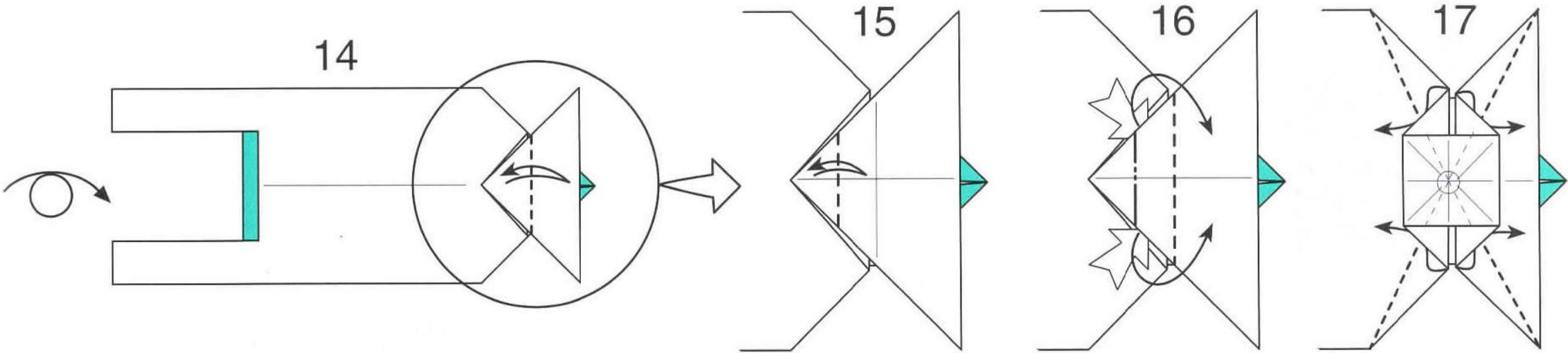


Fold behind (or cut if you don't have a neat edge).

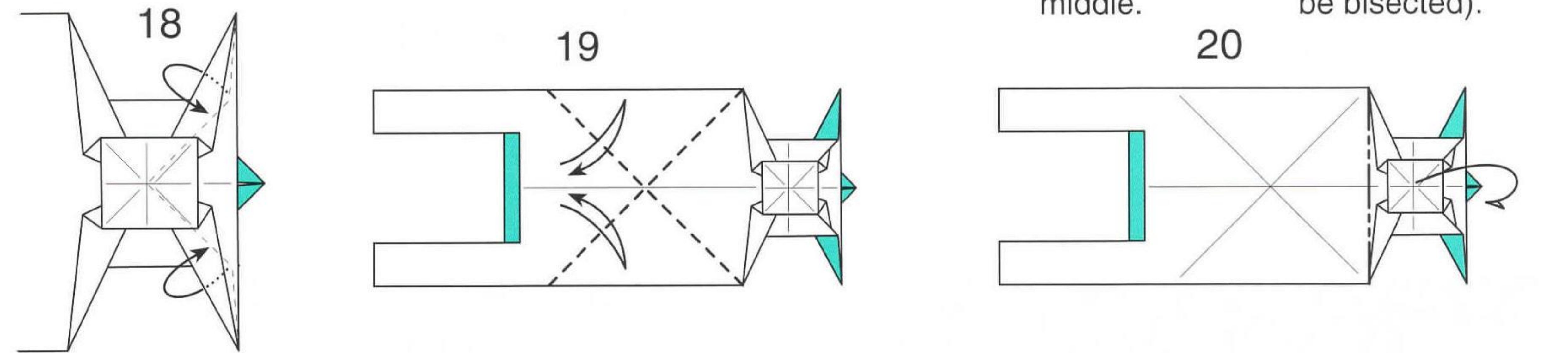


Fold like a Water-bomb base.

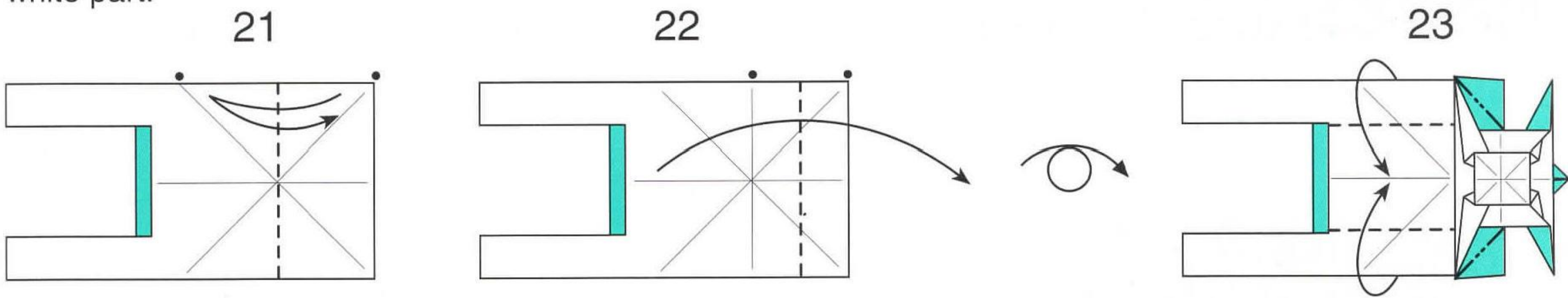




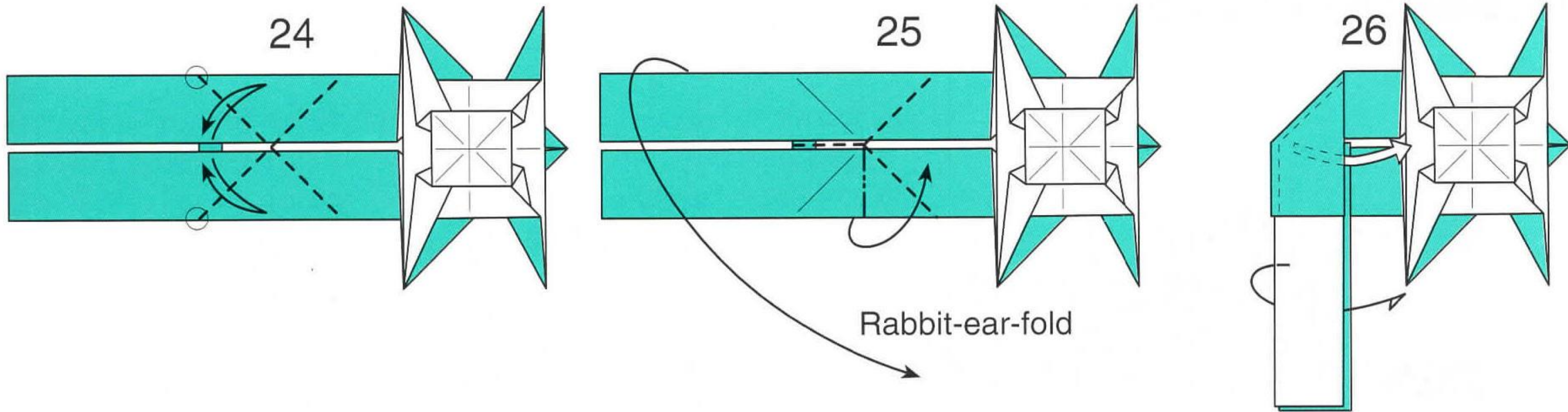
Spread and squash at the middle.
Inside reverse-fold (the angles will not be bisected).



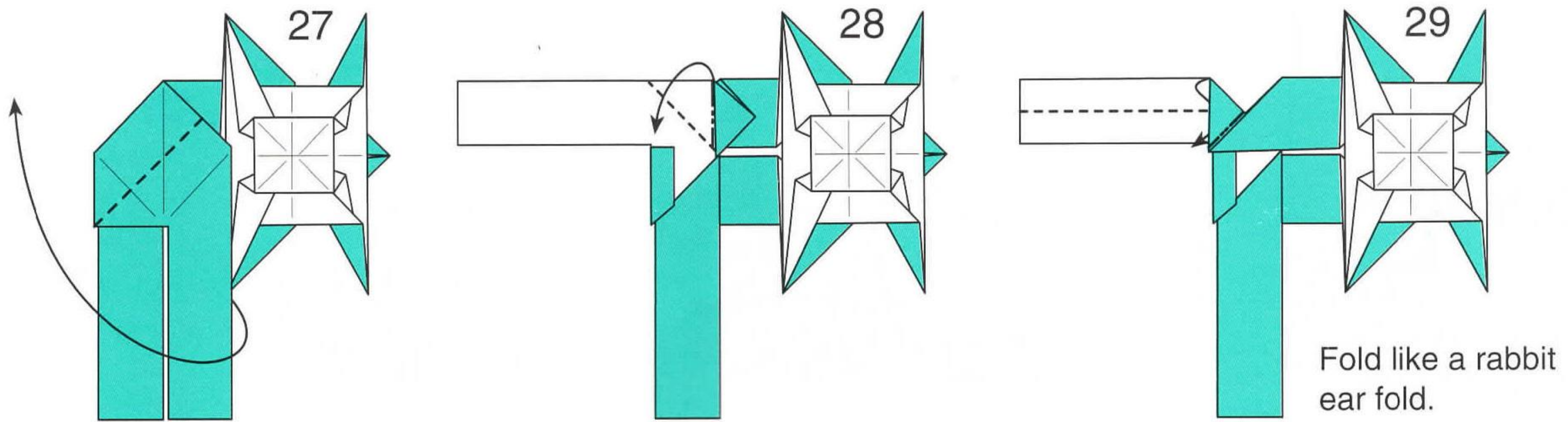
Wrap to hide the white part.



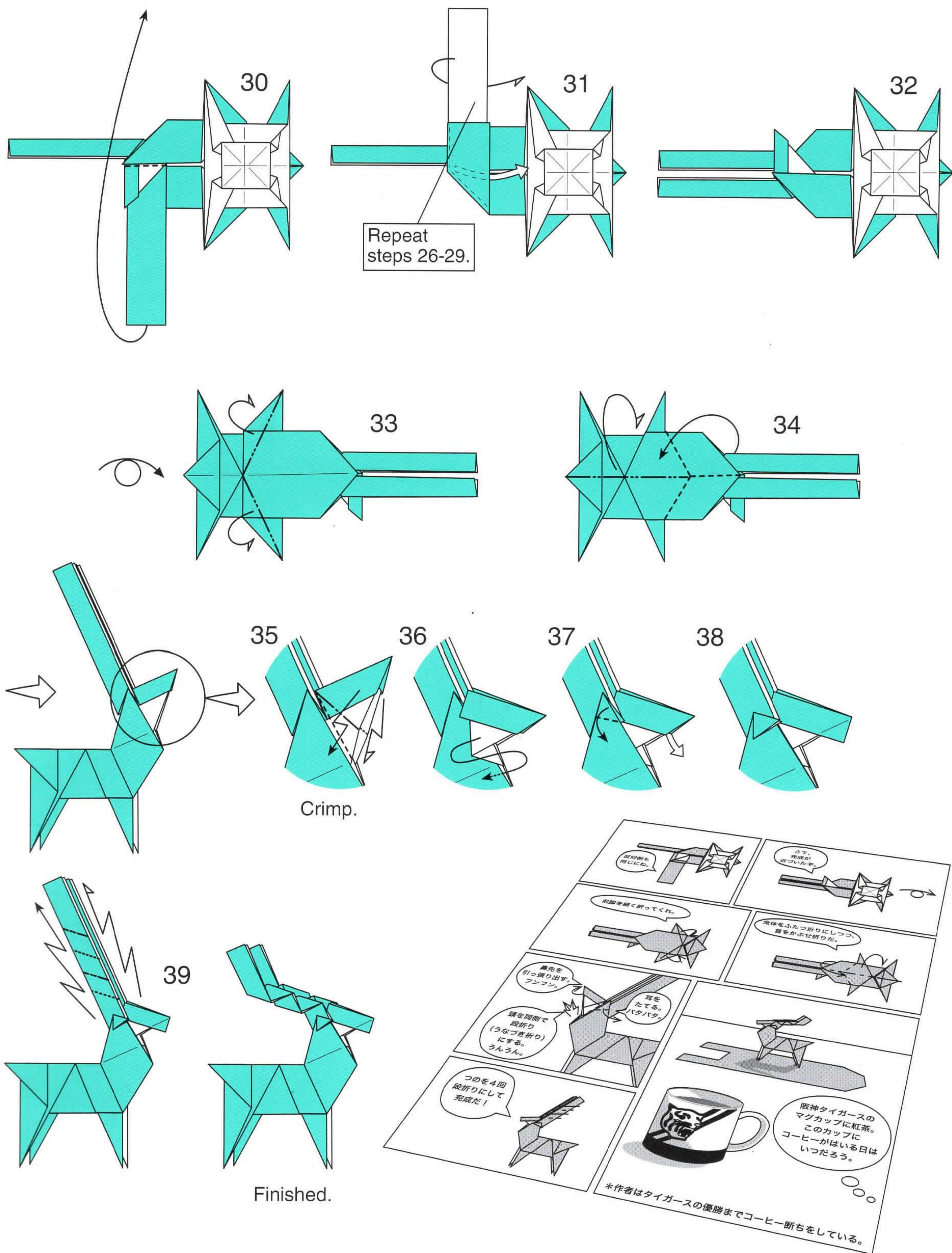
Swivel-fold



Rabbit-ear-fold



Fold like a rabbit ear fold.

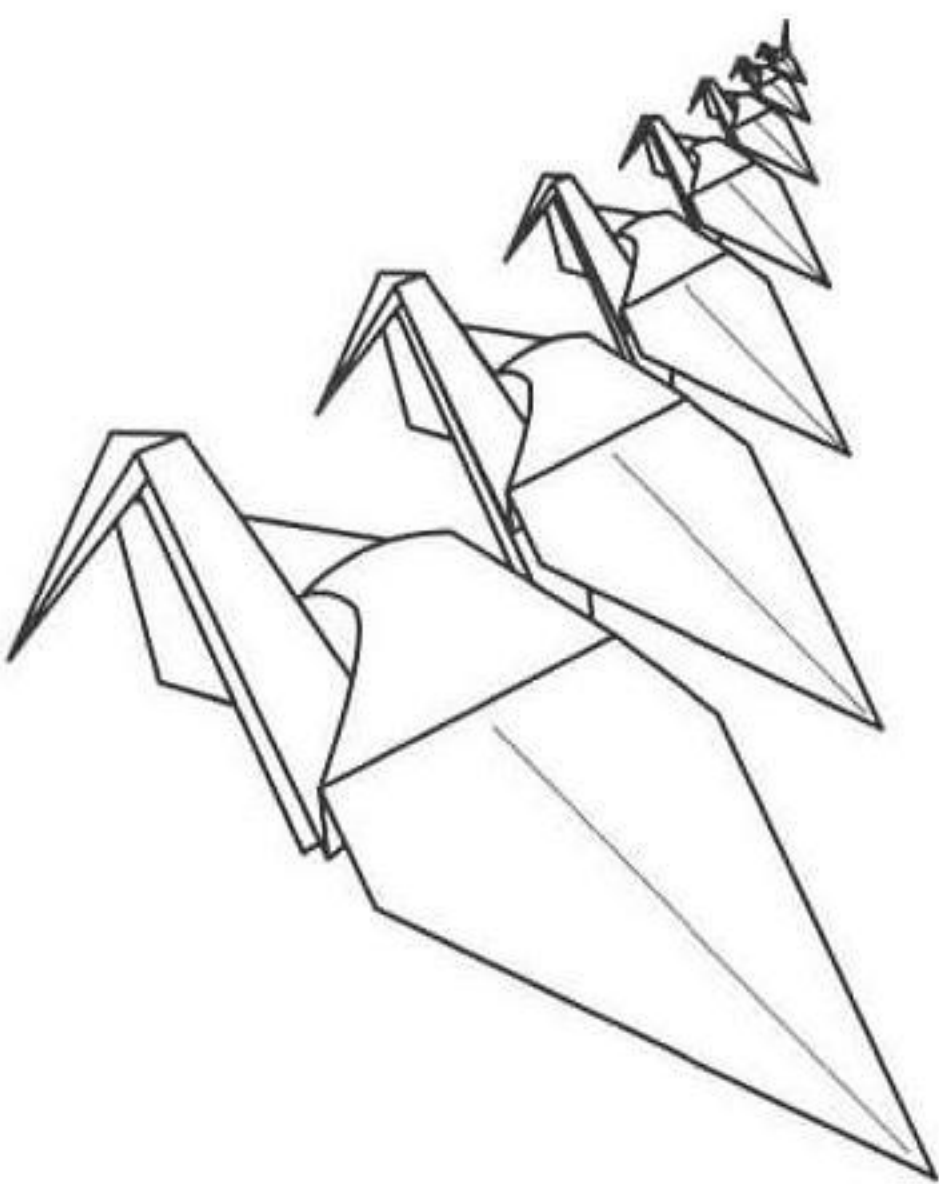


Sample page from *Origami Tanteidan
Convention Book volume 3*
(1997, self-publication, out-of-print)

Connected Cranes, Kotobuki

Theme: Cut

Fold using washi
(Japanese handmade paper).



Let's think about "without cuts" as in "one square sheet without cuts" based on a model with some cuts.

Cuts in *Sembazuru Orikata*

In 1797, Rito Akisato, who was known for his *Miyako Meisho Zue* (*Pictures of Landmarks in Kyoto*), published a book of kyoka (comic haiku) titled *Hiden Sembazuru Orikata*. The book contains 49 models of connected-crane designed by Gido, who was the chief priest of Choenji temple at Kuwana city, under the pen name of Rokoan.

This book has a big historic value as the oldest known book of recreational origami (versus ceremonial origami). In addition, the models in the book are still attractive today even though they are more than 200 years old.

Although each crane is just an ordinary traditional *Orizuru*, the connections of cranes are as interesting as puzzles and filled with surprises. Some examples from the book are shown on this page, *Sugomori*, *Seigaiha*, *Kuretake*, and *Imosemaya*.

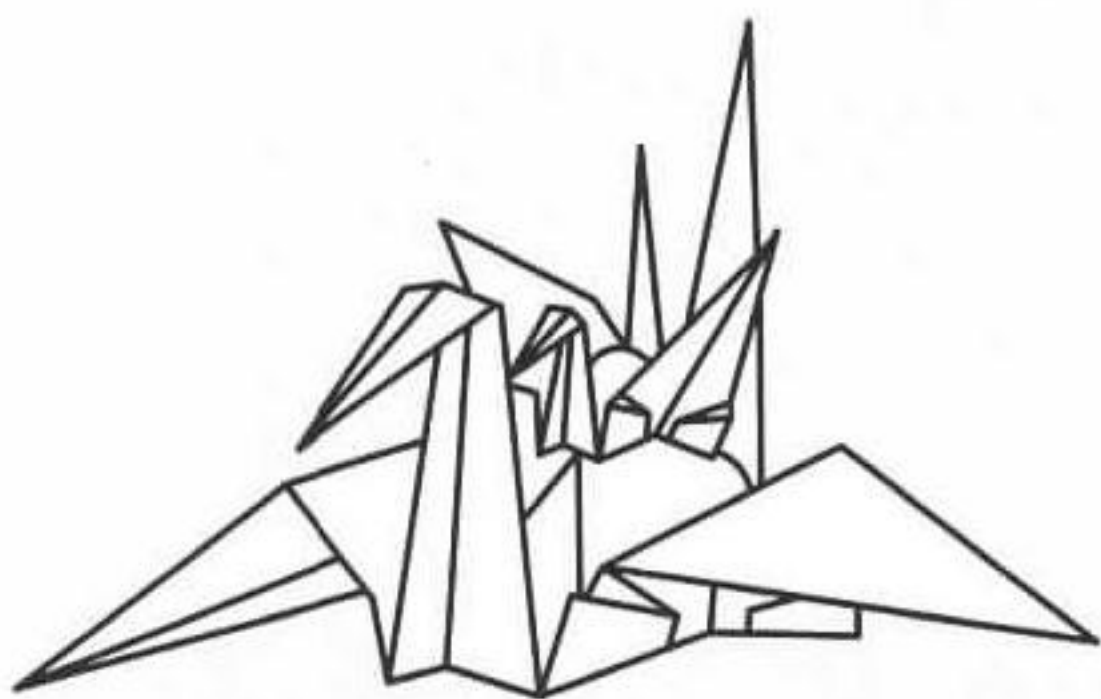
The book contains no folding diagrams but cutting patterns and pictures of finished models. Although they include many cuts, all the models adhere to two rules:

1. Start from a rectangle (including square) sheet.
2. Do not cut off any part.

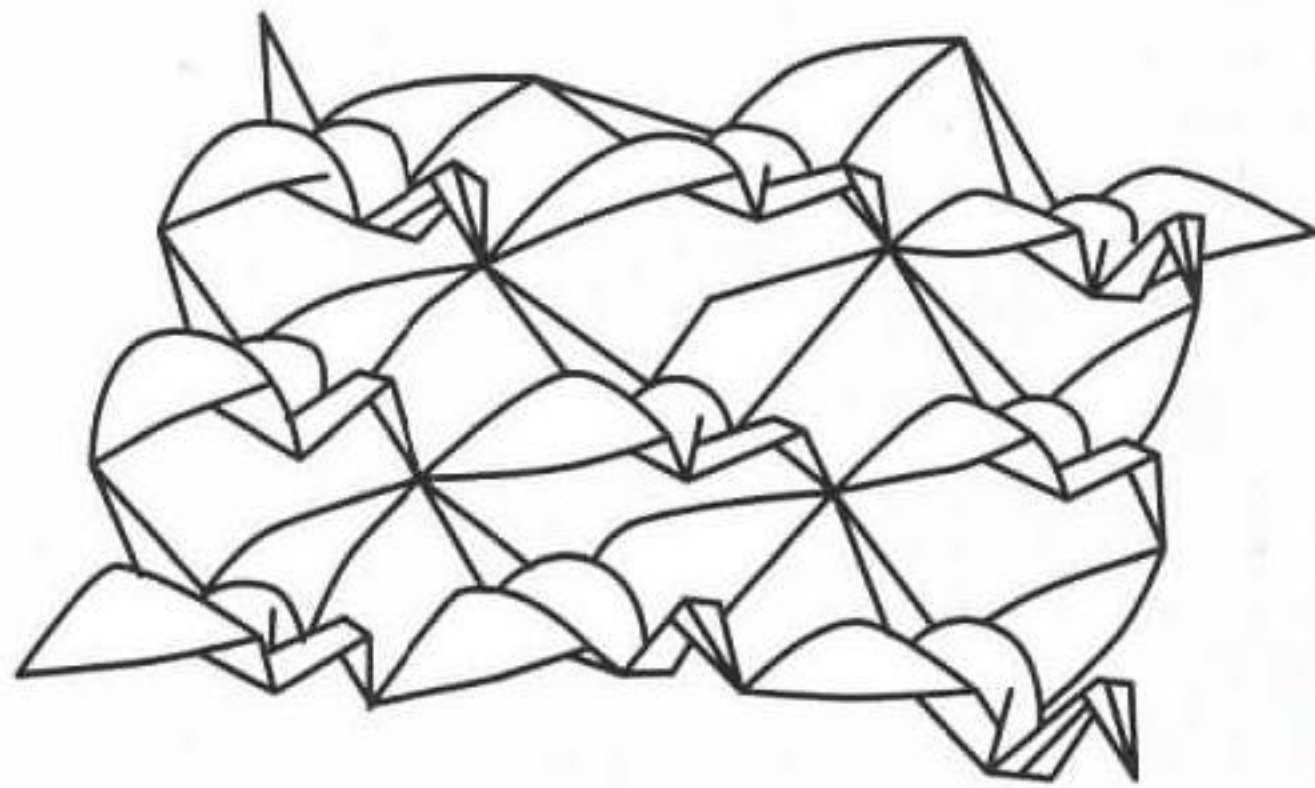
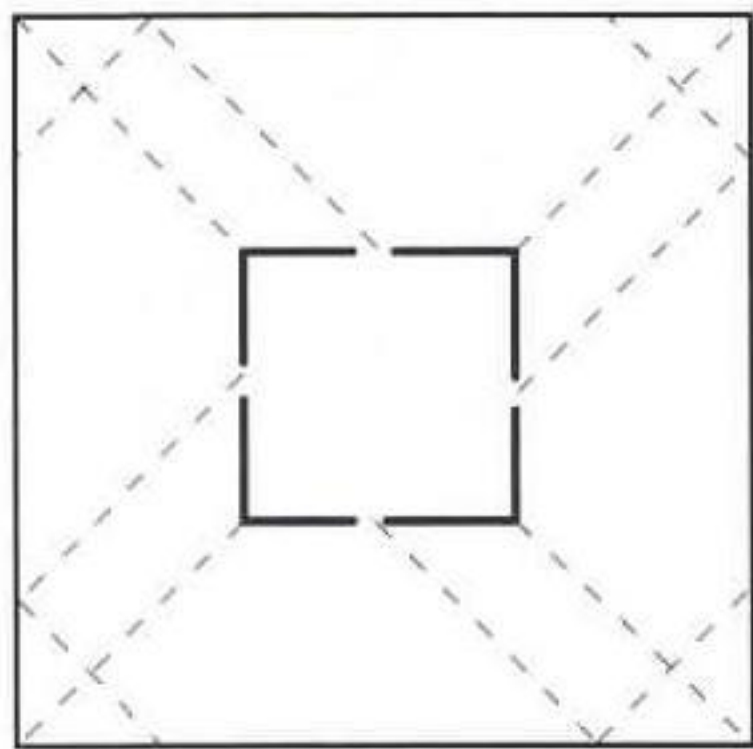
Japanese traditional origami (then called "orikata" or "orisue") was different from modern origami in that cuts were not avoided. Nevertheless, the models of *Sembazuru Orikata* are still popular origami even now.

That is because, in my opinion, the models are geometric and puzzle-like. Moreover, even if they includes cuts, the main sequences still consist of folds, and cuts are subsequent to folds.

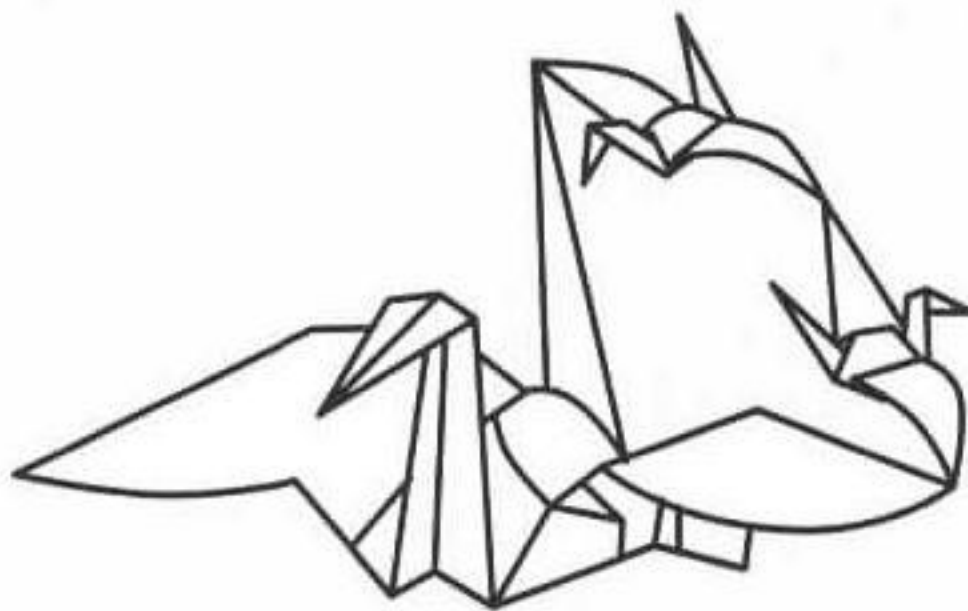
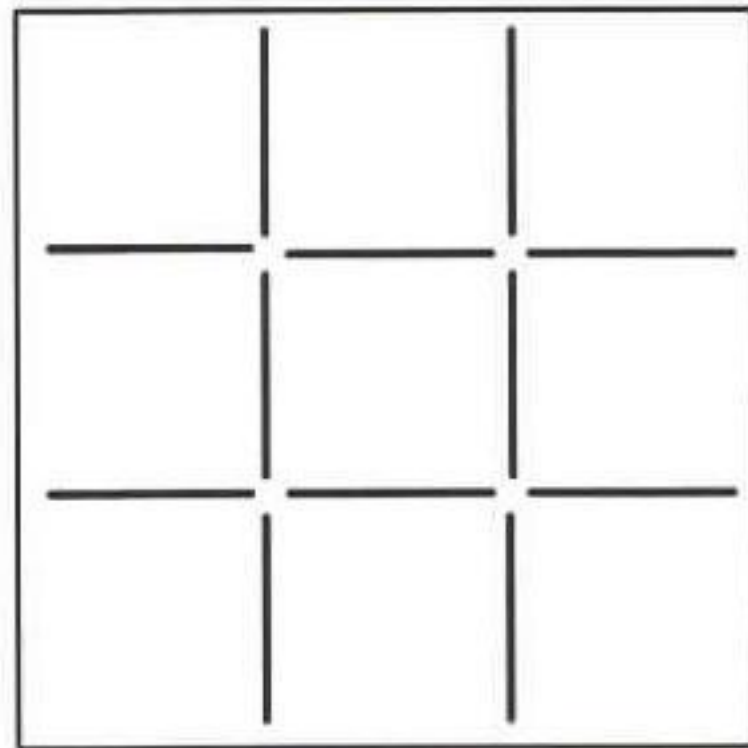
By the way, such connected-crane models were traditionally called "sembazuru," or literally one-thousand cranes. But more recently the Japanese call it "renkaku" or "renzuru."



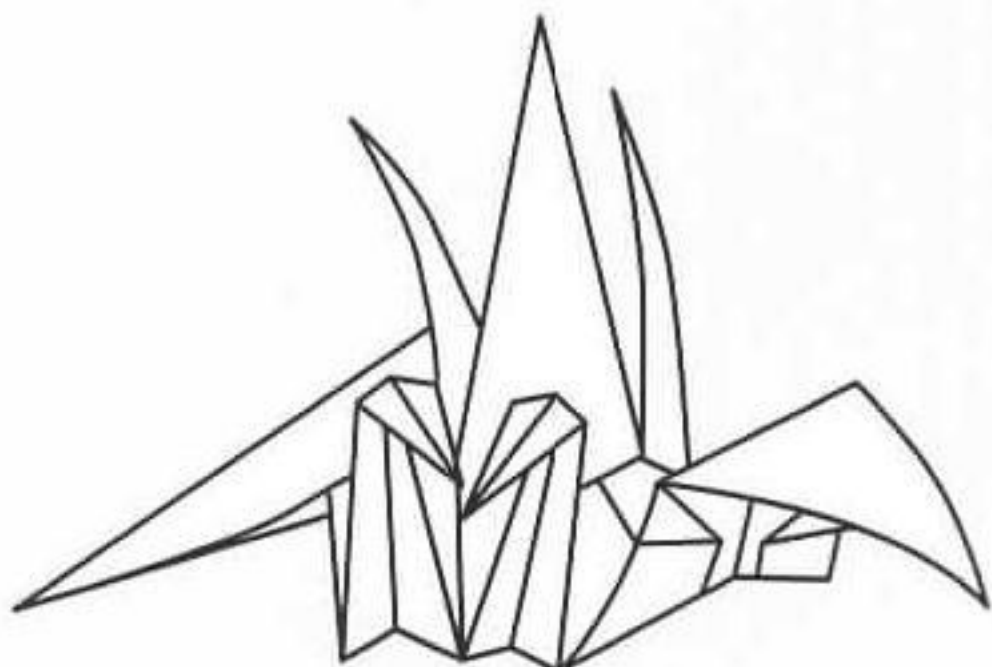
巢籠



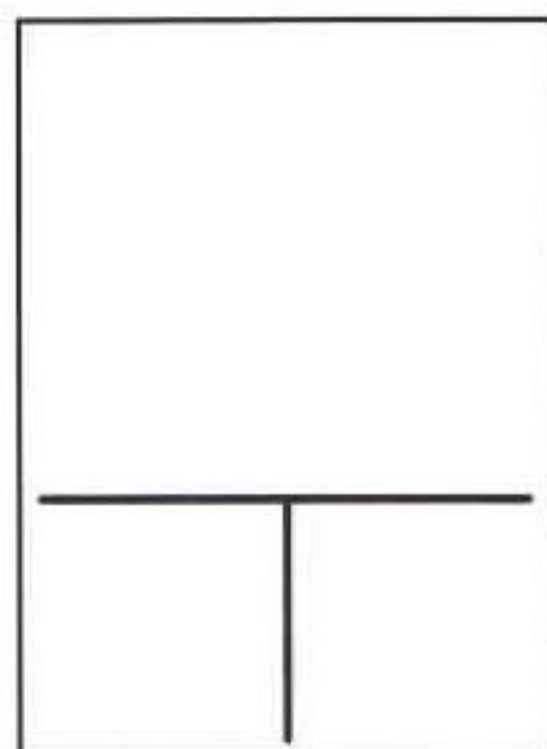
喜海波



呉升



妹脊山



Cuts in origami

Some say cuts are prohibited in origami. But if cuts are really prohibited, we must use paper that has no border, such as an infinitely wide plane or a sphere. We can only obtain a square sheet by cuts. Moreover, cutting relates to the number of sheets used for a multi-piece model.

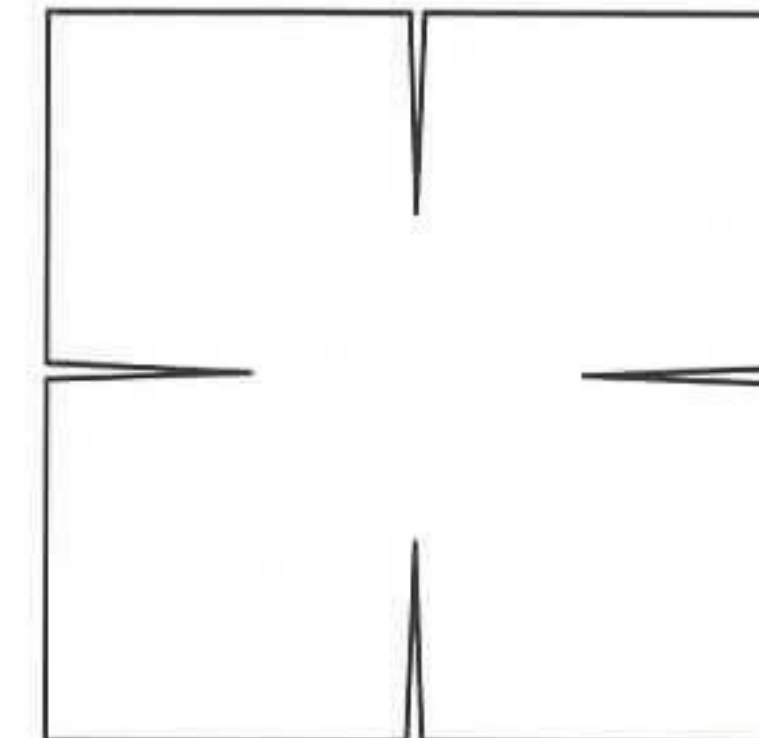
For example, instead of starting from two square sheets, one can start from one sheet of 1 : 2 rectangle and cut it in half.

Of course, cutting also closely relates to the shape of paper.

For example, the picture on the right is the shape for *Crab*, appearing in a private encyclopedia of 19th century titled *Kayaragusa*, which contains historic records of origami.

At first glance, it looks nothing but a square with cuts.

But we can also say it is a hexadecagon with four 360° angle corners and twelve right angle corners. That is, we can say this model is folded using one hexadecagon sheet without cuts.



The shape of paper for Crab from Kayaragusa.

For me, the home of origami is still in a square without cuts. But, in a broader perspective, my criteria of "origami-like" is how elegant the model is in a geometric sense.

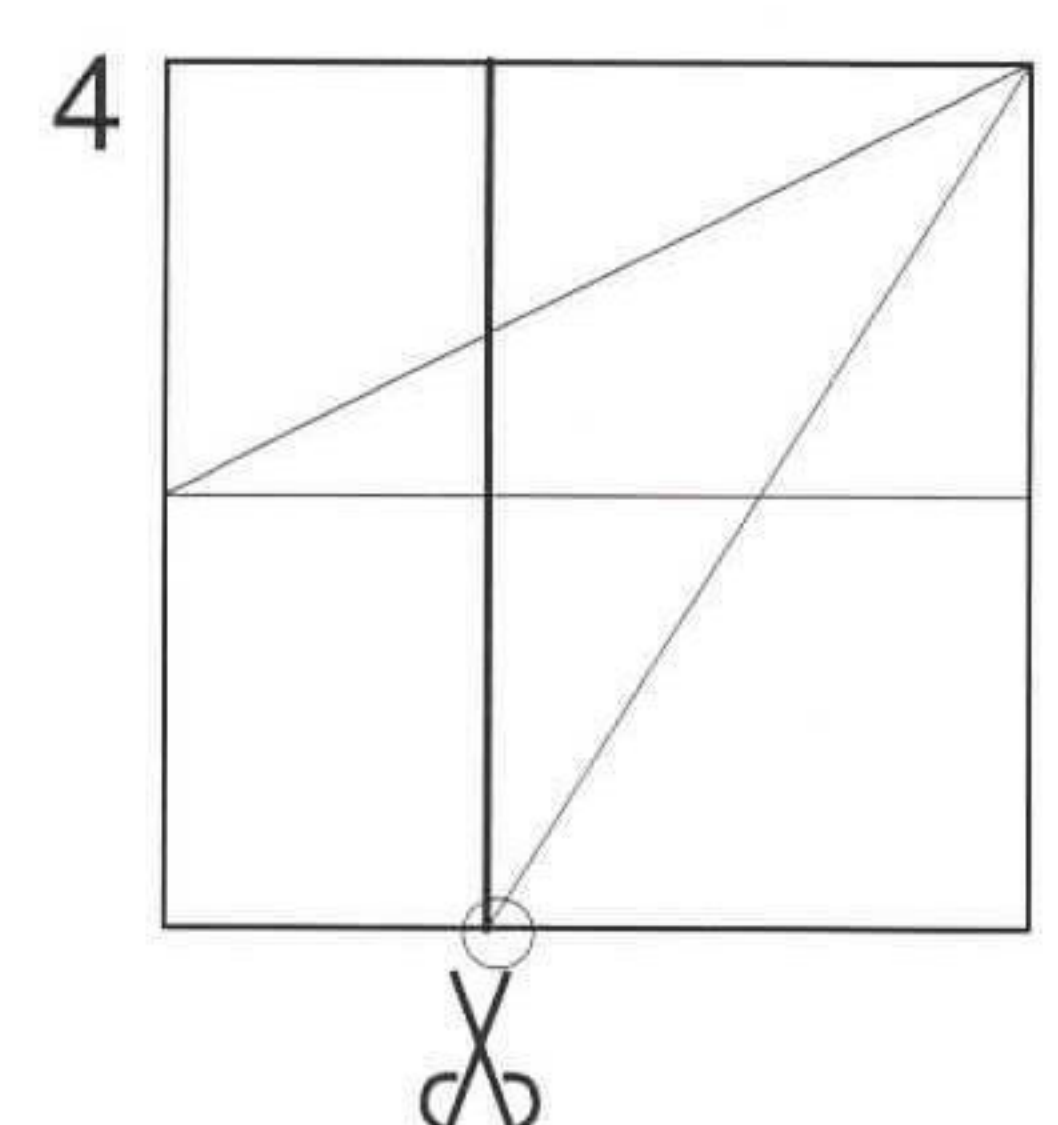
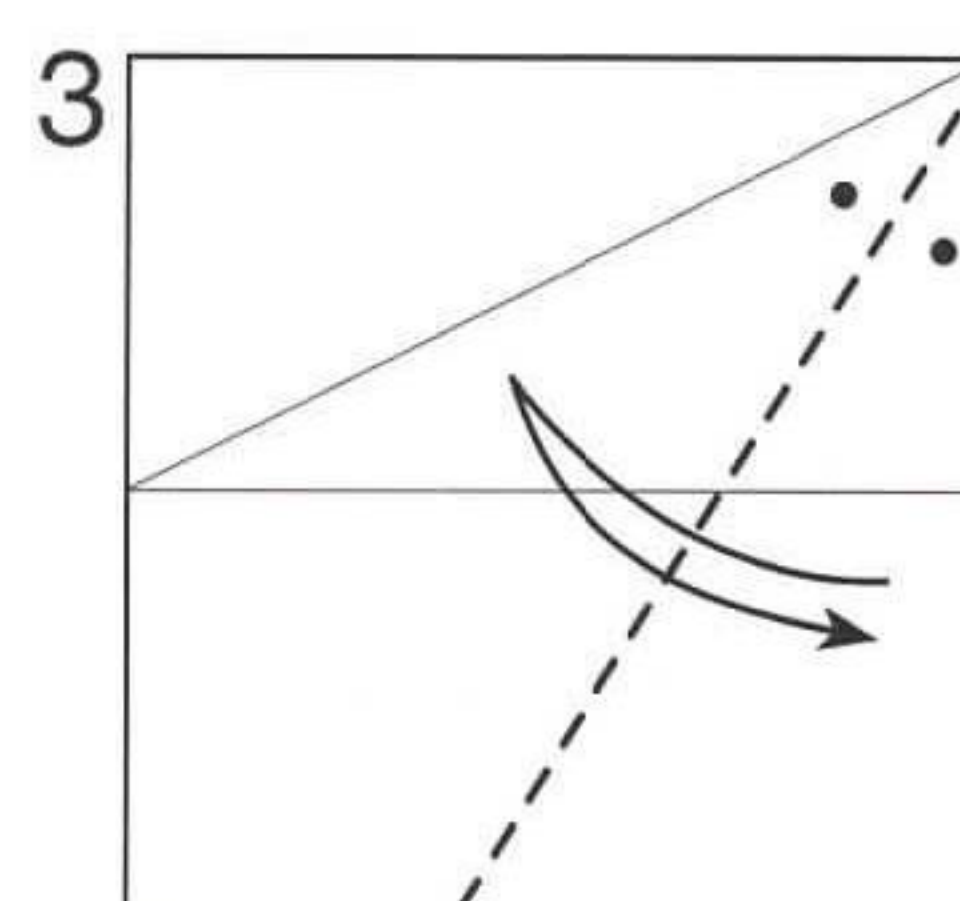
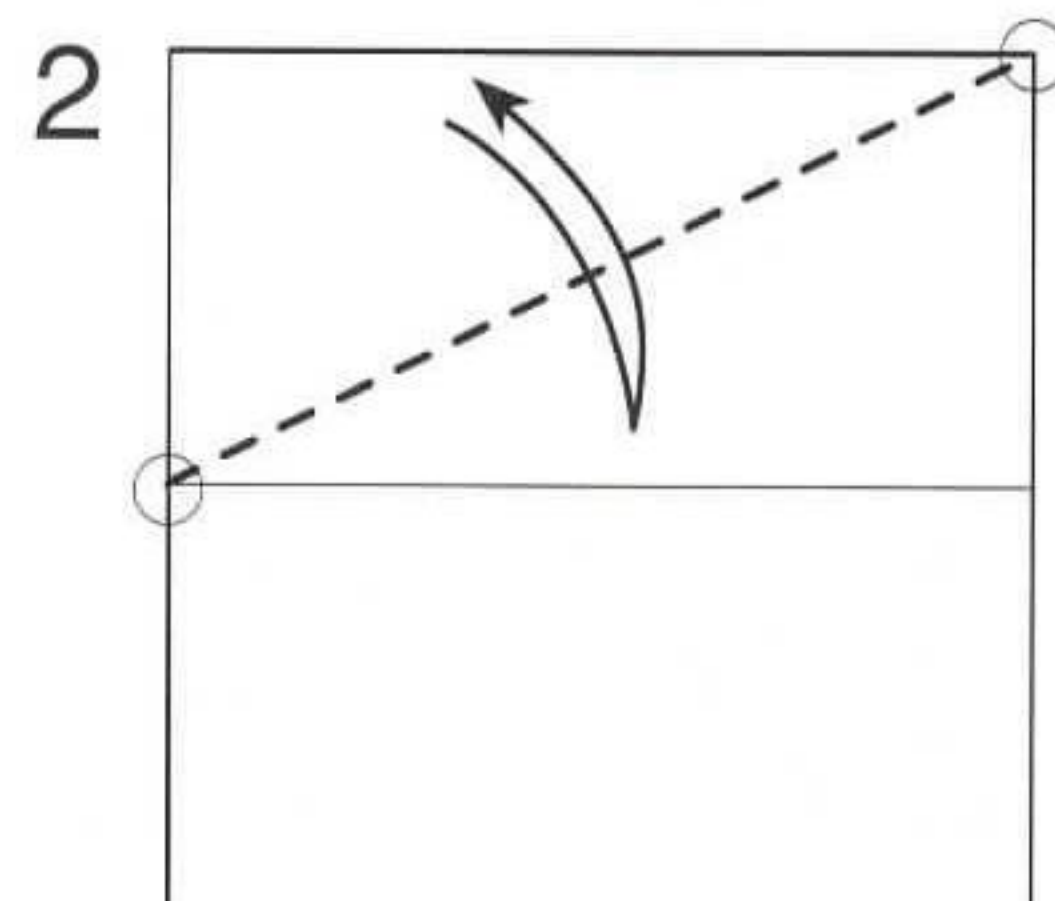
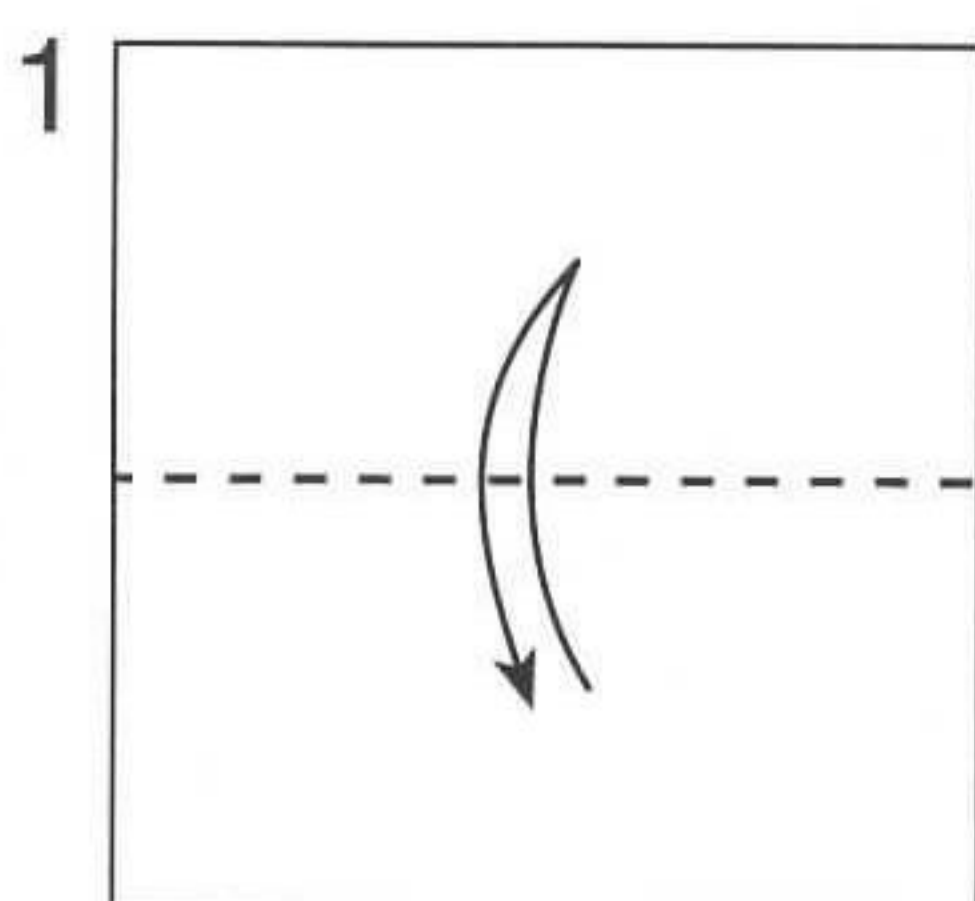
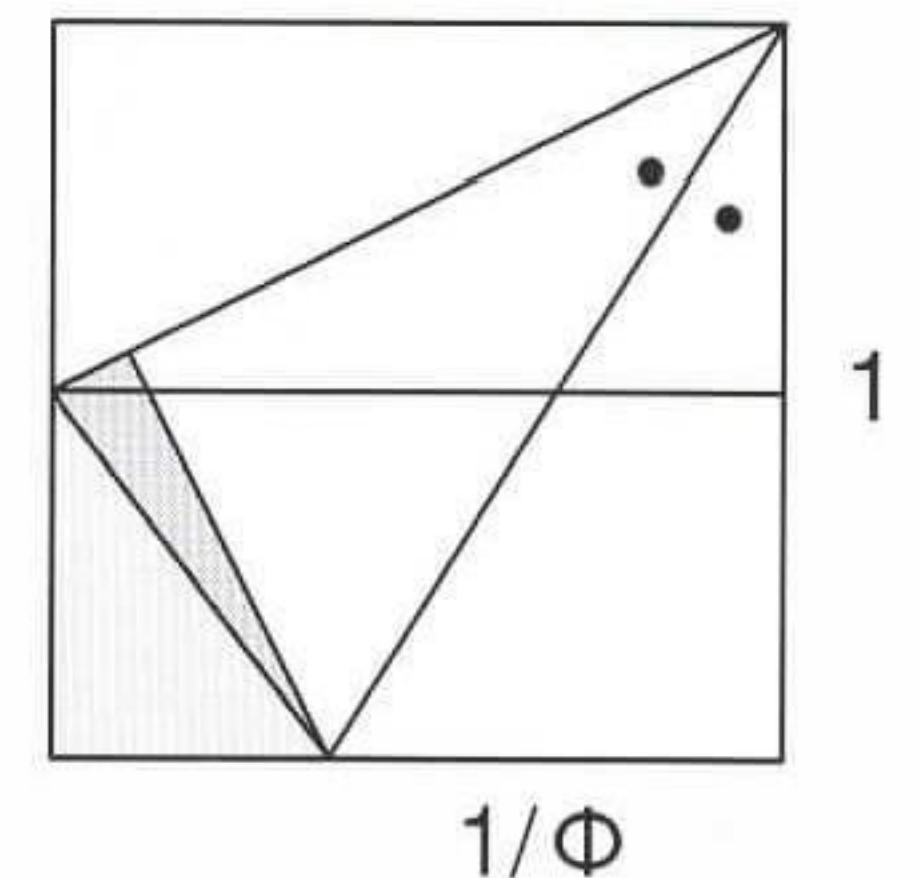
From that point of view, models in *Sembazuru Orikata* are truly origami-like. The rule of "one rectangle sheet without cuts-off" is as well elaborated as "one square sheet without cuts."

Here is my connected-crane model that I believe Rokoan did not come up with. To avoid cuts-off, you must fold smaller and smaller cranes infinitely. But in reality, it will be impossible to fold more than five or six.

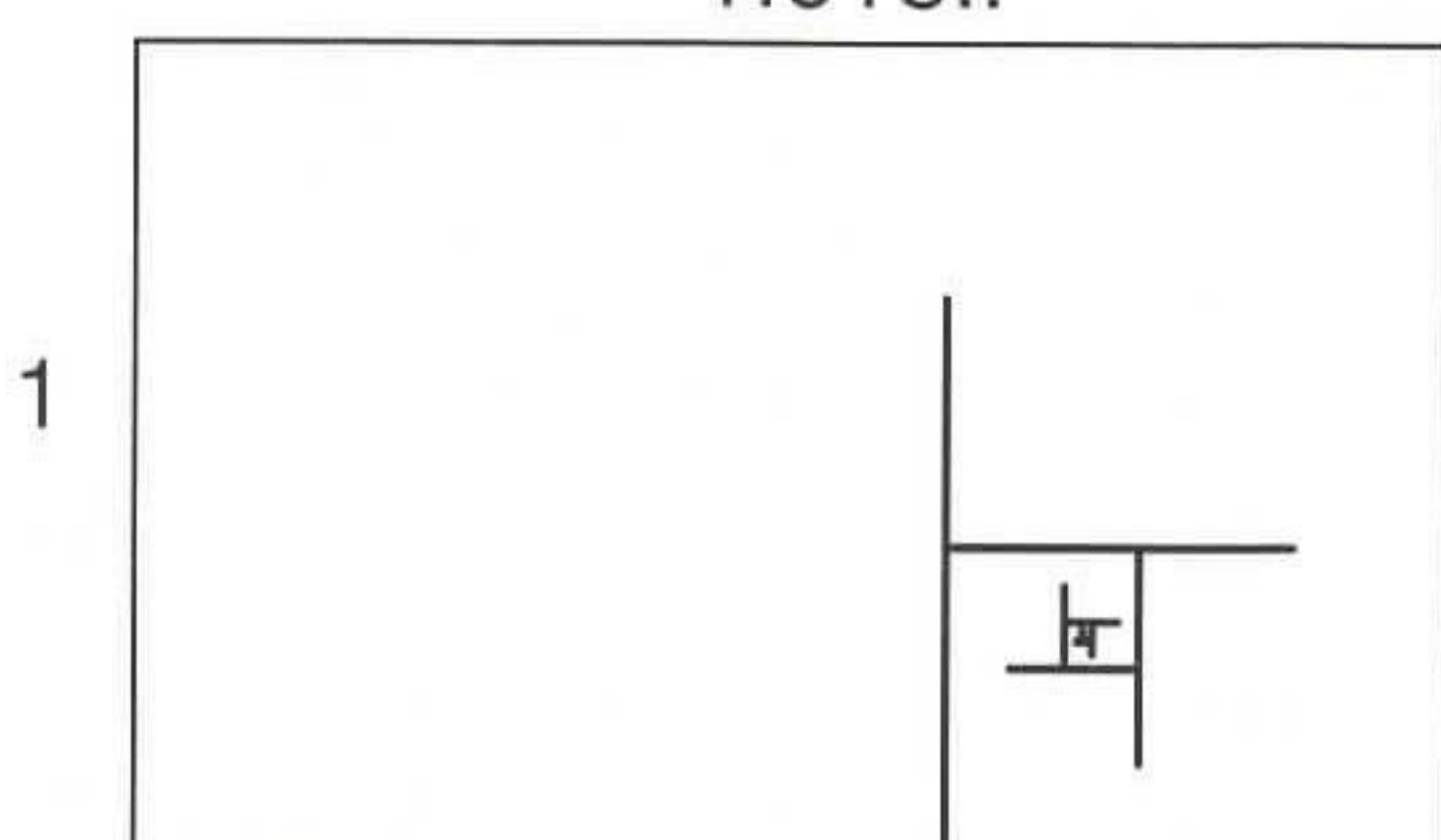
It is titled *Kotobuki* because it resembles to the kanji character for "kotobuki" (long life or celebration). I think it is also reminiscent of the chain of generations because of its infinite repetition, and that it is associated with cranes flying by Mount Fuji in a picture of Rosetsu Nagasawa.

Steps 1-4 constructs the golden ratio Φ (phi) = 1.618... = $(\sqrt{5} + 1) / 2$ by folding a square.

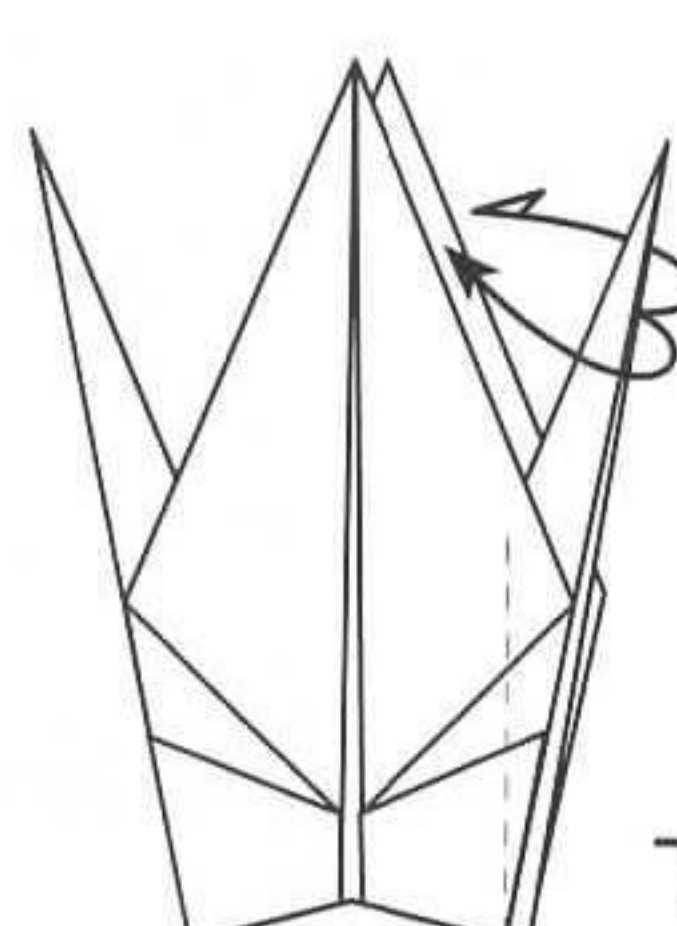
It is easier to measure with a ruler, though.



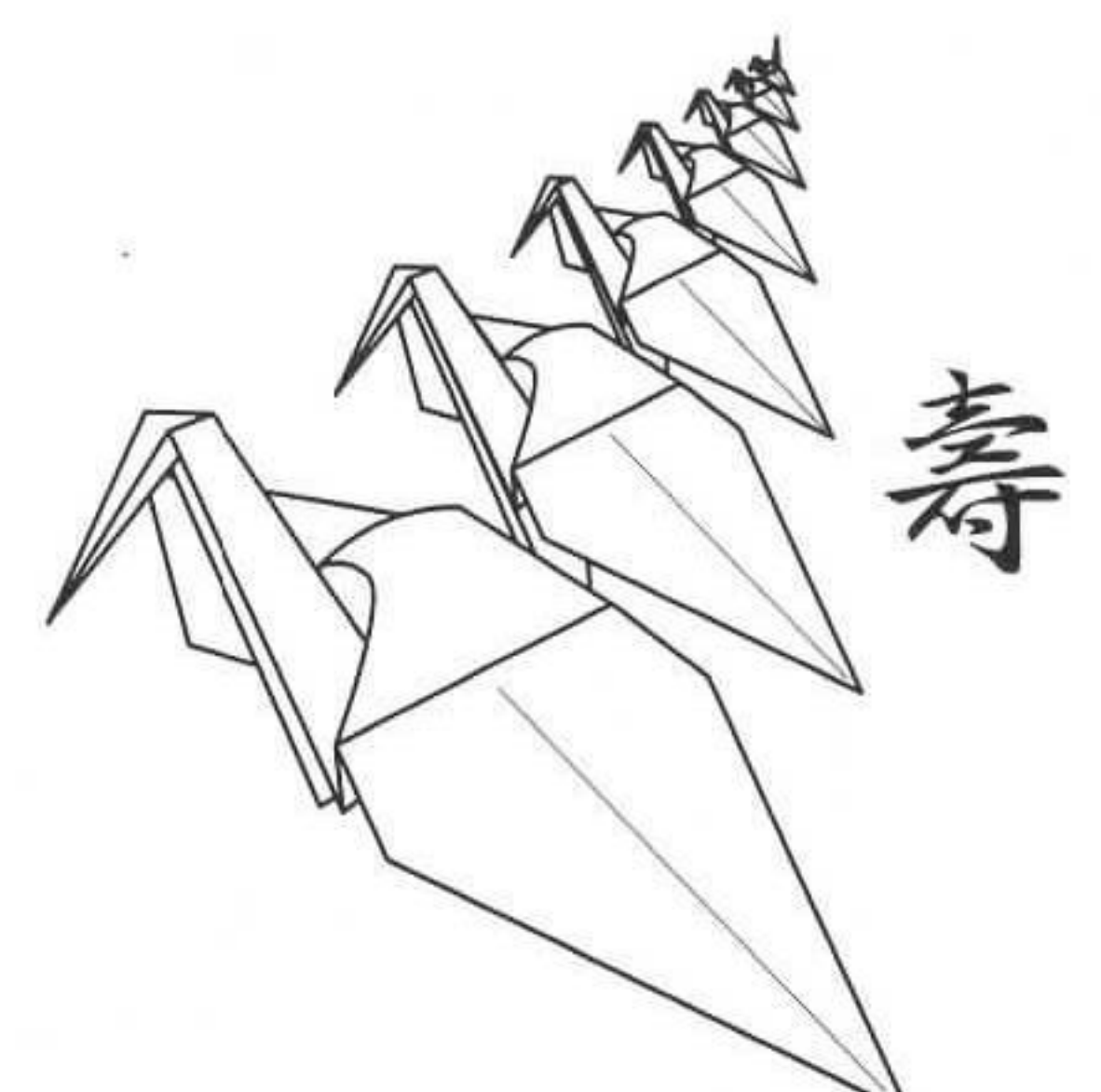
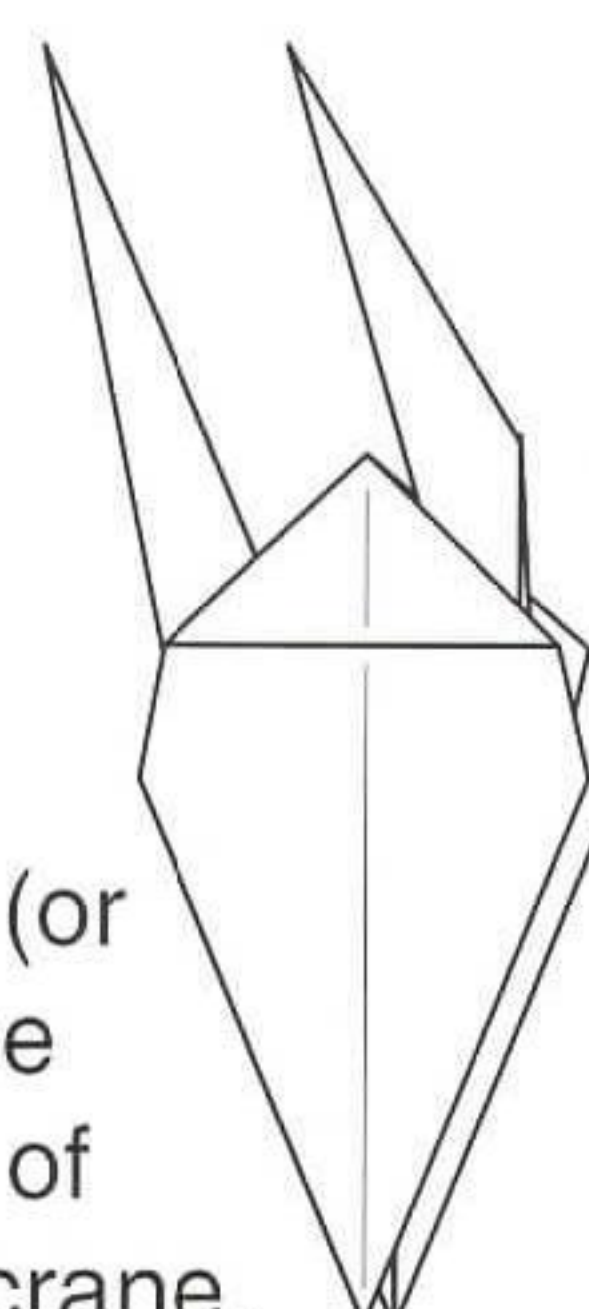
1.618..

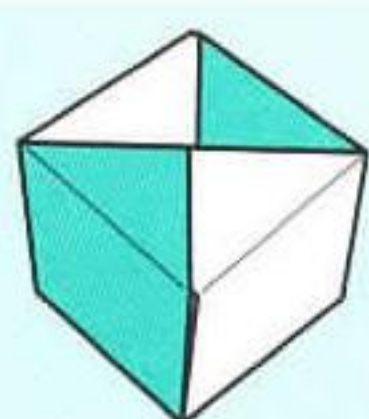


Cut up to the middle of the side of the smaller square.



The legs (or tail) will be the head of the next crane.

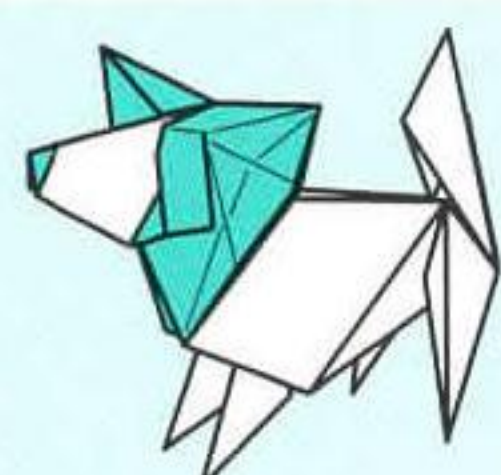




Gift Box

Theme: Iso-area

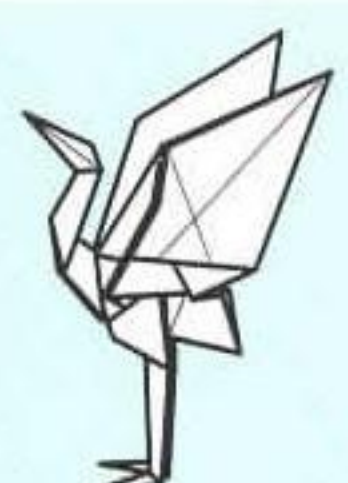
In this model, the front and back sides of paper are folded almost identically.



Papillon

Theme: Composition of points

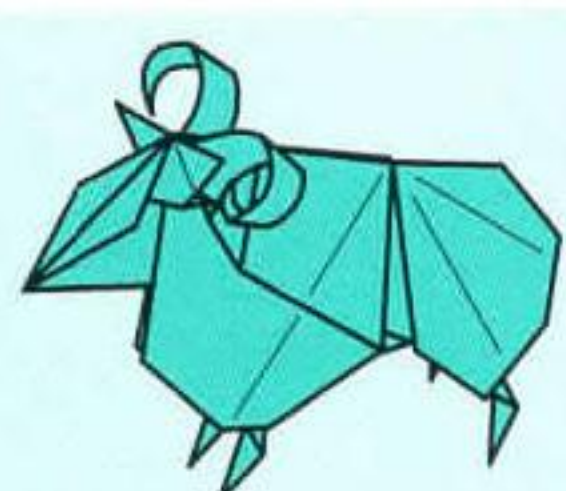
Compares the composition of points with that of *Wild Boar* to show the basics of technical folding and origami design.



Standing Crane

Theme: Technical folding

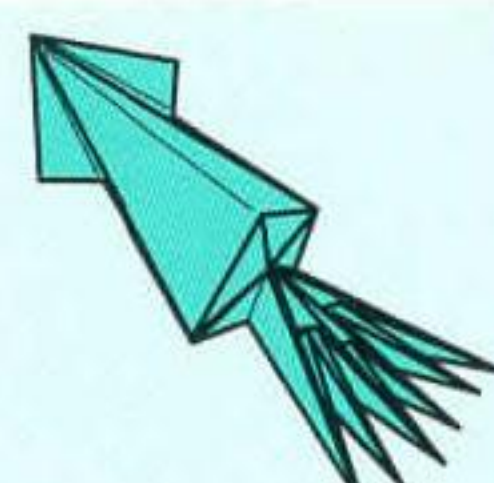
Explains technical folding from a practical point of view by analyzing the crease pattern of this model.



Sheep

Theme: Why from a square?

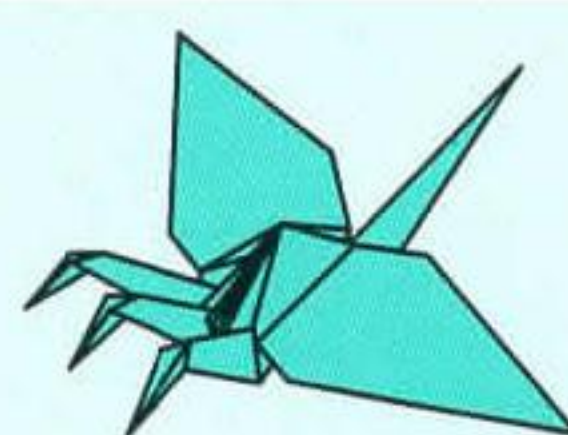
Ponders about origami design derived from a square shape by the crease pattern examination.



Squid

Theme: Axis of symmetry

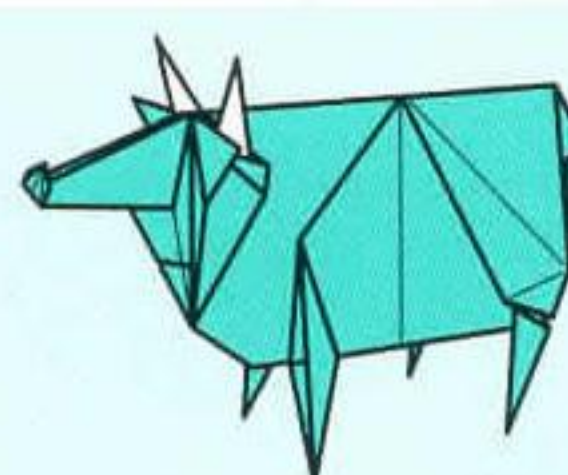
Examines two types of axis of symmetry of the square, i.e. diagonal and parallel lines.



Three-headed Crane

Theme: Technical folding; Preparation

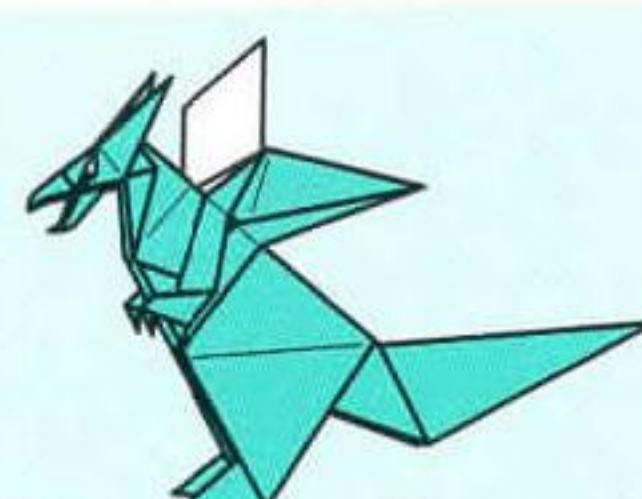
Explains how to construct a crease pattern from a sketch of branches. Also explains the idea of preparation.



Cow

Theme: Pig base

Explains features of the Pig base and their importance as the basics of technical folding.



Western Dragon

Theme: Y-pattern

An example of model that has many instances of Y-shaped crease pattern.

Chapter 4

Intermediate Models

"Everything should be made as simple as possible, but no simpler."

Albert Einstein



Horse

Theme: Geometric construction

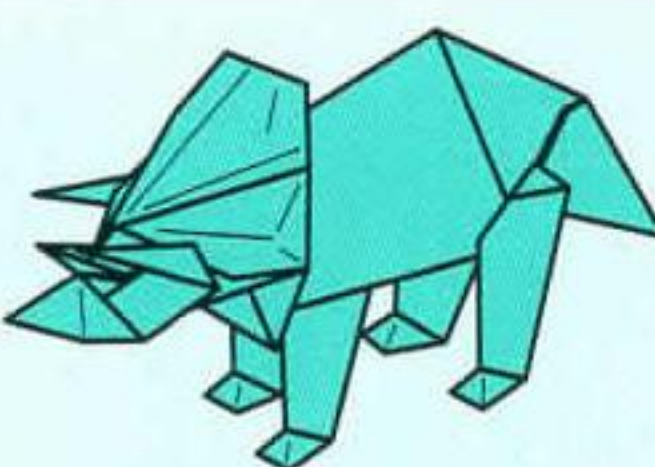
Shows that paper-folding can be used to replace a straight-edge and compass in folding landmarks.



Rabbit

Theme: Solid body

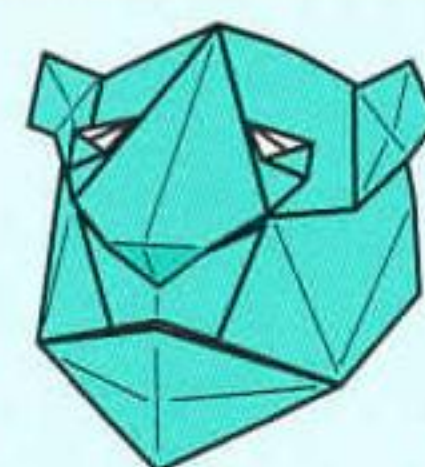
Illustrates some methods of making three-dimensional origami models.



Triceratops

Theme: Open-back, Open-belly

Explains the notion of open-back and open-belly as one of the origami design styles.



Tiger Mask

Theme: Polyhedron

Explains a basic technique to make three-dimensional models using polyhedra.



Devil Mask

Theme: Variation

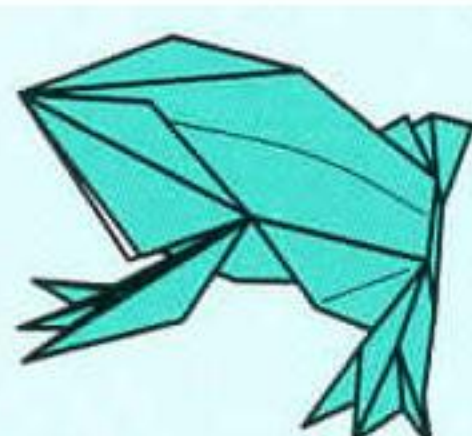
As a variation of *Tiger Mask*, this model provides a typical example of how one model is modified into another.



Penguin

Theme: 15 degrees; Cone

This model is based on 15° angle or one sixth of the right angle. Also examines curved surfaces that can be made from a flat surface.



Frog

Theme: Approximation

This model makes use of the approximation $5\sqrt{2}-3 \div 4$. Explains the difference between origami and pure geometry, where lines have no width and planes have no thickness.



Pyramid

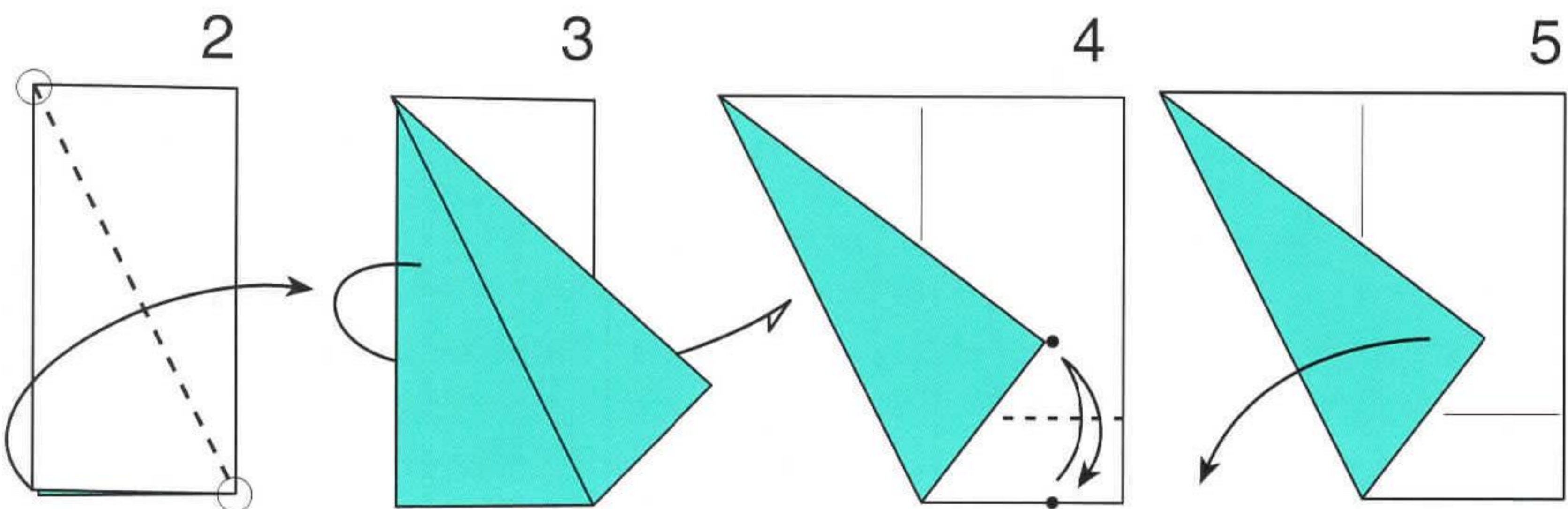
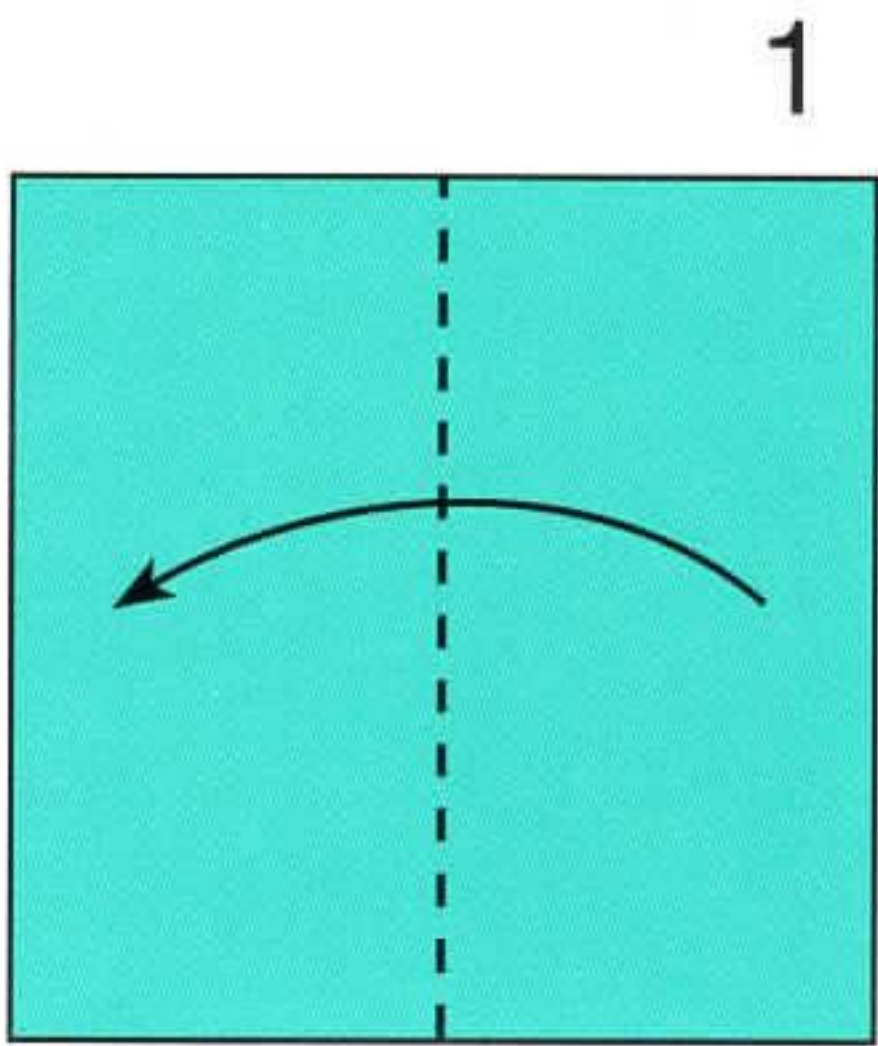
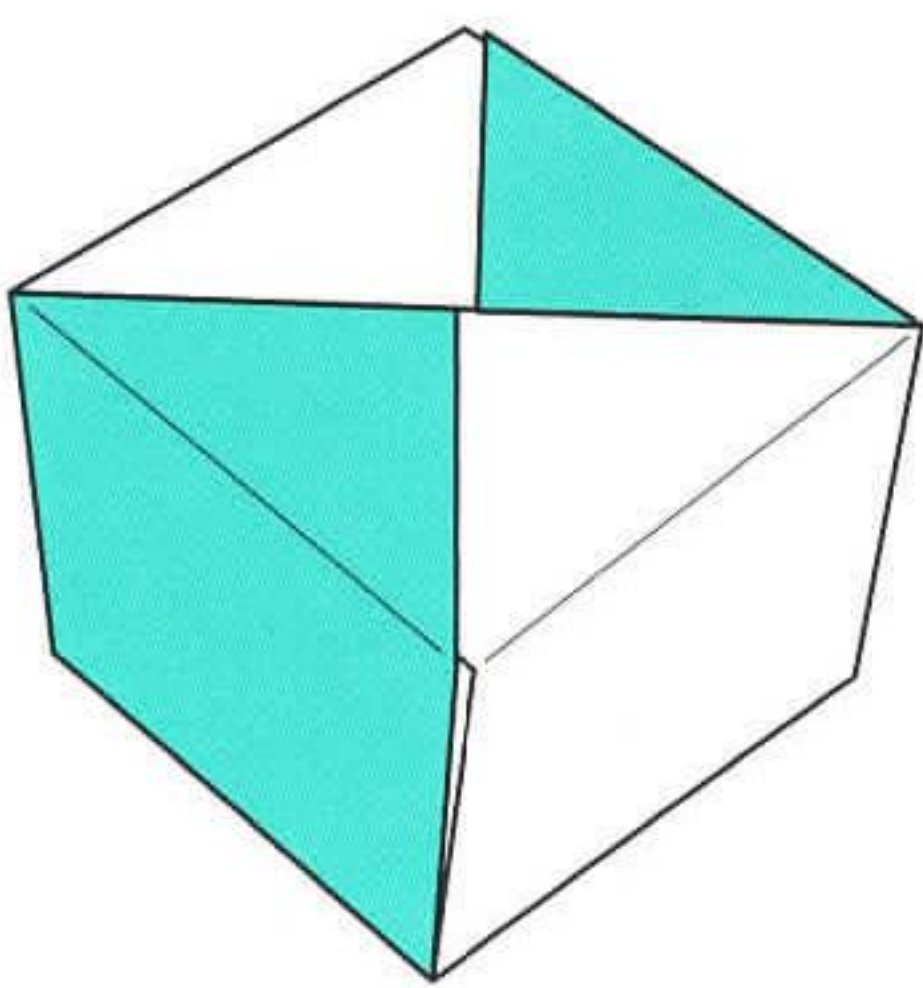
Theme: Infinite folding

An example of model that can be folded in the same pattern infinitely until the physical limitations of the paper.

Gift Box

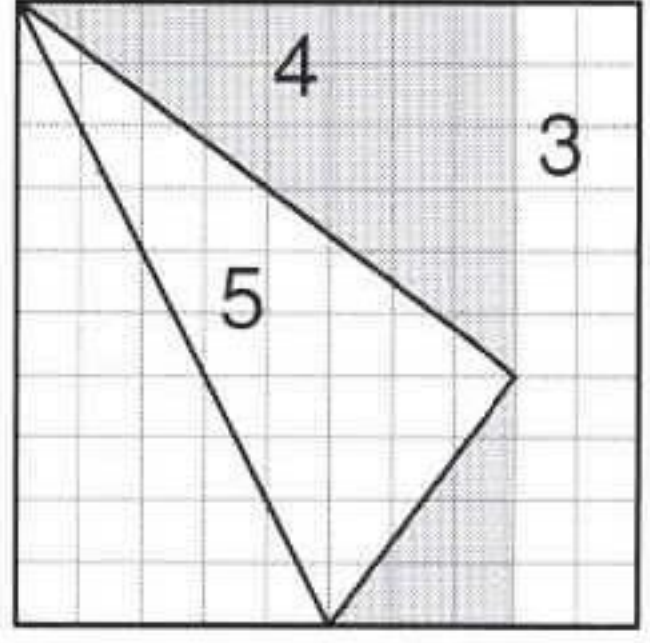
Theme: Iso-area

Fold using 6" (15 cm) origami paper.

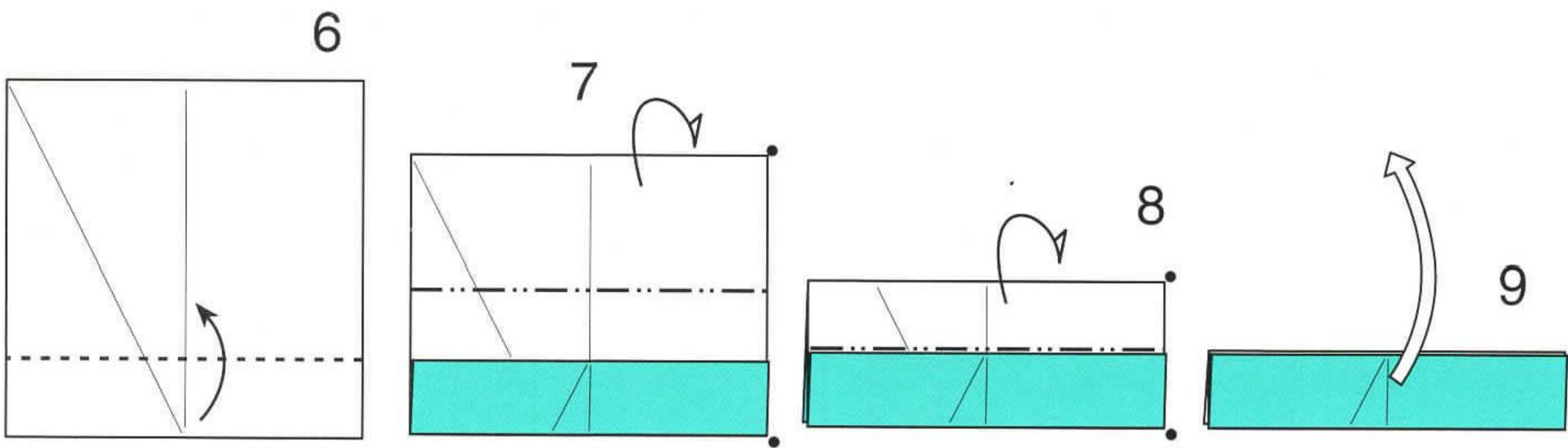


Pinch at the edge.

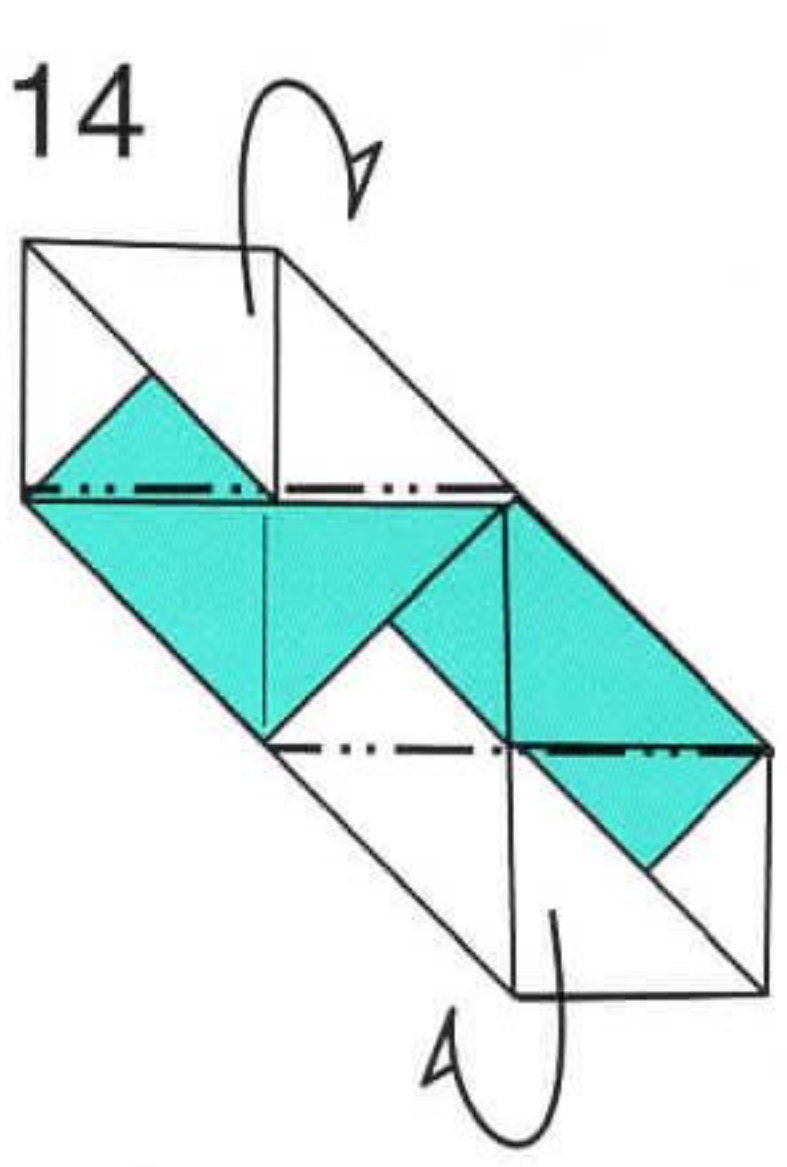
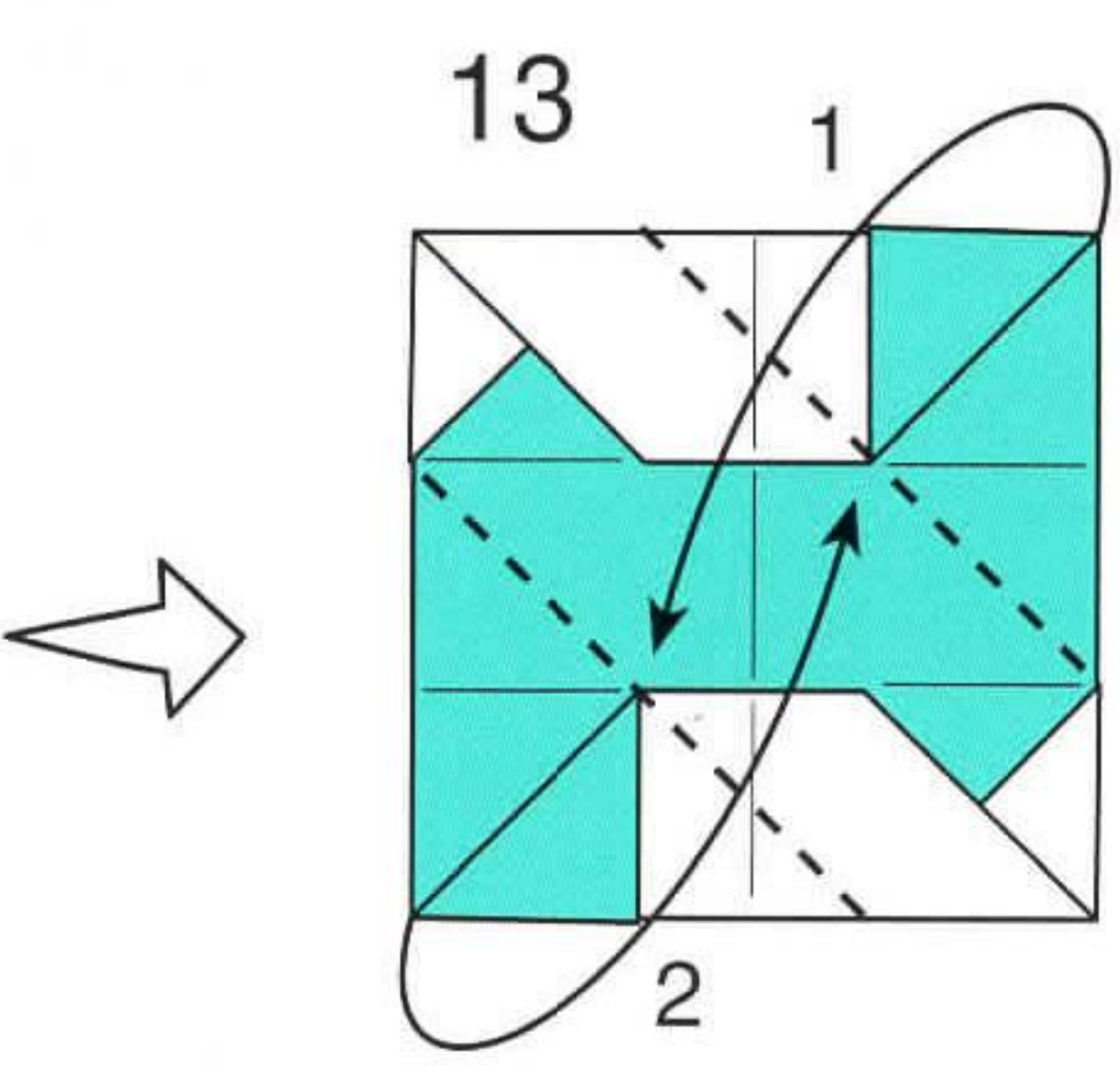
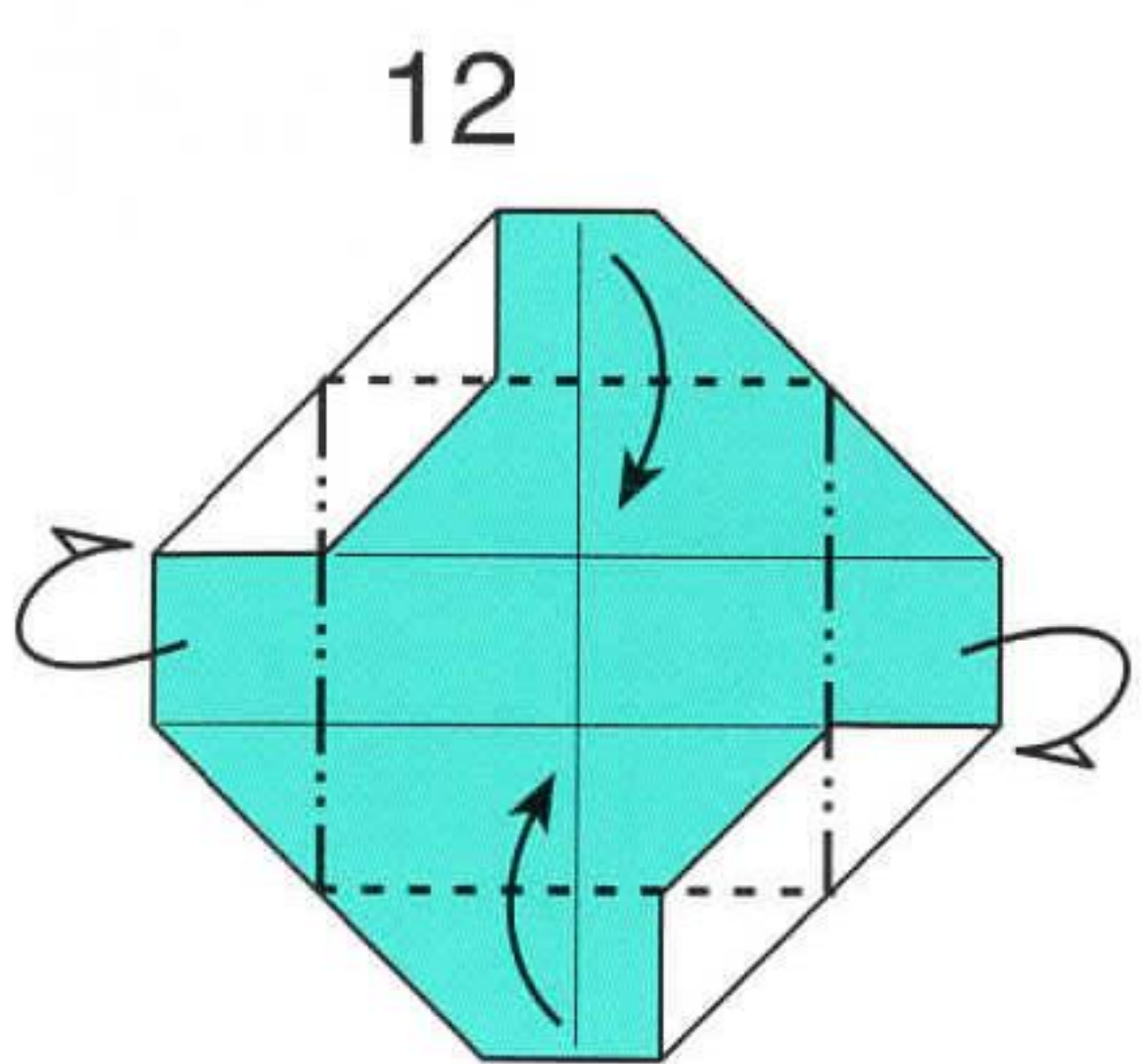
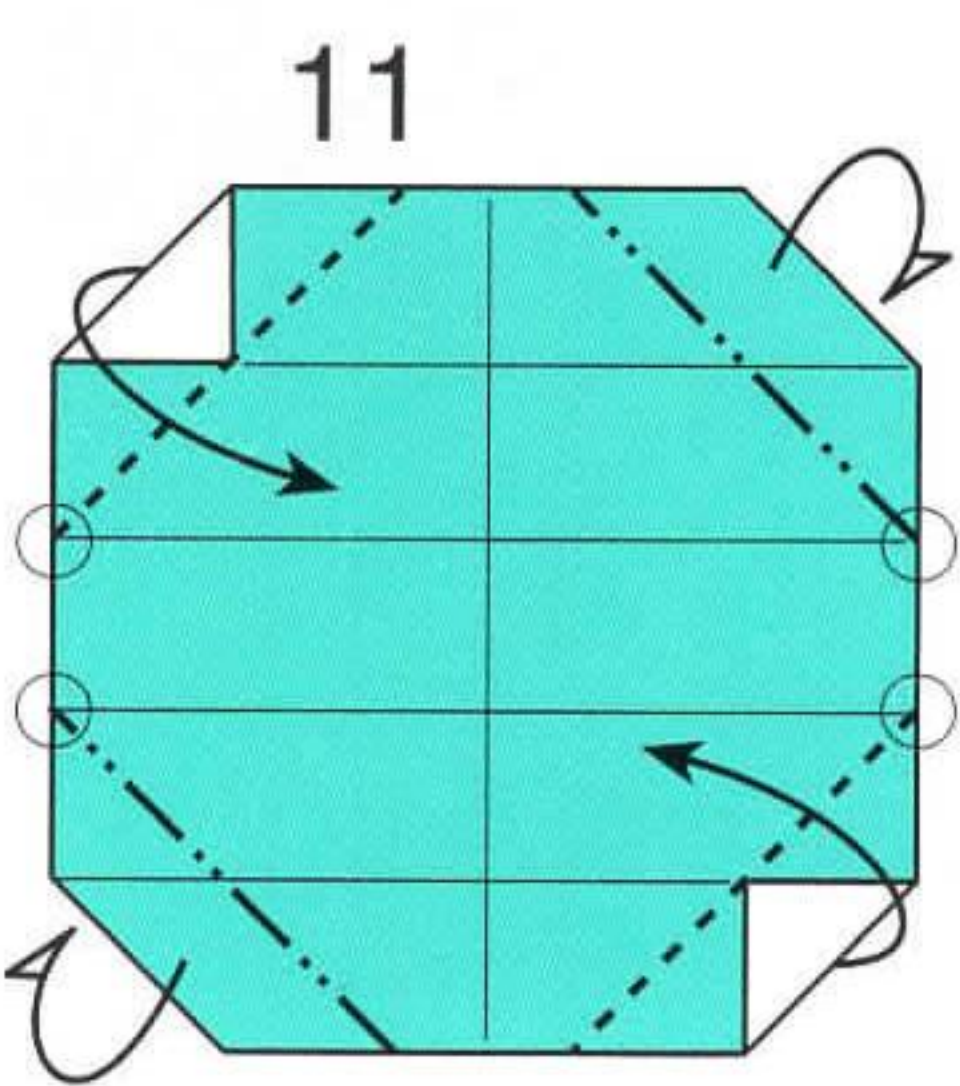
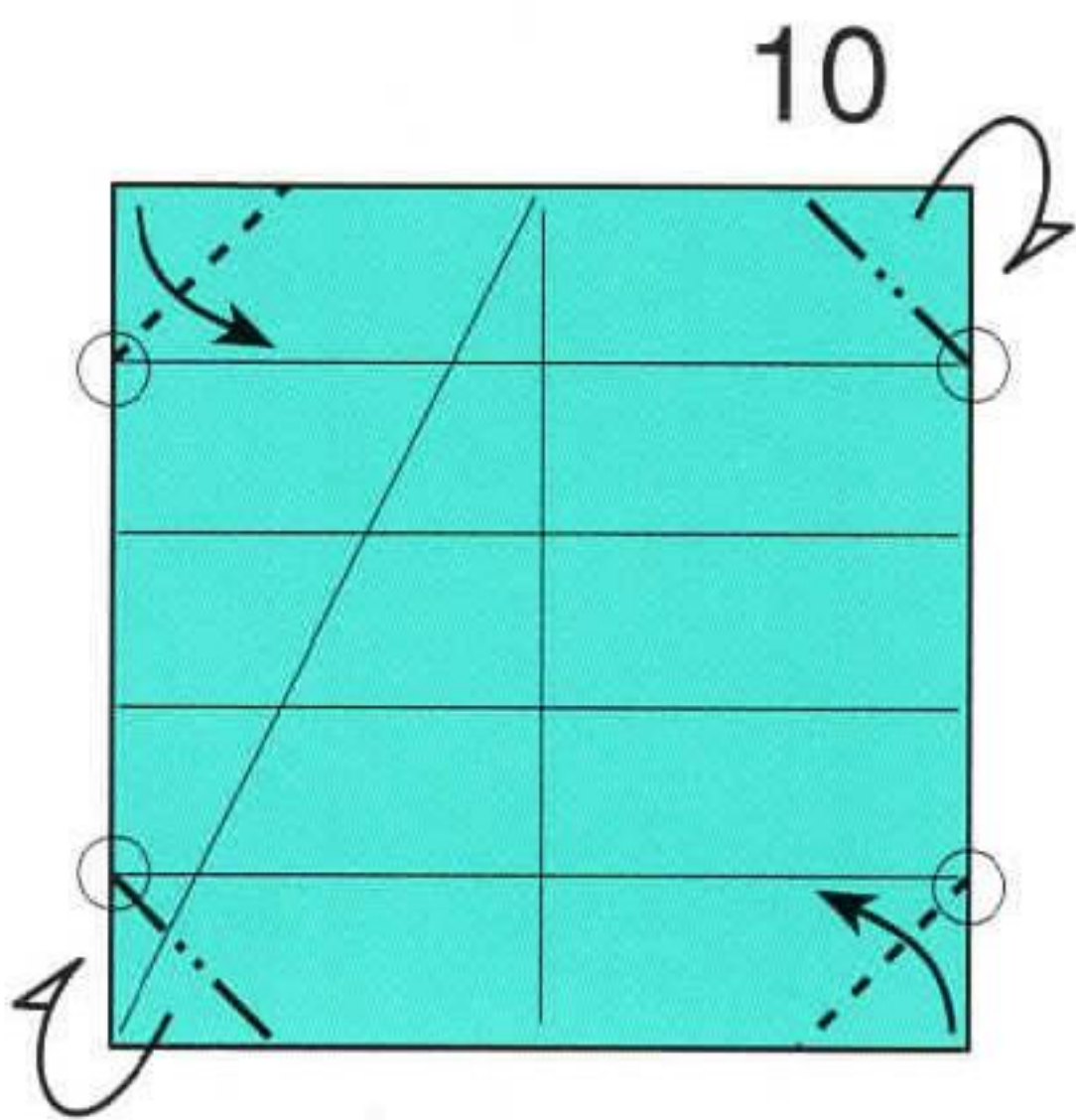
Steps 1-5 are the sequence to accurately divide a side into five. You can confirm it in steps 6-8.



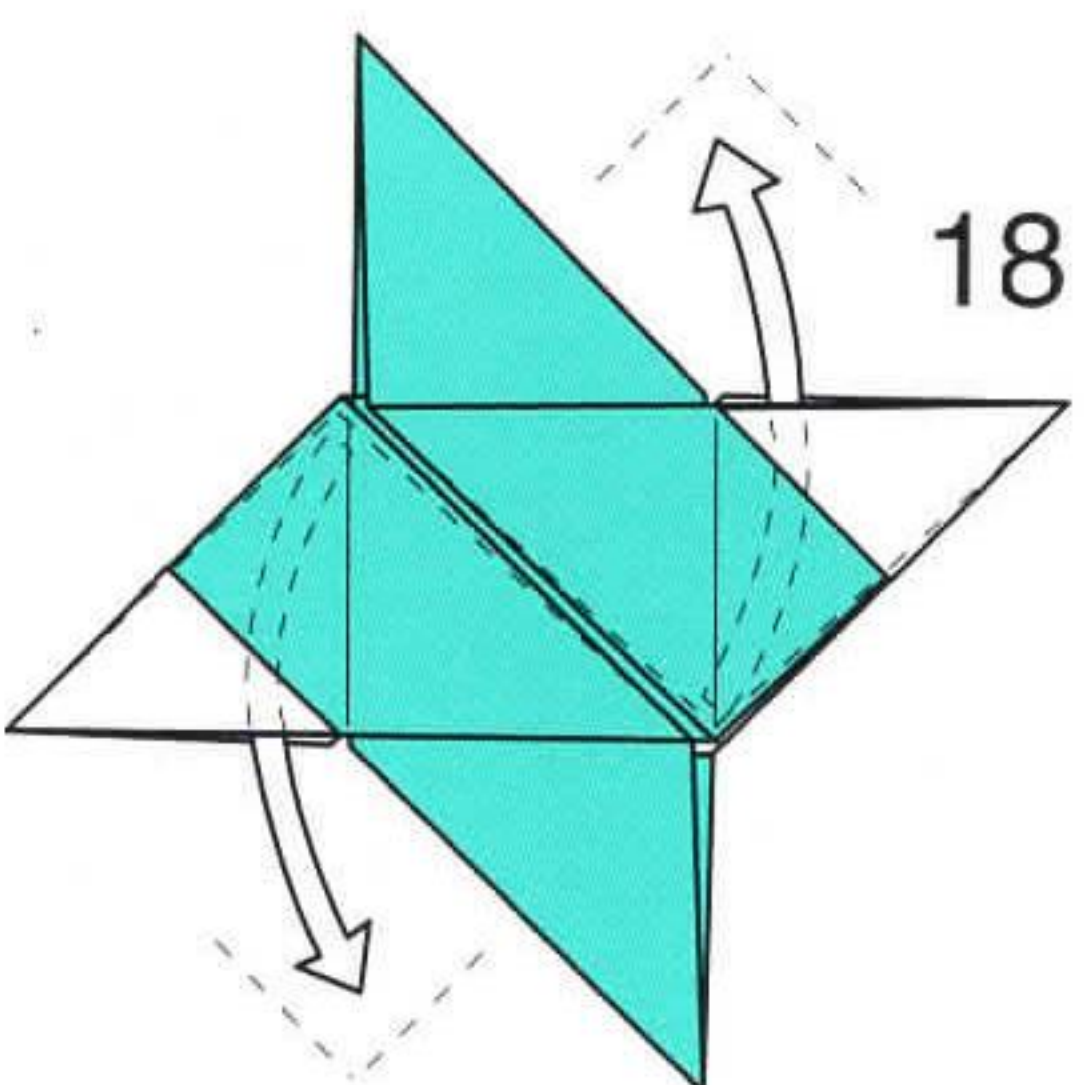
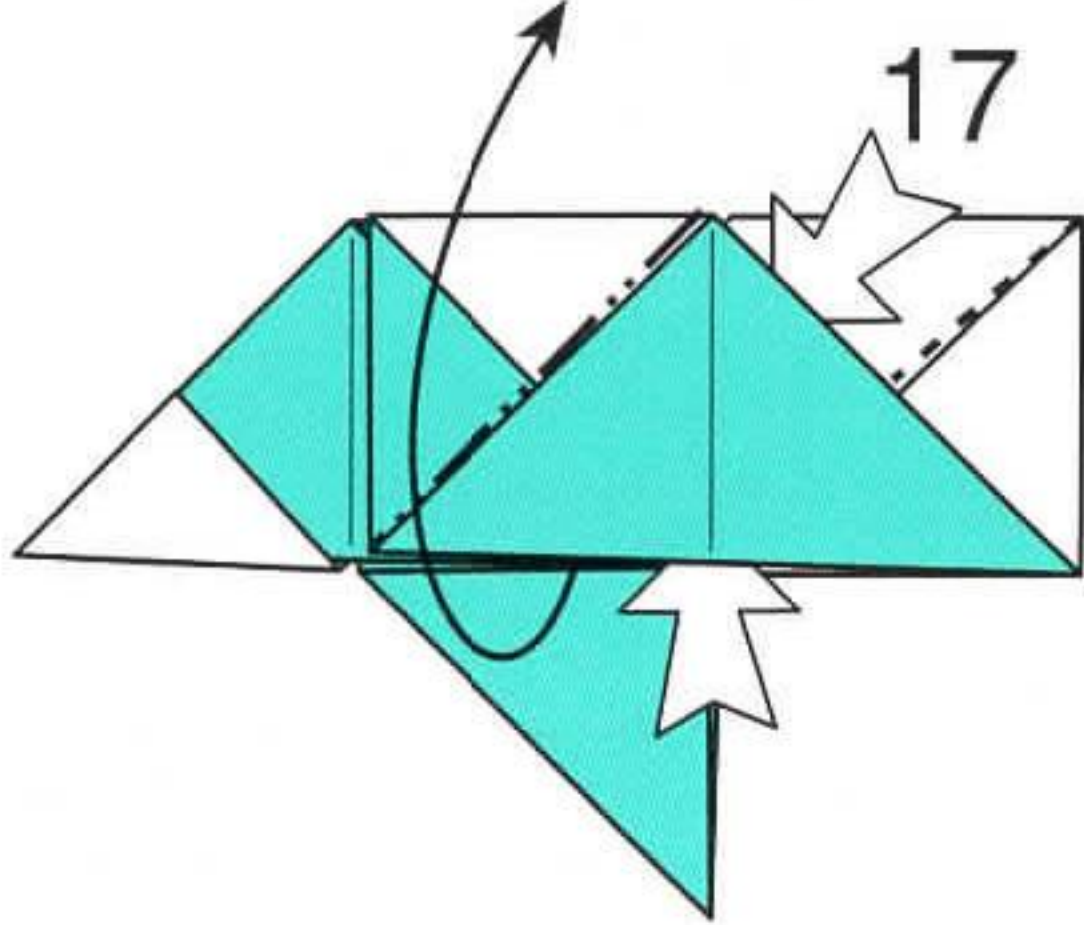
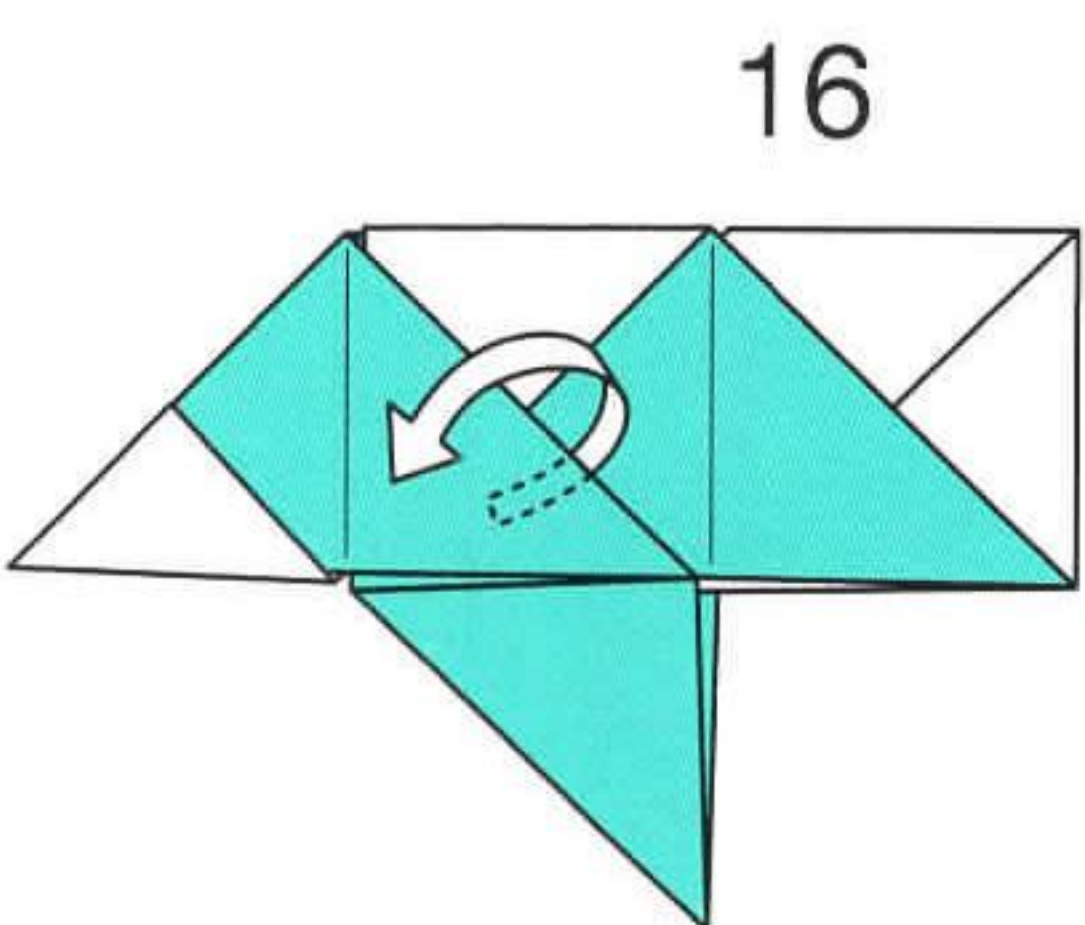
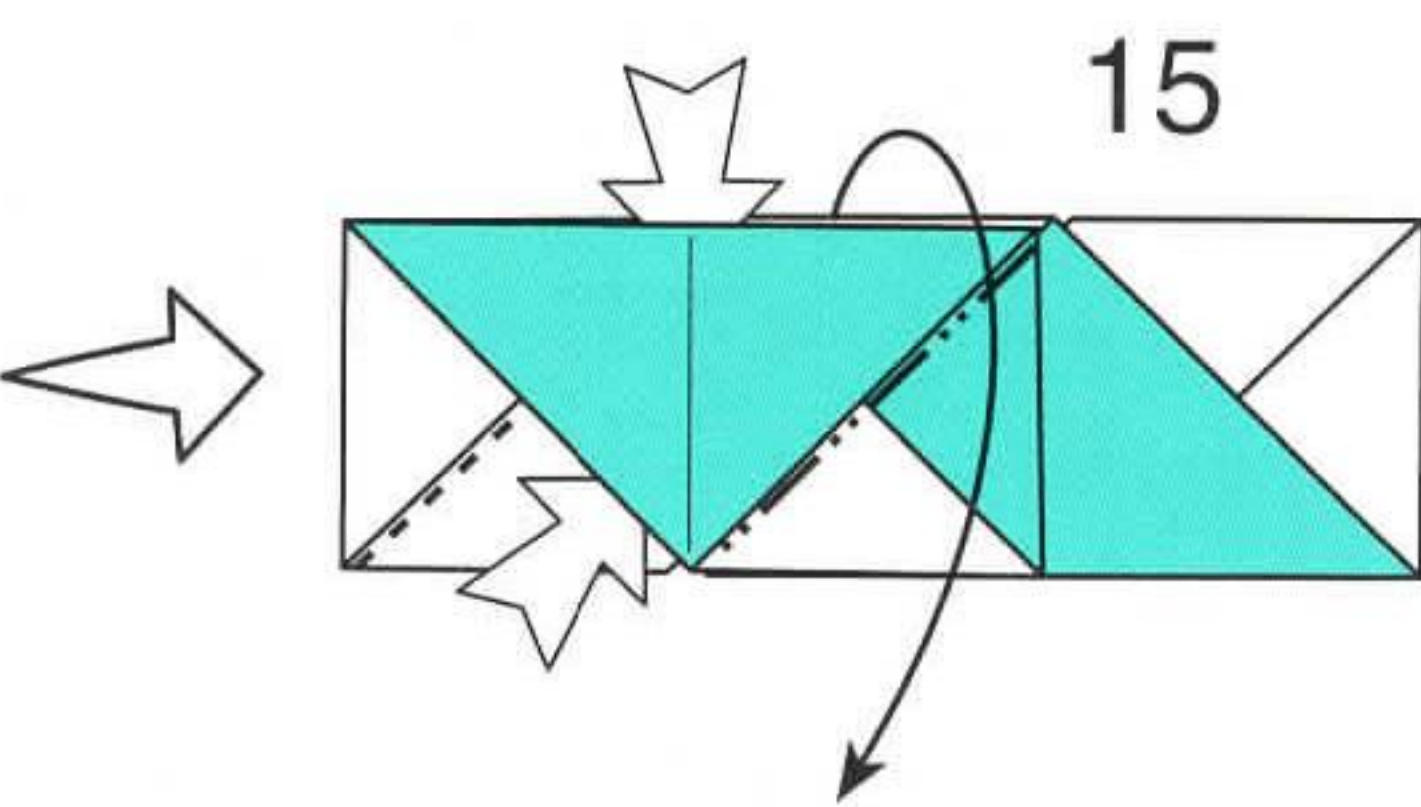
The key to prove this construction. The ratio of the sides of two gray triangles is 3 : 4 : 5.

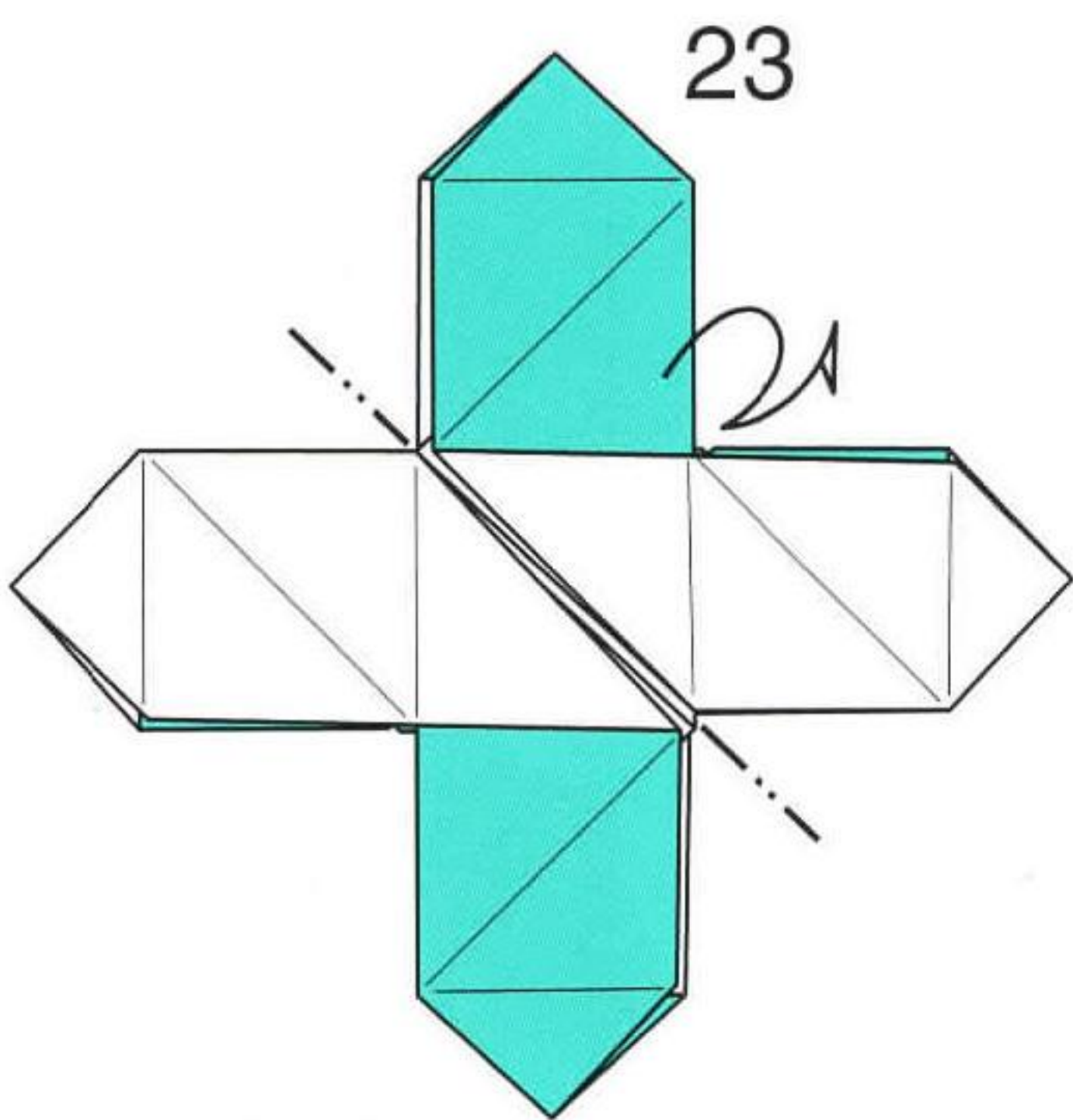
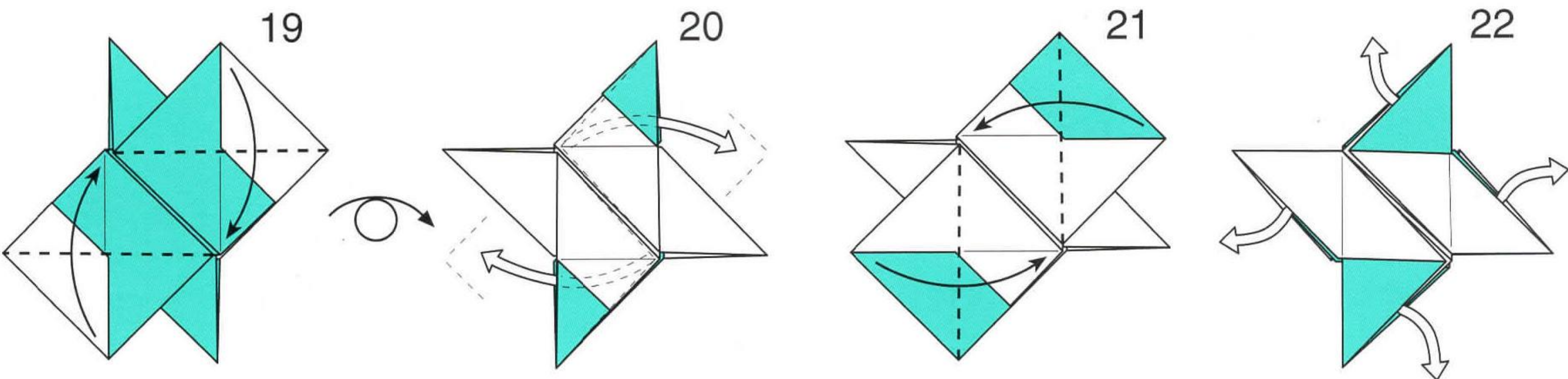


Extend the crease made in step 4.



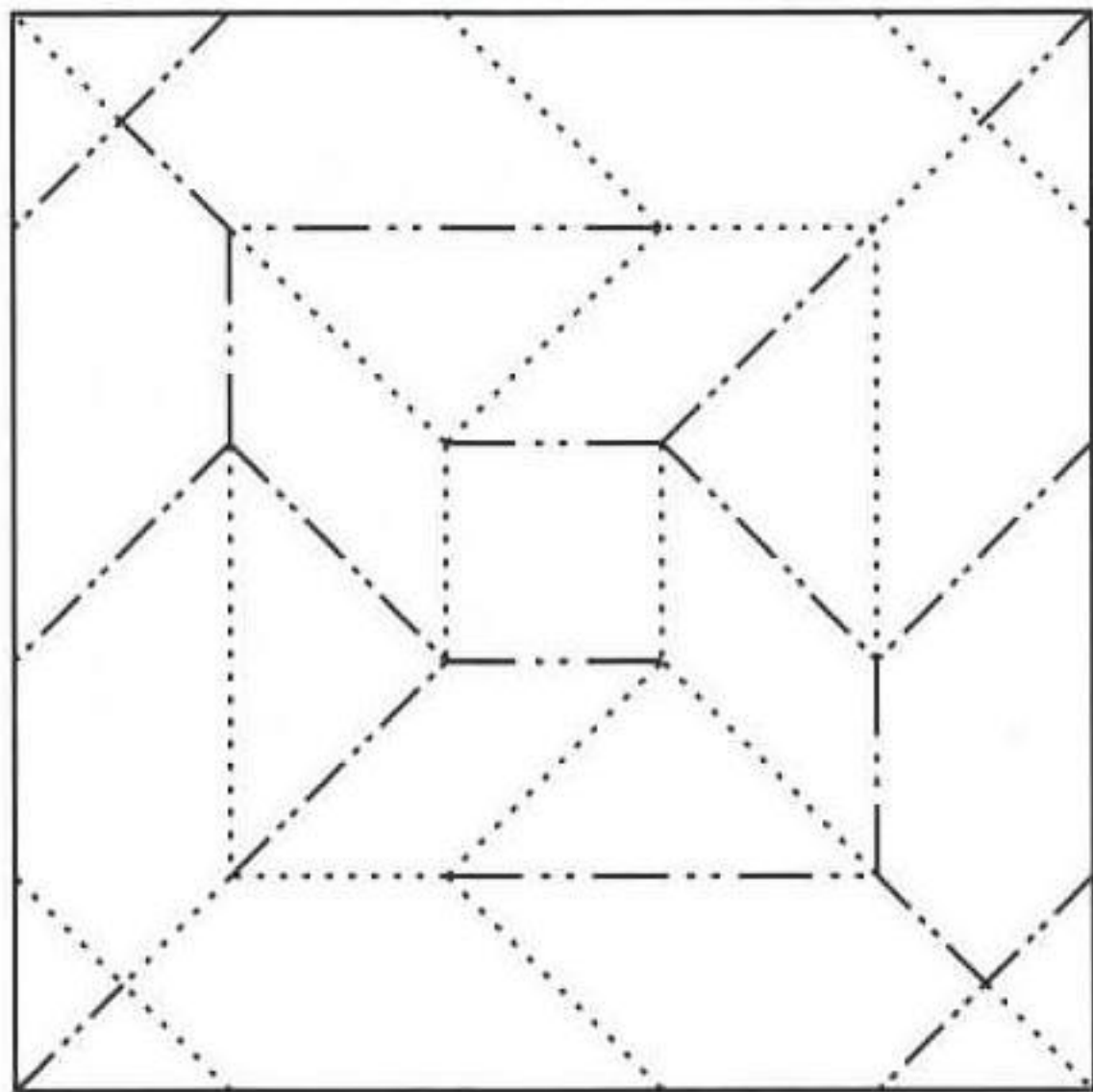
Fold according to the sequence indicated.



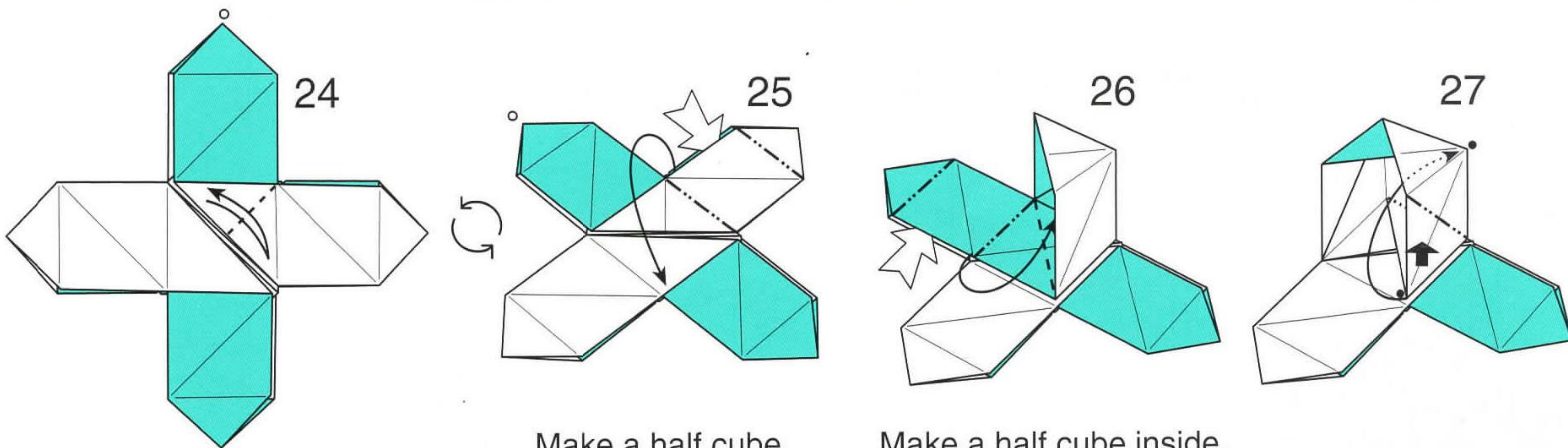


Iso-area

The model is iso-area in steps 18 and 23. In other words, the creases are identical at the front and back sides of paper. The notion of iso-area folding was introduced by Toshikazu Kawasaki with his *Iso-area Cube* and some other examples. It corresponds to **rotoinversion symmetry** in crystallography. The word “rotoinversion” comes from “rotation and inversion.” Note that inversion corresponds in origami to reversing mountain and valley folds and rotating 180°. This model is also an example of **twist folding**, coined by Shuzo Fujimoto.

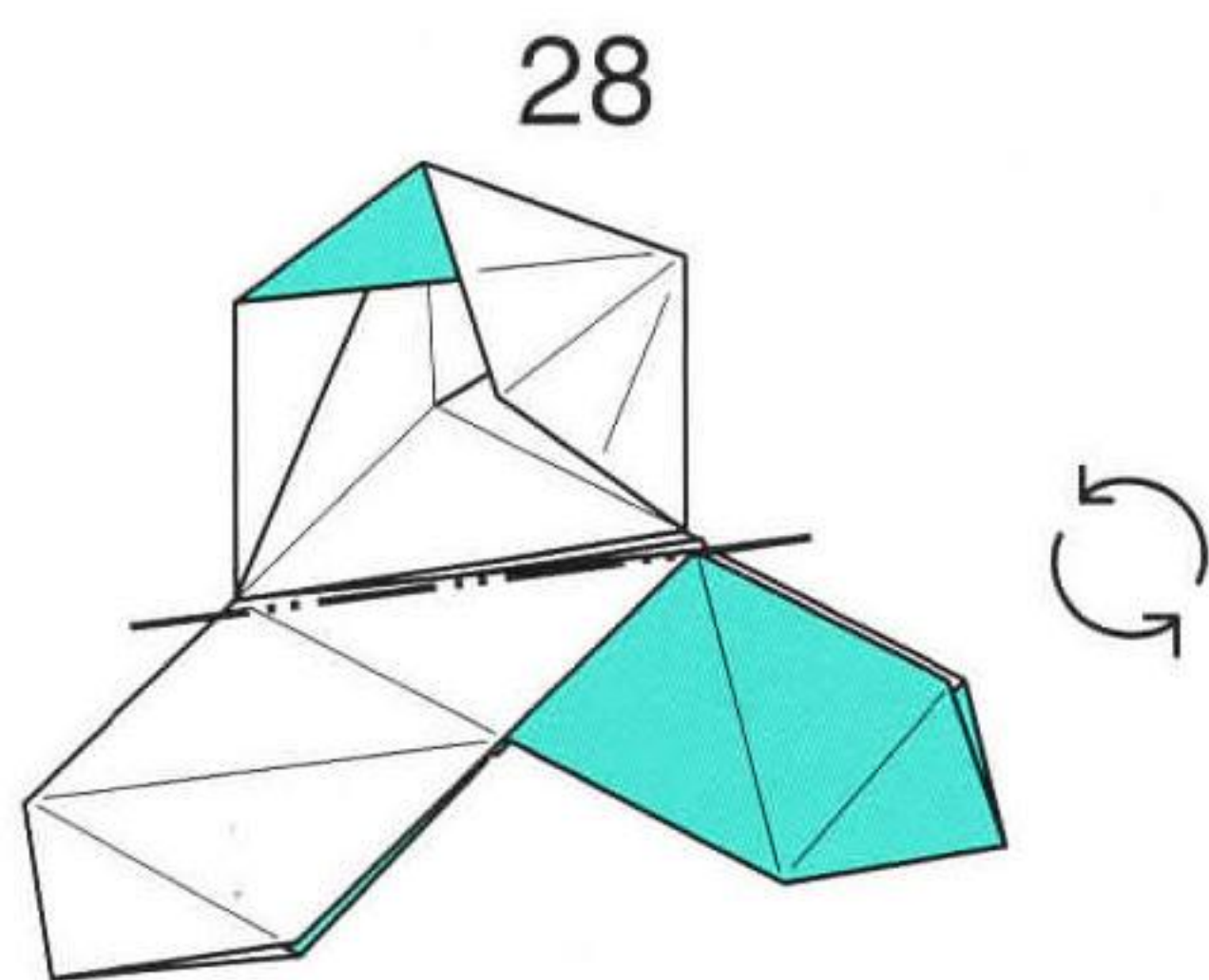


The crease pattern on step 23 will be the same if you reverse mountain and valley creases and rotate.

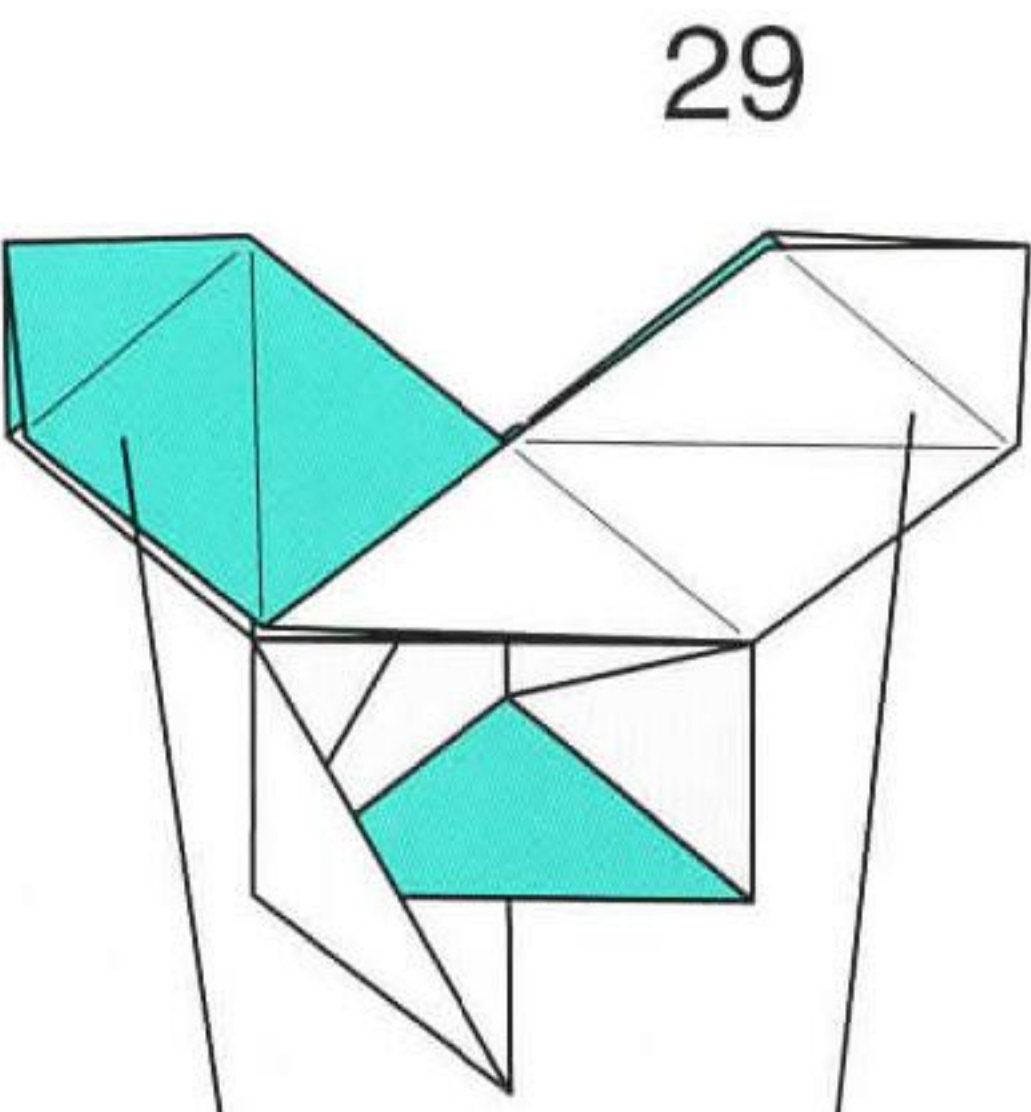


Make a half cube.

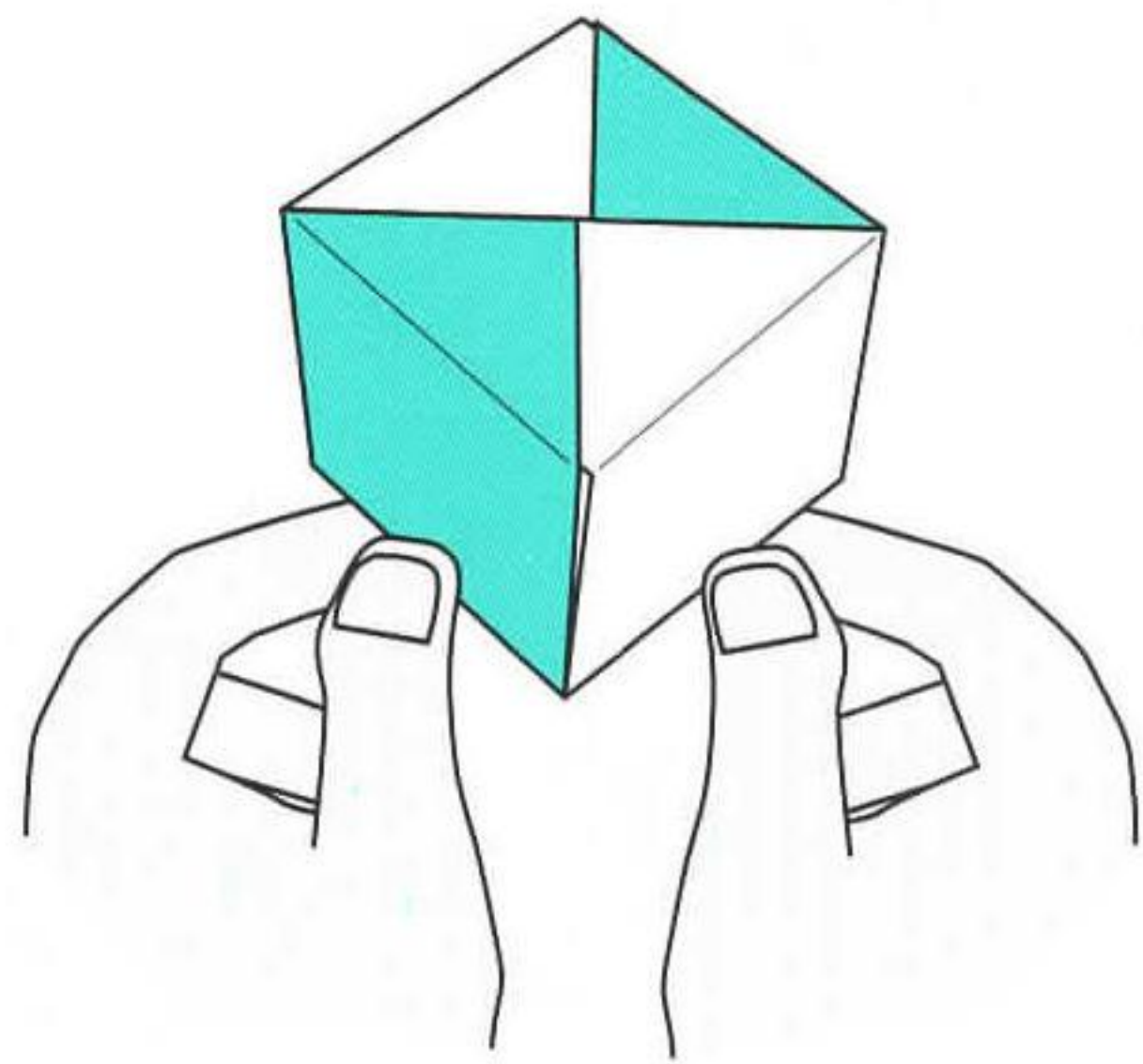
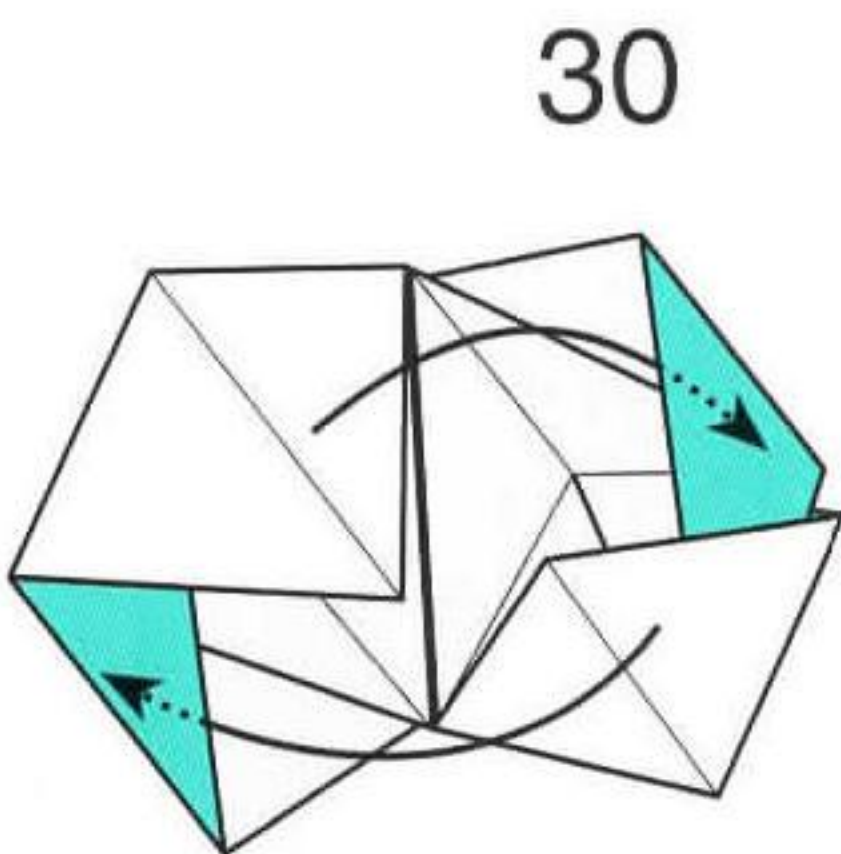
Make a half cube inside.



Mountain-fold on the center



Repeat steps 25-27.

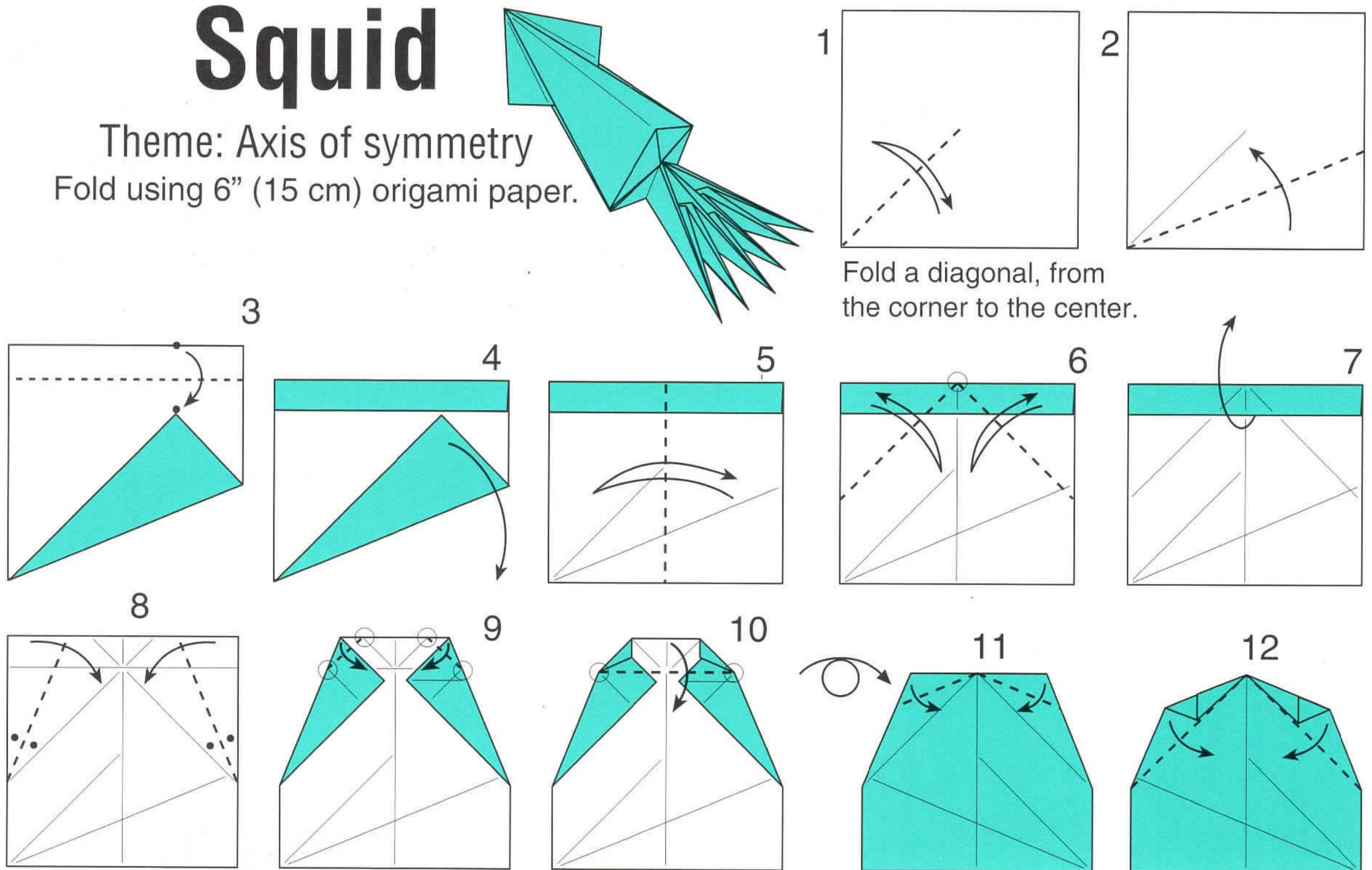
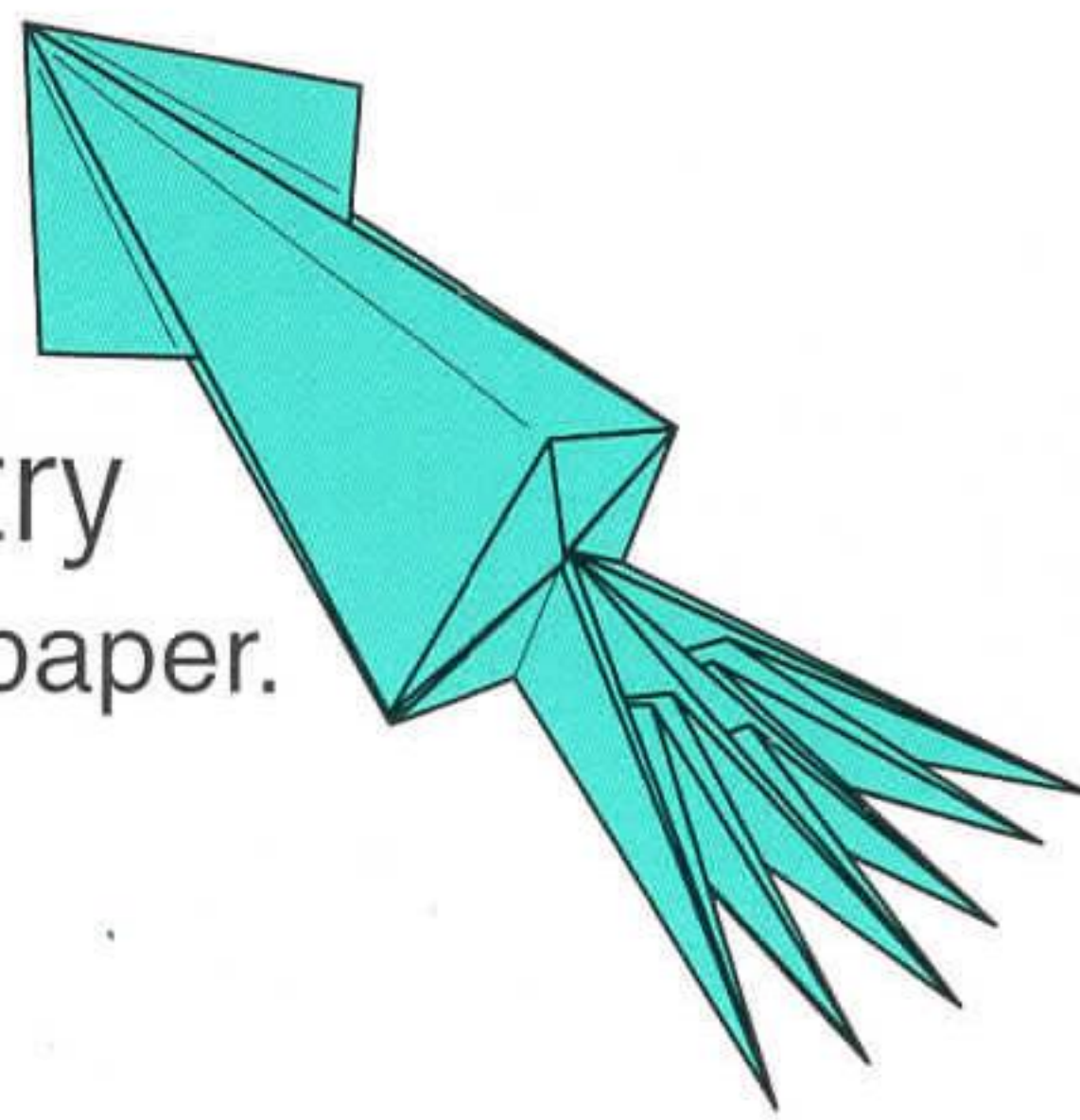


To finish, pinch firmly all eight edges so that the cube does not open.

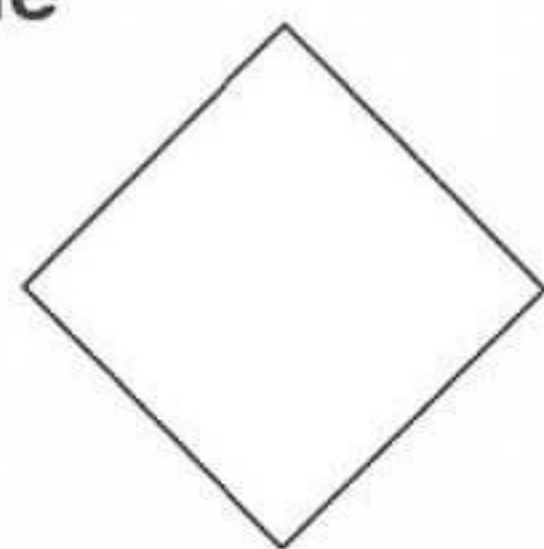
Squid

Theme: Axis of symmetry

Fold using 6" (15 cm) origami paper.



Axis of symmetry of the square



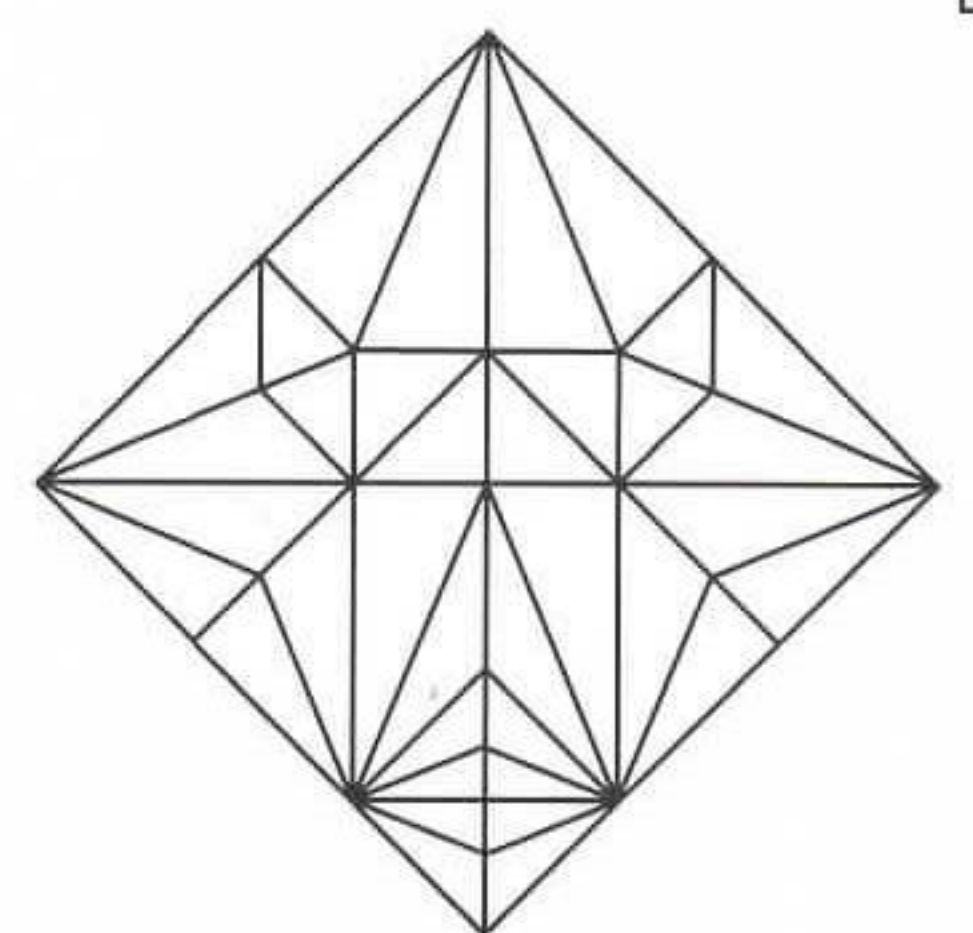
The square on the right looks larger, although they have the same area.

You may have seen the illusion created by the same square which looks different when placed "horizontally" or "diagonally." Not only the area but also the shape itself often looks different, to a point that the shape on the right is sometimes called diamond instead of square.

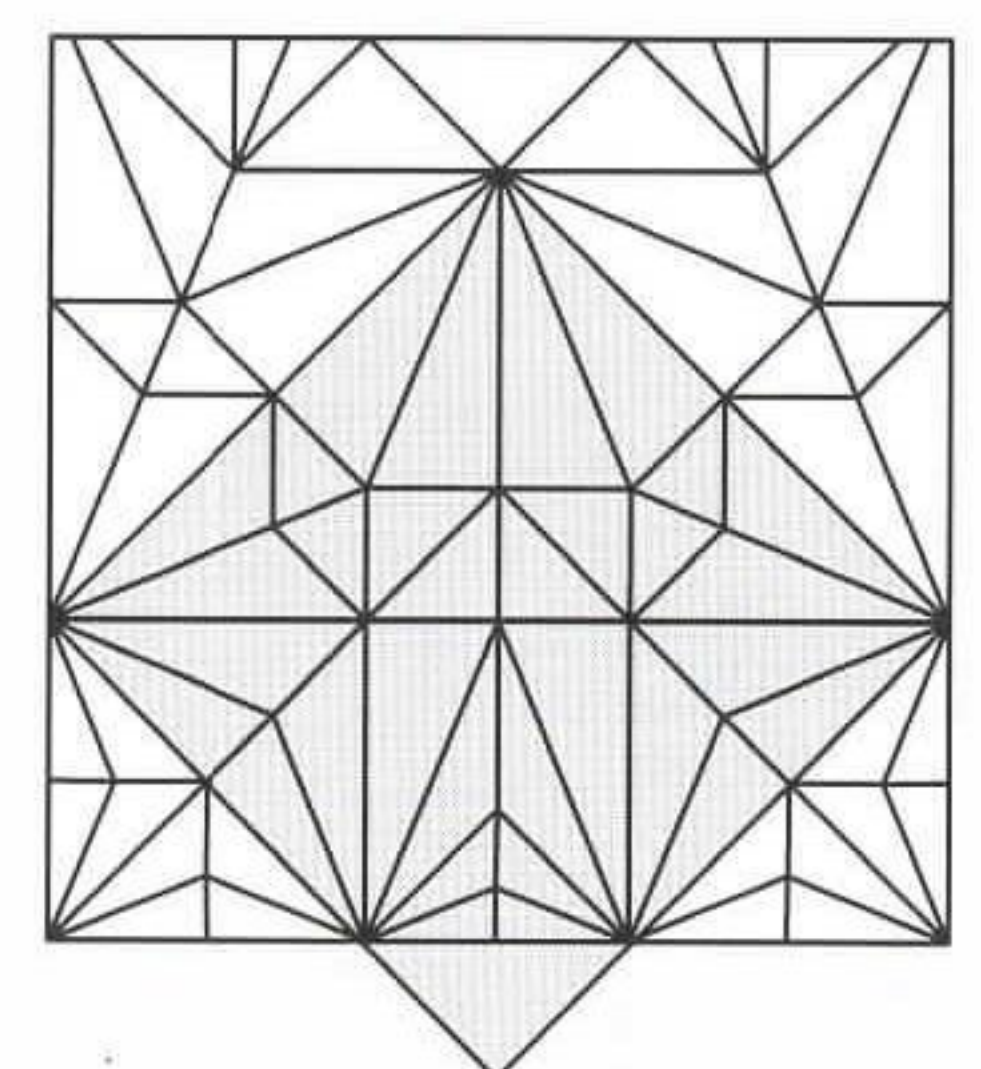
In other words, the square has two different facets. That is the reason for the general attraction of the use of the square for origami. When designing models, the first thing we decide is, in most cases, the axis of symmetry, which is usually either a diagonal line or a line parallel to the side. The decision is both annoying and enjoyable for designers. (I said "usually" because some models have asymmetric structures, as in *Snake*, or structures of rotation or rotoinversion symmetry, as in *Gift Box*.)

The notion of axis of symmetry is also useful when modifying existing models. One example is the use of the blintz fold as in *Elephant*, and this *Squid* is a derivative example of that.

First I designed *Carrot*, which is basically a pyramid with leaves. Since it also looked like a squid for me, I wanted to add fins to make it closer to a real squid. At the same time, I wanted to keep the crease pattern intact because it already was a high quality design. So I rotated it 45° and placed it in a larger square. Then I found a crease pattern that offered fins in the right position.

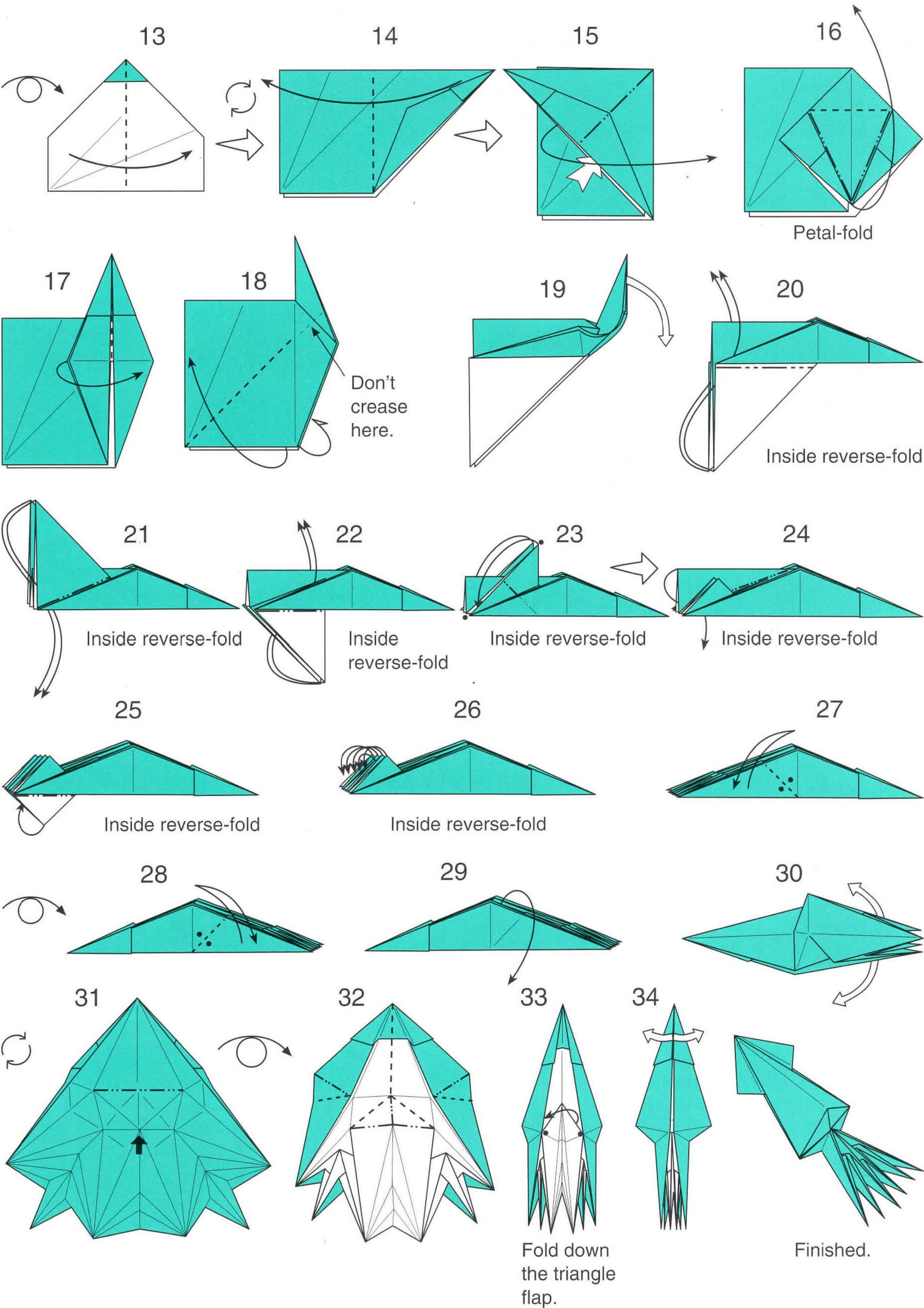


The crease pattern of *Carrot* (mountain and valley folds are not shown).



The crease pattern of *Squid* (mountain and valley folds are not shown).

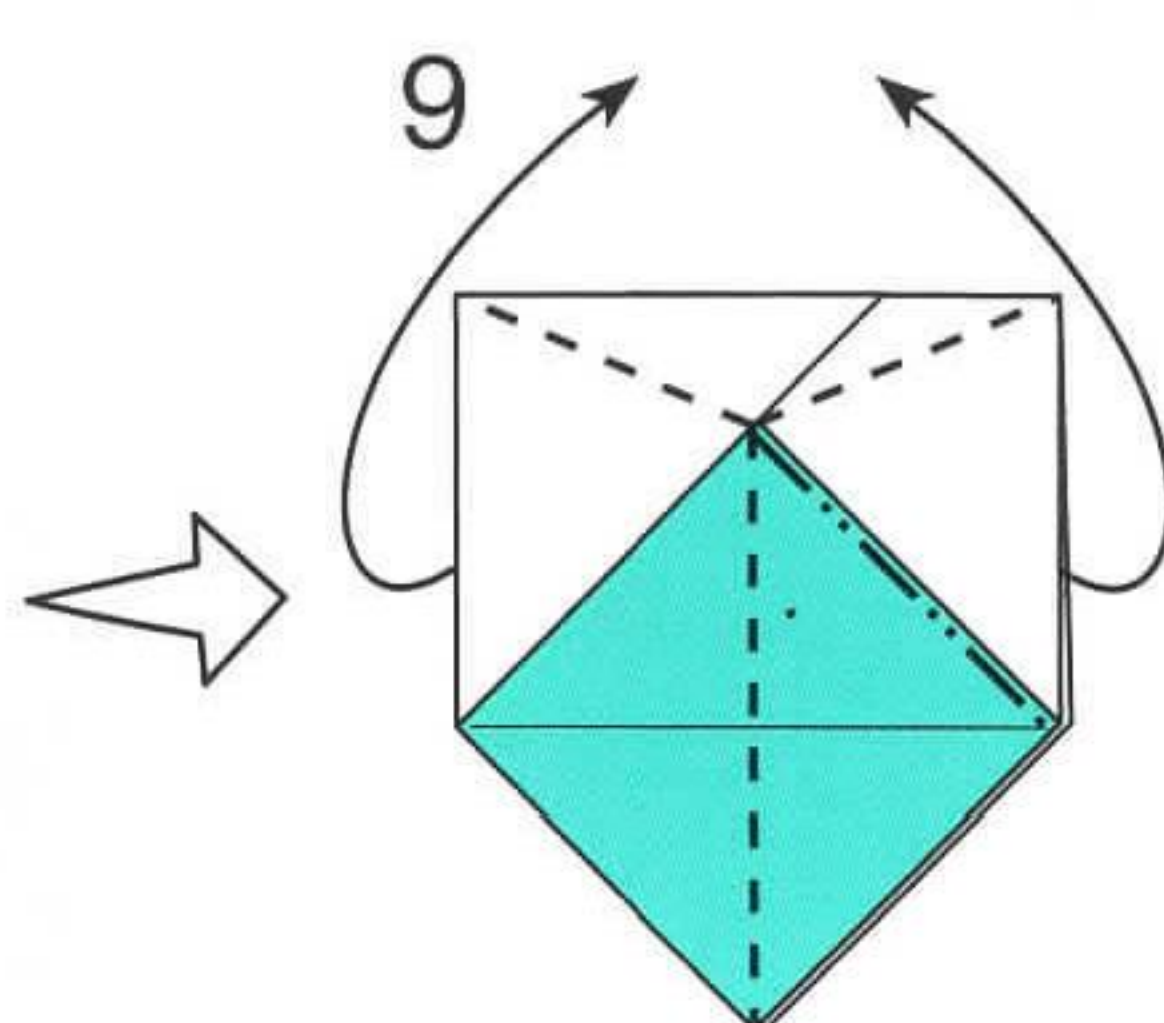
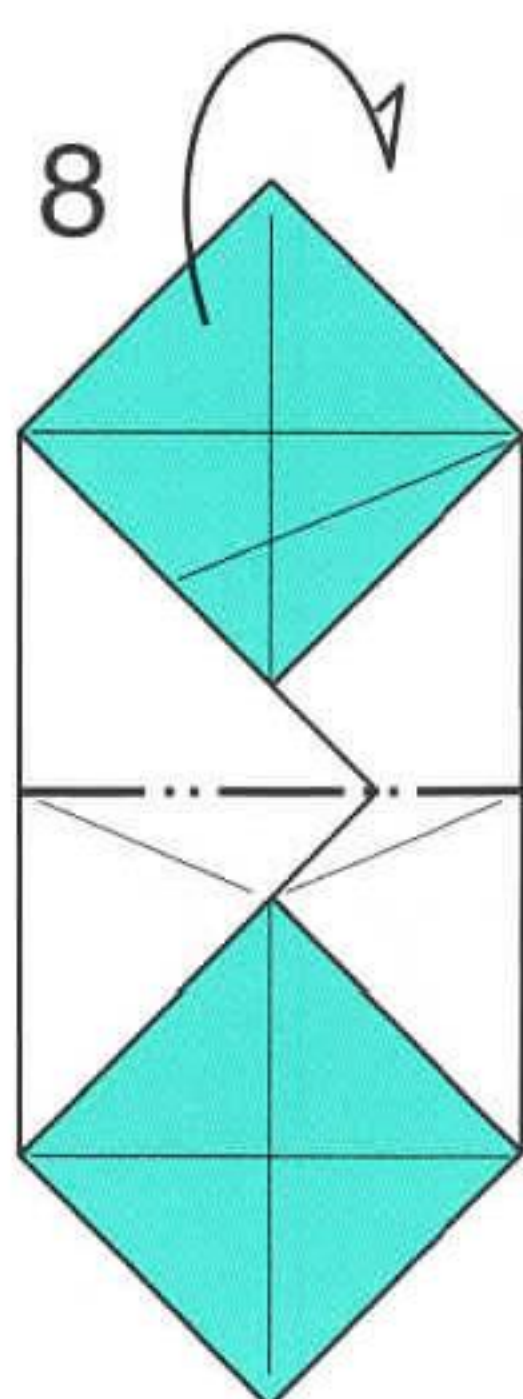
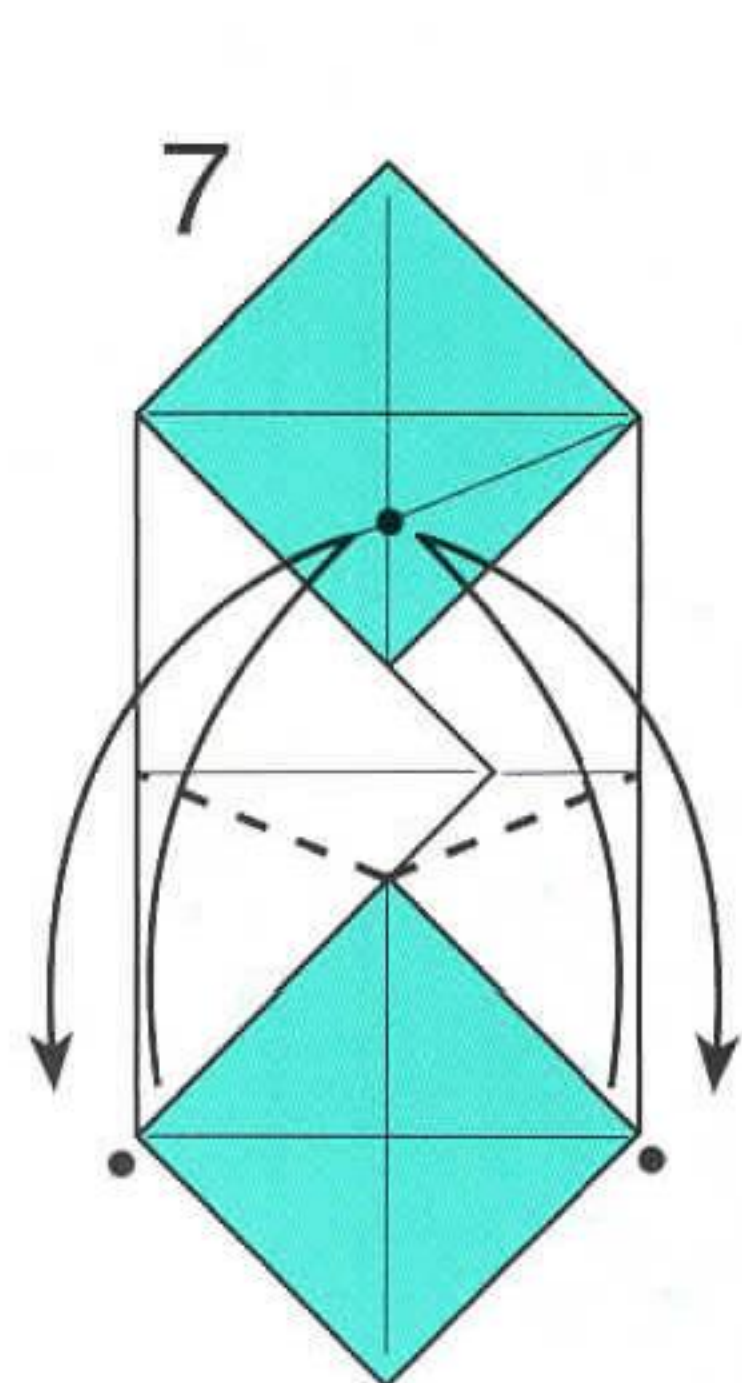
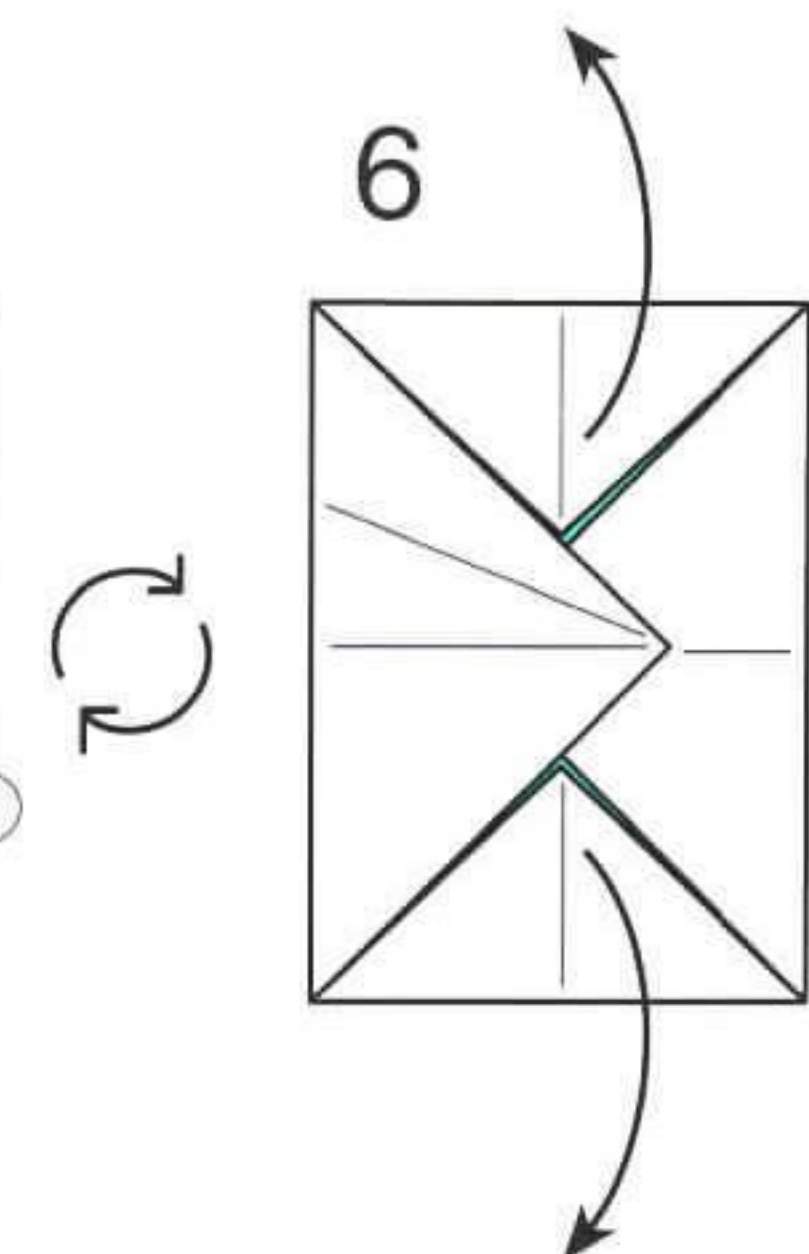
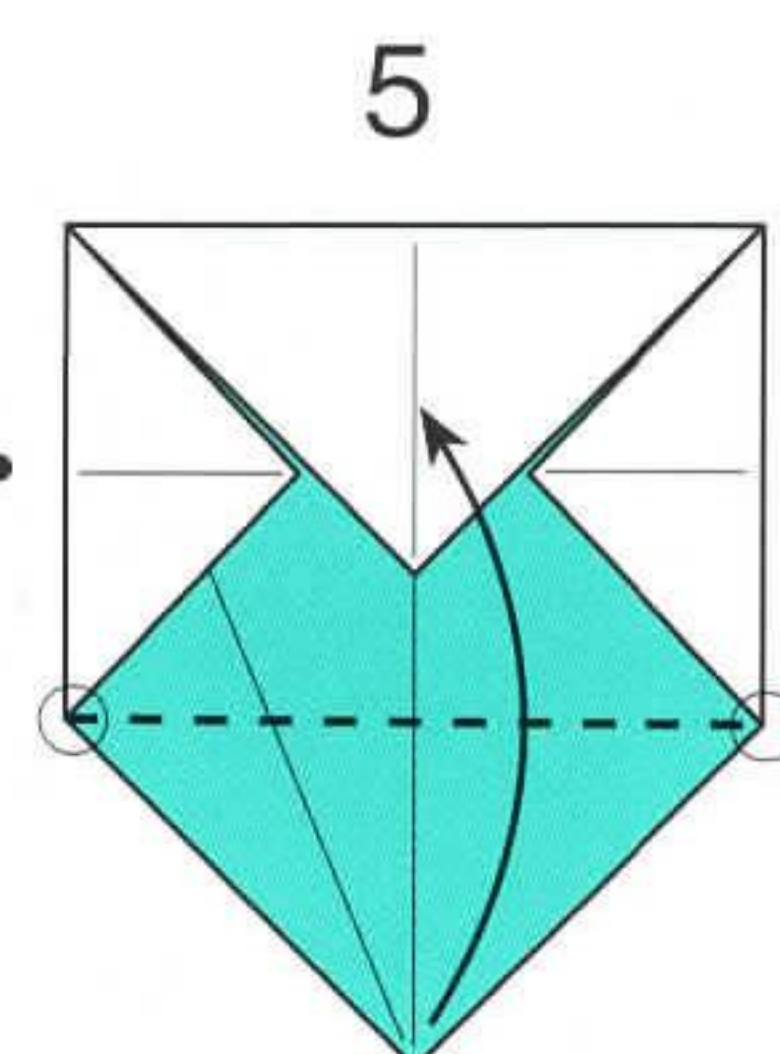
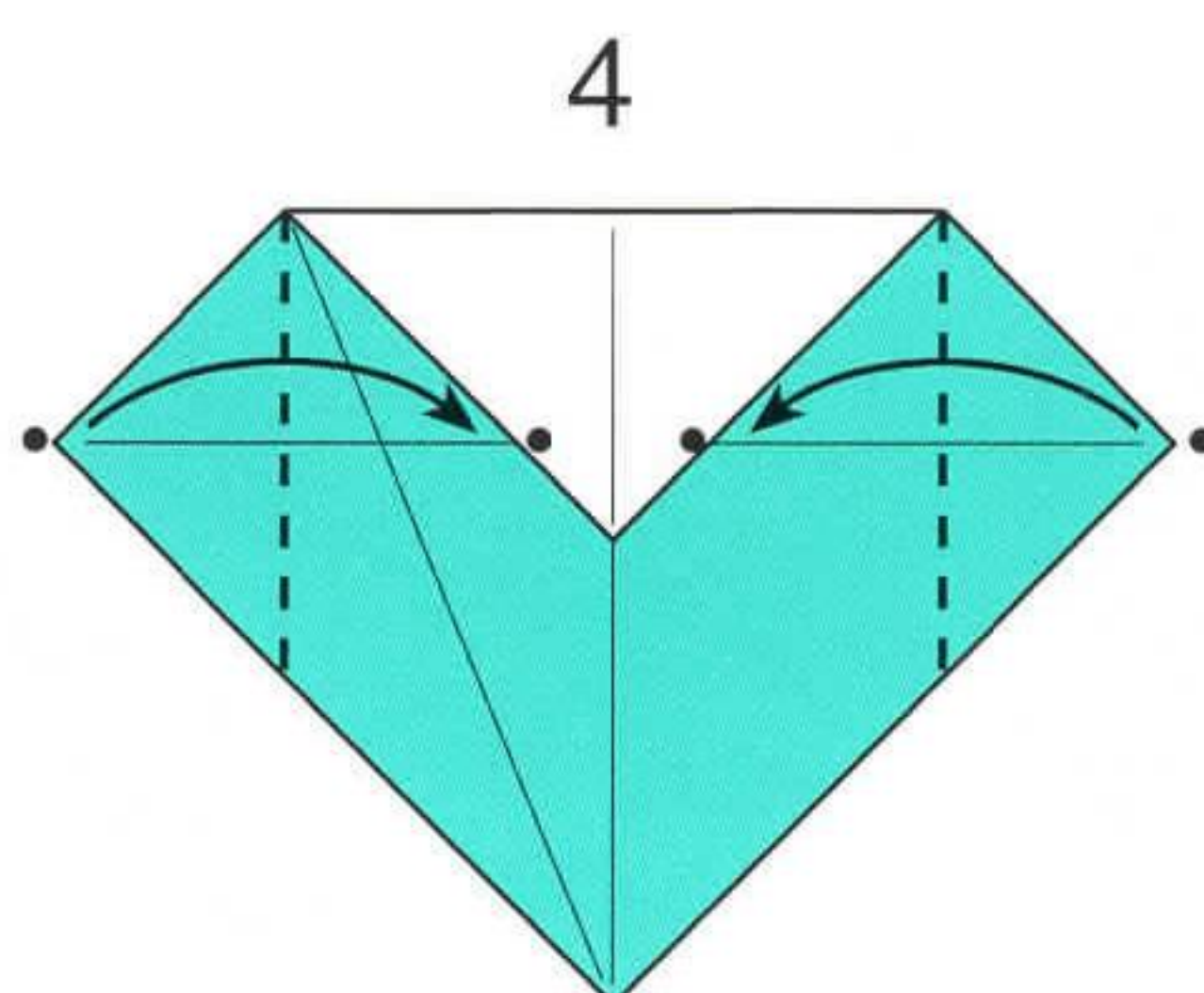
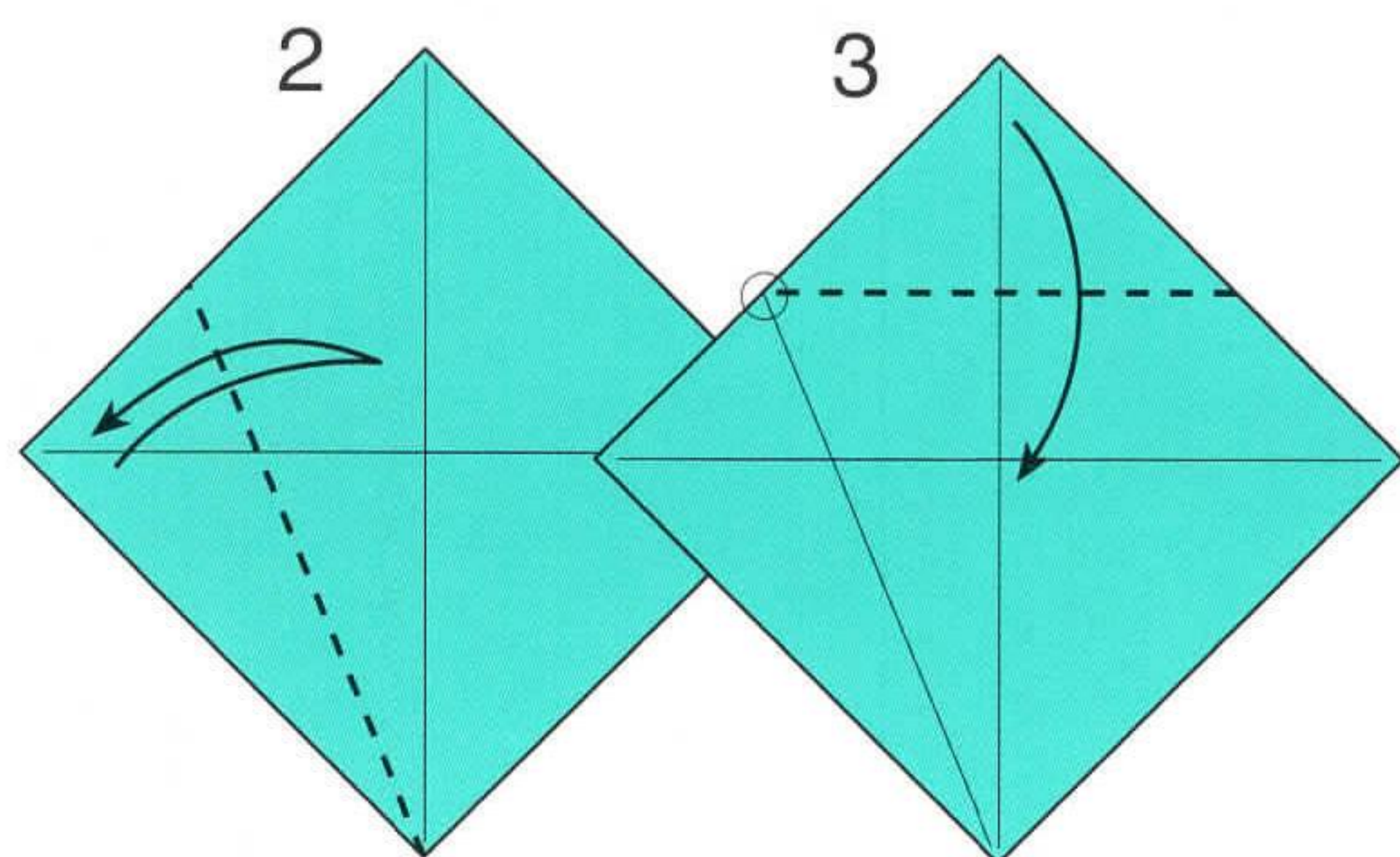
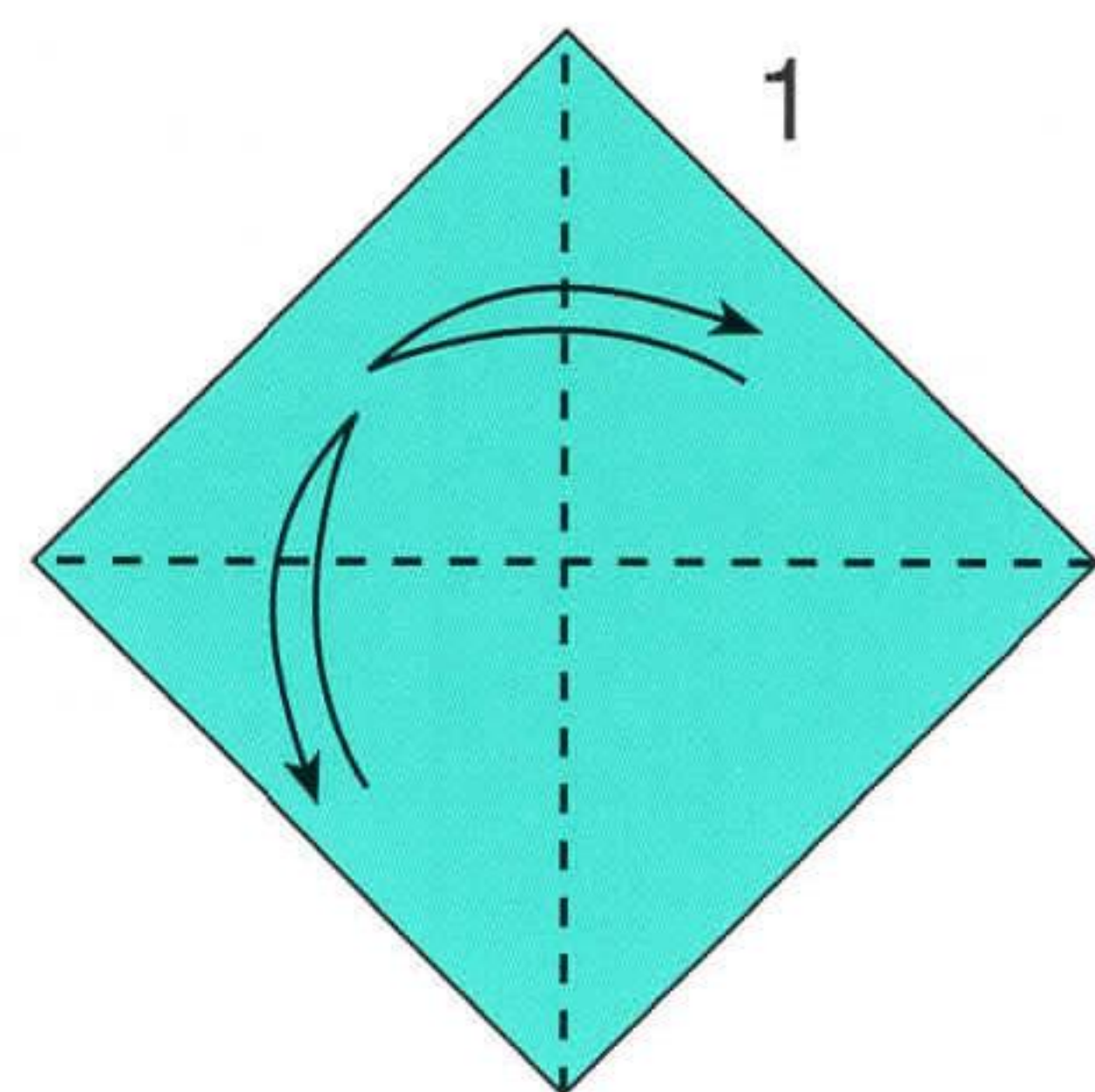
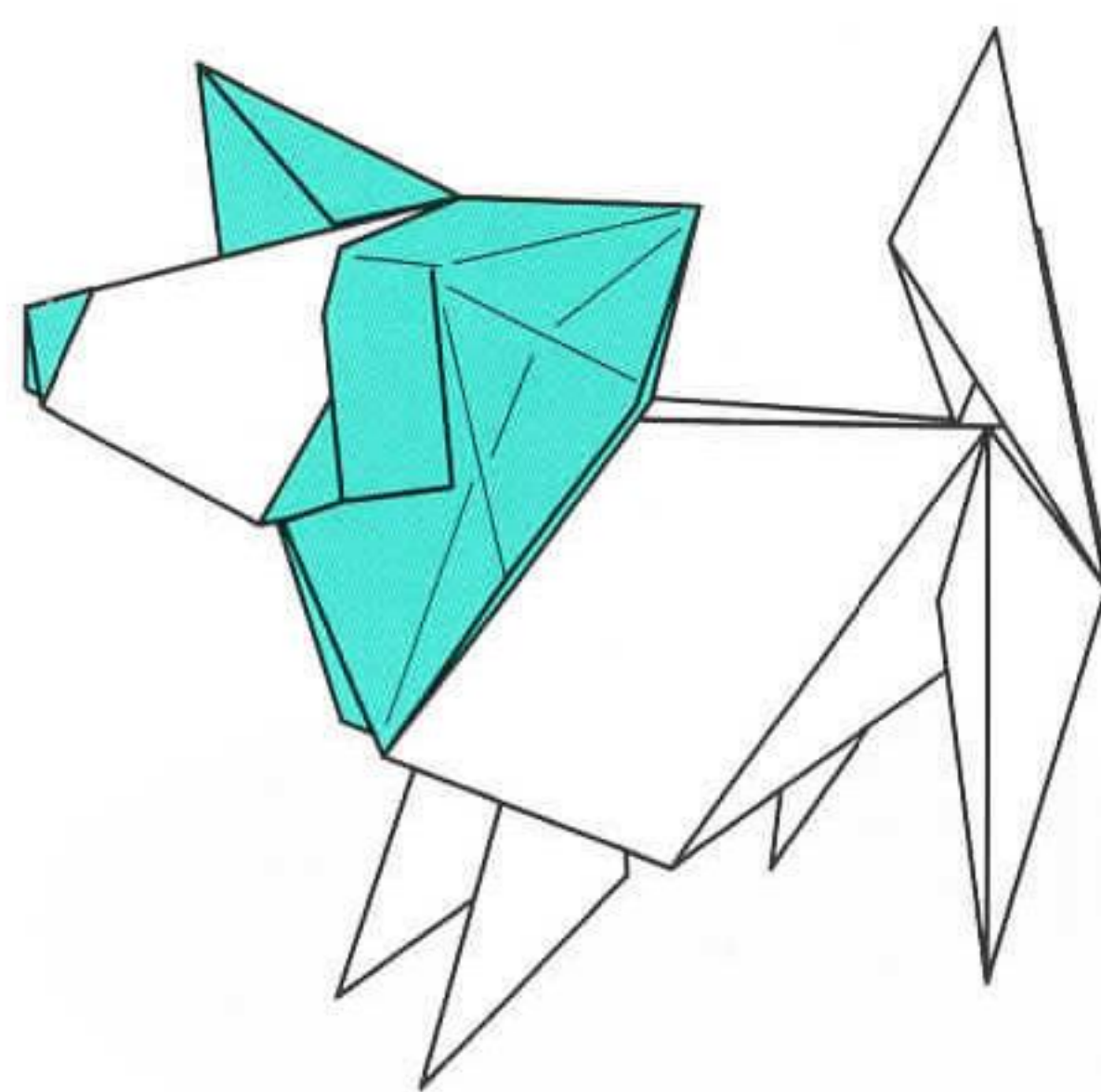
The gray area is the same to the *Carrot*.



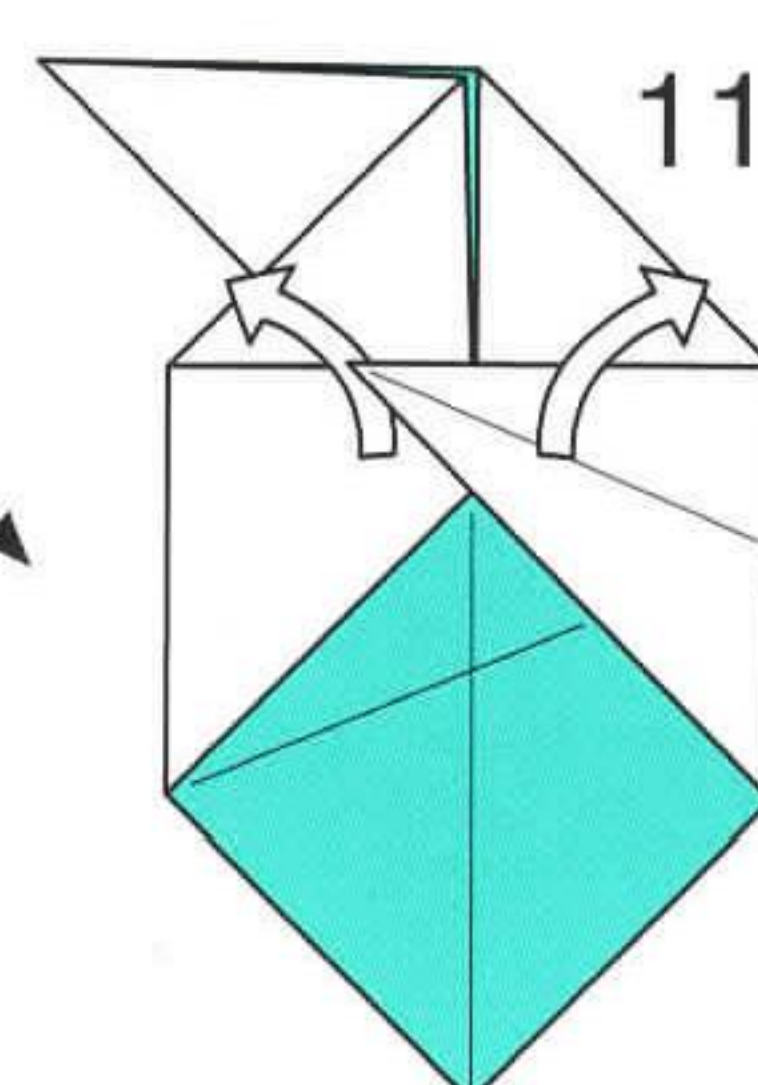
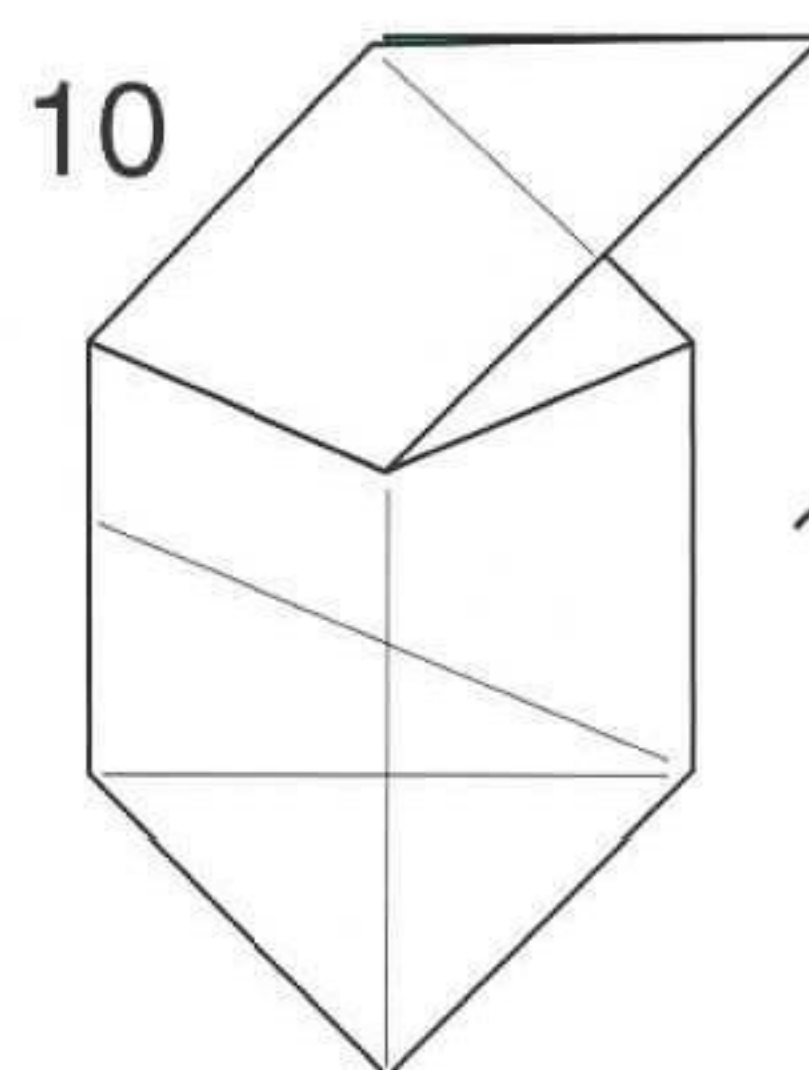
Papillon (Dog)

Theme: Composition of points

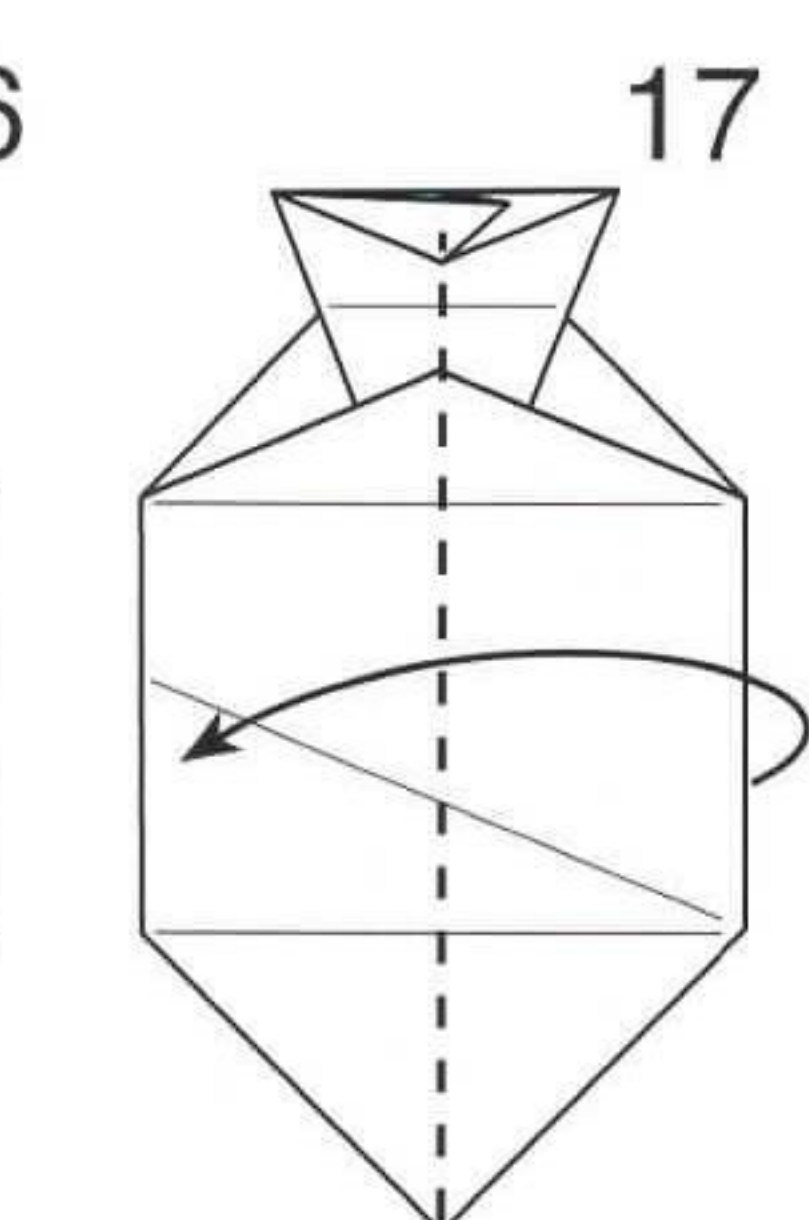
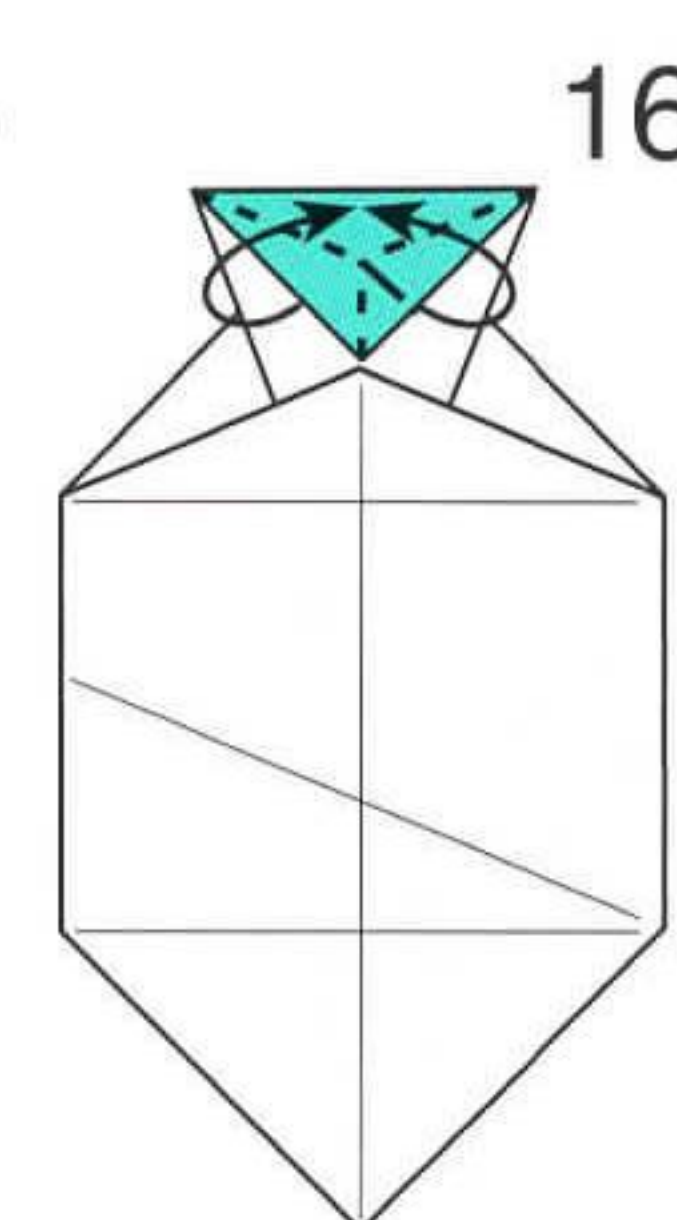
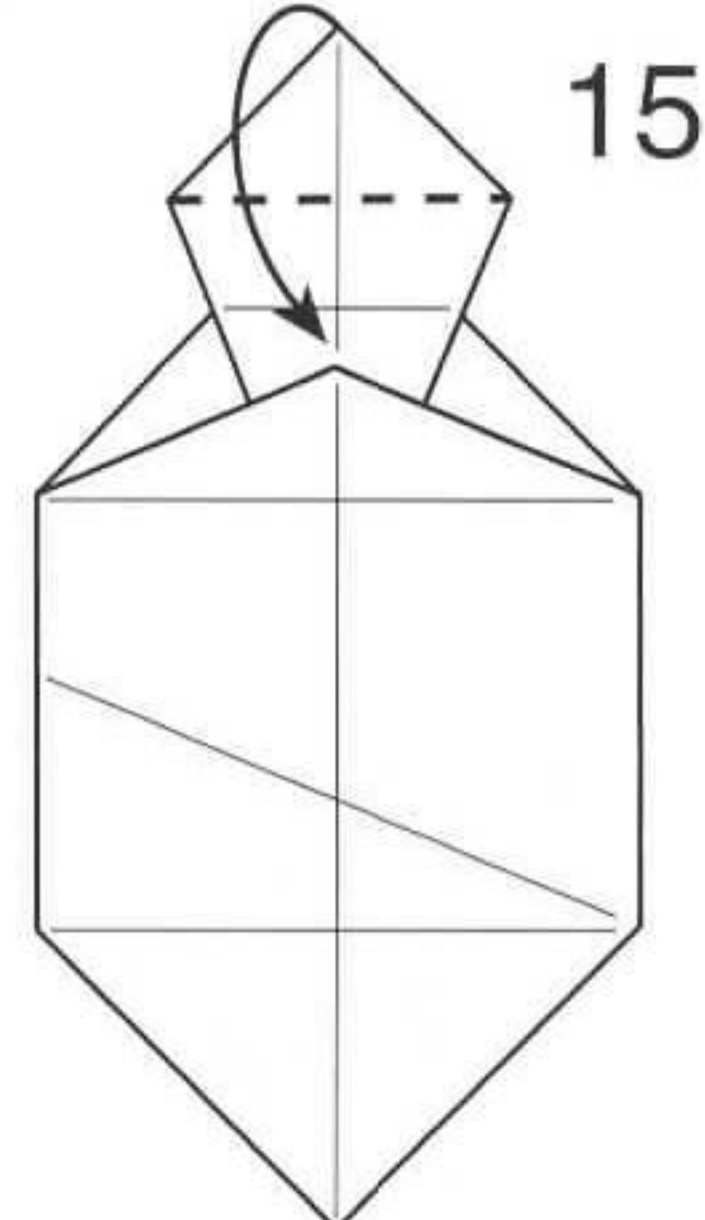
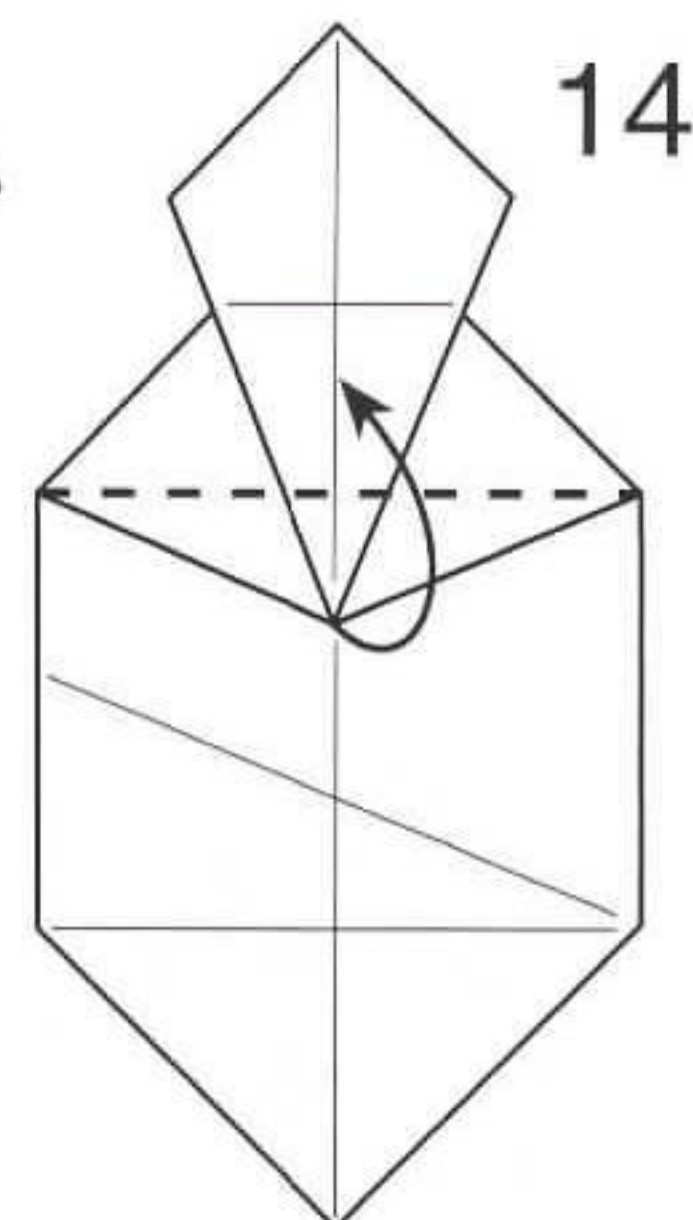
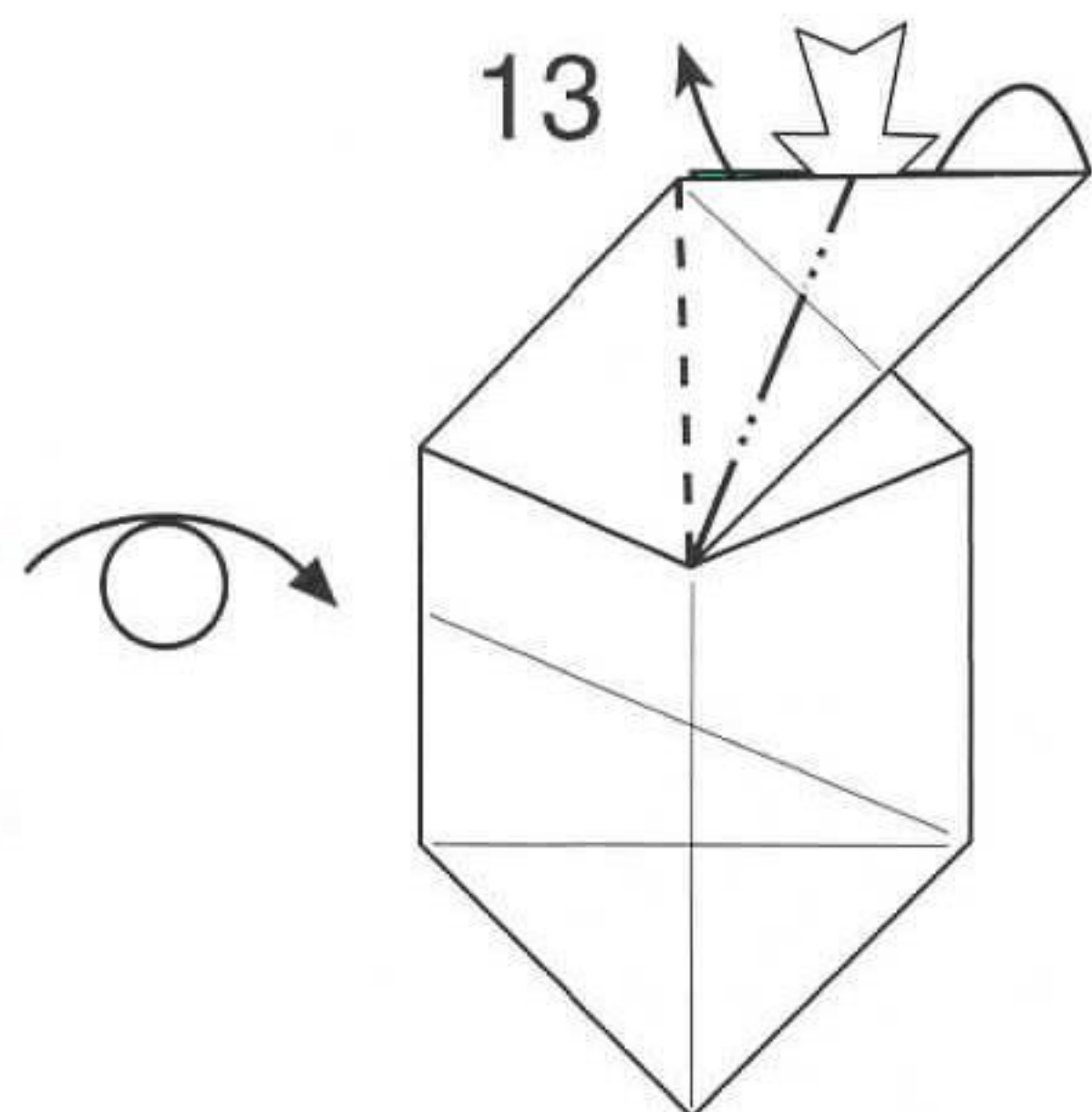
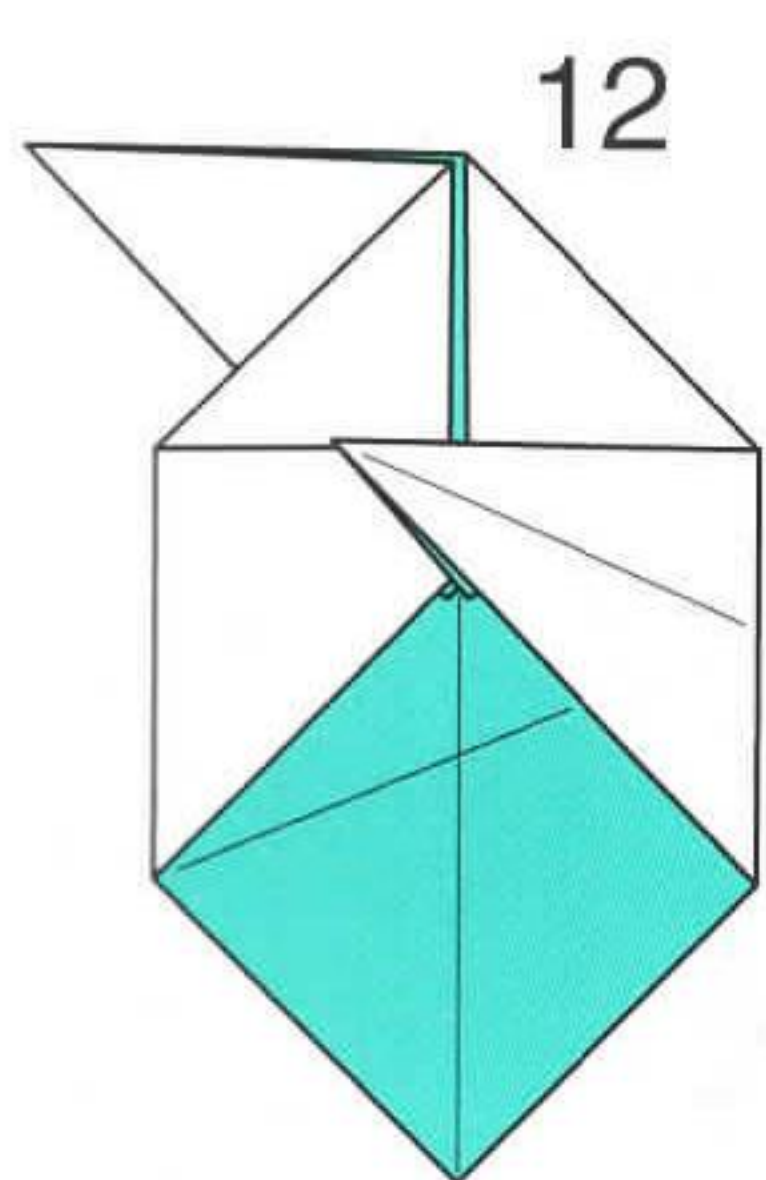
Fold using 6" (15 cm) origami paper.



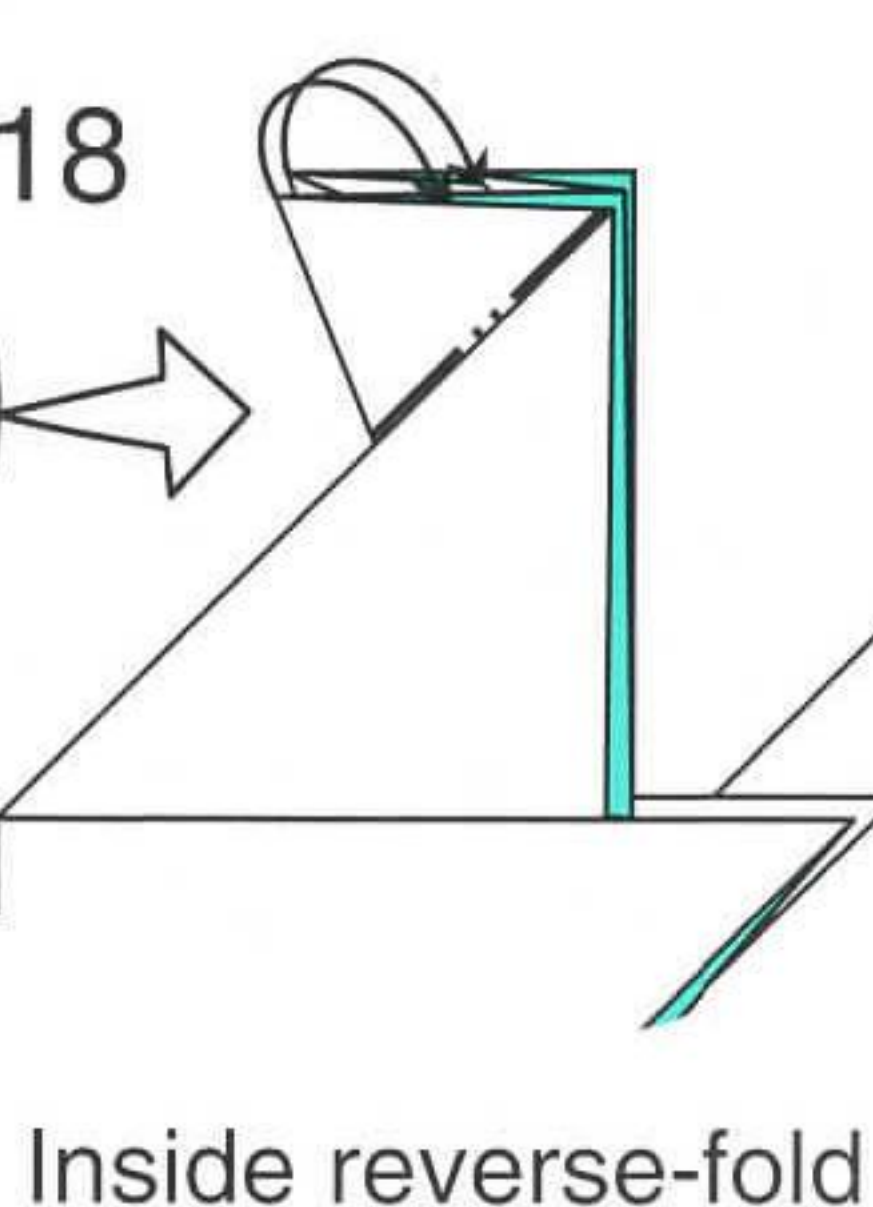
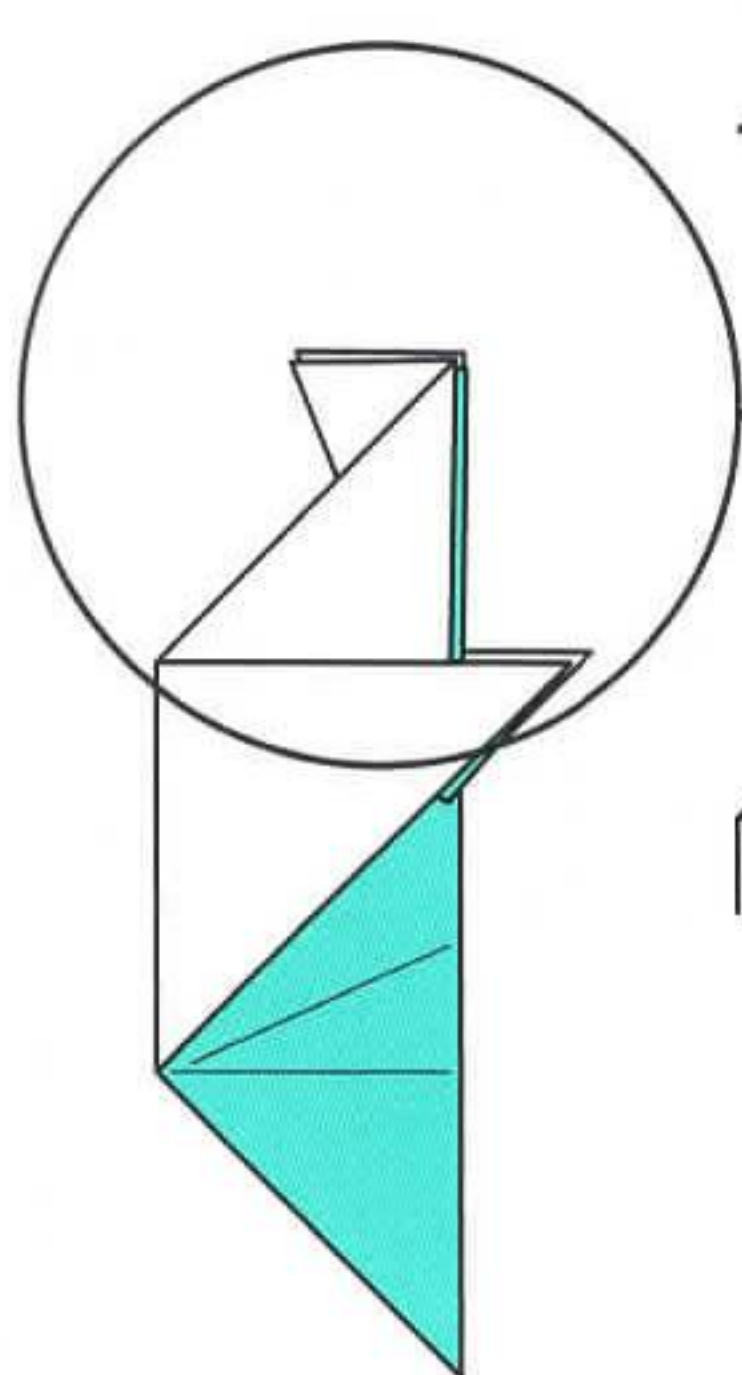
Fold like a rabbit ear fold.



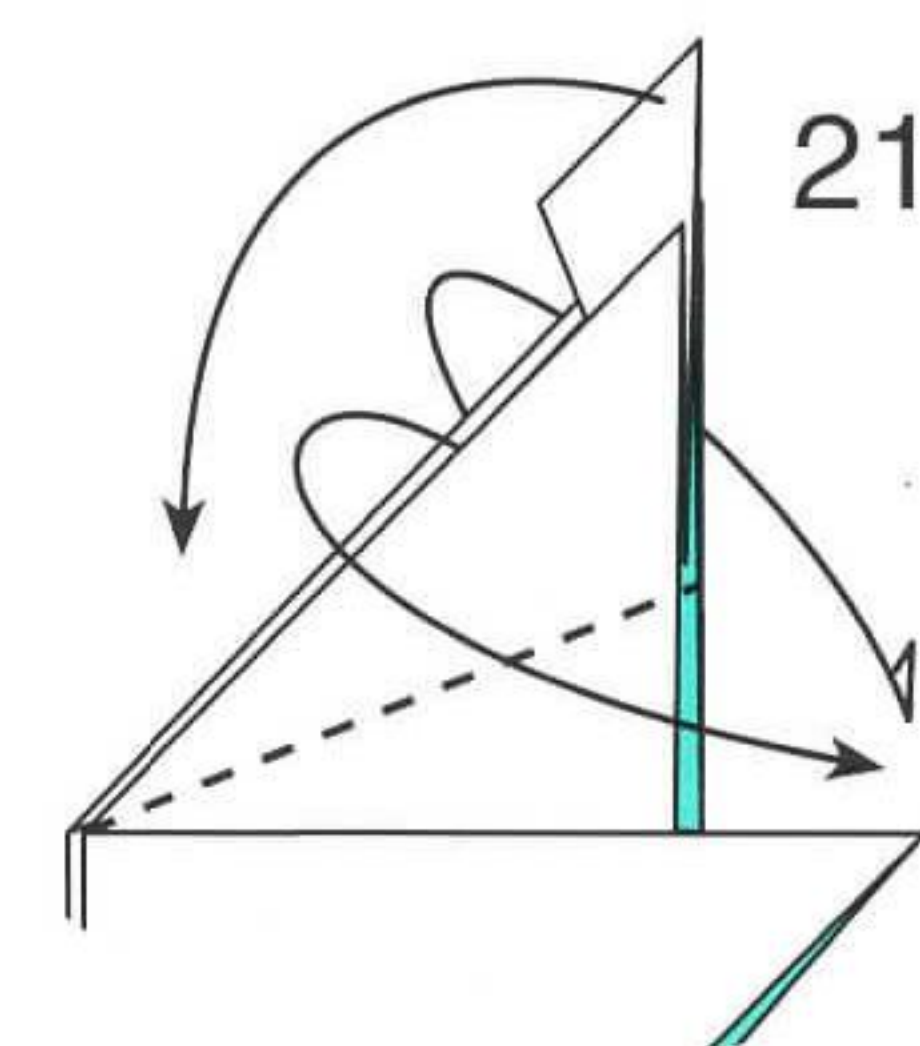
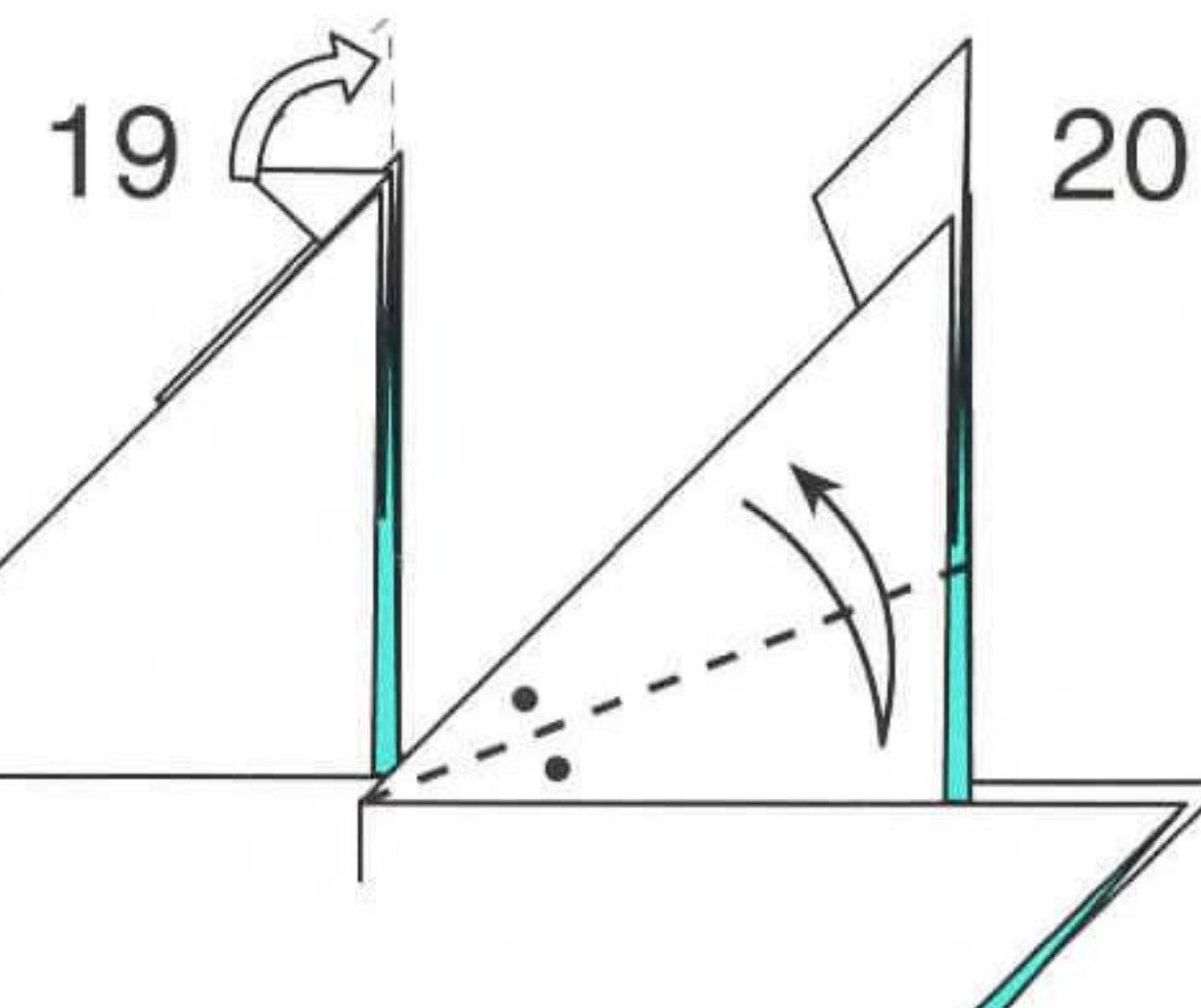
Unwrap the interlocked layers.



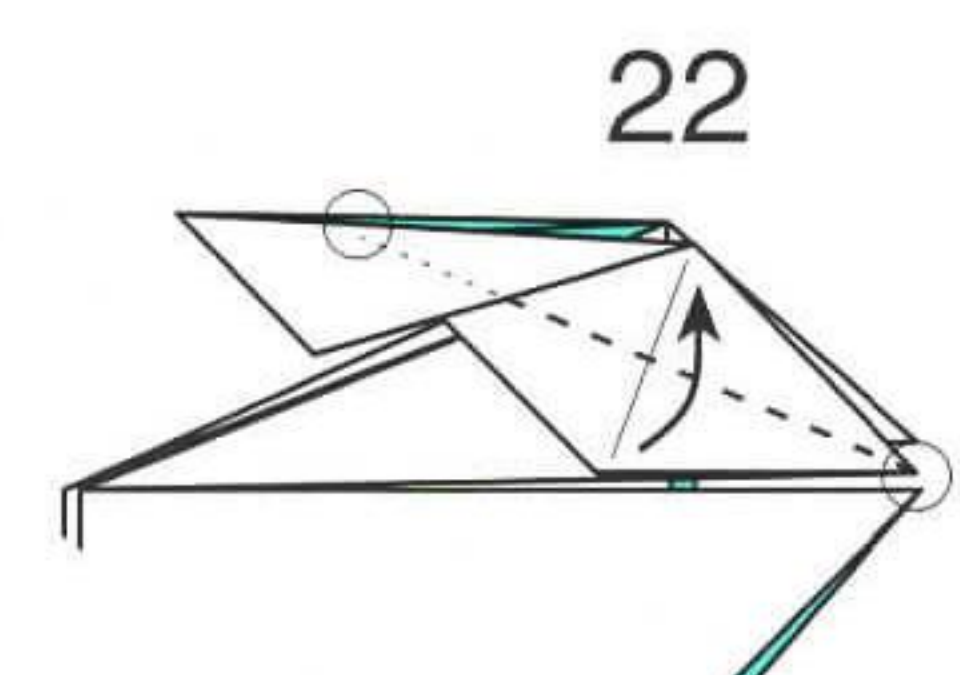
Rabbit-ear-fold



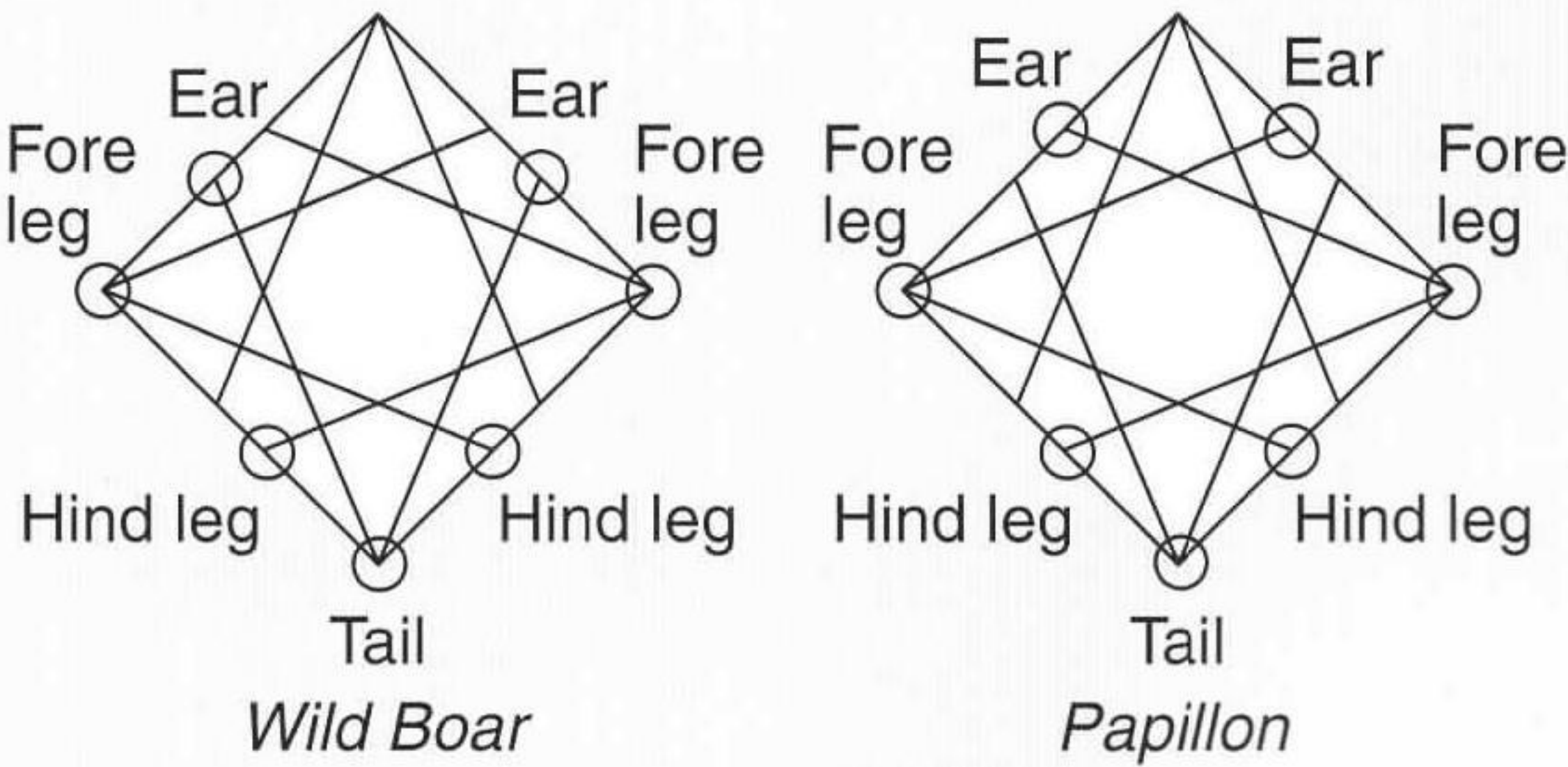
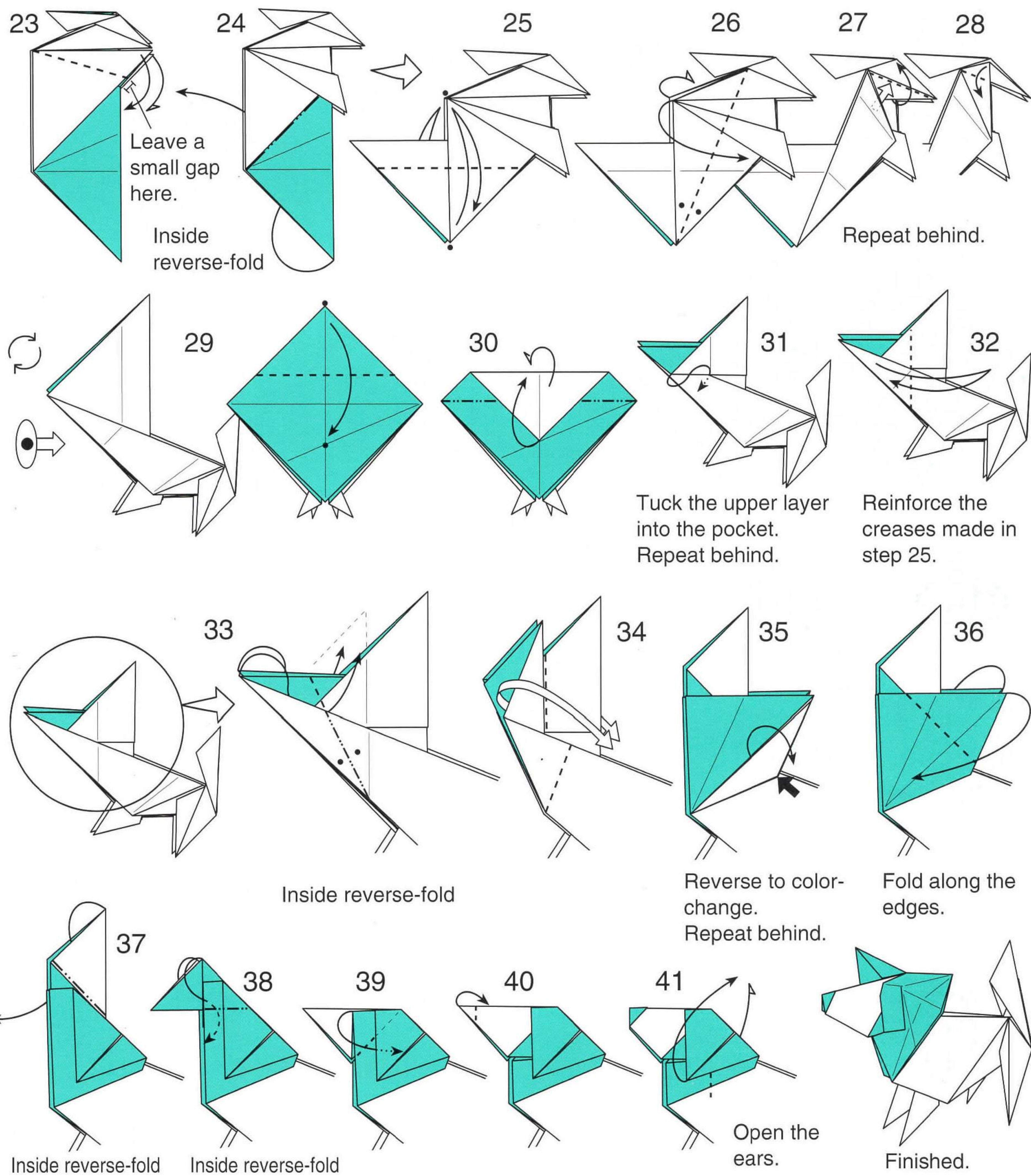
Inside reverse-fold



Fold like an outside reverse fold.



Repeat behind.

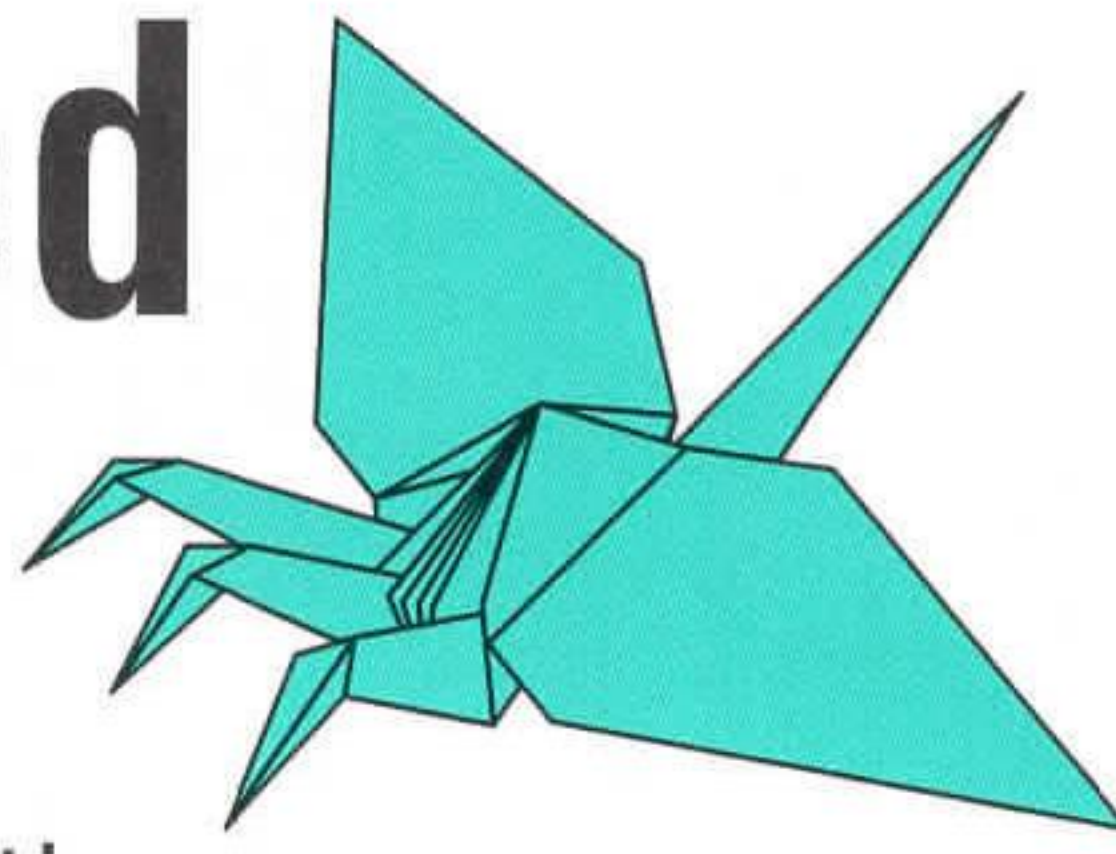


Composition of points

The composition of this *Papillon* is very similar to that of *Wild Boar* in **Simple models**. They are different only in the position of the ears and the nose. So, this means, you can design other quadruped animals by modifying *Wild Boar* or *Papillon*.

In fact, I designed other breeds of dogs and other animals like a cat from their variations.

Three-headed Crane



Theme: Technical folding; Preparation

Fold using 6" (15 cm) origami paper.

The idea of this model came from a mystery novel called *Tokeikan-no Satsujin (Homicide of Clock Pavilion)* by Yukito Ayatsuji, where a character folds a three-headed crane. But the model only existed inside the author's head at the time of the writing.

Basics of technical folding and preparation

A square has only four corners. However, we need six flaps to make a three-headed crane, for its two wings, three heads, and one tail (or one flap for both legs). The stick figure on the right represents the required flaps. Although *Papillon* has eight flaps, a head, two ears, four legs, and a tail, they are too short to be used for the crane. So, how can we do it?

The easiest solution is to start from a hexagon. But that will be against the "one square sheet without cuts" rule.

Another solution is to prepare extra points in a square, such as using the blintz fold.

Start from a square, fold in half to make an isosceles right triangle, and make it square again by assembling the three corners together. Then we have four points on one corner of the square that are prepared for three heads. But, if we fold a Bird base with the prepared square and unfold, we can see that the crease pattern consists of four Bird bases. Re-arranging these creases, we will obtain nine long flaps. This pattern is more suitable for an insect with six legs, a head, a thorax, and an abdomen, than a three-headed crane.

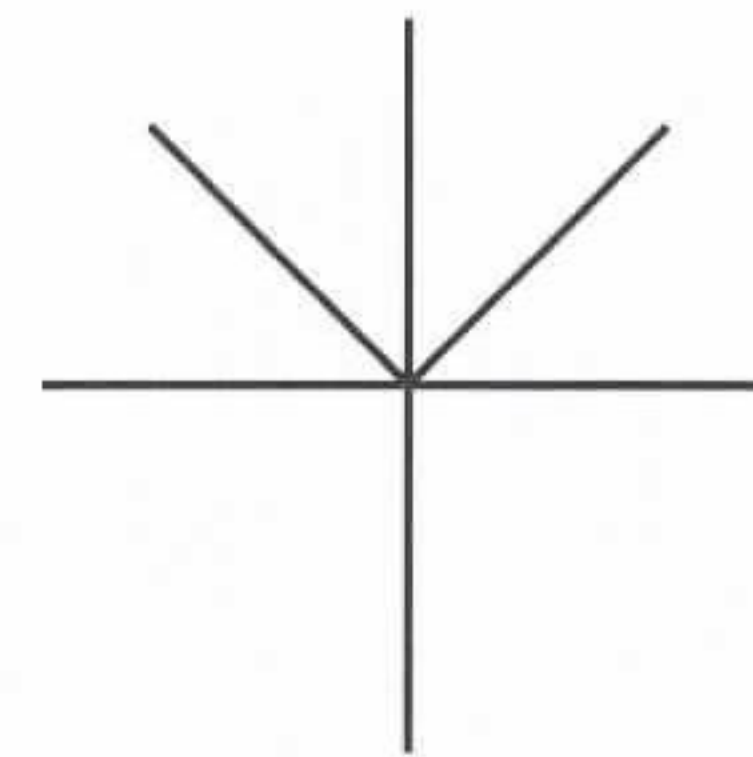
So, there should be a more efficient pattern that offers six flaps of the same length from a square.

Toshiyuki Meguro, Fumiaki Kawahata, and Robert Lang developed a design method called circle-packing. In the crease pattern of *Papillon*, I put circles only to indicate the places of points, not the length.

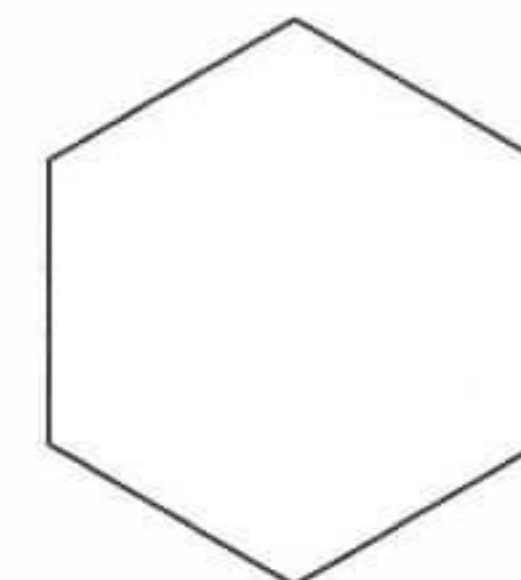
One can indicate the length of points with the radii of circles, because a flap requires an area of circle whose center is at the tip of it and whose radius equals to its length. Kawahata explained it by an intuitive analogy of an umbrella, that the radius of an umbrella equals to its length when folded. Note that a flap requires only a half or a quarter of the circle if the center is on the edge of paper.

The circle packing on the right, for example, gives six flaps. From it, we can fold a Bird base that has six flaps. And the base is larger than that from the prepared square above. Note that two of the four corners of the square will be folded inside and will not become points in the finished model.

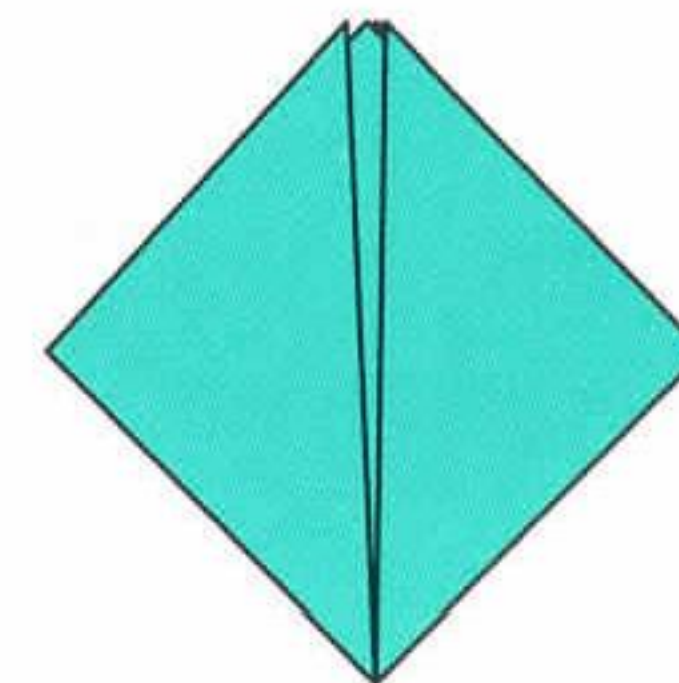
That means, the model can be folded from a hexagon that is inscribed in a square (shown on the right). Now, we have come back to the first idea of starting from a hexagon, but this hexagon is easier to fold from a square.



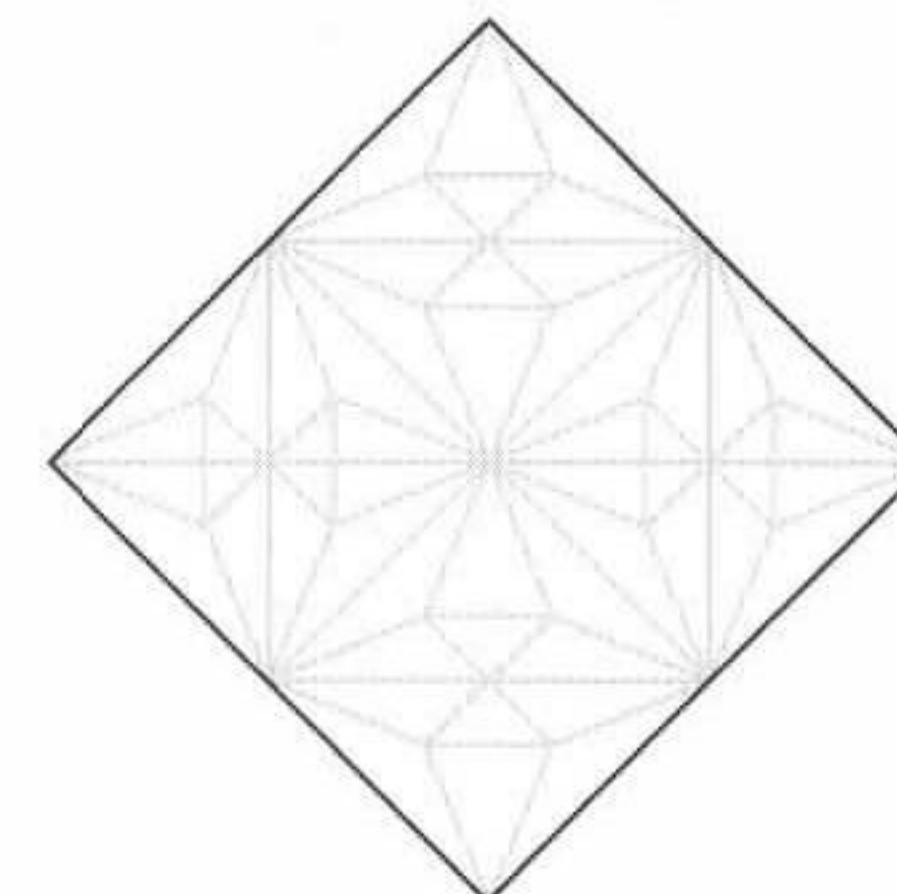
The basic tree figure for a three-headed crane



Starting from a hexagon?



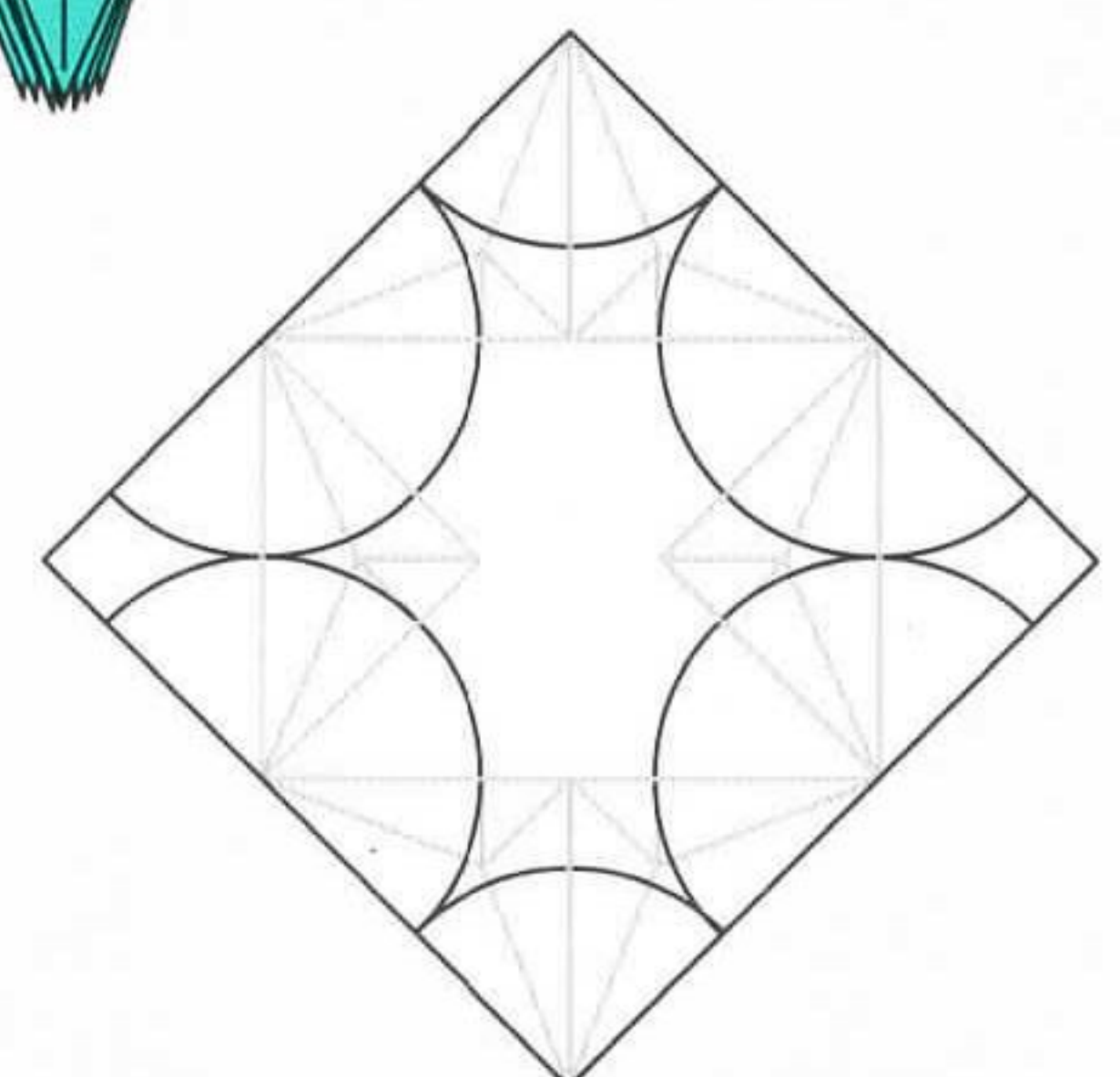
A prepared square



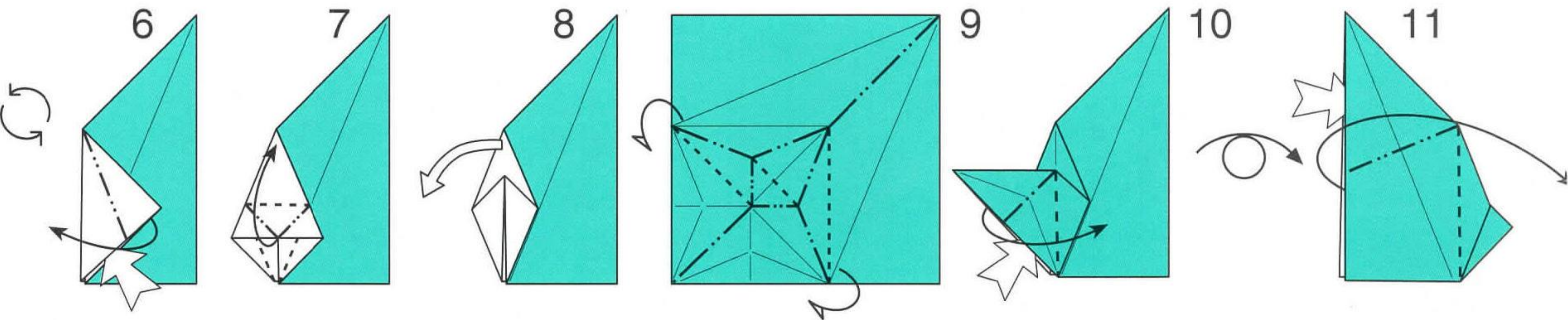
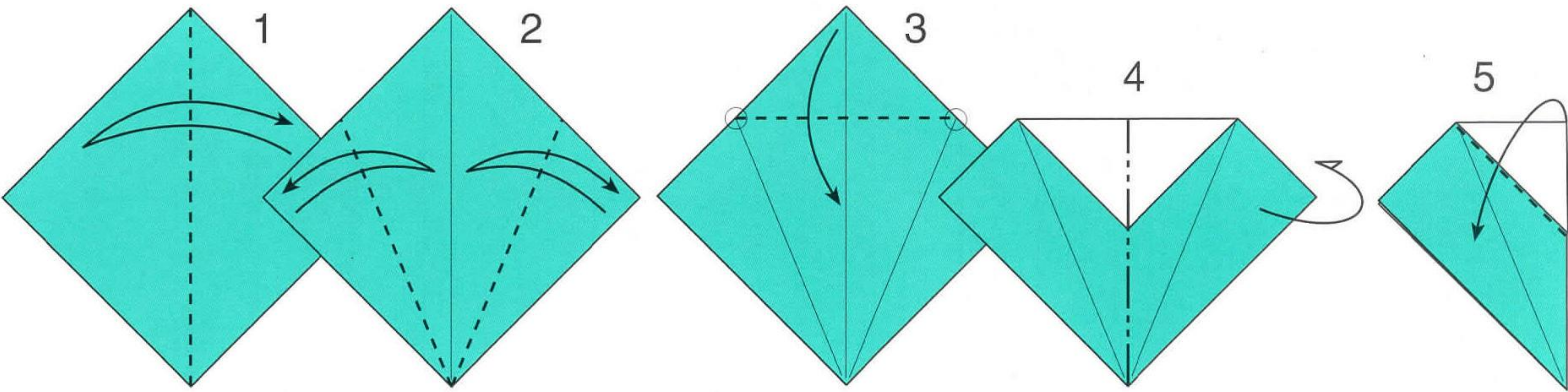
The crease pattern of Bird base from the prepared square (mountain and valley folds are not shown).



Base from the above crease pattern
It has nine long flaps.



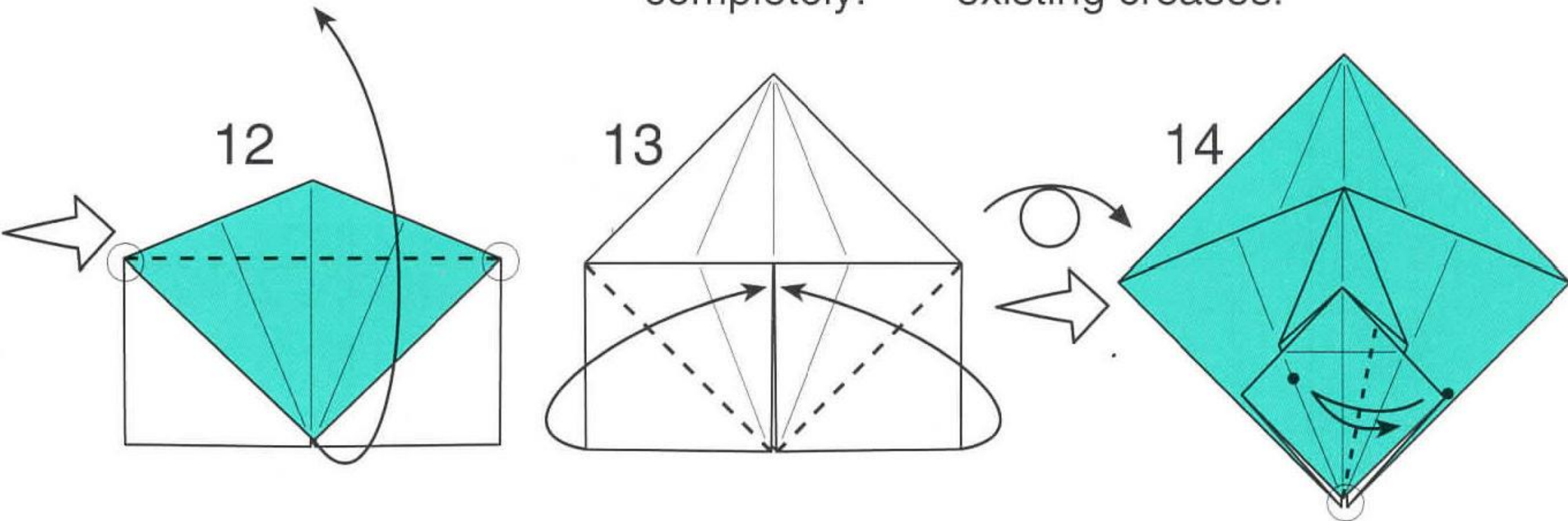
Six circles packed in a square, each of which corresponding to a flap. Gray lines are part of the crease pattern.



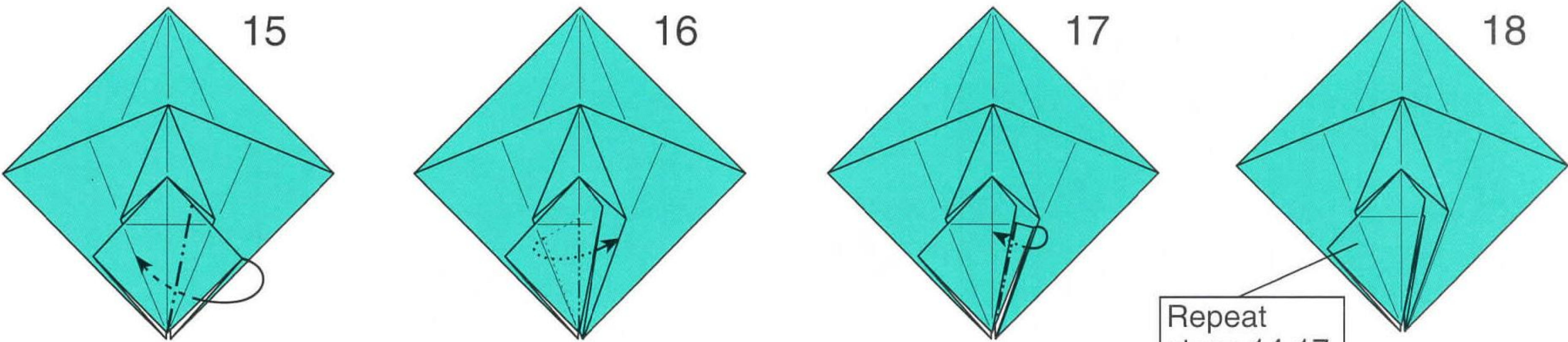
Petal-fold

Unfold completely.

Collapse using existing creases.



Step 14 can be seen as a prepared square, with three points on one corner.

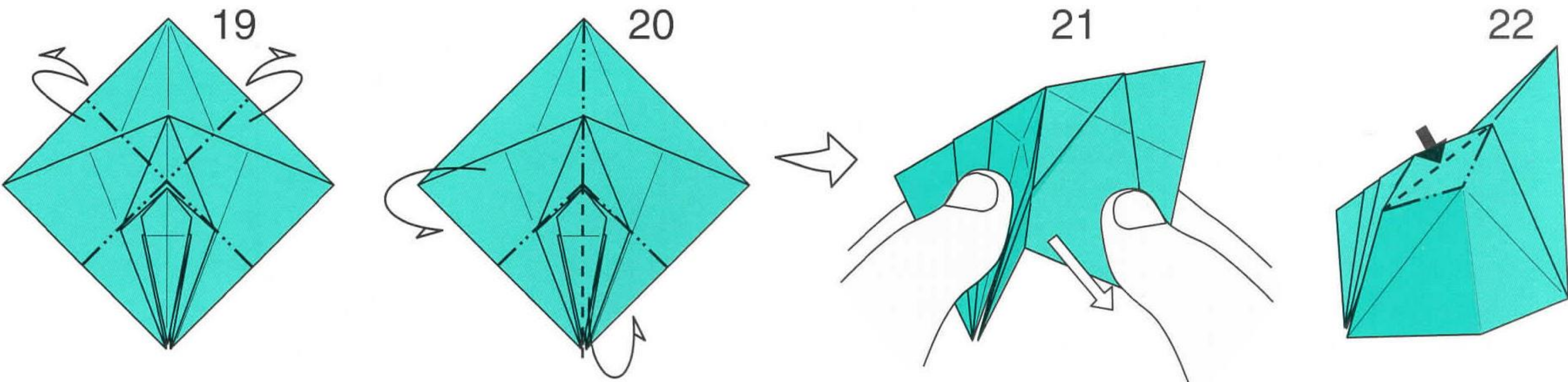


Repeat steps 14-17.

Inside reverse-fold

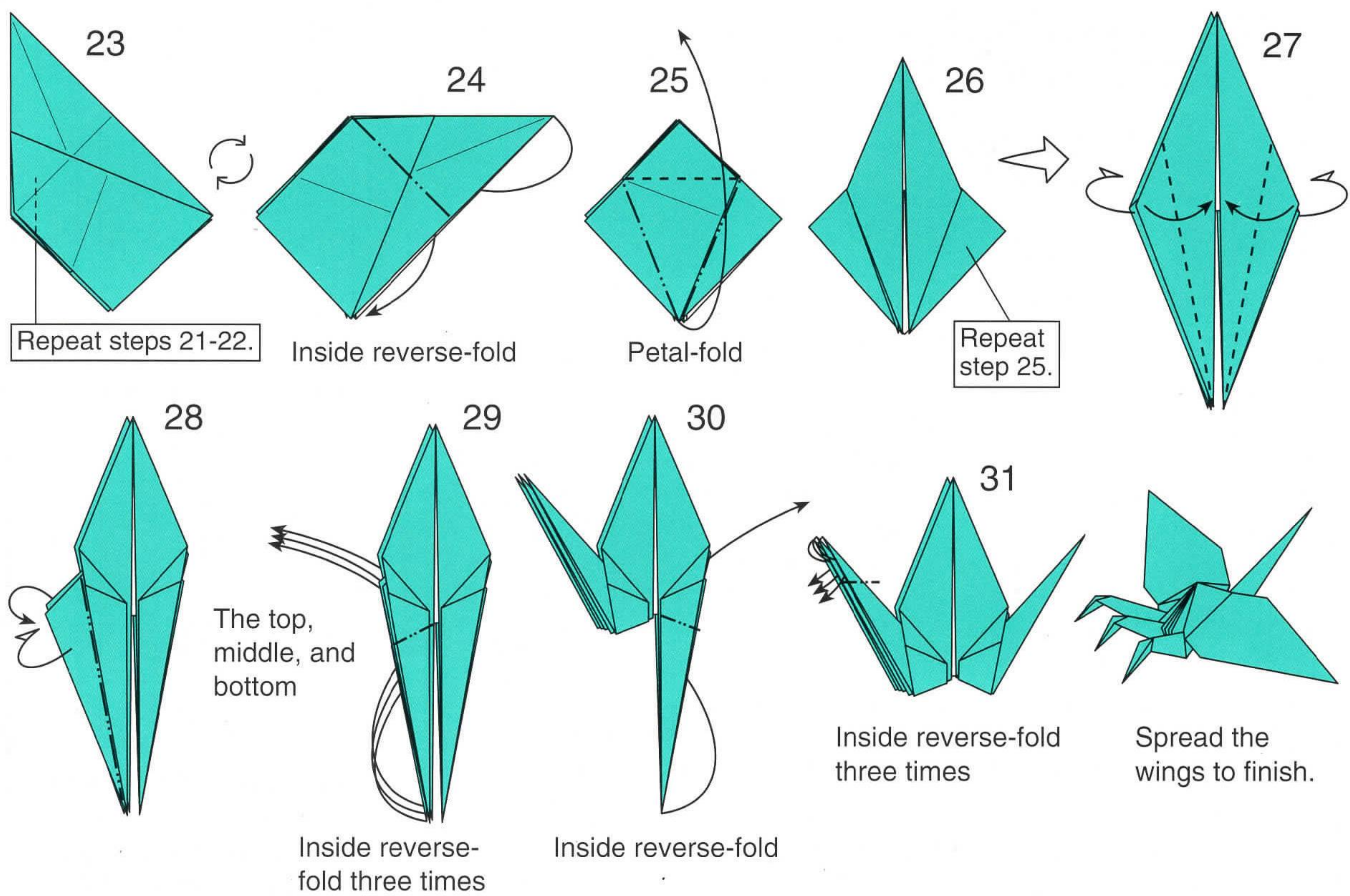
Inside reverse-fold inside.

Inside reverse-fold



Inside reverse-fold while folding the model in half

Push in the rhombic part.



Basics of technical folding: “Molecule”

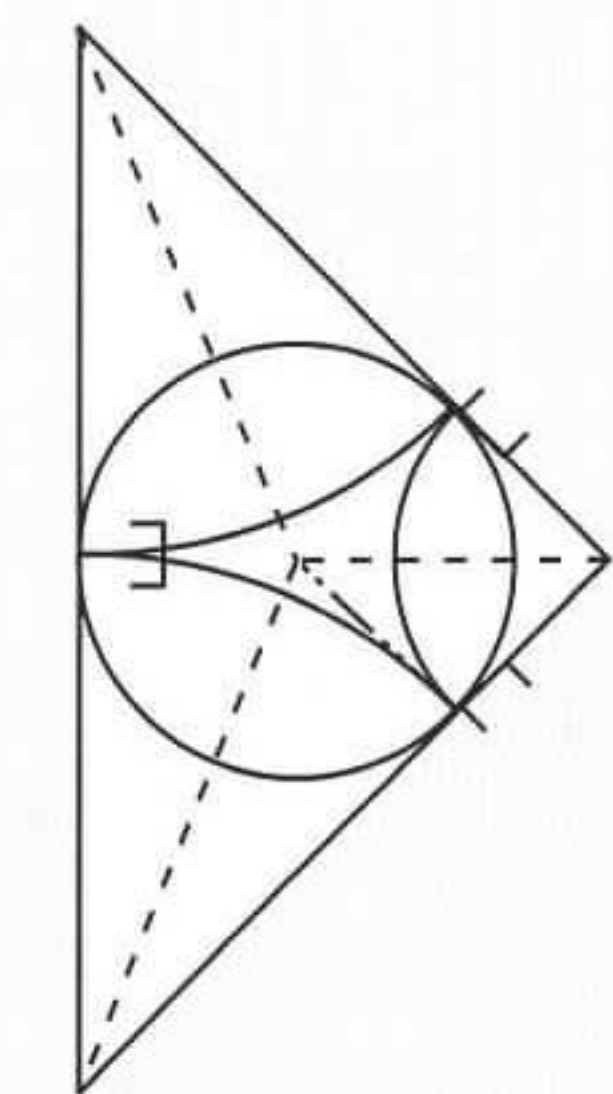
I have said that the length of a flap corresponds to the radius of the circle in technical folding. I also introduced circles inscribed in a triangle in *Orizuru Transformation* in **Fundamental Models**. Though it may be confusing, these two types of circle are different. They intersect with each other at a right angle, as shown on the right.

From a different point of view, the radius of the inscribed circle can be seen as the length of obtuse “flap,” or the “width” of the flap in the original orientation.

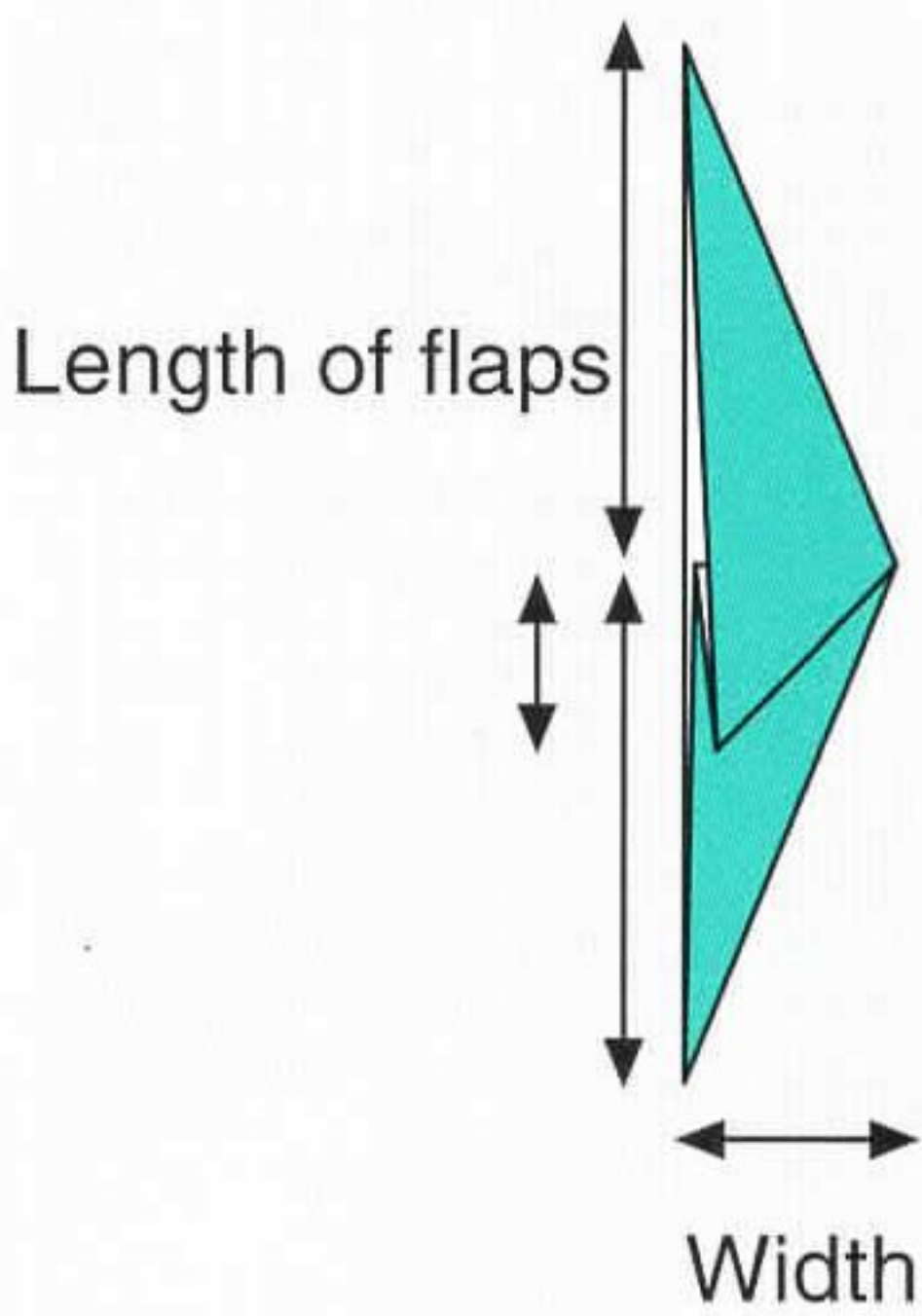
An area with a set of related creases, such as in the “rabbit ear fold of isosceles right triangle” on the right, is sometimes called **molecule**, term created by Toshiyuki Meguro who was inspired by my notion of **atom**, which is an area without creases, such as the triangles shown in *Wild Boar*.

Origami molecules can be polymerized just as in Chemistry. A unit molecule is called monomer, and a compound of small number (2-100) of monomers is called oligomer. “Oligo-,” as in oligosaccharide, means “a few.” Plastics is compound of more molecules and called polymer, as “poly-” means “many.”

If a rabbit ear fold were a monomer, a Bird base would be an oligomer because it consists of four monomers. Why don’t we call it oligami? Then, a super-complex model, such as *Ryujin* or Eastern Dragon designed by Satoshi Kamiya with all its scales, would be called a polygami. Even though it consists of so many molecules, the model is still a developable combination of developable units. By the way, be careful to spell this pun correctly, as “polygamy” means plural marriage.



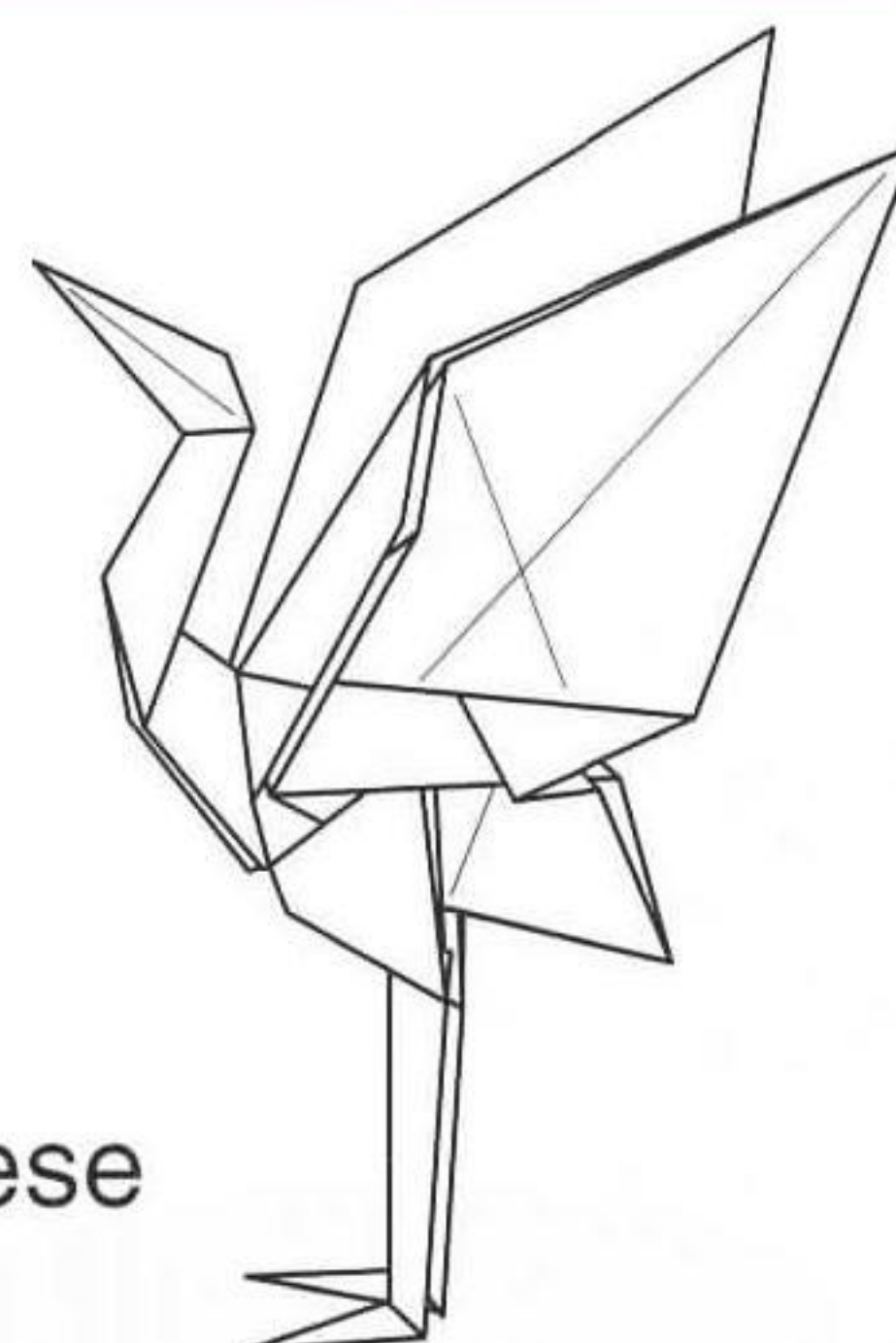
A rabbit ear fold



Standing Crane

Theme: Technical folding

Fold using 6" (15 cm) origami paper. Thin washi (Japanese handmade paper) larger than 8" (20 cm) is better.



Standing Crane and practical technical folding

The subject of the previous model, Three-headed Crane, is rather eccentric. Its basic structure can be applied to a two-legged crane by just flipping the front and the back. However, the middle flap would be too long for the tail of the crane. We only need five long flaps, which can be obtained by the crease pattern on the right. It is the crease pattern of Standing Crane. The thin lines define the composition of points, and the thick lines (black and gray) represent the creases. Note that mountain and valley creases are not shown.

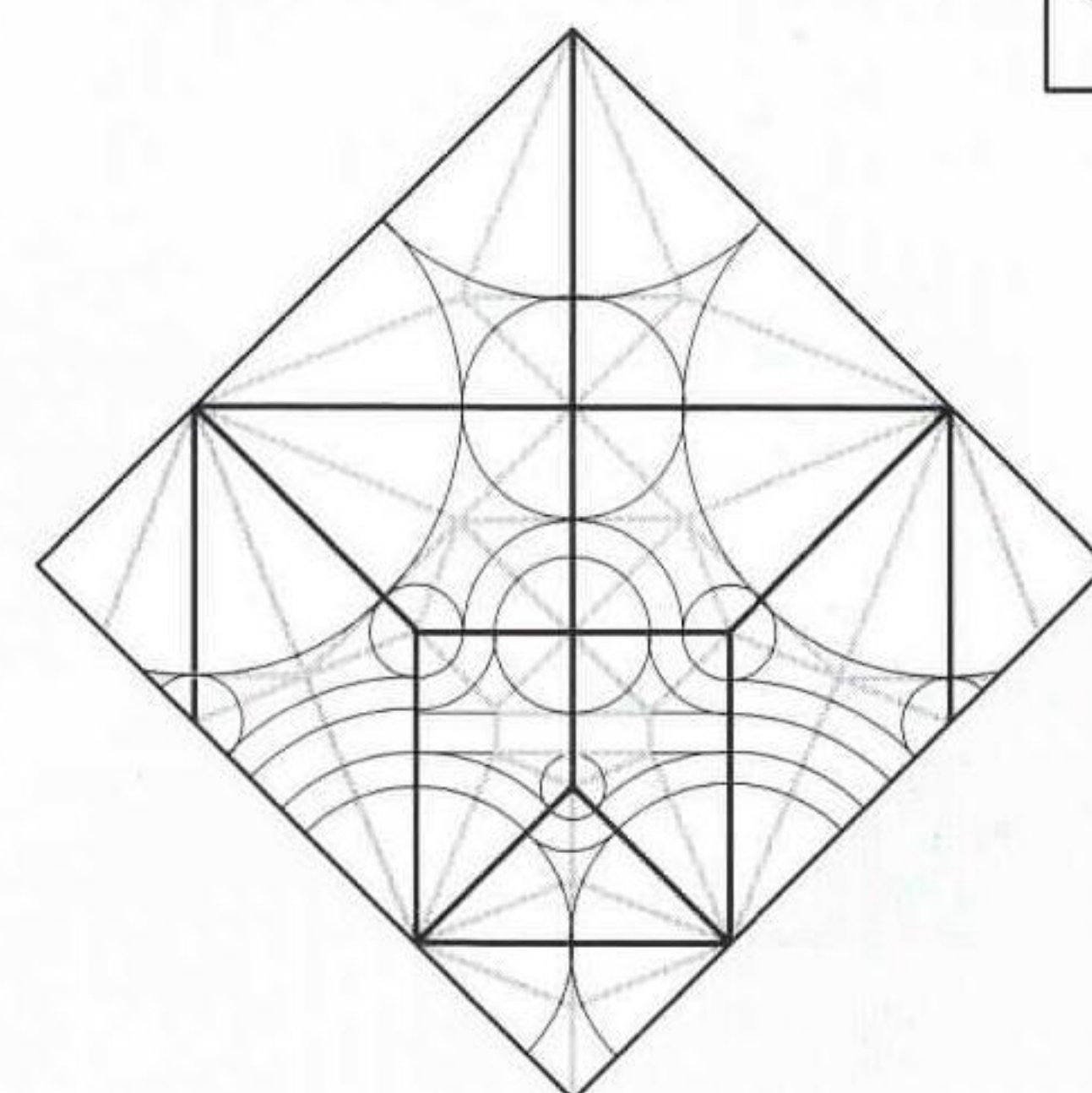
If you follow the thin lines, you can find river-like areas besides circles that correspond to flaps. Whereas a circle represents a branch, a river corresponds to a trunk that connects some branches. Compare the pattern with the tree figure on the right.

To understand the crease pattern, look at the areas surrounded by the thick black lines, or "molecules." Each area, except the two triangles at both ends that will be folded inside, will be folded so that all the sides are aligned, as the quadrangles discussed in Orizuru Transformation. Because of this special feature, called single-value by Toshiyuki Meguro or uniaxial by Robert Lang, we can easily combine many "molecules."

You may think that the trunk is too long for a structure of the crane. In fact, we can use a composition without rivers to obtain a tree without trunks. With such composition, however, it is difficult to arrange the angles of creases, and the flaps tend to have random shapes, even though they have desired lengths. Such a model is not likely to be easy to fold.

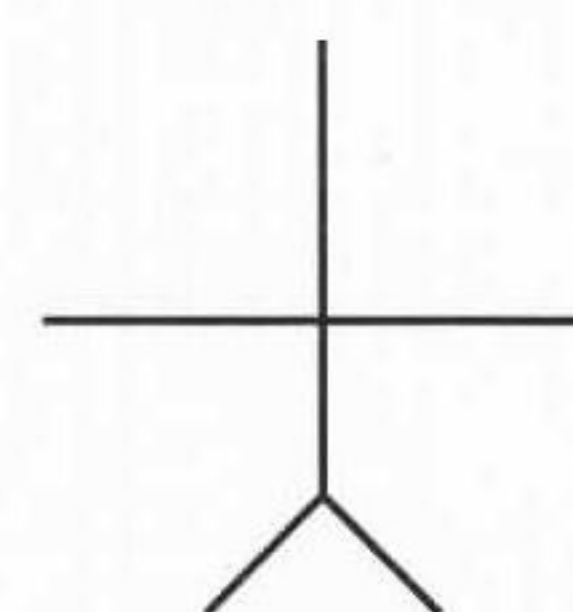
We can make an ordered structure with random angles by, for example, placing points on a grid. But arranging angles is one of the easiest ways to design clear and clean models. For this model, rather than taking care of the length of points, I arranged triangles and quadrangles with specific angles (such as those explained in Wild Boar), as if they are tiles, so that the entire crease pattern is flat-foldable. Actually, I came up with another pattern, which is shown on the right.

Just as Three-headed Crane can be folded from a hexagon, this model can be folded from a pentagon shown on the right, with one right-angled corner and four 67.5° corners.



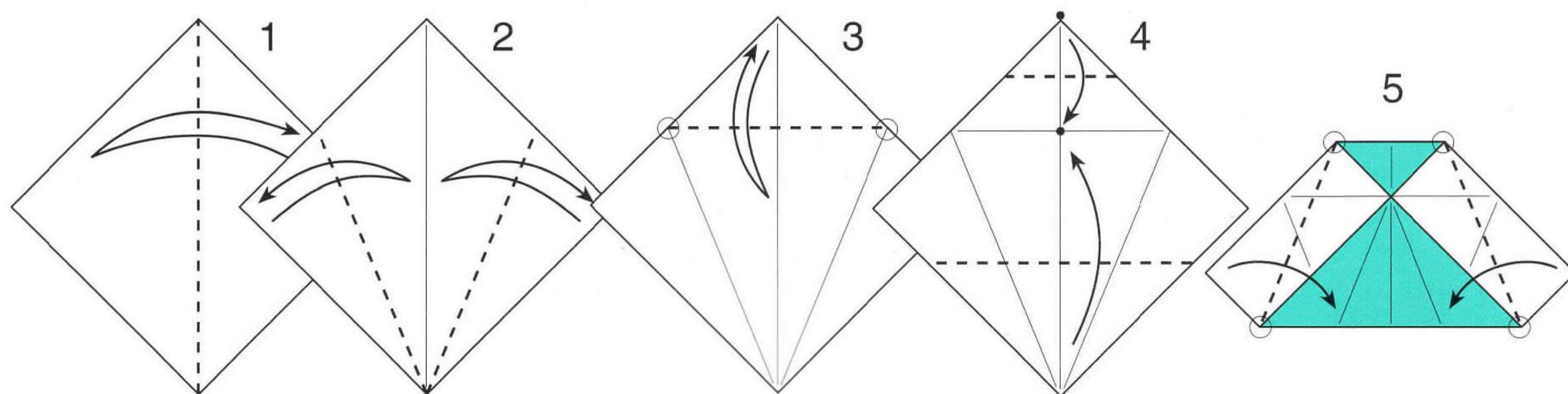
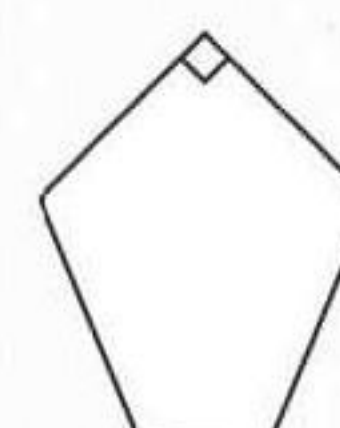
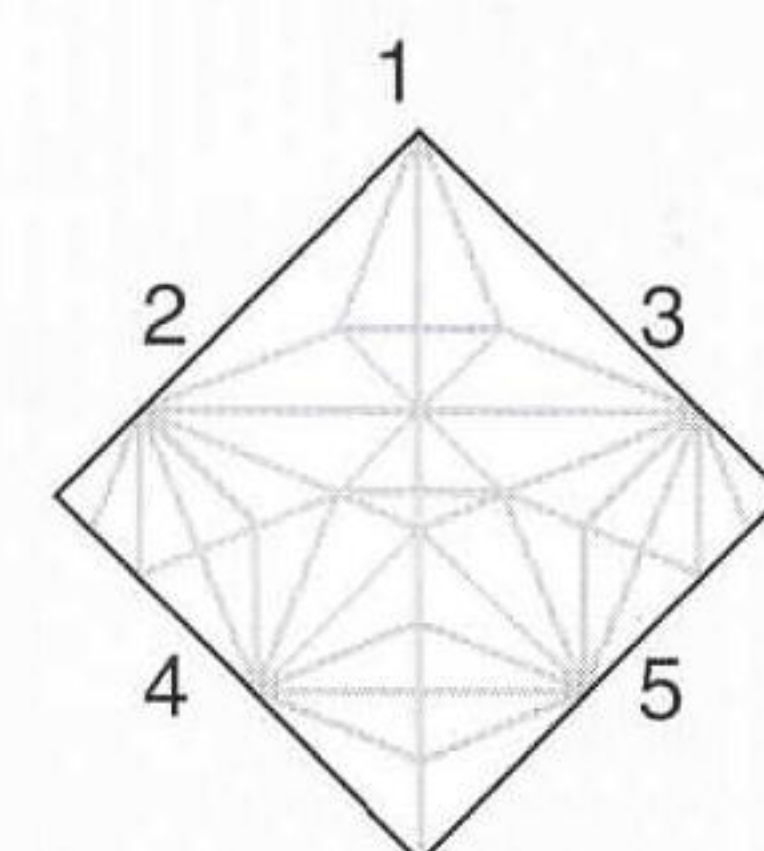
Composition of points and creases.

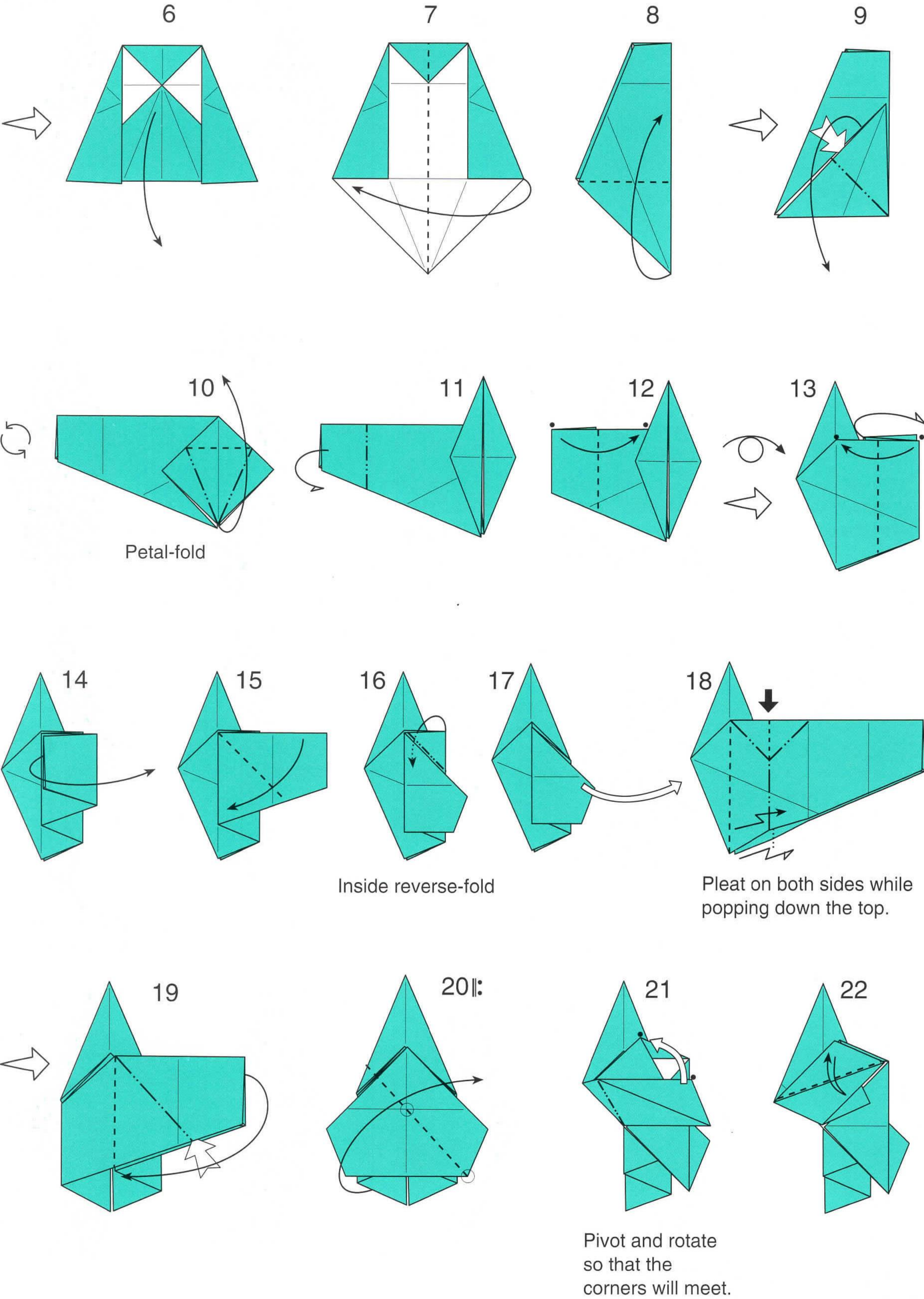
Circles represent flaps, and areas surrounded by thick black lines are "molecules."

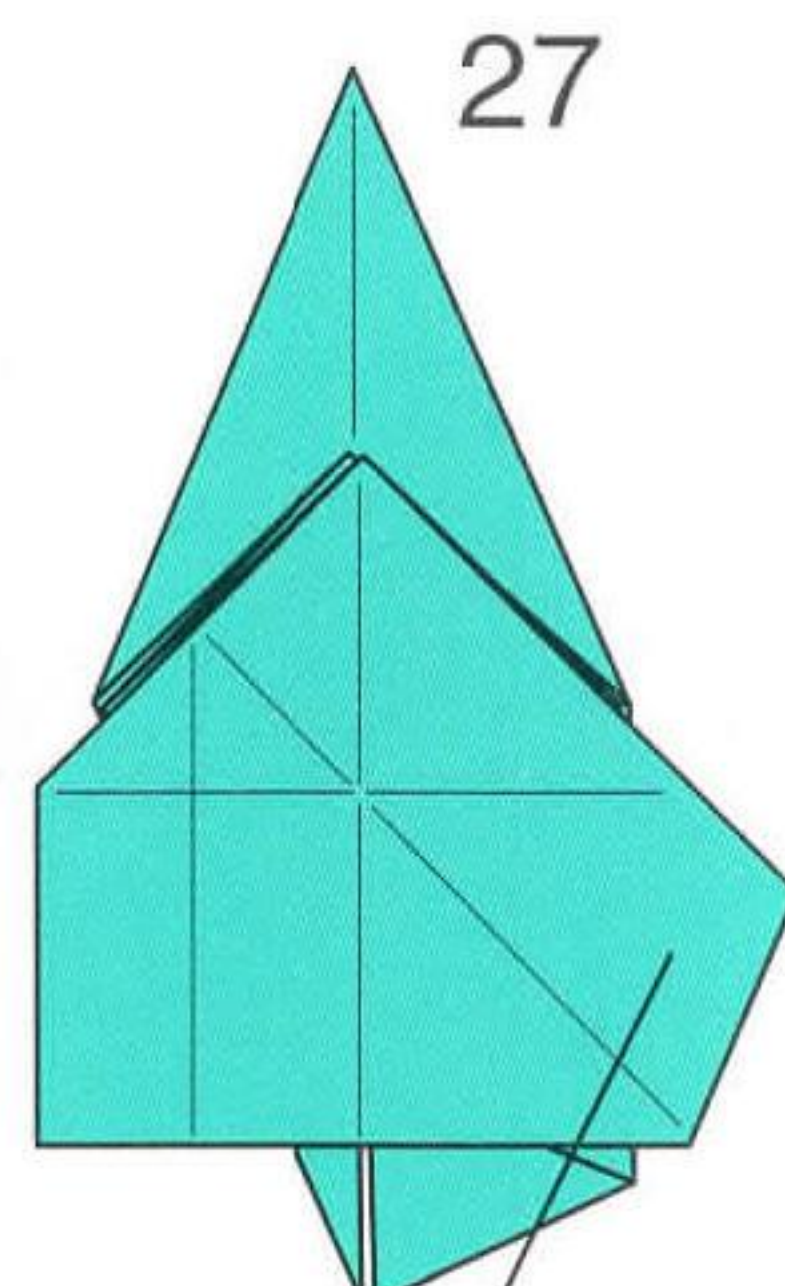
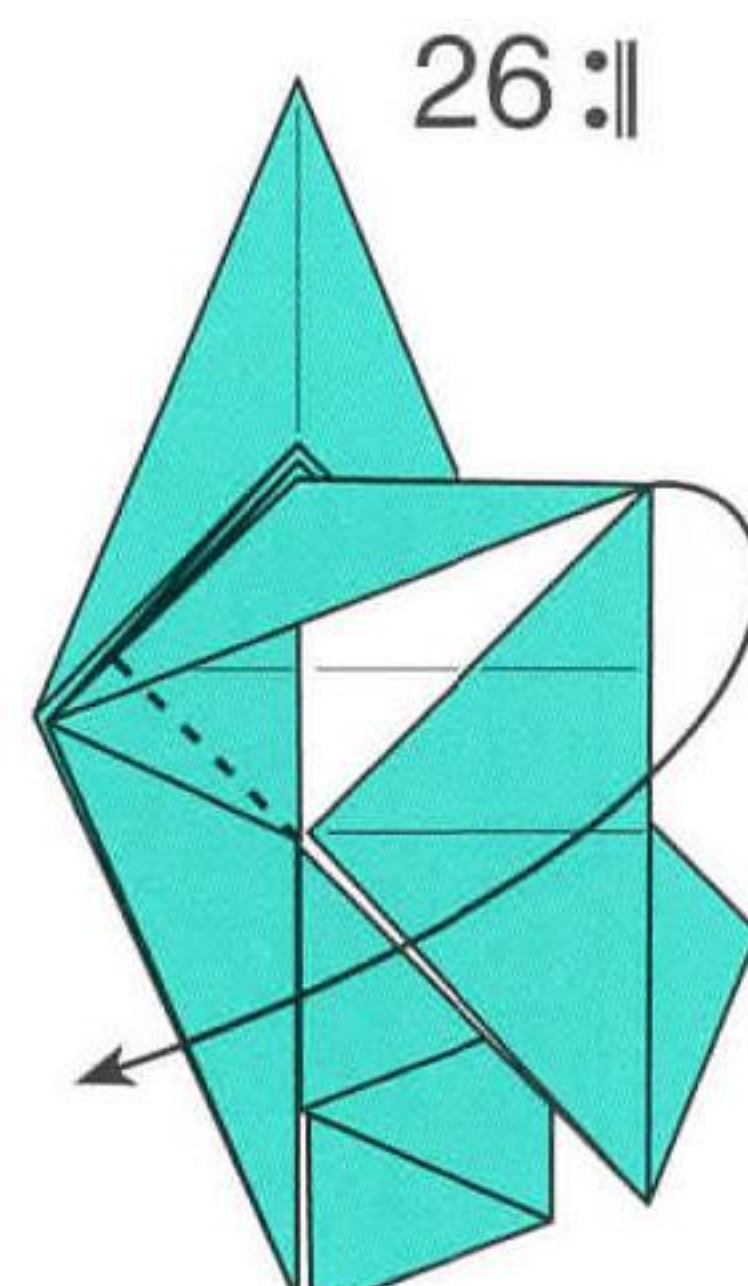
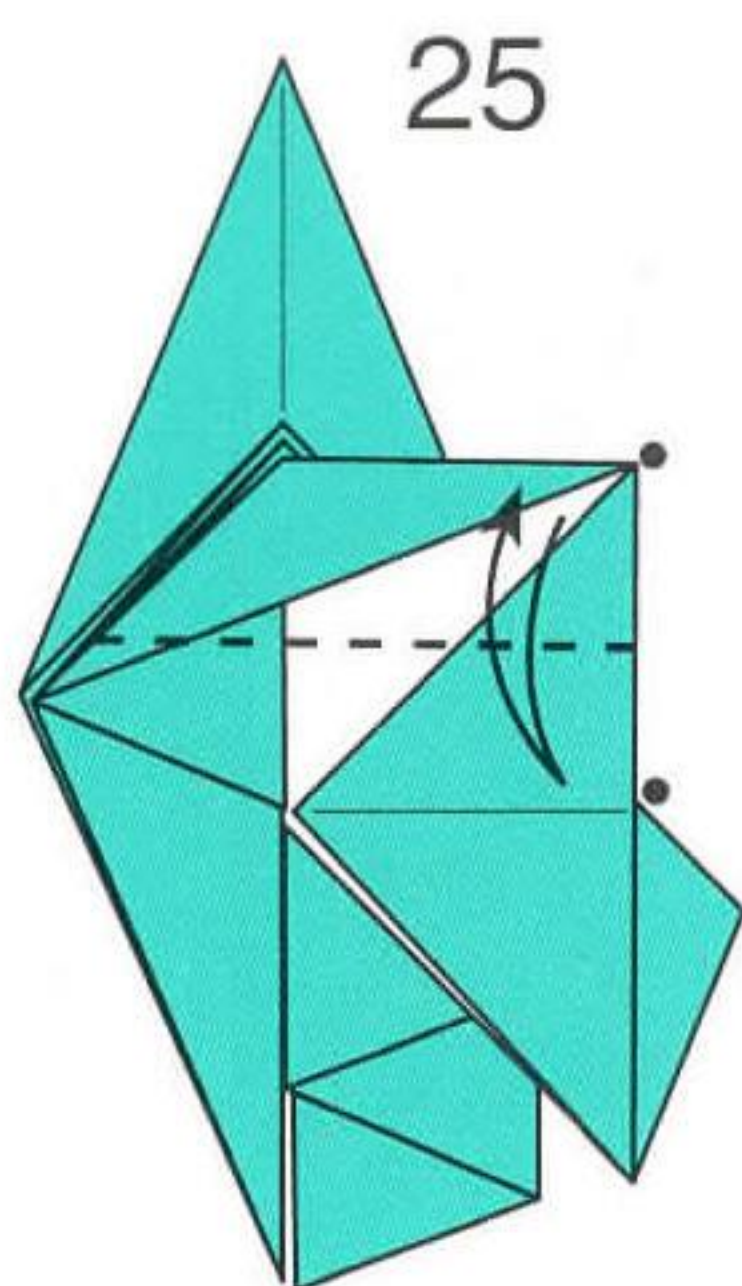
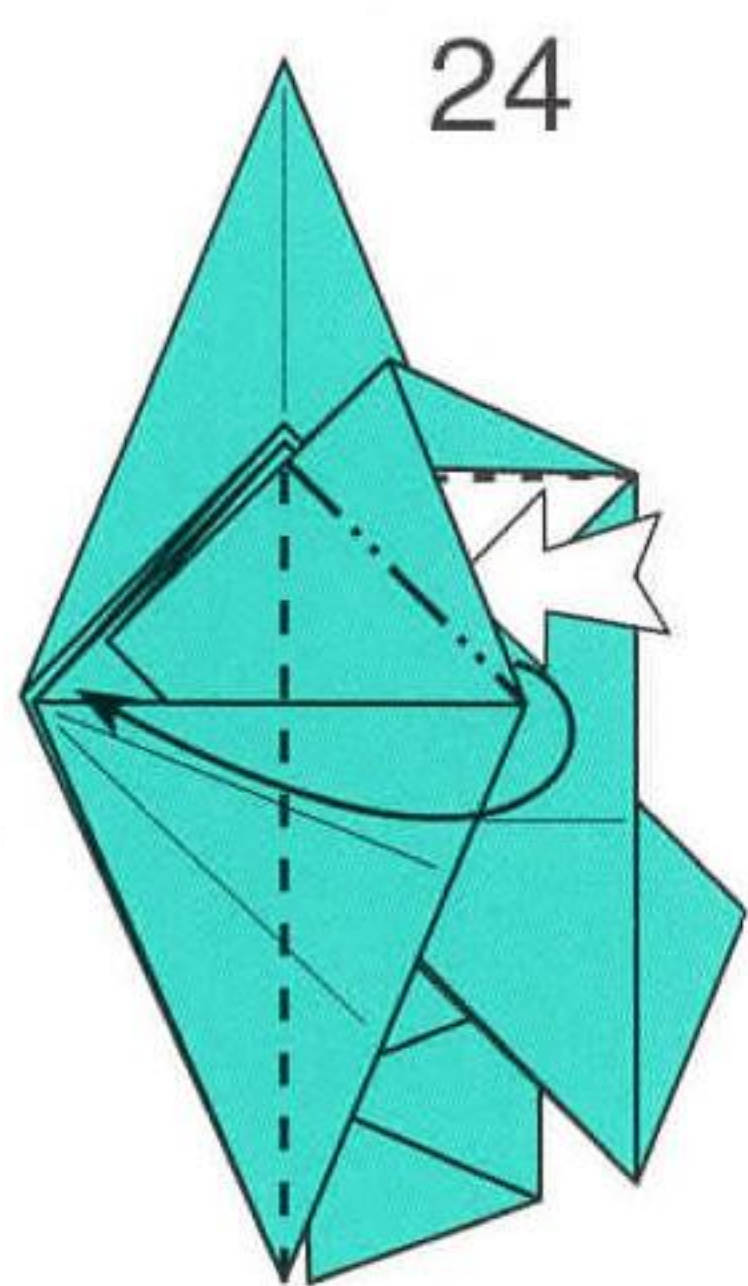
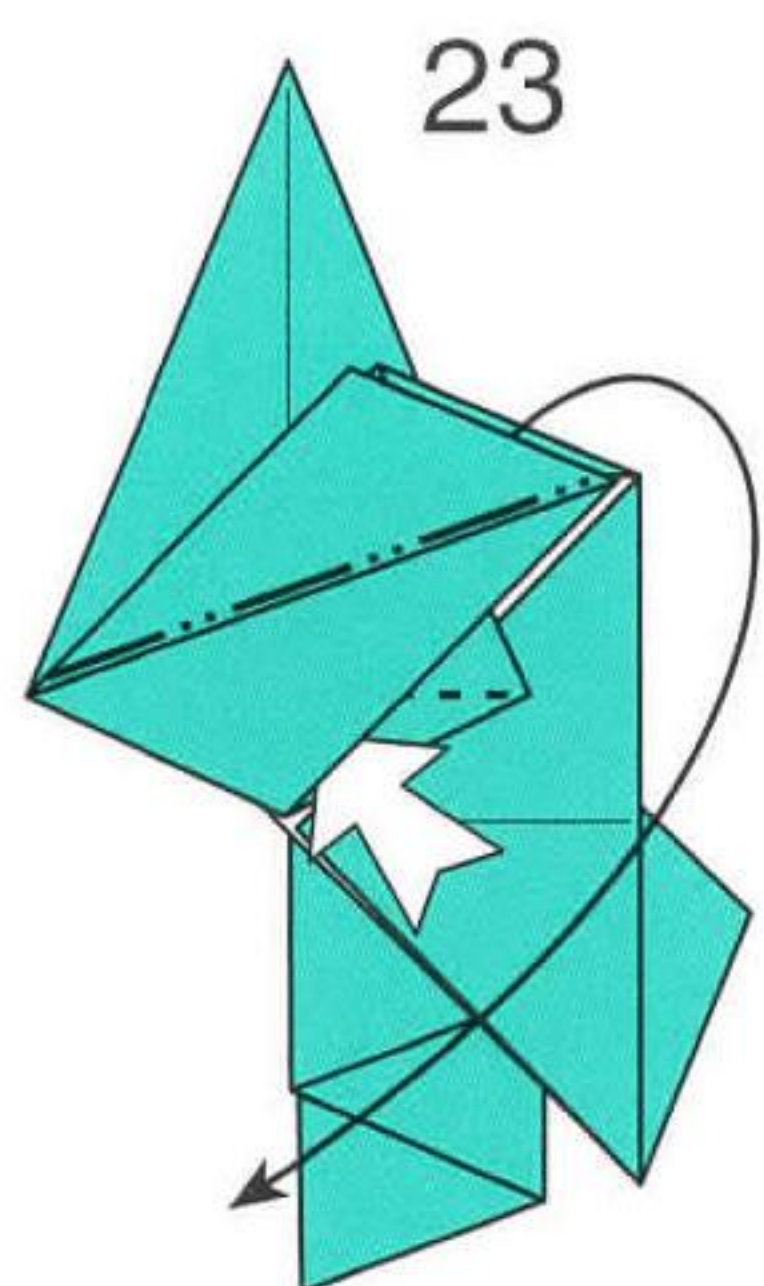


Tree figure (short branches are omitted). The trunk connects the branches.

Another crease pattern for five long points

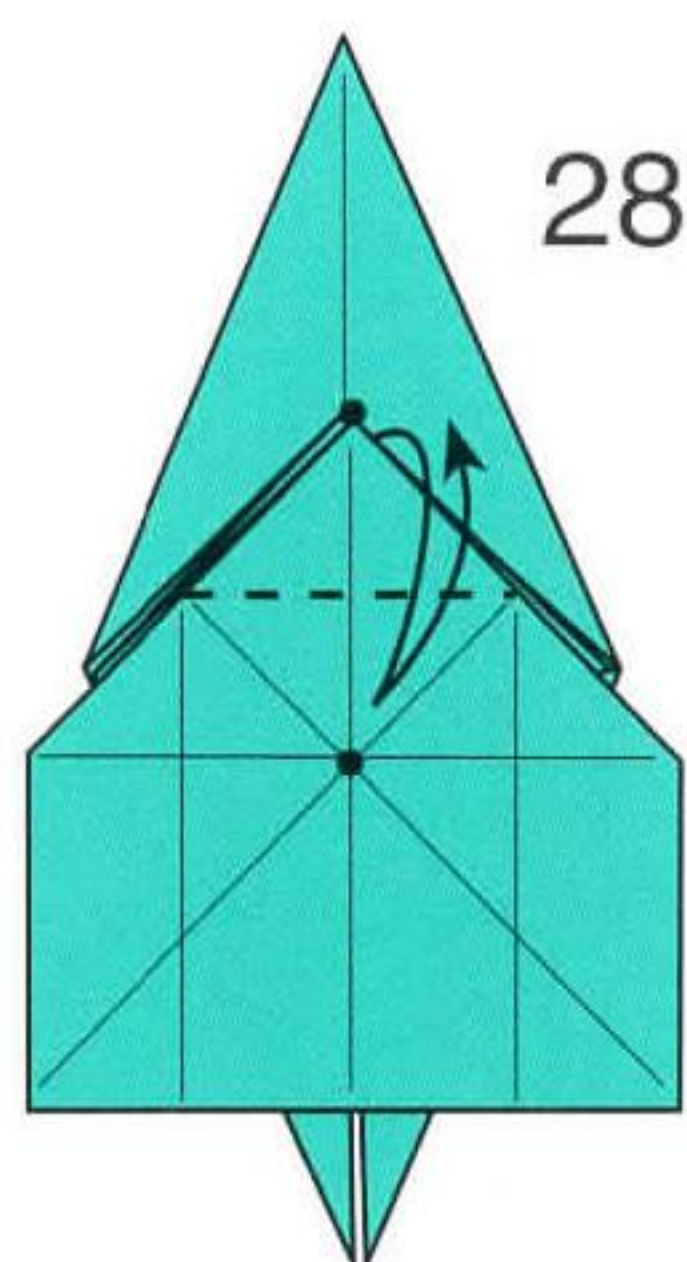




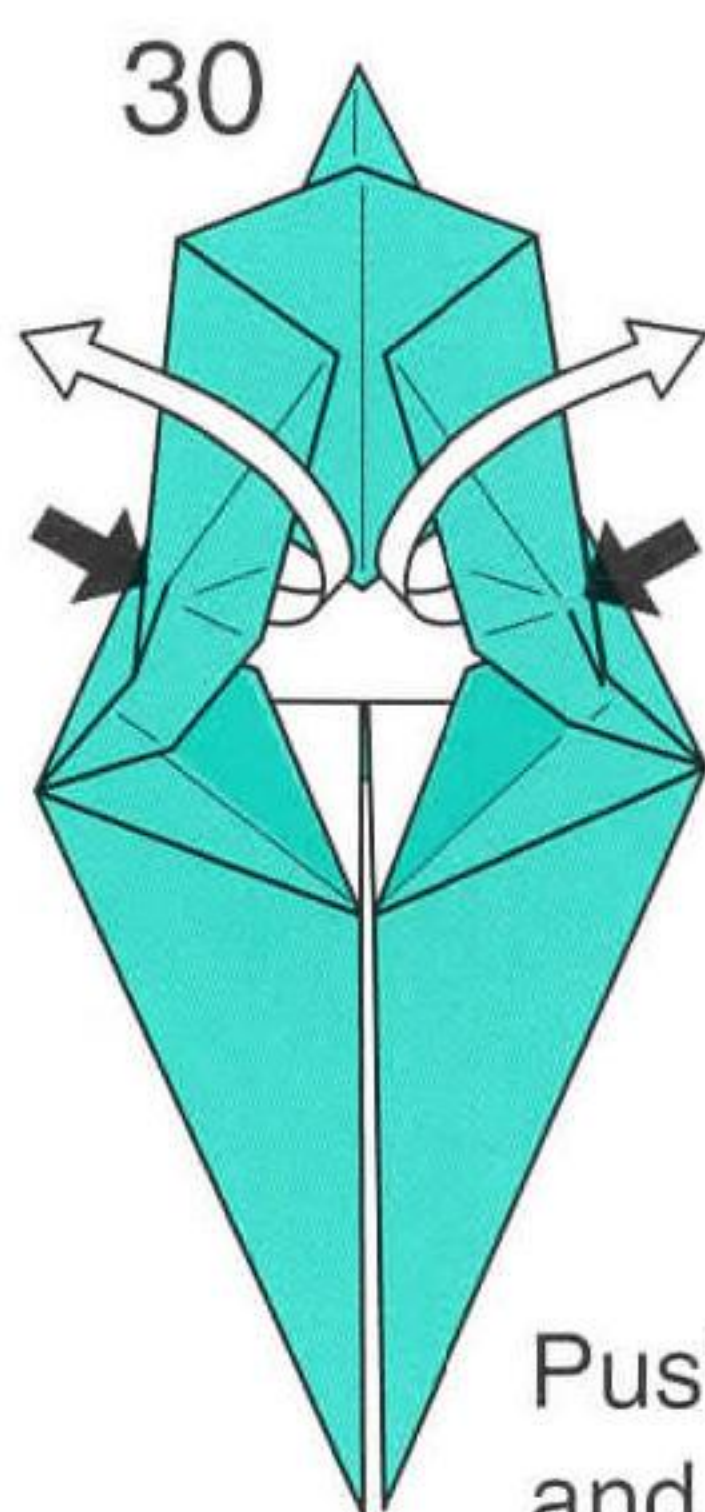
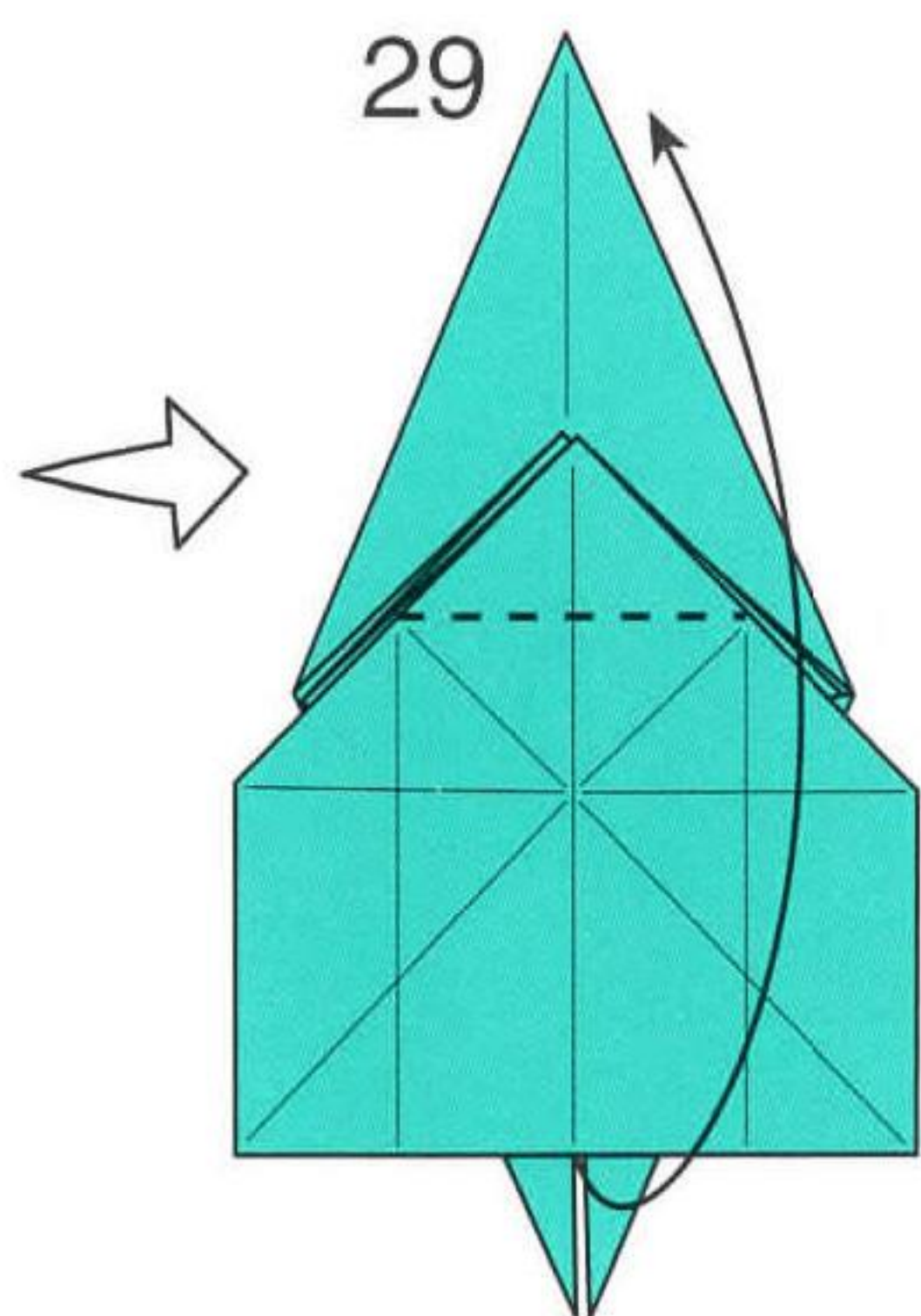


Fold the layers firmly.

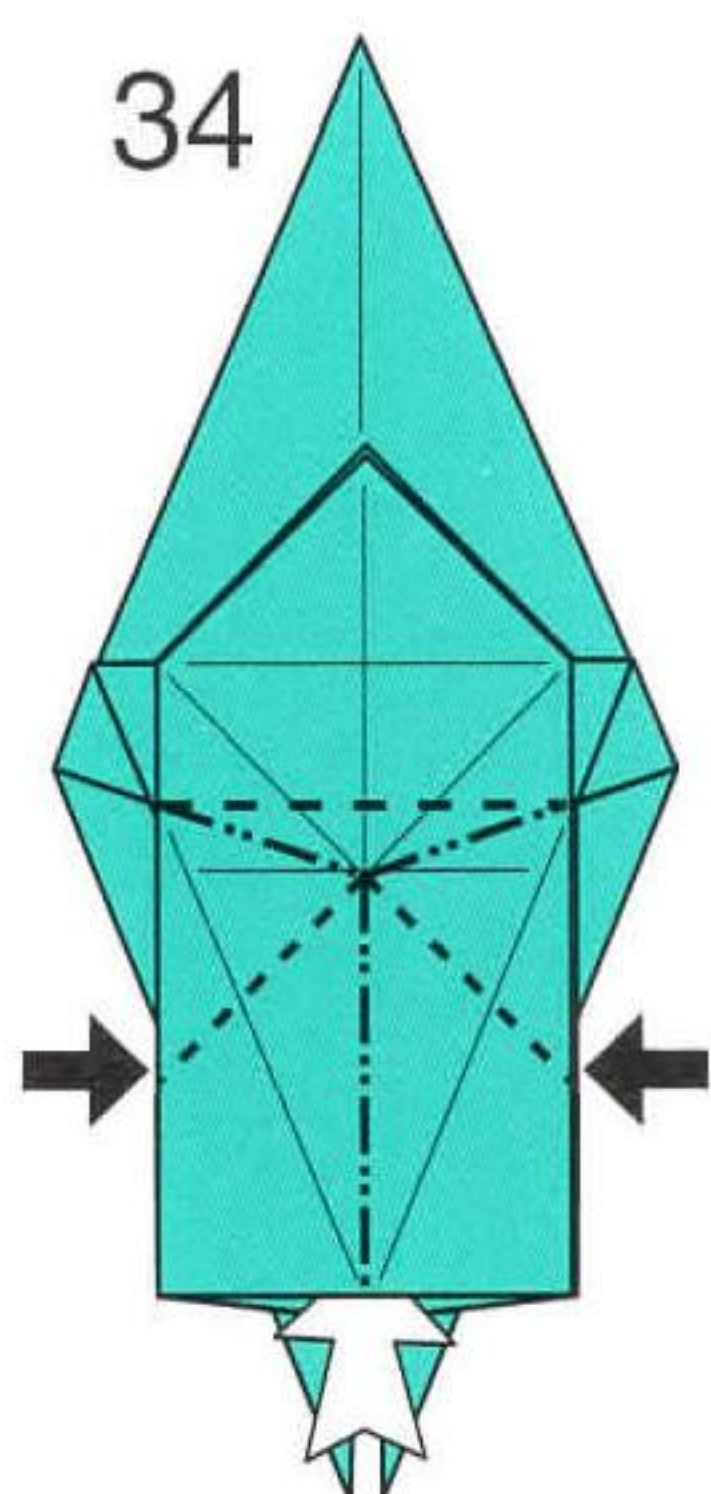
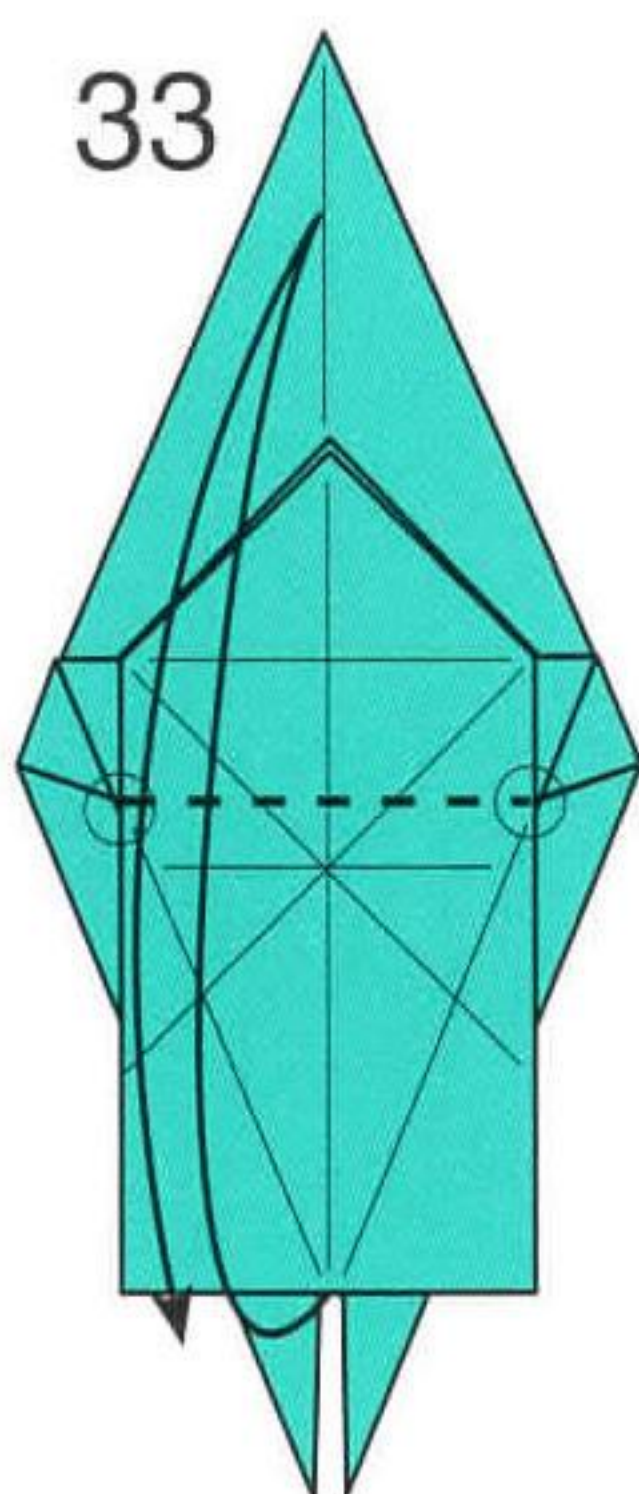
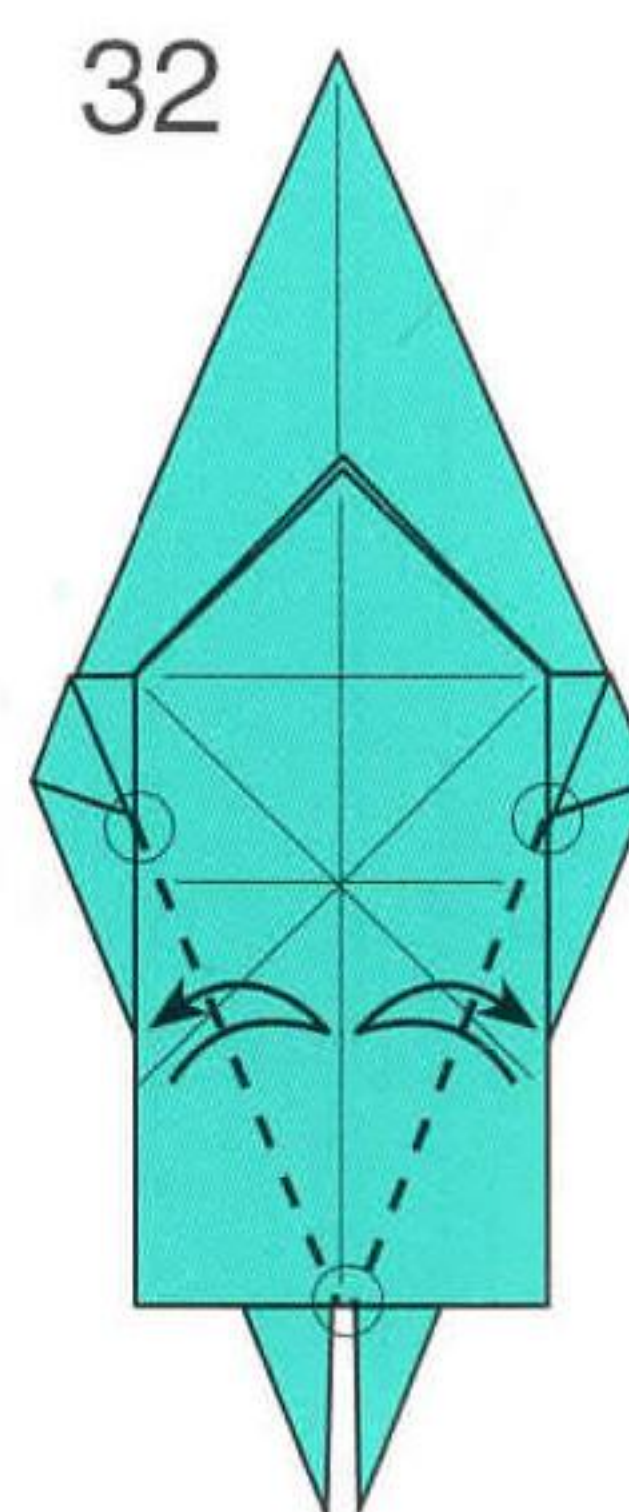
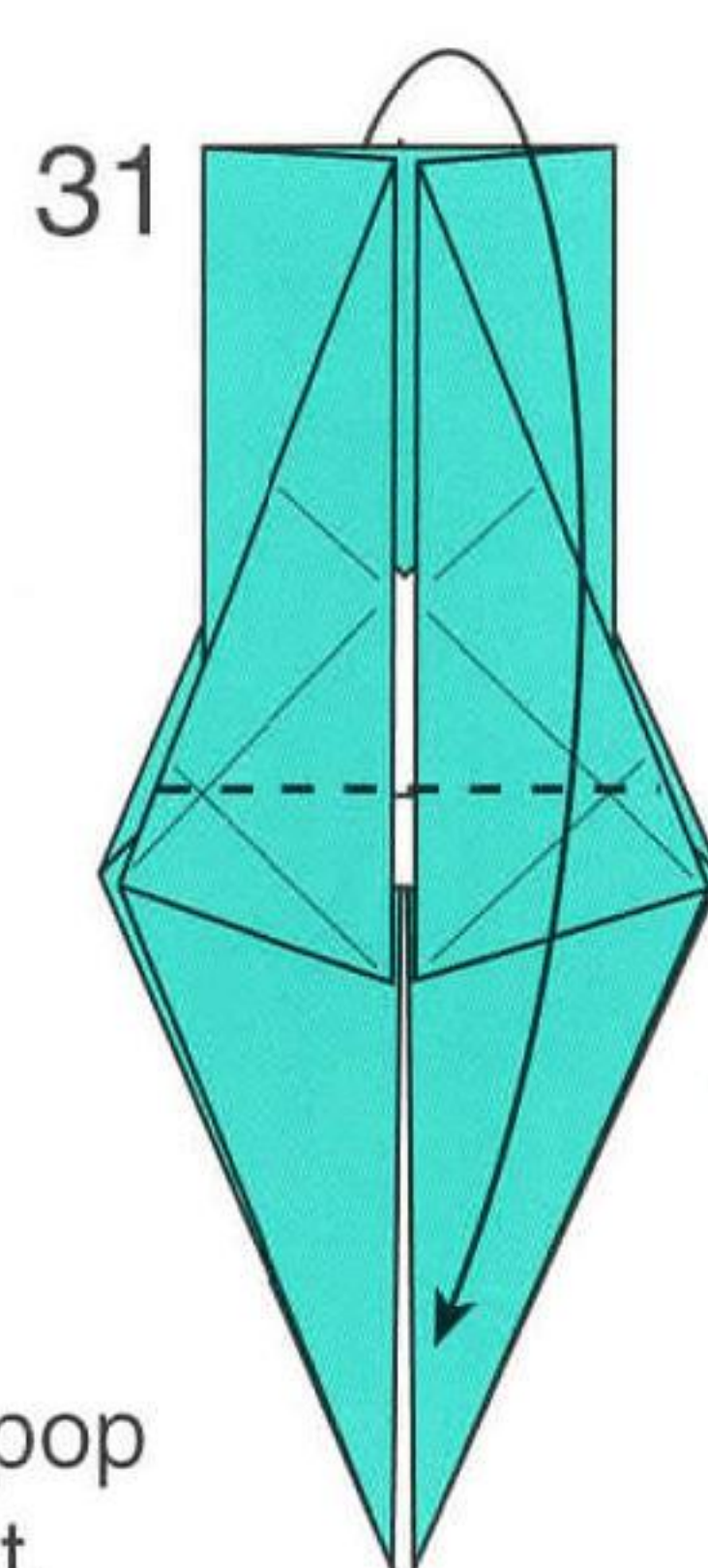
Repeat steps 20-26.



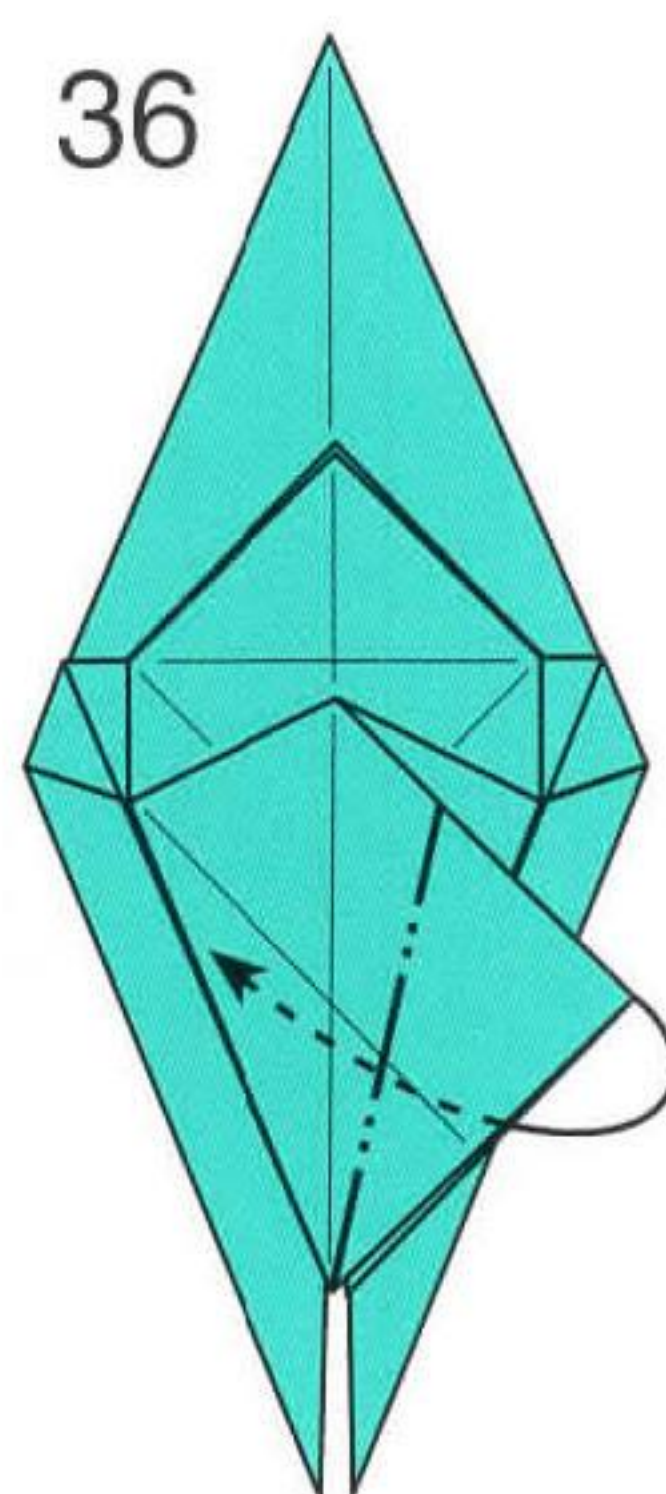
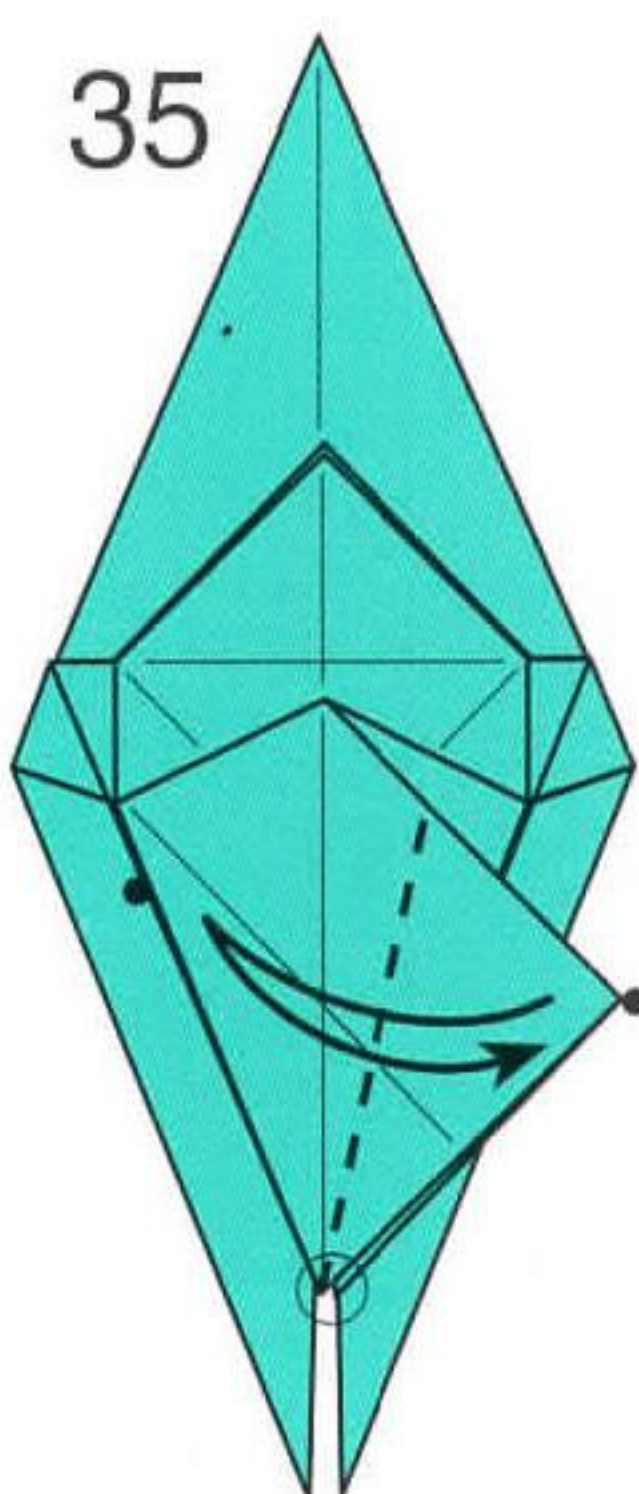
Fold and unfold only the upper layer.



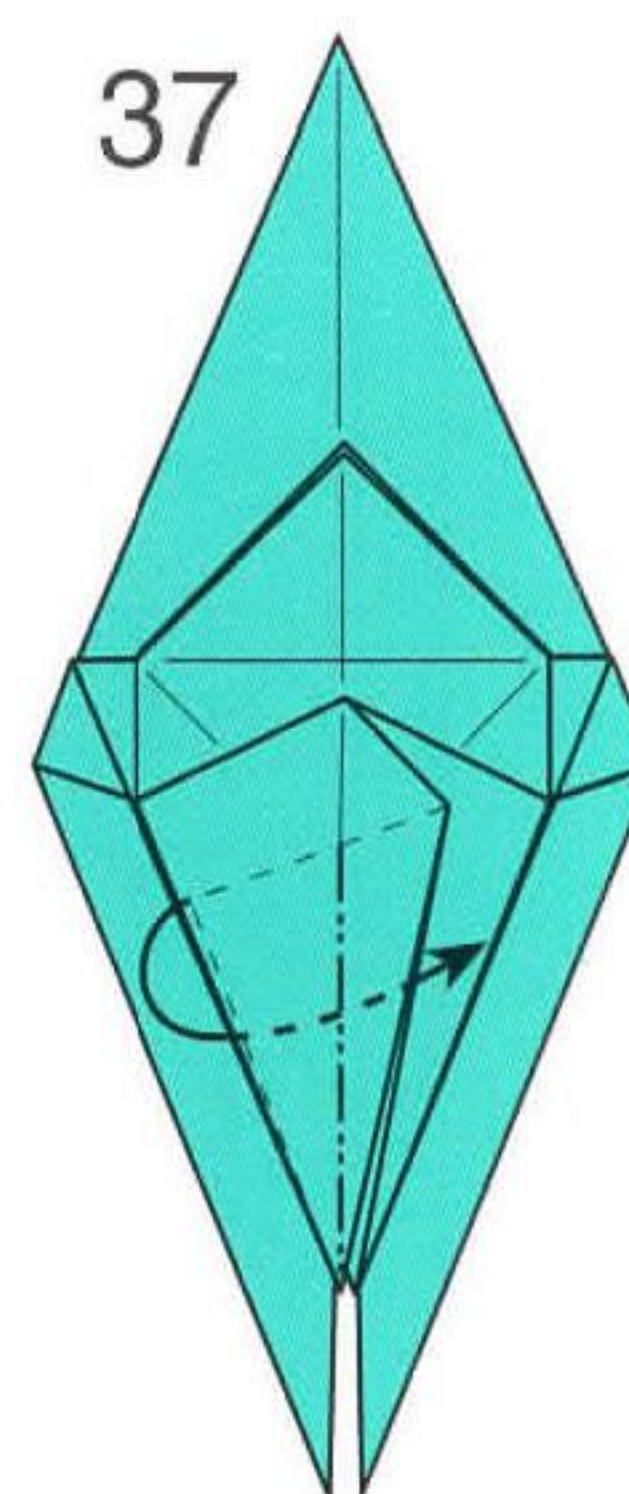
Push in to pop and fold flat.



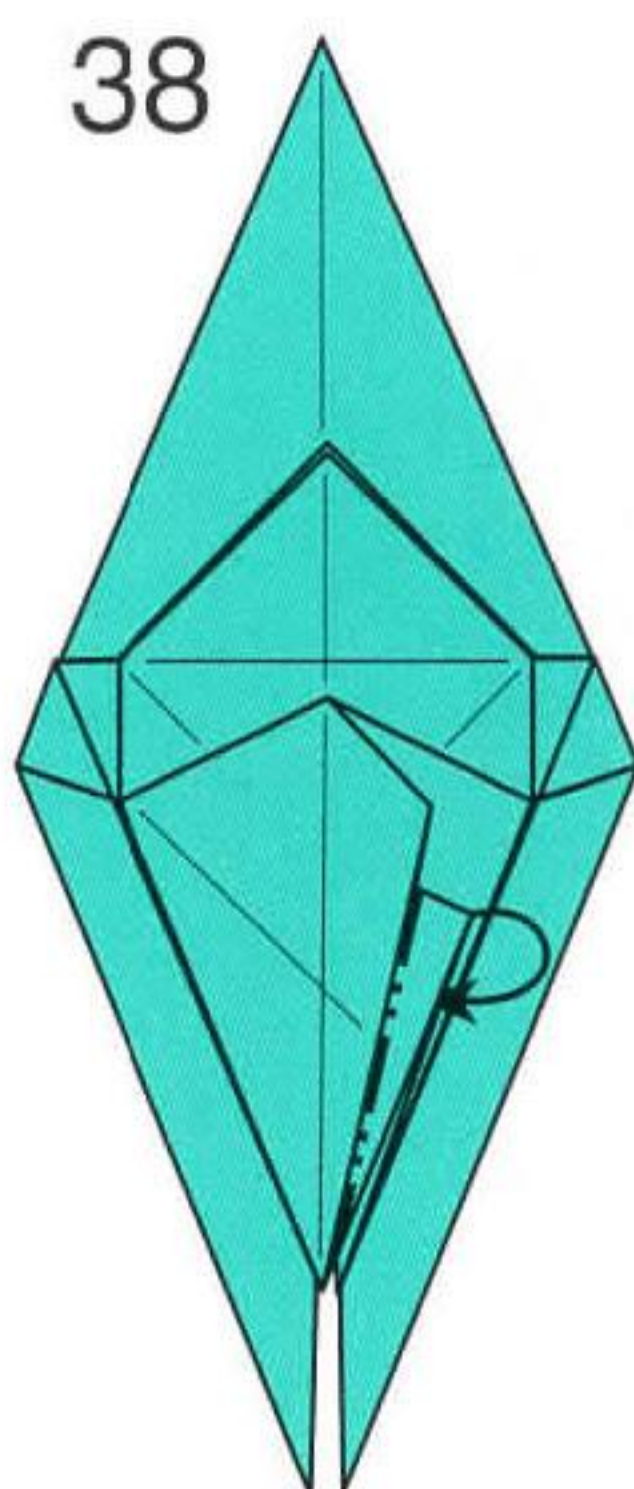
Pinch to make an isosceles right triangle.



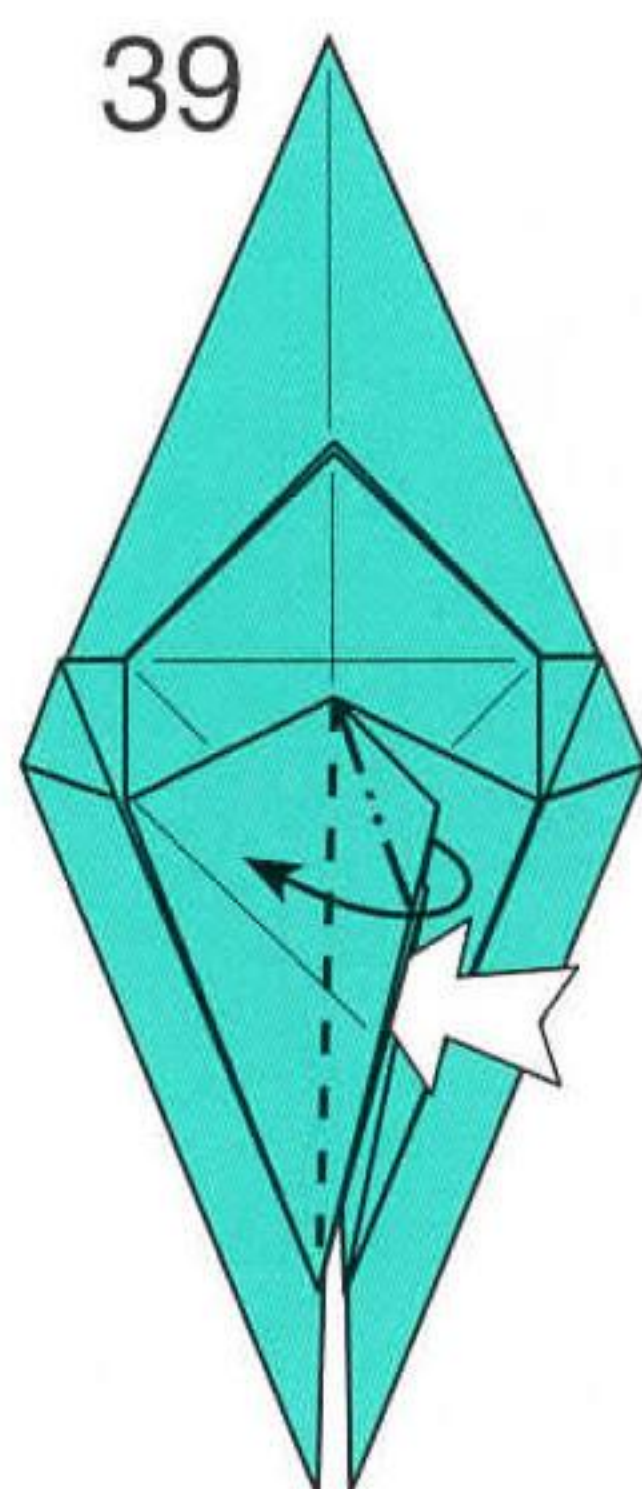
Inside reverse-fold



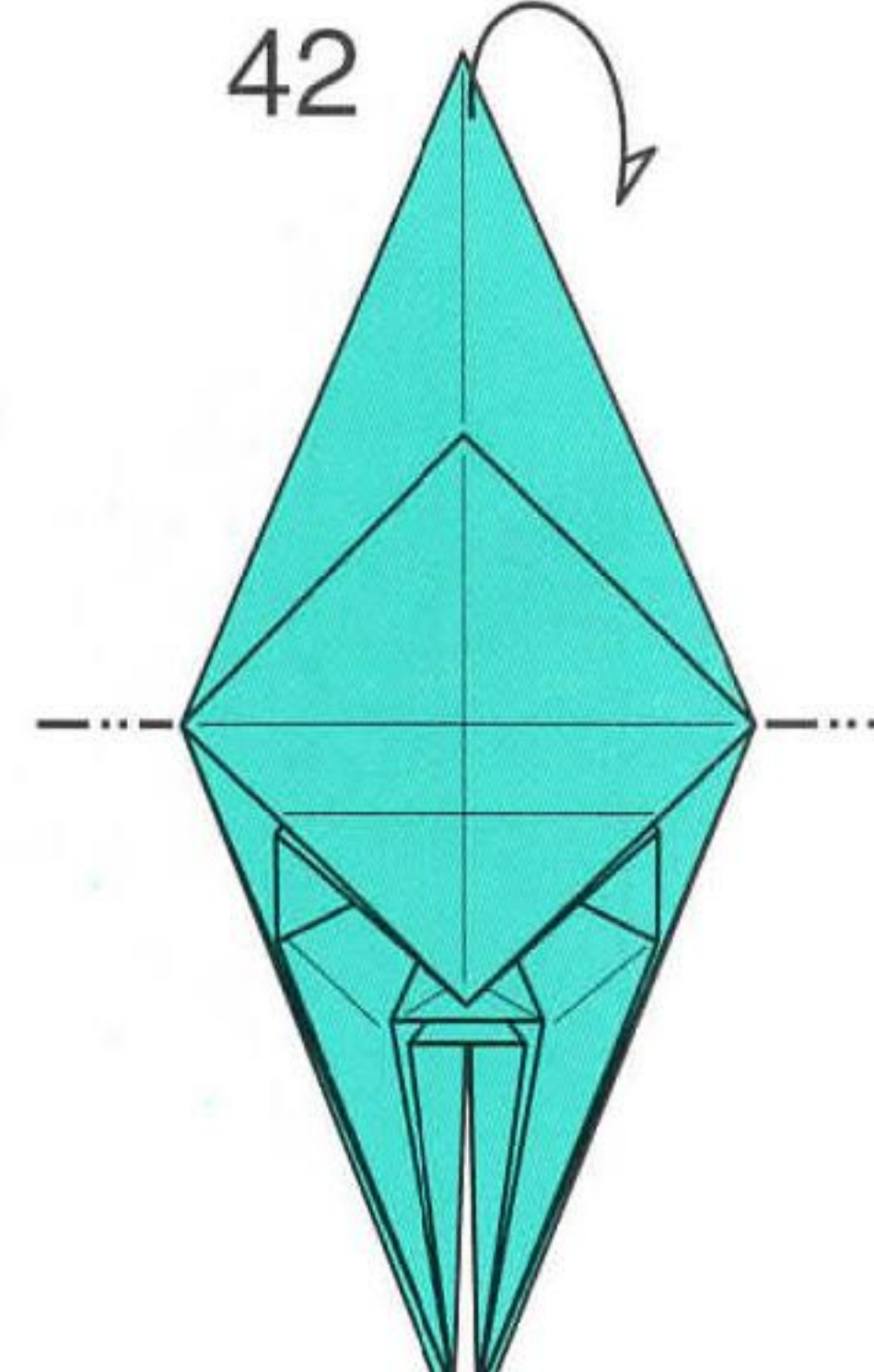
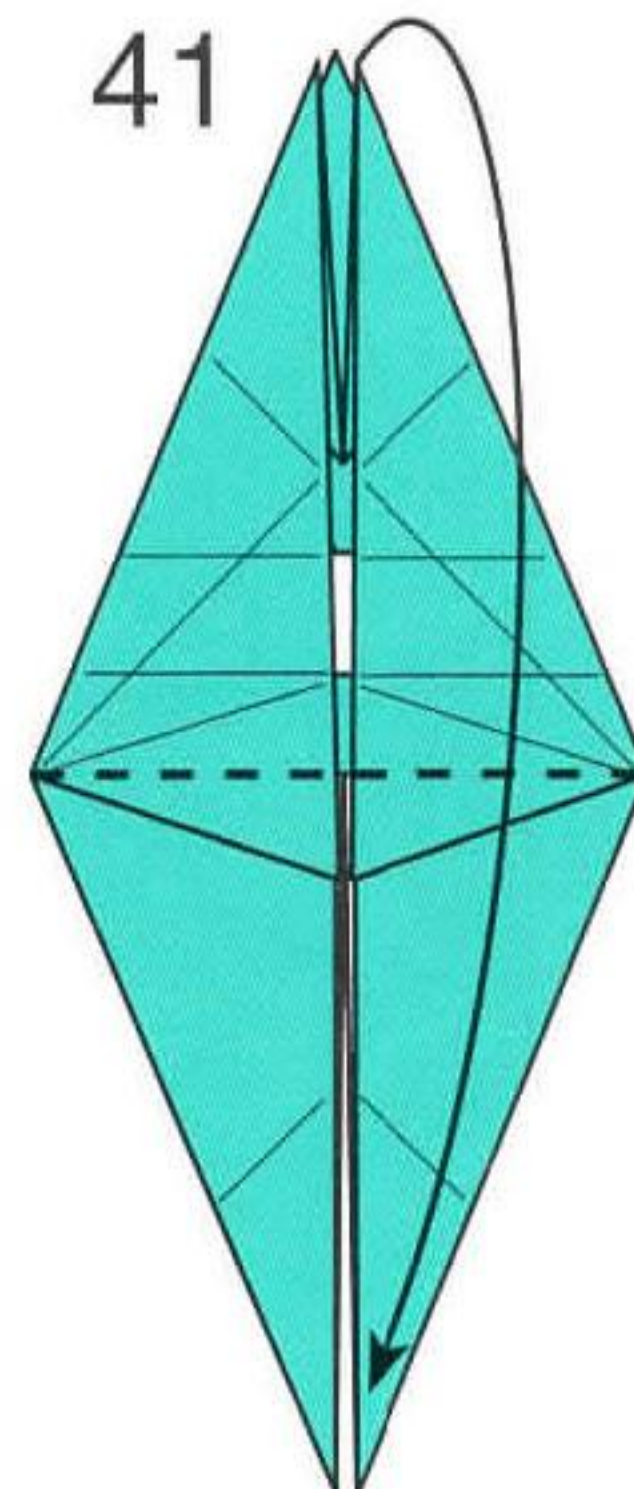
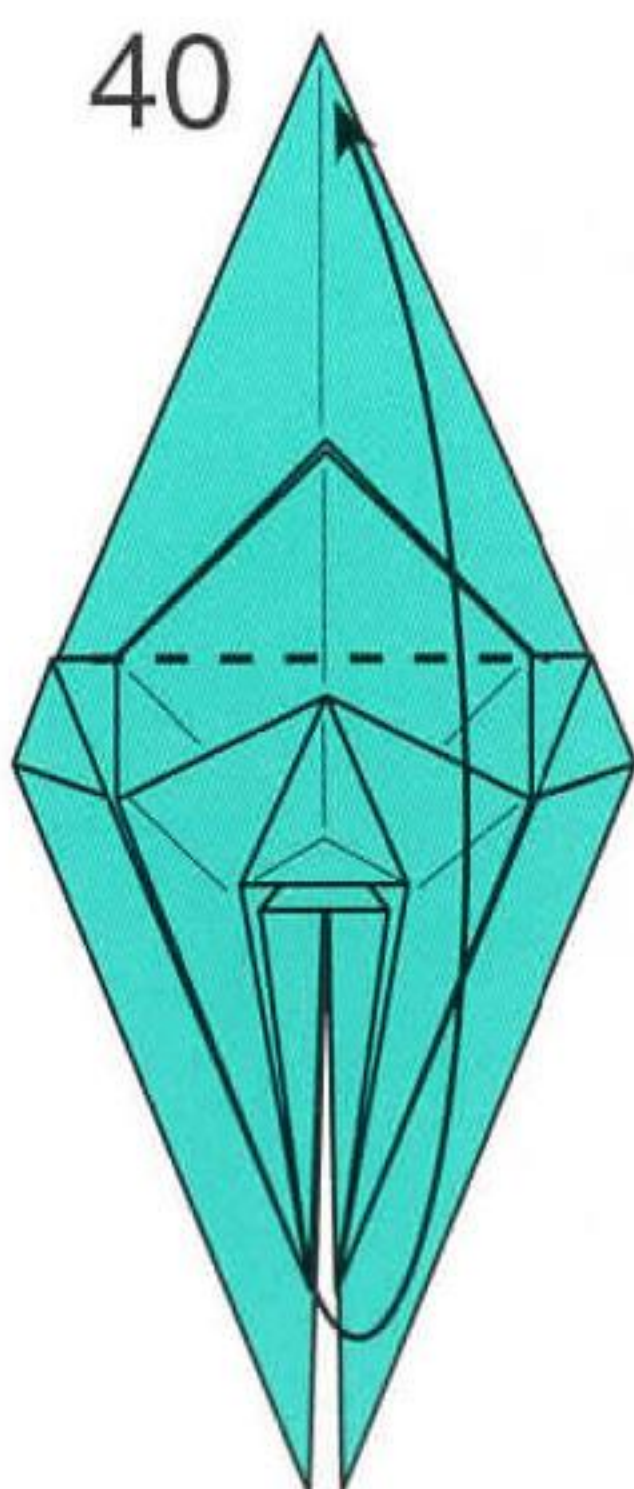
Inside reverse-fold inside



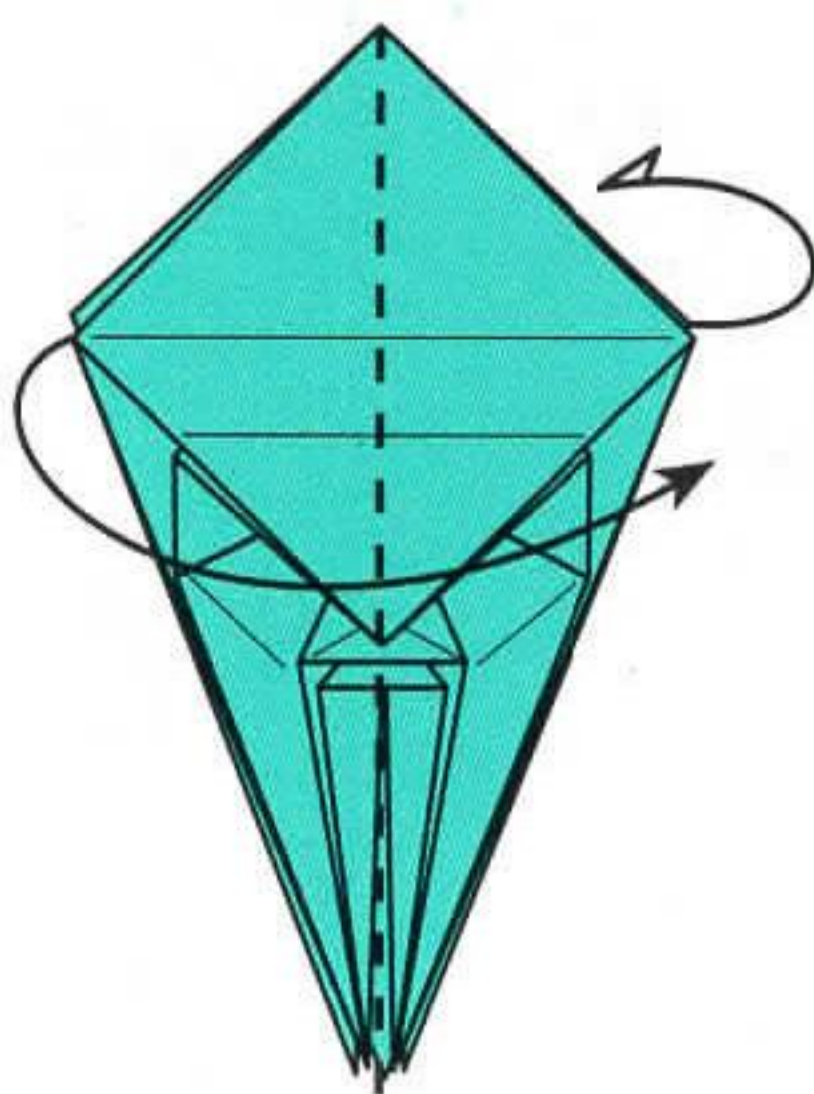
Inside reverse-fold



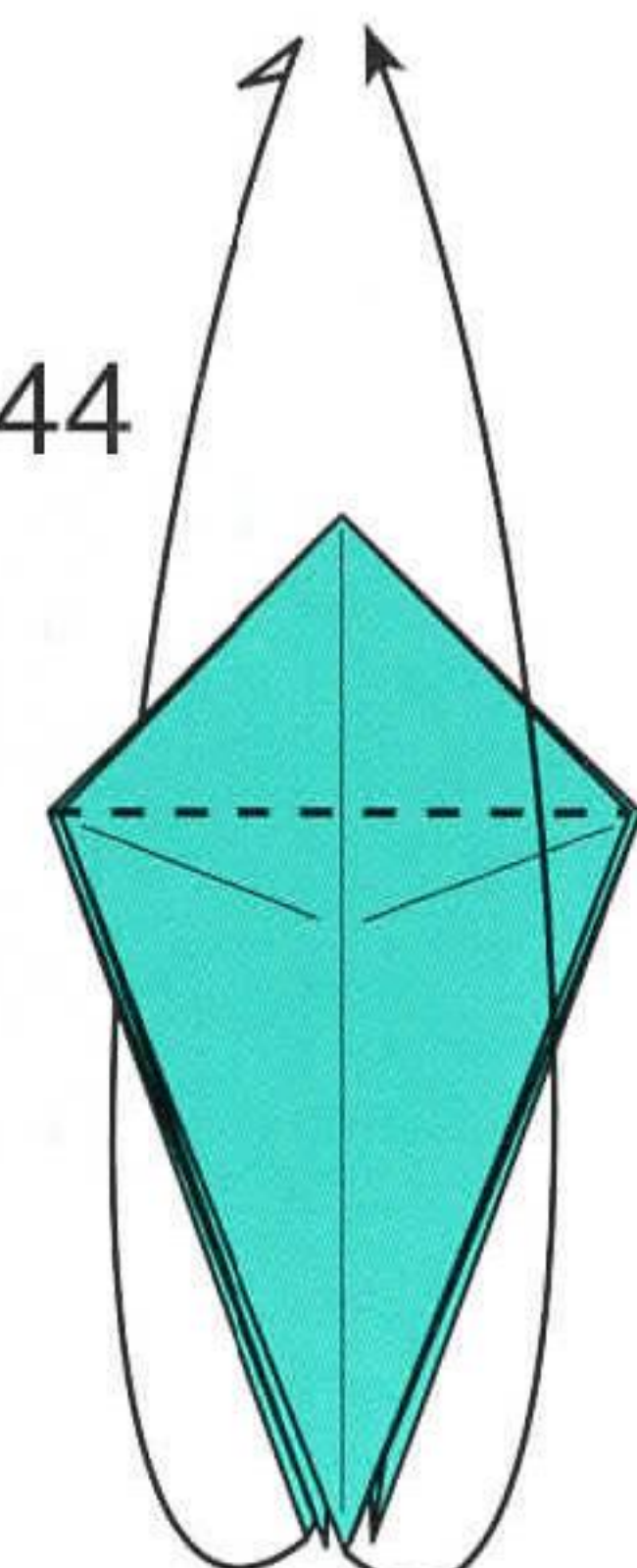
Squash so that the model is symmetric.



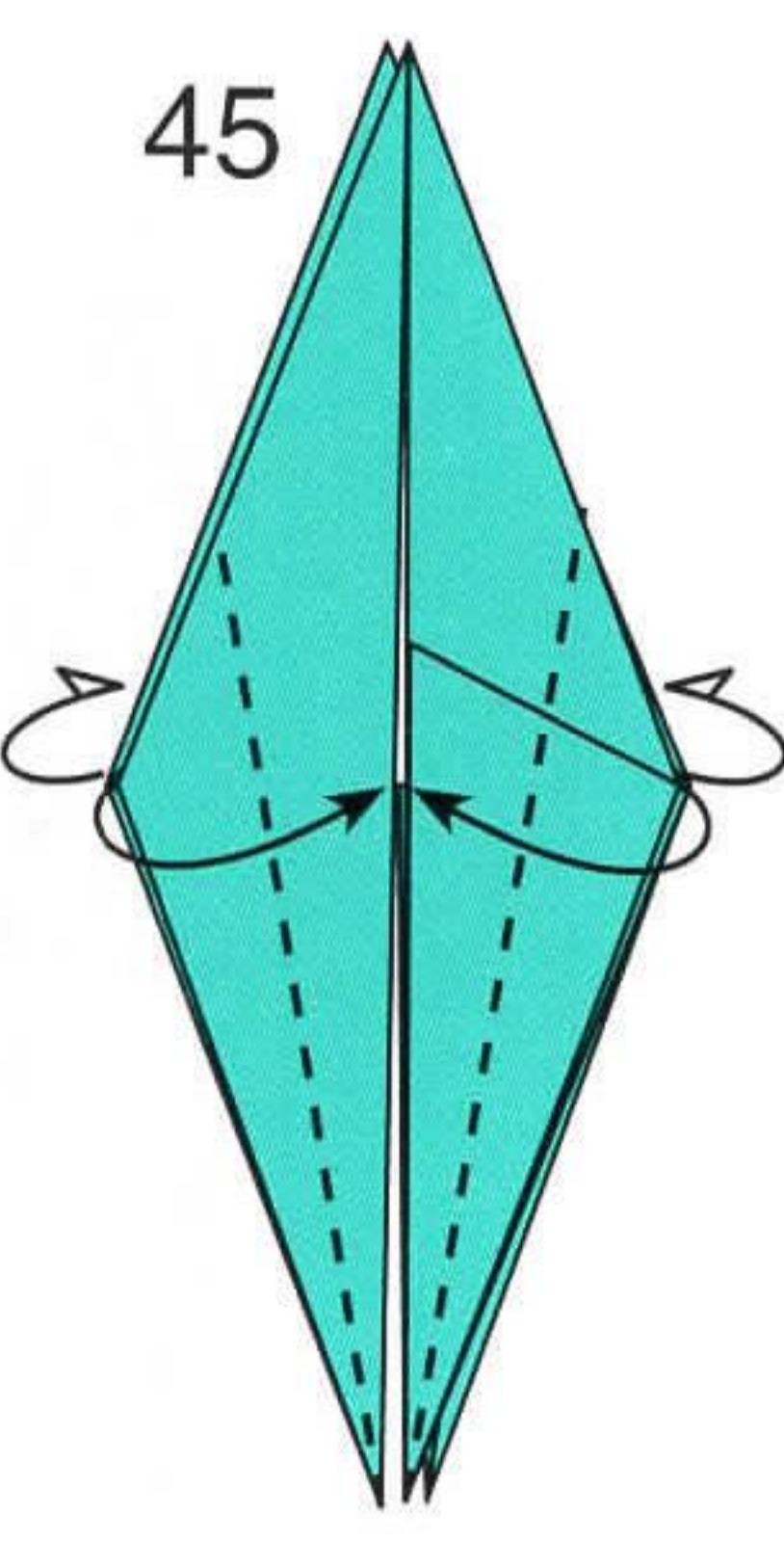
43



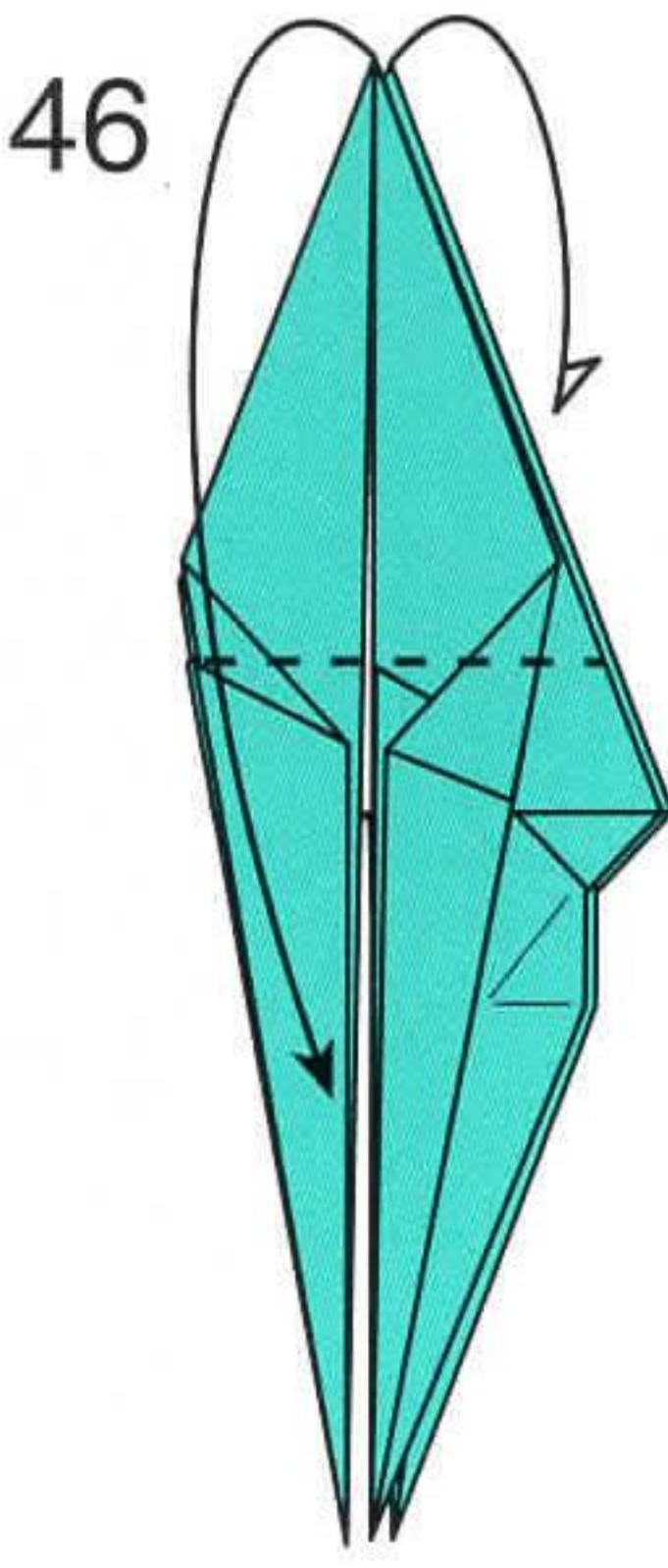
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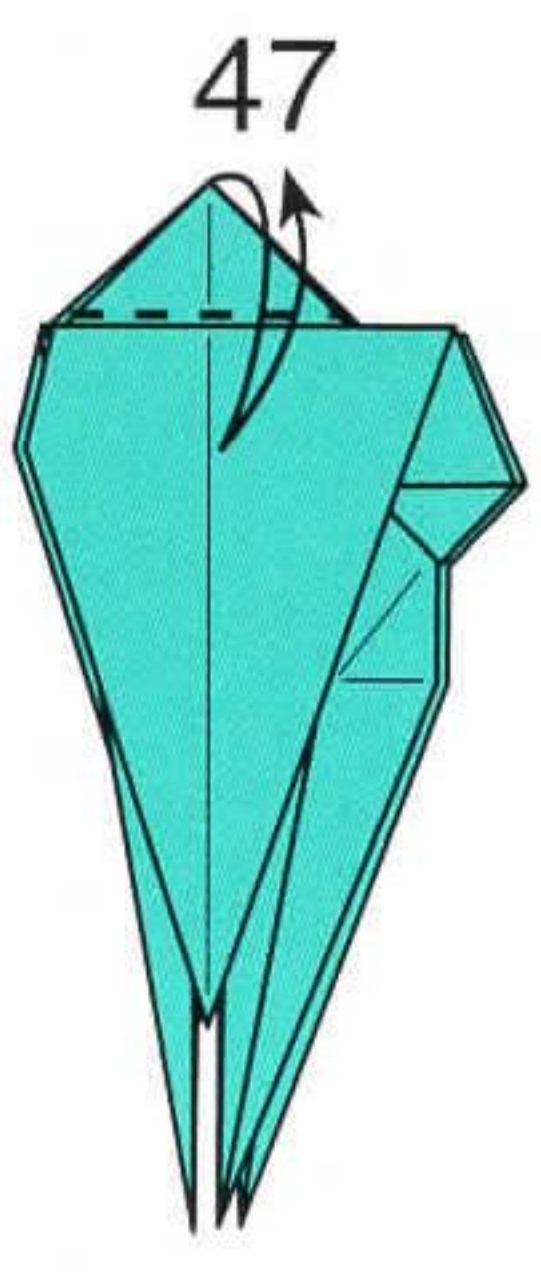
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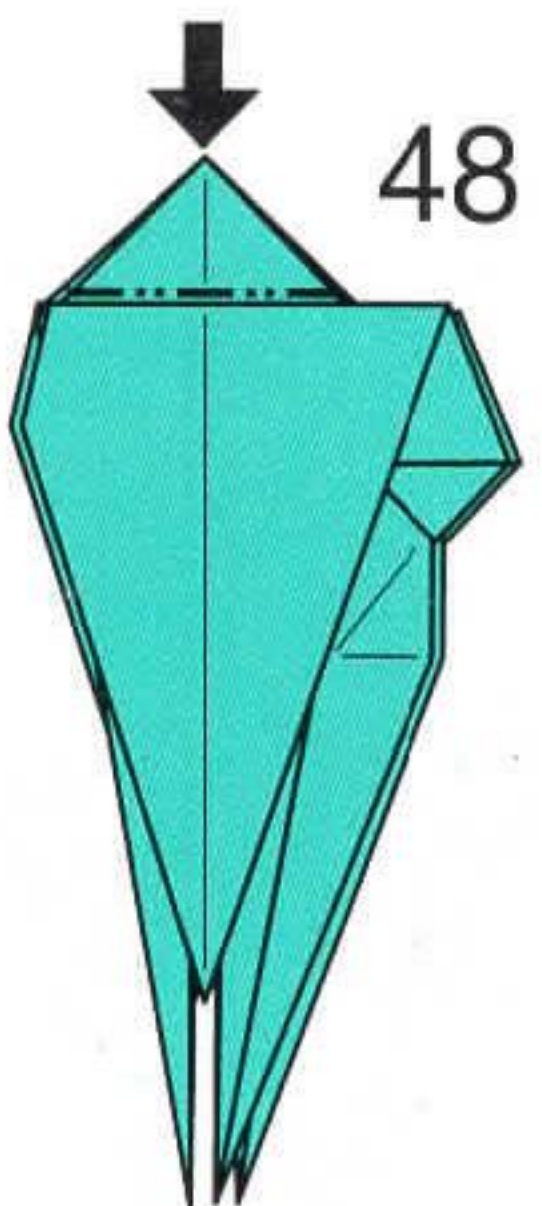
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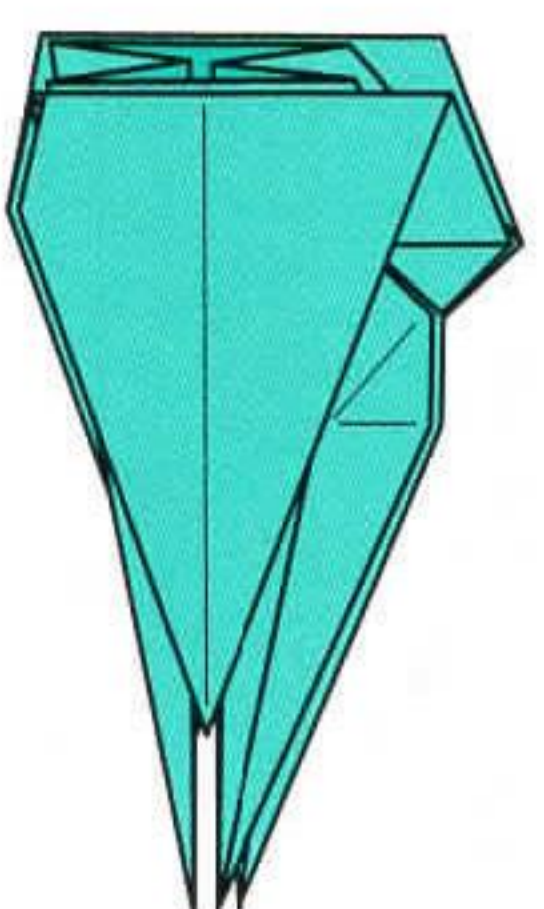
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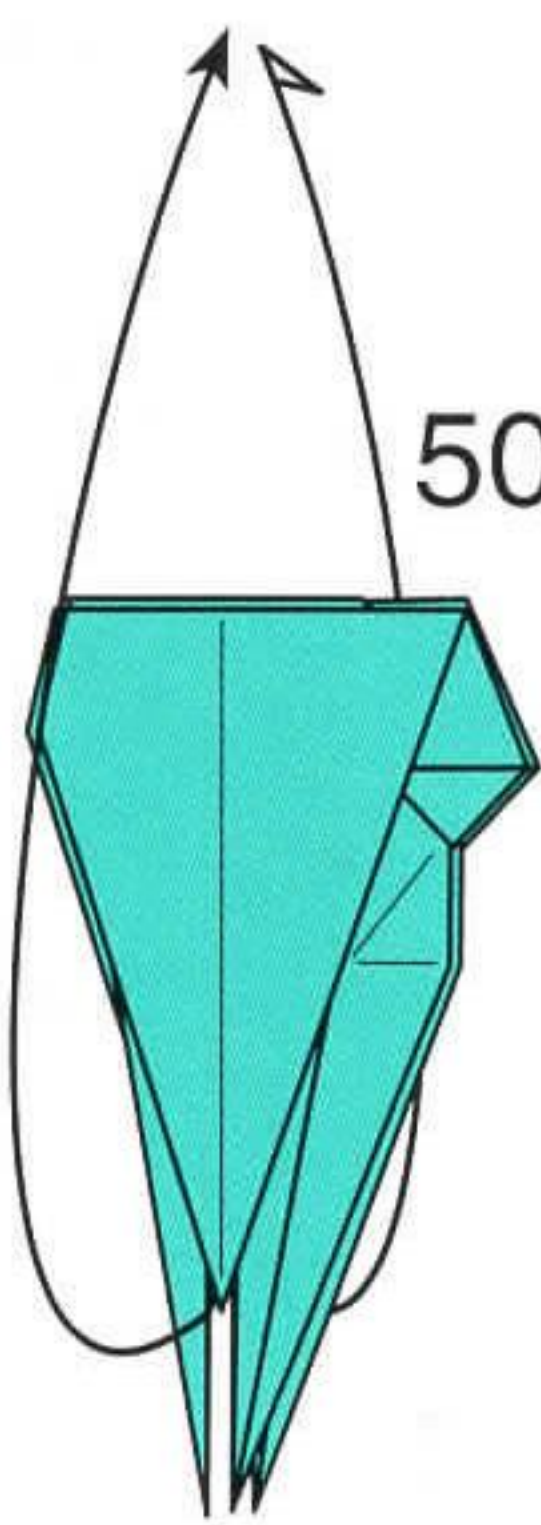
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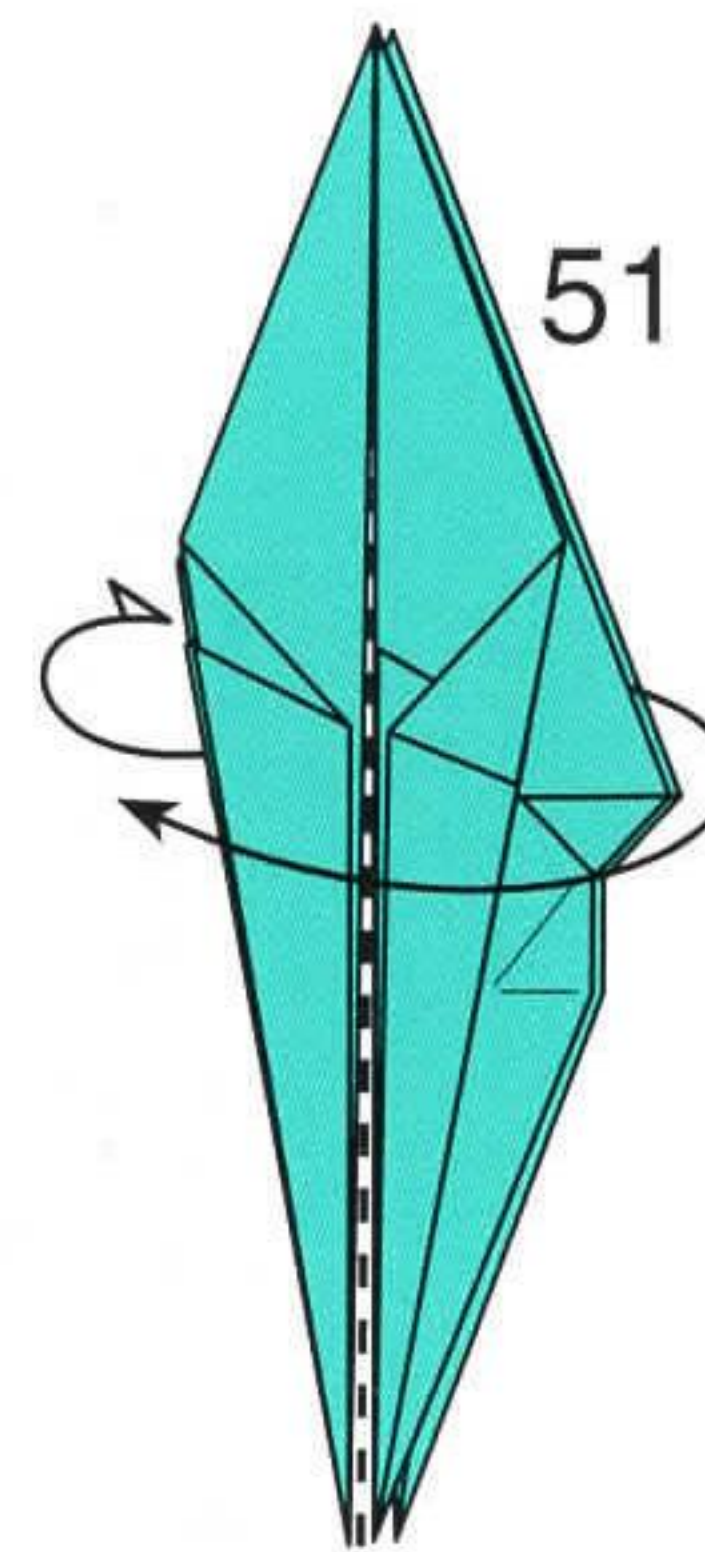
49



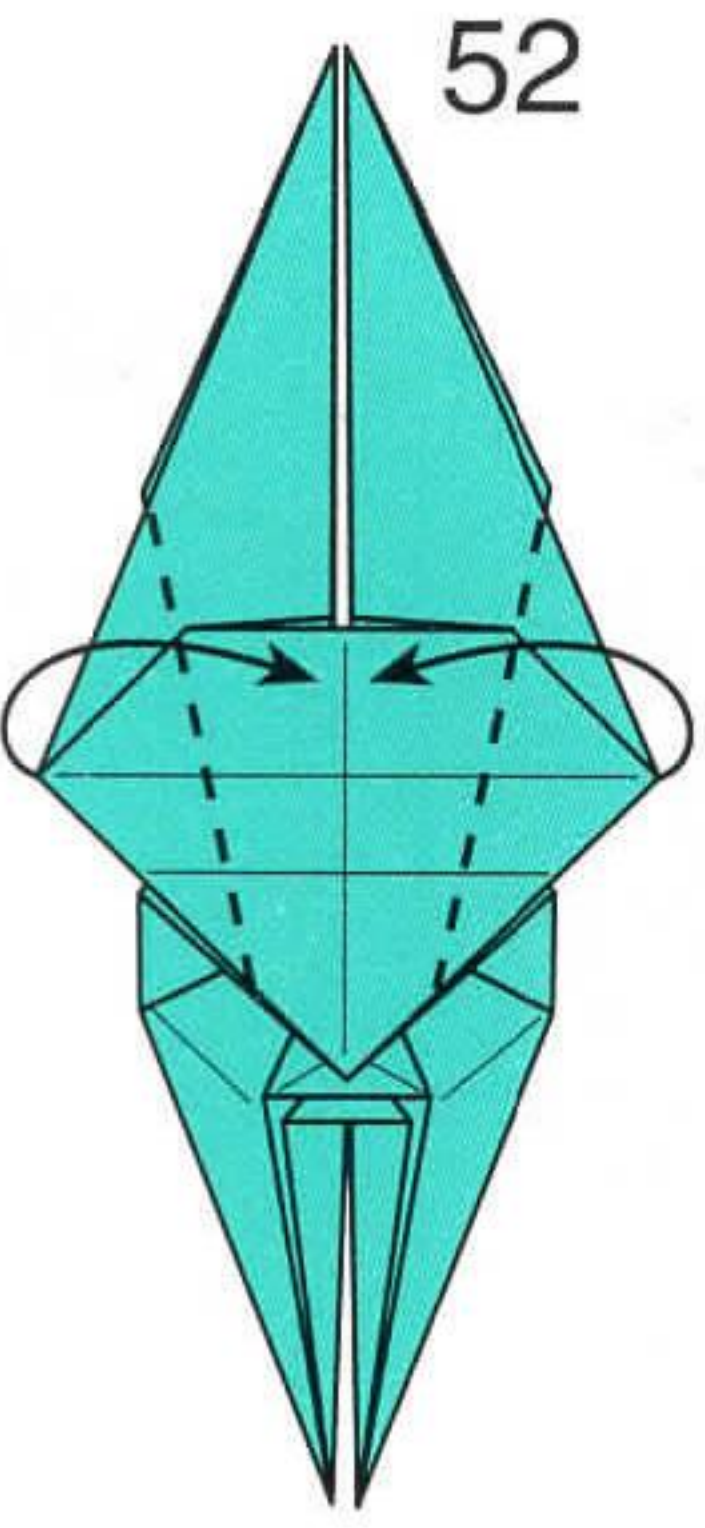
50



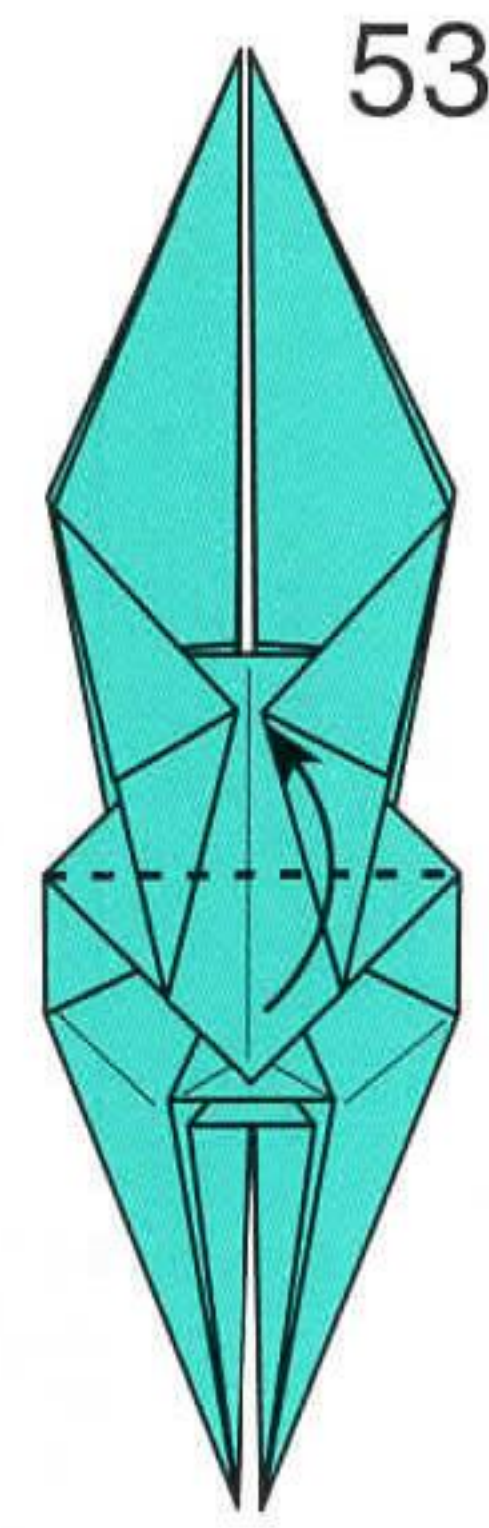
51



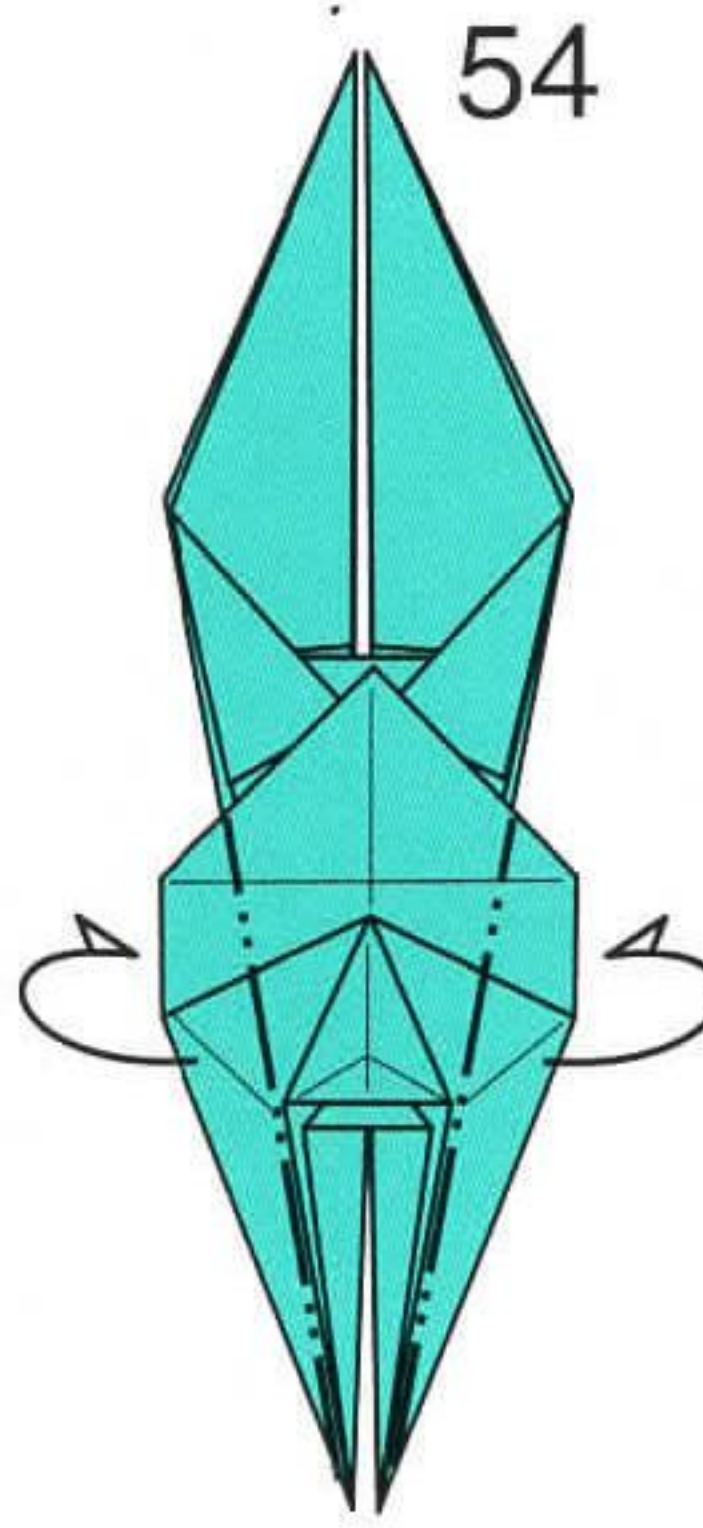
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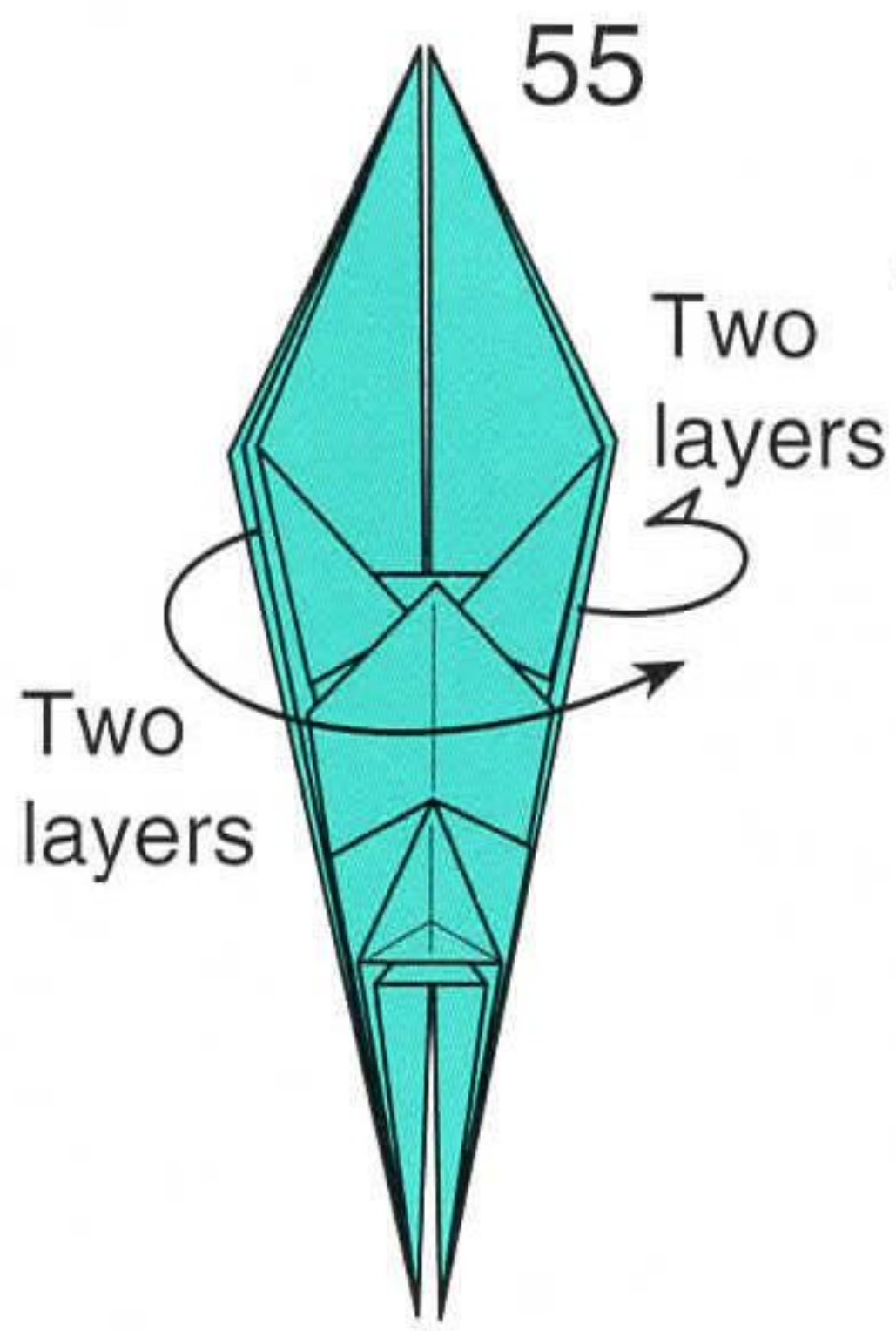
53



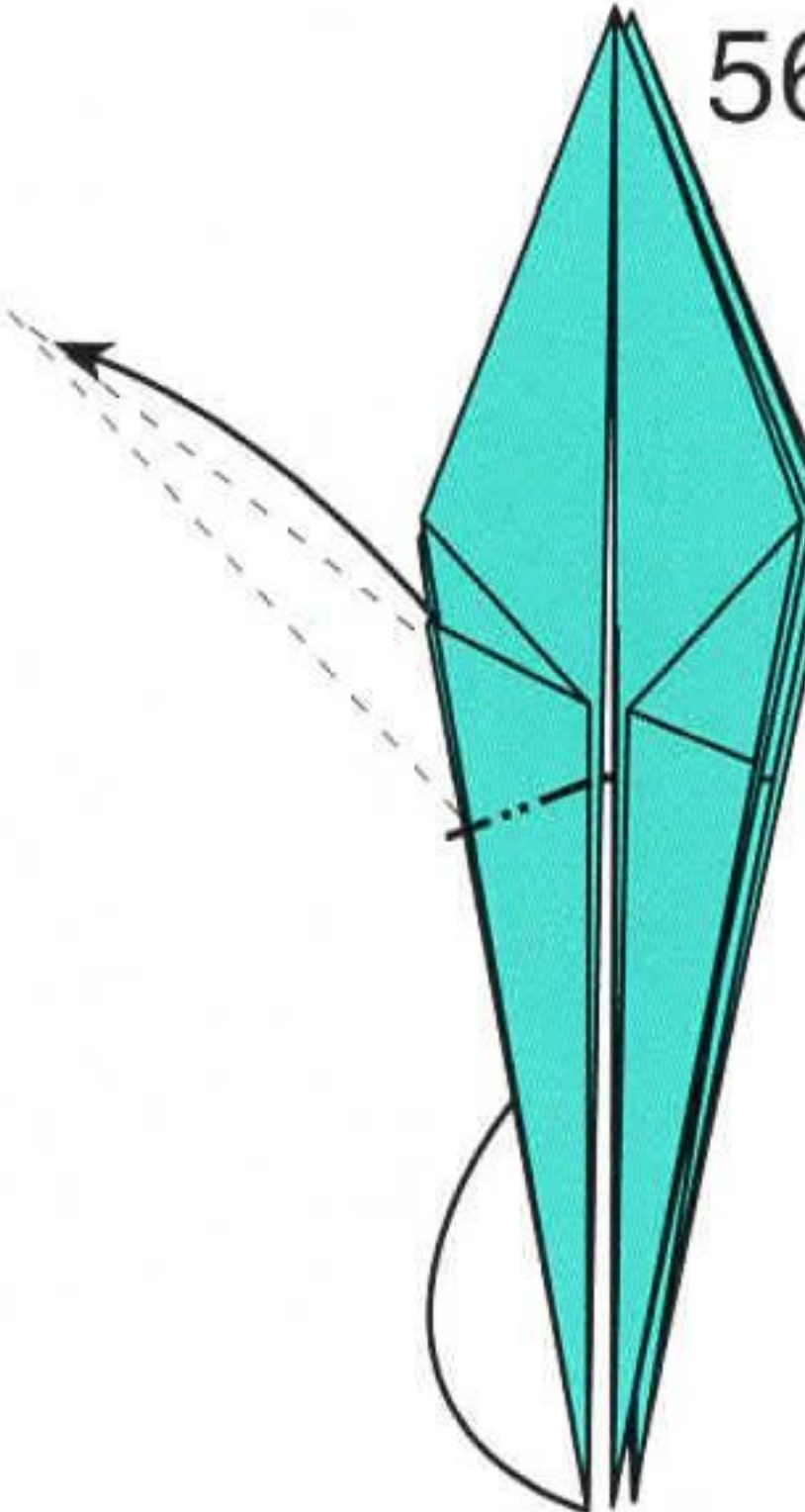
54



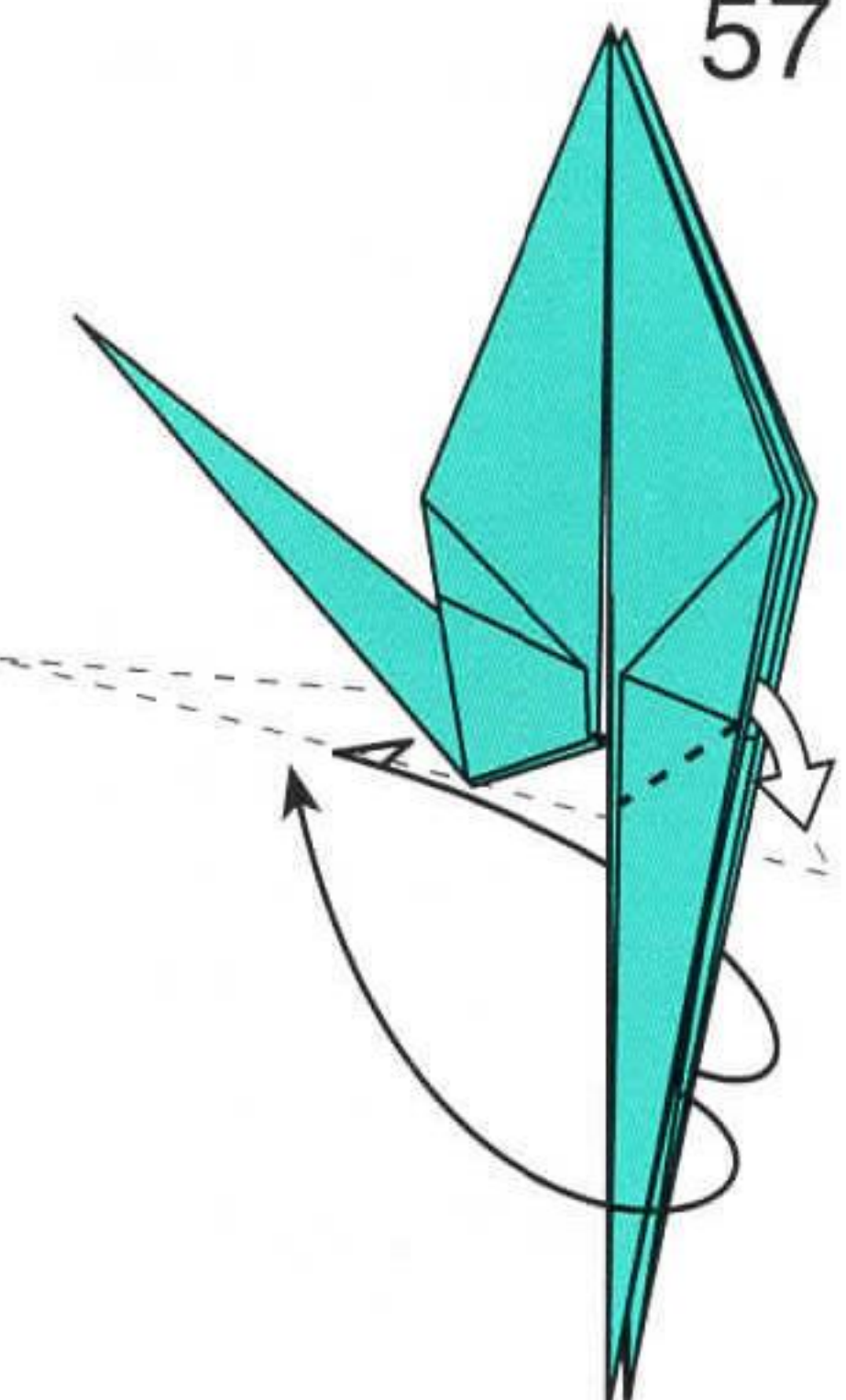
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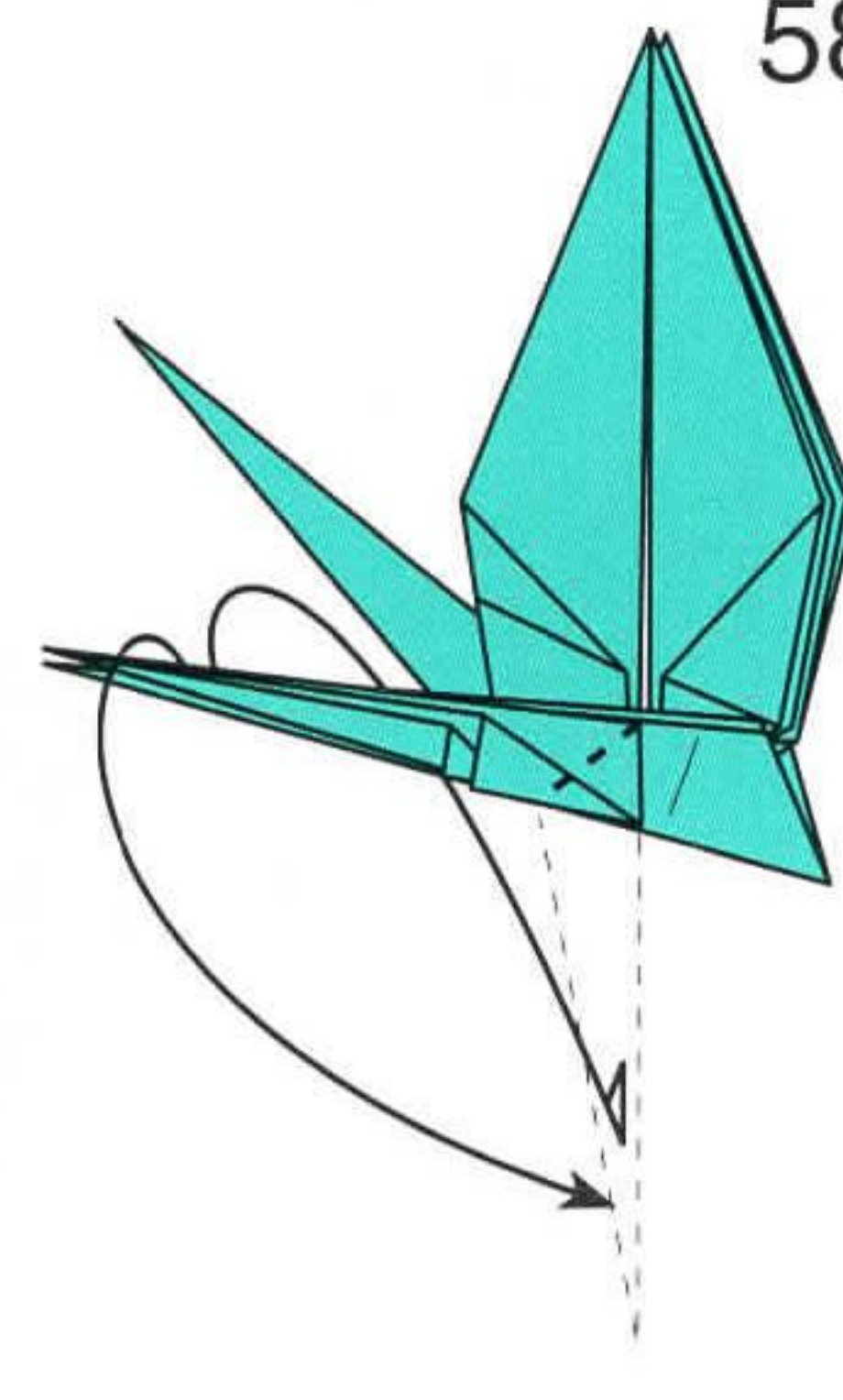
56



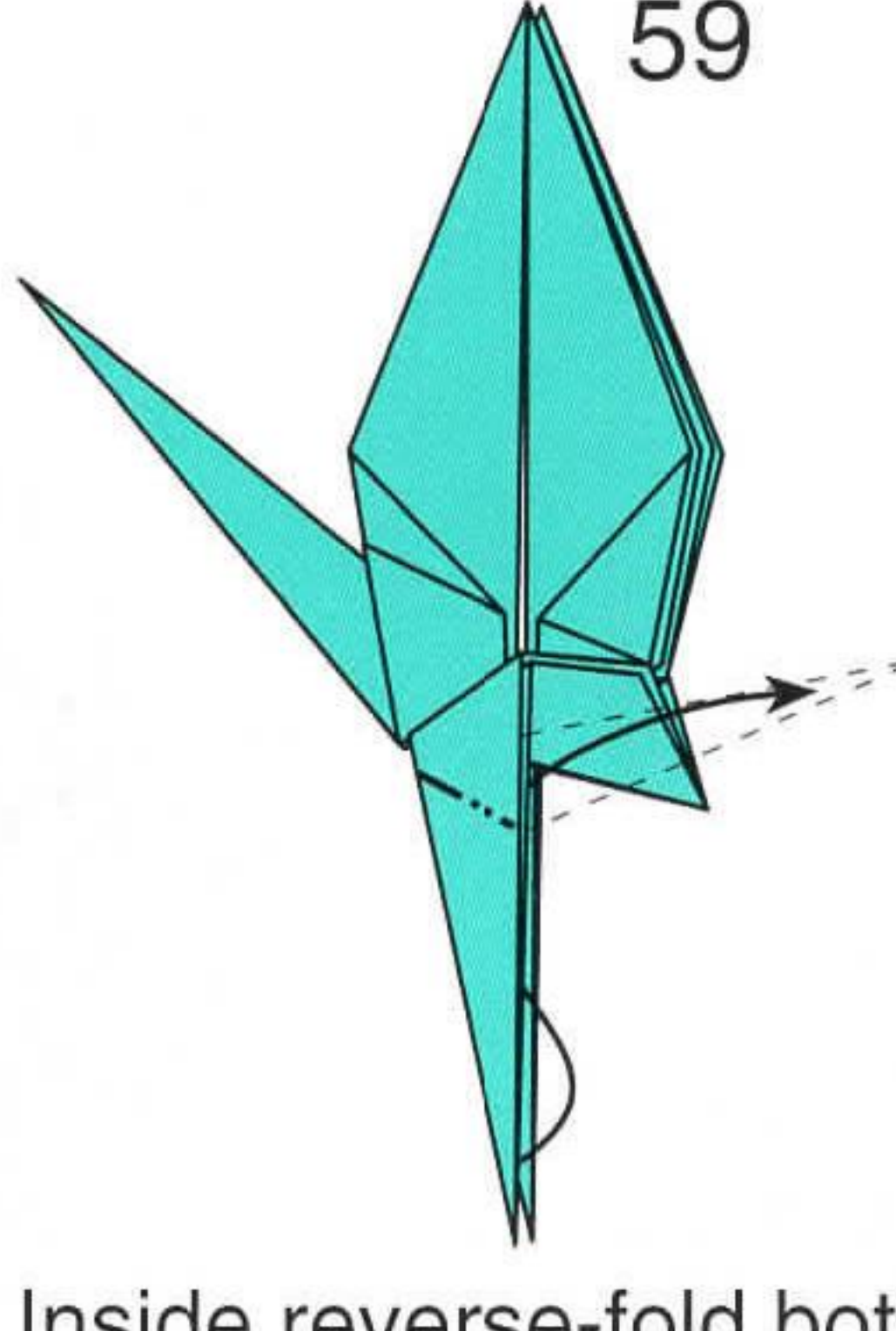
57



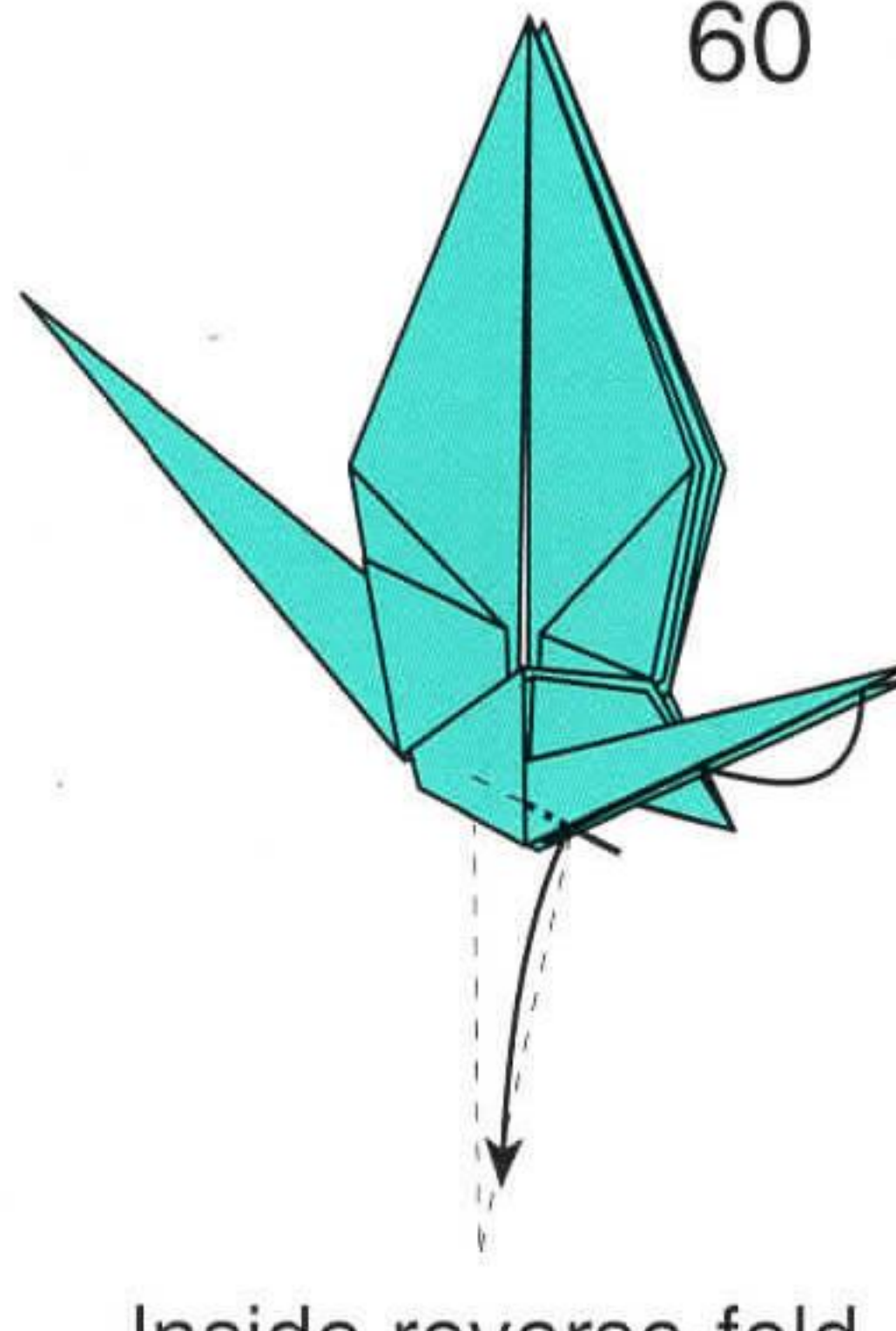
58



59



60



Open-sink.

Steps 48-49 show a typical open sink fold. Compare it with a closed sink fold in *Giraffe*.

Fold along the edges.

Fold behind into the top-most gap.

Two layers

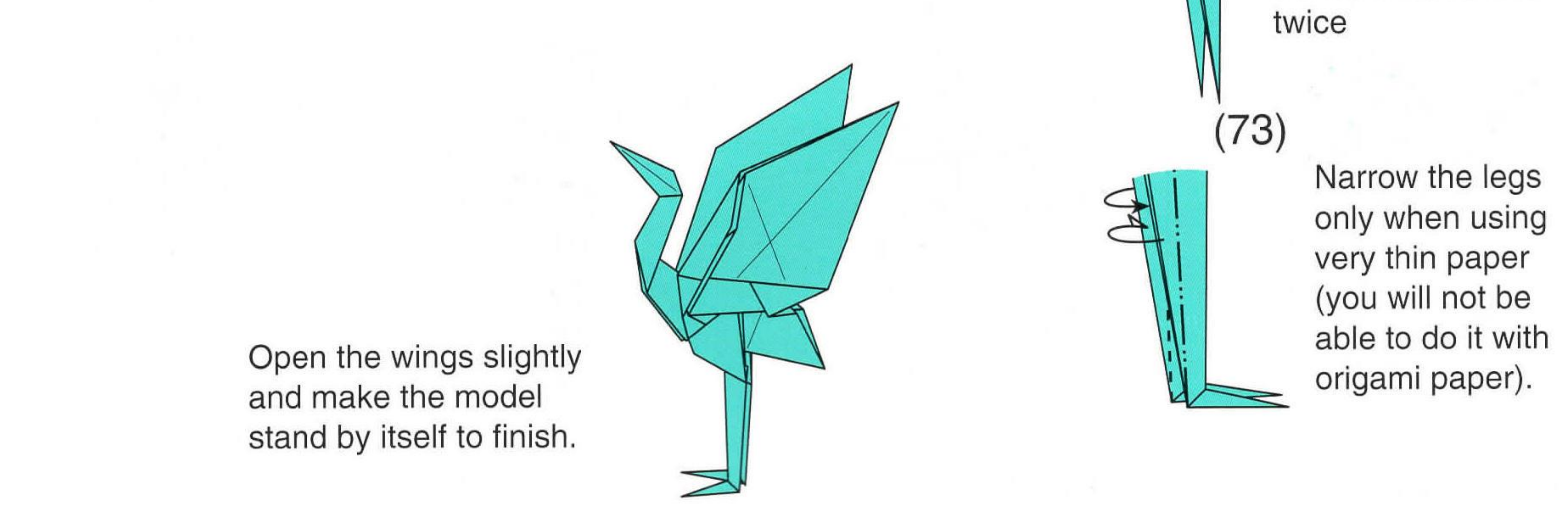
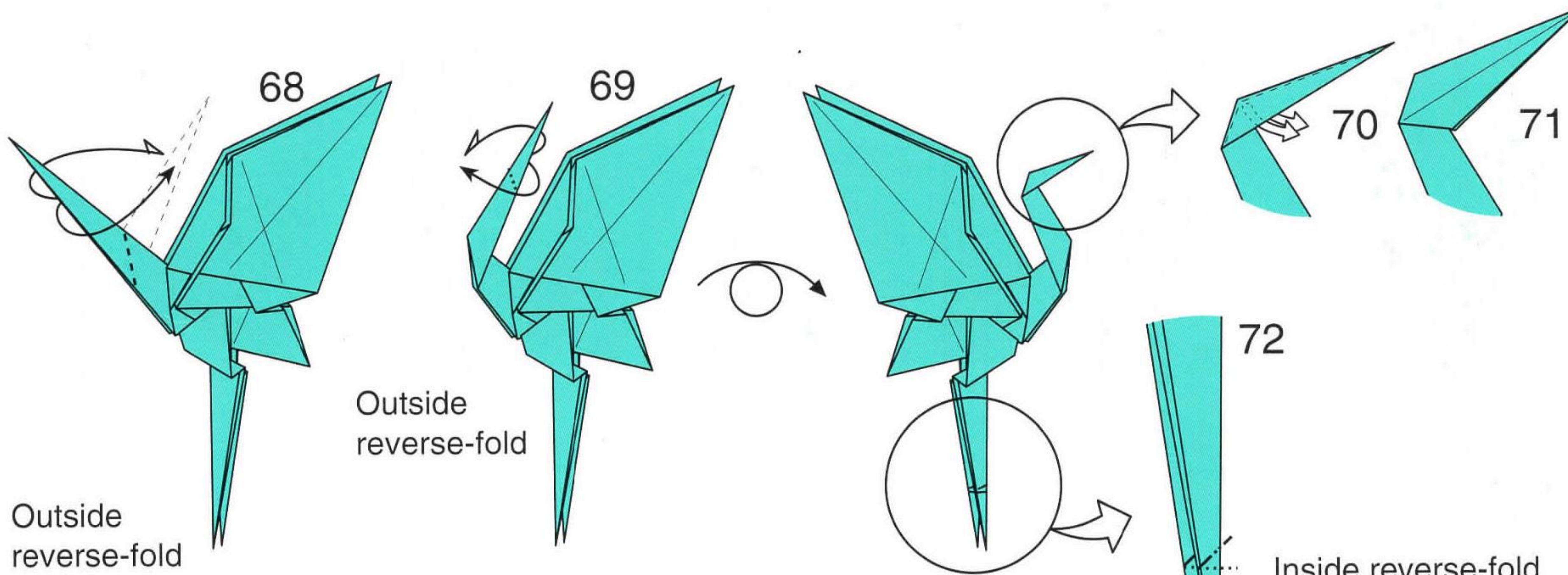
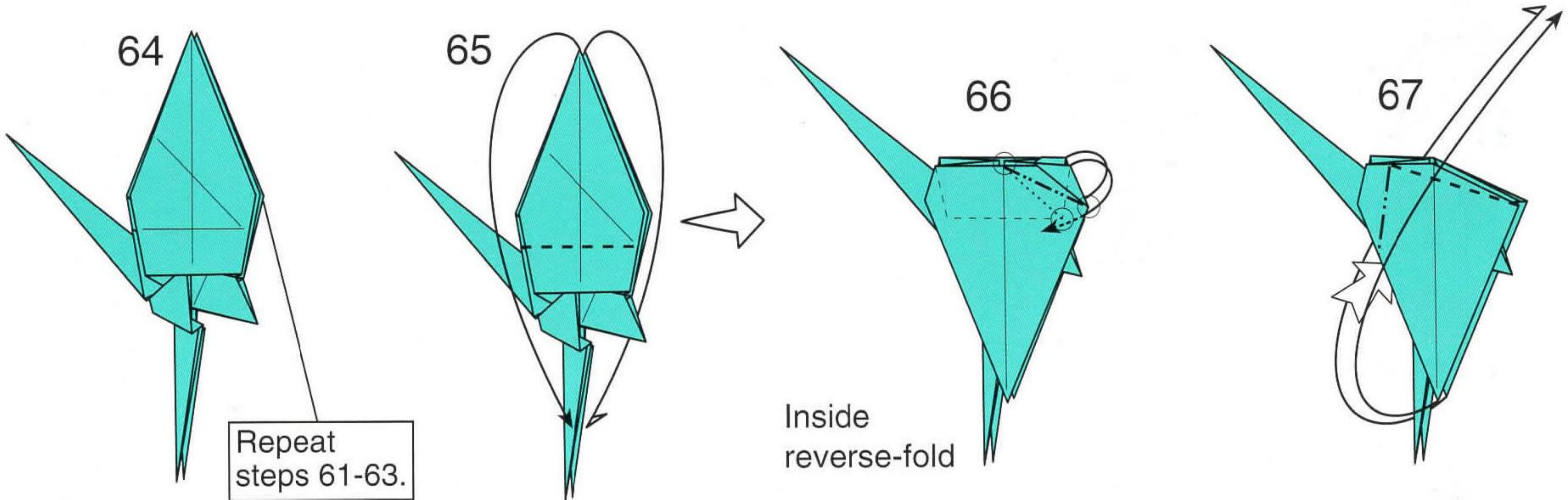
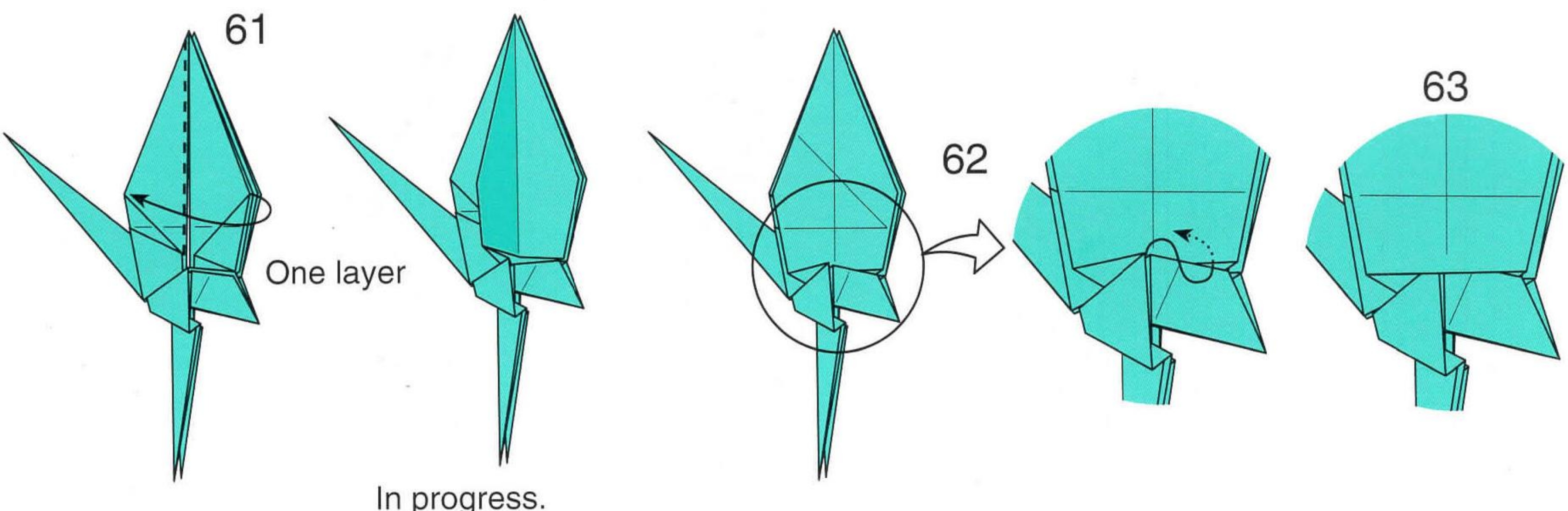
Inside reverse-fold

Outside reverse-fold

Outside reverse-fold

Inside reverse-fold both points simultaneously at the root

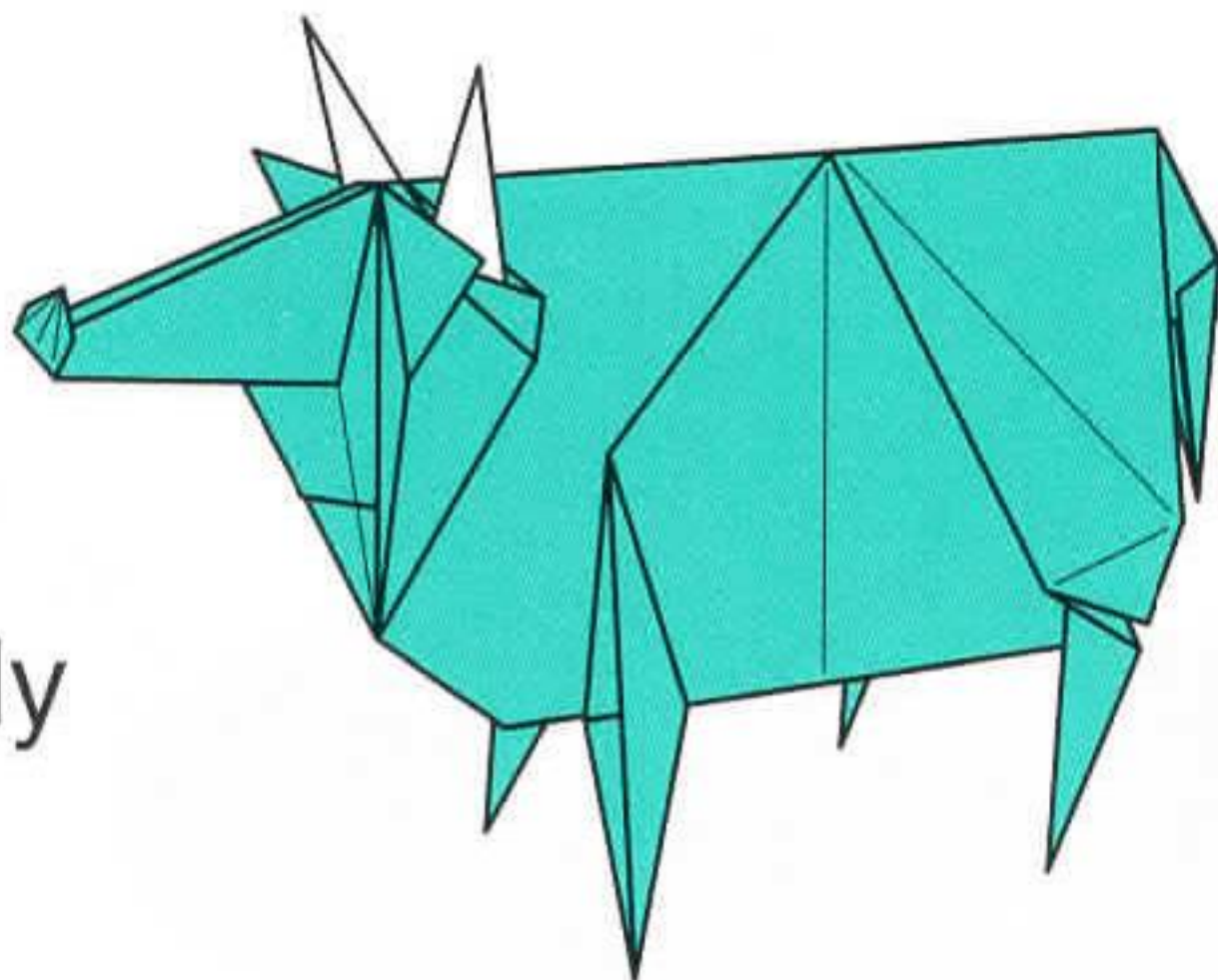
Inside reverse-fold



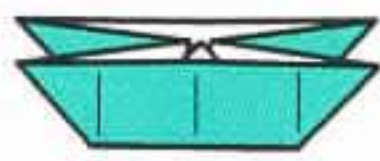
Cow

Theme: Pig base

Fold using 6" (15 cm) or preferably larger origami paper.



Step 5 shows a (blintzed) Pig base. Though it looks similar to traditional *Double Boat* (shown below), they are completely different.



Pig base

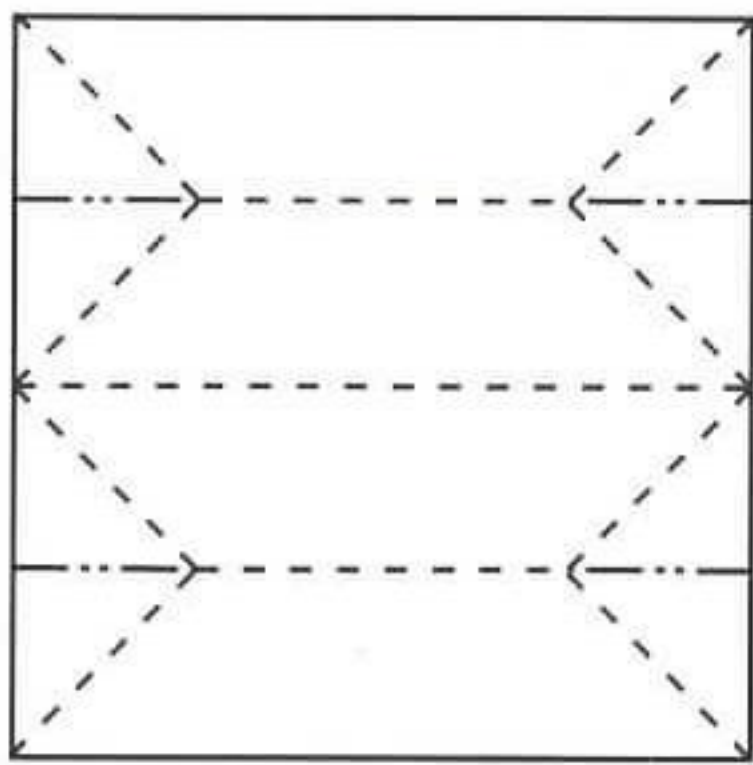
In *Standing Crane*, I explained the trunk in a tree structure. The base of traditional *Pig* shows a structure with a typical use of the trunk. The Pig base has a trunk in the middle and three branches at each end. You can see the central river in the circle-river diagram that corresponds to the trunk.

From the viewpoint of “molecules” or areas of grouped creases, the base consists of two quadrangular “molecules,” that is, two 1 : 2 rectangular “molecules.”

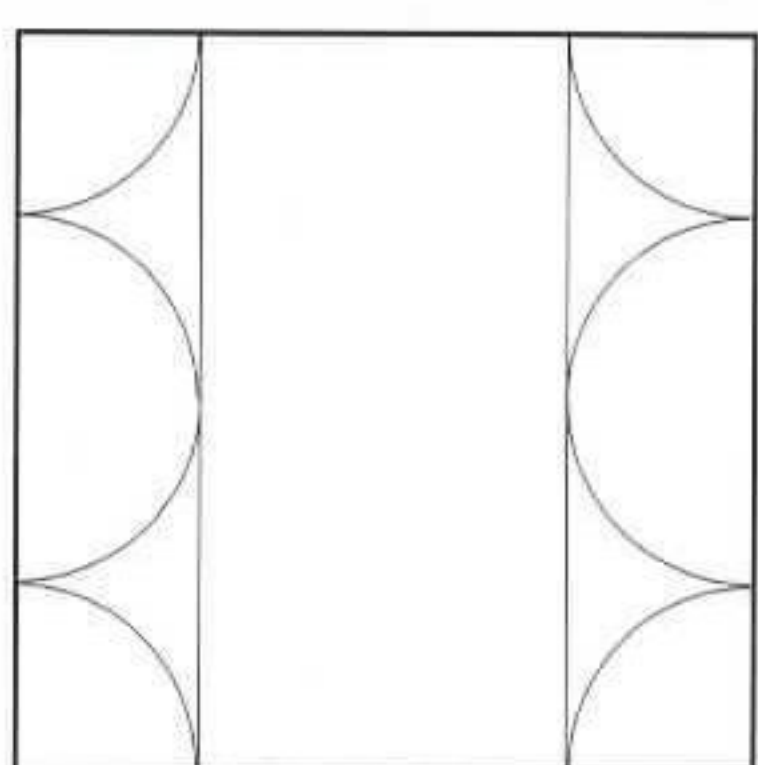
Now, let’s take a closer look at quadrangular “molecules.” Any quadrangle can be folded so that all edges align. (Robert Lang proved that it is true with any polygon, but here we examine only quadrangles.) For example, as explained in *Orizuru Transformation*, a quadrangle that has an inscribed circle can be folded as shown in the left and center picture in the middle row. The center quadrangle is folded in the same way as a Water-bomb base from a square. If we extend this pattern to a rectangle and other quadrangles, we must add a crease to make a trunk.

The crease pattern on the right is for Tiger I published before. Although it has more creases because it is based on 22.5° angles, you can see two 1 : 1.5 rectangle “molecules” next to each other. They define the basic structure, and the other parts create flaps for ears. So this pattern can be applied to different quadruped animals.

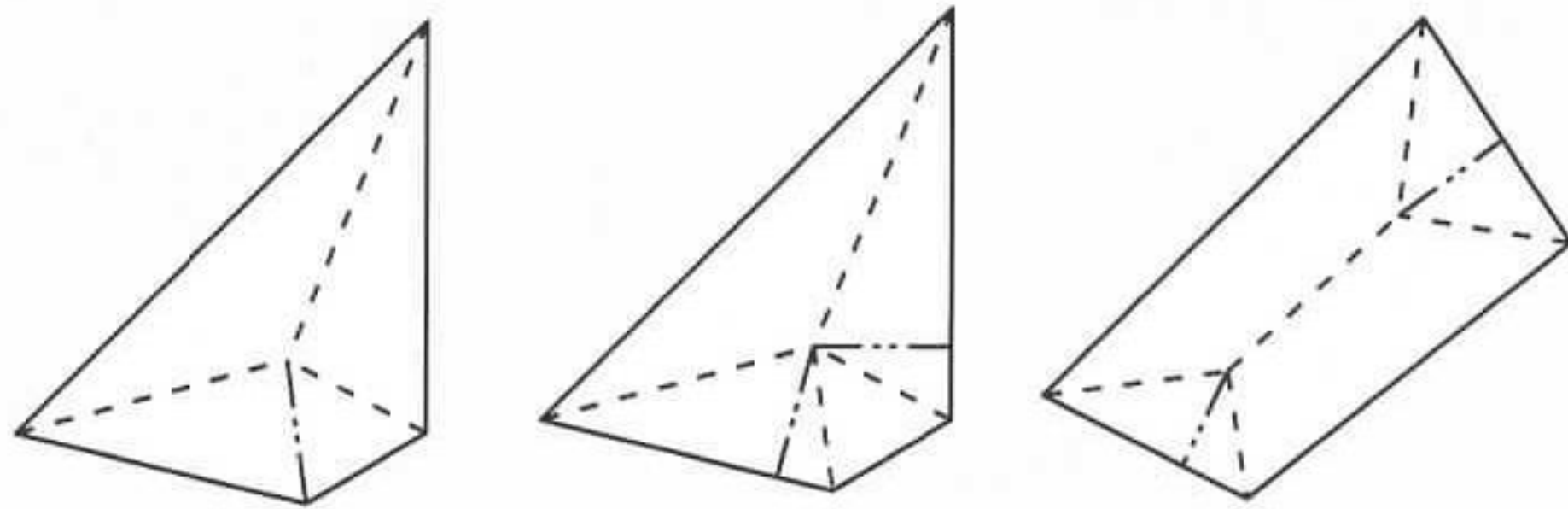
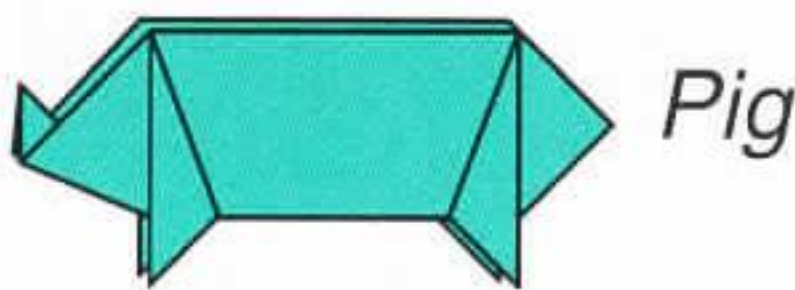
This *Cow* is also derived from a Pig base, though not from the crease pattern on the right. Before transformed in step 6, it starts with a blintzed Pig base (step 5).



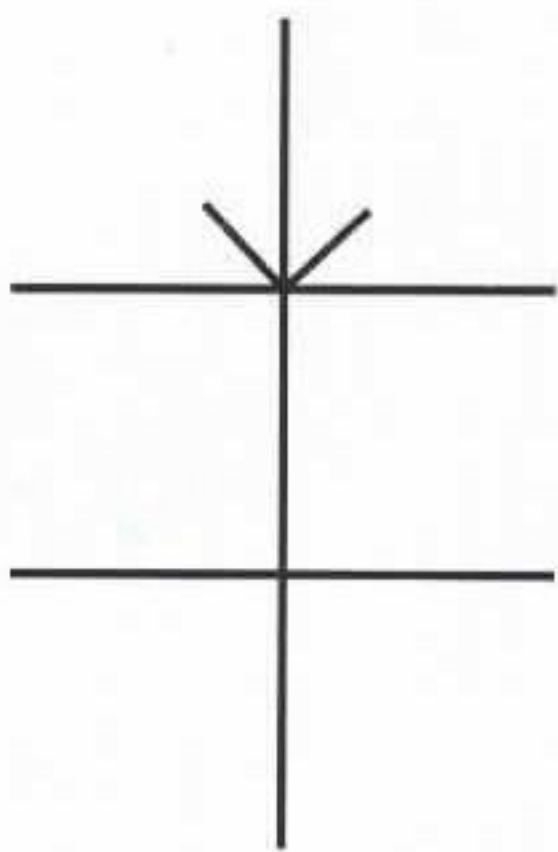
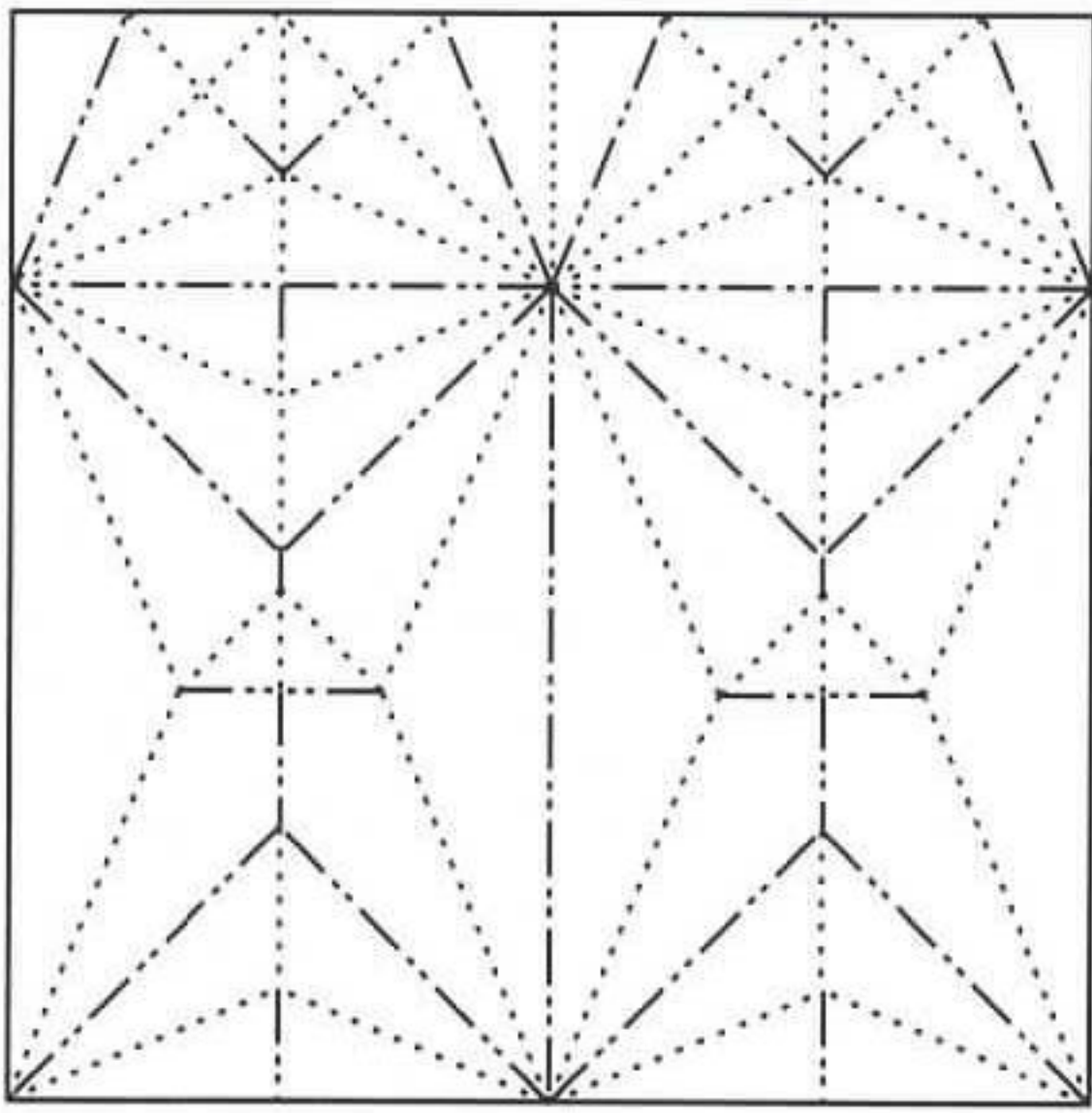
The crease pattern of the Pig base.



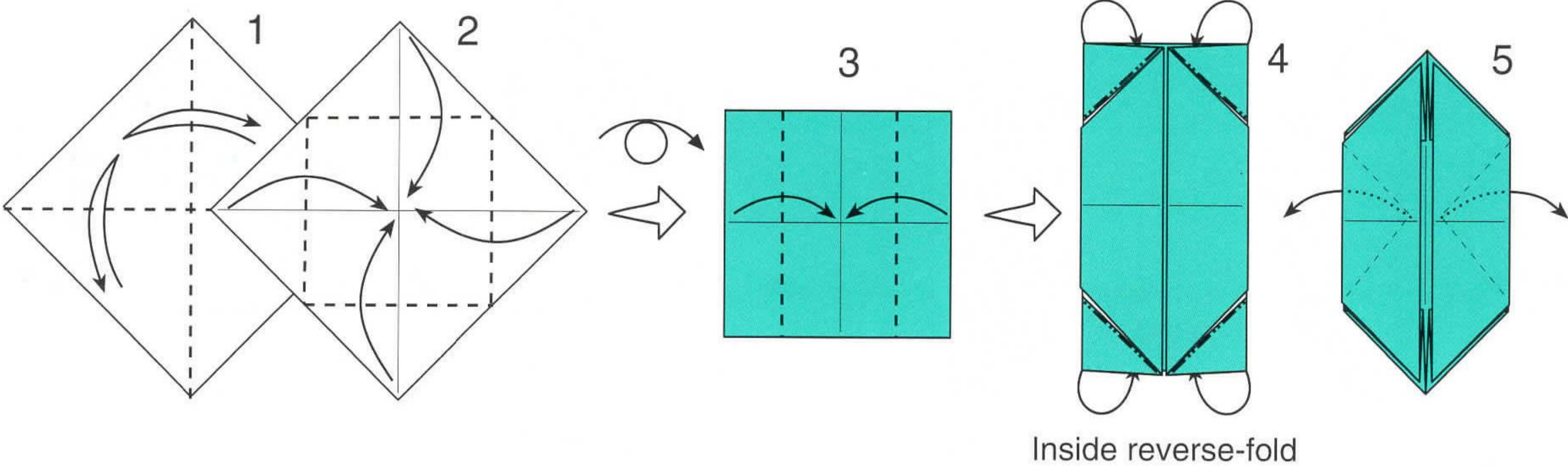
The tree figure of the Pig base.



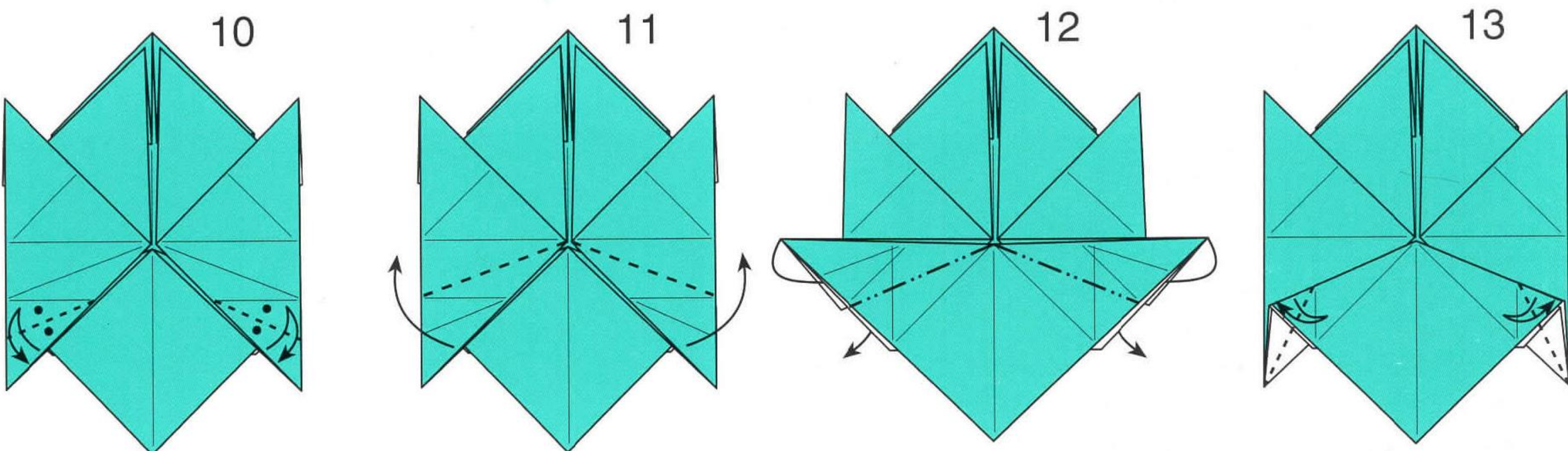
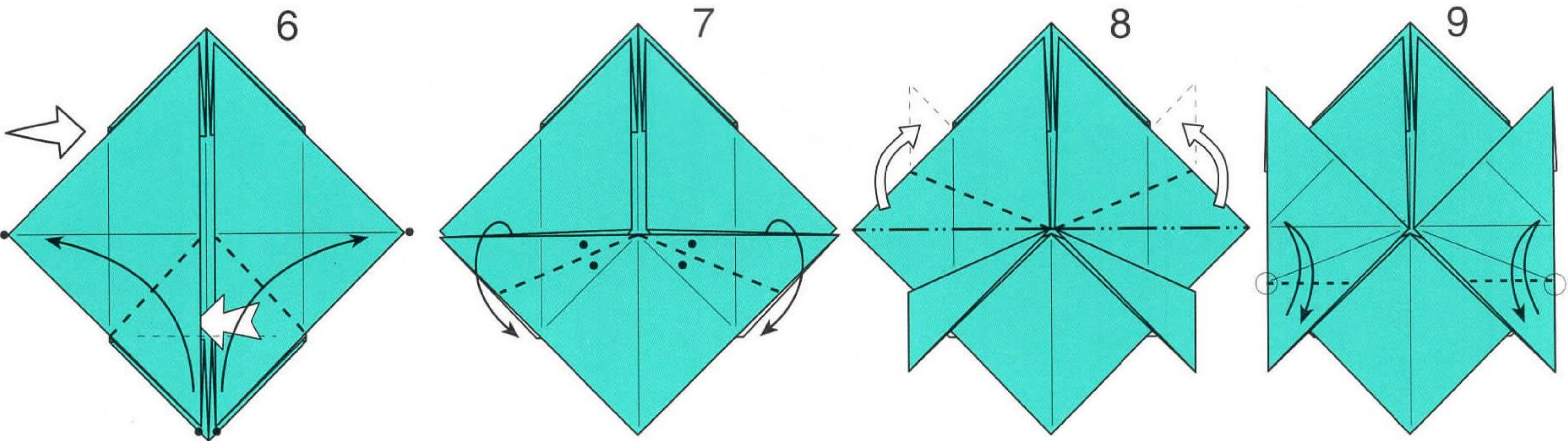
Folding quadrangles to align all the edges. (The quadrangles on the left and center has an inscribed circle.)



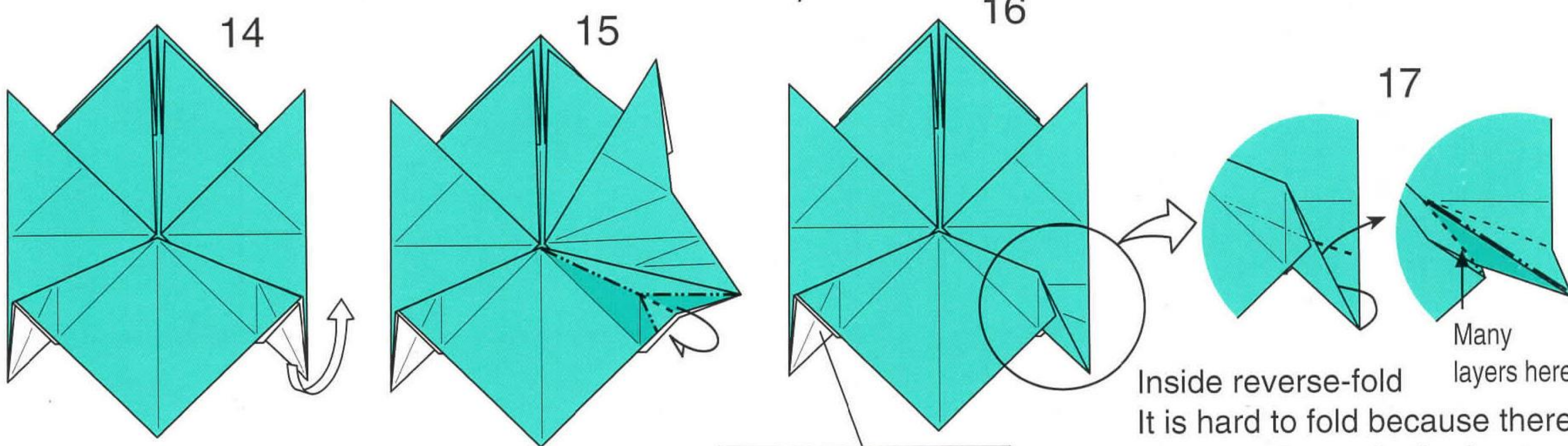
A crease pattern that can be used for the design of different animals.



Inside reverse-fold



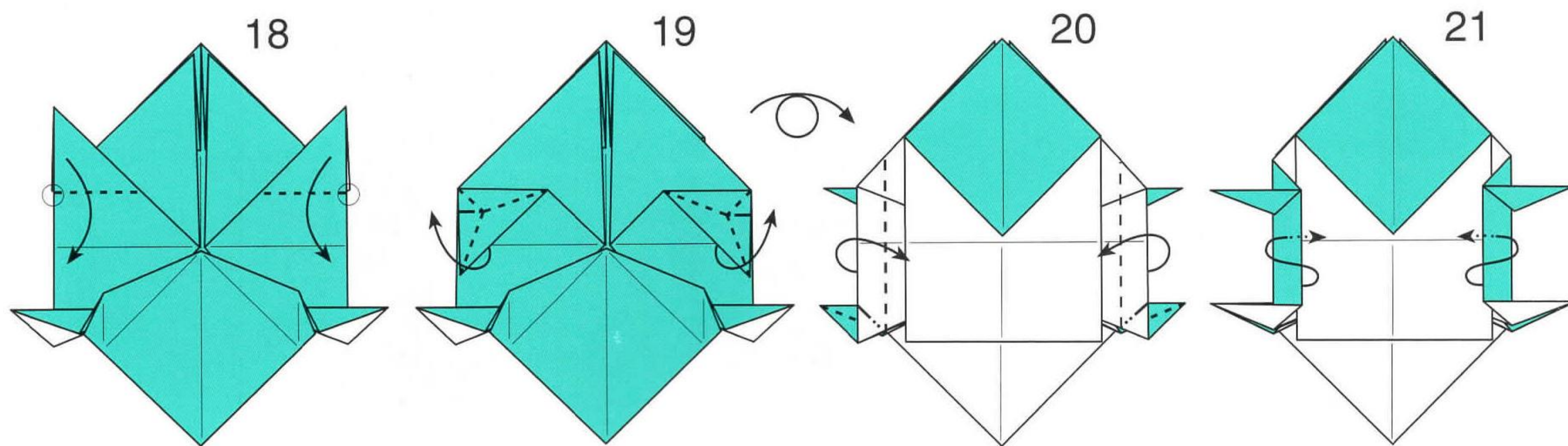
Inside reverse-fold
under the second layer



Open slightly.

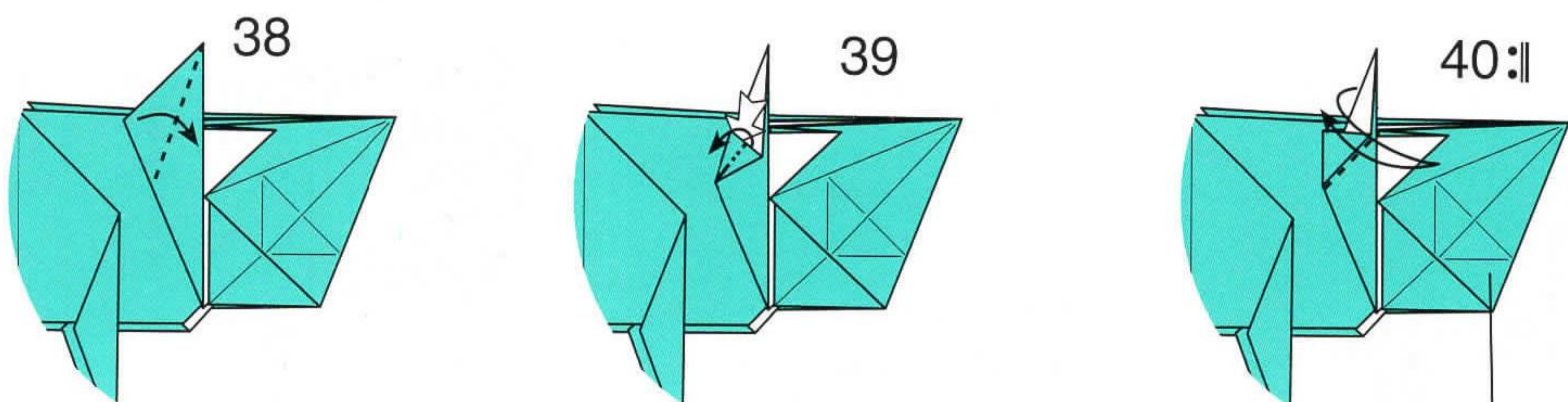
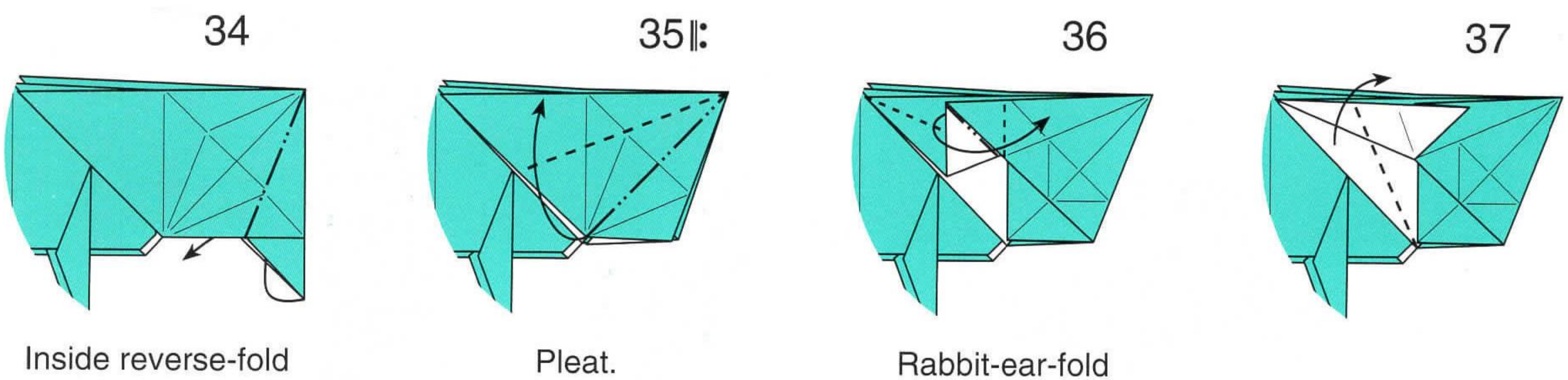
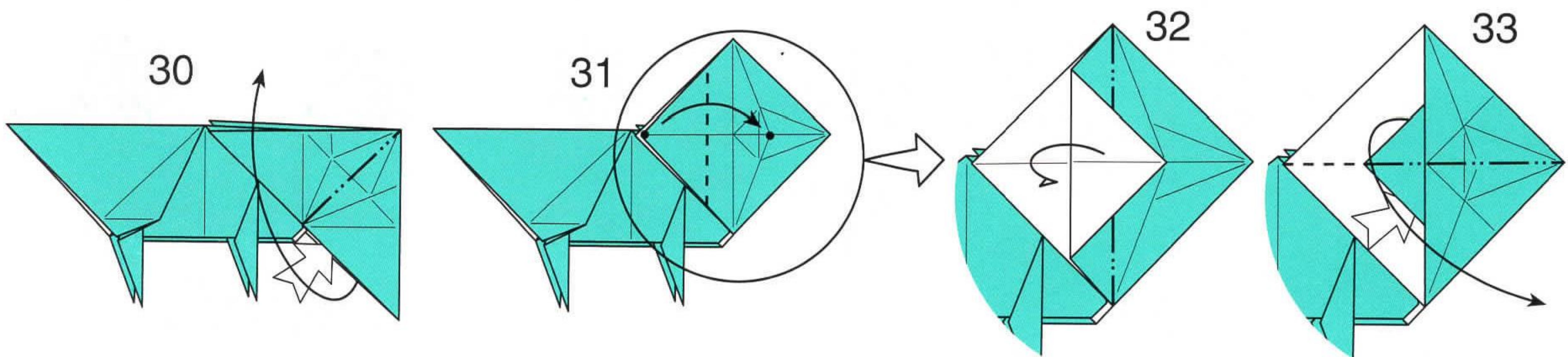
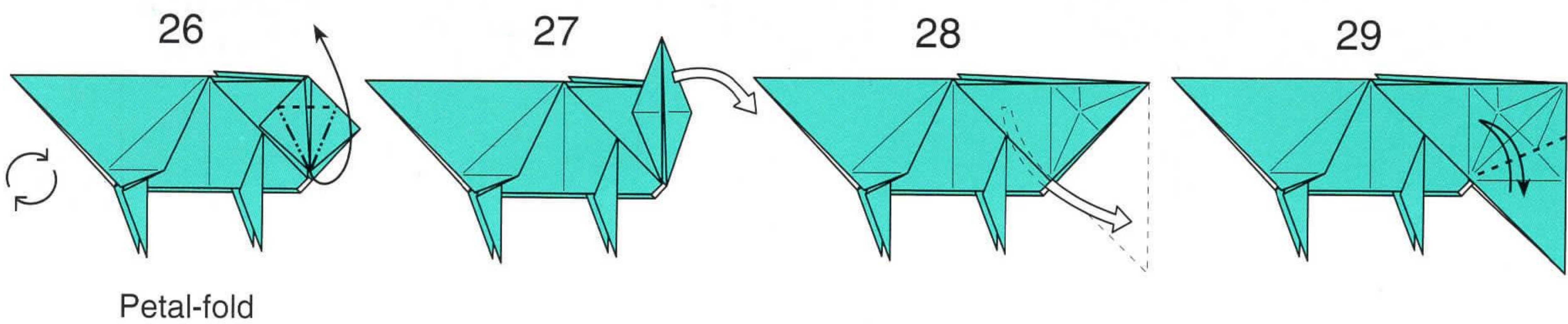
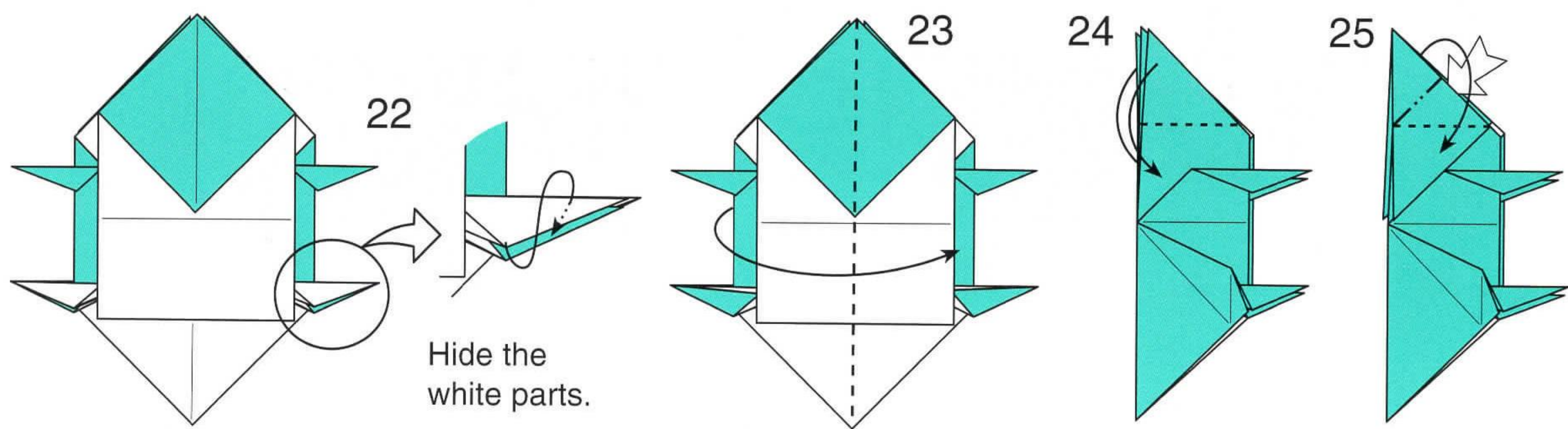
Repeat steps 14-15.

Inside reverse-fold
It is hard to fold because there
are many layers in the front.
Repeat on the other side.



Rabbit-ear-fold

Swivel-fold



Repeat steps 35-40.

41

42

43

44

Petal-fold

45

Reverse the flap inside.

46

47

48

Inside crimp.

49

Inside reverse-fold

50

51

52

53

Push in carefully so that the face is symmetric (paying attention not to crack the forehead).

54

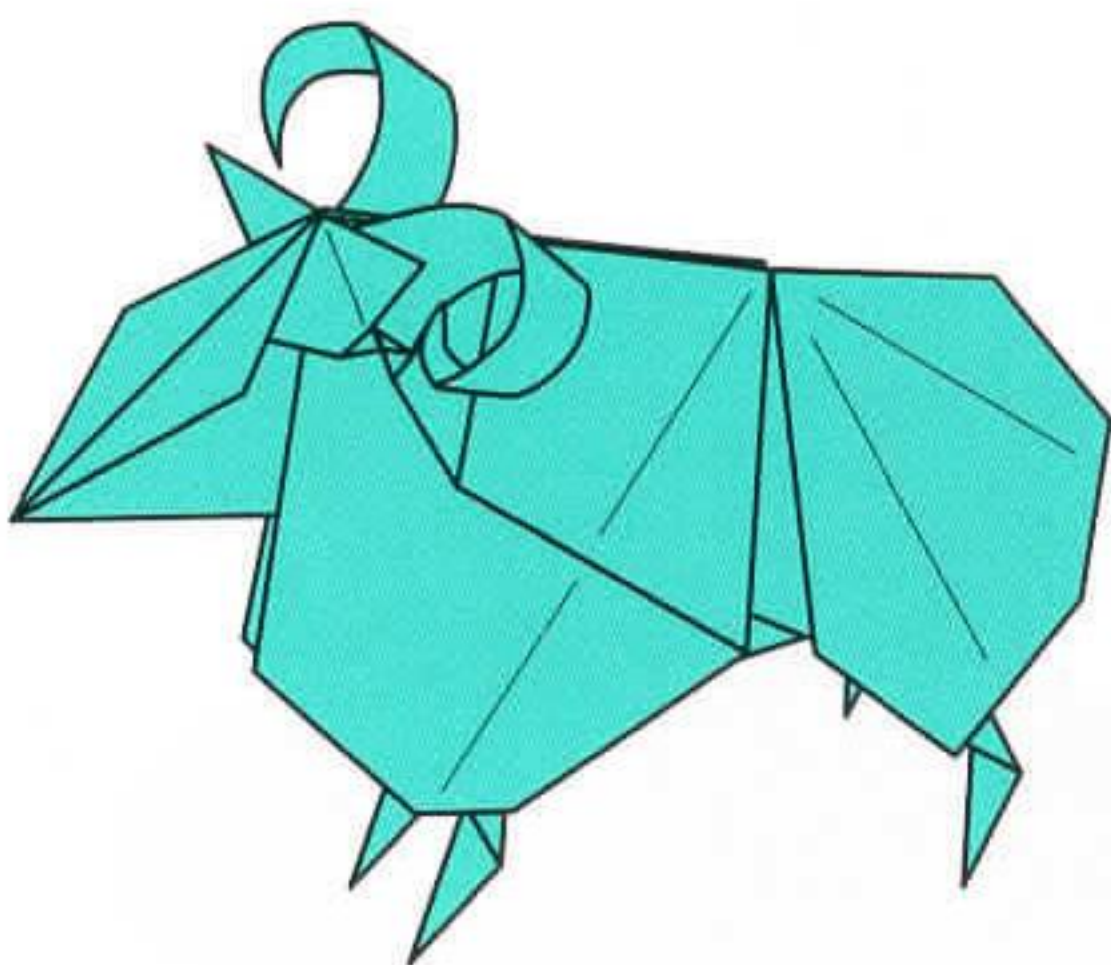
55

56

Lift the head to face forward and bend the horns forward using the creases made in step 40.

Sheep

Theme: Why from a square?
Fold using 6" (15 cm) origami paper.



The crease pattern below looks like a lion head for me. I would say that is another instance of "mitate."

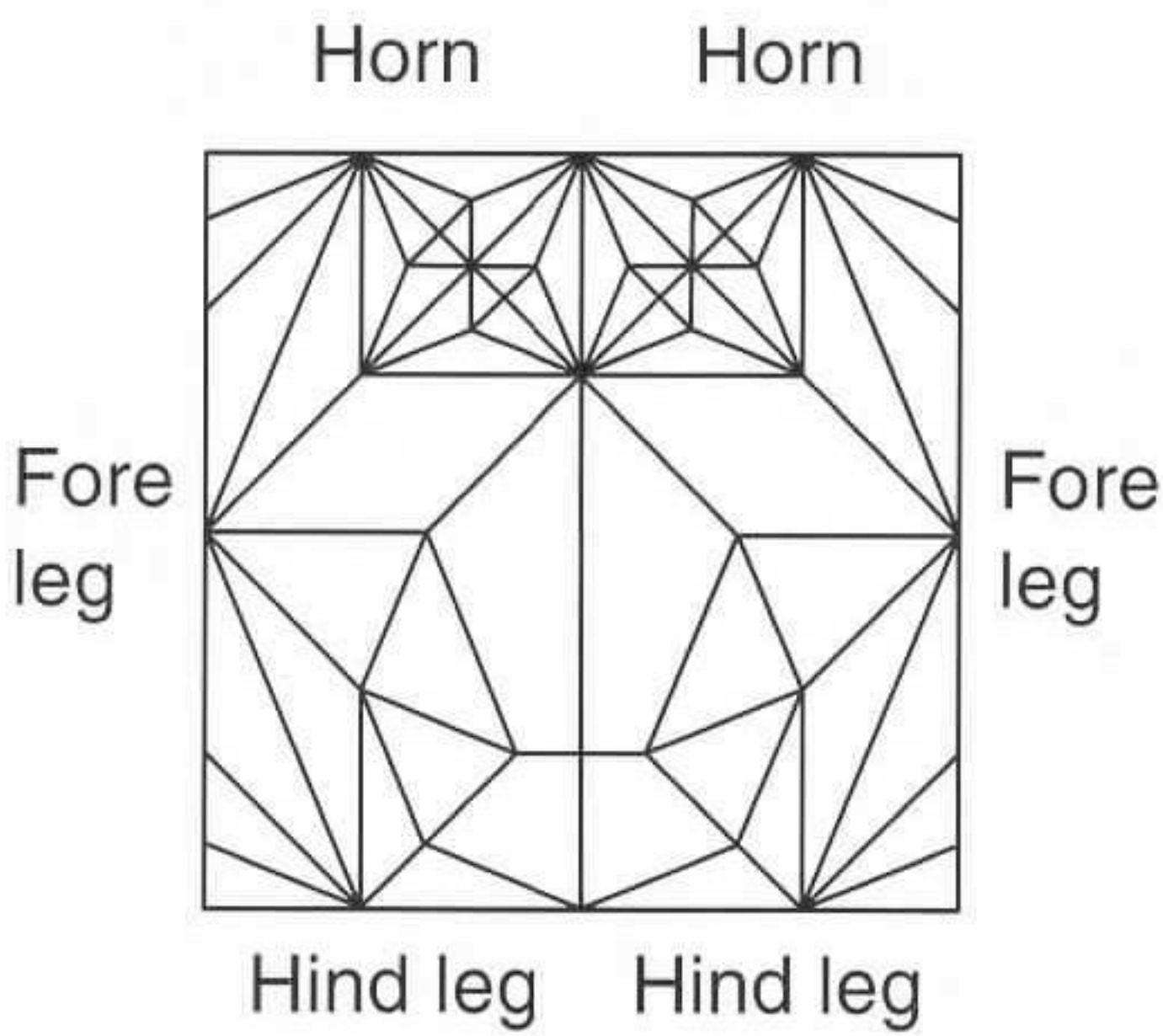
Why from a square?

The crease pattern of *Sheep* is shown on the right. You can see that none of four corners of the square is used for a point like a horn or a leg. This model can be folded from a hexagon inscribed in a square, just like *Three-headed Crane* can be folded from a hexagon and *Standing Crane* a pentagon.

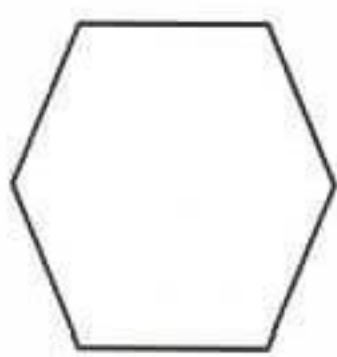
Then, you may wonder if these models are really folded from squares. My answer is the following. First, as seen in *Three-headed Crane*, it is unexpectedly often the case that we can use a square more efficiently when we do not use corners for points. That puzzle-like unexpectedness is a significant part of origami. And it becomes more unexpected when we start from a "simple" shape of square.

Moreover, a design is based on and has an affinity to square if it requires a shape that can be easily derived from a square. It is natural to fold such a design using a square sheet, just the same as we do not fold *Orizuru* using the star shape shown on the right.

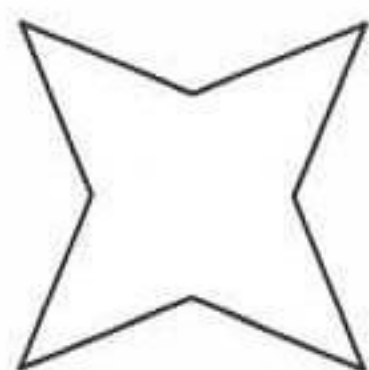
Which is true? That the creases harmonize with the square because we are using a square, or that the square is chosen as the handiest shape because we standardize angles and other aspects? I would say this is a chicken and egg question. Anyway, I strongly feel that the square is interesting and very rich.



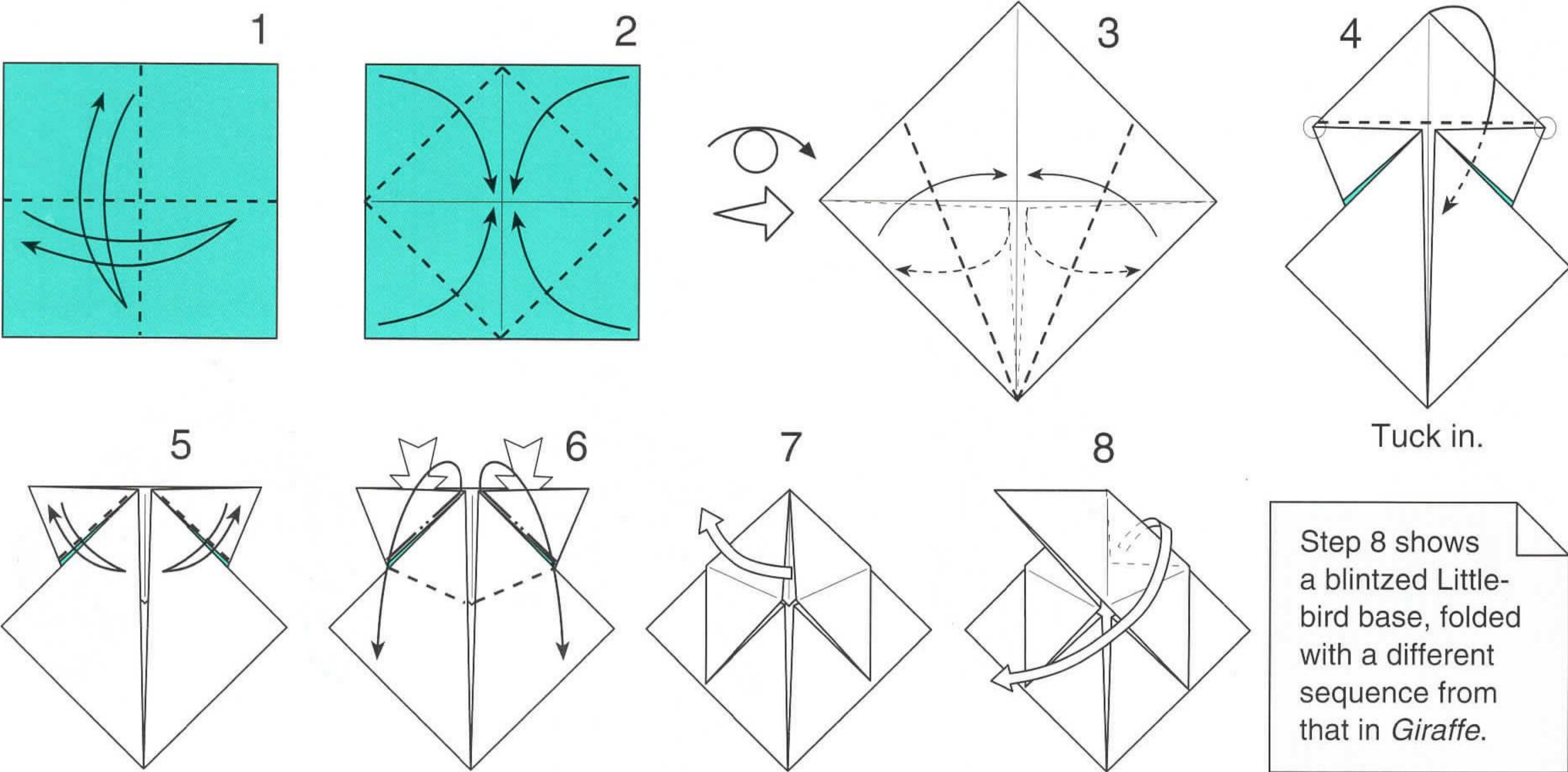
The crease pattern of *Sheep* (mountain and valley folds are not shown).



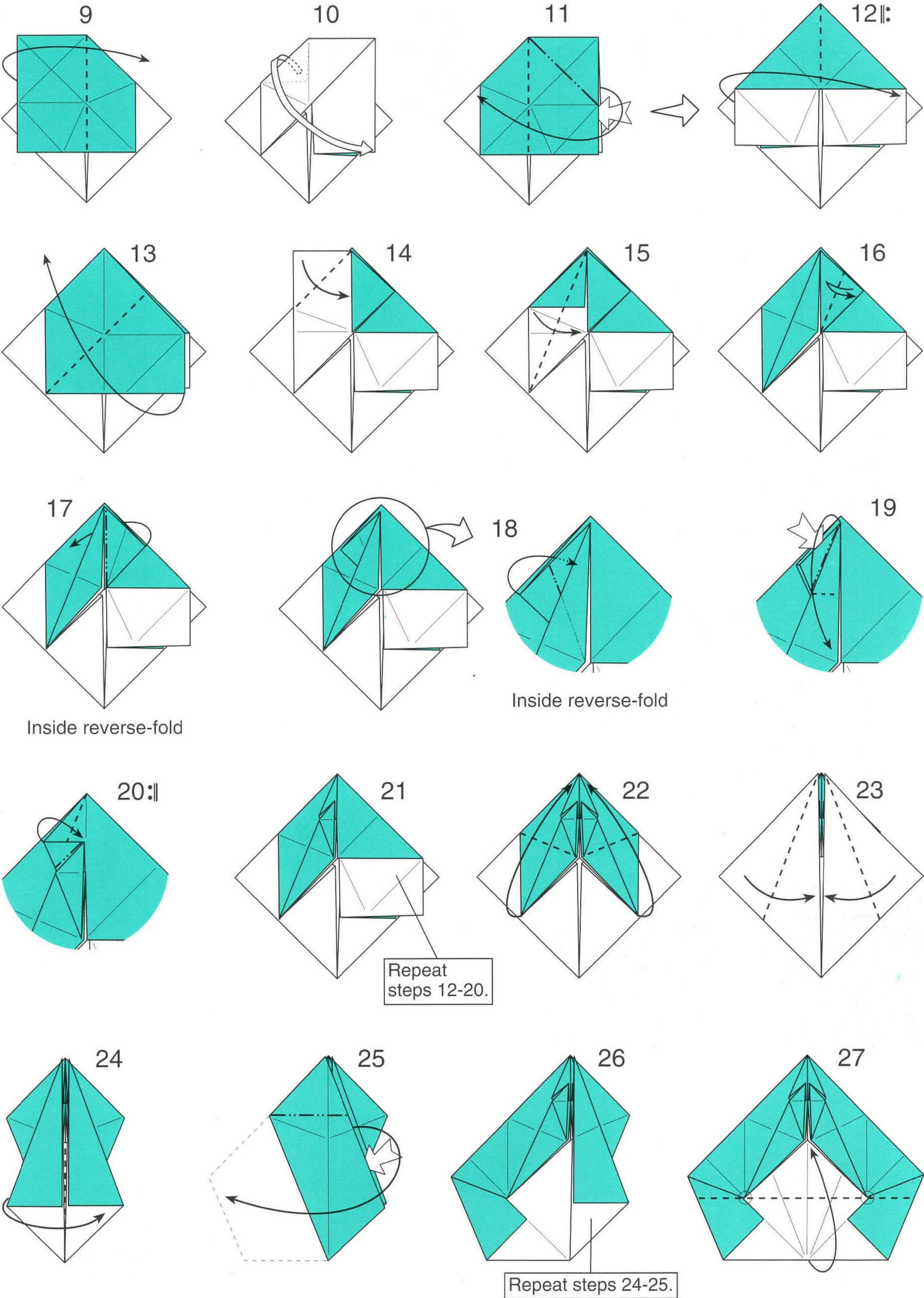
The basic structure of *Sheep*.

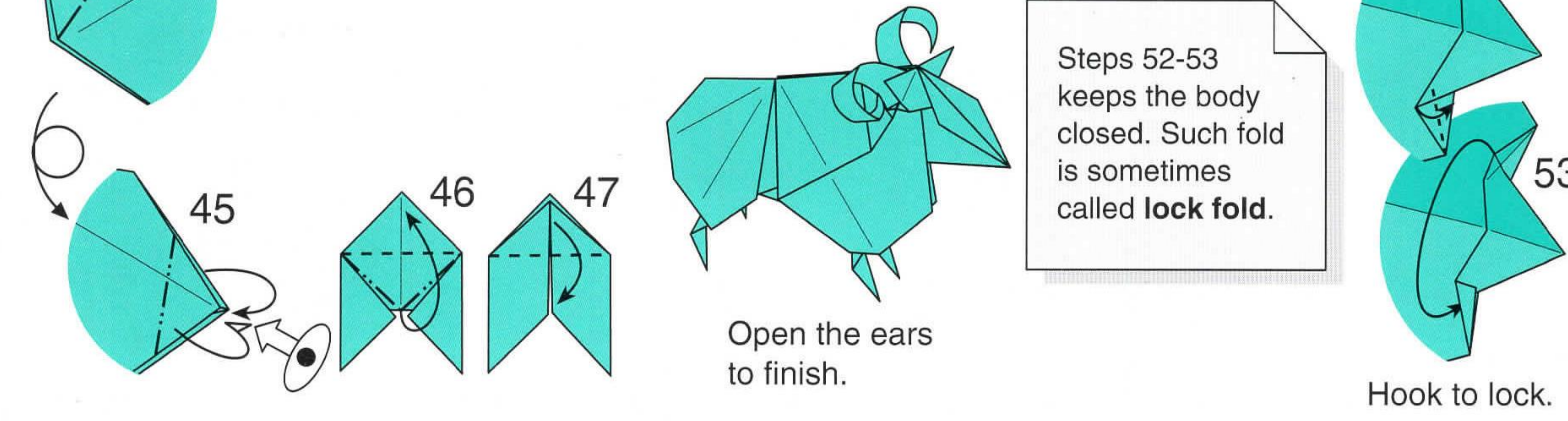
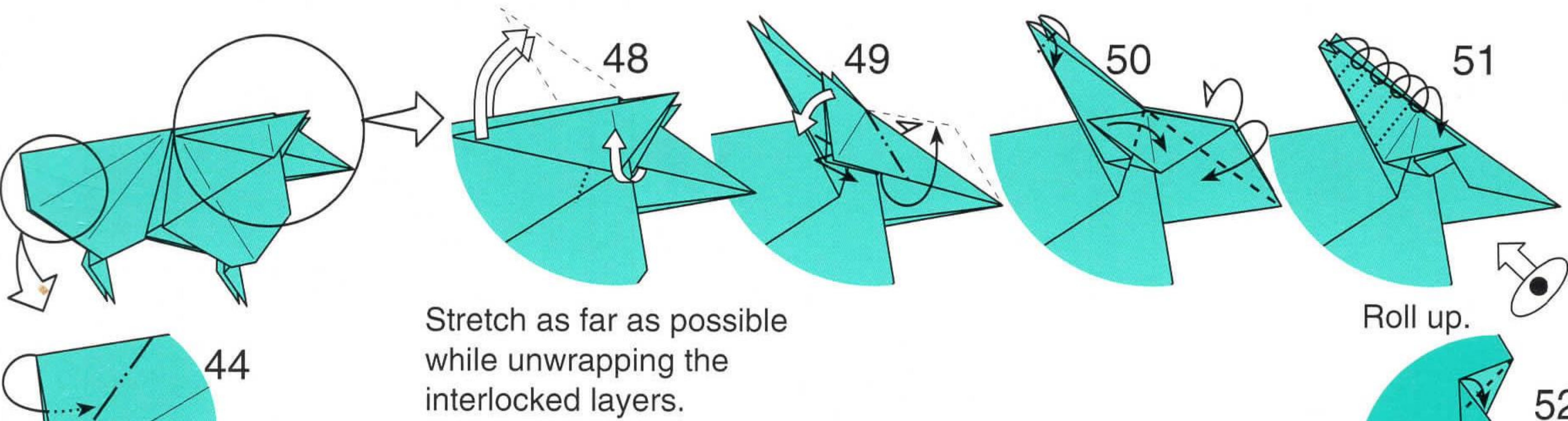
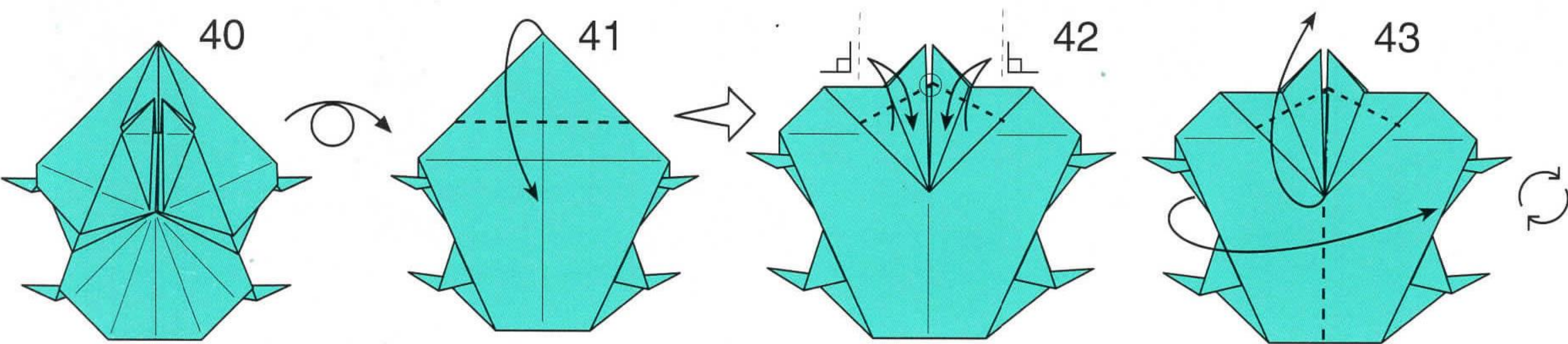
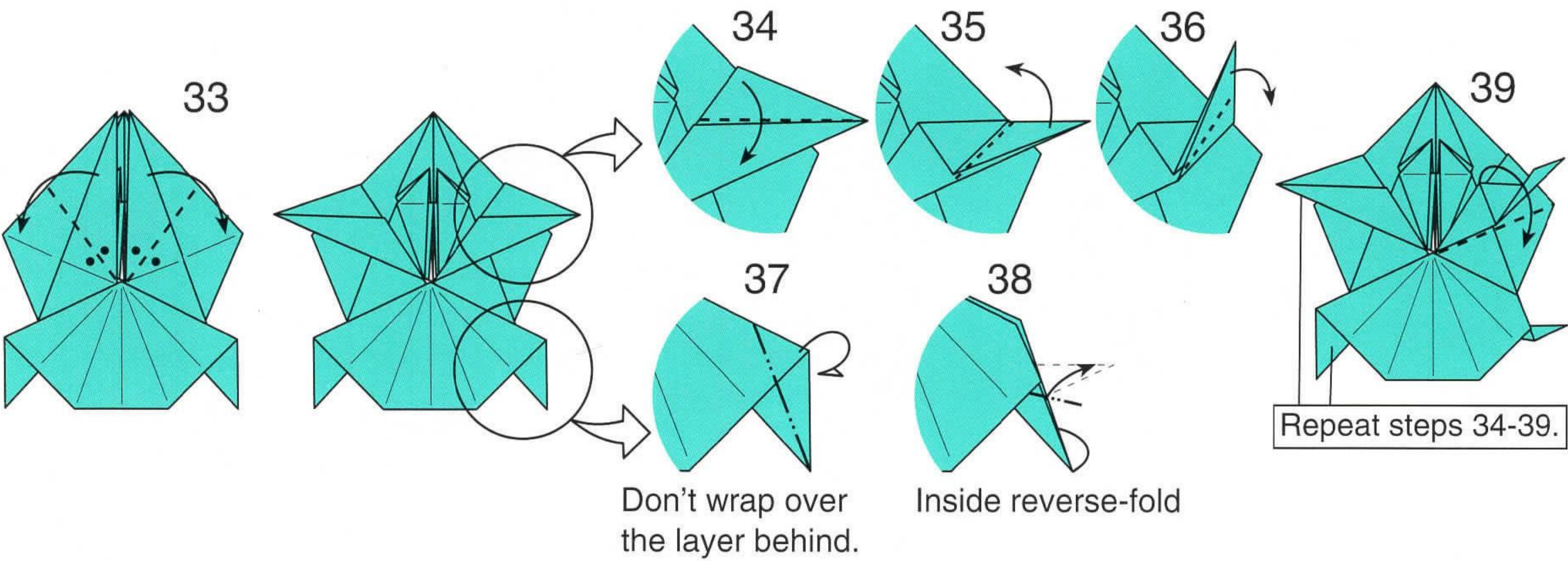
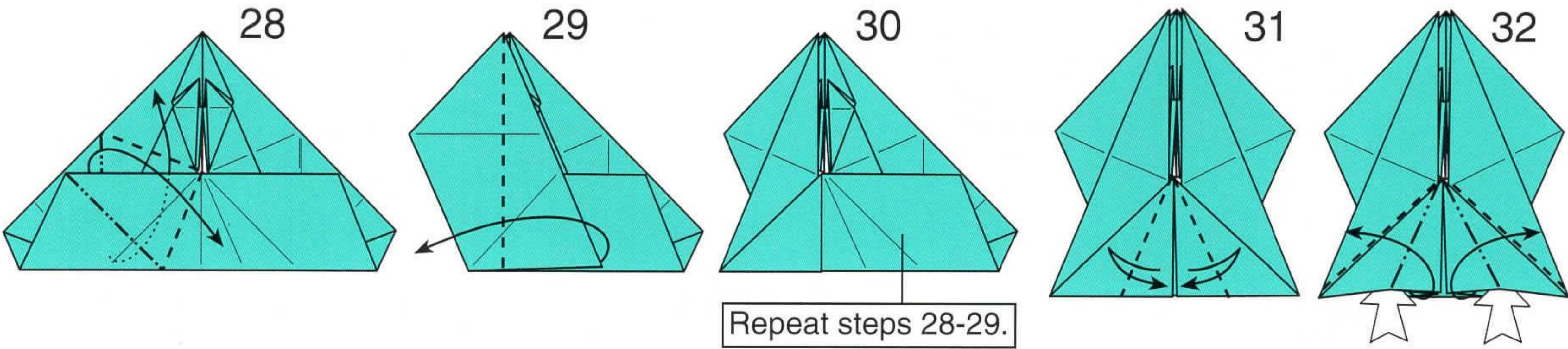


Orizuru can be folded using this shape.



Step 8 shows a blintzed Little-bird base, folded with a different sequence from that in *Giraffe*.

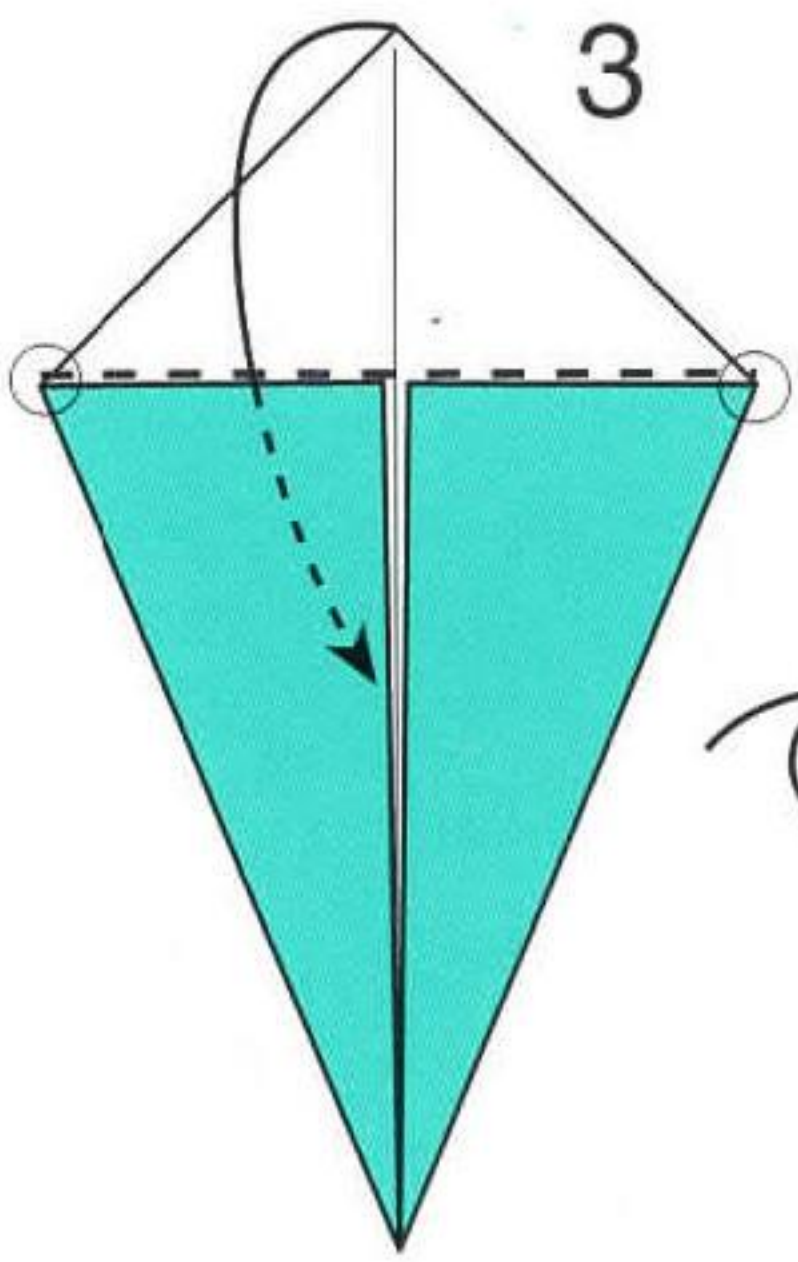
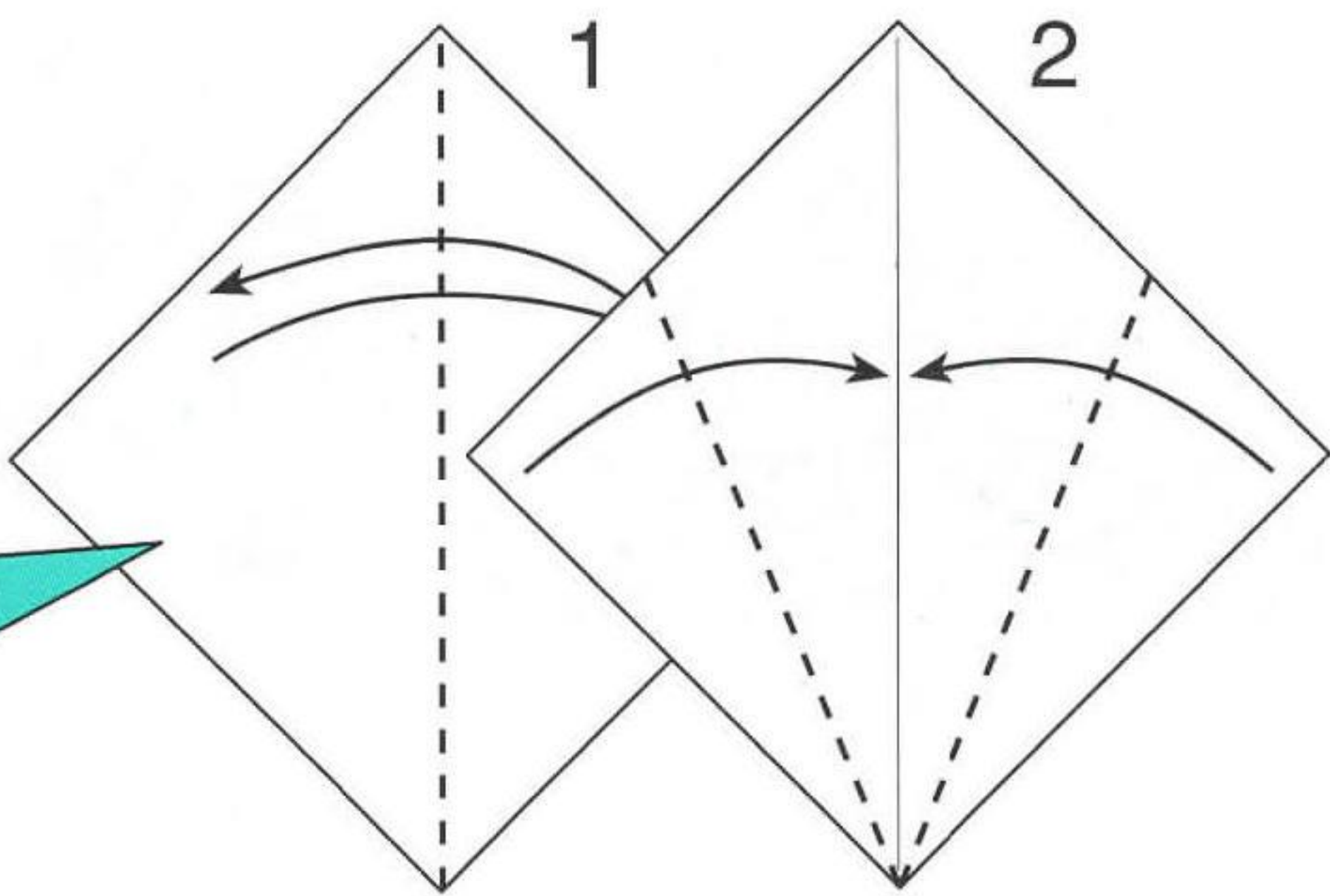
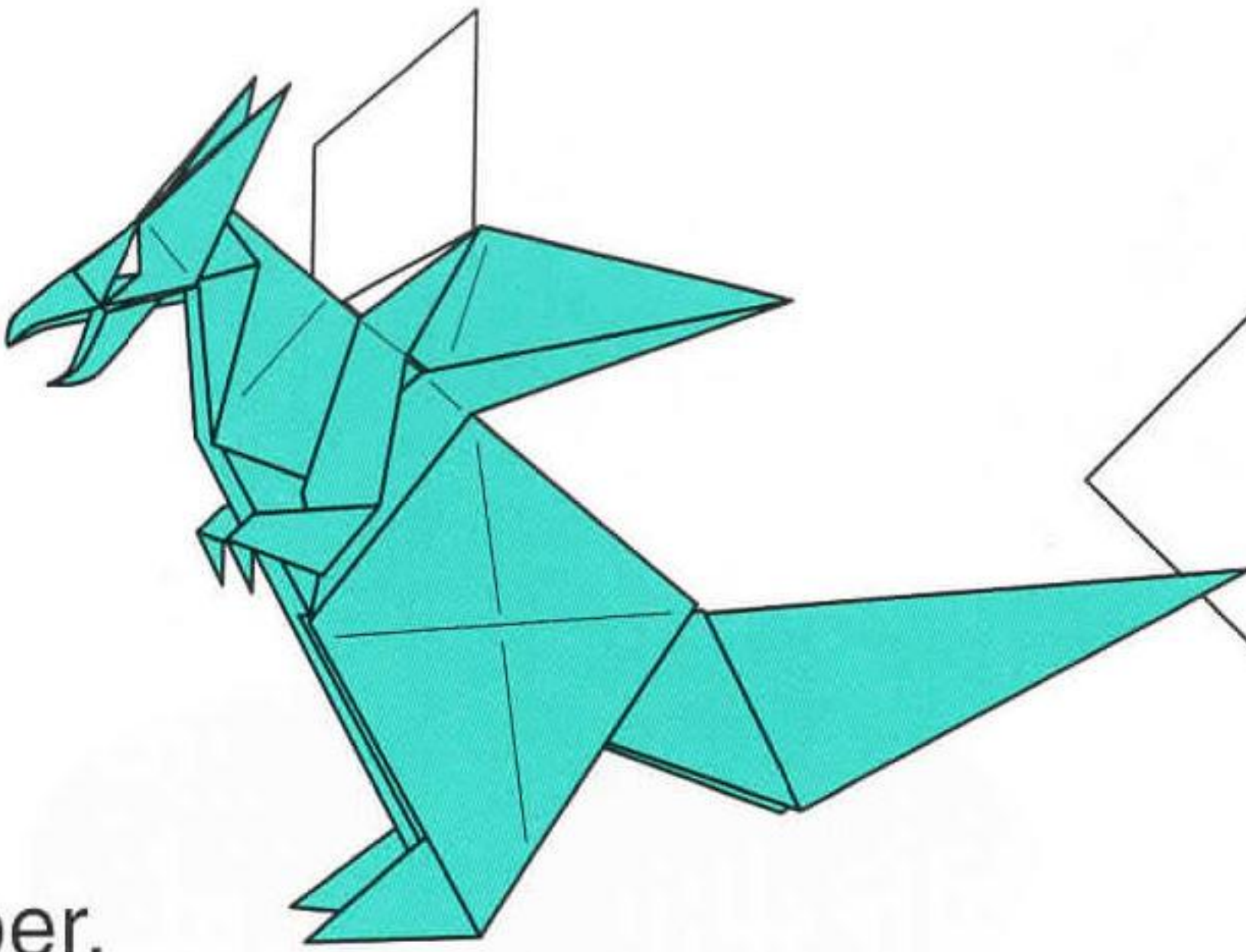




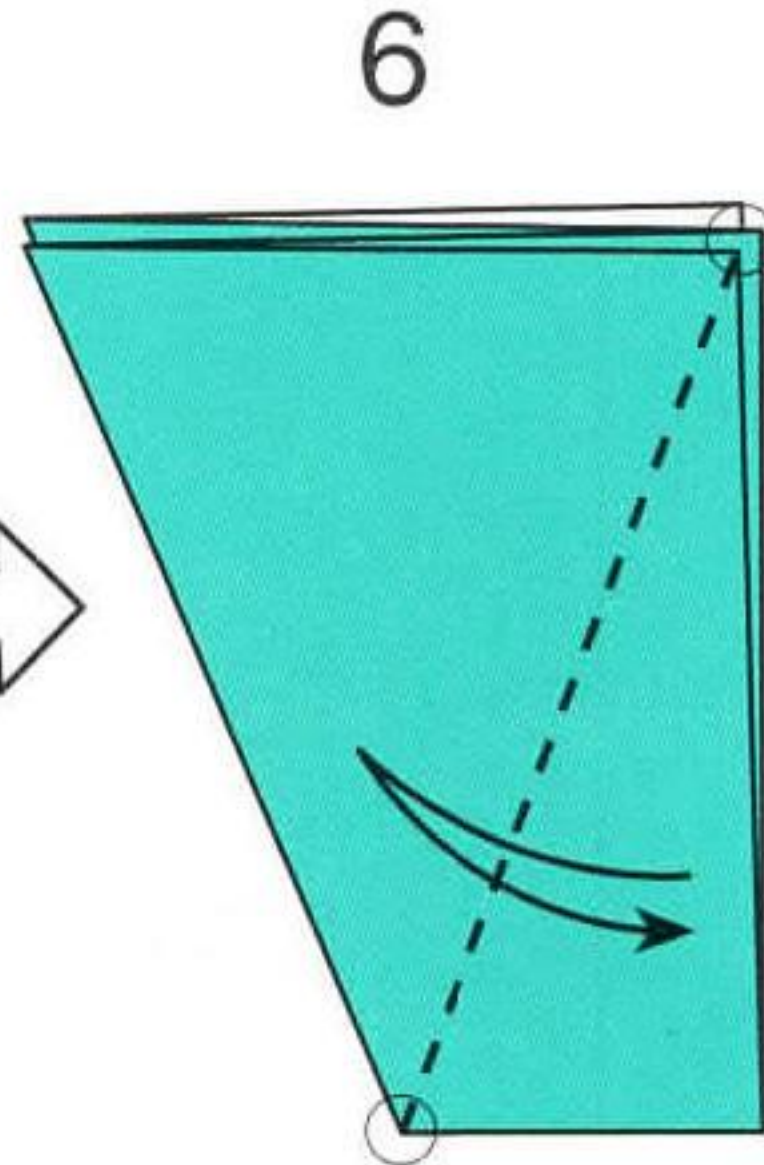
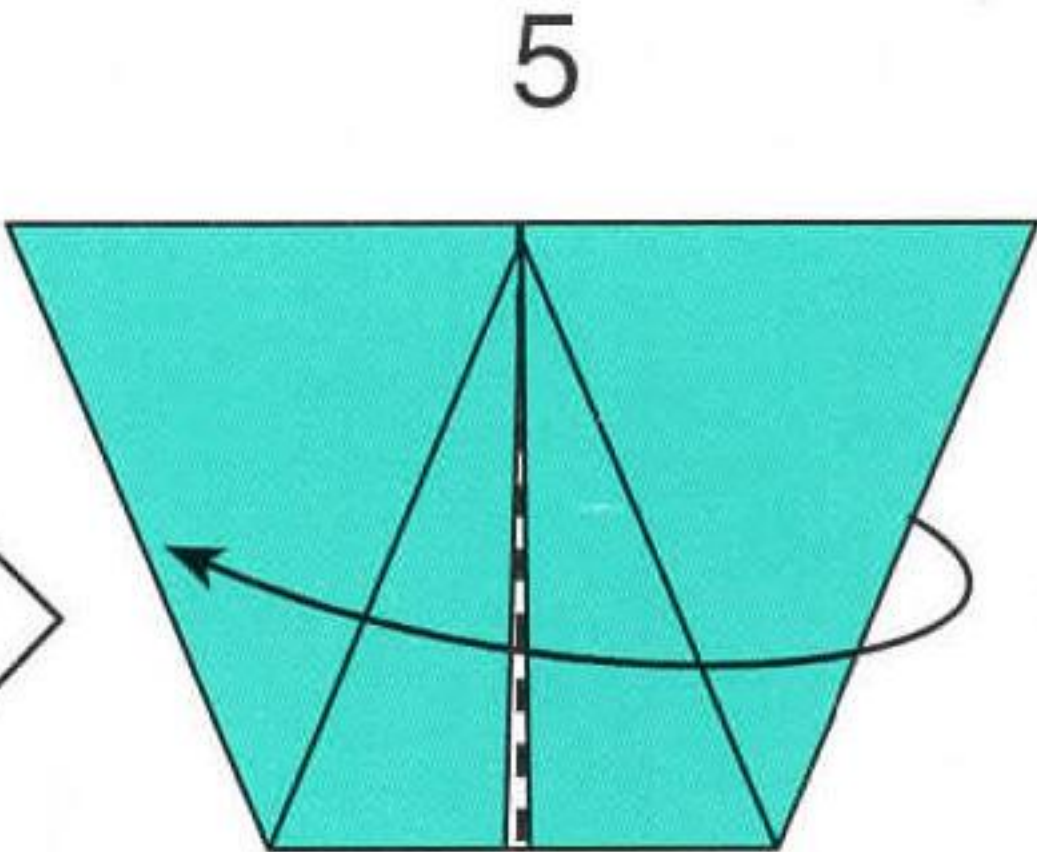
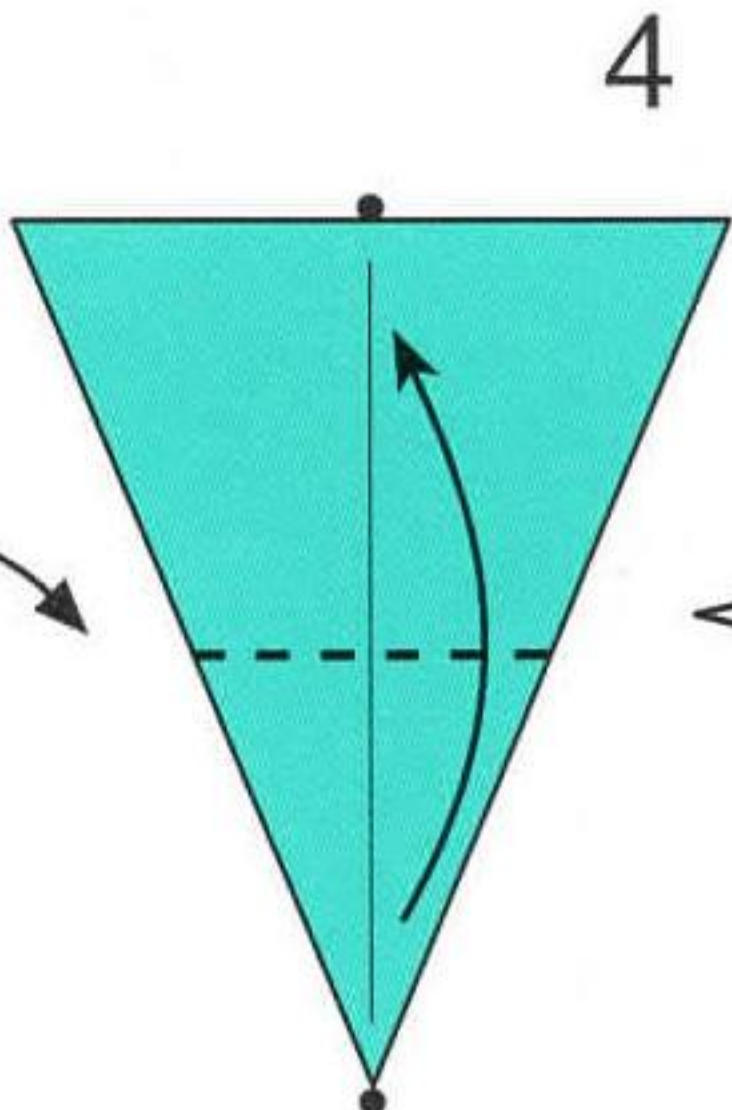
Western Dragon

Theme: Y-pattern

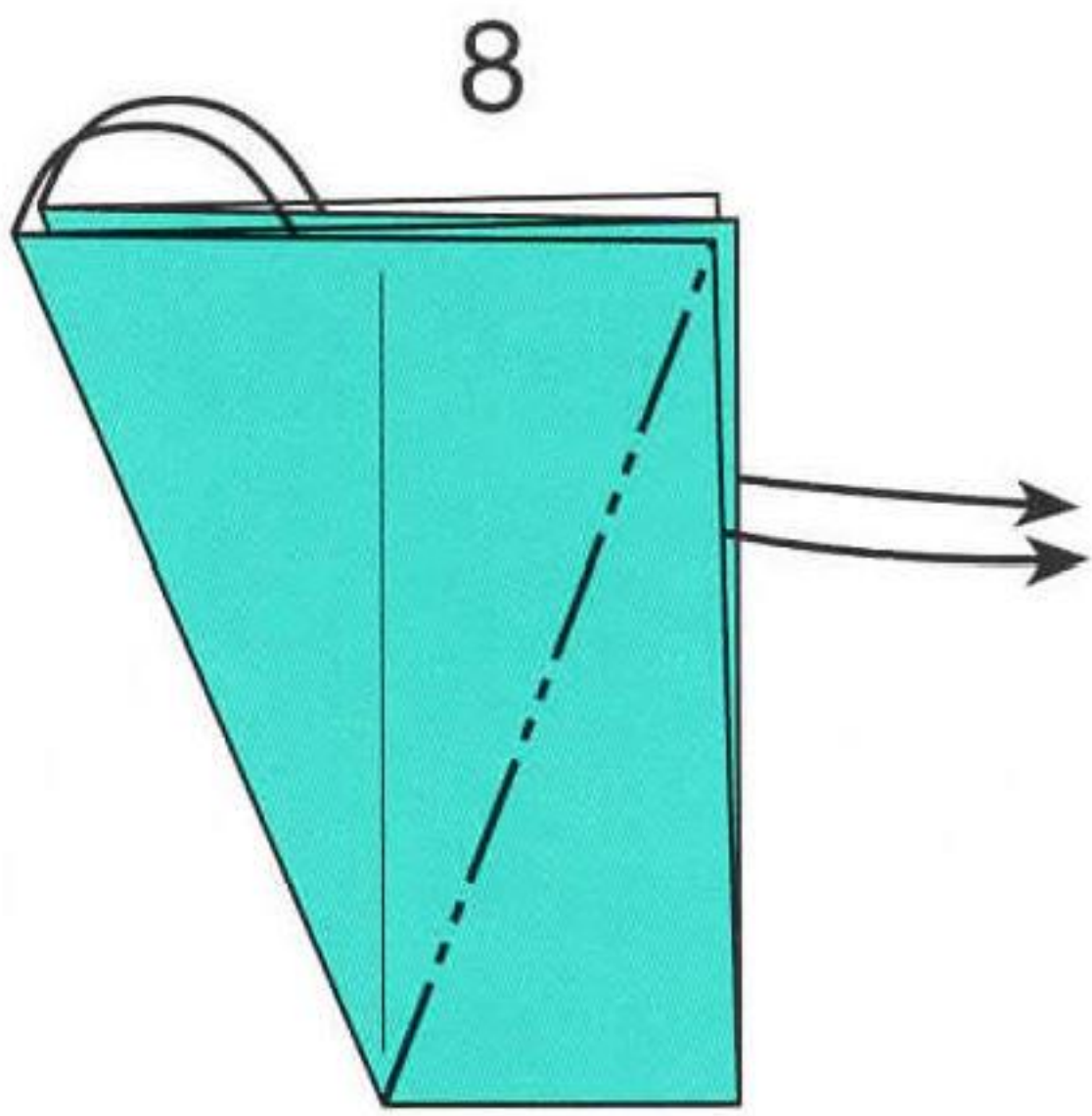
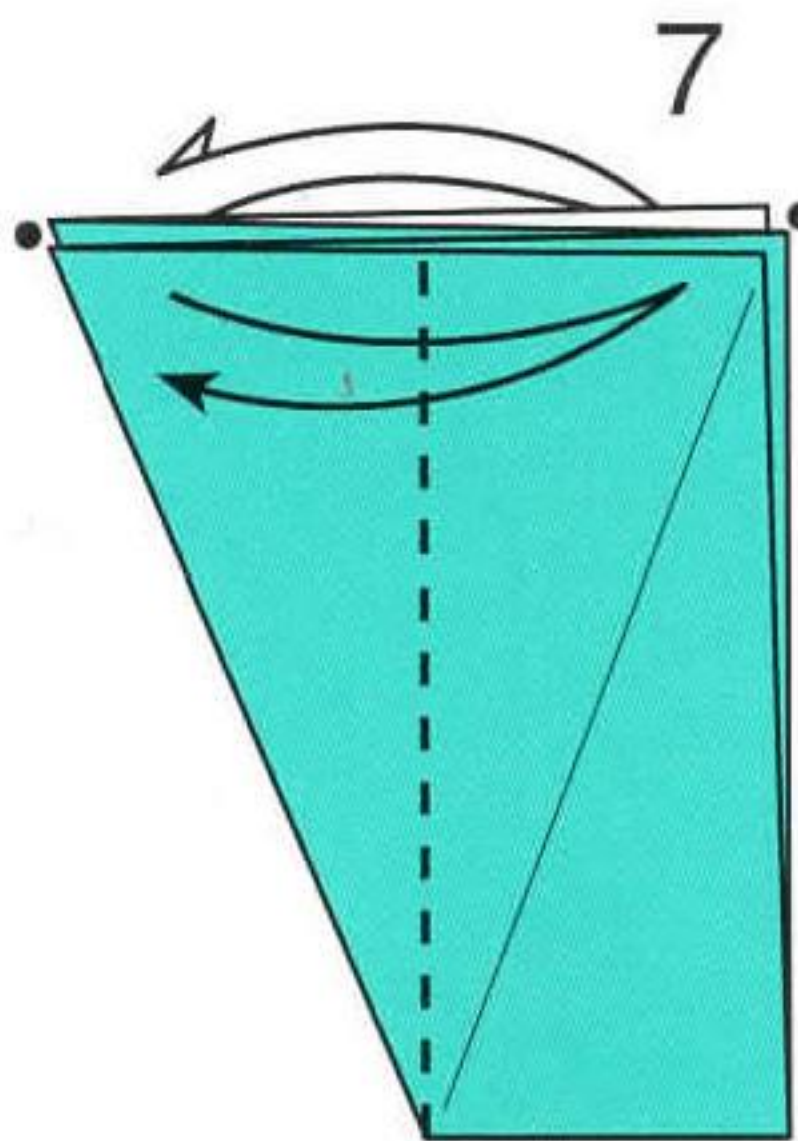
Fold using 6" (15 cm) or preferably larger origami paper.



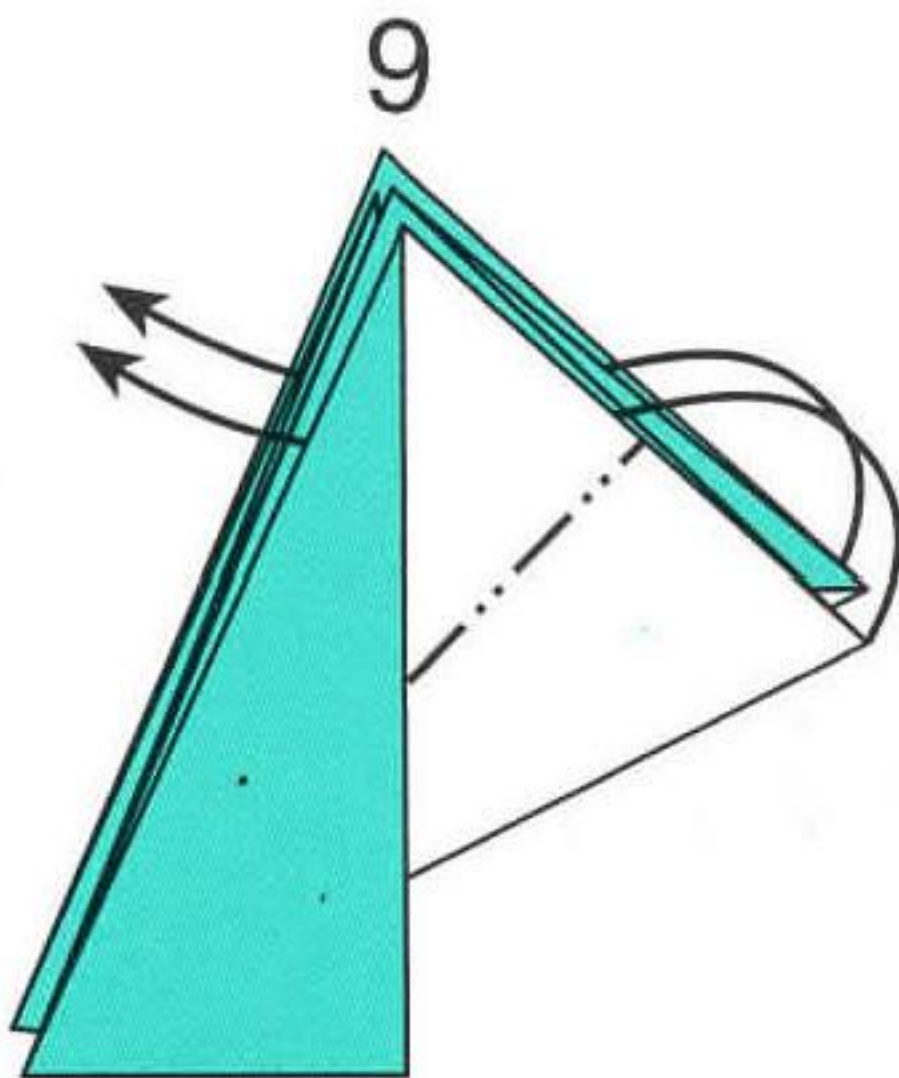
Tuck in.



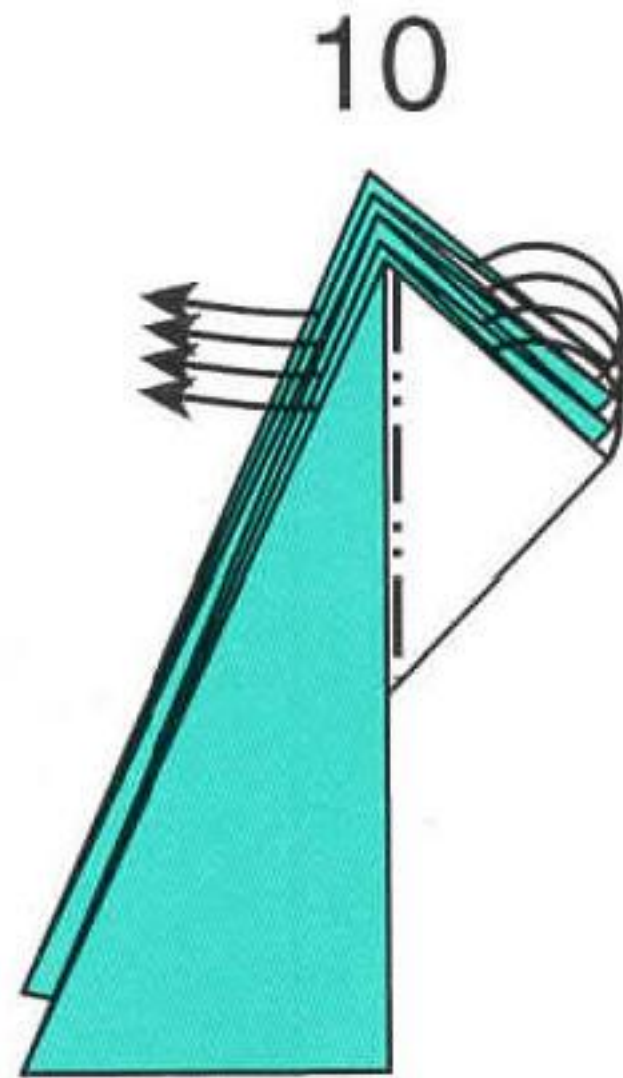
Pay attention to align the inside reverse folds neatly in steps 8-11.



Inside reverse-fold



Inside reverse-fold



Inside reverse-fold



Inside reverse-fold

Y pattern

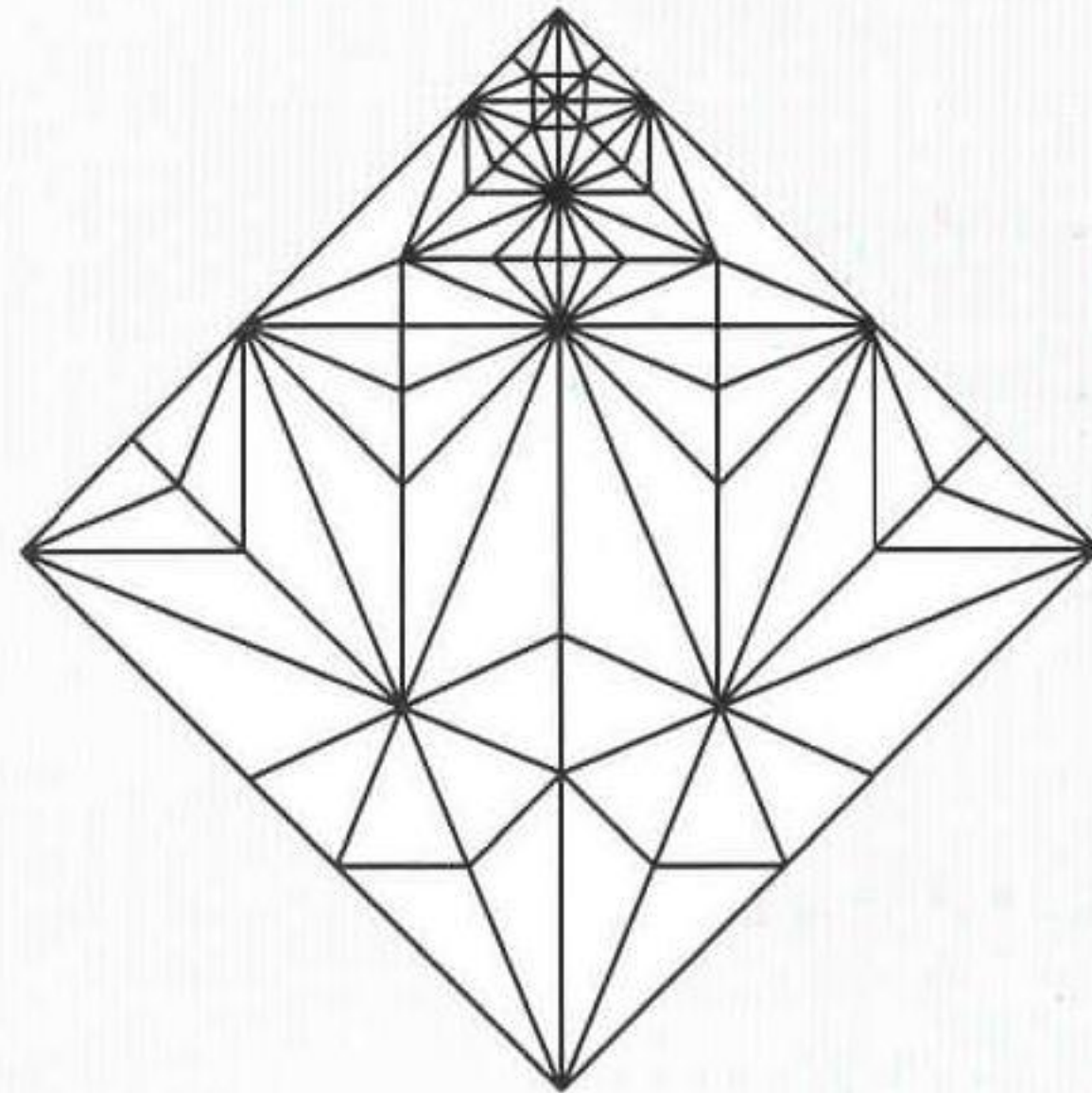
You can see in the crease pattern of *Western Dragon* large and small arrowhead-shaped isosceles triangles (**Y pattern**, shown below). Although it has already appeared repeatedly in *Tree* in **Simple Models** and *Squid* in this chapter, this pattern cannot be seen in any traditional models.

I used to call it "secondary triangle," but in this book I call it "Y pattern."

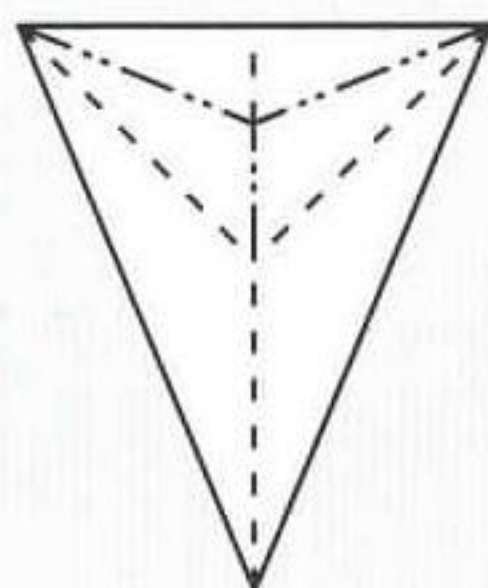
The discovery of this pattern was one of my breakthroughs in my origami design because, in addition to not being used in traditional models, the pattern has a broad range of applications.

This pattern is a kind of "molecule" as "an area with a set of related creases." But it is not single-value or uniaxial, that is, it cannot be folded so that all the edges align. However, it is still handy as an embedded element of design because the angles are standardized.

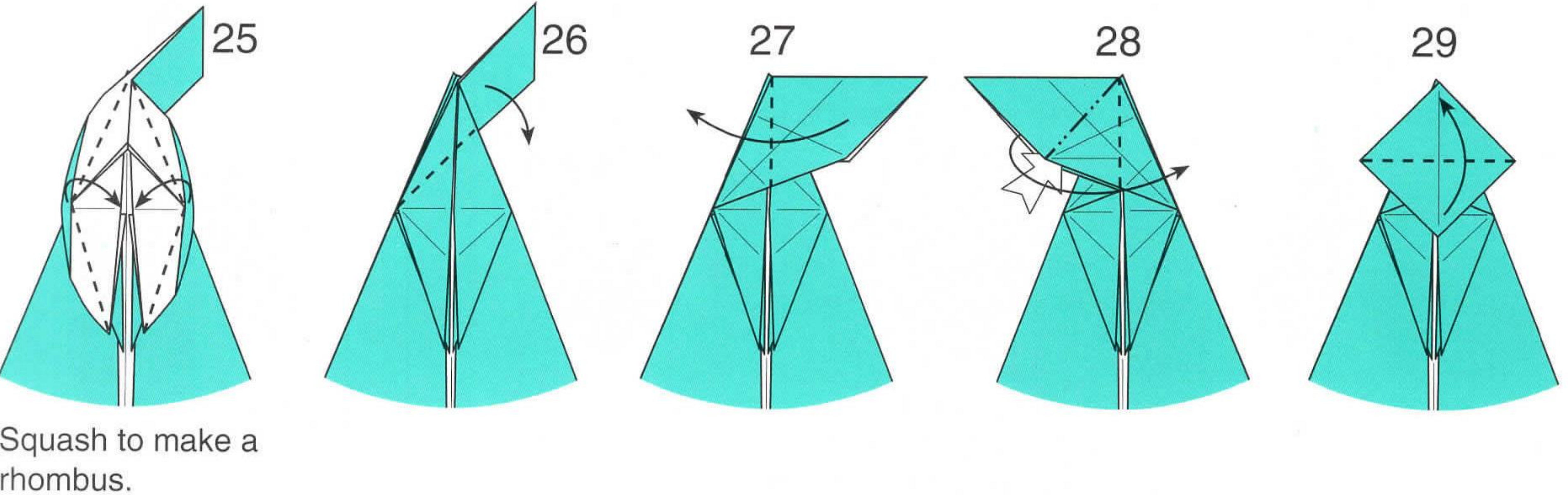
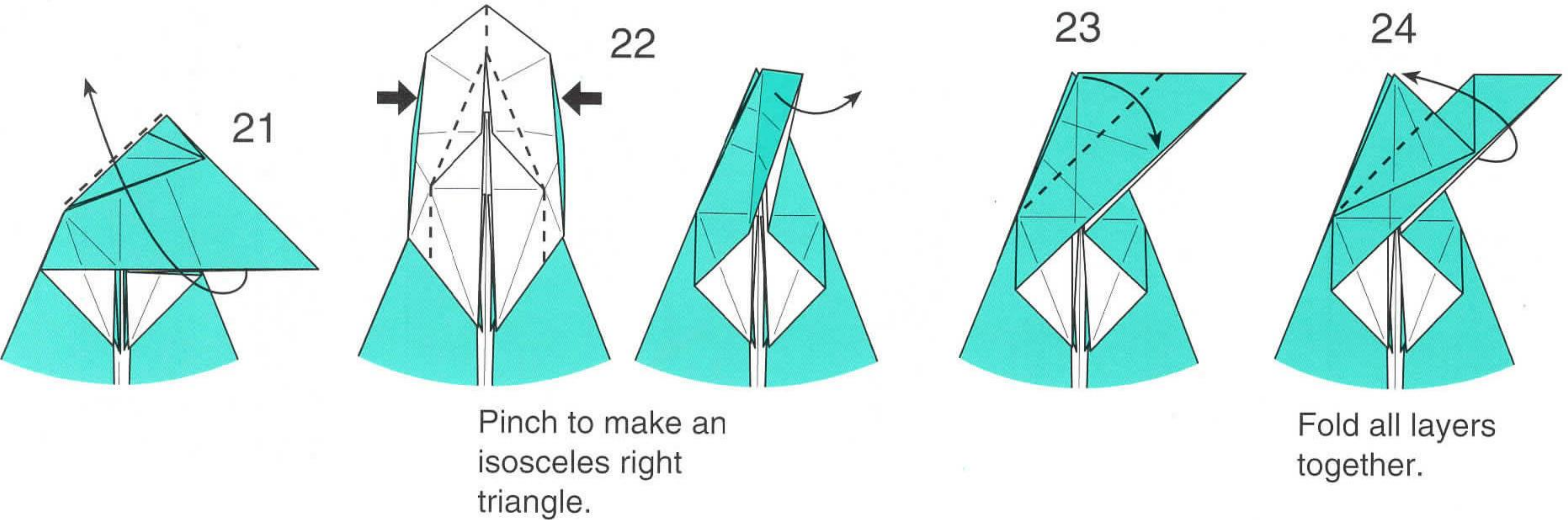
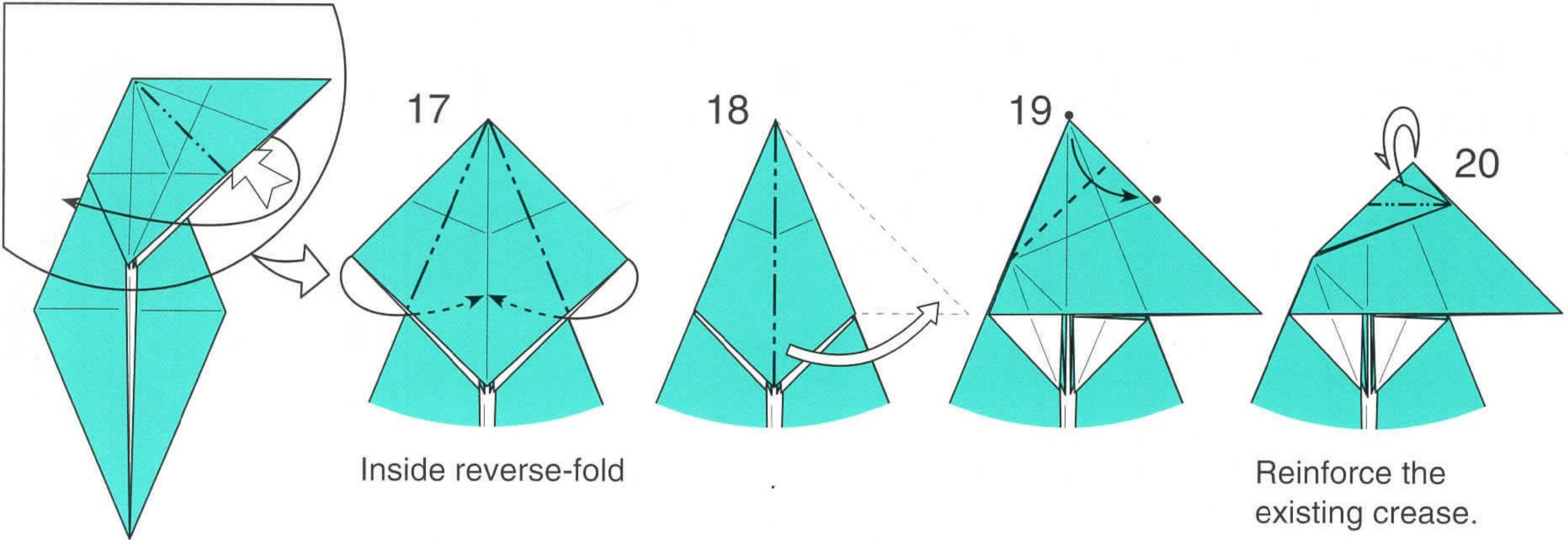
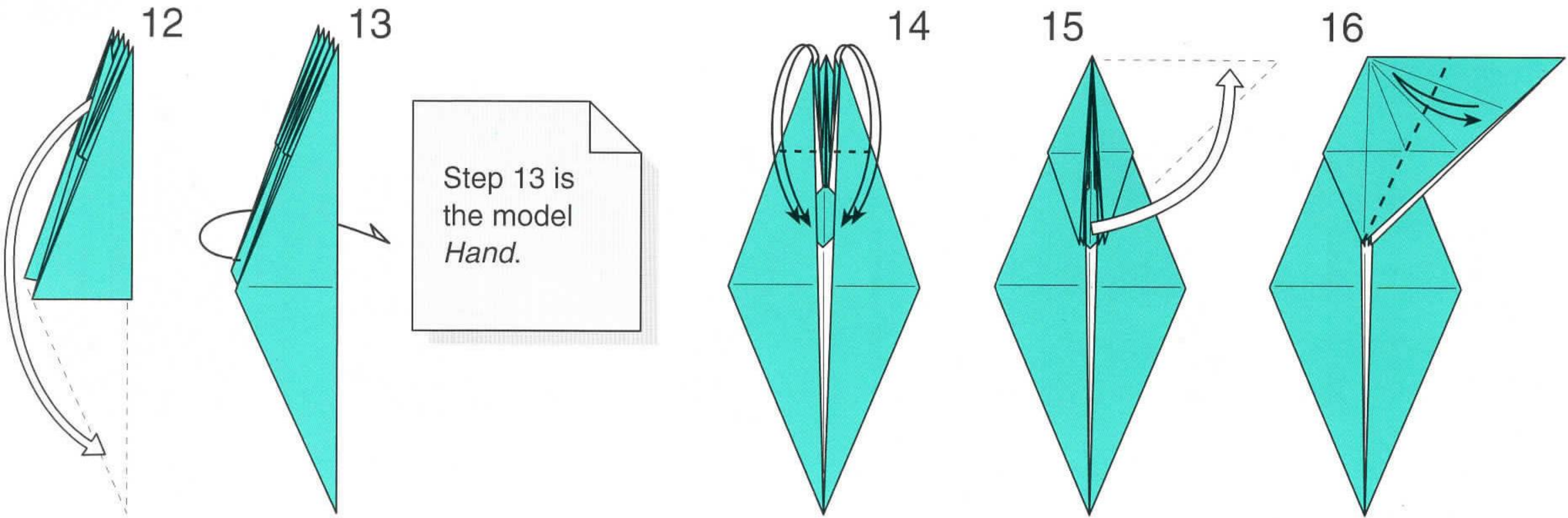
This pattern offers a combination of one long flap and two shorter ones.

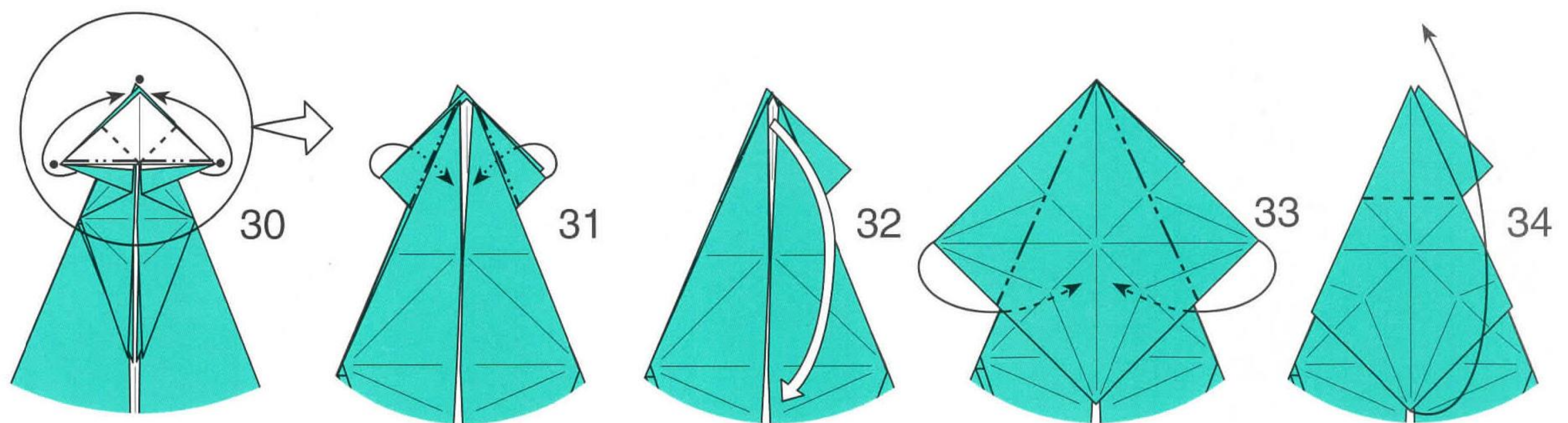


The crease pattern of *Western Dragon* (mountain and valley folds are not shown).



"Y pattern."

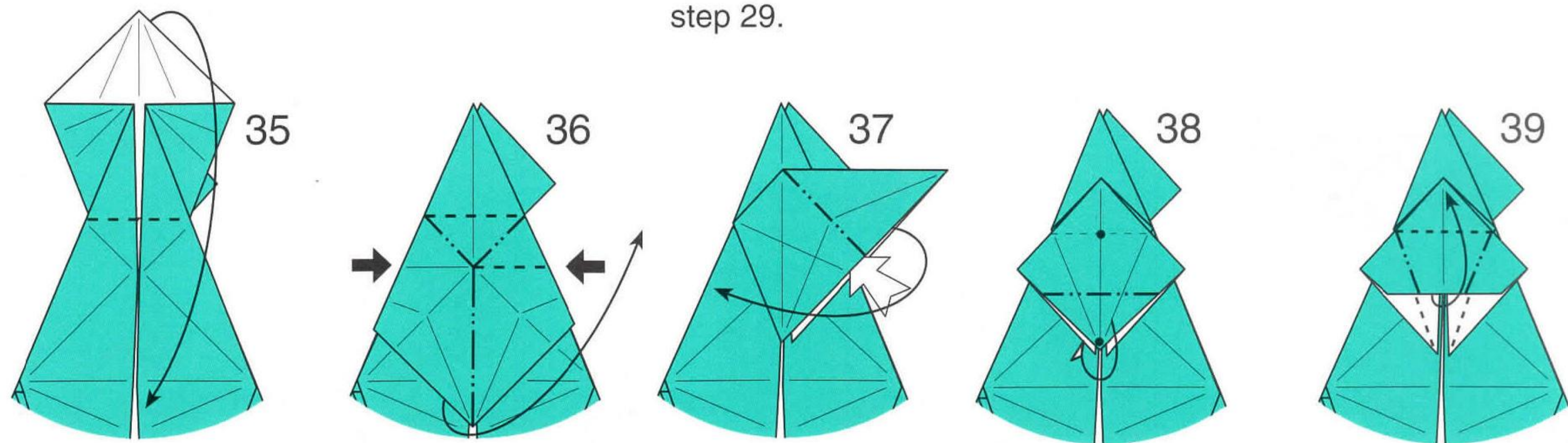




Inside reverse-fold

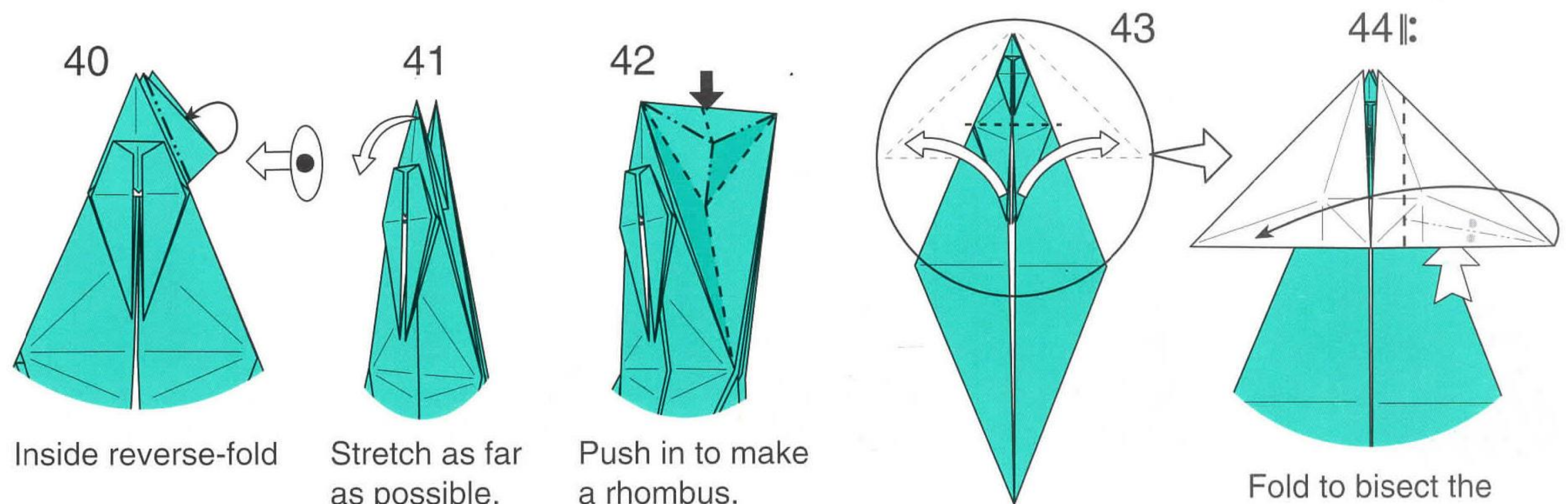
Unfold back to step 29.

Inside reverse-fold



Fold like a Bird base using existing creases.

Petal-fold

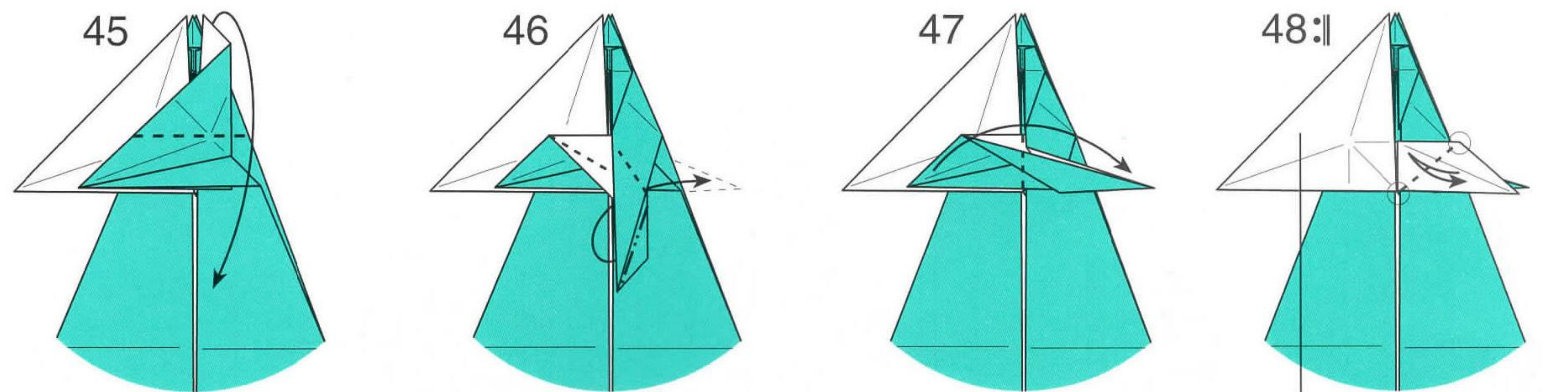


Inside reverse-fold

Stretch as far as possible.

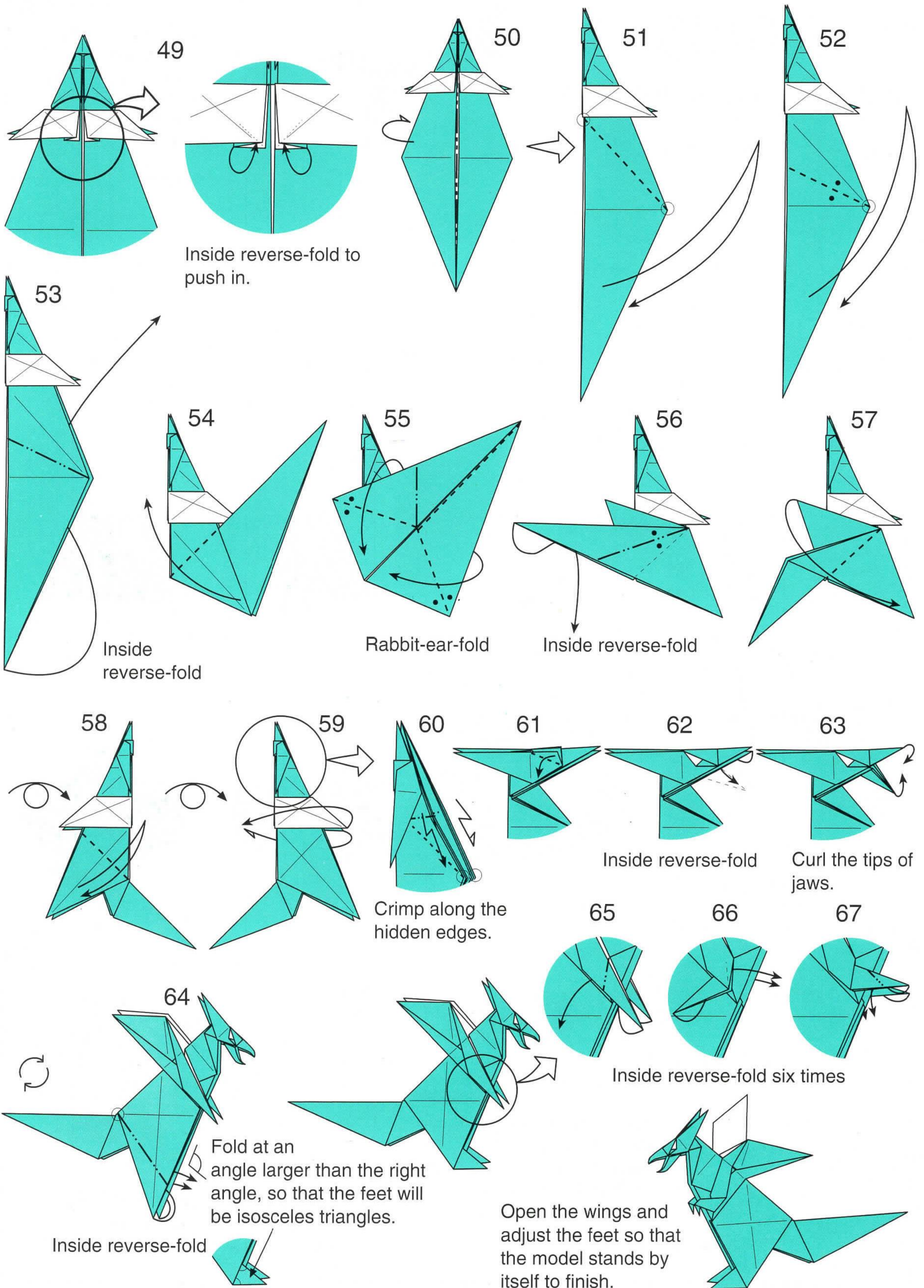
Push in to make a rhombus.

Fold to bisect the angle behind.



Fold like a rabbit ear fold. (The corner of the white triangle will not be bisected.)

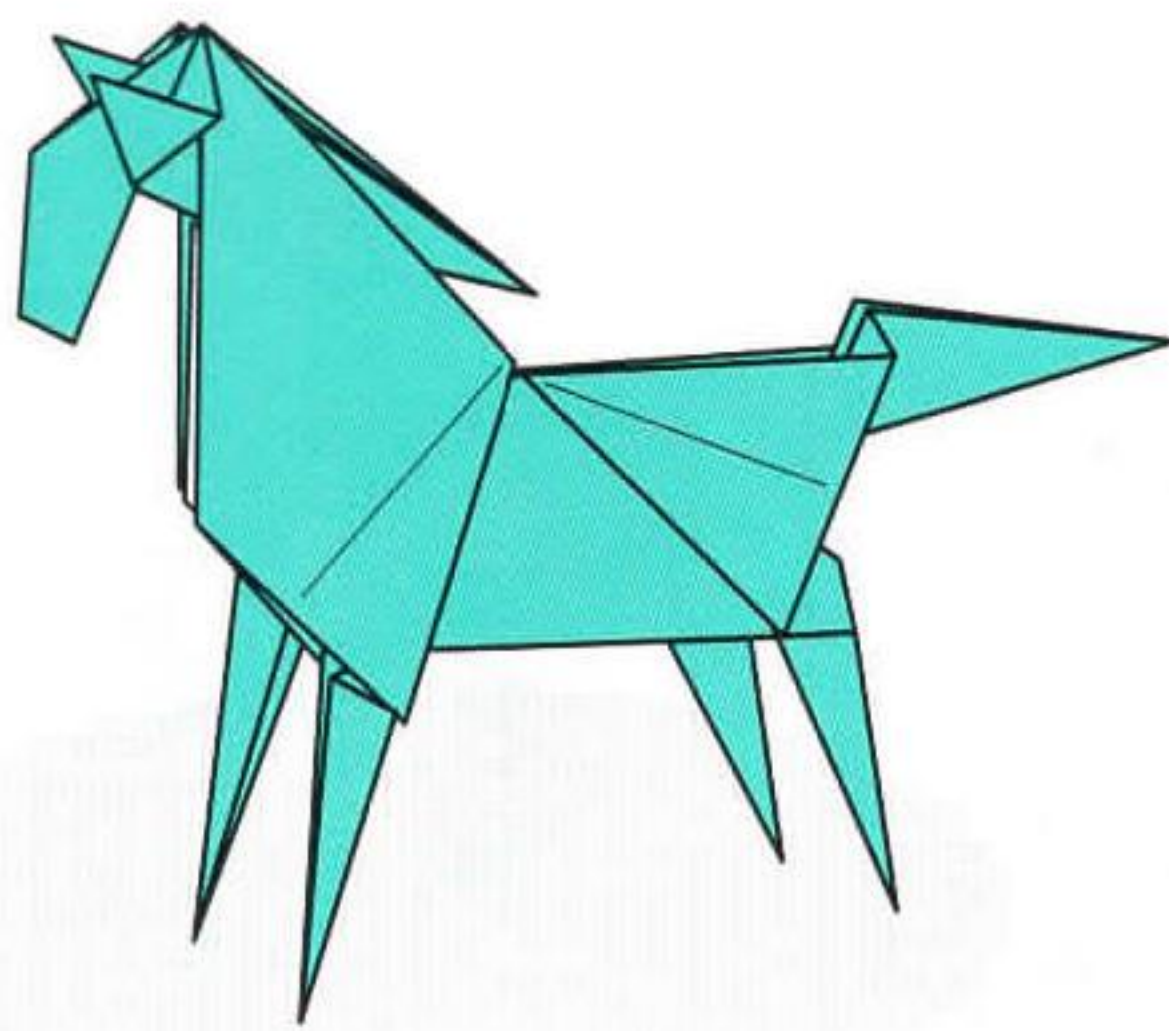
Repeat steps 44-48.



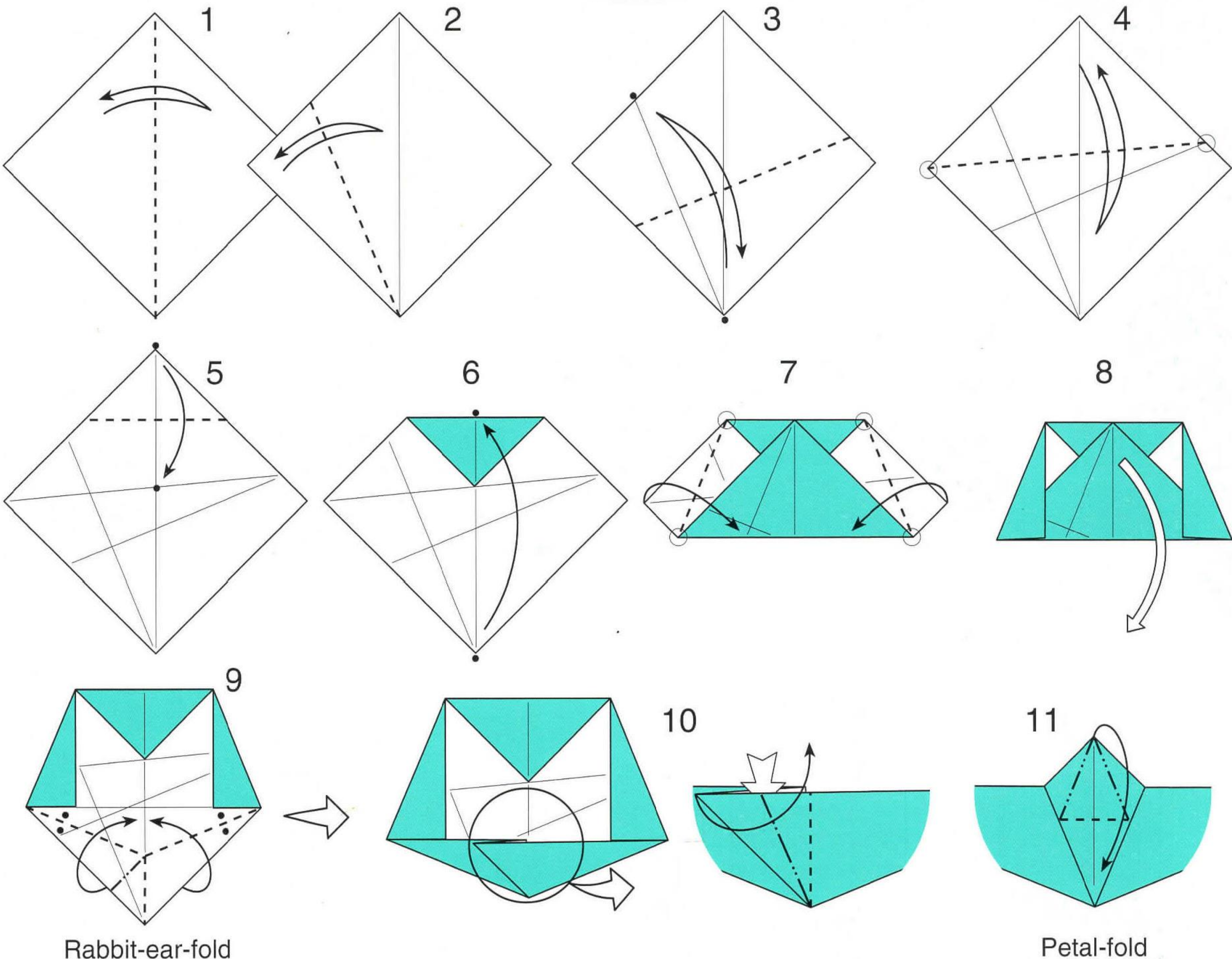
Horse

Theme: Geometric construction

Fold using 6" (15 cm) or preferably larger origami paper.



You can draw a line on a sheet of paper by folding it. At the same time, you can use the sheet itself as a straight-edge and compass, and beyond.

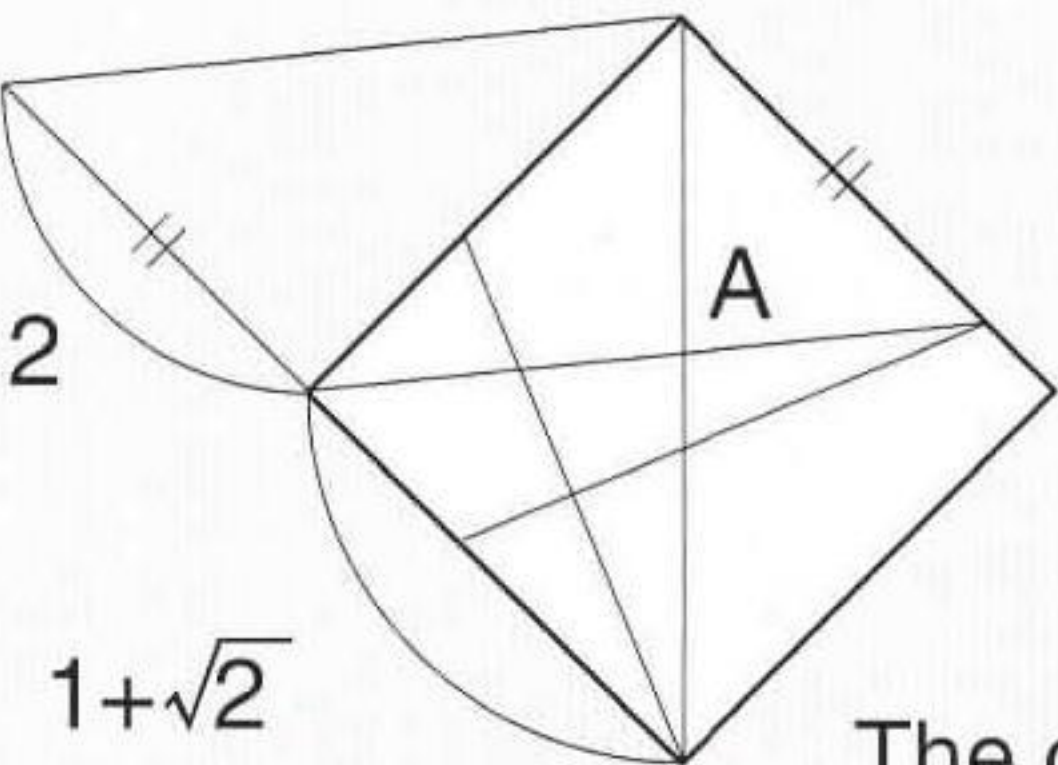


Rabbit-ear-fold

Petal-fold

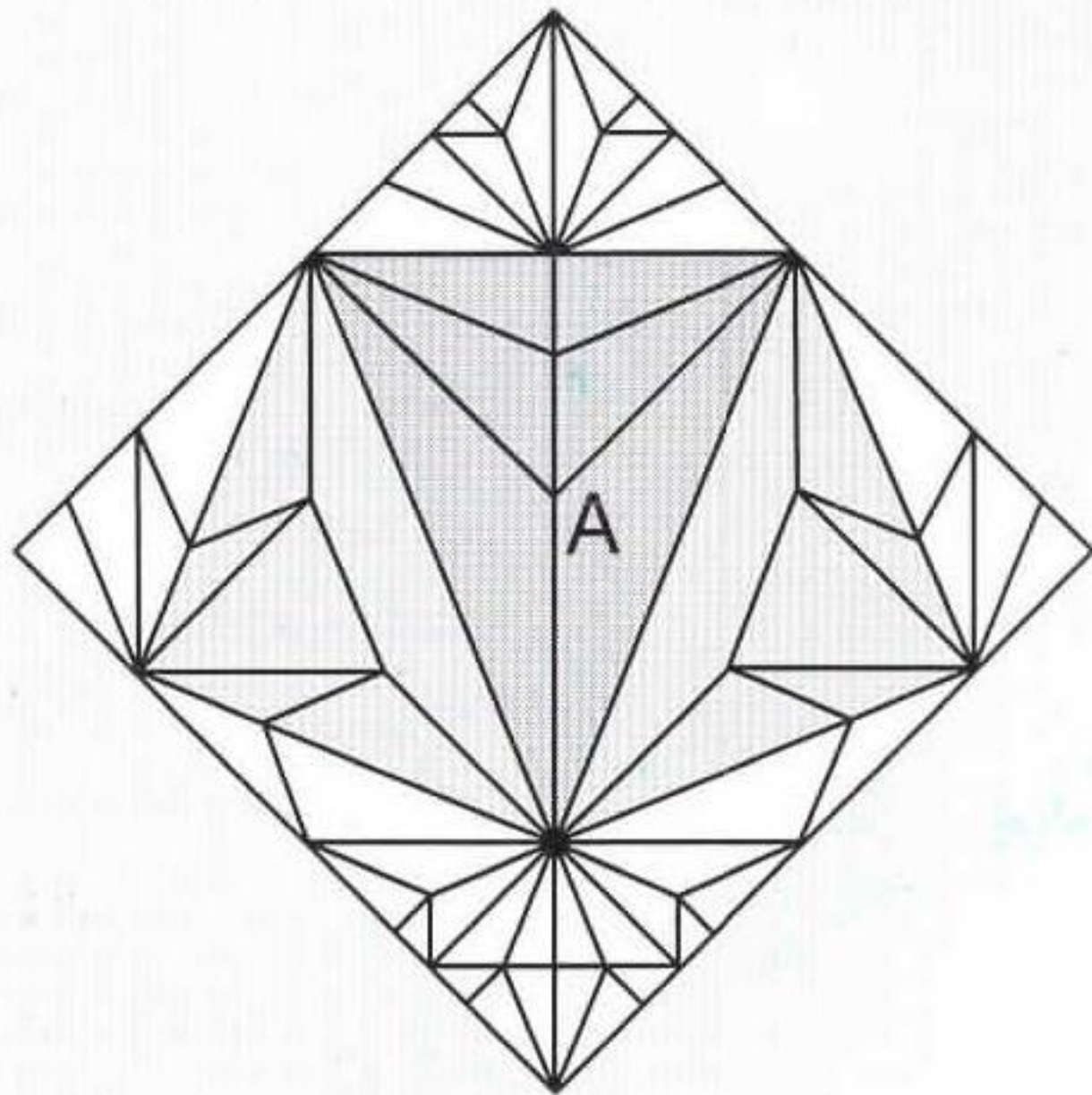
Folding the landmark in this model

While the main design aspect of this Horse is its mane, its structure is the Y pattern at the center with two isosceles right triangles on the sides. Though it is clear, this structure requires some clever folds to find the landmark A, which divides the diagonal in $2 : 1 + \sqrt{2}$. The picture below explains the meanings of the construction made in steps 1-4.

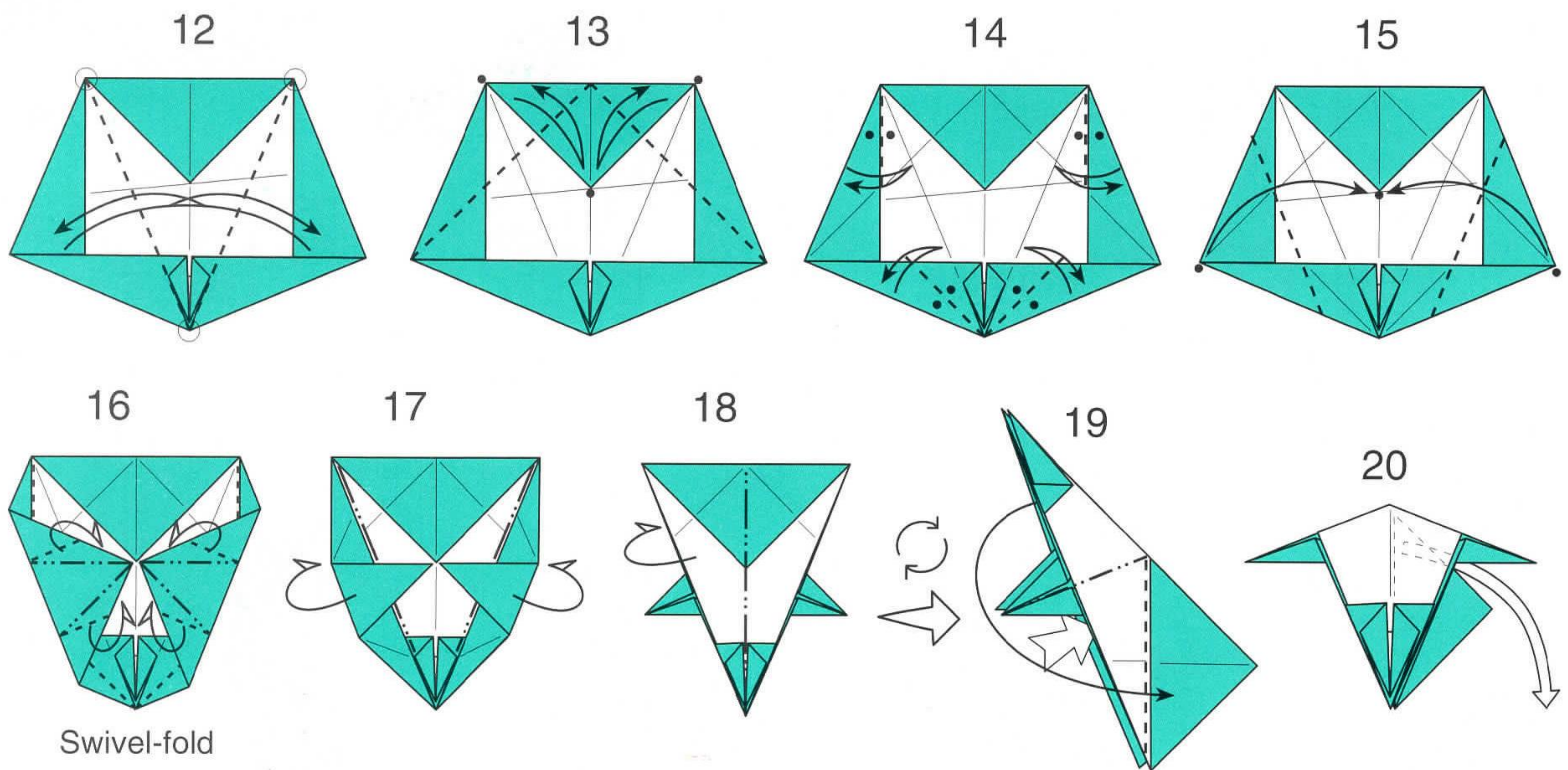


The construction made in step 1-4

We extend the side to obtain the desired ratio, and transfer that ratio onto the diagonal by folding the parallel line. This method can be applied in many cases.



The crease pattern of *Horse* (mountain and valley folds are not shown; underlying triangles are shown in gray).



Constructions in origami

We have already seen some constructions in this book, such as the trisection of a side with Haga theorem in *Conch*, dividing a side into five in *Gift Box*, and folding the golden ratio in *Connected Cranes: Kotobuki*. Because folding flat is equal to drawing a straight line, it is natural to regard origami as a tool for geometric constructions.

Humiaki Huzita formulated six folds, each of which draws one straight line that has definite landmarks, and Jacques Justin added the seventh. Huzita called them axioms, but they are not axioms in the mathematical sense. They are rather “origami procedure that draws one straight line.”

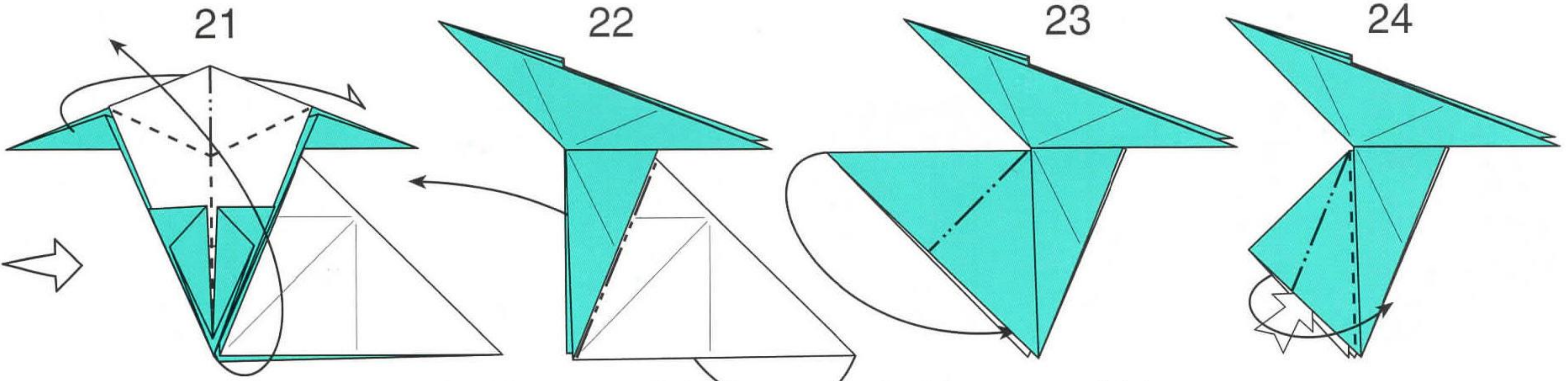
1. Fold a point onto another point.
2. Fold a line onto another line.
3. Fold along the line connecting two points.
4. Fold along the line that passes through a point and is perpendicular to a line.
5. Fold along the line that passes through a point and places another point onto a line.
6. Fold a point onto a line and another point onto another line.
7. Fold along the line that places a point onto a line and is perpendicular to another line.

The combination of folds 1 through 5 is equivalent to solving quadratic equations, which in turn is equivalent to the constructions with a straight-edge and compass. The construction in this *Horse* and other constructions like making a pentagon are possible with these folds. A typical example of fold 4 is step 4 of *Tree*, and that of fold 5 is step 3 of *Penguin*, which comes later in this book.

By adding fold 6, some constructions that are impossible with a straight-edge and compass become possible, since the fold is equivalent to solving cubic equations. Fold 6 is not unnatural. In fact, fold 3, which corresponds to drawing a line with a straight-edge, is sometimes more difficult than fold 6 unless points are placed on the edges.

Hisashi Abe emphasized these when he solved two of three **Classical Greek Problems**, **angle trisection** and **doubling the cube**, using fold 6.

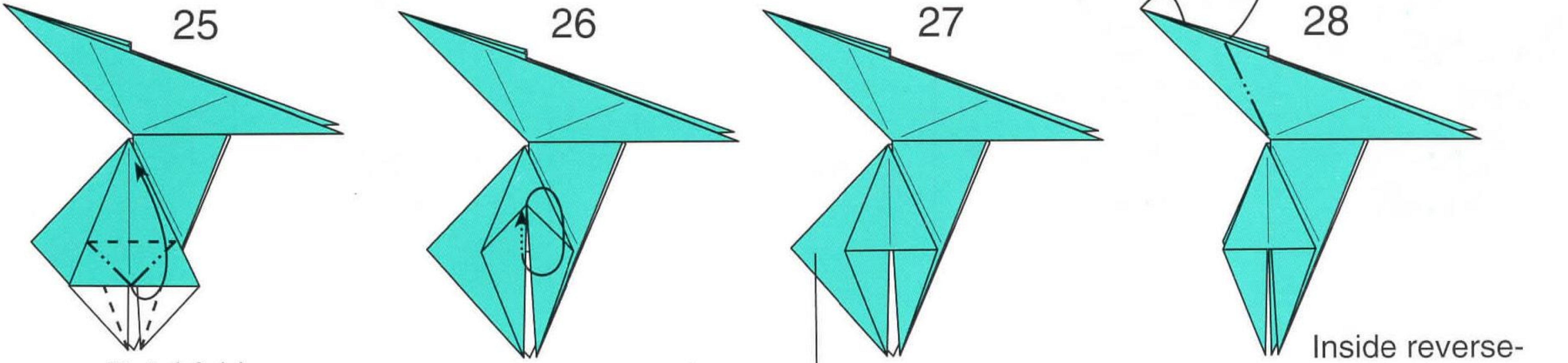
Note that these two problems cannot be solved with finite procedures of a straight-edge and compass. In the 19th century, Pierre Wantzel proved this by relating geometric constructions to the order of equations. It is also known that these constructions are possible if we use special tools. That is, origami is just one of such tools that is different from a straight-edge and compass. The other problem, **squaring a circle**, is also proved to be impossible because it involves the circular constant, which makes this problem more difficult.



Rabbit-ear-fold while folding the model in half

Inside reverse-fold

Inside reverse-fold

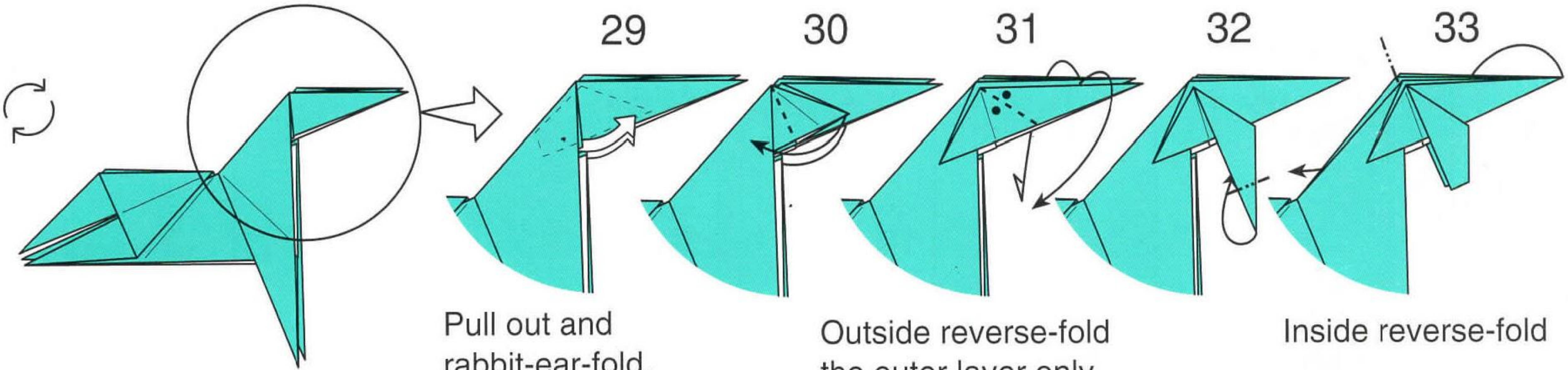


Petal-fold

Reverse the flap inside.

Repeat steps 24-26.

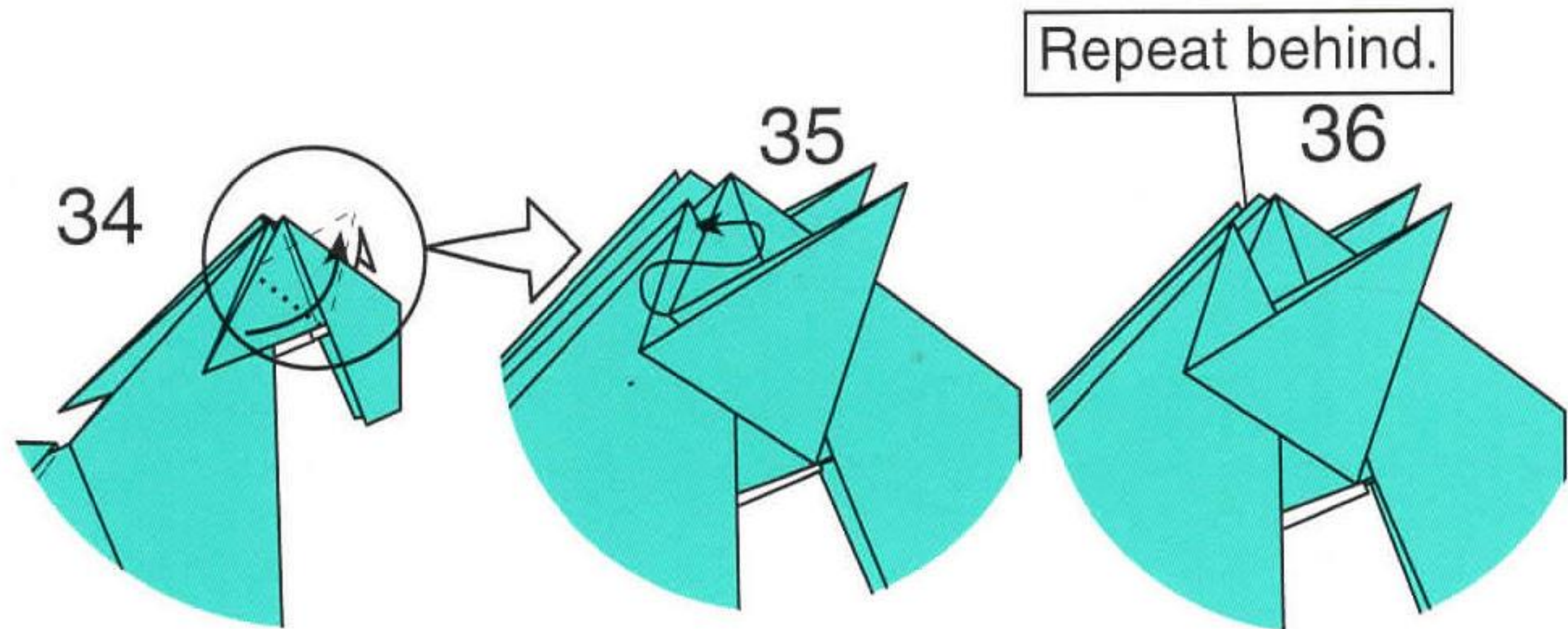
Inside reverse-fold through the center gap using the existing creases



Pull out and rabbit-ear-fold.

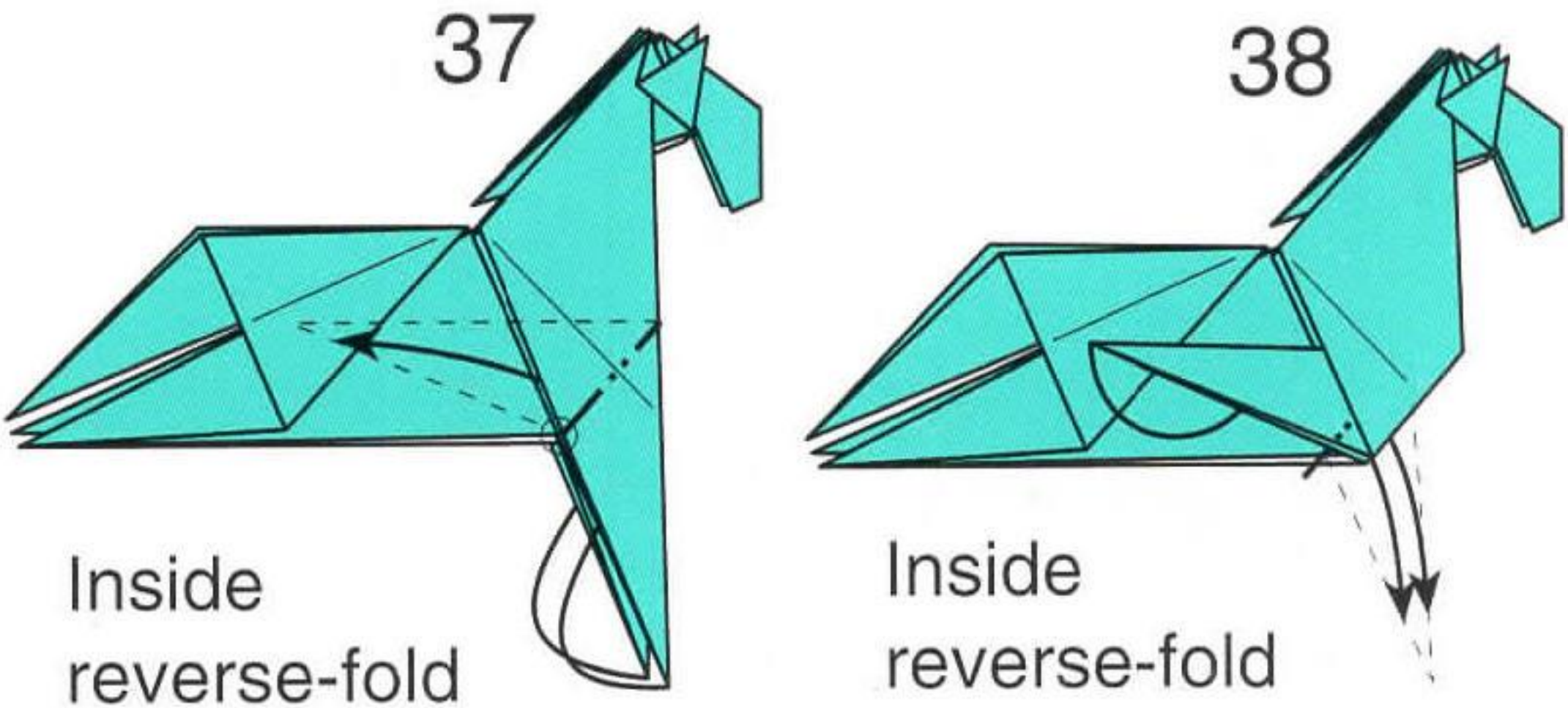
Outside reverse-fold the outer layer only

Inside reverse-fold



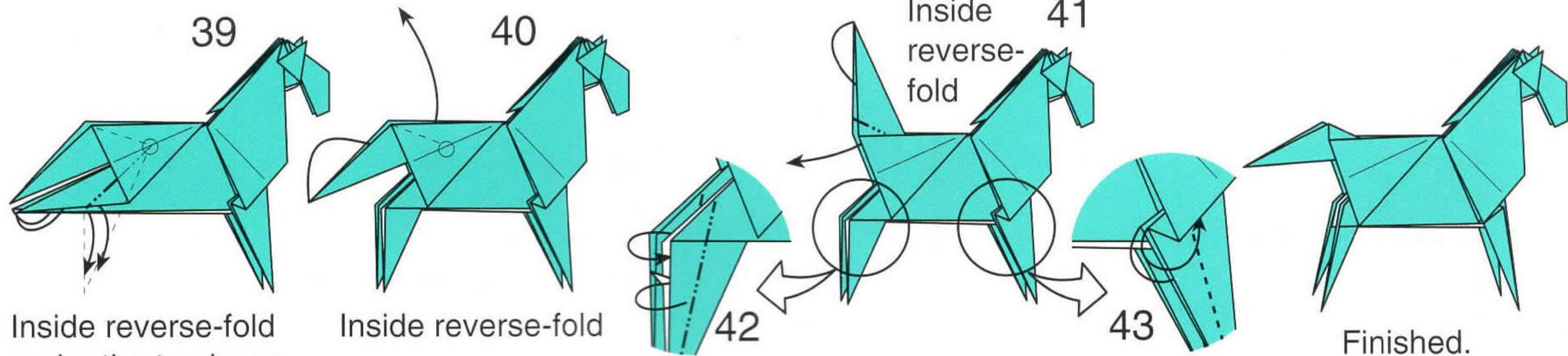
Change the order of the layers to keep the head closed and to open the layers for the mane.

Repeat behind.



Inside reverse-fold

Inside reverse-fold



Inside reverse-fold under the top layer

Inside reverse-fold

Inside reverse-fold

Inside reverse-fold

Repeat behind.

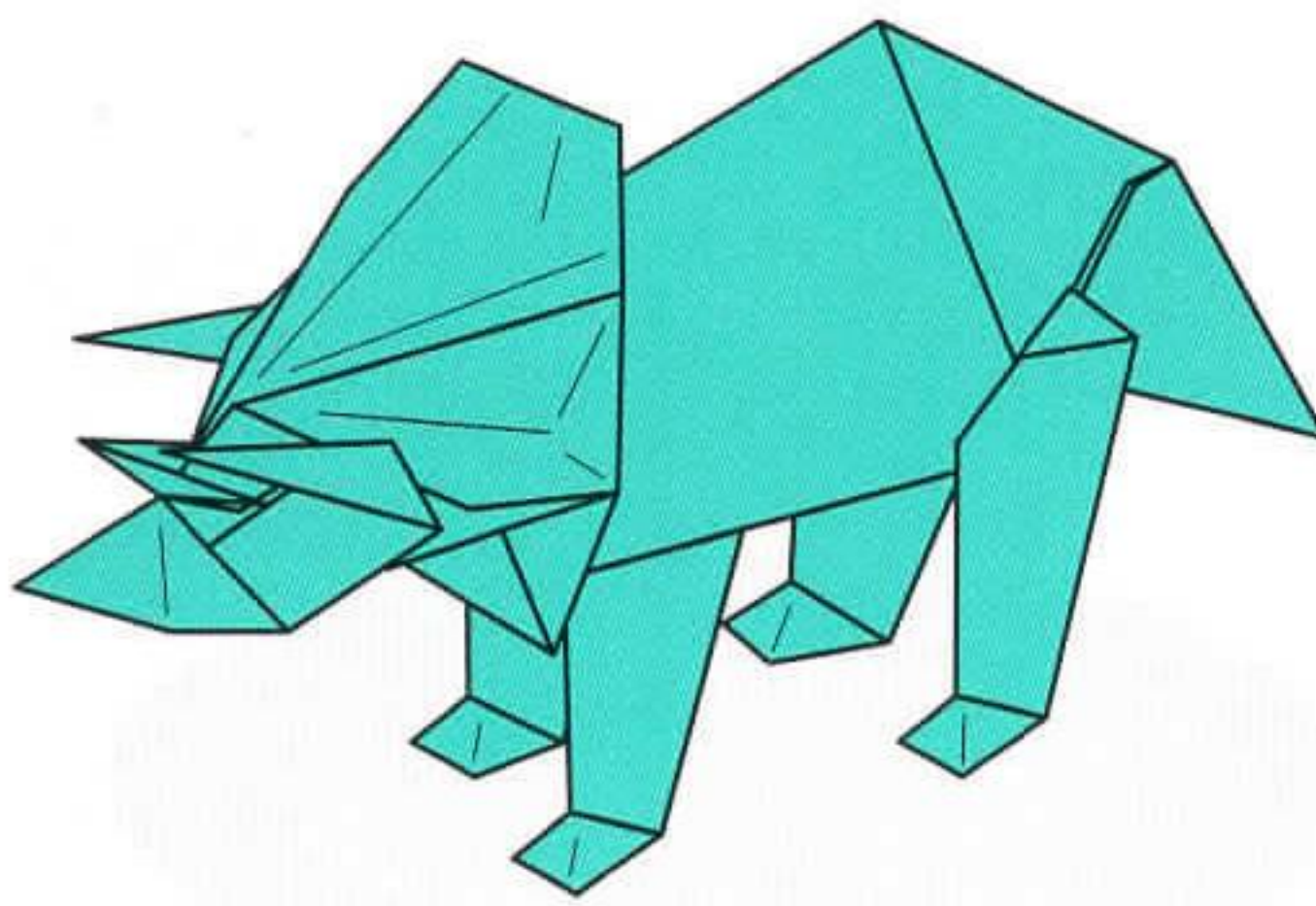
Inside reverse-fold

Finished.

Triceratops

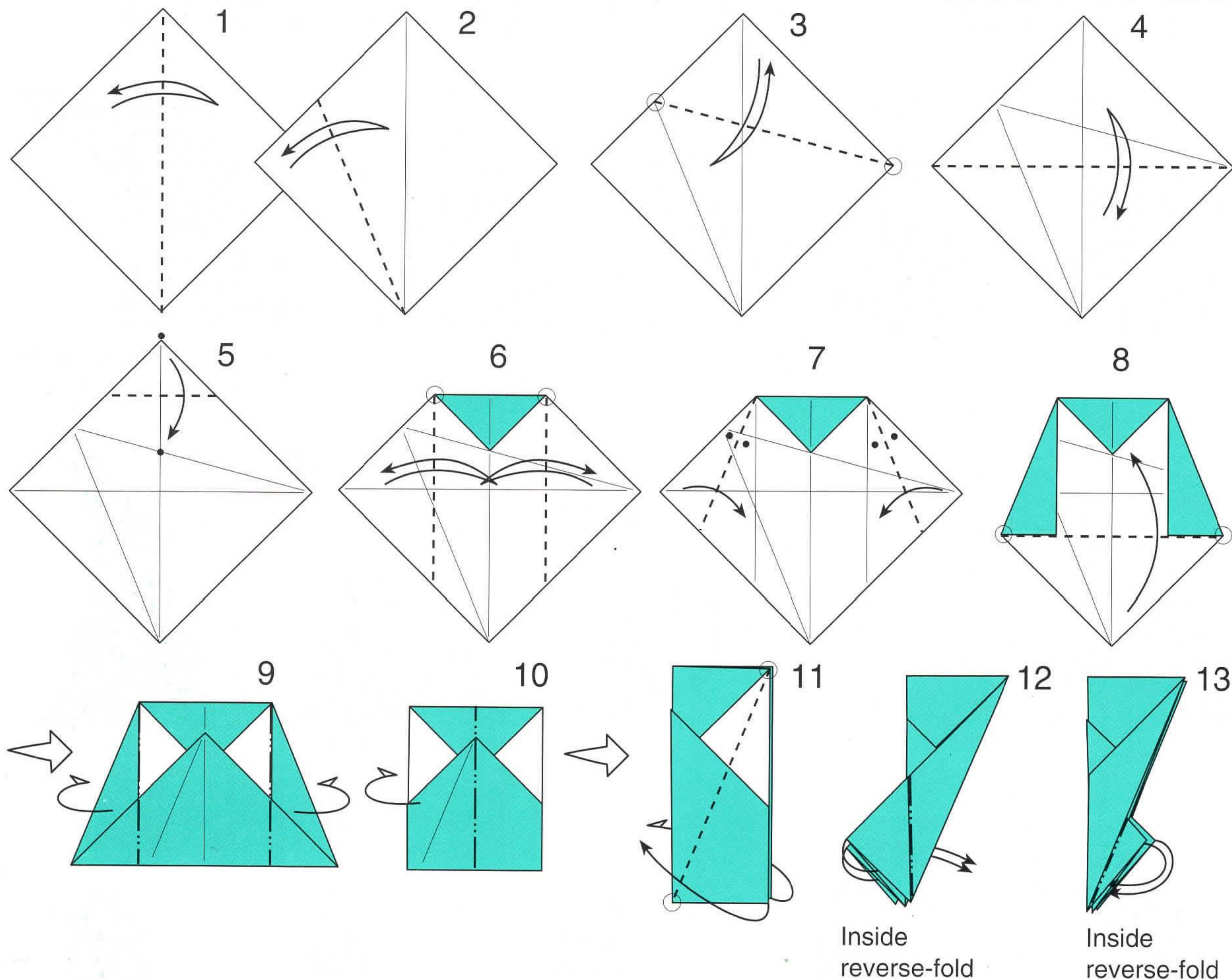
Theme: Open-back, Open-belly

Fold using 6" (15 cm) or preferably larger origami paper.



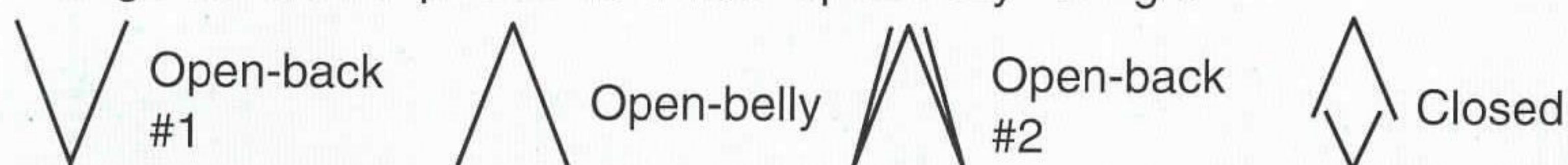
This model, like Horse, requires some construction to find the landmark.

Steps 1-3 indicates the ratio of $\sqrt{2} : 1 + \sqrt{2}$.

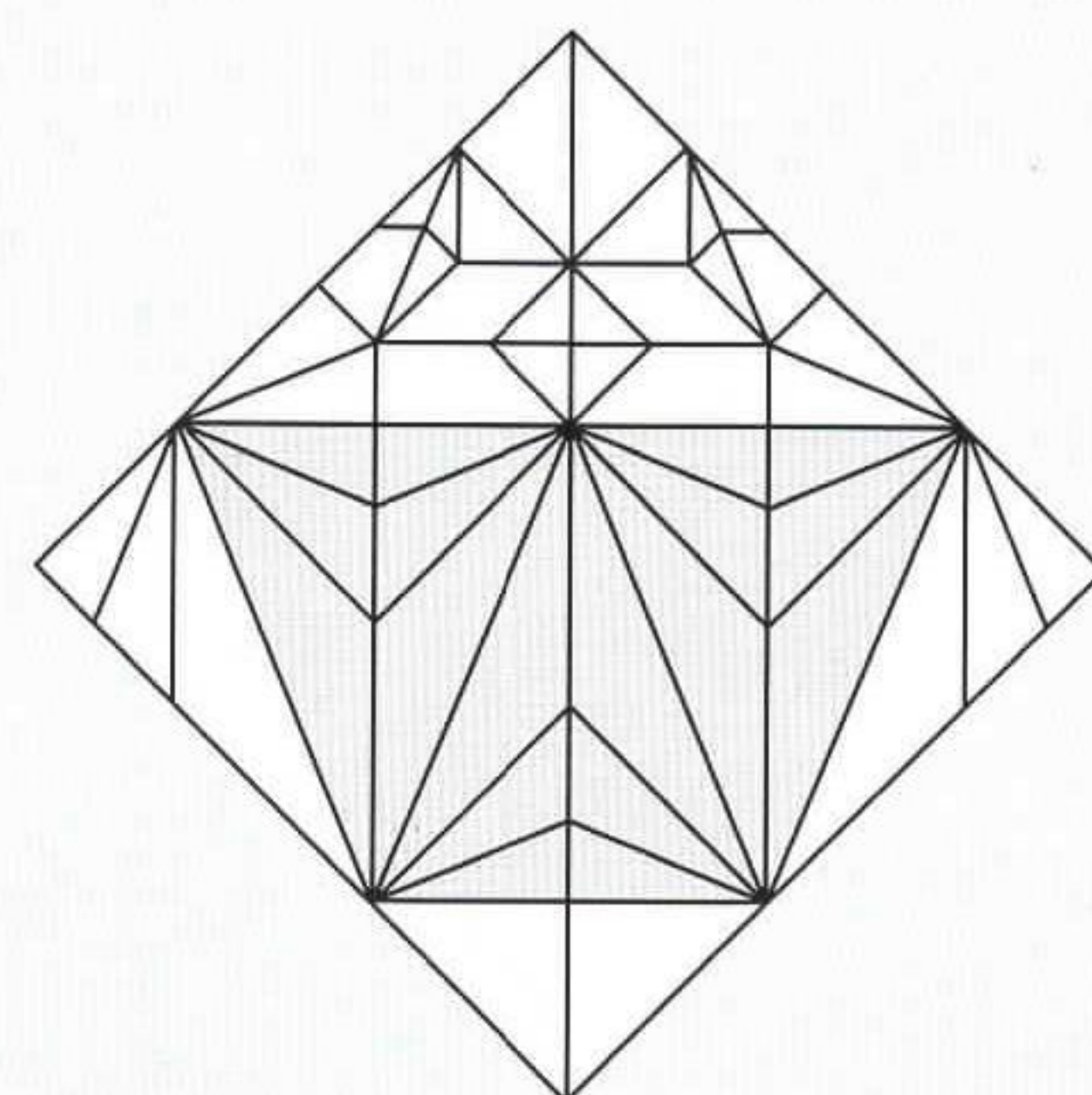


Open-back and open-belly

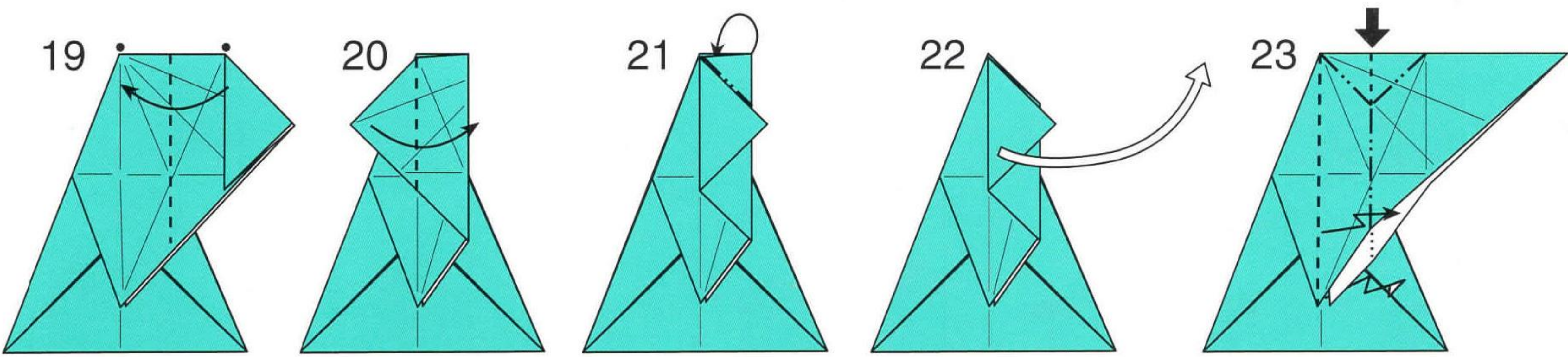
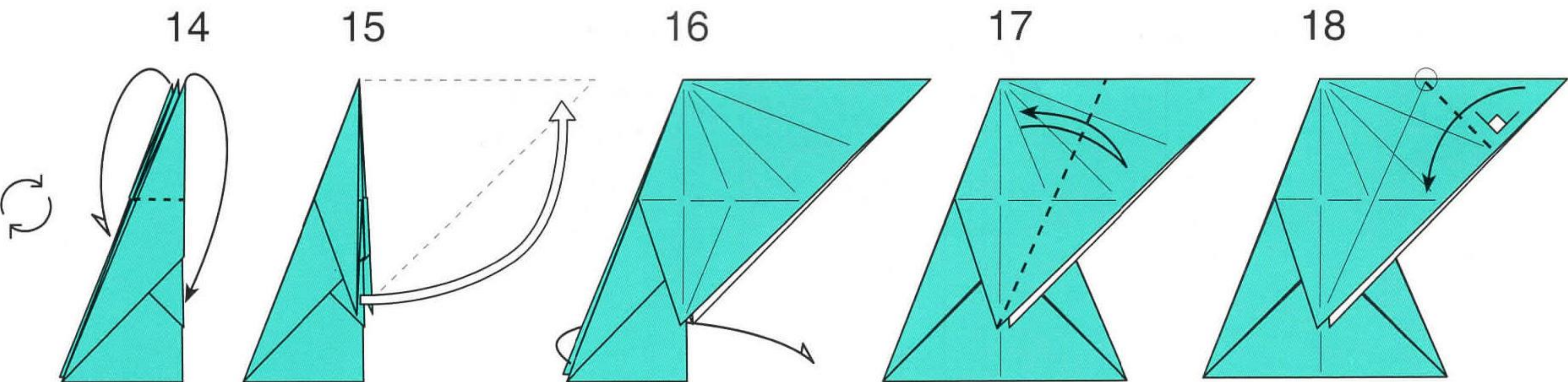
The design of origami animals can be classified by their cross sections, as shown below. Open-back design should be avoided when we want to emphasize the broad back of an animal. A Triceratops is one of such animals. I once designed a triceratops, with the almost same crease pattern as this model, using "open-back #2" design. But I was not satisfied for that reason, and modified the model by reversing upside down. Then I was able to change the crease pattern to a nice "open-belly" design.



Such reverse method does not always work well. But reversing an existing design upside down or front-side back often results in a different "mitate." For example, if you reverse the head and tail of *Three-headed Crane*, you may see it as a phoenix, if not a crane.

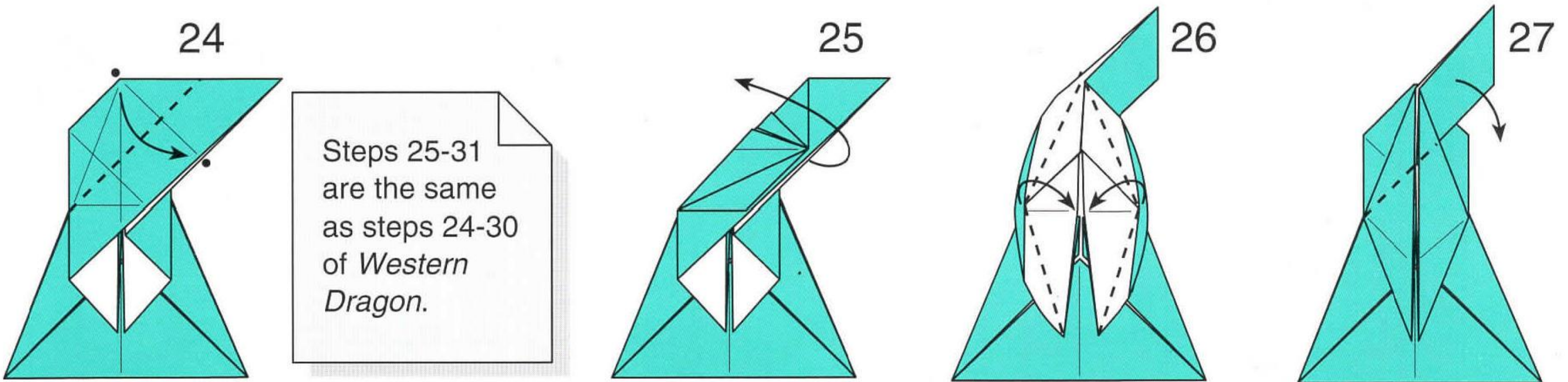


The crease pattern of *Triceratops* (mountain and valley folds are not shown; "Y patterns" are shown in gray).



Inside reverse-fold

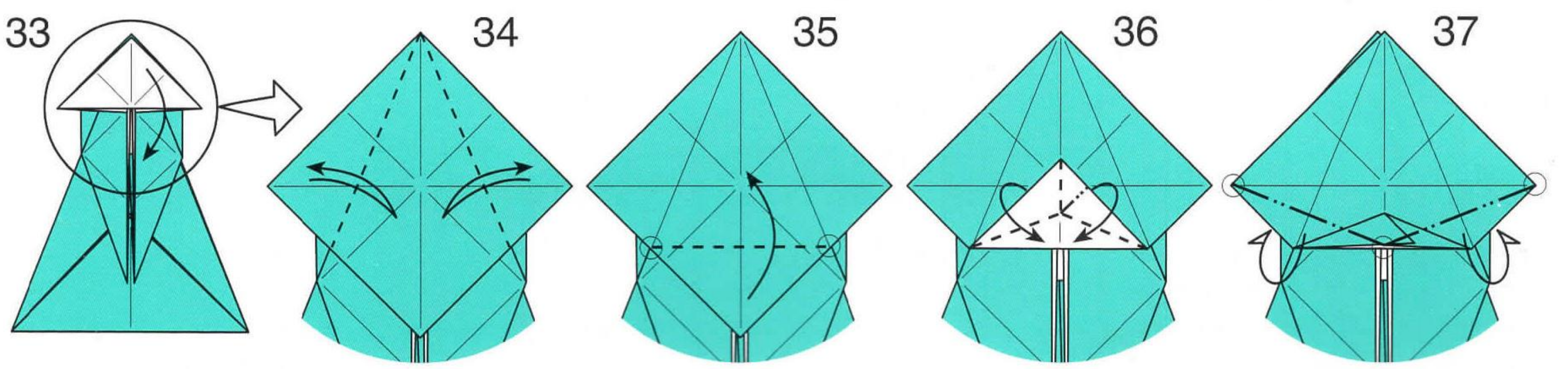
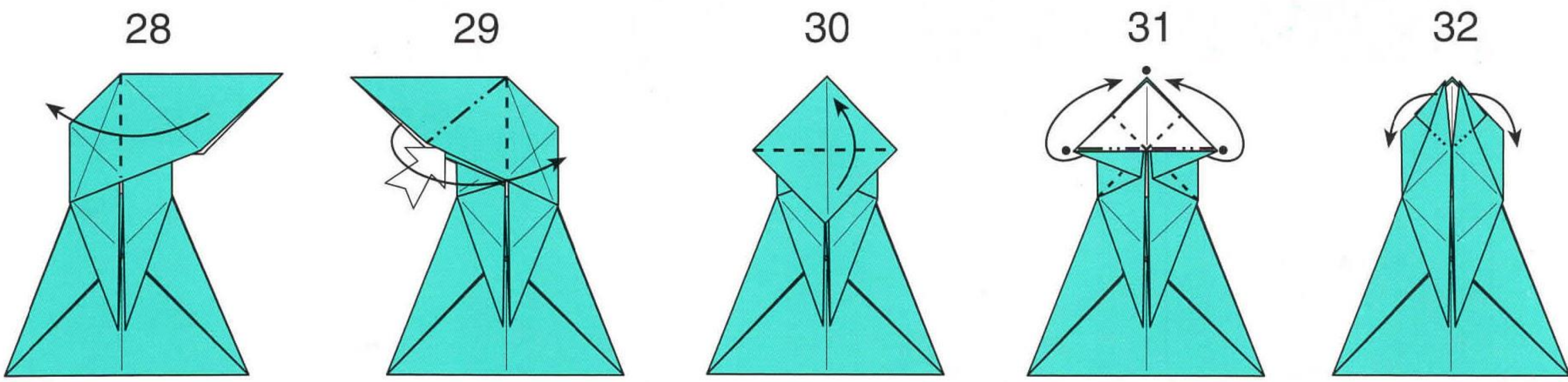
Pleat on both sides while popping down the top.



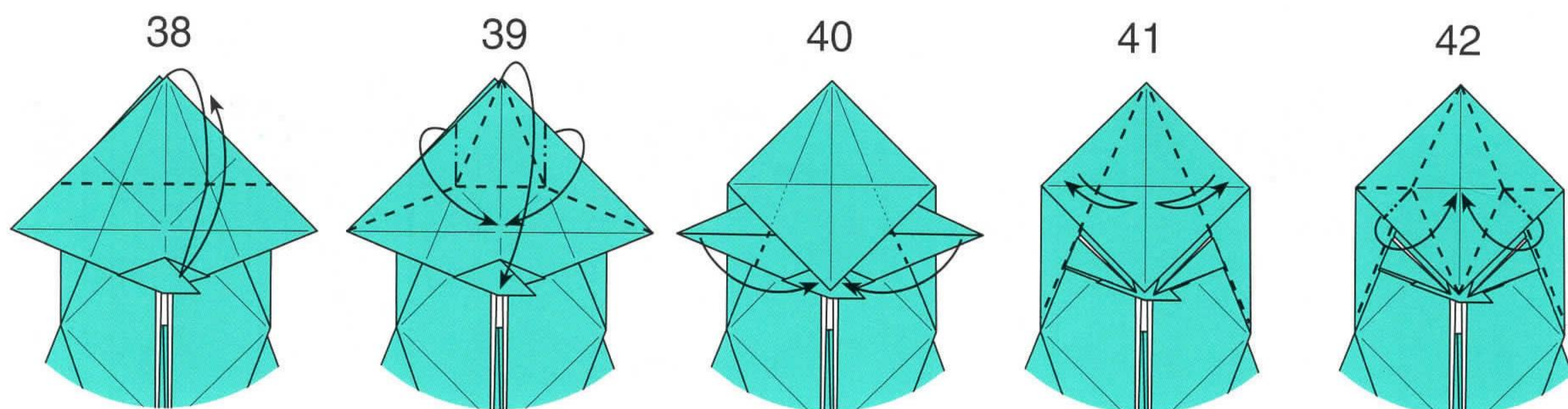
Steps 25-31 are the same as steps 24-30 of *Western Dragon*.

Fold all layers together.

Squash to make a rhombus.

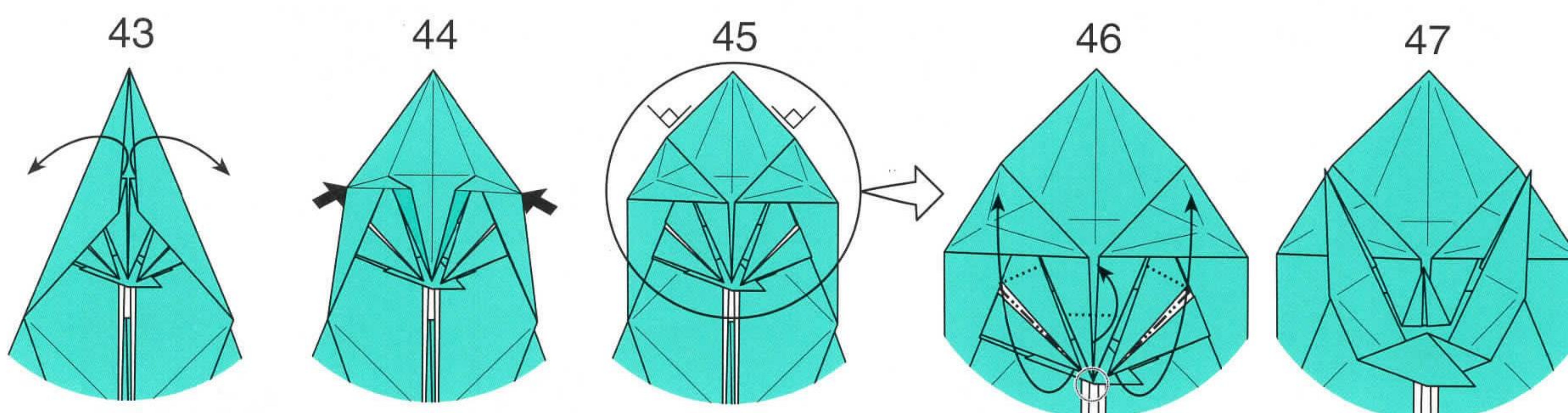


Rabbit-ear-fold



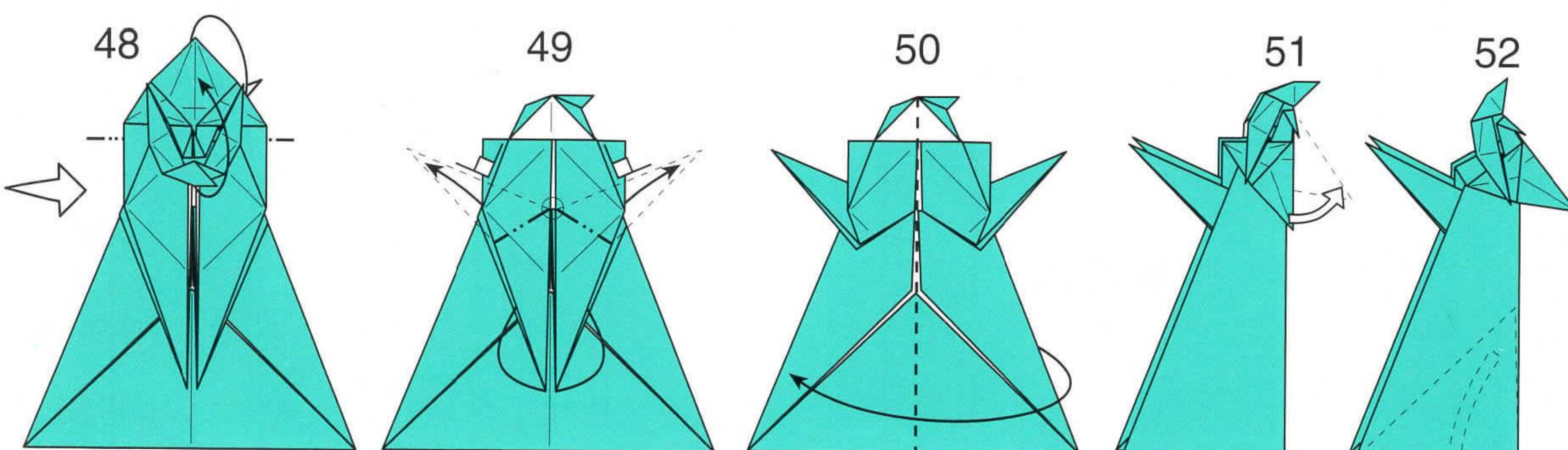
Fold the top layer only.

Swivel-fold

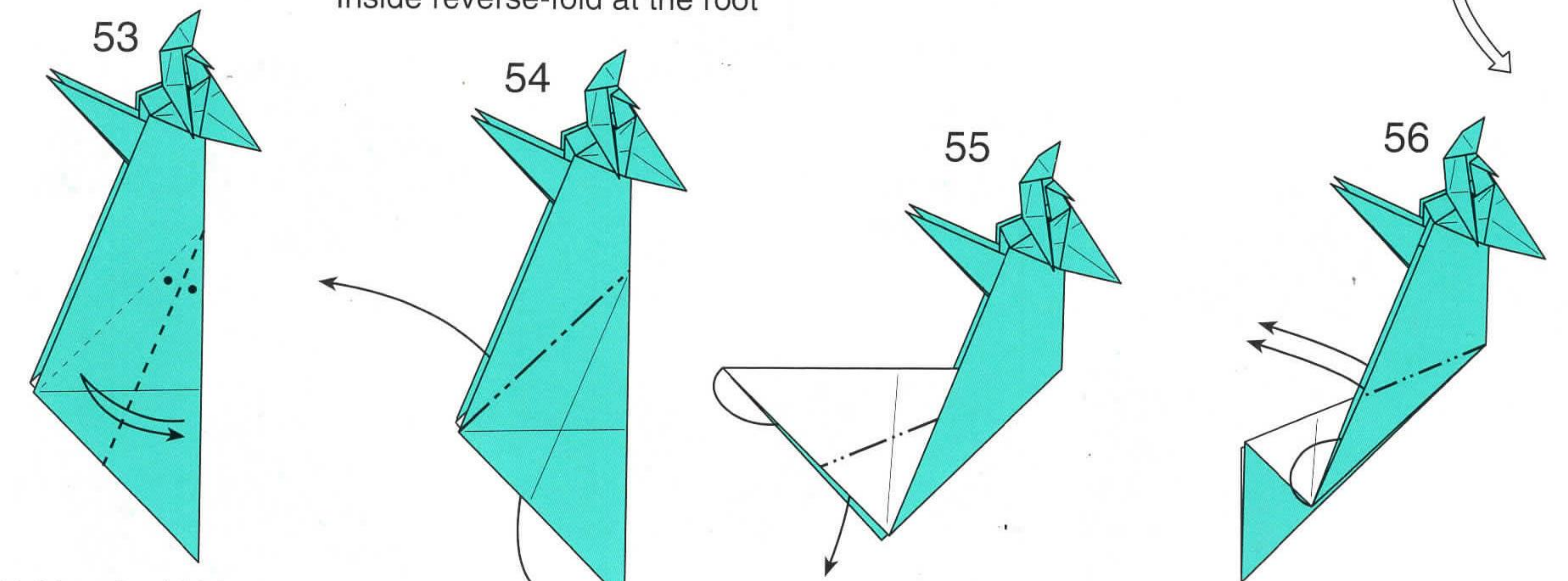


Squash (see the next diagram for the angle).

Fold the side flaps under the flap indicated by the center circle.



Inside reverse-fold at the root

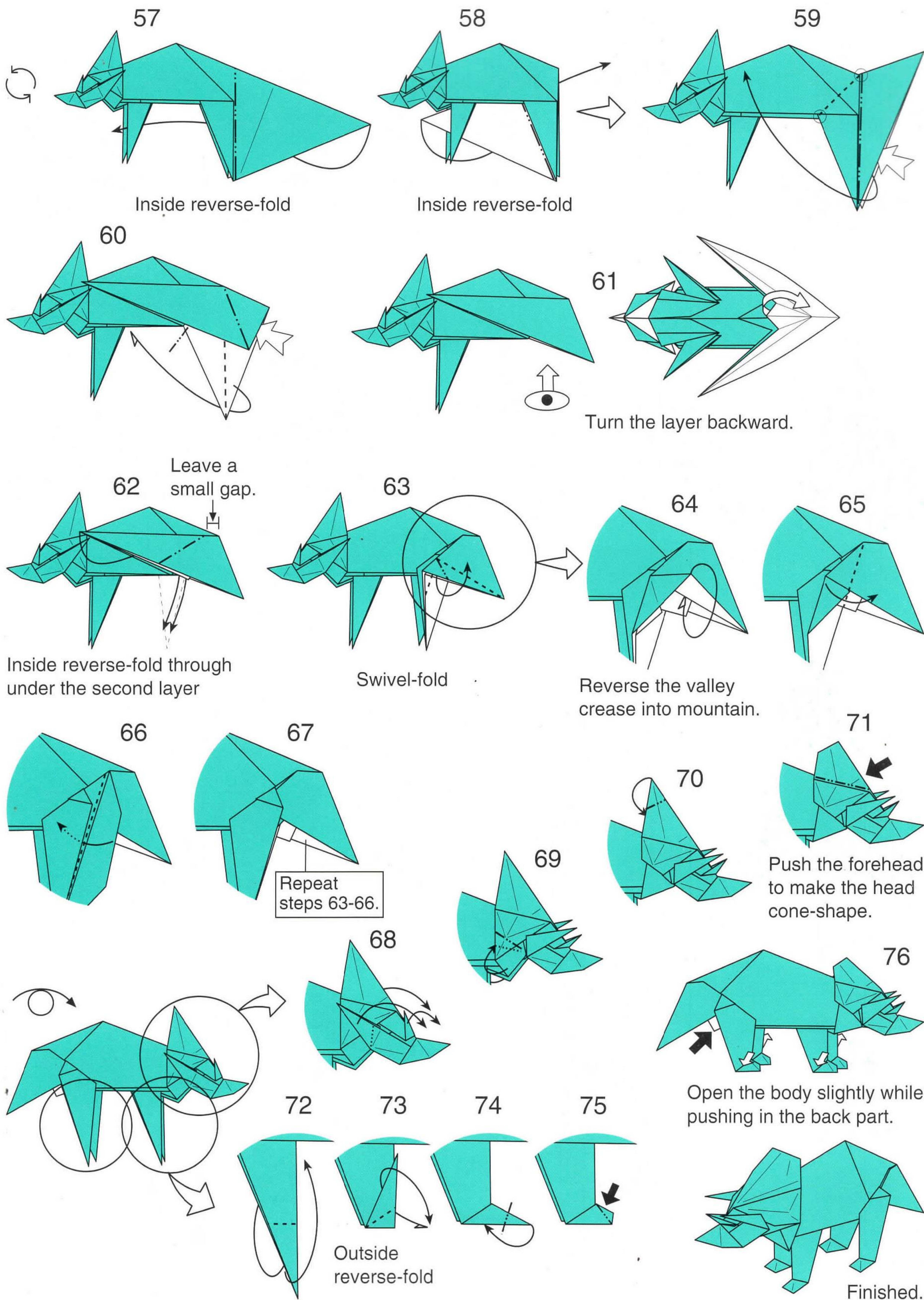


Fold to the hidden edge.

Inside reverse-fold

Inside reverse-fold

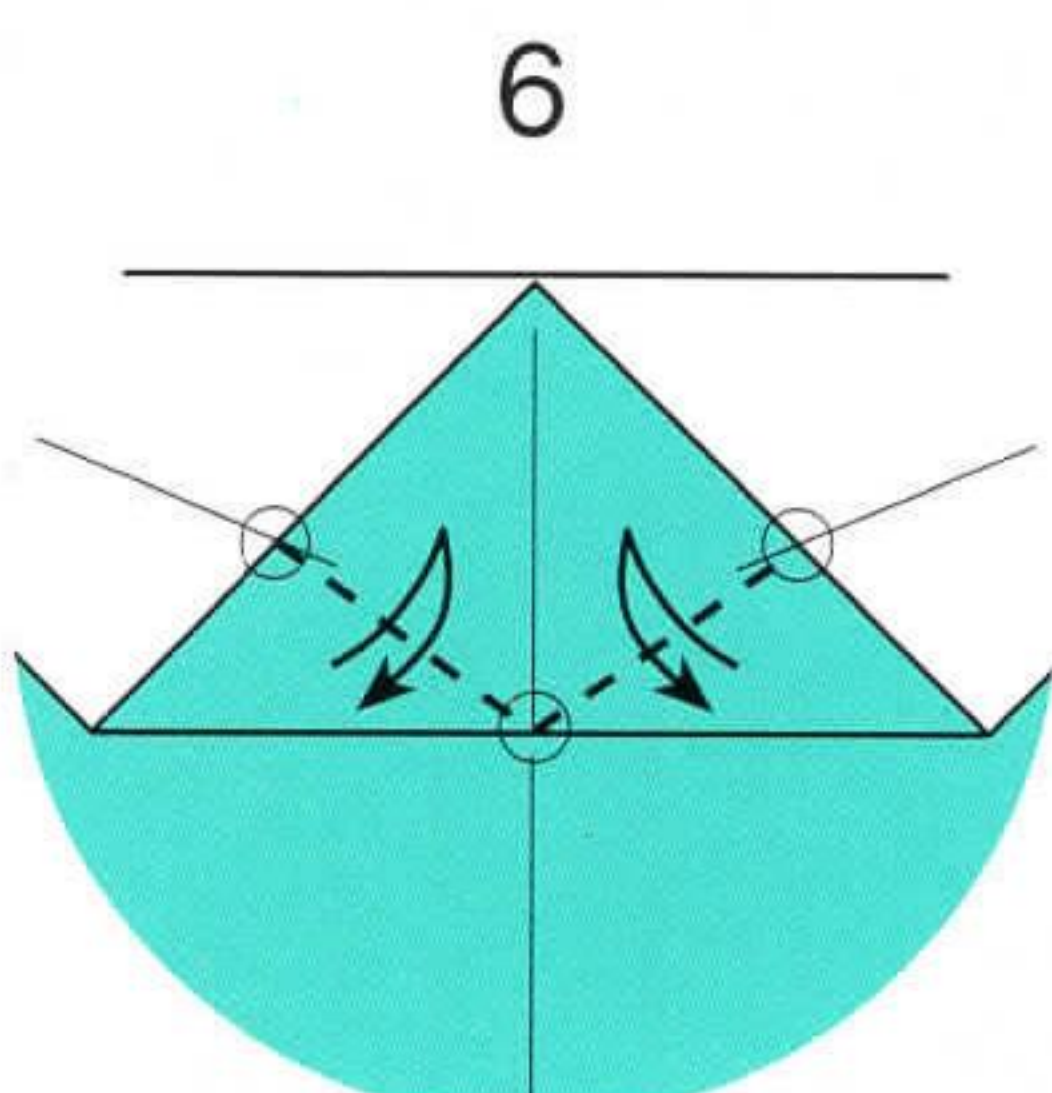
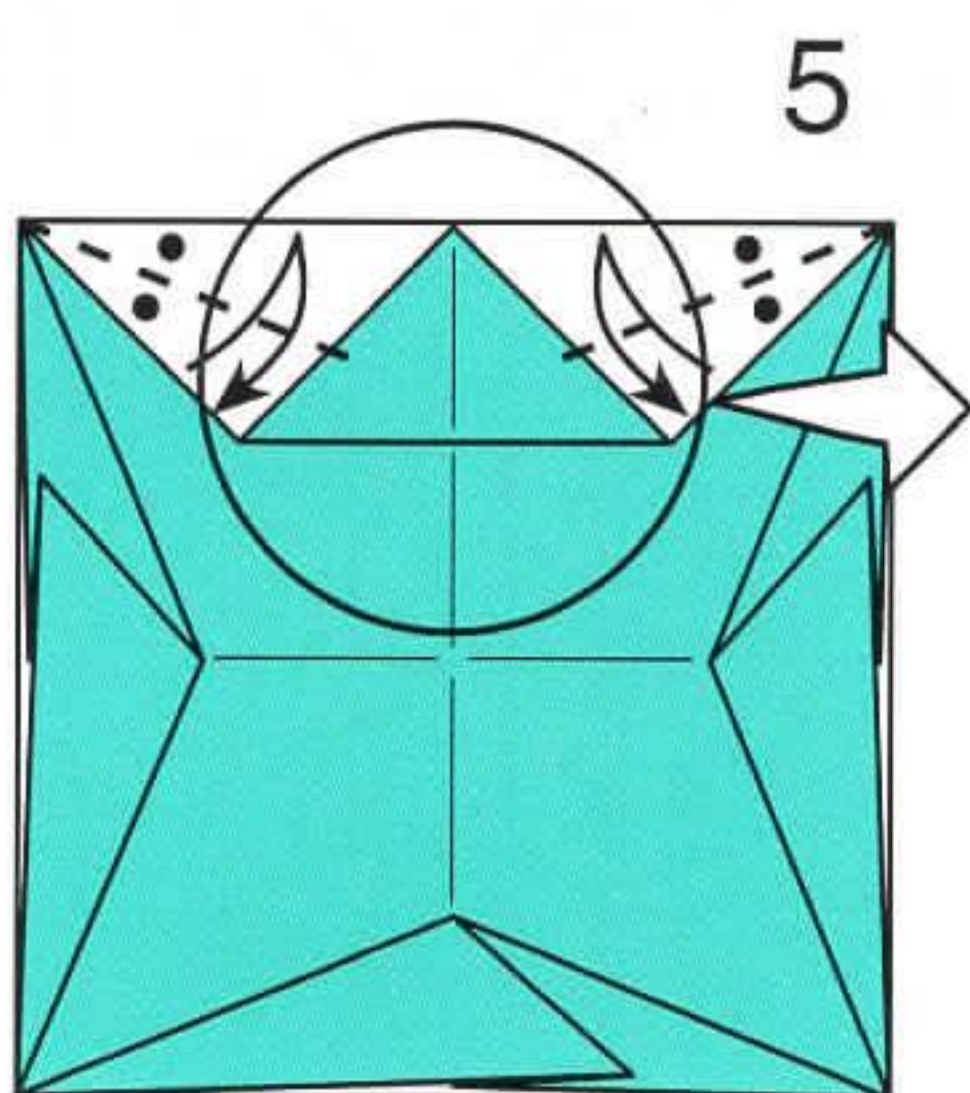
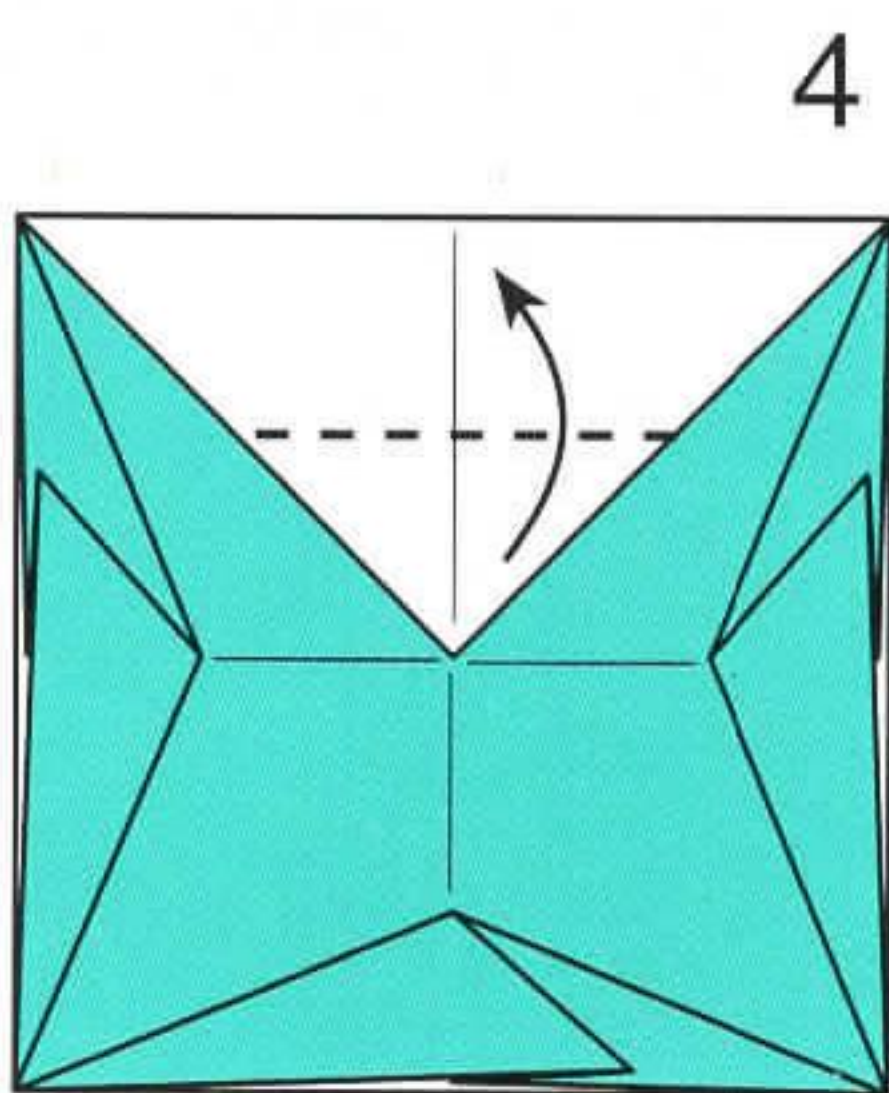
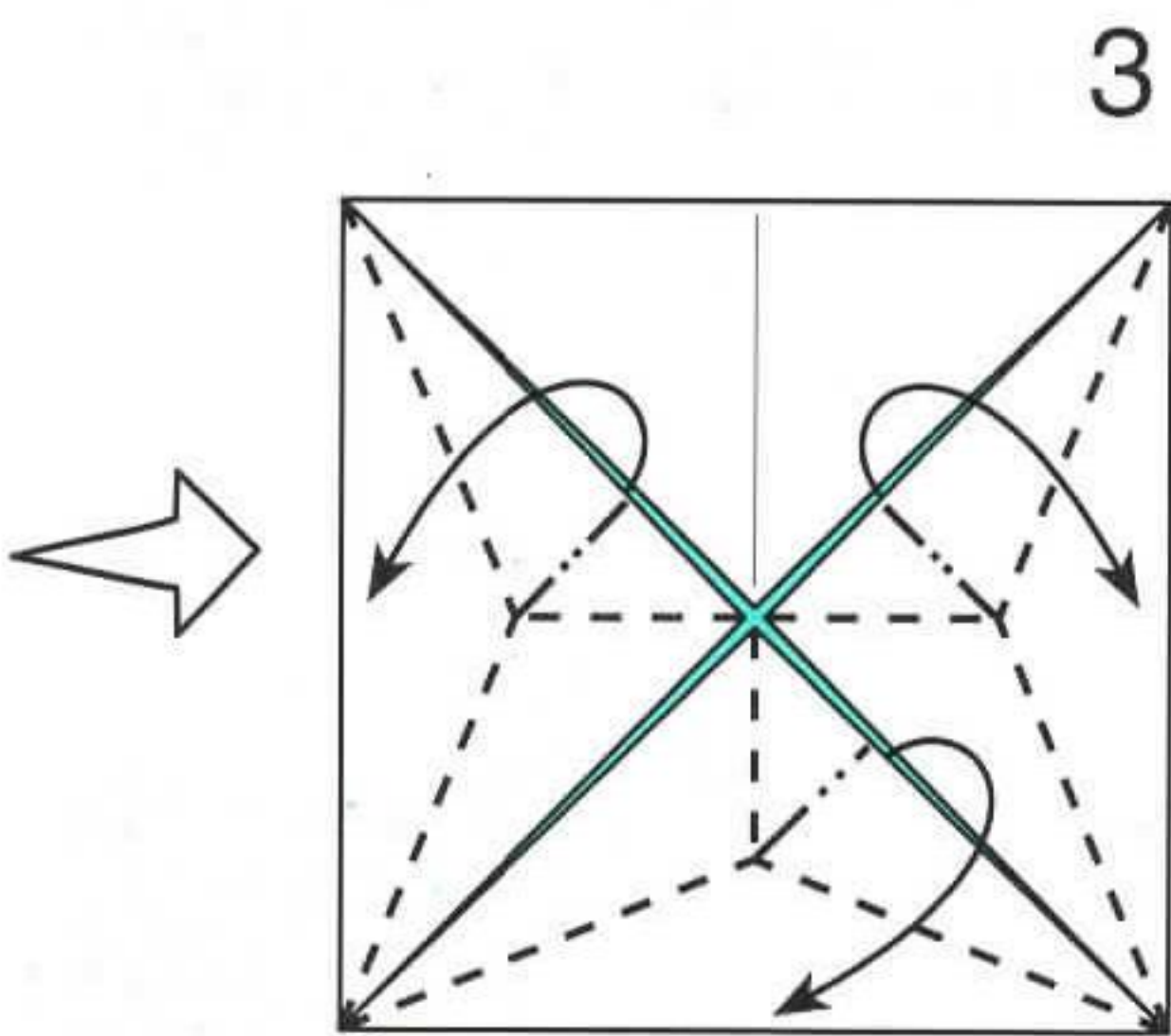
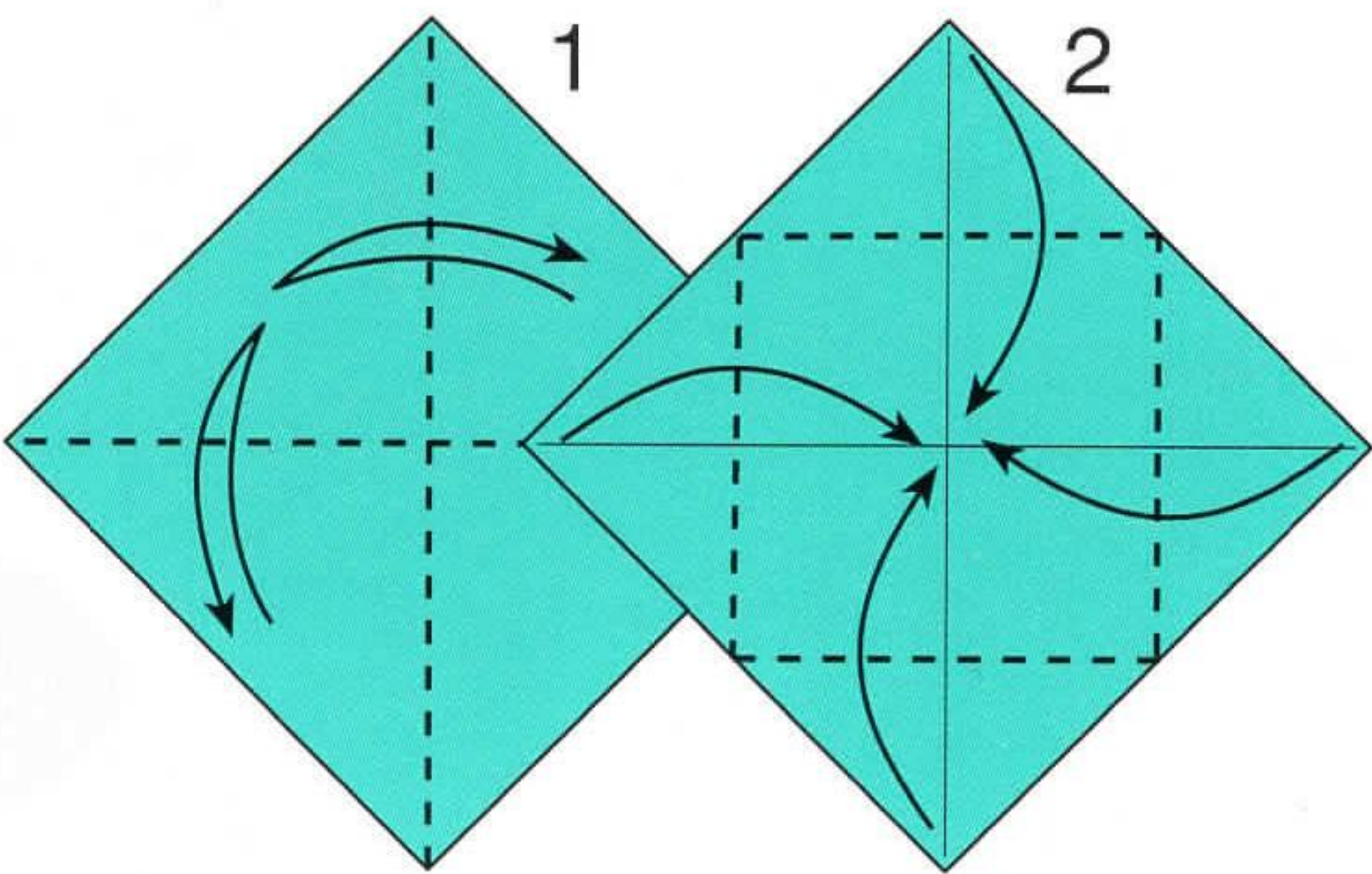
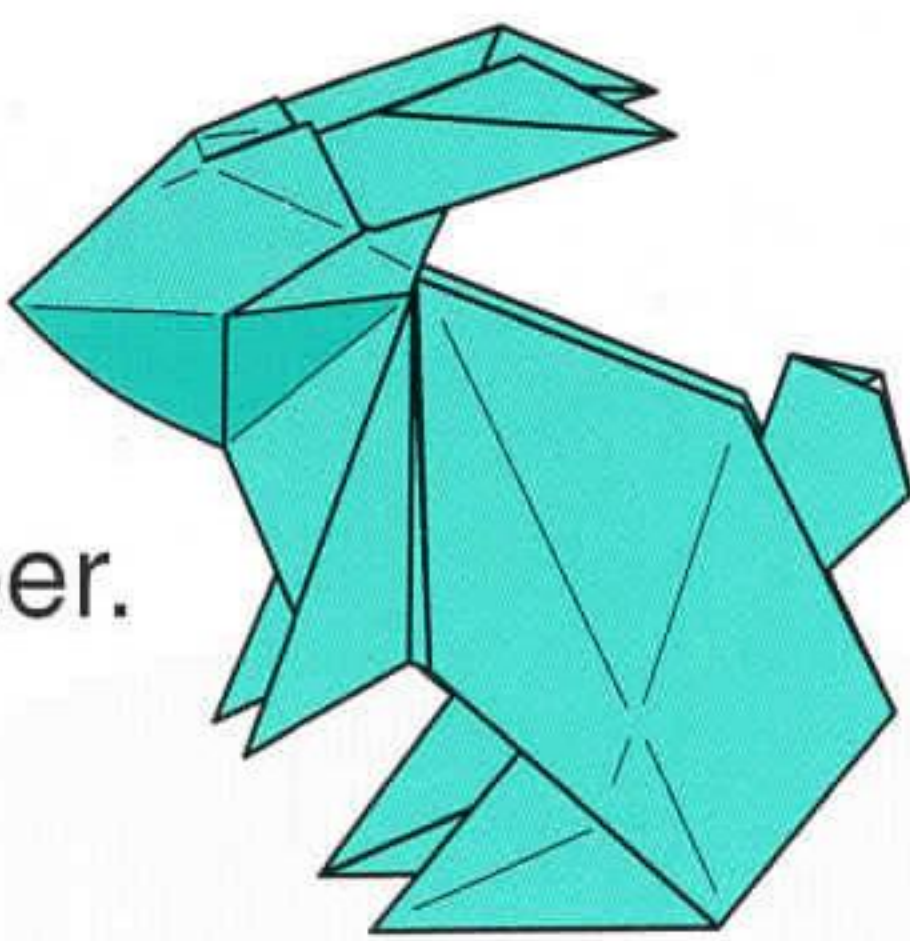
Inside reverse-fold under the top layer



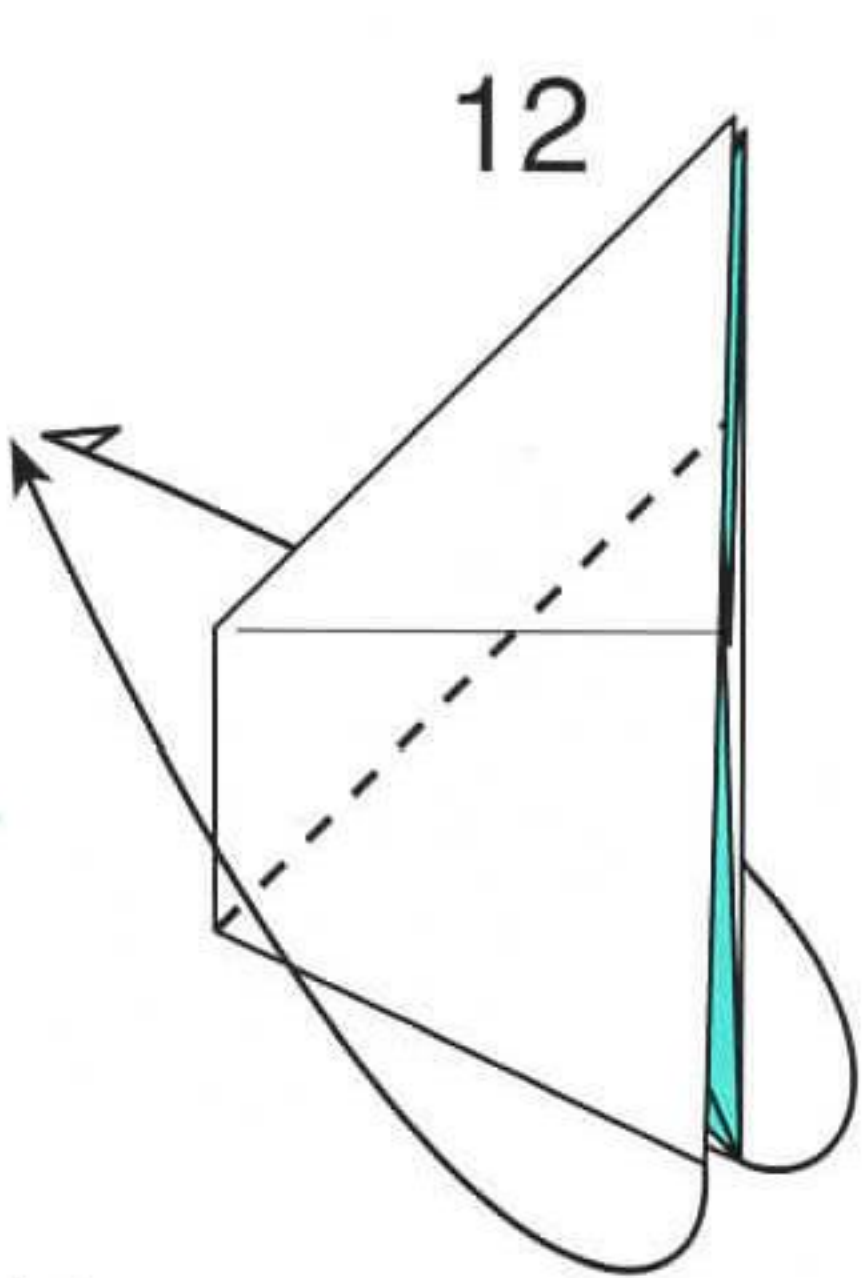
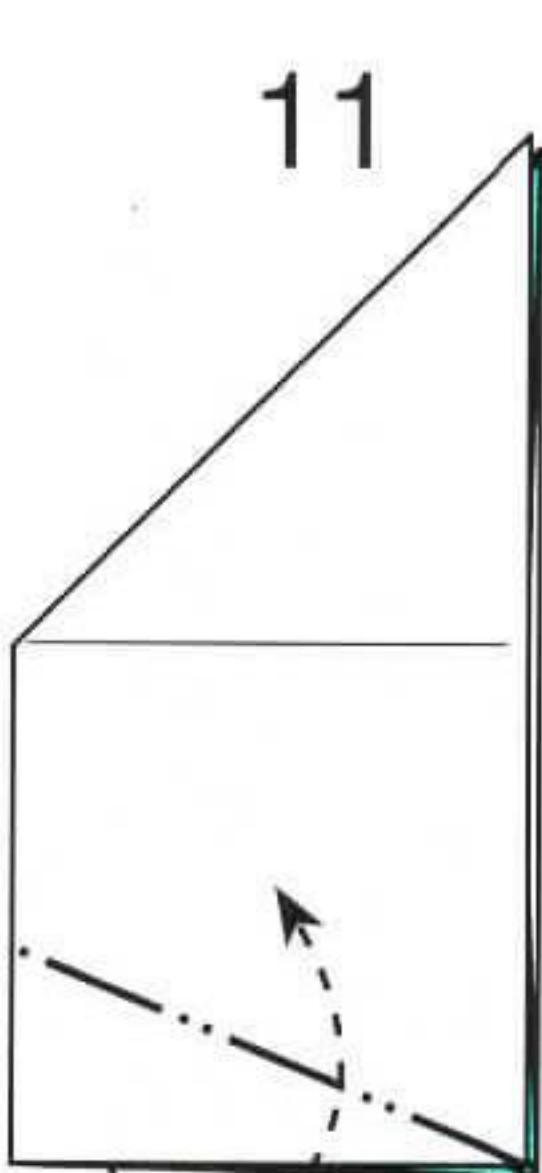
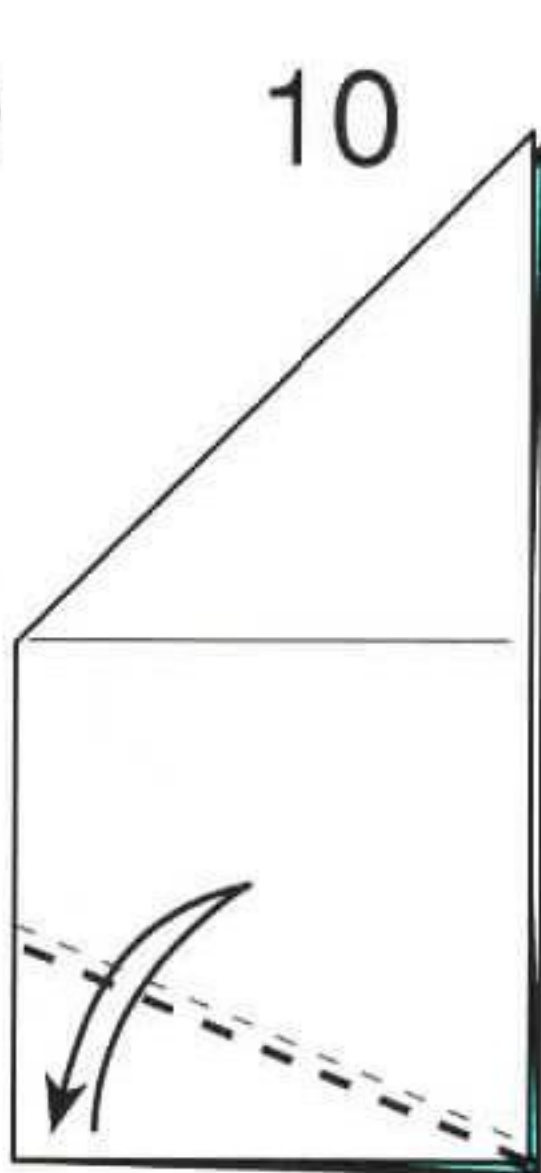
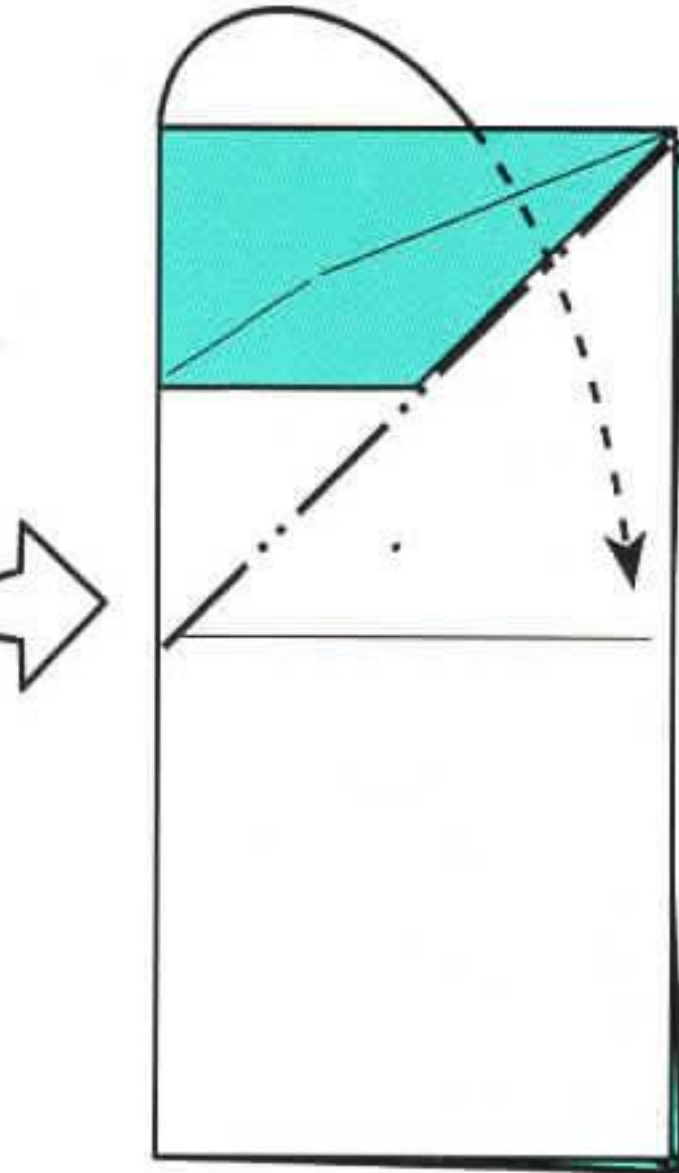
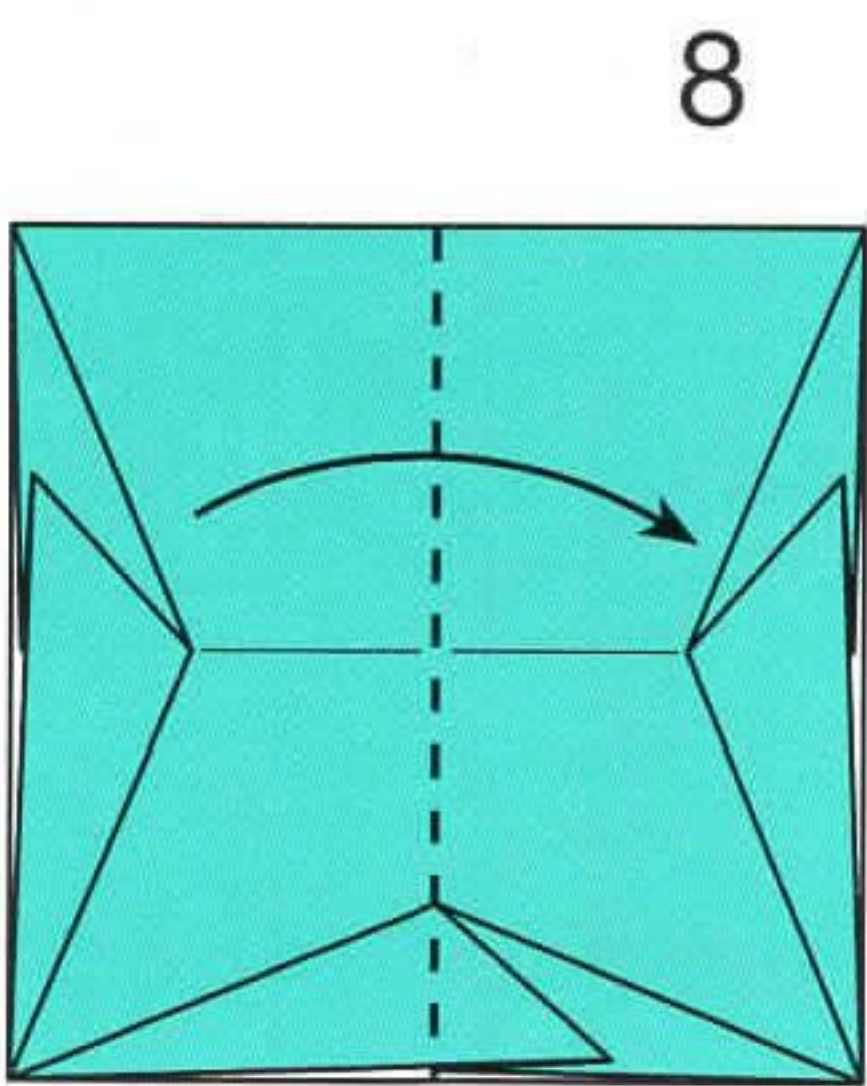
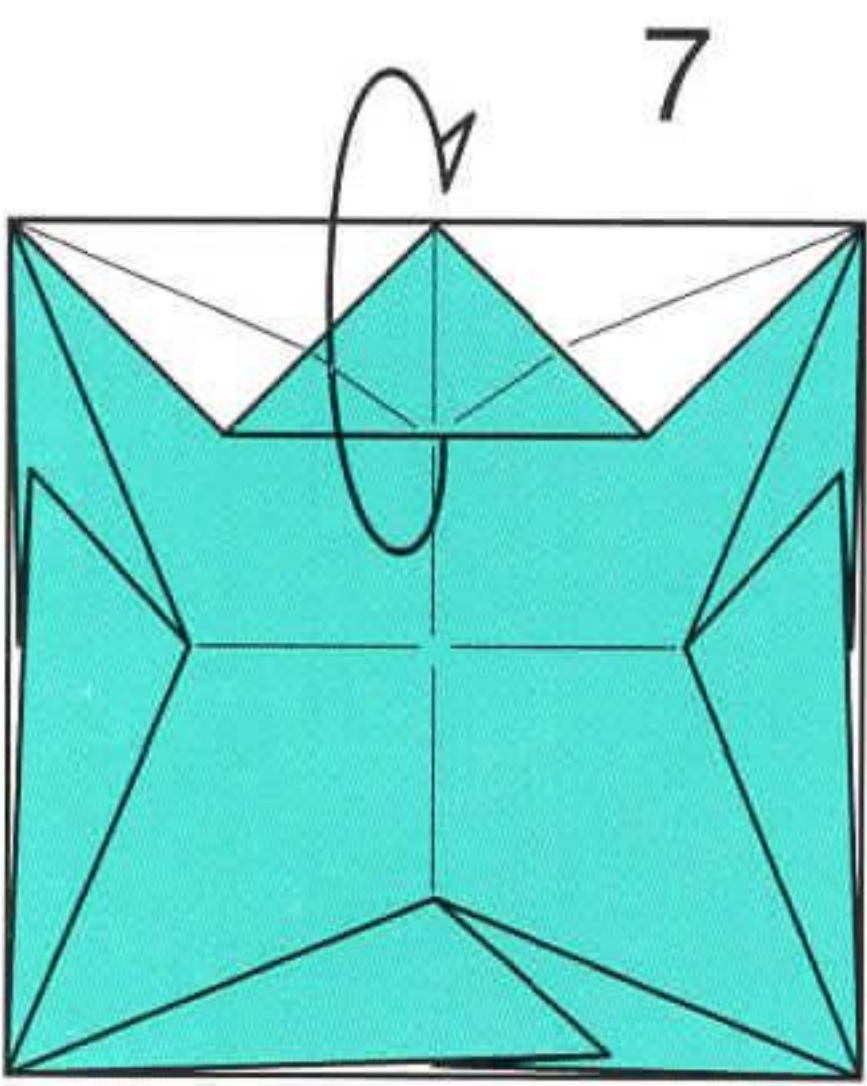
Rabbit

Theme: Solid body

Fold using 6" (15 cm) origami paper.

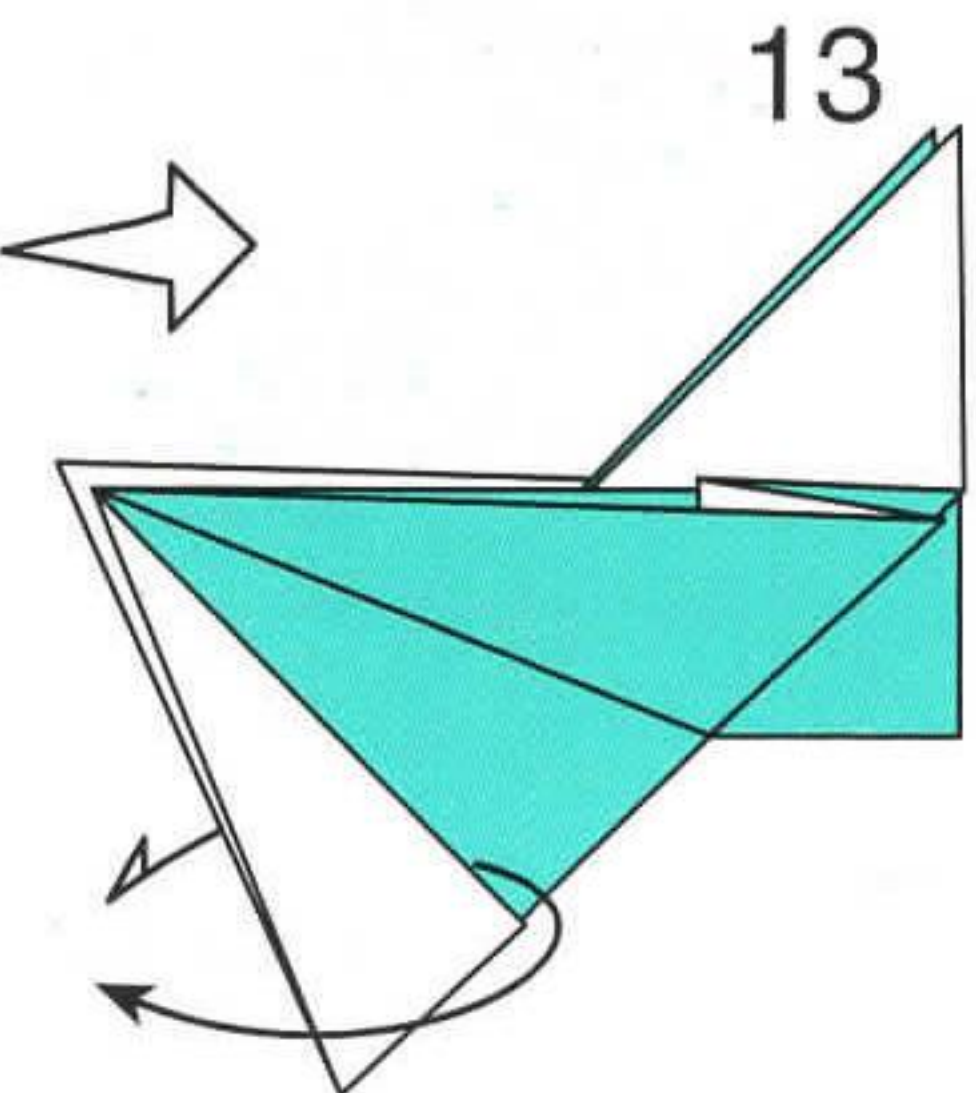


Rabbit-ear-fold three times.

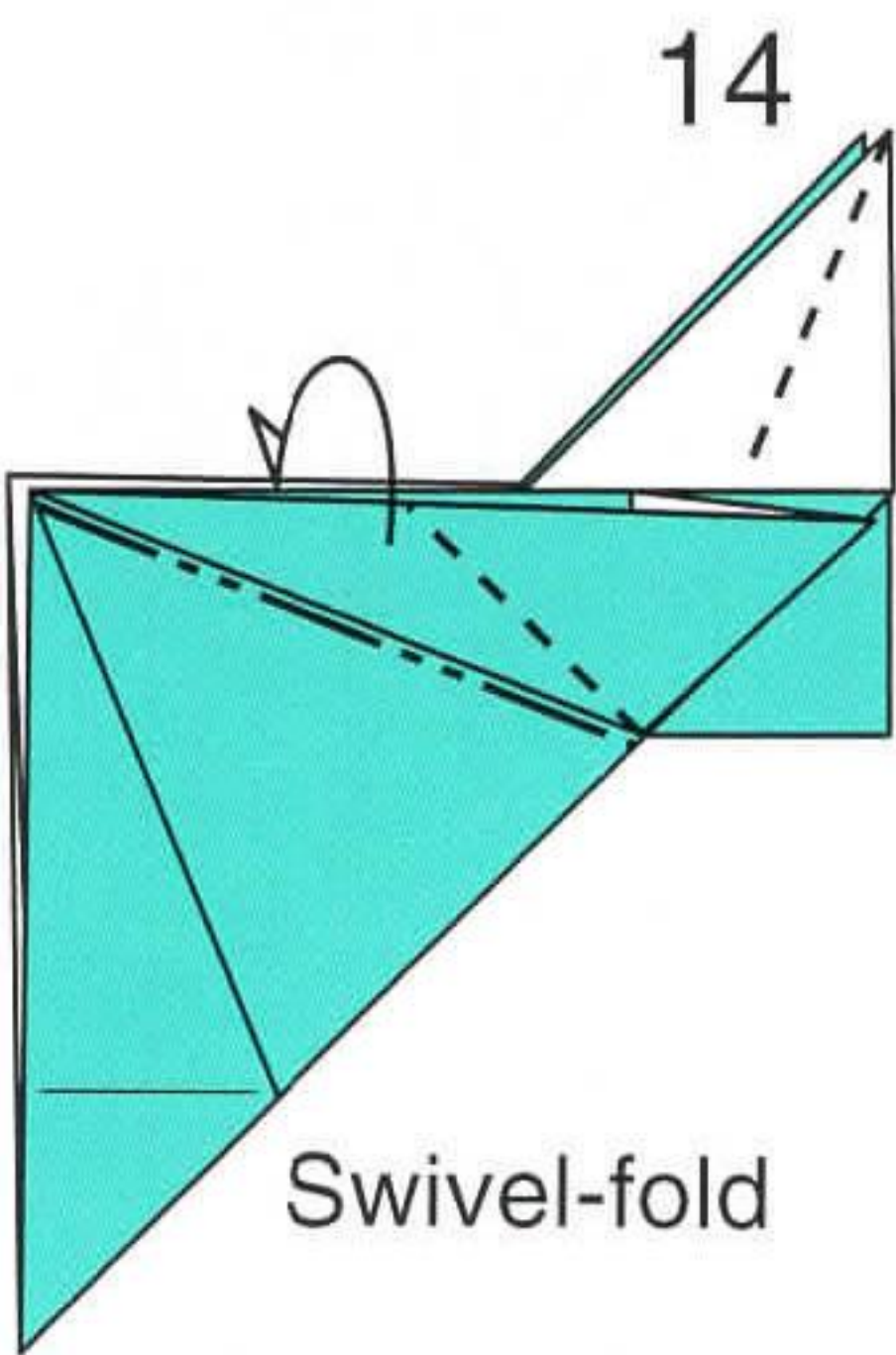


Inside reverse-fold

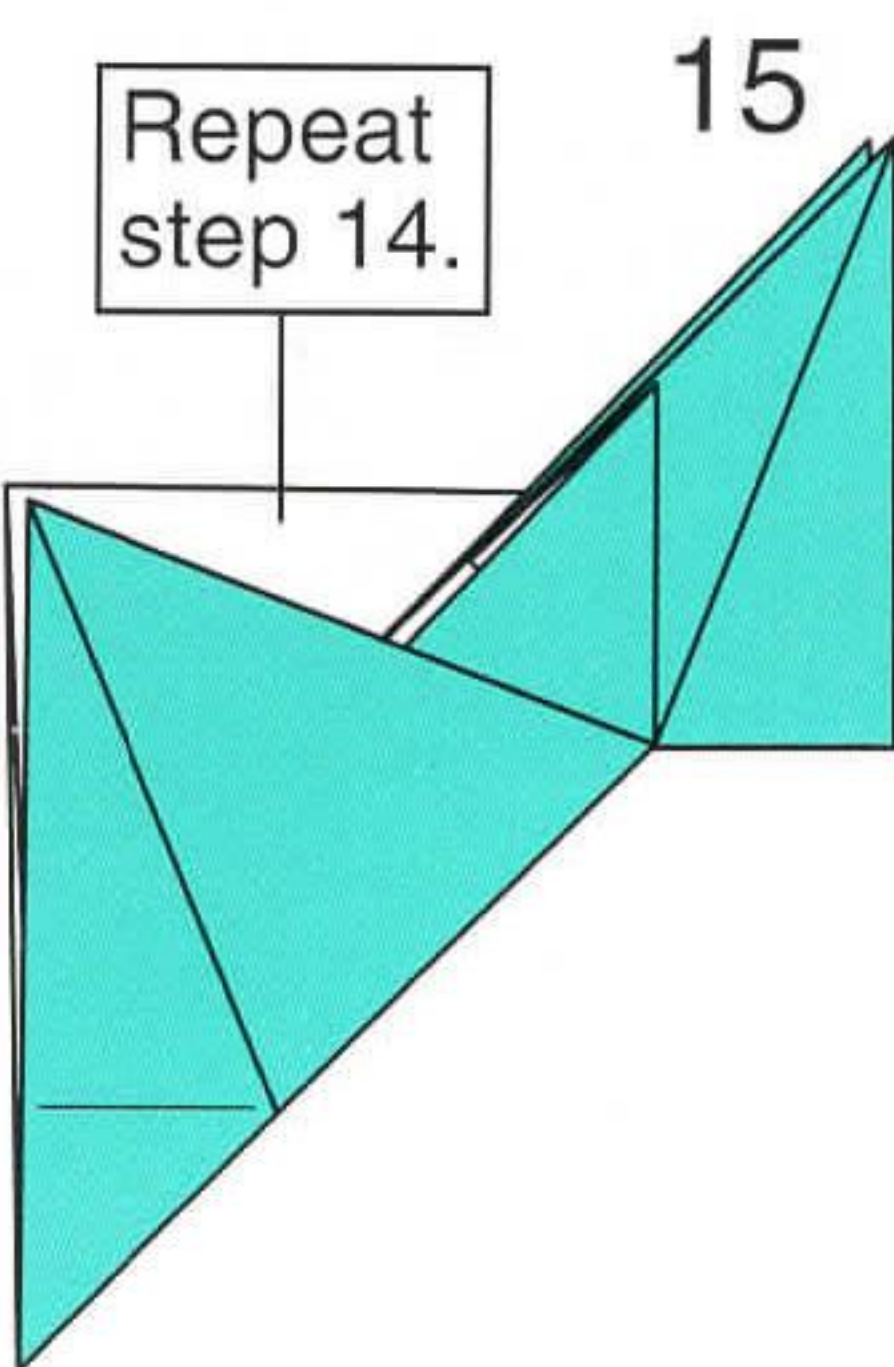
Inside reverse-fold



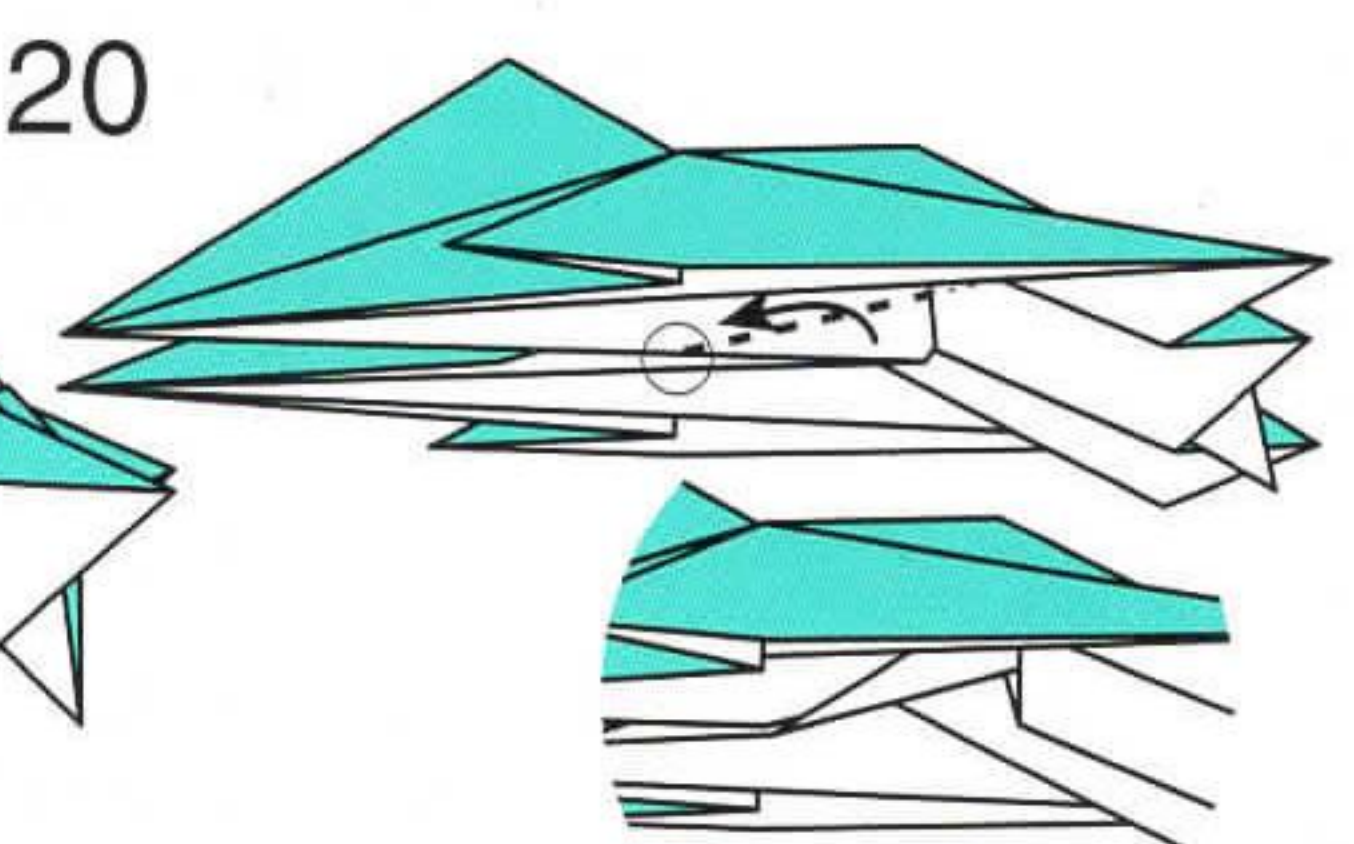
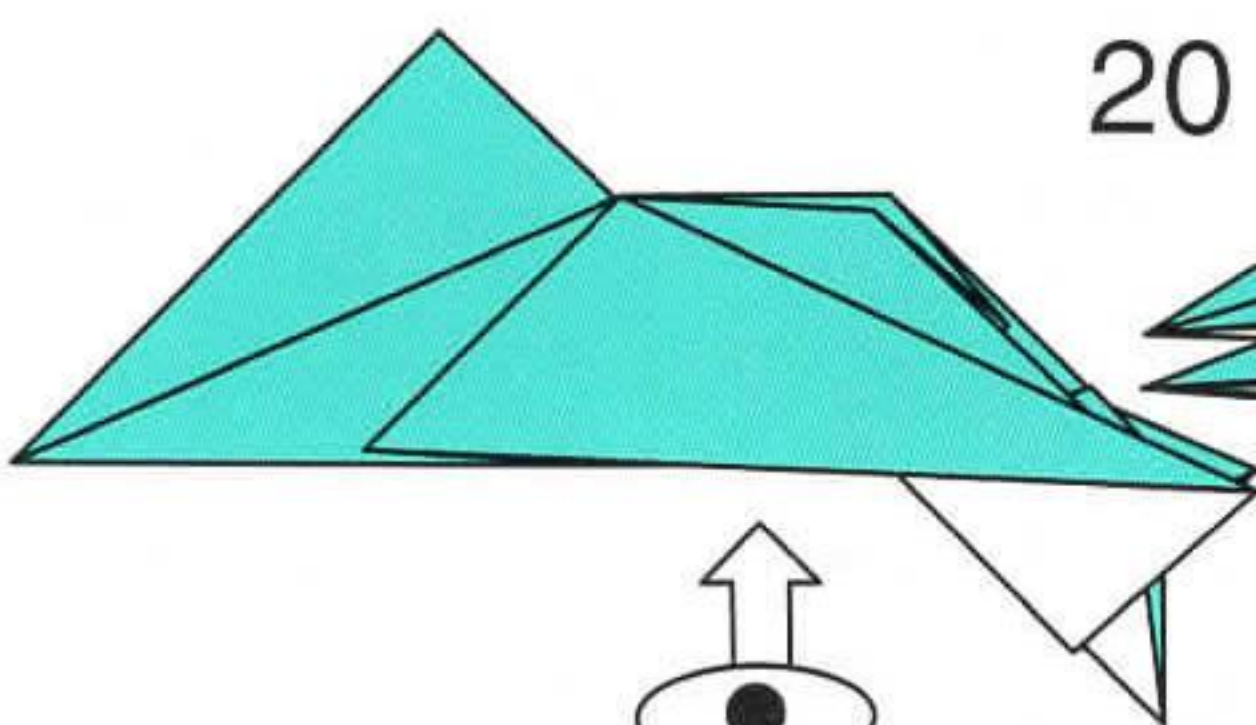
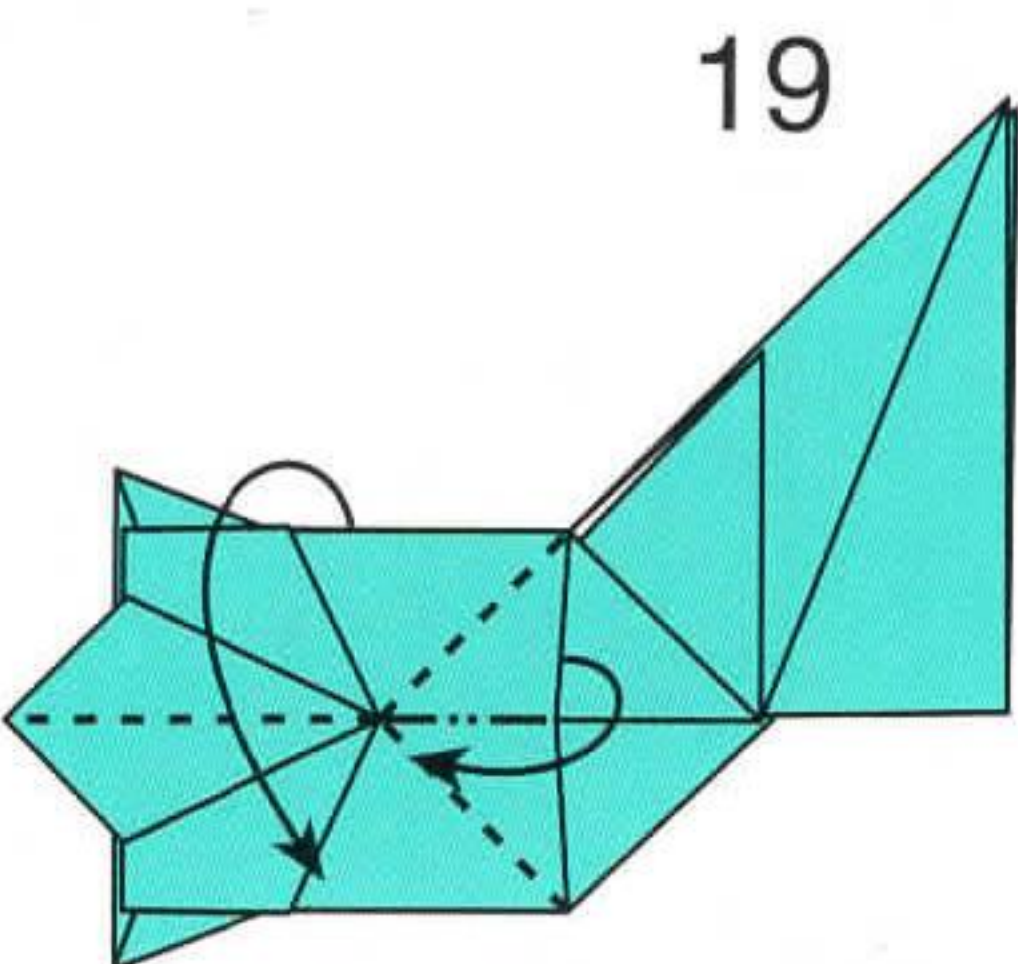
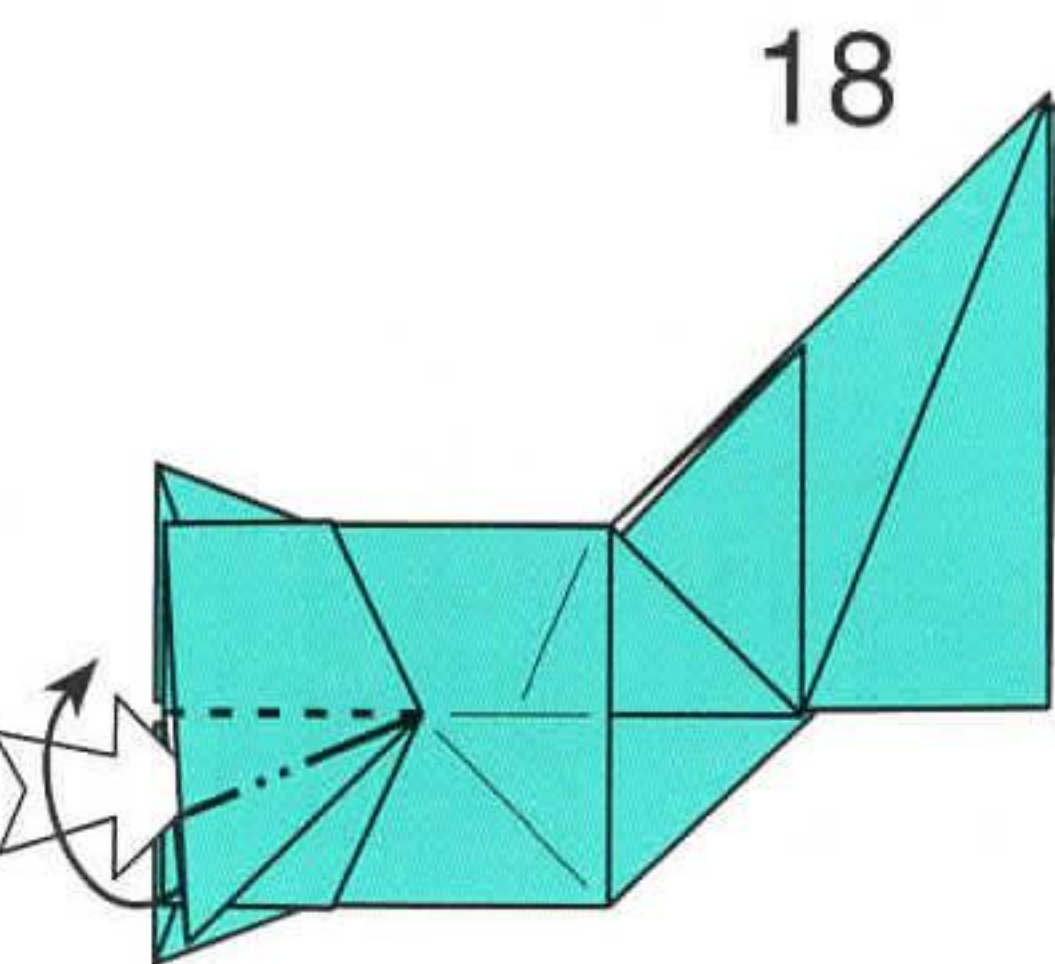
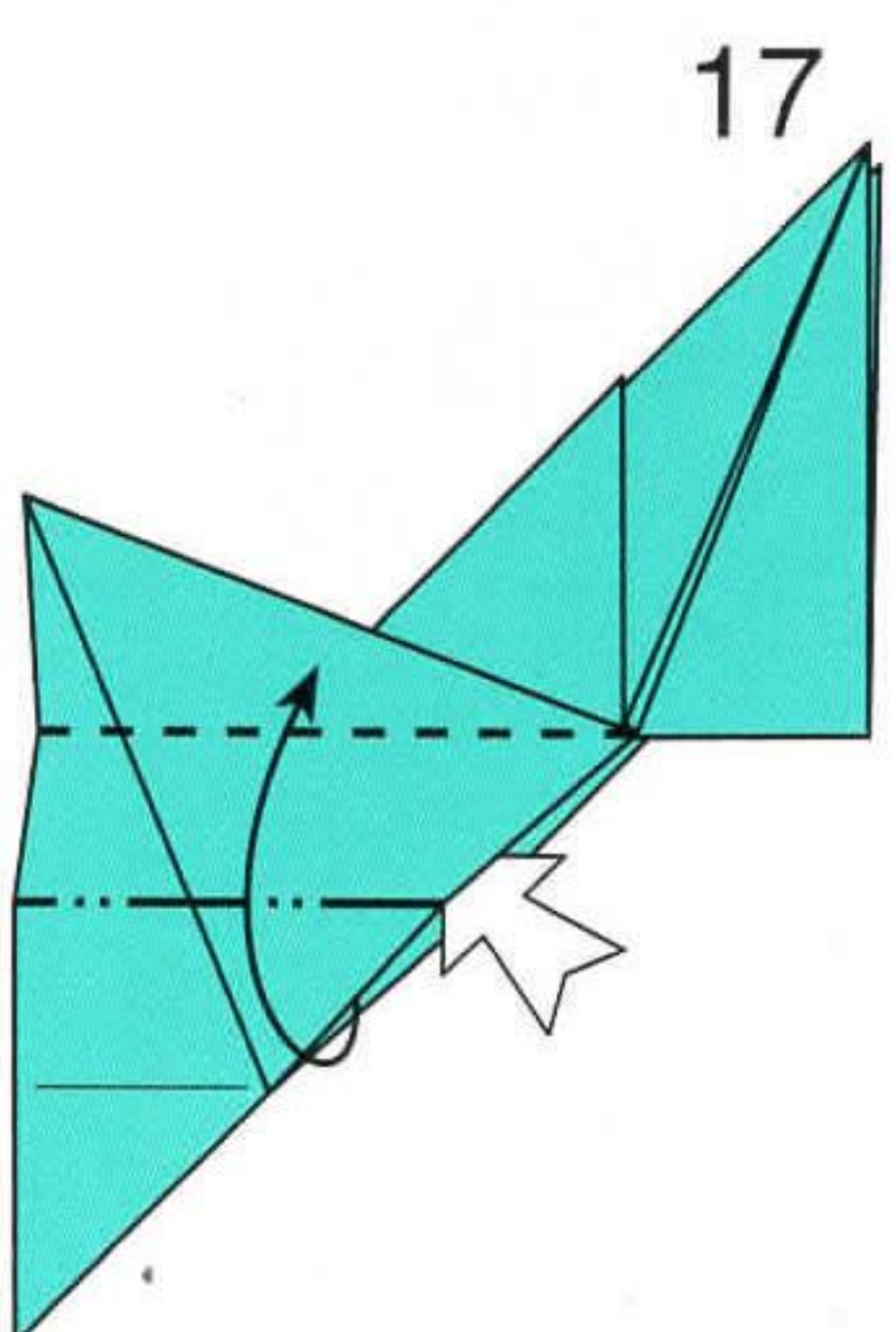
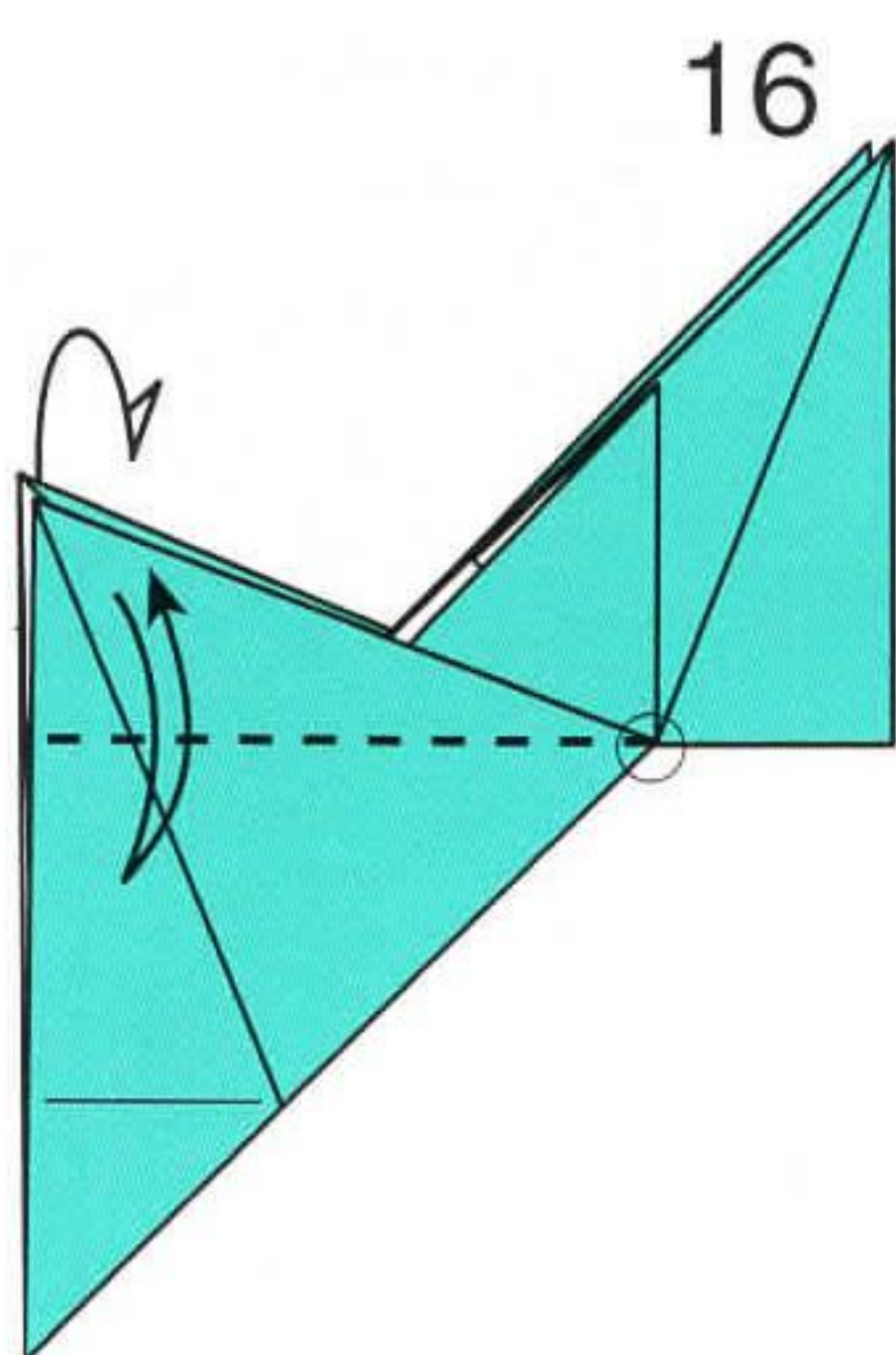
Outside reverse-fold

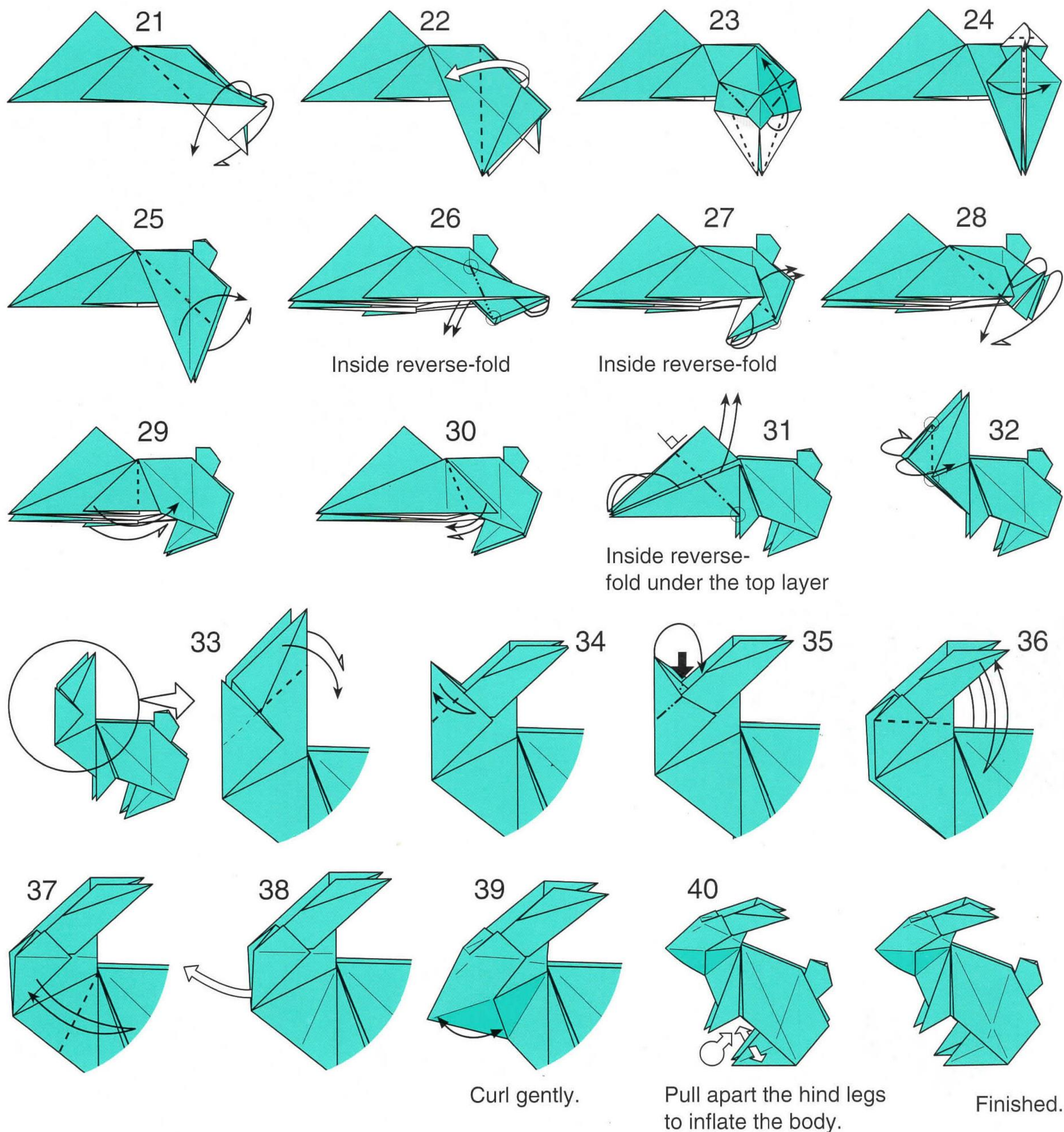


Swivel-fold



Repeat step 14.





Three-dimensional design

I have explained origami design from the viewpoint of branches. But the shape of the model's face is also important. For example, the Bird base is characterized not only by its four long flaps but also by the shape of them.

Speaking of faces, origami models can be seen as a kind of polyhedra, though most of them are flat. Even when the finished model is three-dimensional,

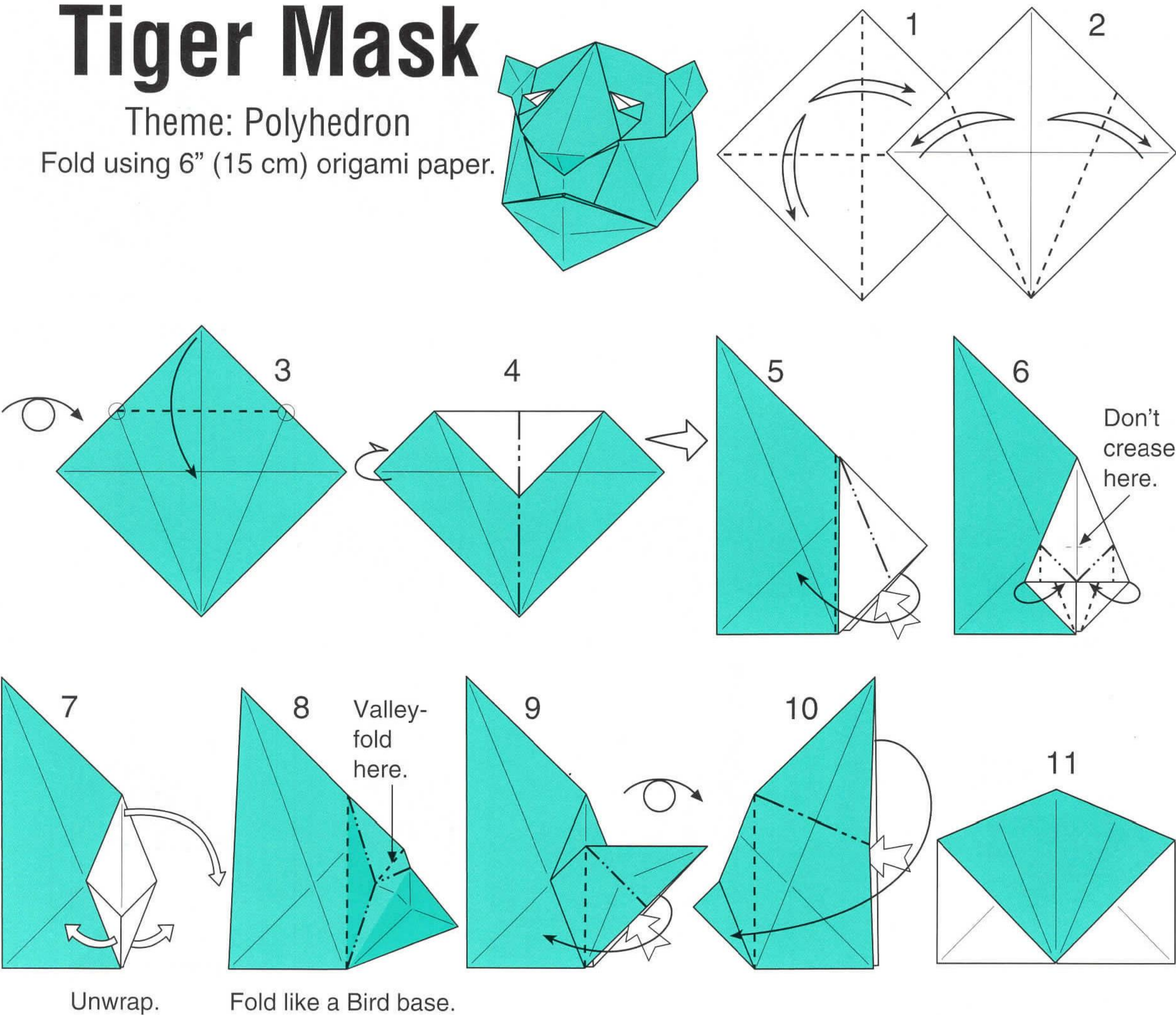
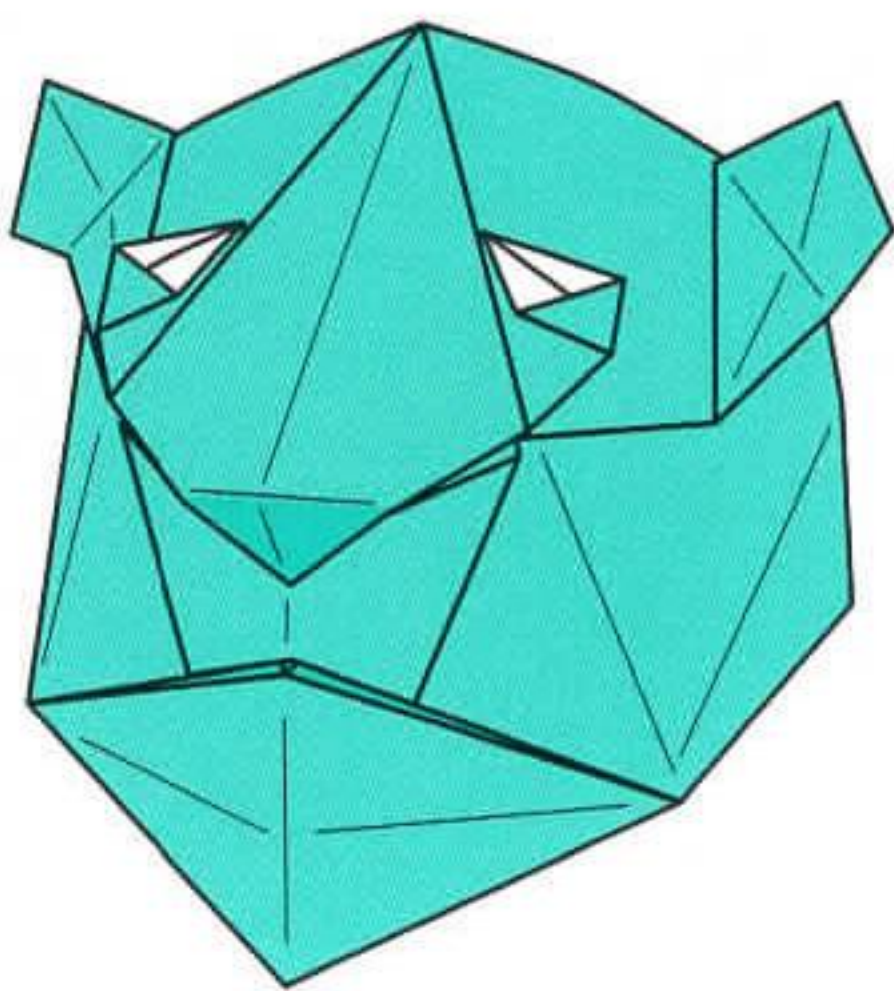
the underlying design is often flat, and the model is just made three-dimensional with shaping (see *Dolphin*).

There are, however, models designed to be three-dimensional. Among already-introduced models, *Squid* is a typical example. And this *Rabbit* makes use of such design in a simple way in its oval head. Compare it with the body, which is made three-dimensional with shaping.

Tiger Mask

Theme: Polyhedron

Fold using 6" (15 cm) origami paper.



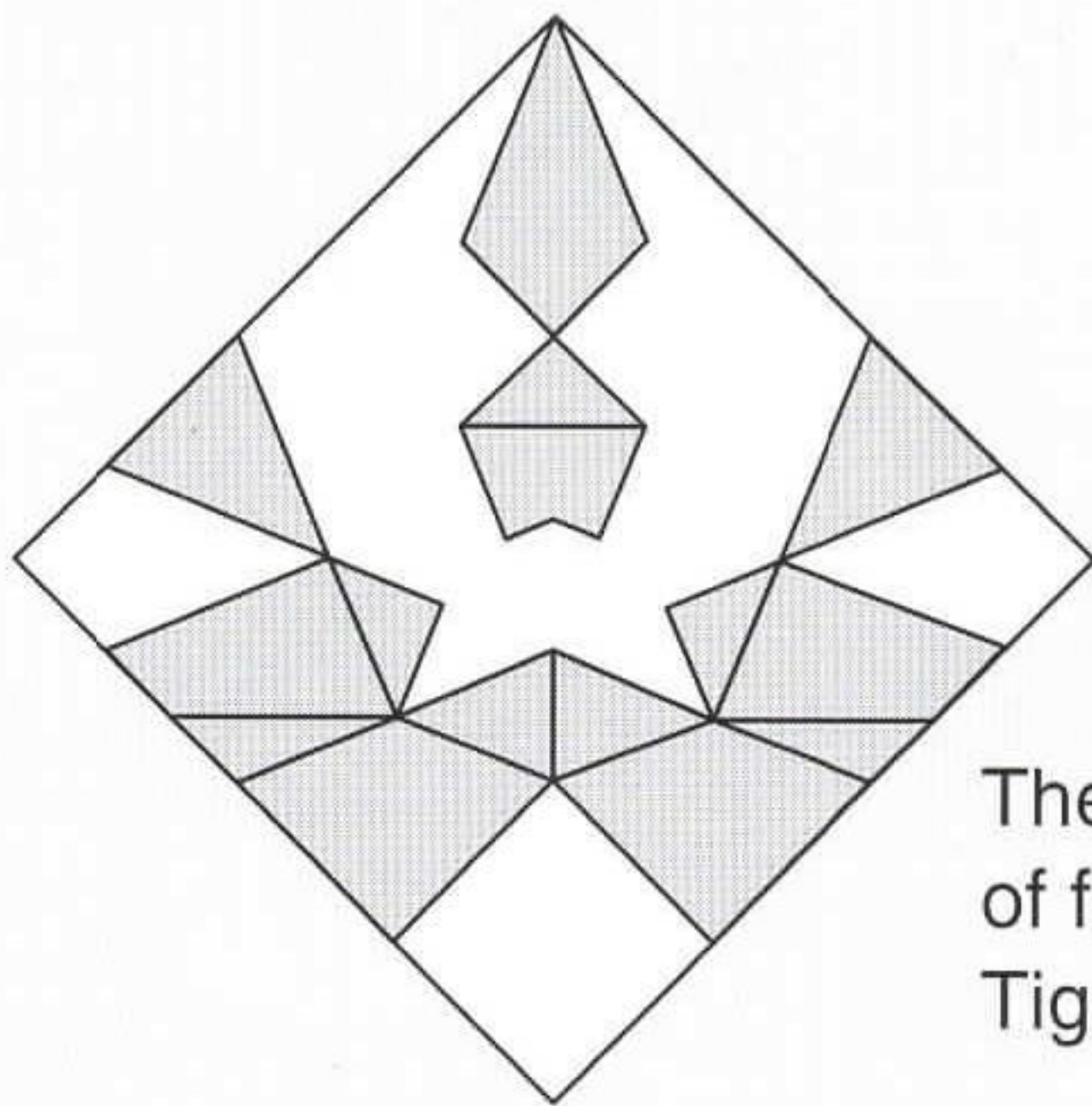
Polyhedral design

In designing a three-dimensional model as in a non-flat polyhedron, the important thing is to determine how to place the faces that will appear on the surface of the model.

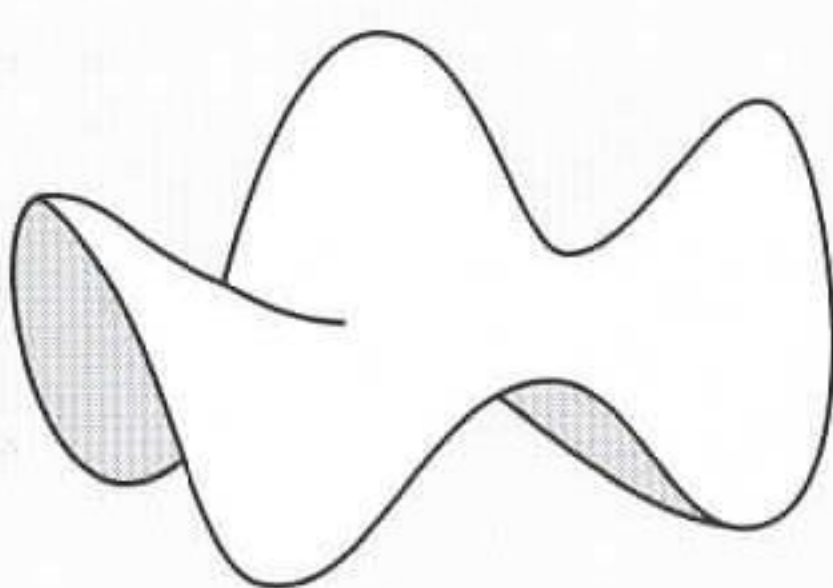
The composition of faces for Tiger Mask is shown on the right. It resembles more to paper-craft development diagrams than crease patterns. But this is not a paper-craft model because it is folded without cuts. We do not cut off the white areas.

There is a basic rule in placing faces. If the corner is either convex or concave, then faces can touch each other at the corner.

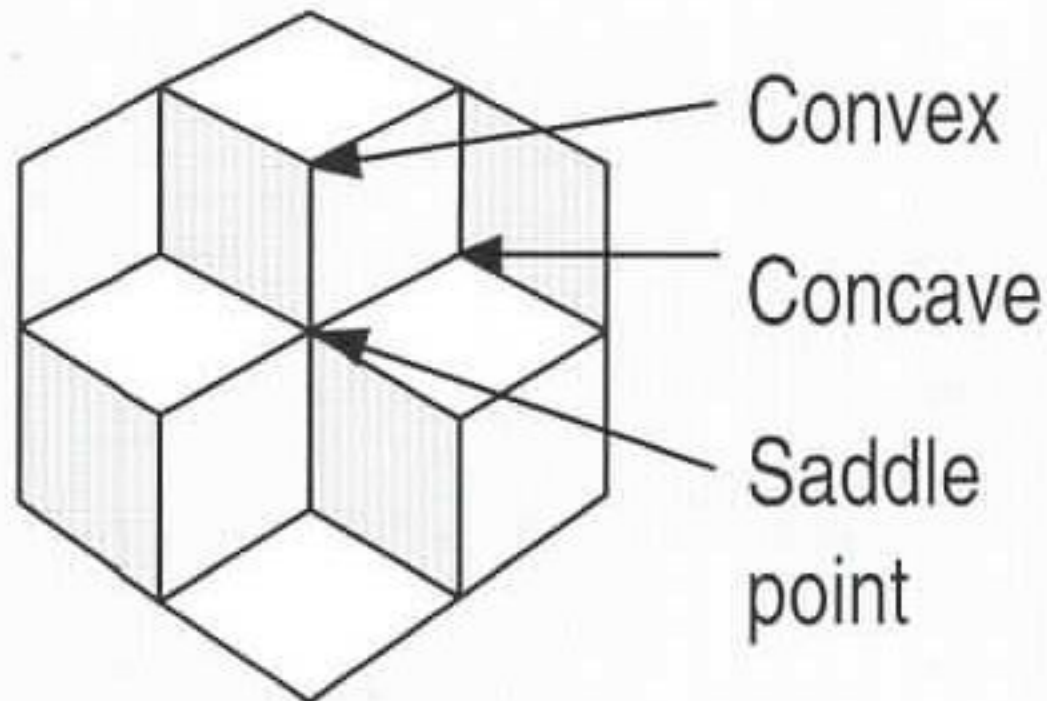
On the other hand, if the corner is a saddle point, in other words, the faces form a saddle surface (shown on the right) around it, then the faces must be placed separately at appropriate distances. Some areas must be pleated and hidden, because the angle around the corner is larger than 360°. In this model, there are two saddle points at each side of the nose.



The composition of faces for Tiger Mask.



An example of saddle surface



12

About 1/2

13

Fold to wrap the layer behind.

14

Fold to wrap the layer behind.

15

Squash-fold so that the white parts become isosceles right triangles.

16

Squash-fold so that the white parts become isosceles right triangles.

17

Fold to wrap the layer behind.

18

Fold to wrap the layer behind.

19

Fold to wrap the layer behind.

20

Fold to wrap the layer behind.

21

Fold to wrap the layer behind.

22

Fold to wrap the layer behind.

23

Inside reverse-fold

24

Fold inside using the existing crease.

25

Fold inside using the existing crease.

26

Fold inside using the existing crease.

27

Fold inside using the existing crease.

28

Fold inside using the existing crease.

29

Repeat steps 26-28.

30

Repeat steps 26-28.

31

Stand up the layer.

32

Stand up the layer.

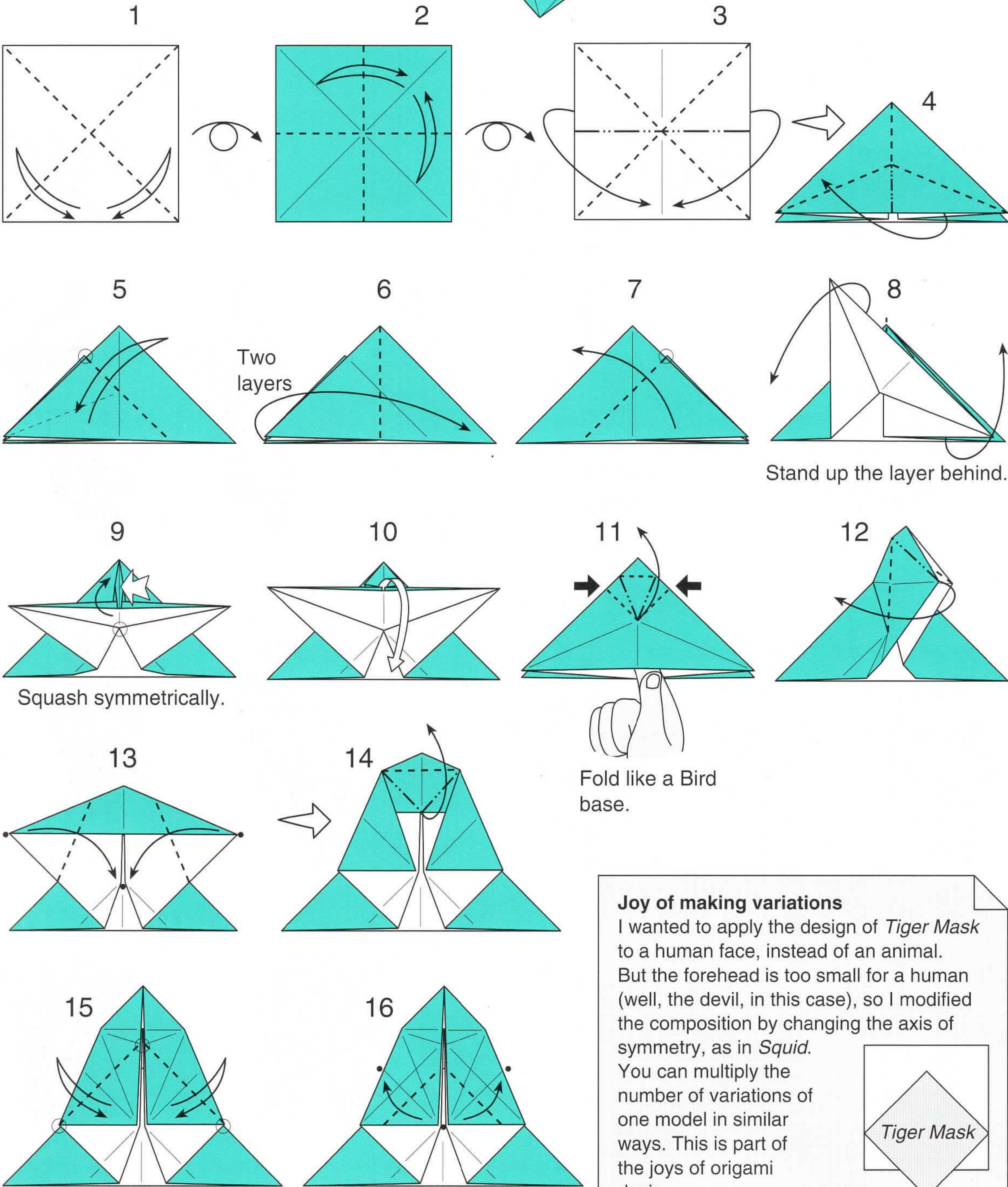
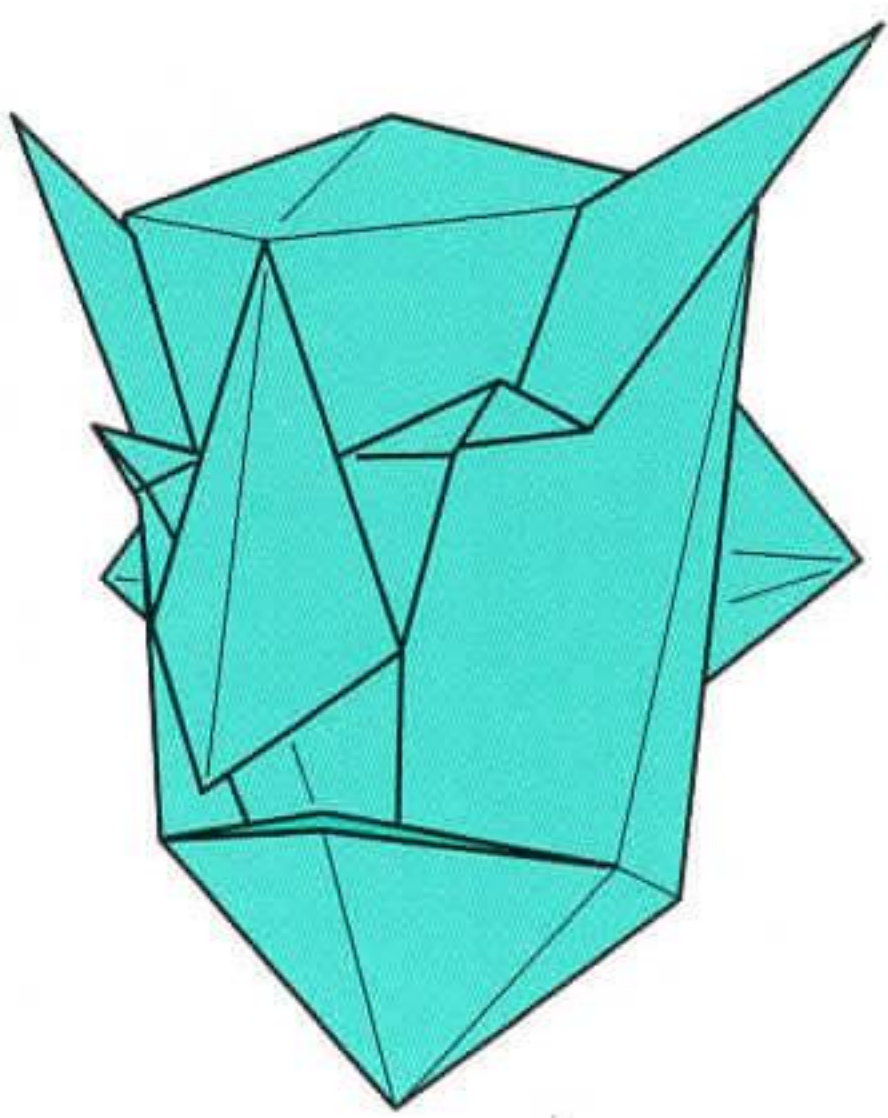
33

Finished.

Devil Mask

Theme: Variation

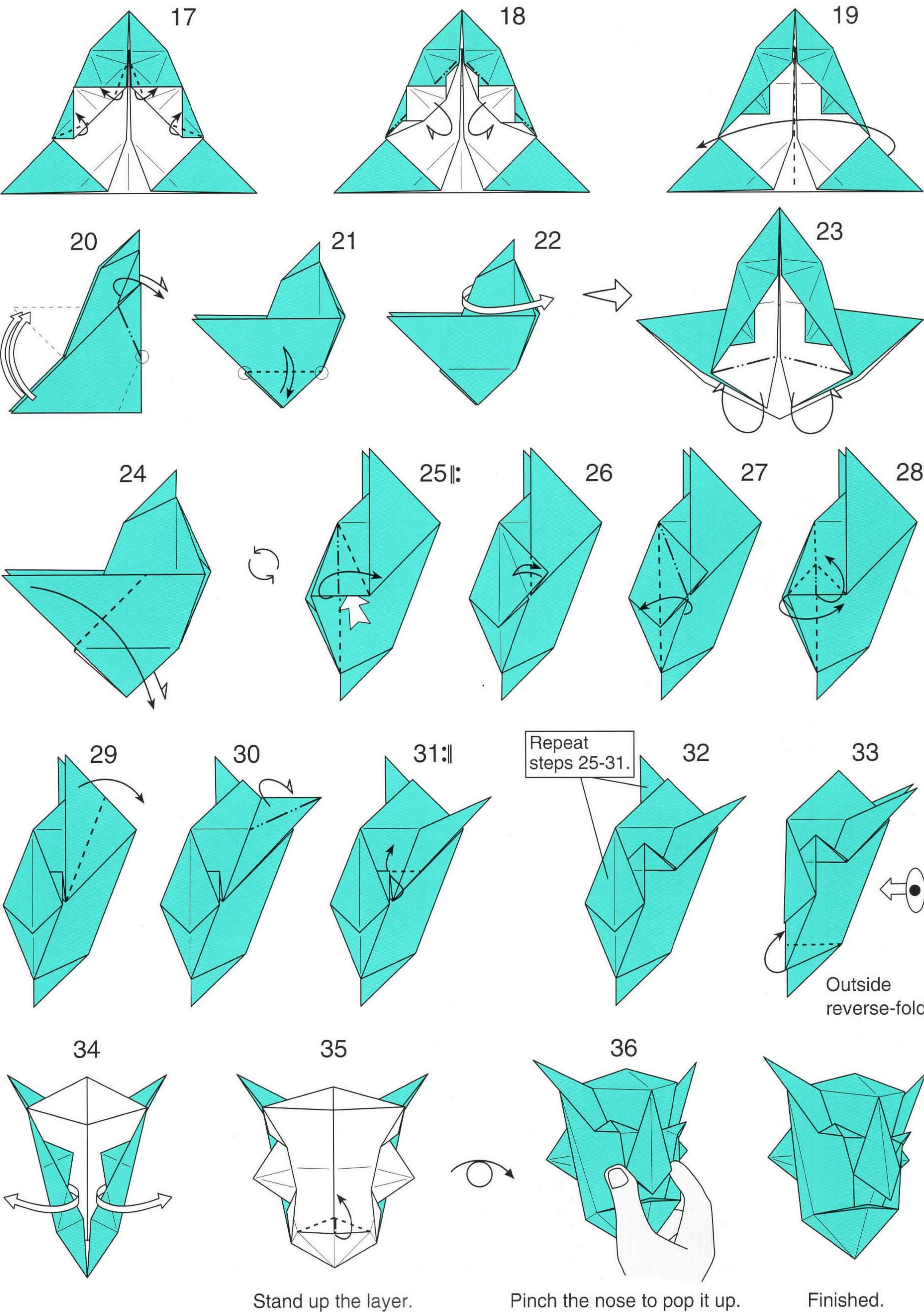
Fold using 6" (15 cm) origami paper.



Joy of making variations

I wanted to apply the design of *Tiger Mask* to a human face, instead of an animal. But the forehead is too small for a human (well, the devil, in this case), so I modified the composition by changing the axis of symmetry, as in *Squid*. You can multiply the number of variations of one model in similar ways. This is part of the joys of origami design.





Stand up the layer.

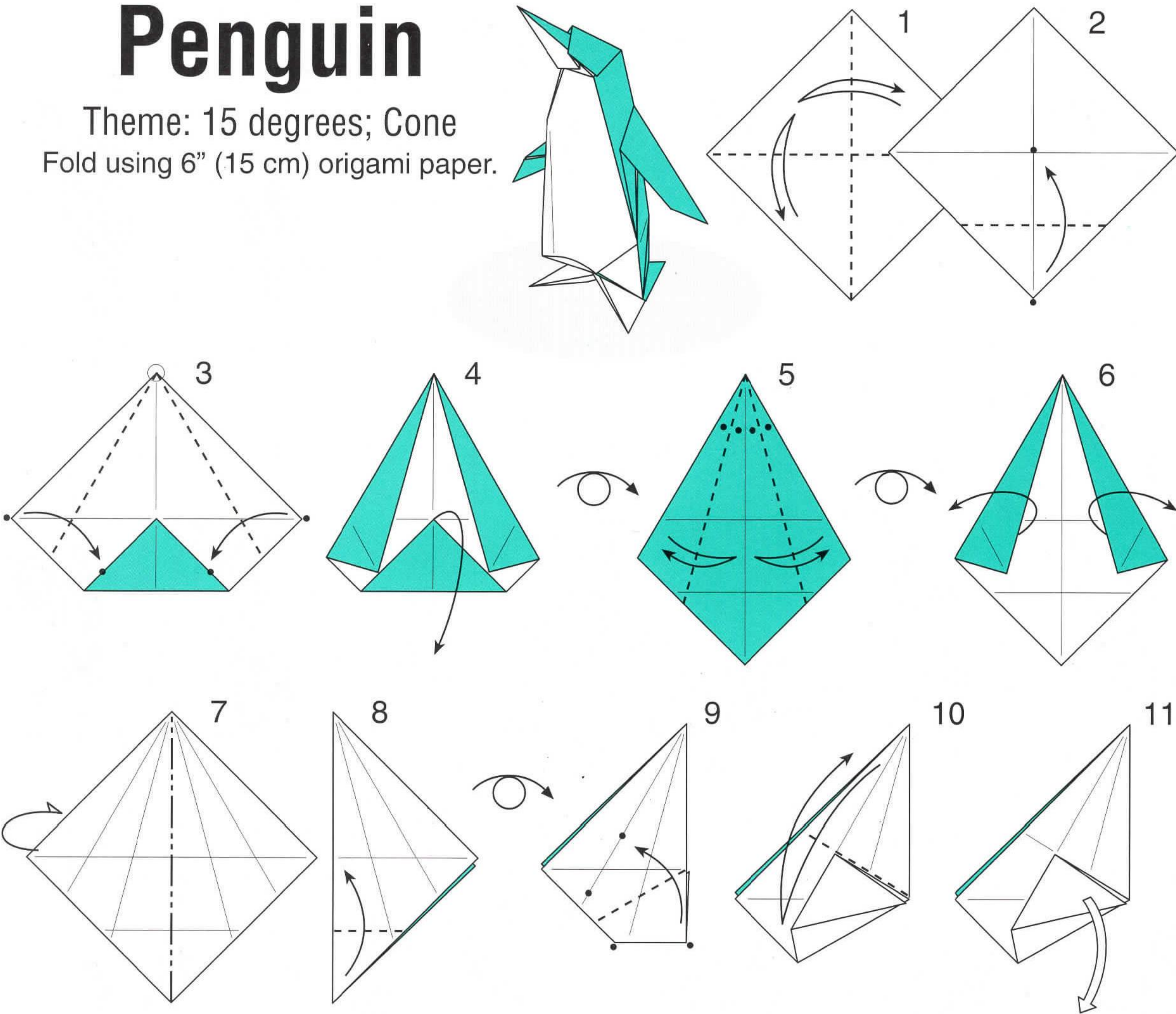
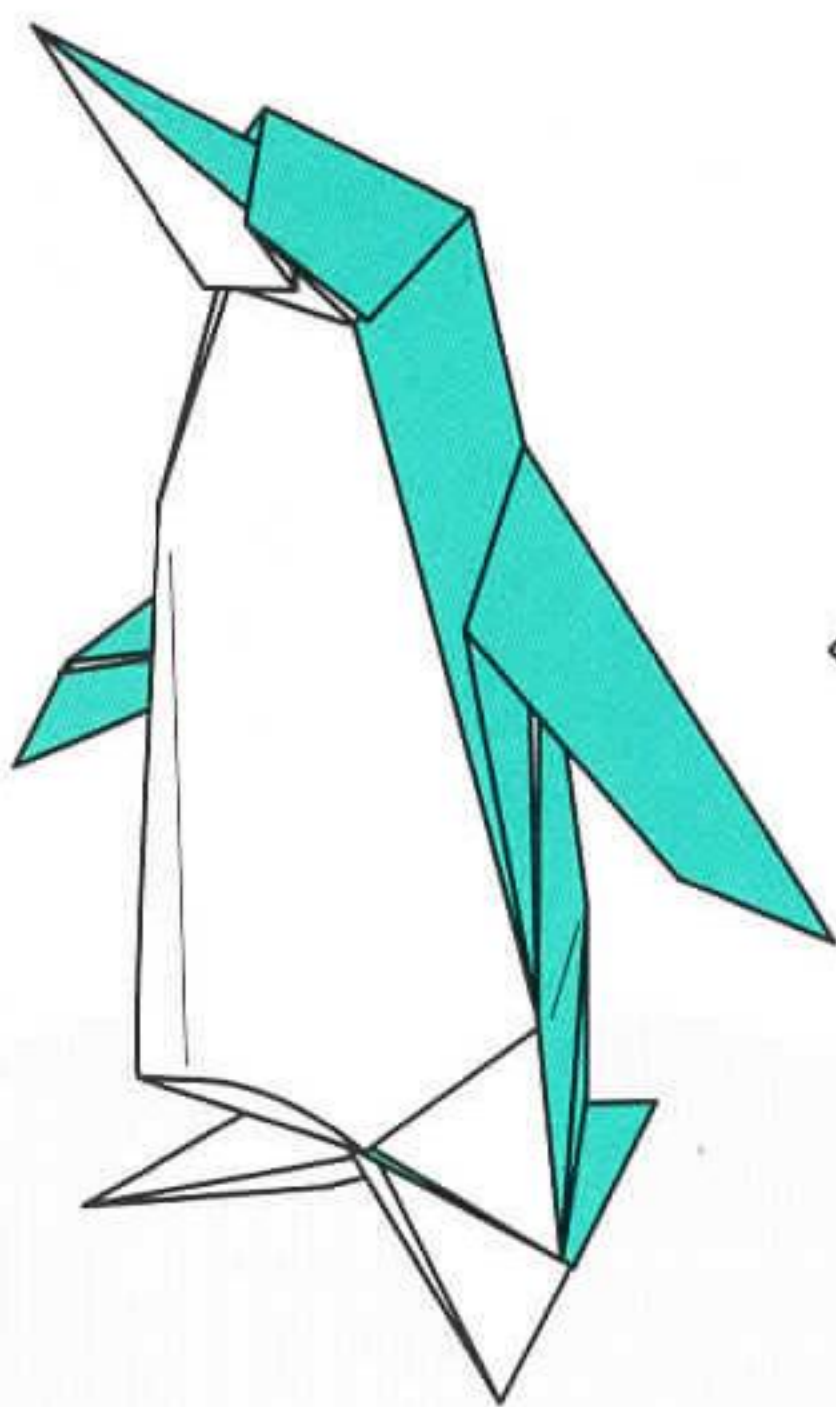
Pinch the nose to pop it up.

Finished.

Penguin

Theme: 15 degrees; Cone

Fold using 6" (15 cm) origami paper.



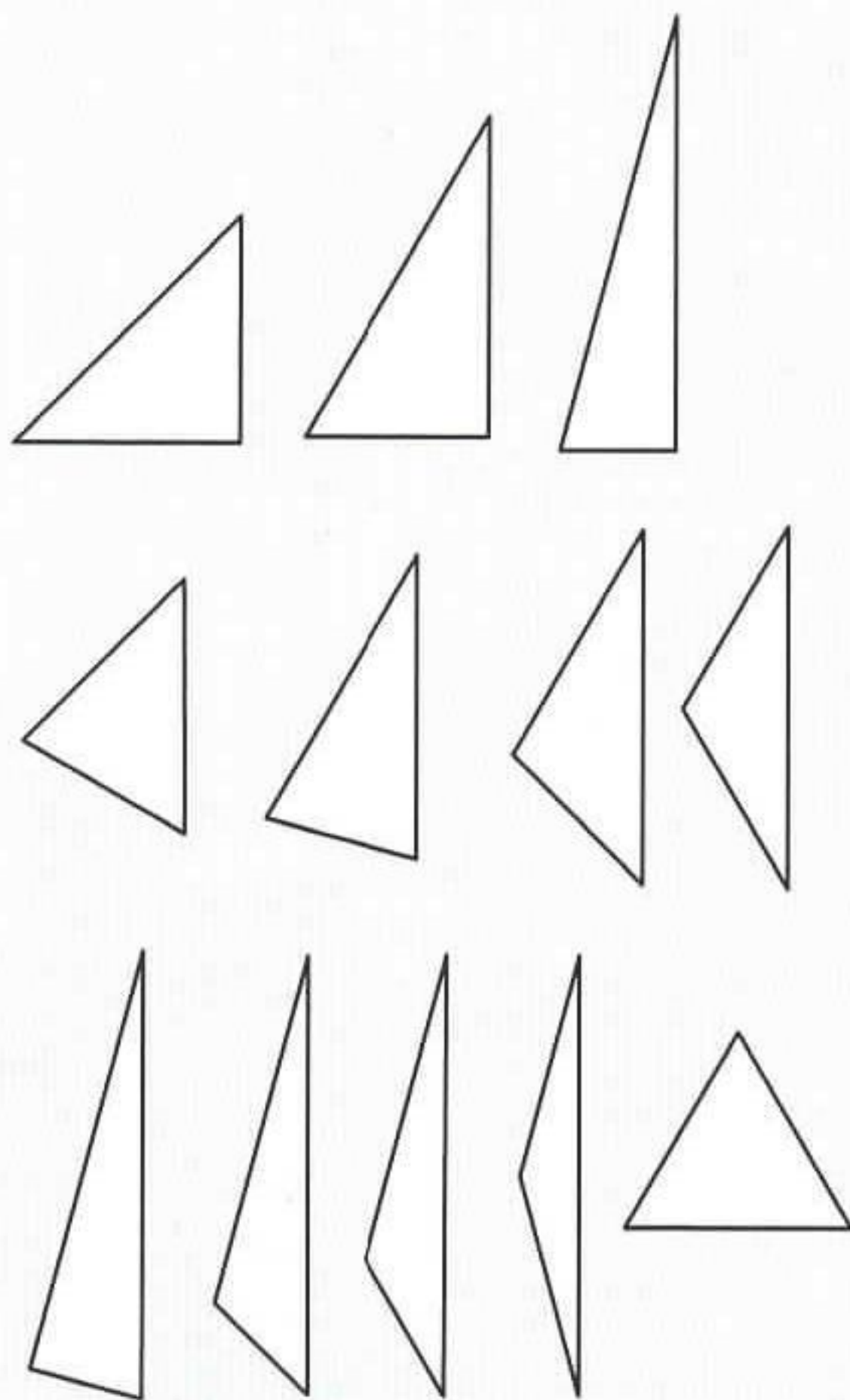
Using the 15° angle

The unit of angle in this model is not 22.5°, or a fourth of the right angle, but 15°, or a sixth of the right angle. The 15° angle is compatible with the square. You will notice that many points and lines meet each other in the sequence.

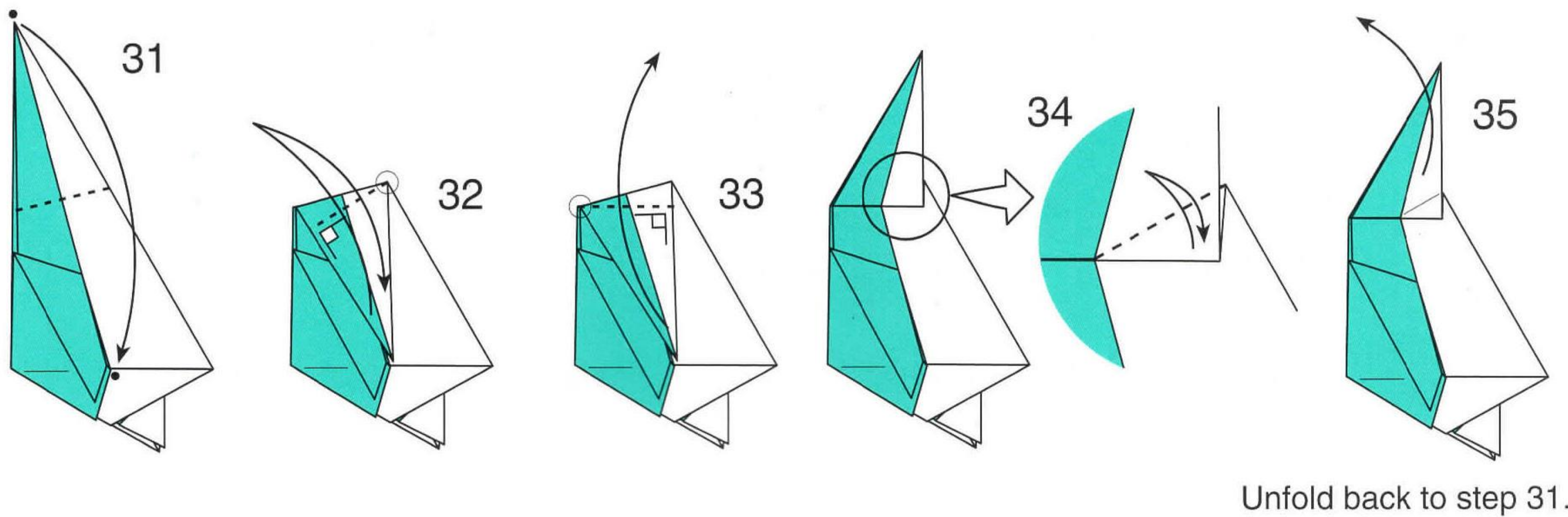
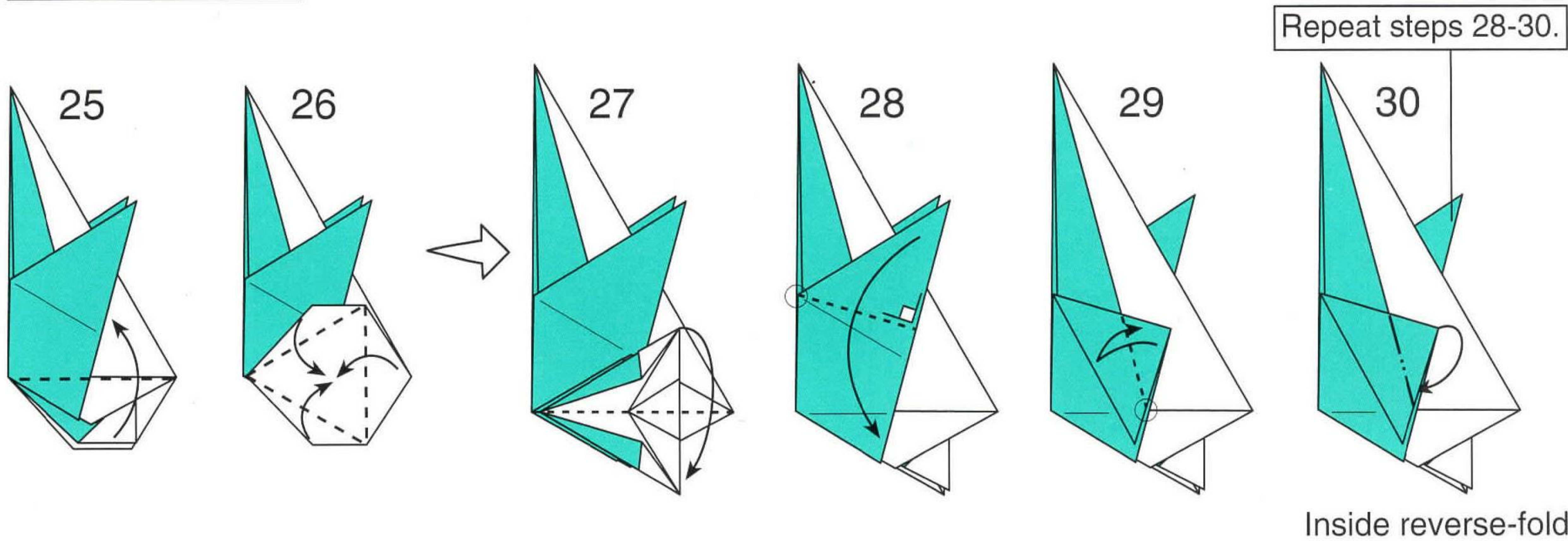
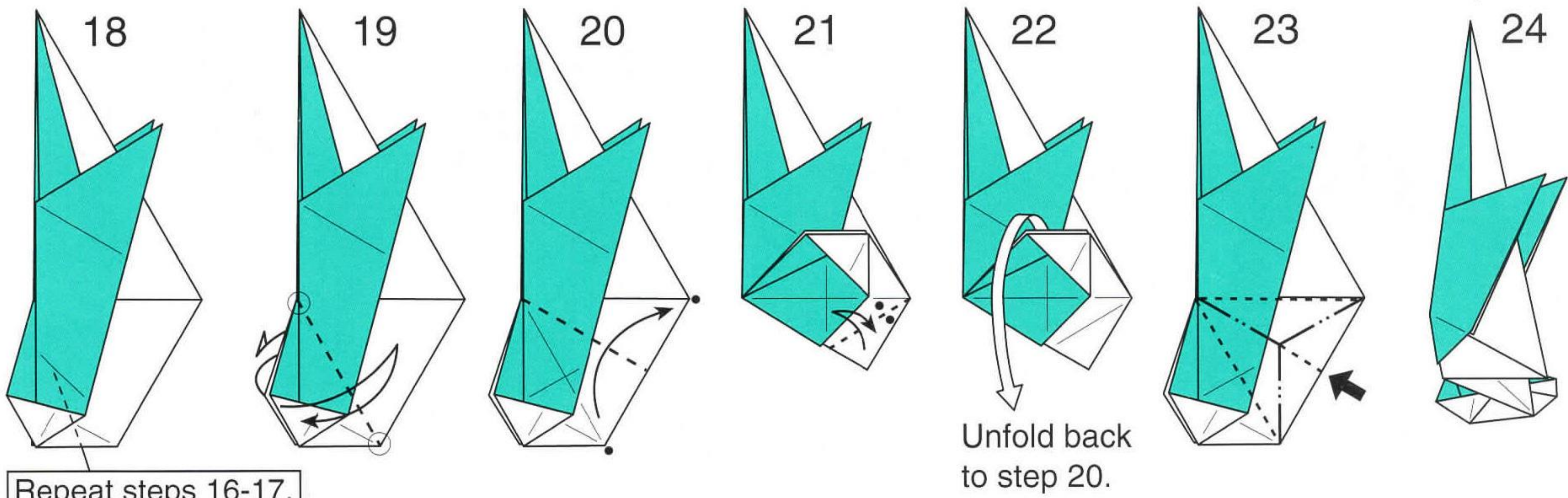
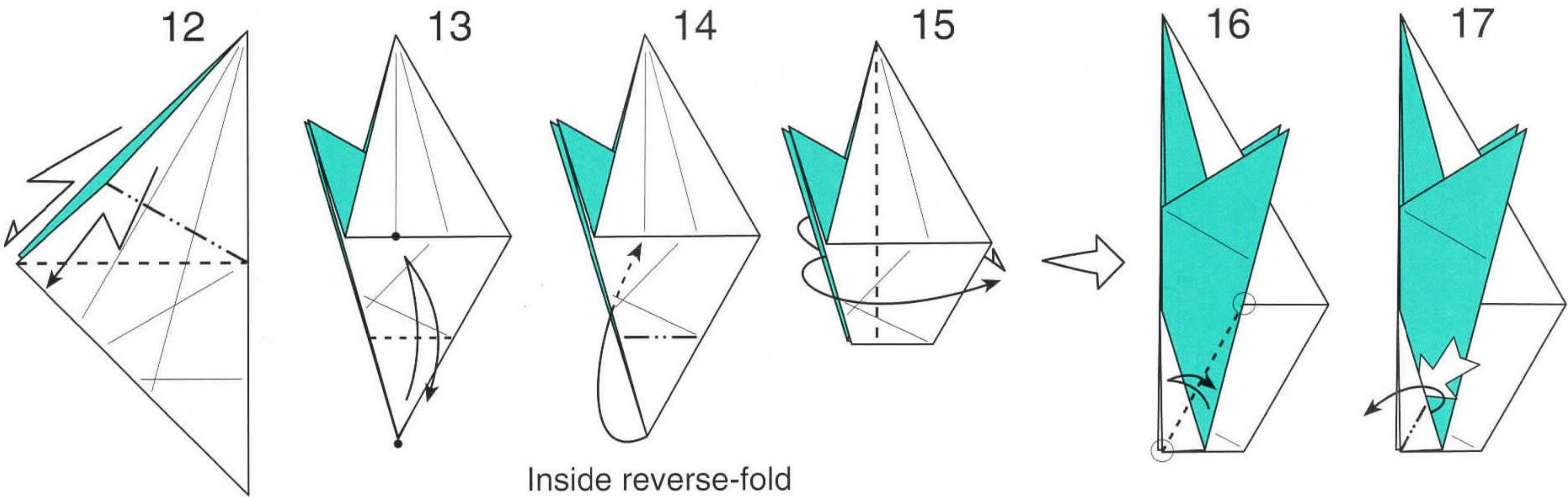
When we standardize the angle, we must define a unit angle. According to my experience, 15° and 22.5° are the most suitable to design, 30° is less suitable, and 18° and other degrees are difficult to use. When the unit is 15°, there are twelve types of triangle faces, which is much more than compared to the five when the unit is 22.5° (see *Wild Boar*). Among the twelve triangles shown on the right, three in the top row are basic.

The unit angle can also be 45°. That is equal to simple box-pleating (see *Snake*). I said “simple” because of the following reasons.

What is standardized in box-pleating structure is the position of corners, rather than the angle, of creases. Using “advanced” box-pleating, we can make an ordered structure that is not based on any division of 360°.



Triangles based on 15° angle units



36

37

38

39

40

41

42

43

44

45

46

47

48

49

50

51

Finished.

Curved surfaces that can be made from flat surfaces.

Although any curved surface, when divided into tiny areas, can be approximated from a plane, only three types of curved surface are developable, in other words, can be developed onto a plane. They are the conical, cylindrical, and tangent surfaces. The basic idea of *Penguin* is, besides using 15° angle unit, making a three-dimensional body with a conical surface instead of a polyhedron that is a combination of planes. The earlier version of this model was closer to the cone.

Cone

Cylinder

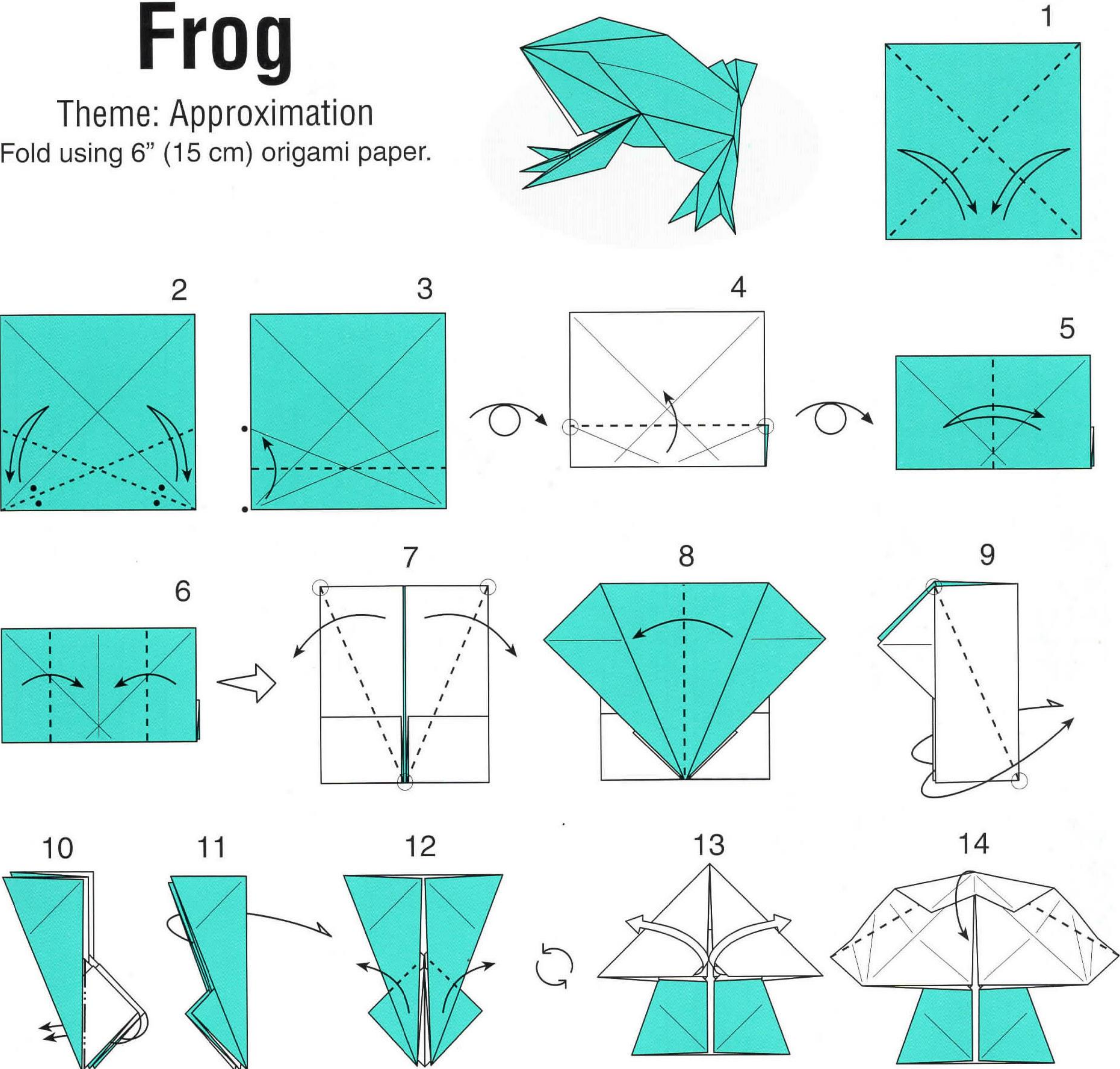
Helical-convolute surface

Examples of conical, cylindrical, and tangent surfaces: a cone, a cylinder, and a helical-convolute surface.

100 Intermediate Models

Frog

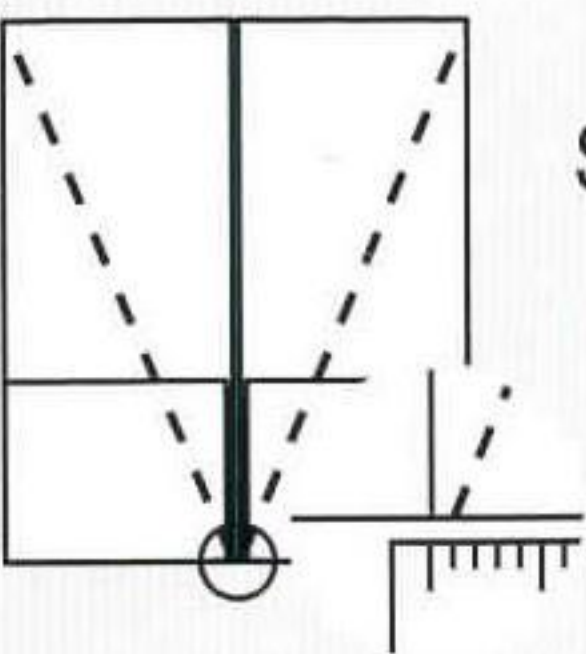
Theme: Approximation
Fold using 6" (15 cm) origami paper.



Inside reverse-fold

Approximation

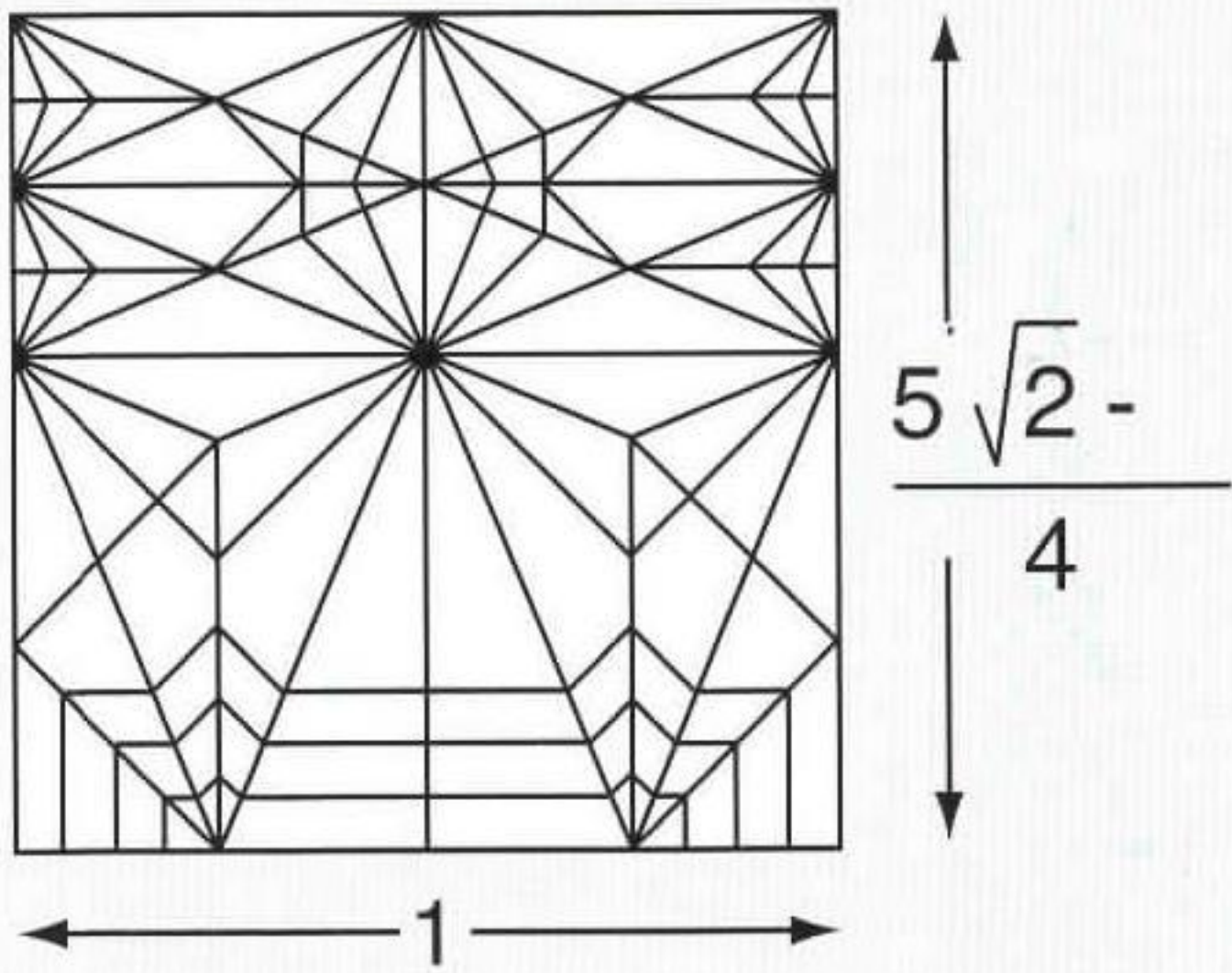
If you calculate assuming that the angles of creases are multiples of 22.5°, then the crease pattern of this *Frog* does not fit in a square, as shown on the right. The ratio of the height to the width is about 1.017...



Step 7

Theoretically, there is a gap of about 1/16".

That means, when folded using 6" (15 cm) paper, there is a gap of about 1/16" (1 mm) at step 7. But in practice, you do not have to bother about it. For some models, folding precisely is essential because errors will be magnified through the sequence. But for other models like this, errors will be absorbed in paper. That is one of the differences between real-world origami and pure geometry, where lines have no width and surfaces have no thickness.



The crease pattern of *Frog* (mountain and valley folds are not shown).

15

16

17

18

19

20

21

Reverse to color-change while paying attention not to unfold step 15.

22

23

24

25

Repeat steps 19-21.

26

27

28

29||

30

31

32

33

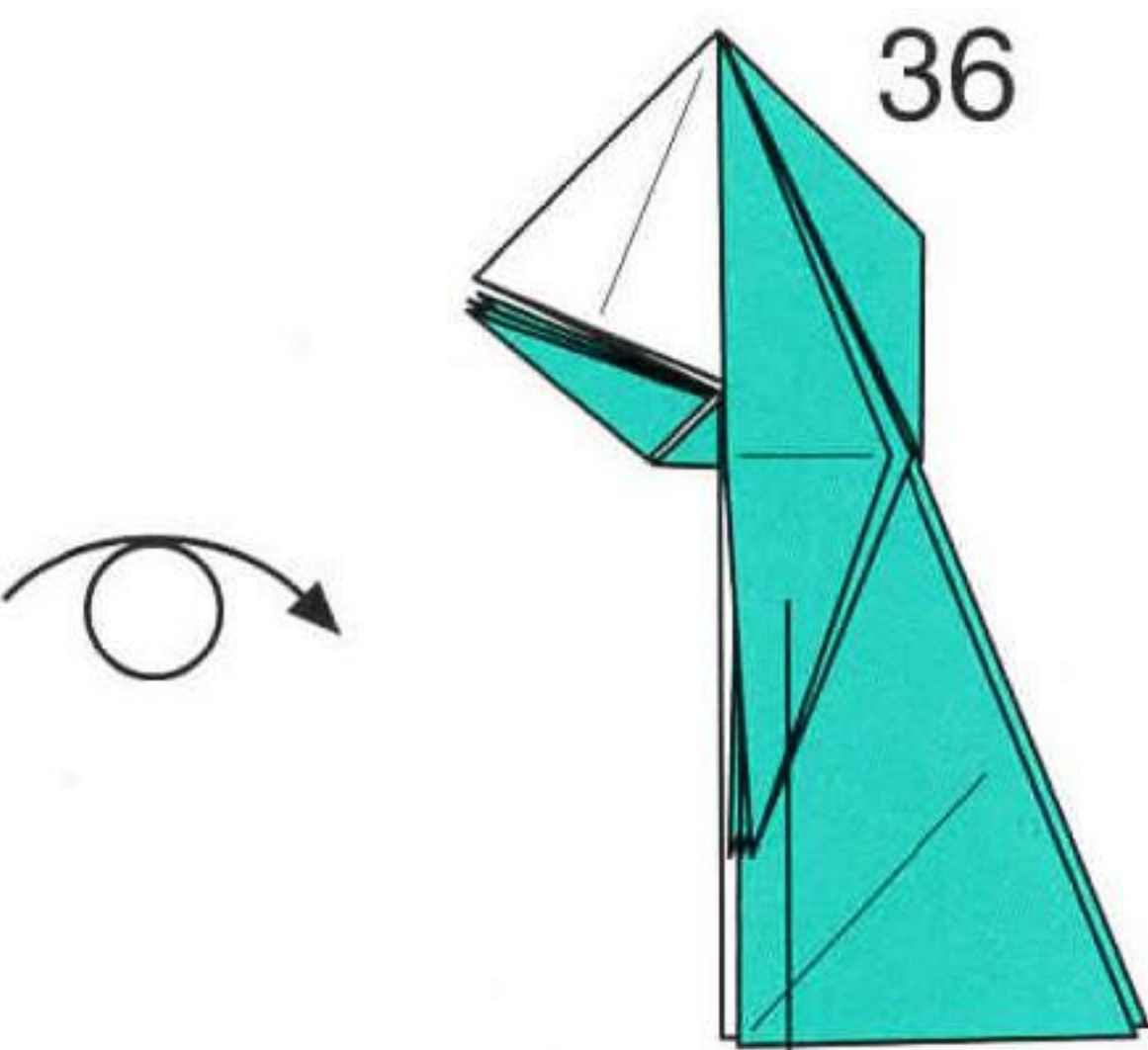
34

35:||

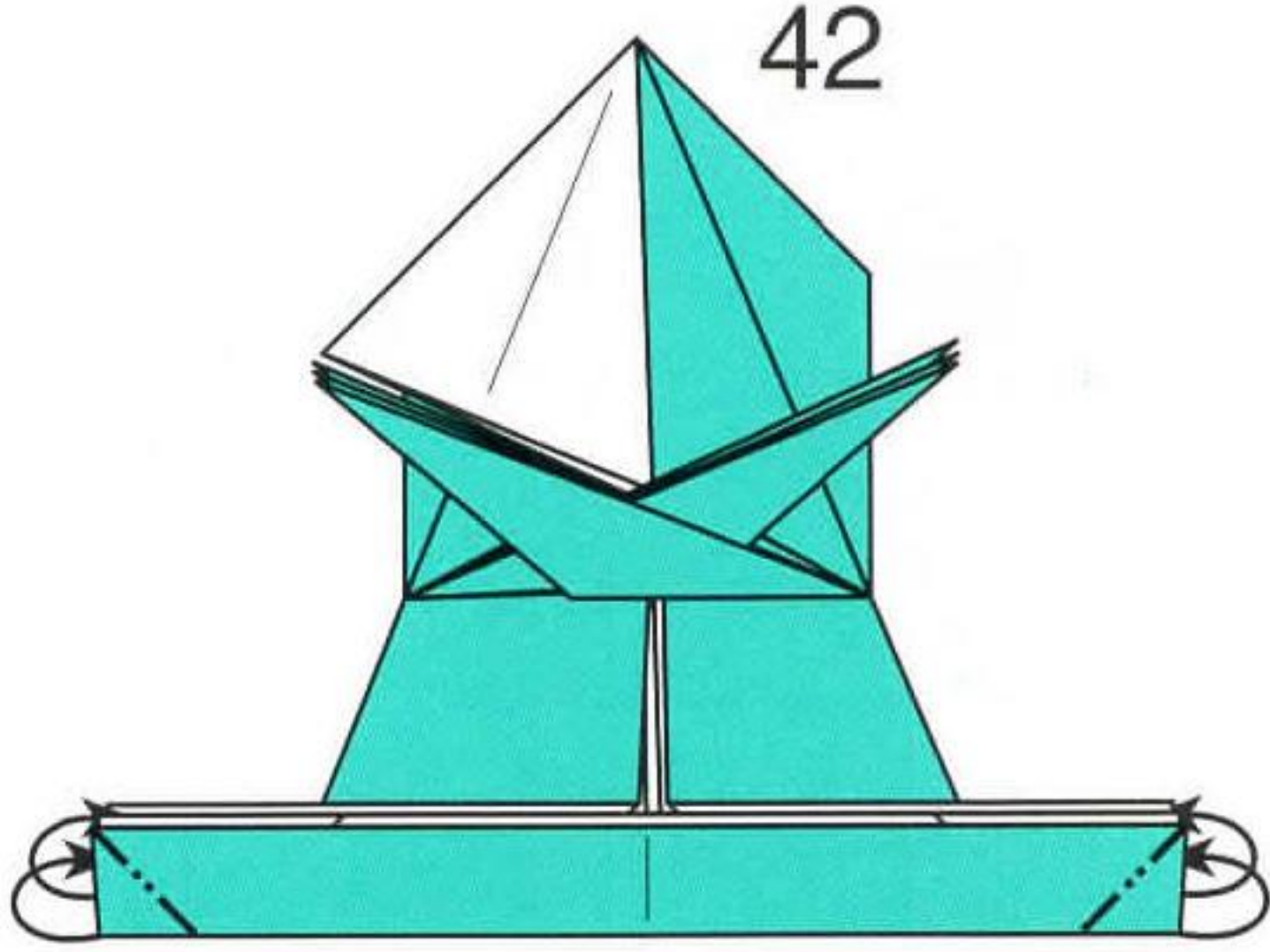
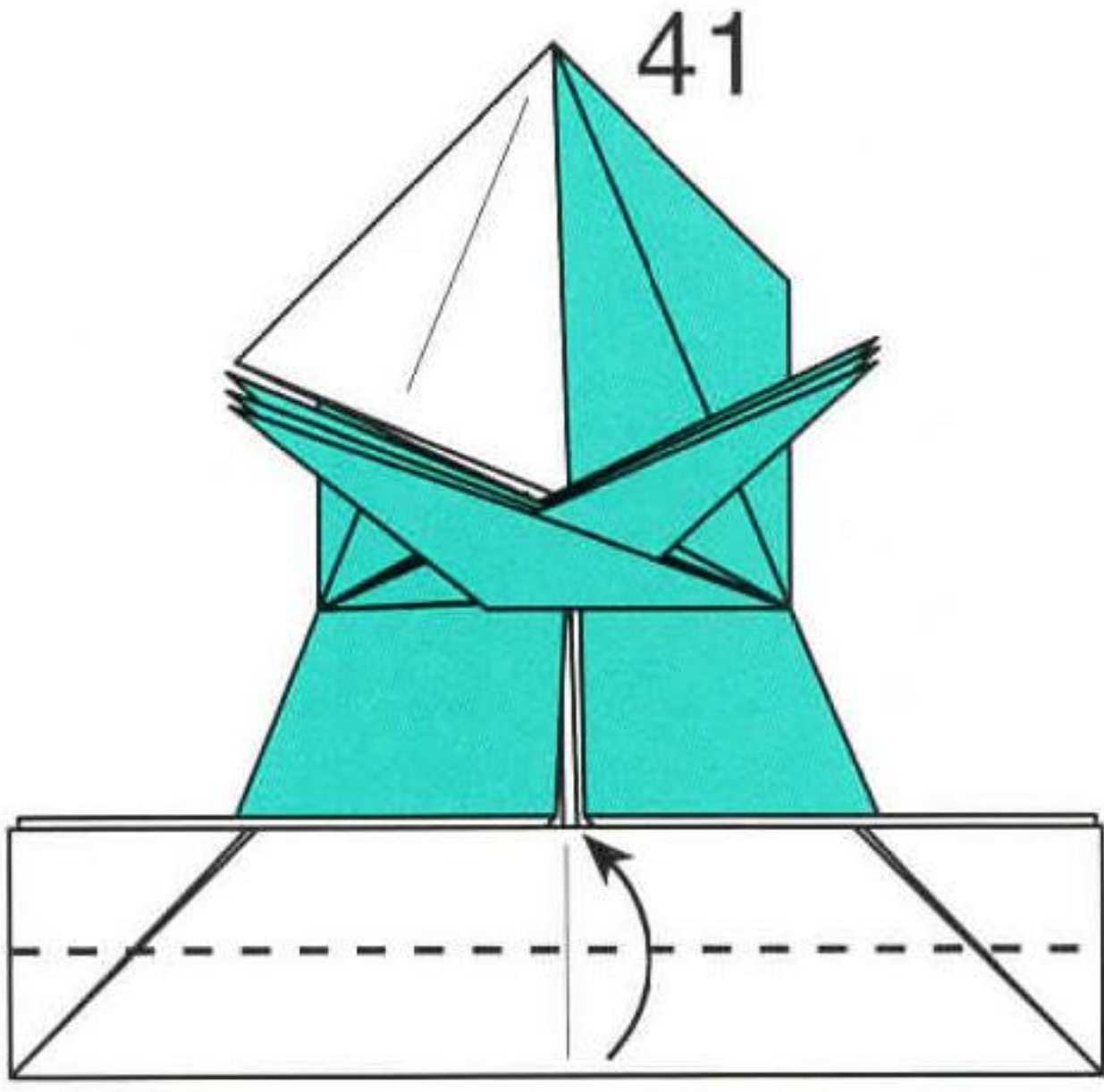
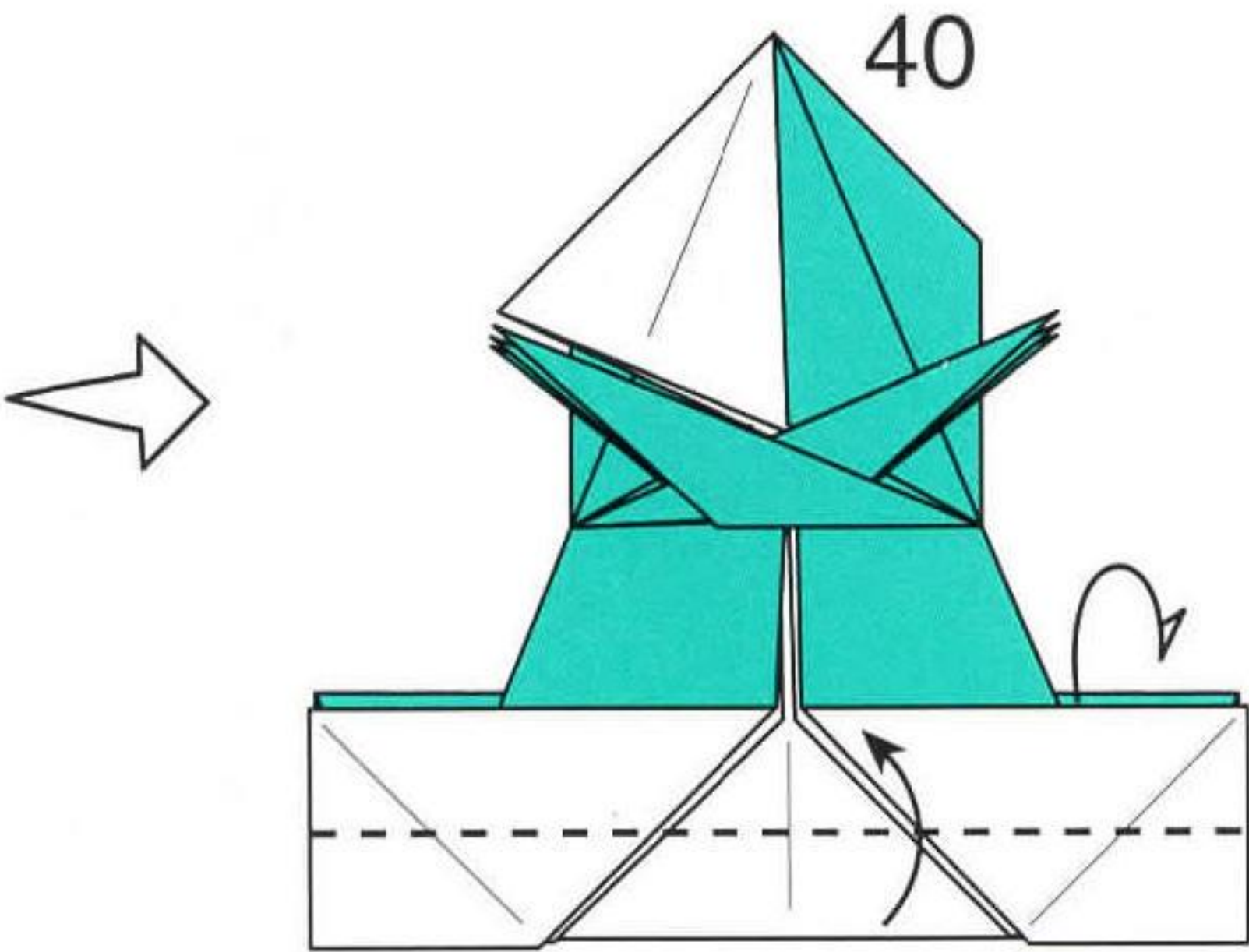
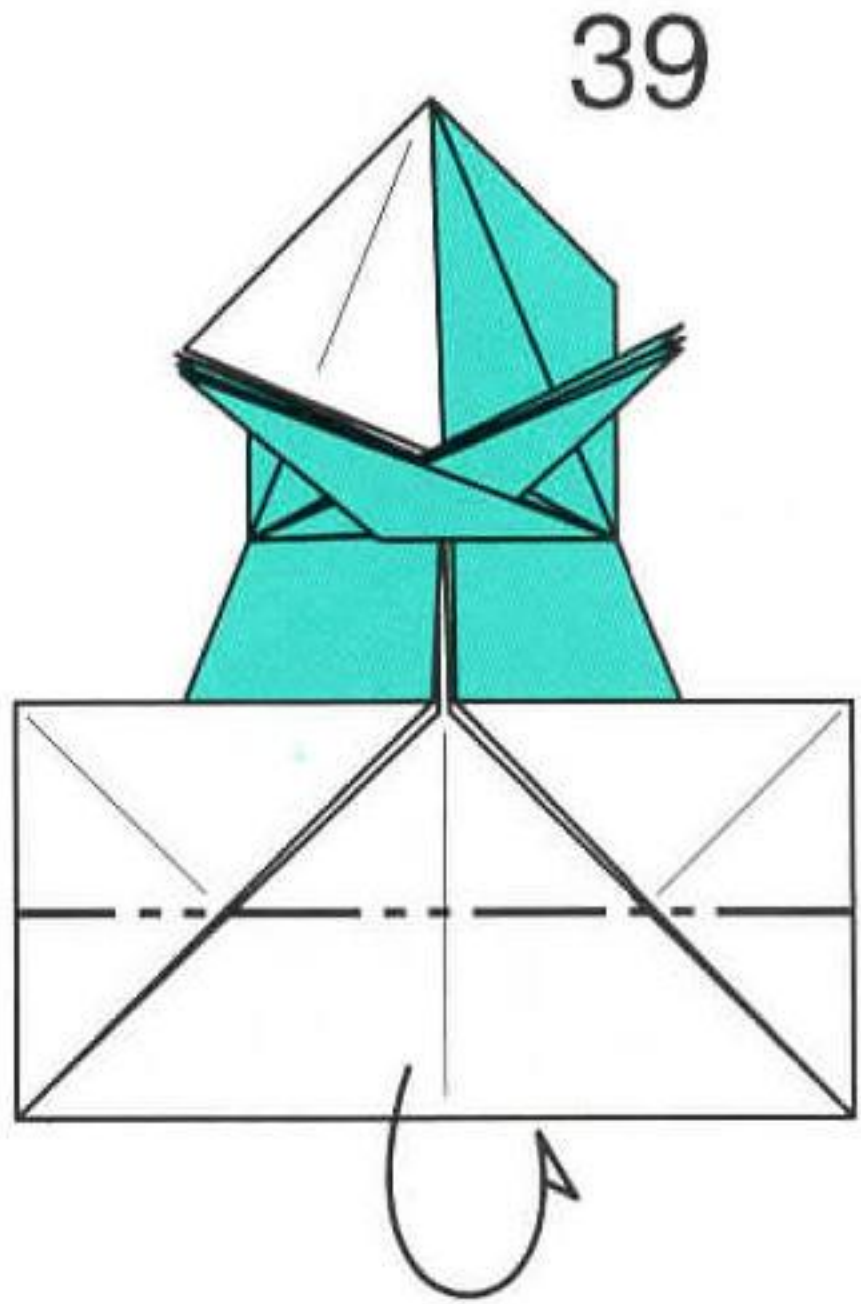
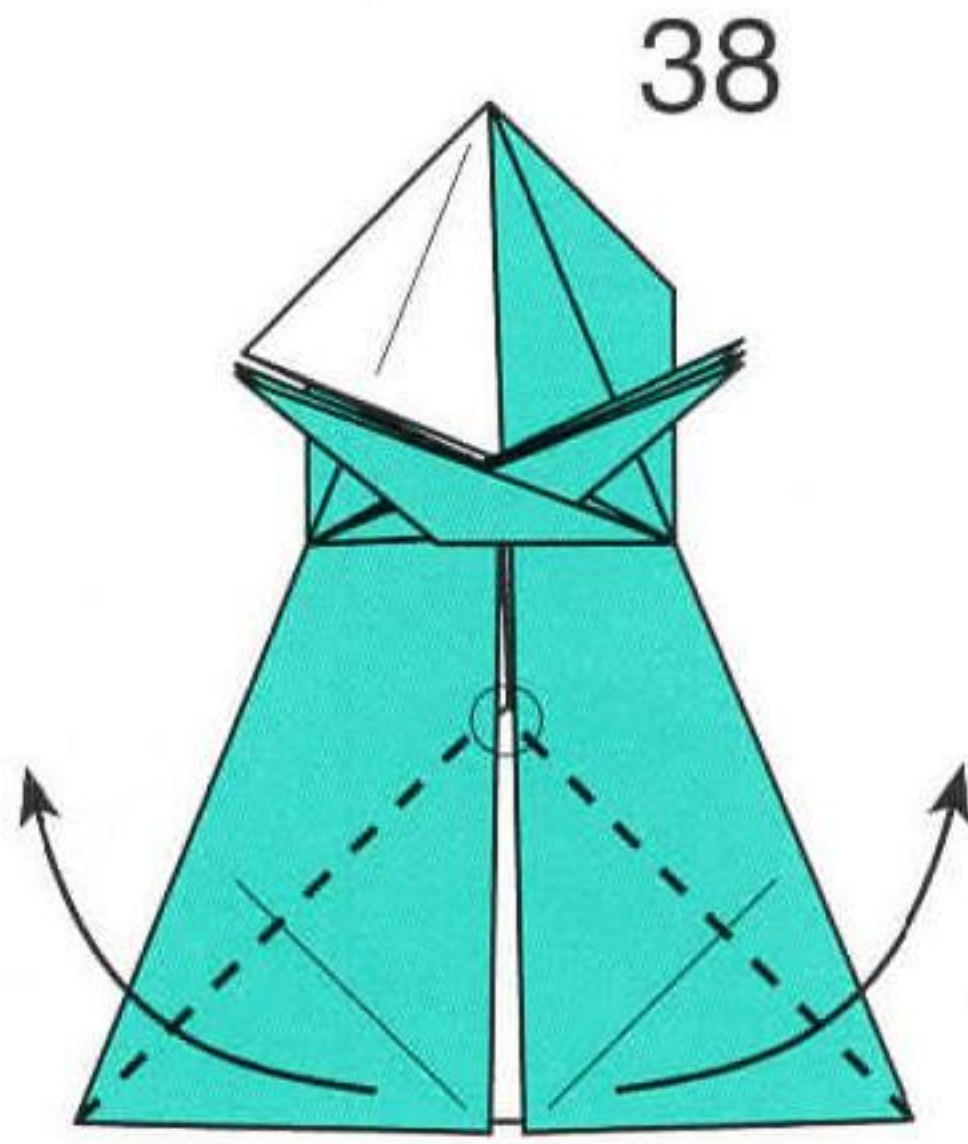
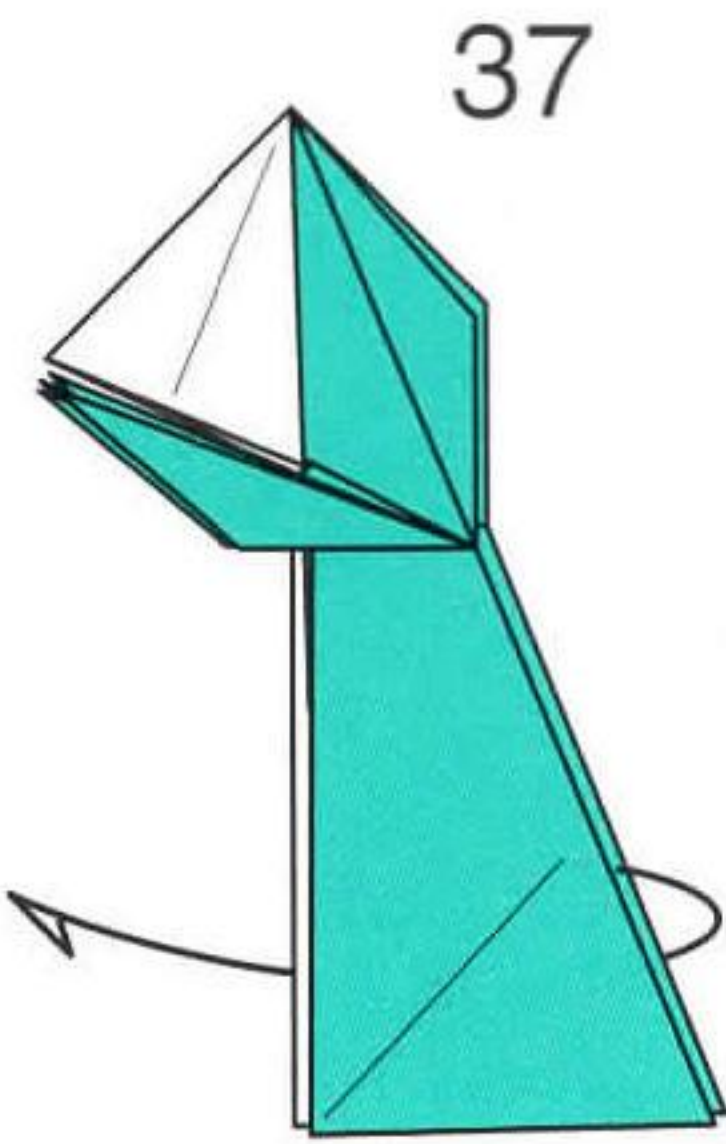
Open slightly.

Pop up from inside.

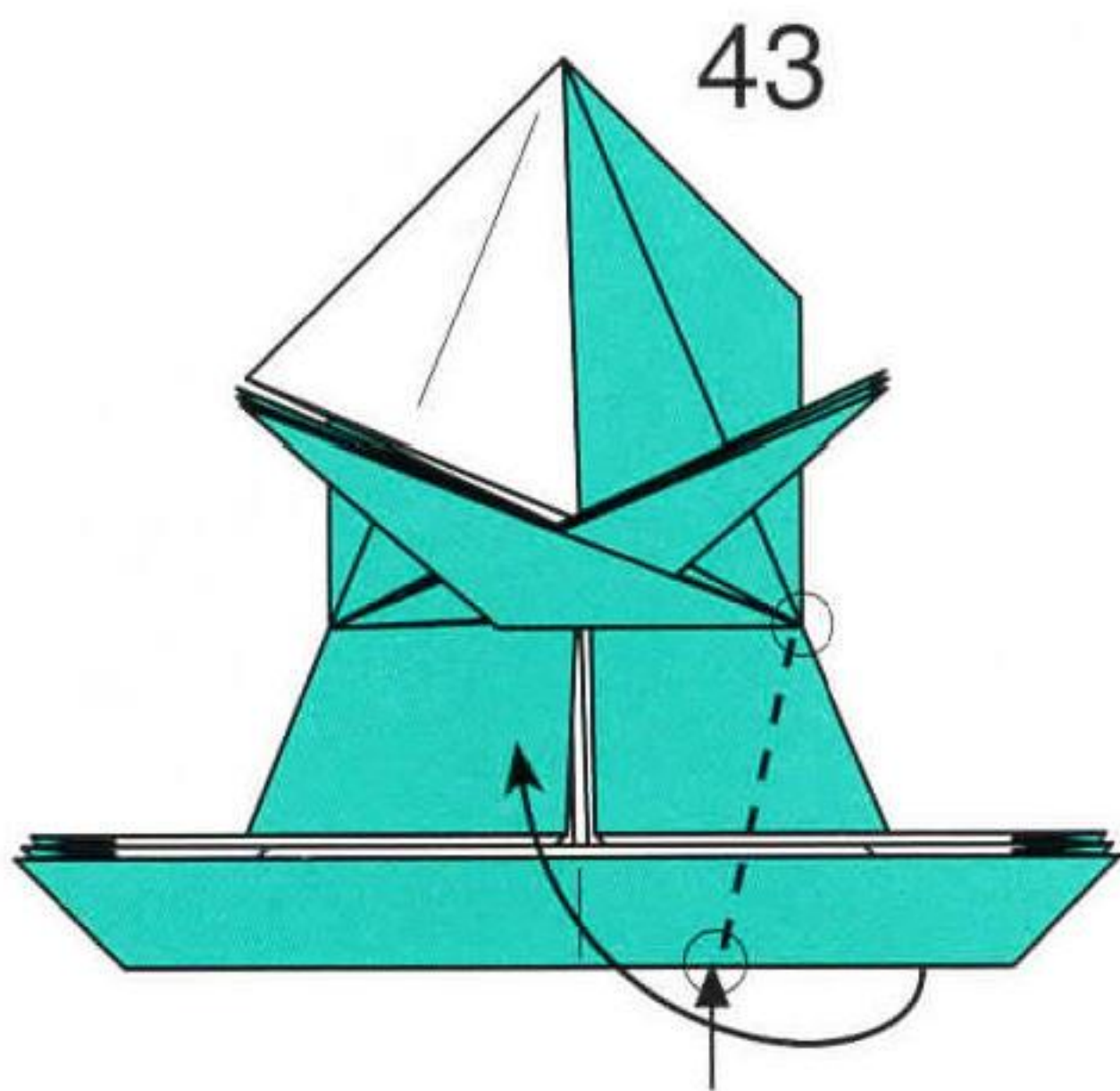
Fold two layers.



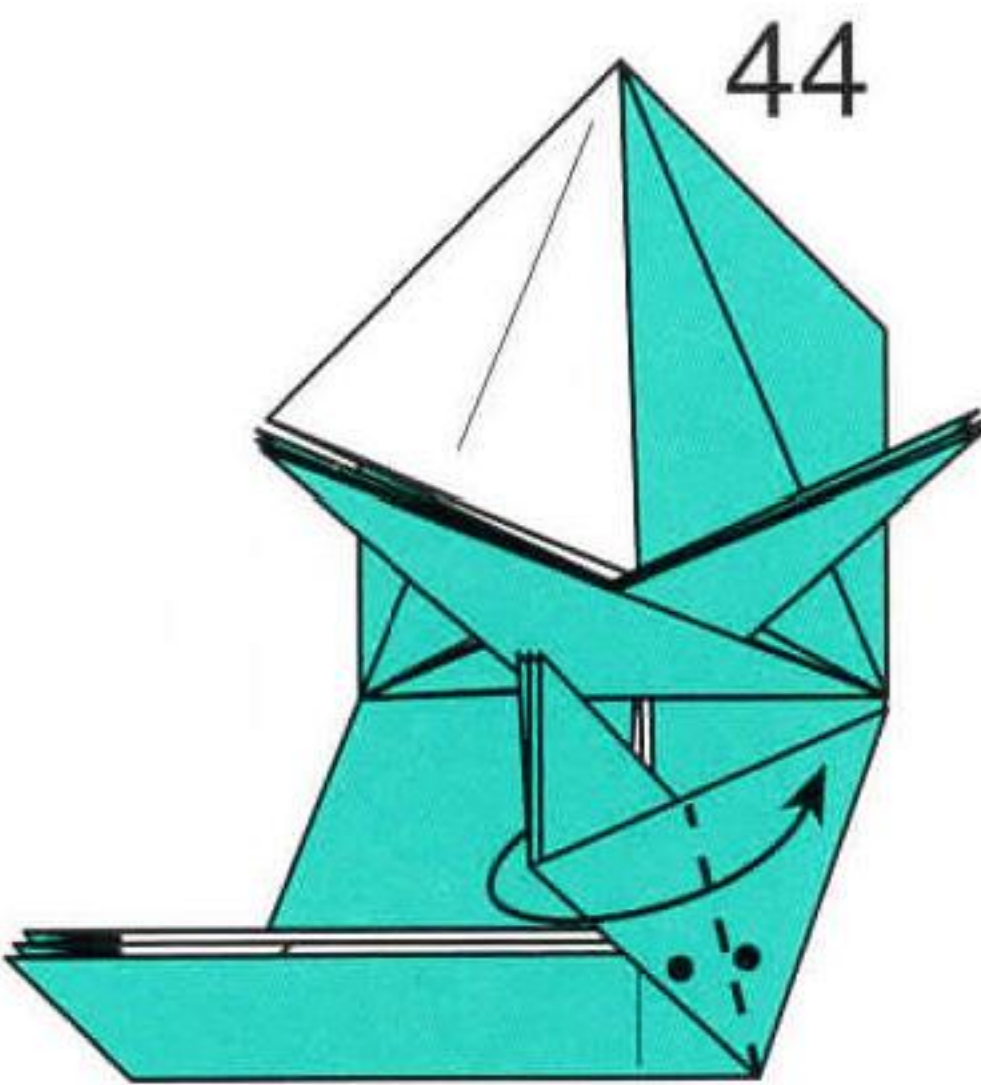
Repeat steps 29-35.



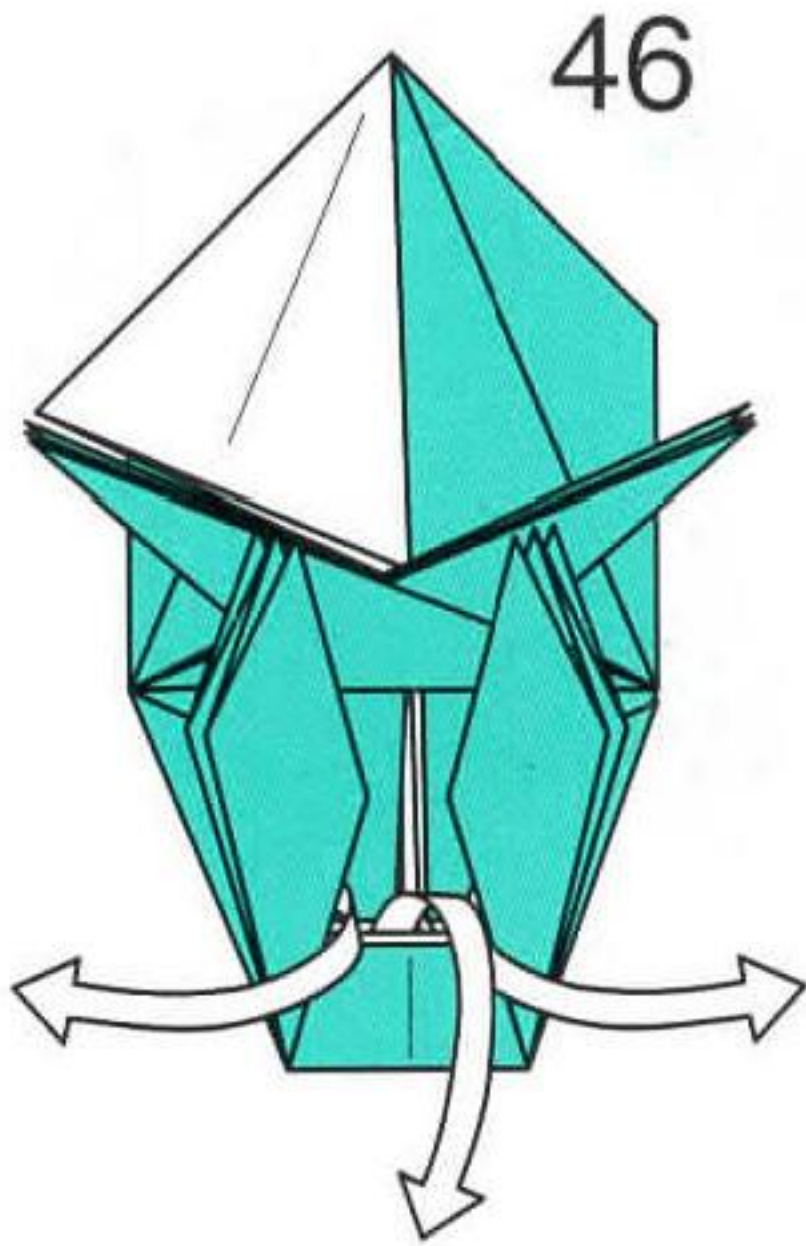
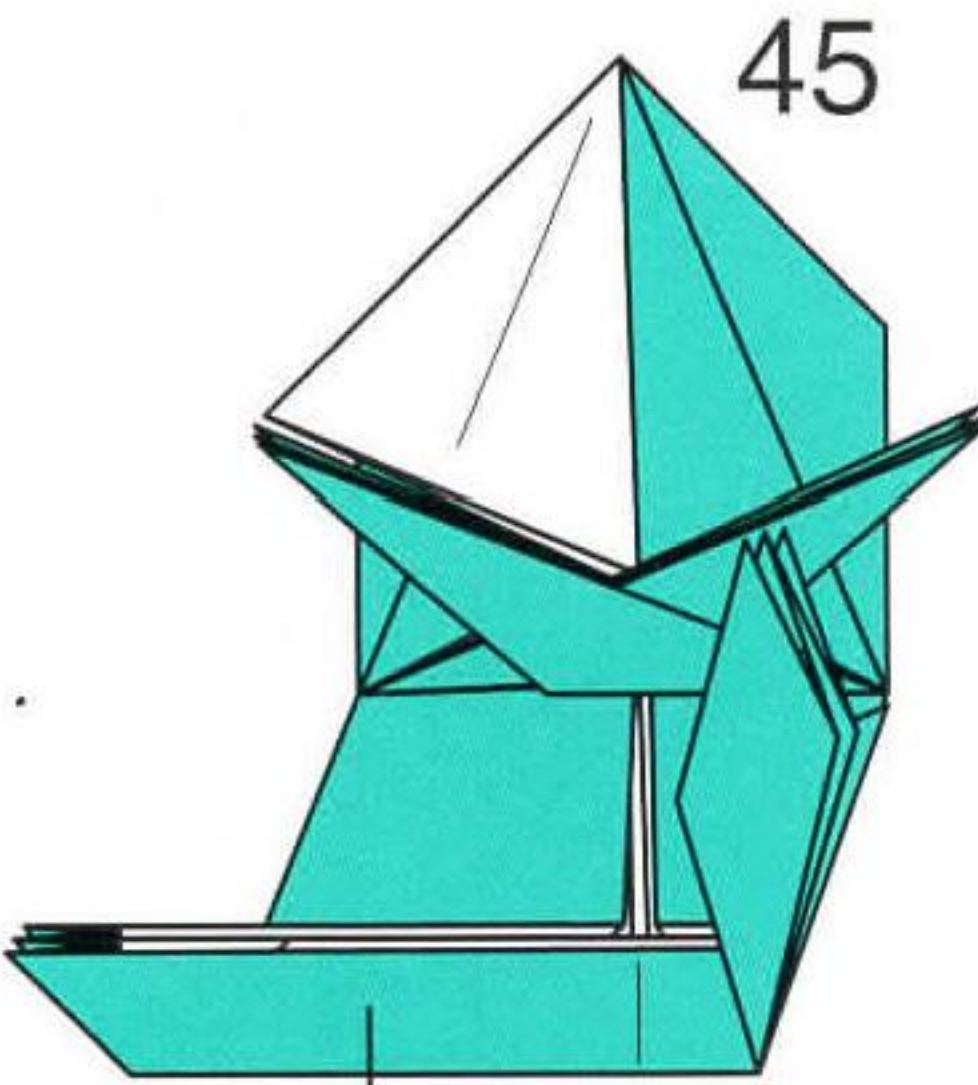
Inside reverse-fold



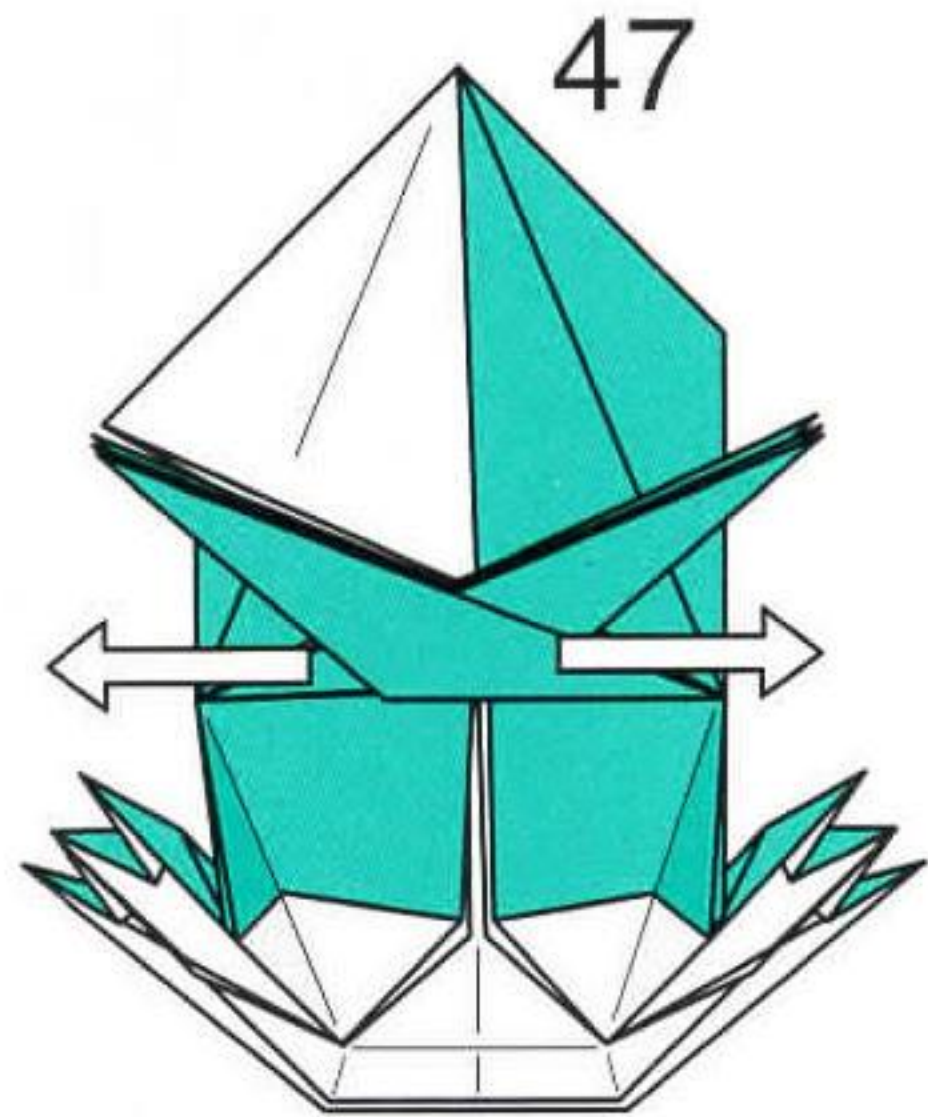
There is a hidden edge here.



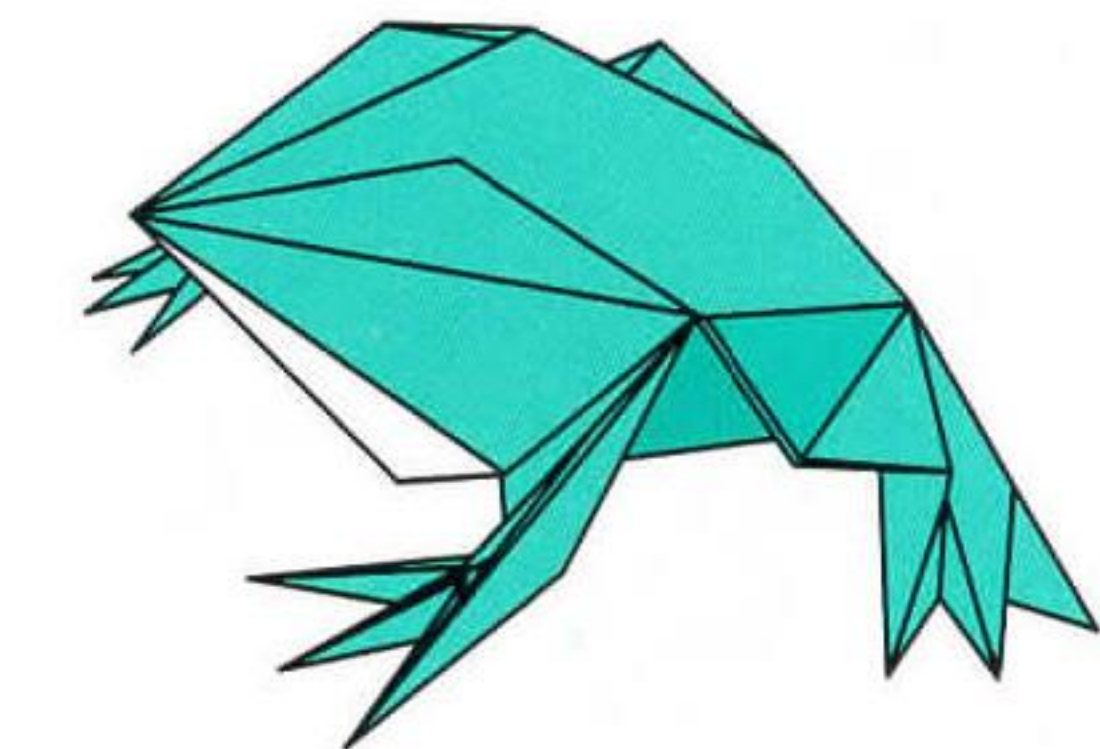
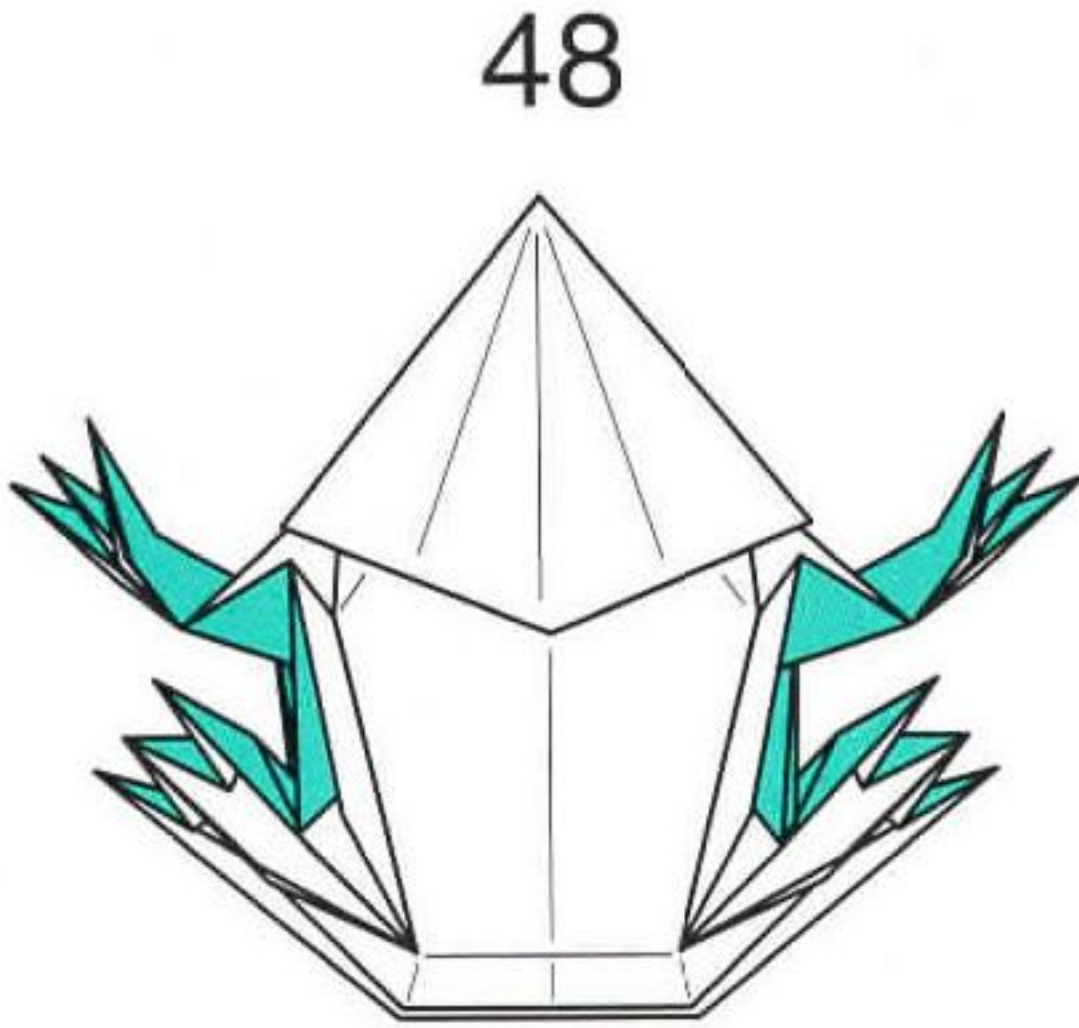
Repeat steps 43-44.



Open to make it 3D box-shape.



Pull apart as far as possible.

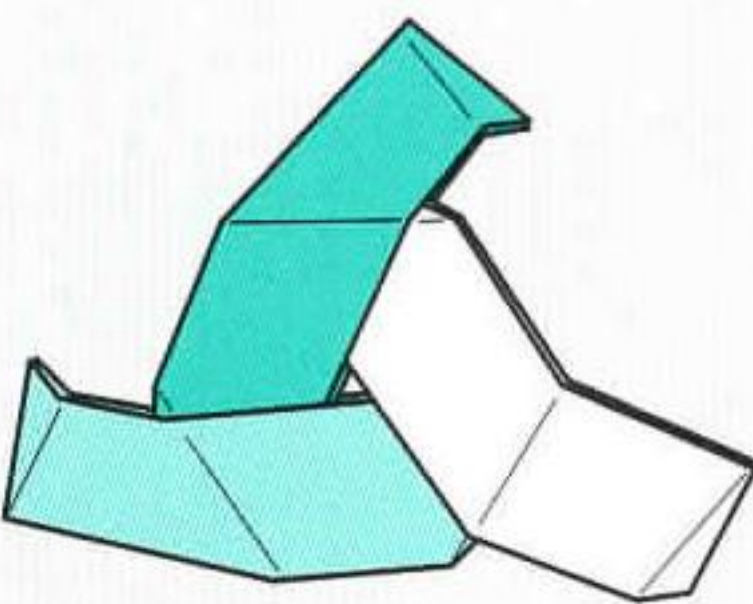
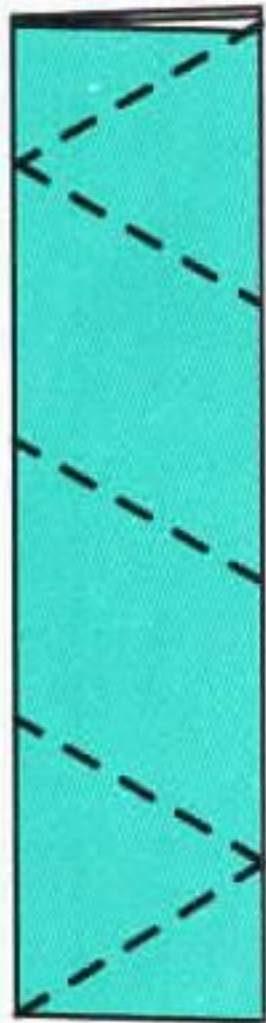


Adjust the model so that it stands on its toes to finish.

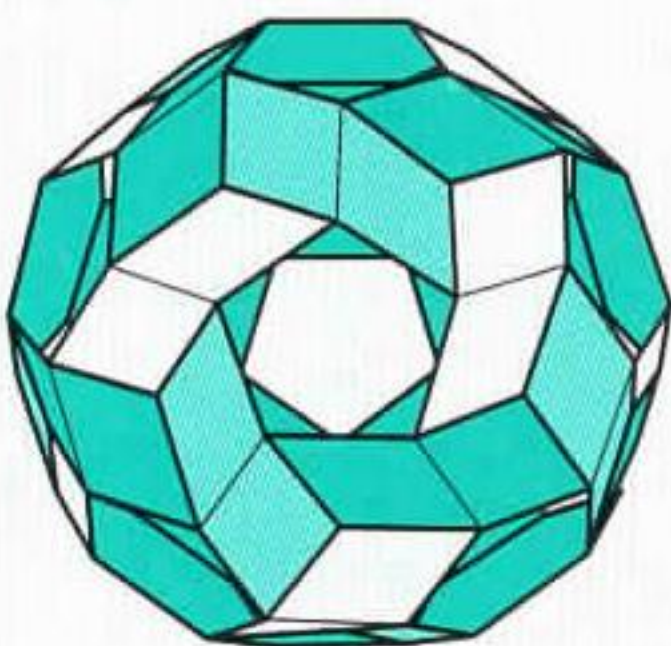
Another interesting approximation

$4 \times \sqrt{3} = 6.928... \approx 7$

Fold a square in fourths, like an accordion, and fold as shown on the right. You will obtain a modular unit that can be assembled as shown below.



Assembly

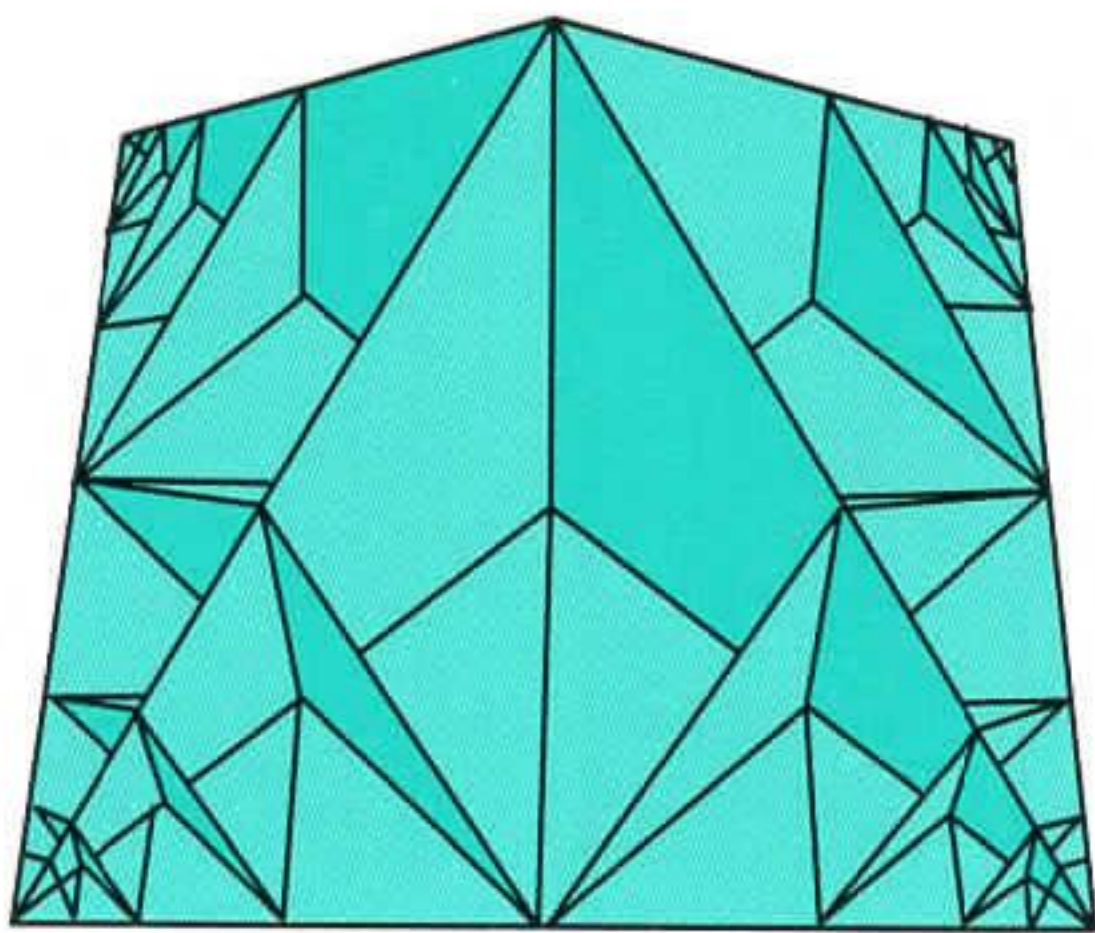


30-piece

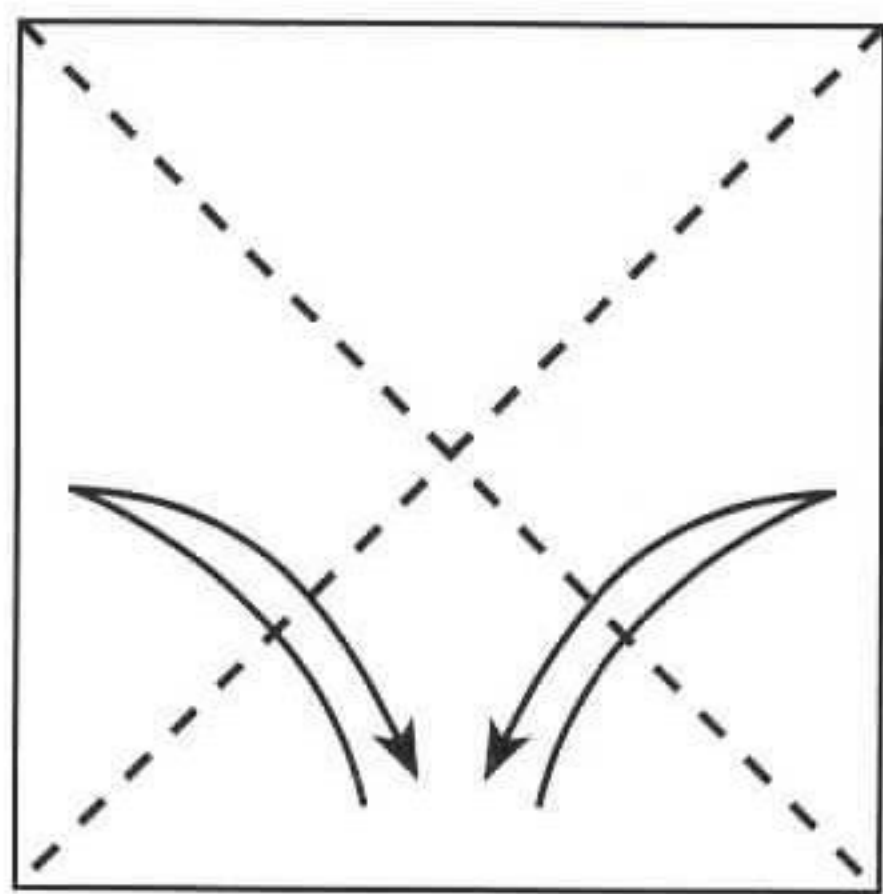
Pyramid

Theme: Infinite folding

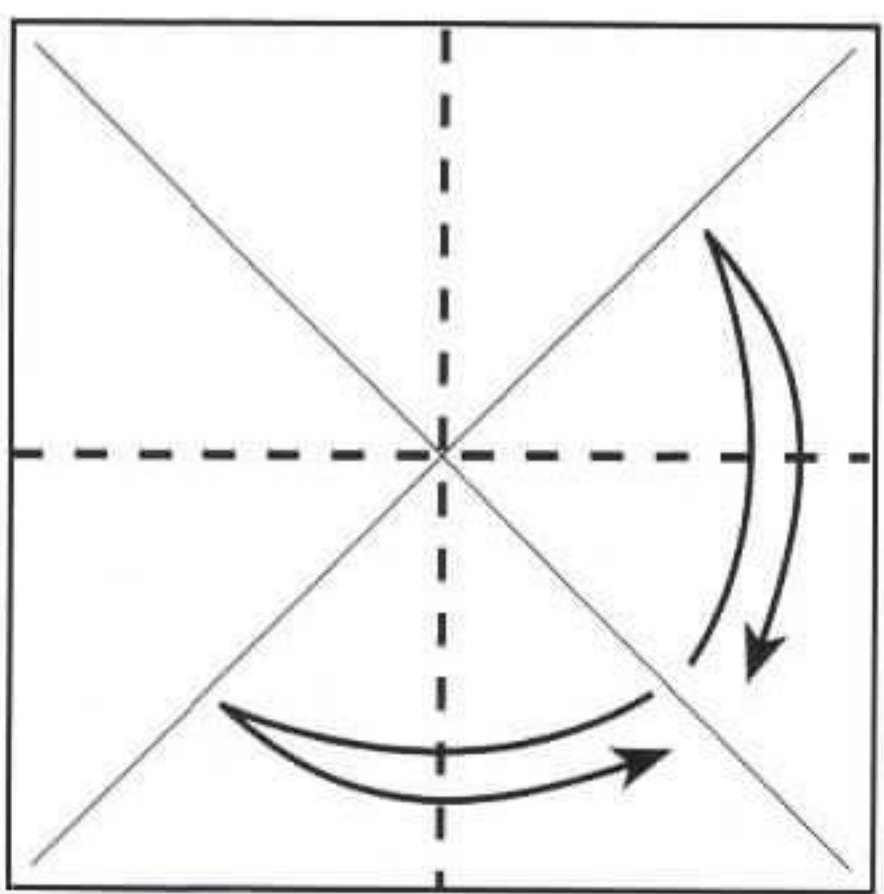
Fold using 6" (15 cm) or preferably larger origami paper.



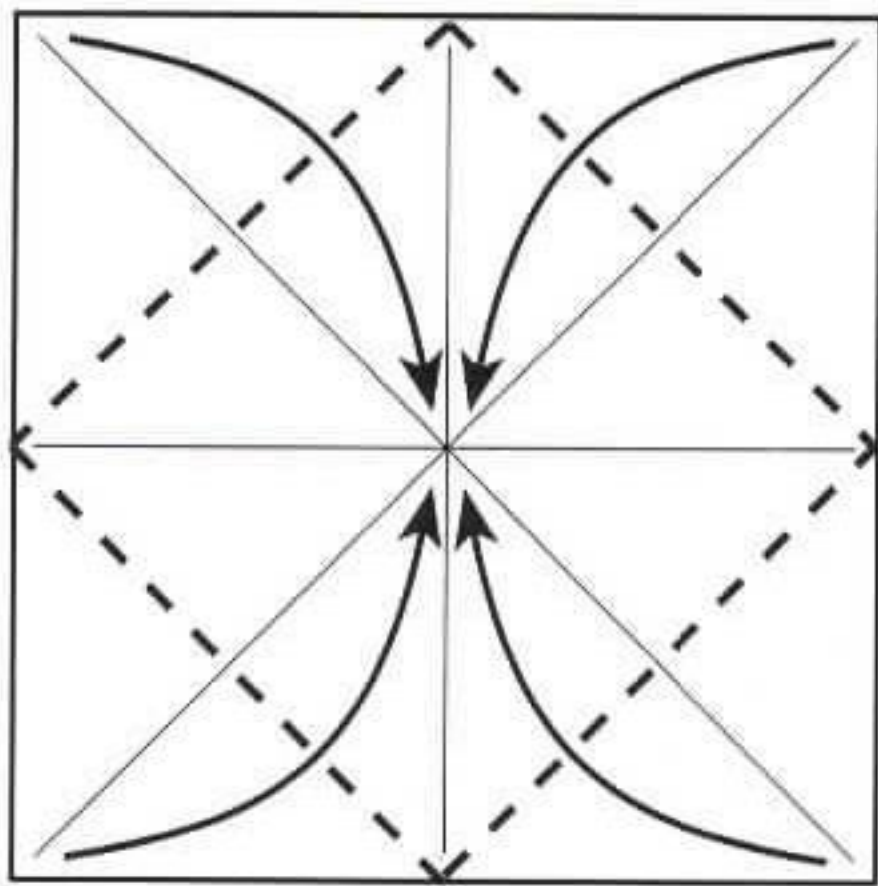
Although the sequence is diagrammed in 33 steps, you can, in theory, repeat the steps as many times as you want.



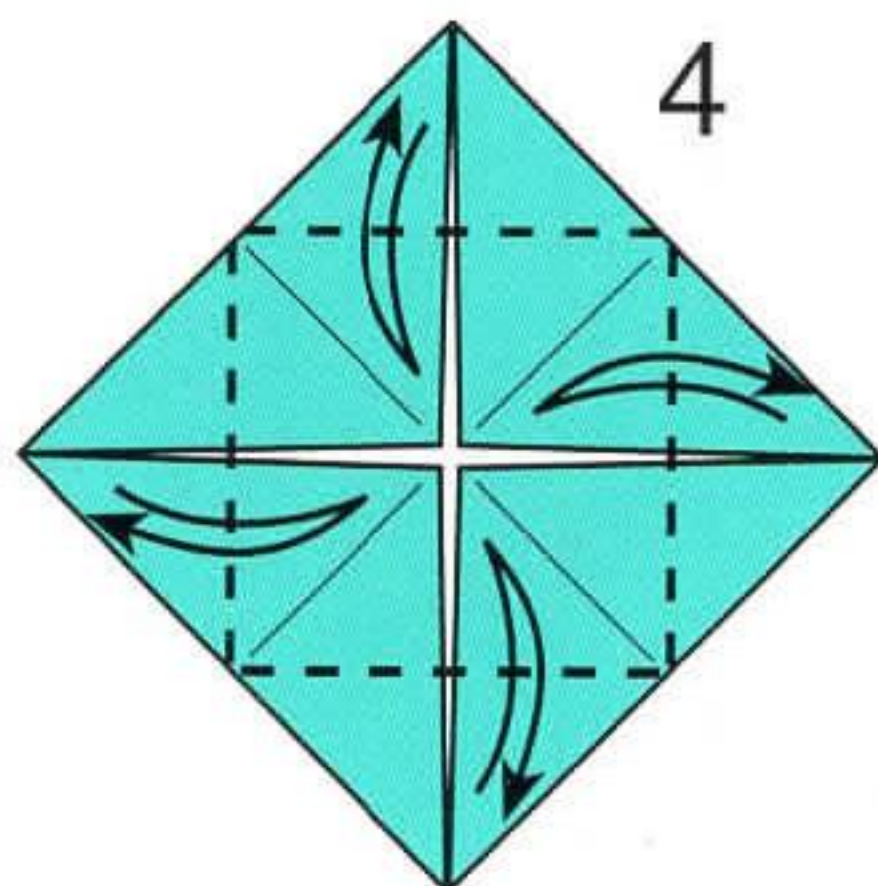
1



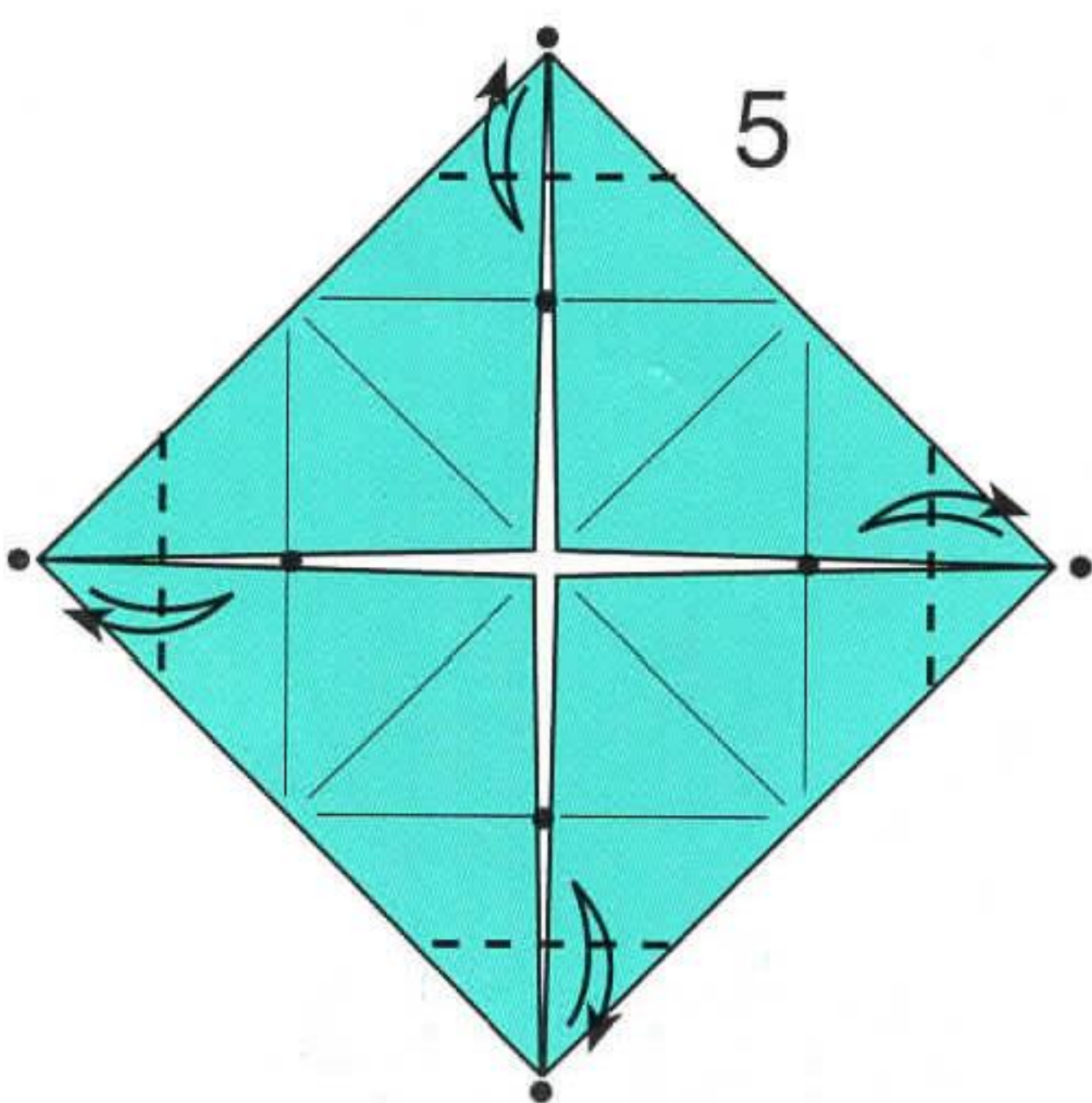
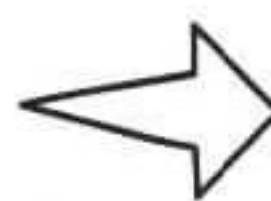
2



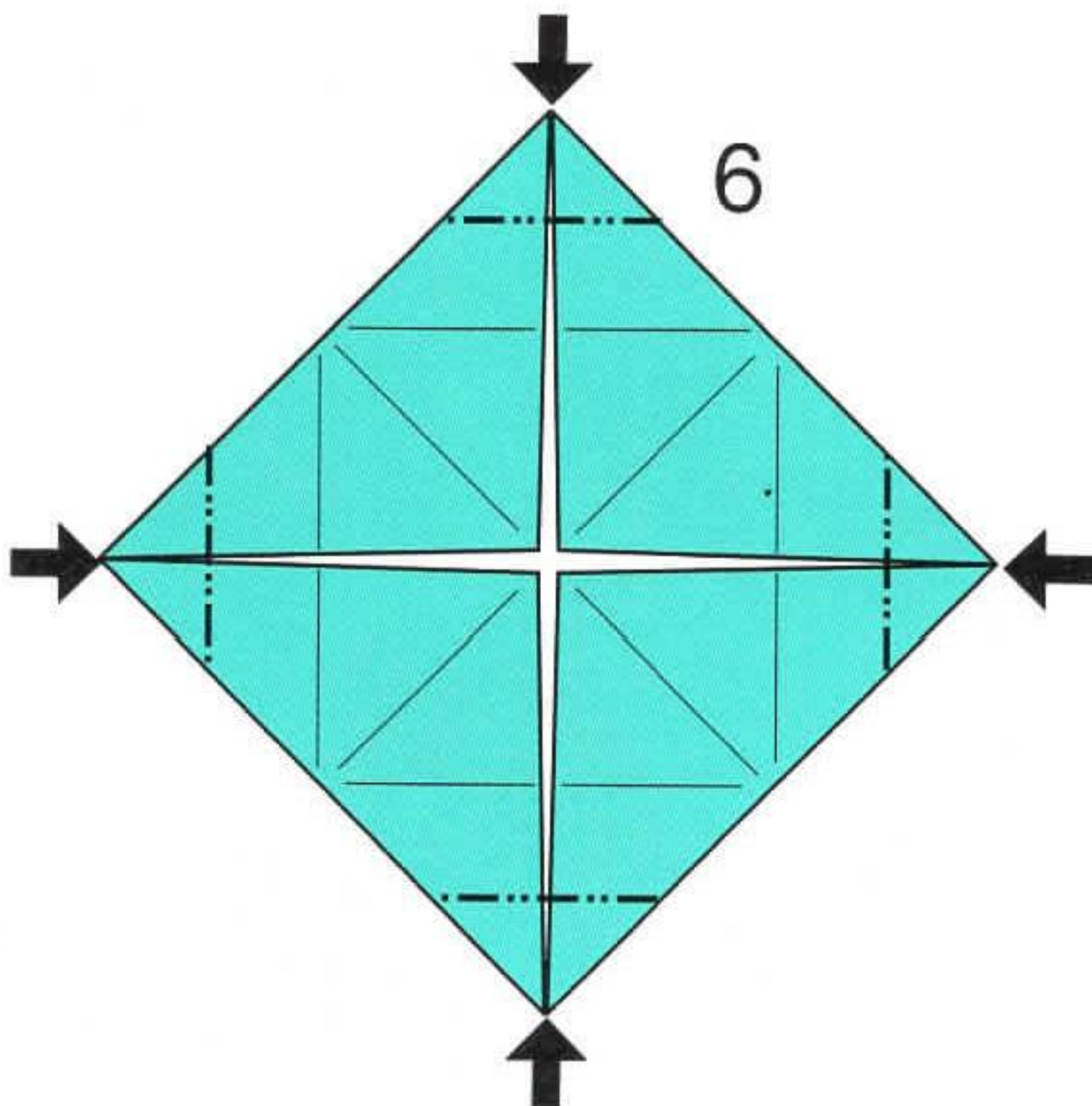
3



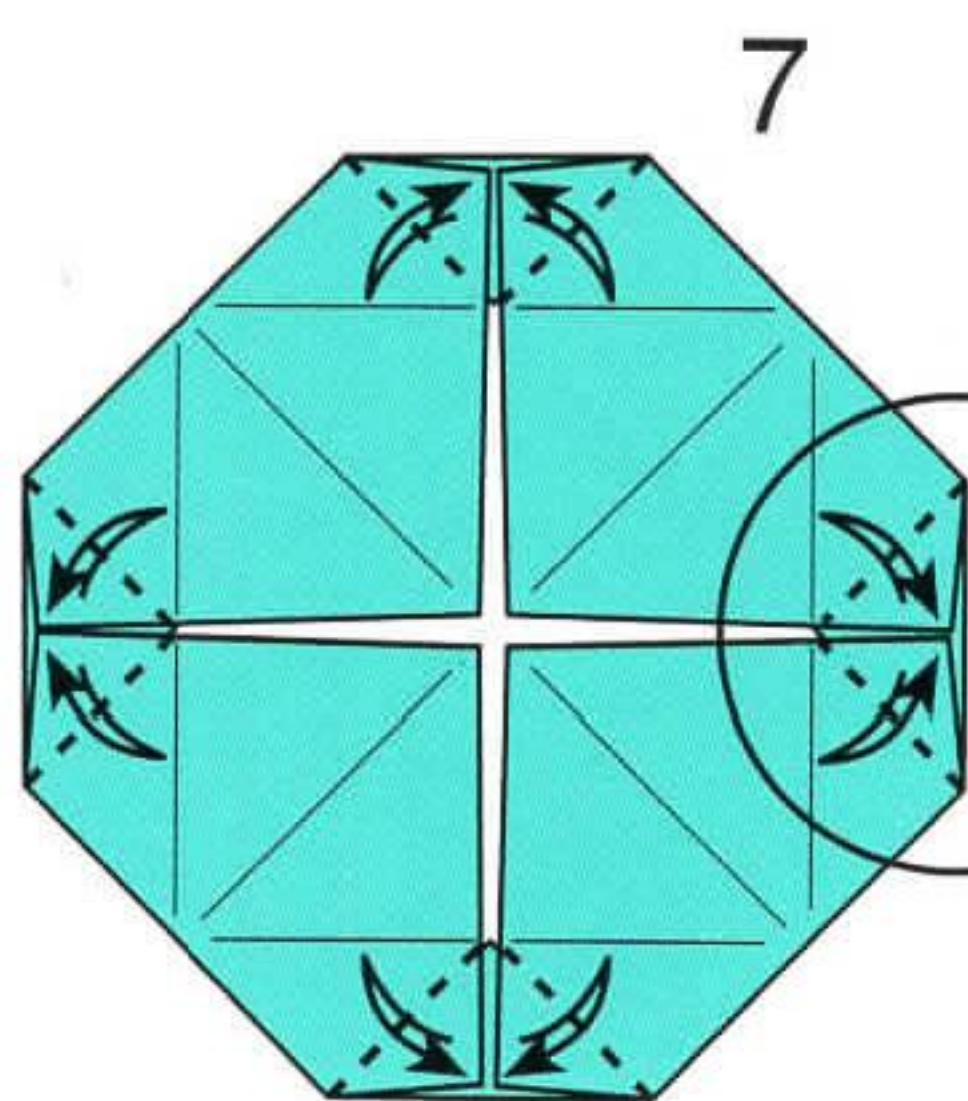
4



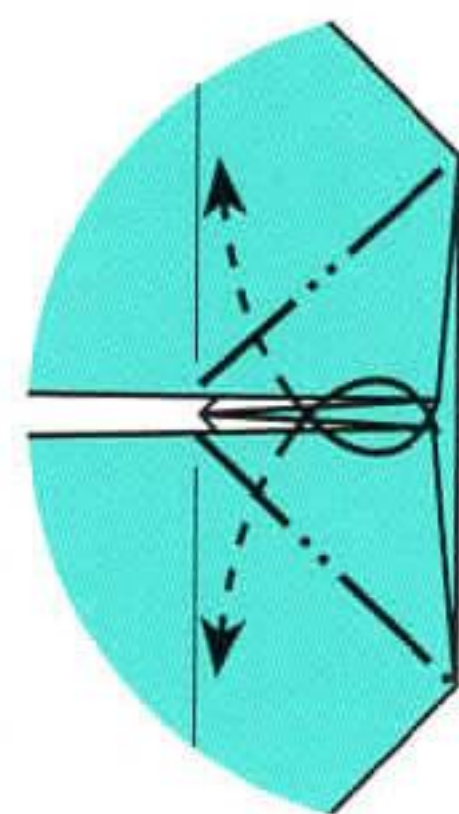
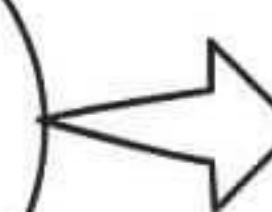
5



6

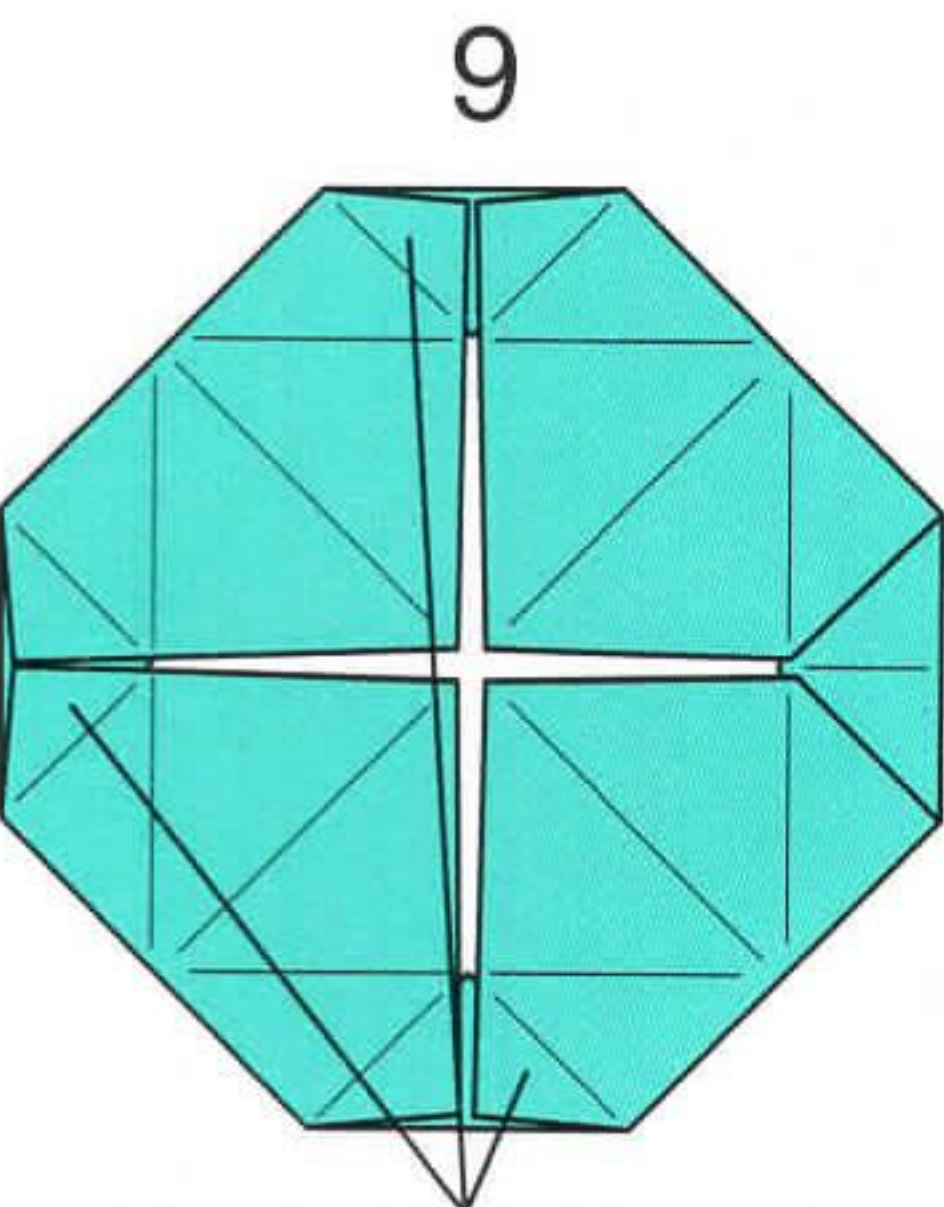


7

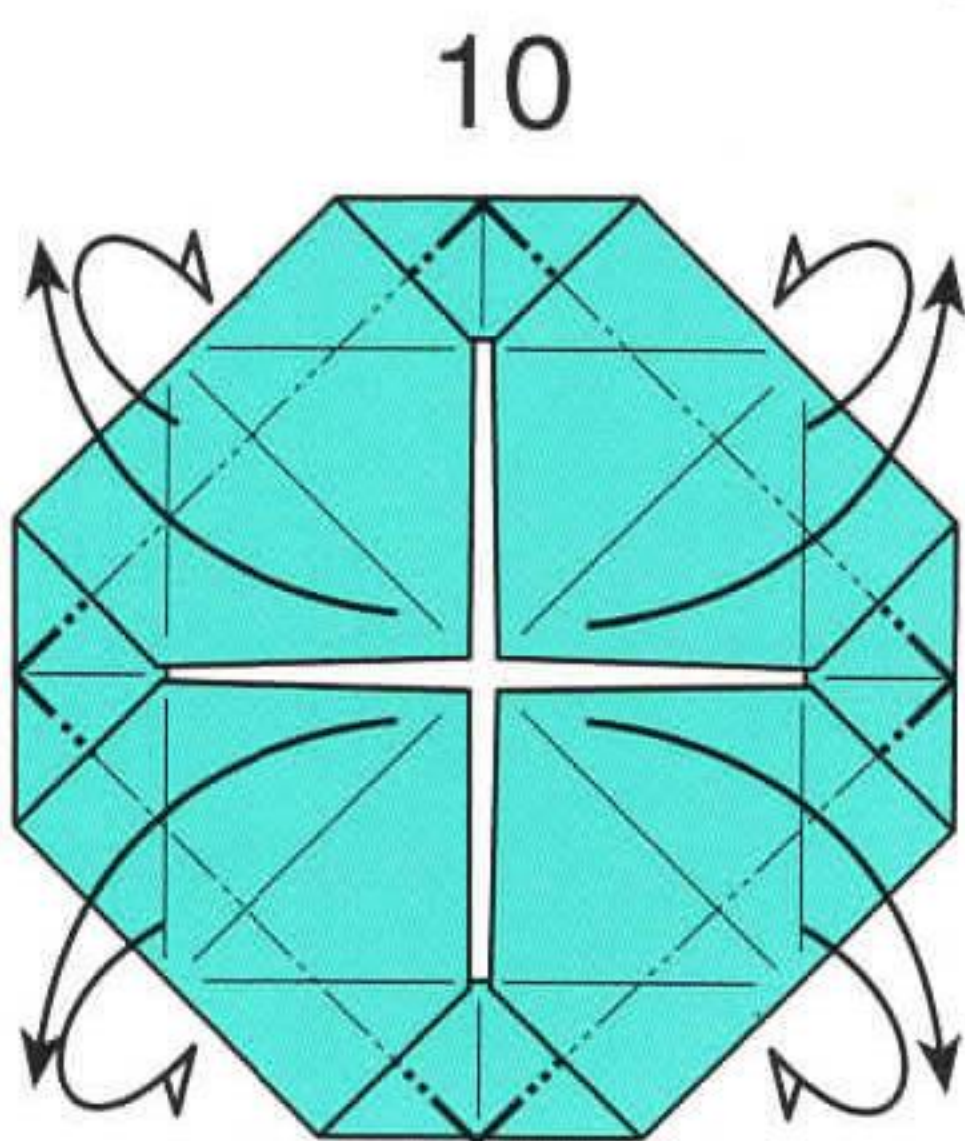


8

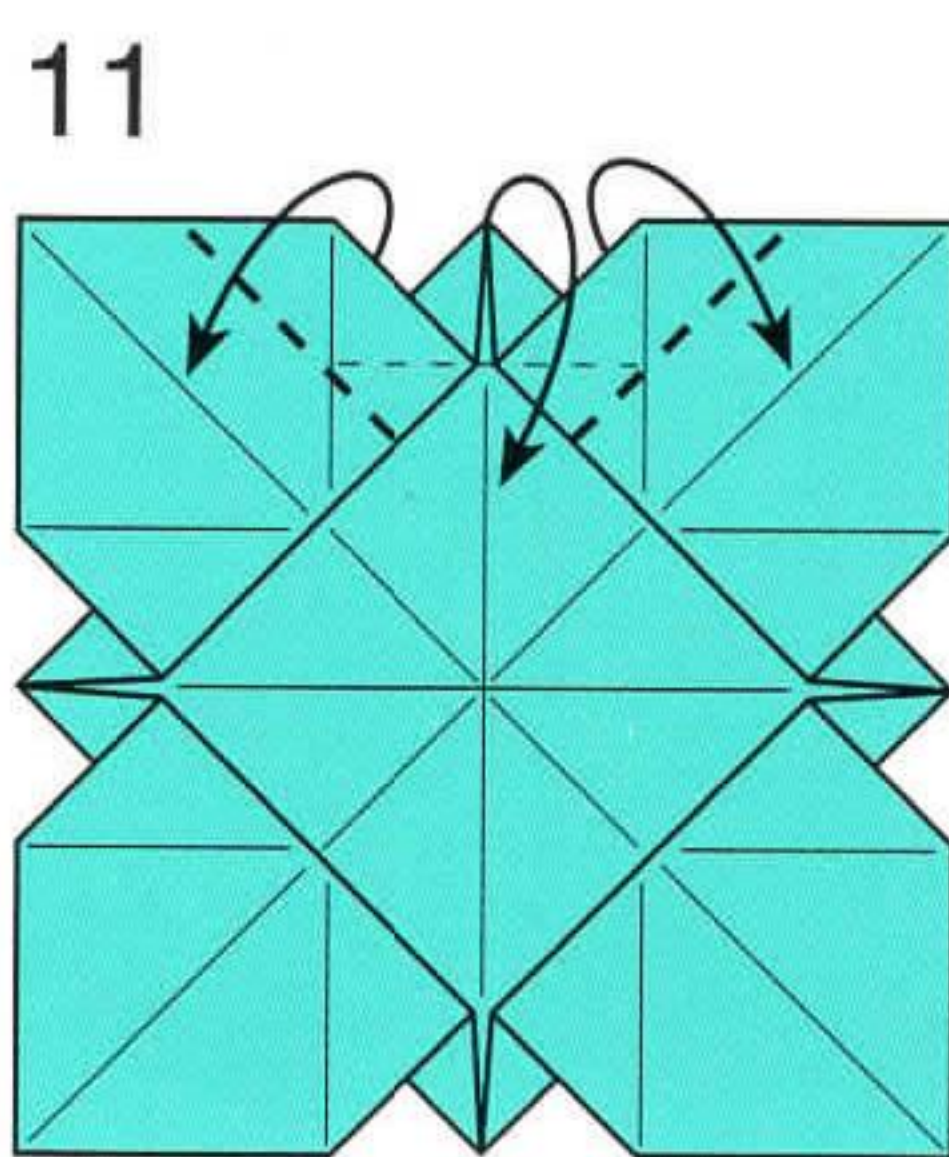
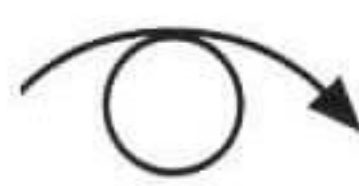
Inside reverse-fold



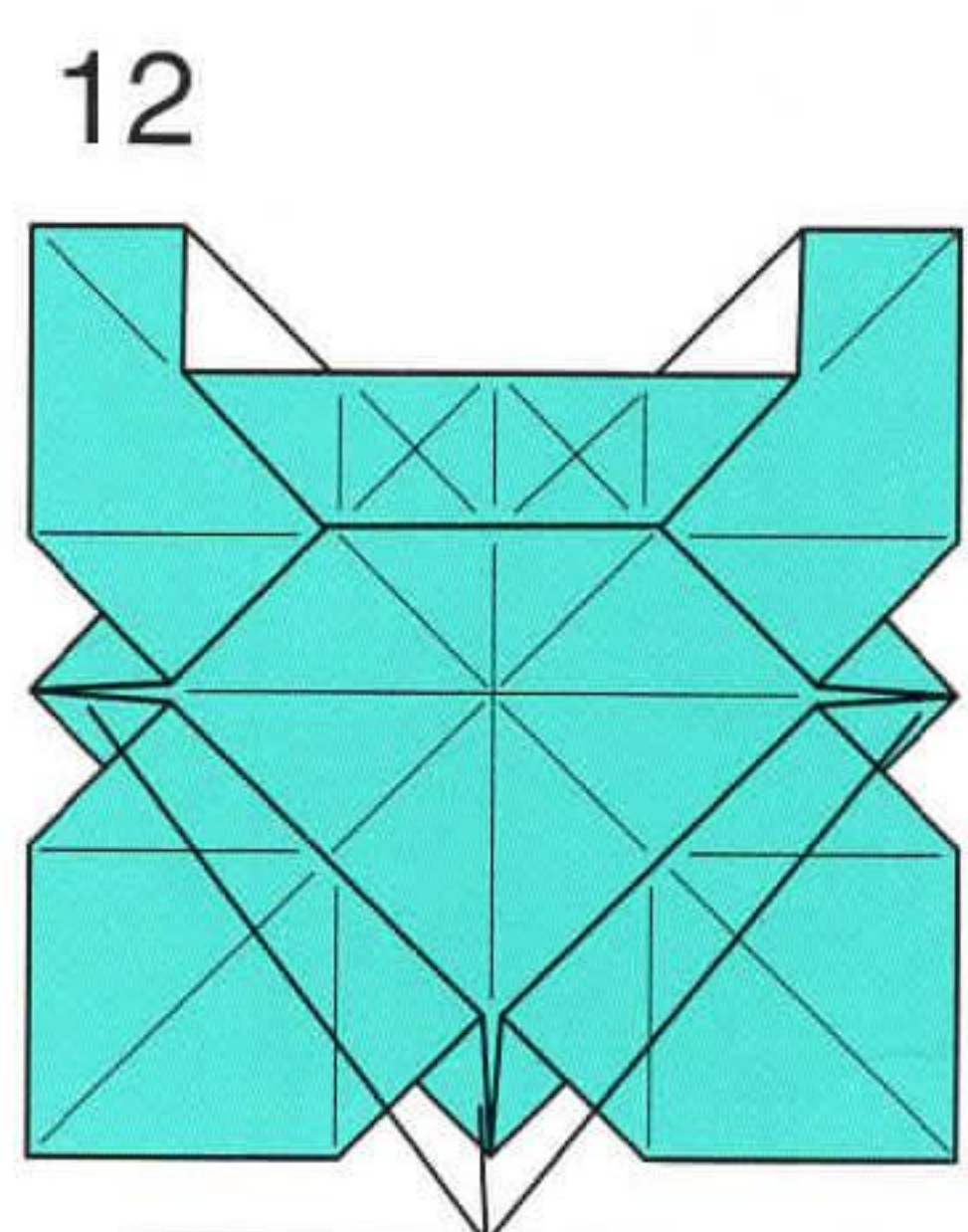
9



10



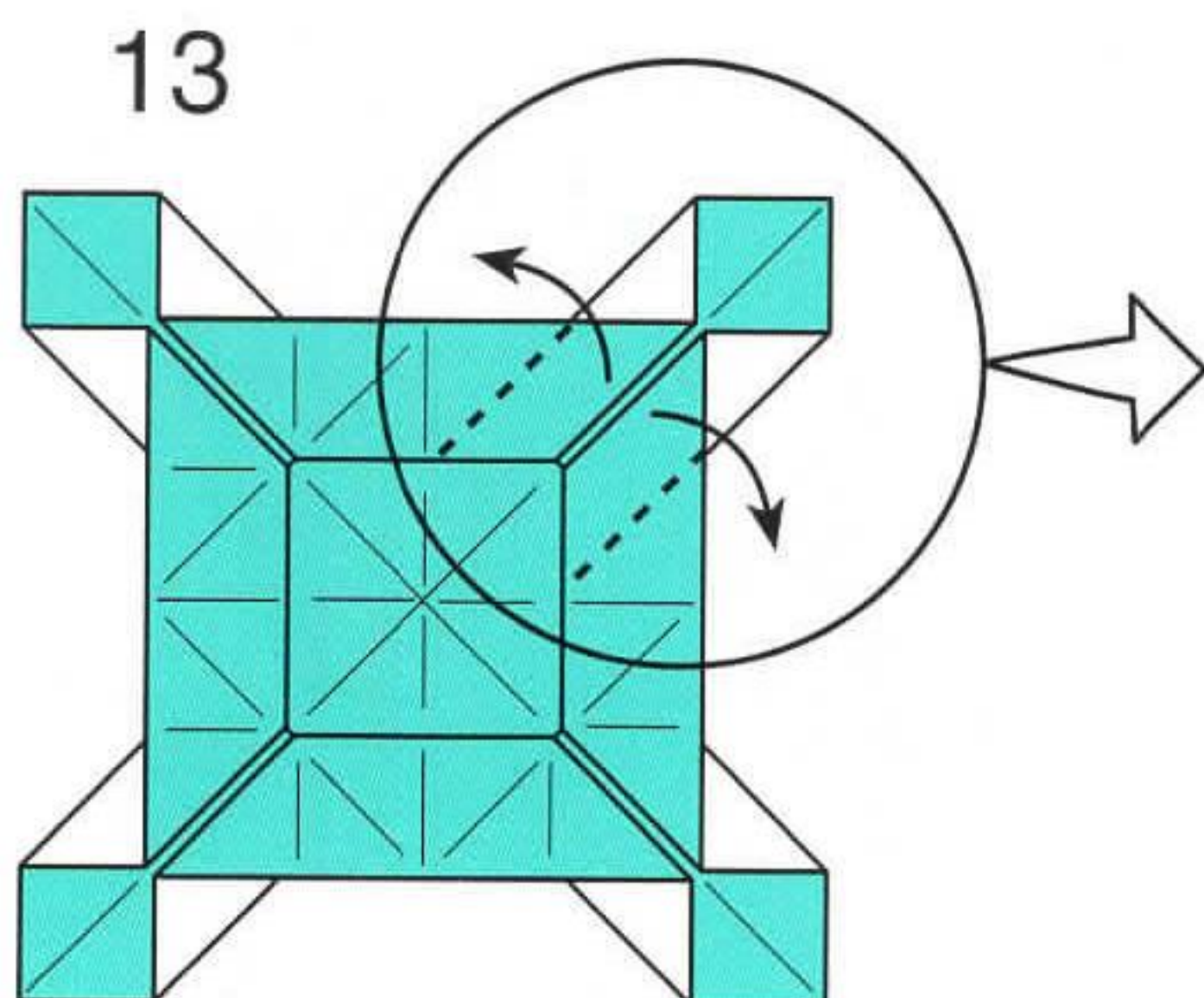
11



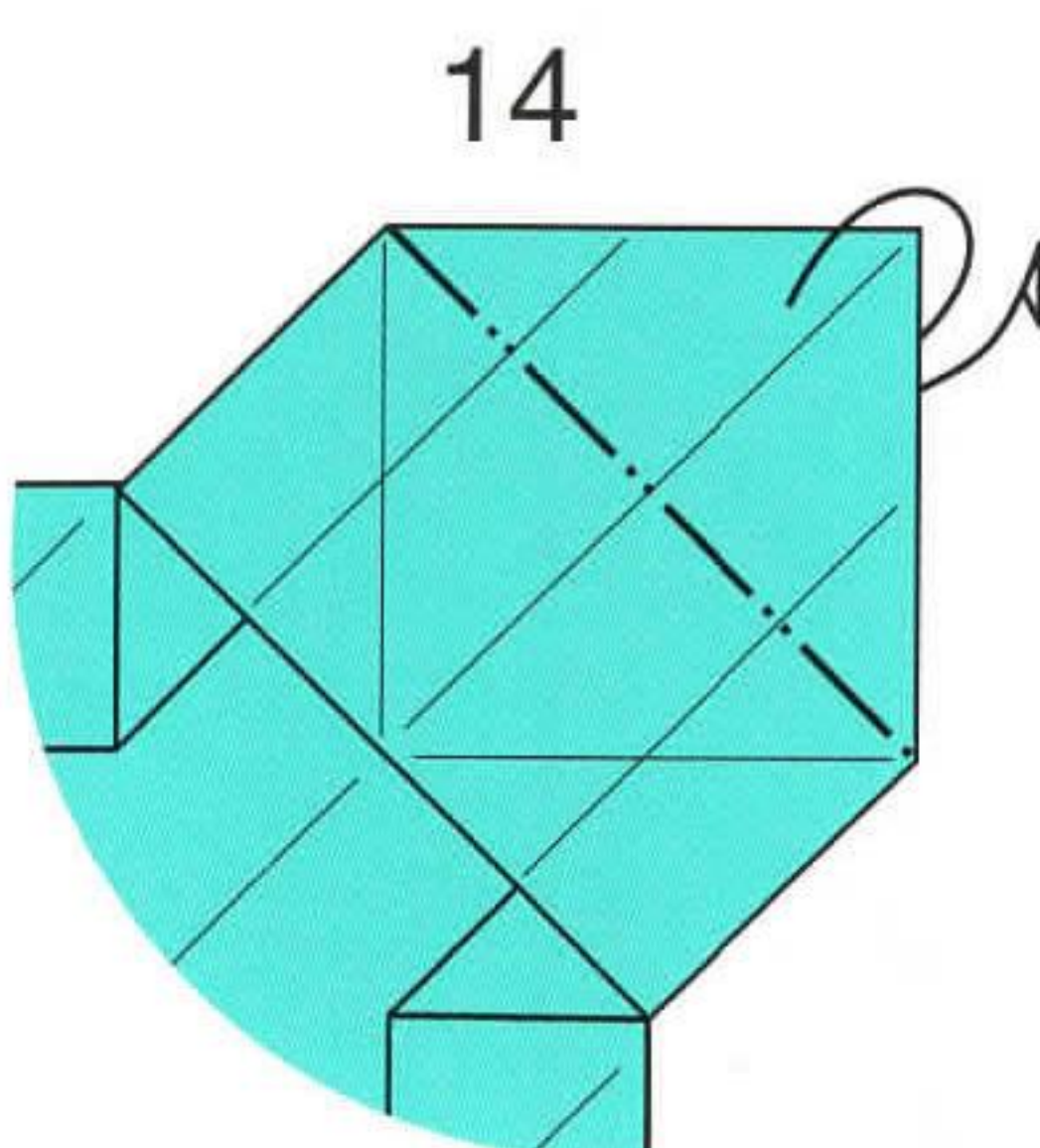
12

Repeat step 8.

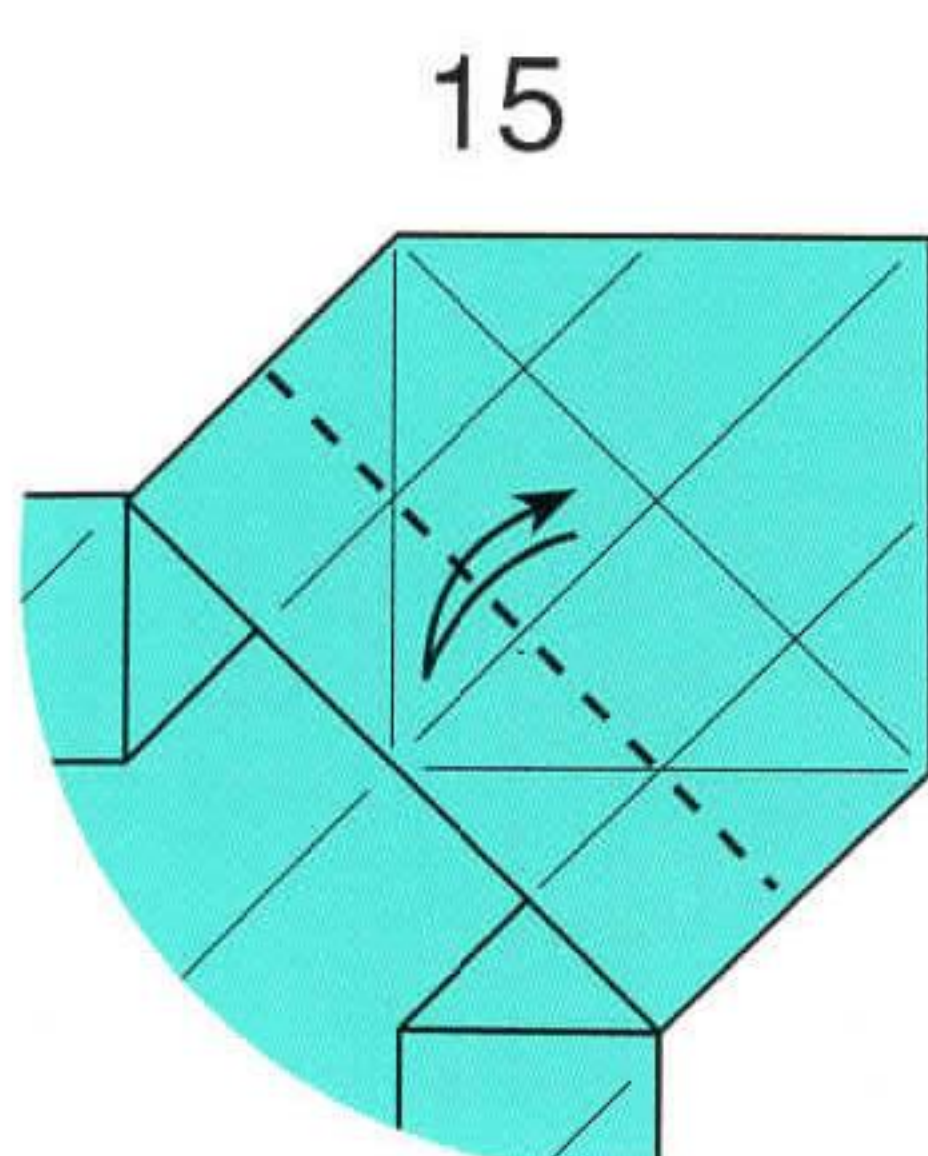
Repeat step 11.



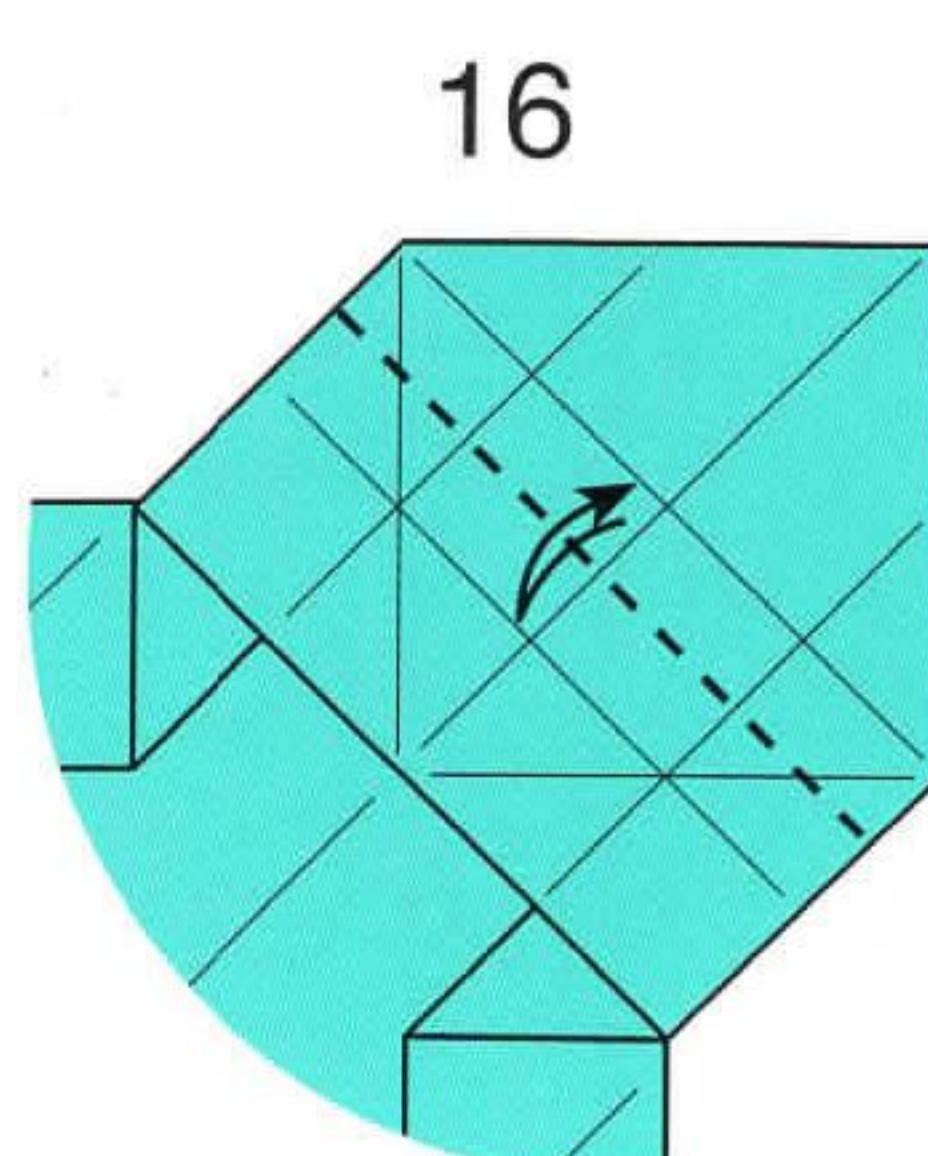
13



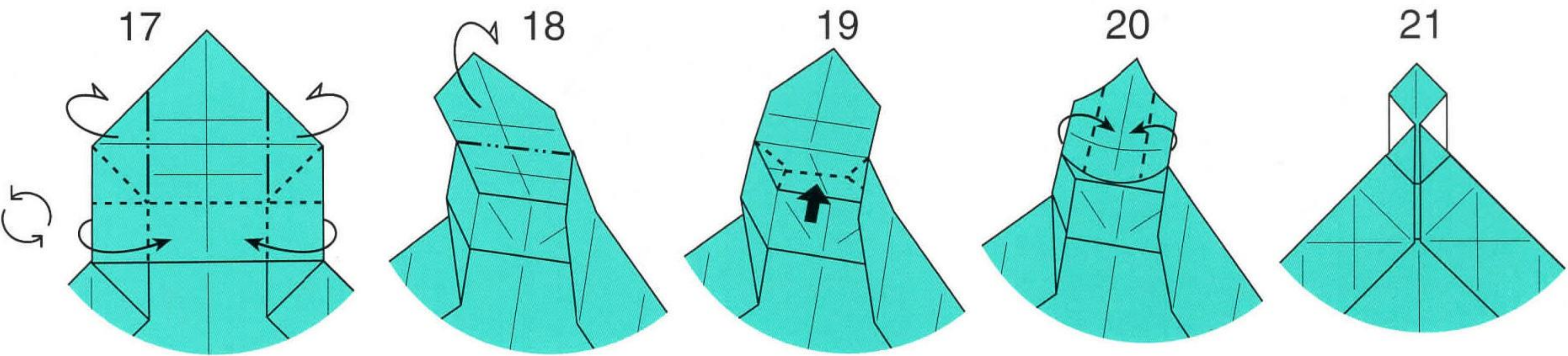
14



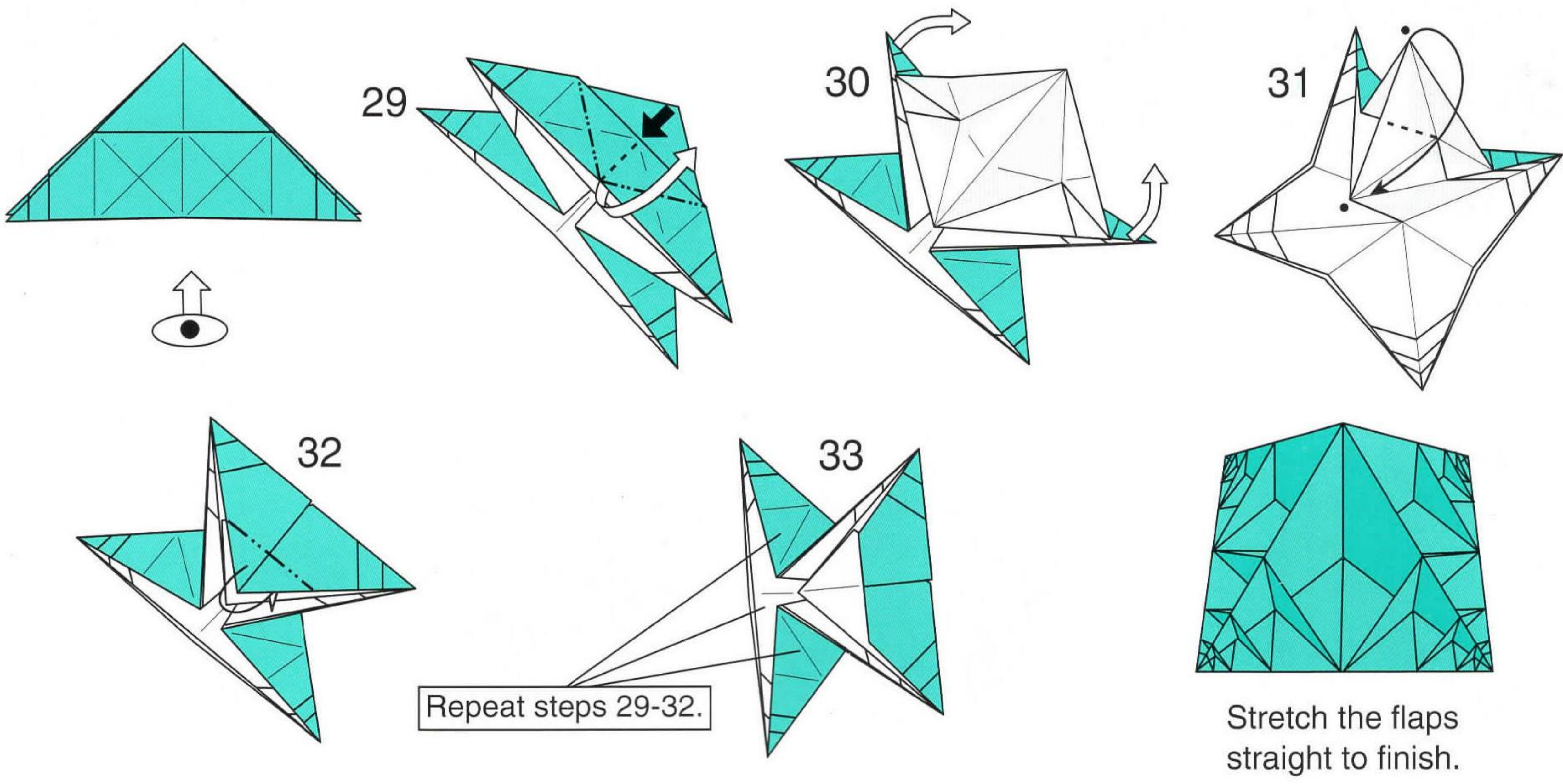
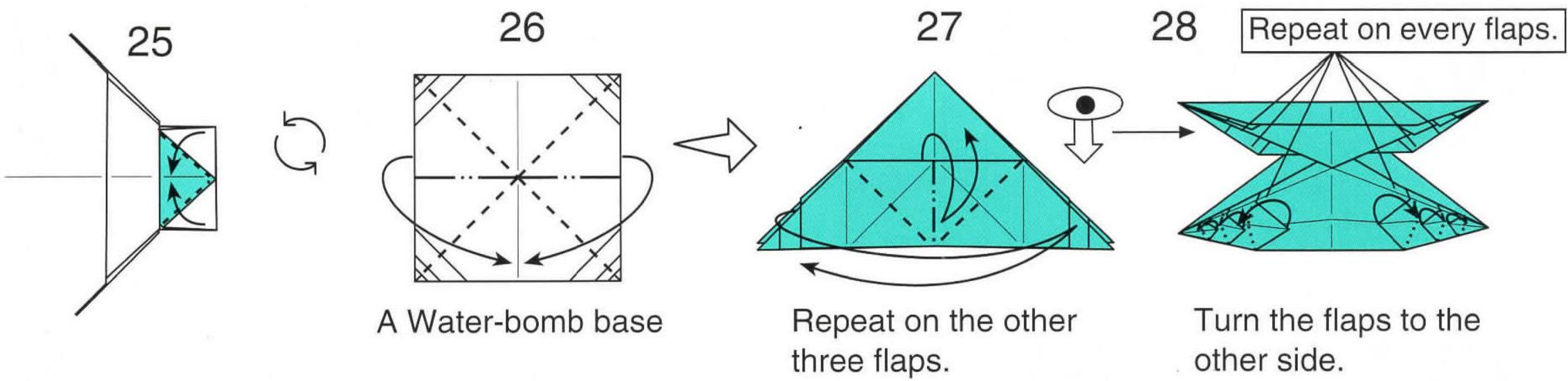
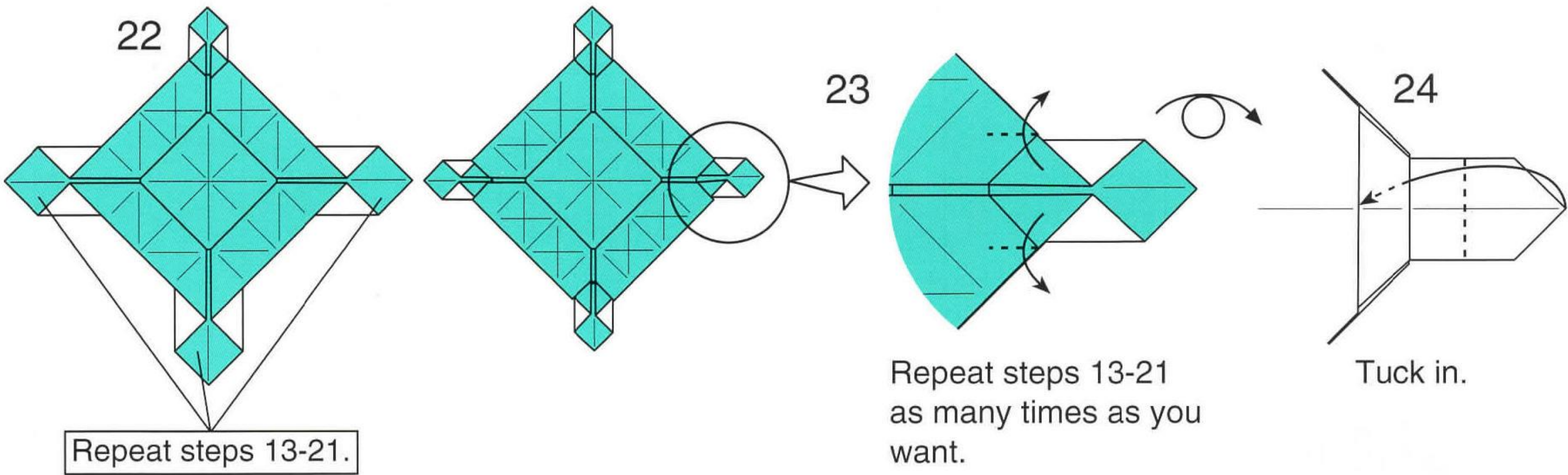
15



16

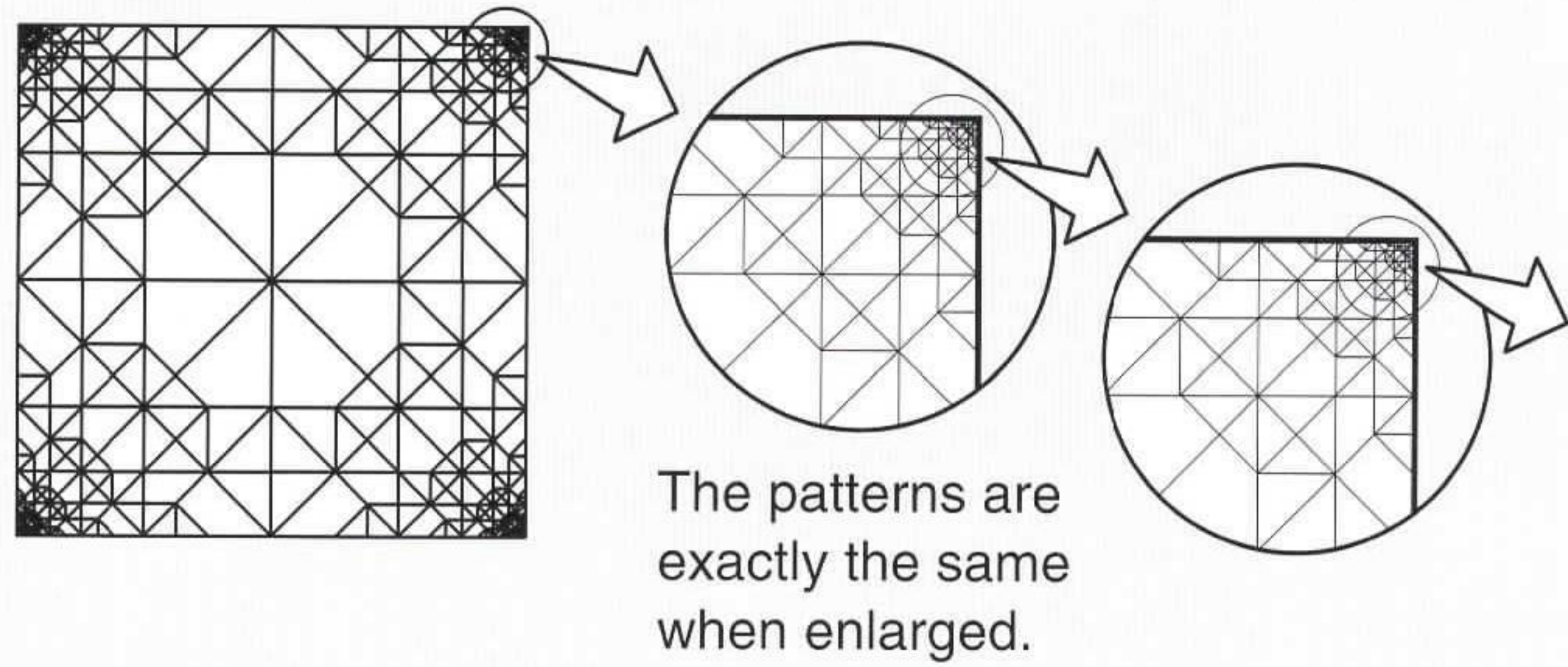


Form a box-like shape.



Folding infinitely

This model Pyramid consists of four similar patterns, each one consisted by smaller and smaller triangular plates converging to one point. Though it may look like branches of a tree, no branch has a sub-branch, unlike *Turkey* that is introduced later.



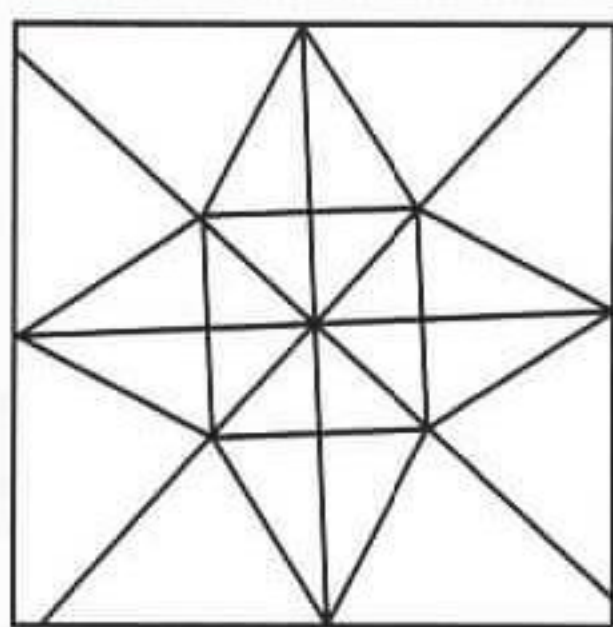
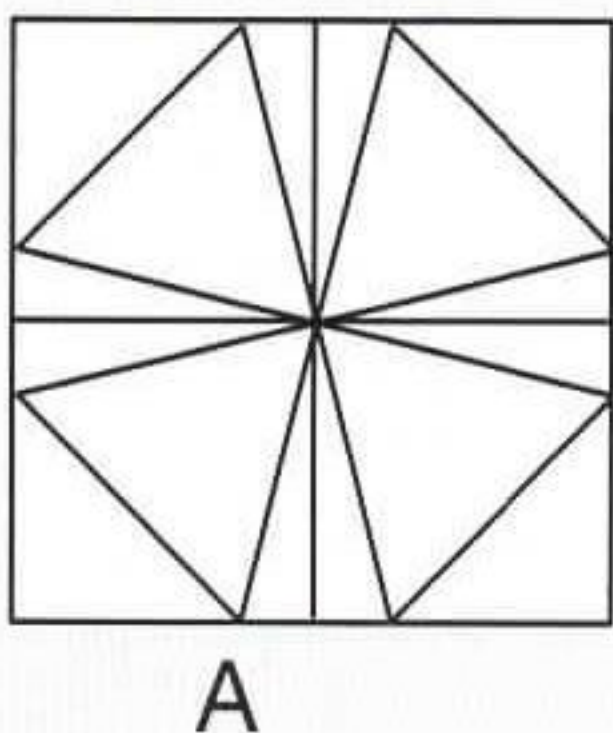
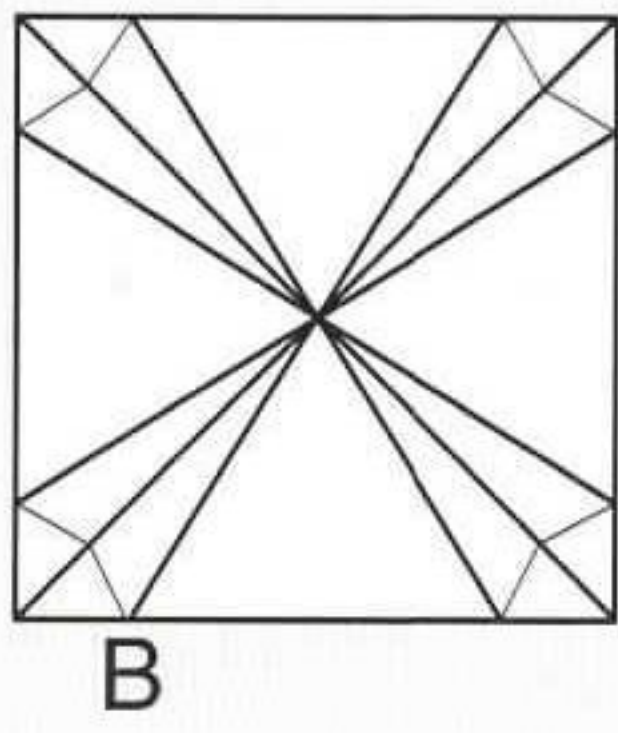
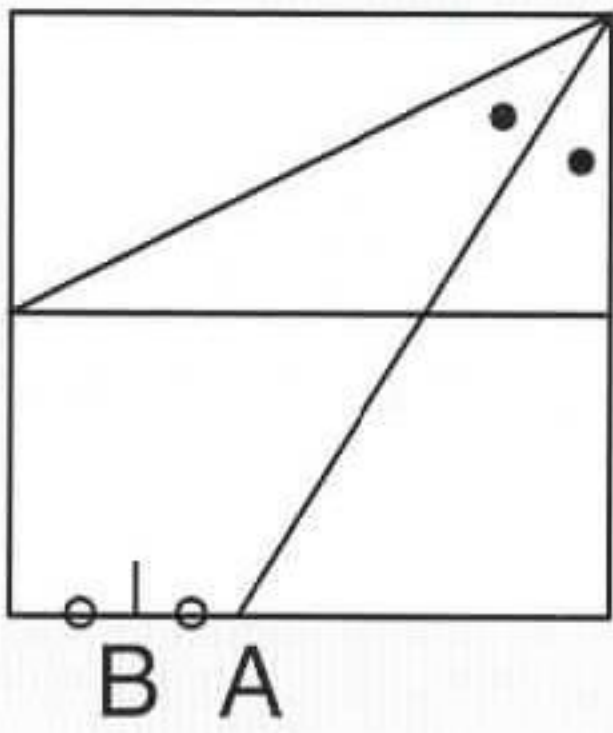
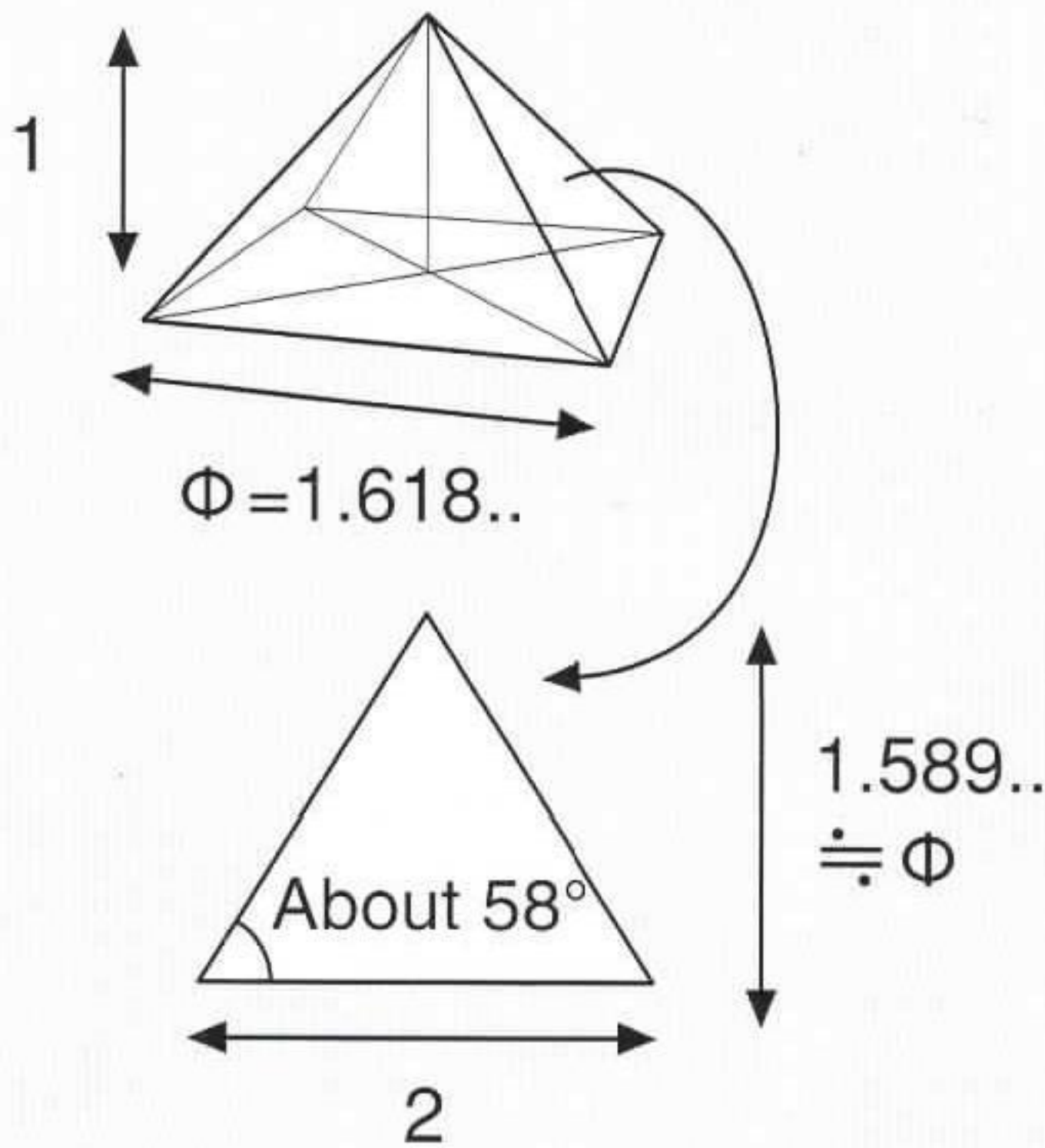
Ushio Ikegami extended this model and achieved a crease pattern that branches both infinitely and recursively. Its structure is highly complex but very interesting.

Folding a mathematically-correct pyramid

In the real pyramids in Giza, the ratio of the height to the base is said to be 1 : 1.618... or the golden ratio. On the other hand, the ratio in this model, where the sides are equilateral triangles, is 1.414... or $\sqrt{2}$, which is slightly different from “true pyramid.”

Interestingly, if the ratio of the base to the height in a square pyramid is the golden ratio, the ratio in the side is 2 : 1.589..., which is nearly equal to the golden ratio.

I found an article “Folding true pyramids” in my own old design notes, where I assumed that the ratio of the base to the height in the side should be 2 to the golden ratio. Some sketches from the article are shown below.



Two types of pyramid without the bottom

A pyramid with the bottom, folded from a rotated Water-bomb base

If folded from a regular Water-bomb base, the vertex angle of each triangle will be greater than 60°, and there will be folded edges on the sides. But the difference can be ignored in practice.

This concludes Intermediate Models.

The next chapter is Complex Models. The models are difficult to fold just because they have detailed folds and many steps. That does not mean simpler models have lower qualities.

As I said at the end of Simple Models, there is no definitive standard for complexity levels in origami. But it is true that the models in Complex Models have a lot more detailed folds. Still, those who have completed the models in this chapter should be ready to fold them without difficulty.



Chick

Theme: Deltahedron

This model is based on one type of deltahedron, a polyhedron whose faces are equilateral triangles, called triangular dipyrmaid.



Peacock

Theme: Miura-ori; Tessellation

The pattern for the tail of this model is the same as Miura-ori, a famous result of engineering of origami.



Turkey

Theme: Self-similar

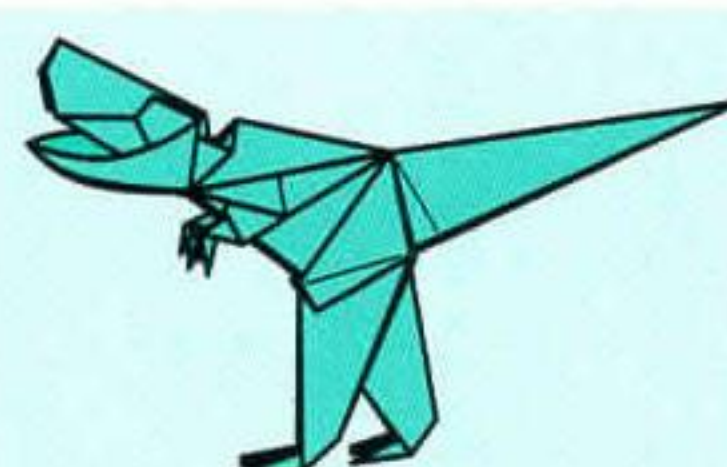
The creases in this model repeat the same pattern in a nesting structure, which relates to fractal geometry.

Chapter 5

Complex Models

“Origami is the multi-dimensional Eulerian path.”

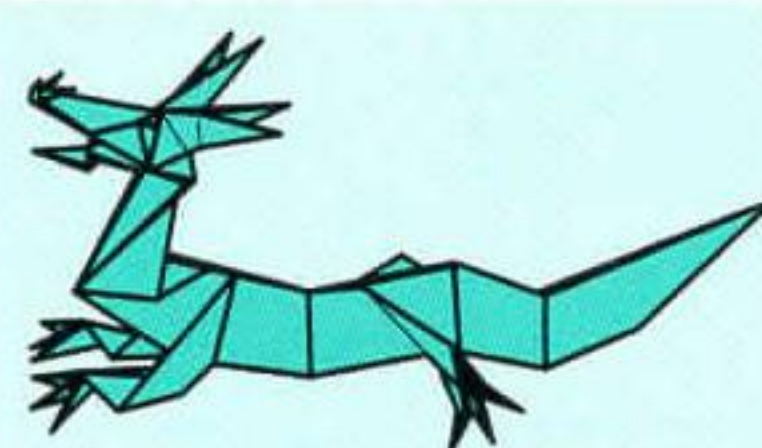
M. J.



Tyrannosaurus

Theme: Realism

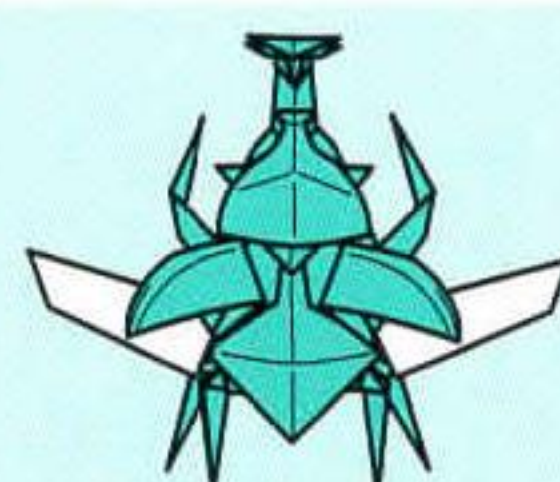
One of the main incentives for origami design is the challenge to realistic illustration.



Eastern Dragon

Theme: Grafting

Explains grafting, or adding new elements to an existing model, using the design of claws of this model as a typical example.



Samurai Helmet Beetle

Theme: No glue, no cuts

Examines the “no glue” rule, one of the basic rules often applied to origami.



Devil

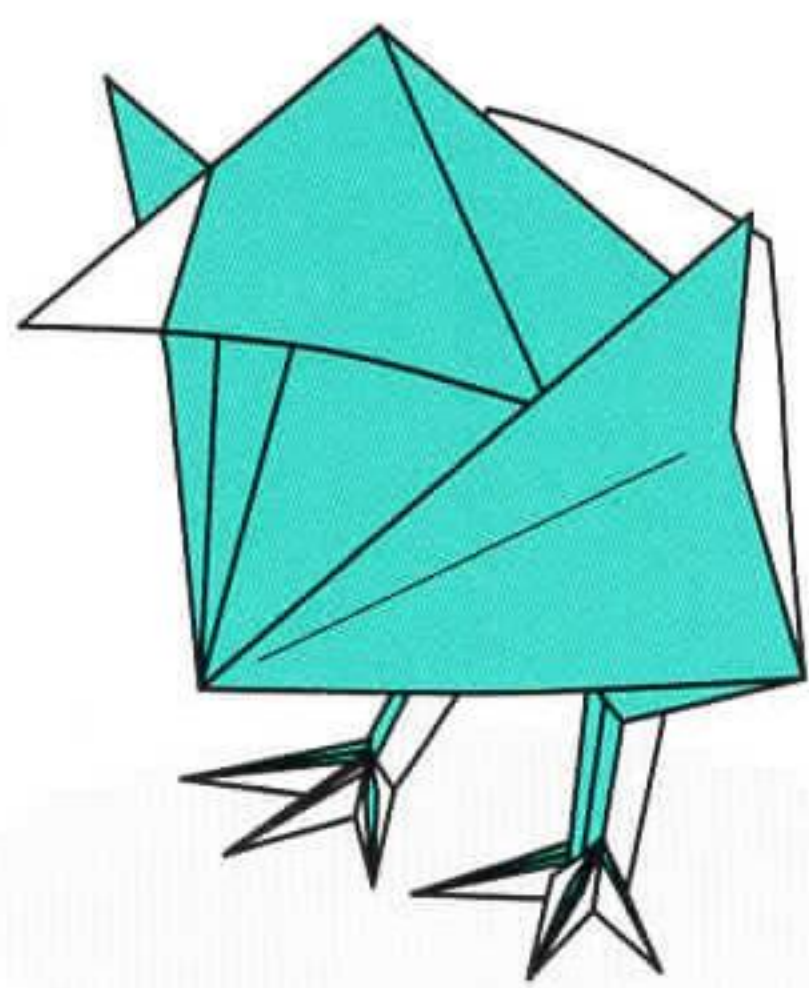
Theme: Taming the devil

Introduces my first-ever published and representative model to conclude this book.

Chick

Theme: Deltahedron

Fold using 6" (15 cm) origami paper.

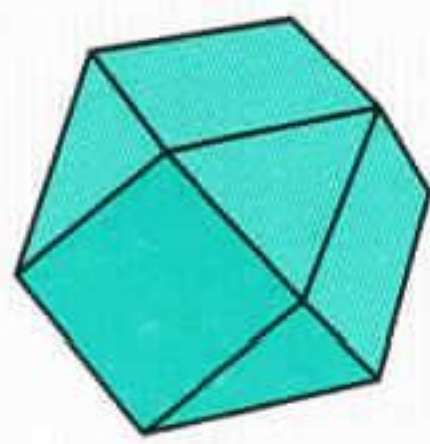


This design came from an image of an egg with legs and a head.

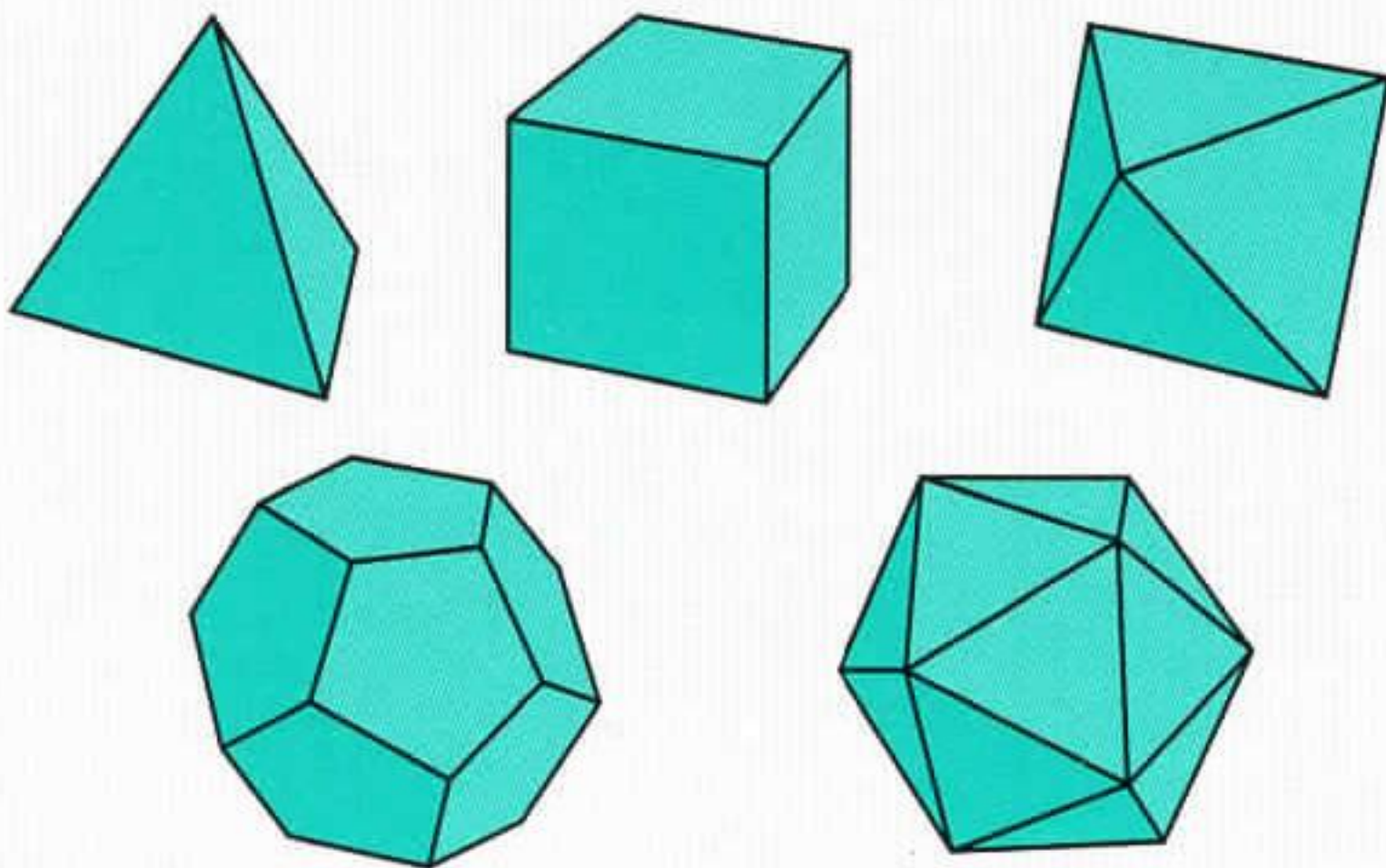
To realize the oval shape, I used one type of deltahedron called triangular dipyramid as its base.

Regular polyhedron and deltahedron

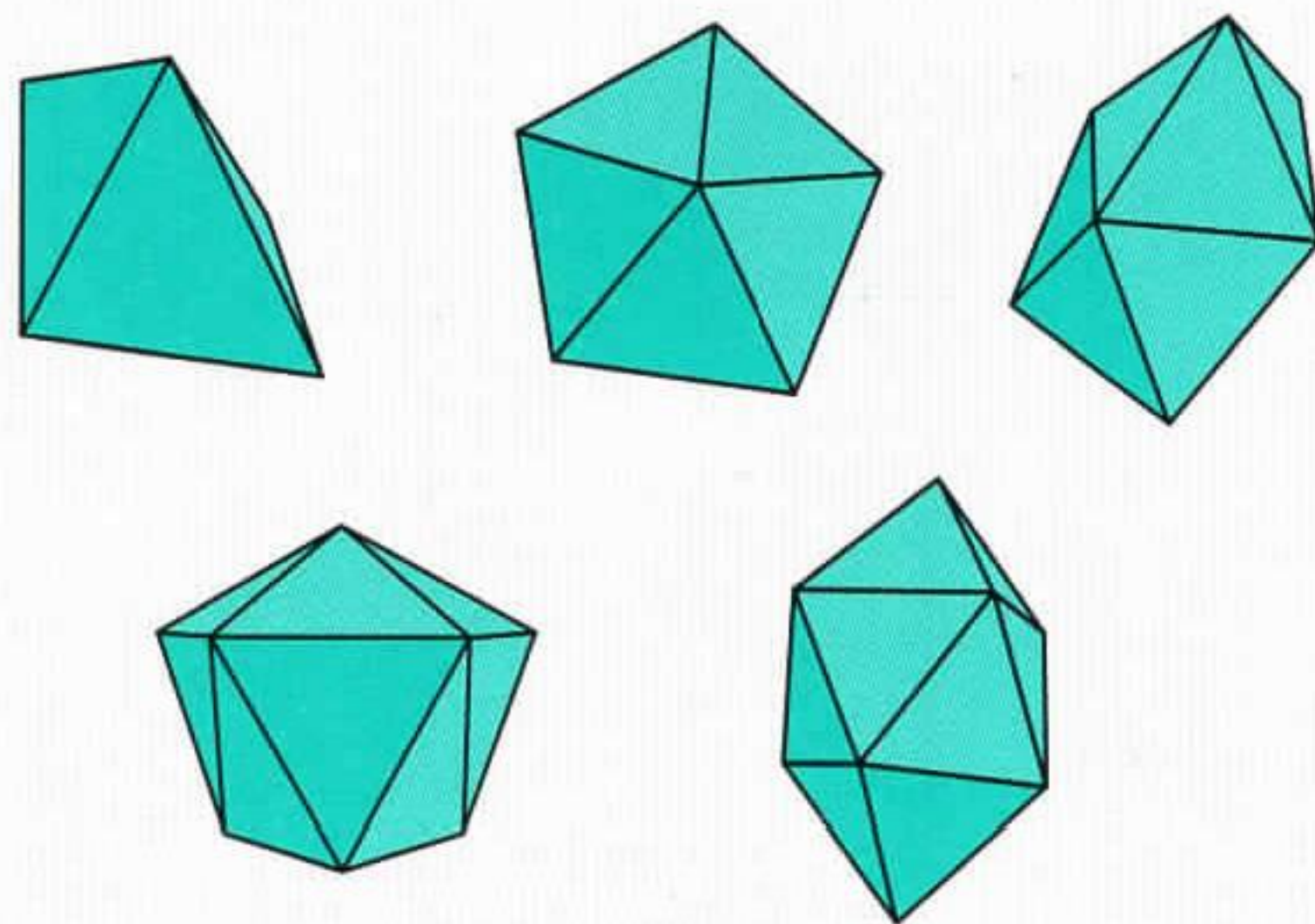
A regular polyhedron is a polyhedron whose faces are congruent regular polygons and whose corners are inscribed in a sphere. There are only five types of regular polyhedron, the tetrahedron, the hexahedron (or the cube), the octahedron, the dodecahedron, and the icosahedron. Among them, the tetrahedron, the octahedron, and the icosahedron have equilateral triangle faces. There are several other convex polyhedra (polyhedra that include in its volume any line connecting two points on its surface) whose faces are equilateral triangles. Such a polyhedron is called deltahedron. There are eight types, including three types of regular polyhedron. The number of faces is 4, 6, 8, 10, 12, 14, 16, or 20. It is interesting that there is not a deltahedron that has 18 faces.



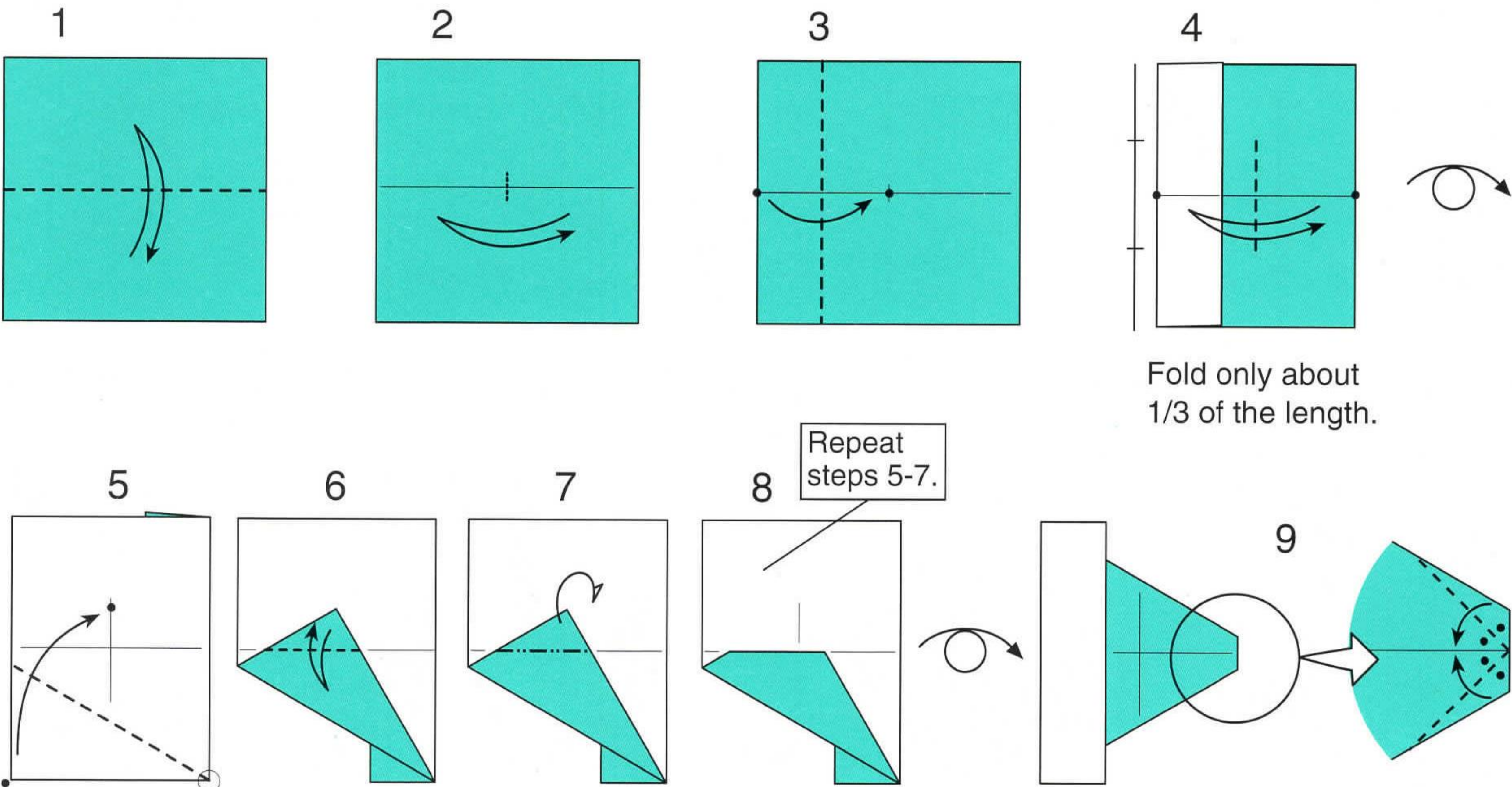
Understanding the shapes of these polyhedra and their truncated families (for example, a cuboctahedron is shown on the left) will add to some "aha effect" during the assembly of modular origami models.

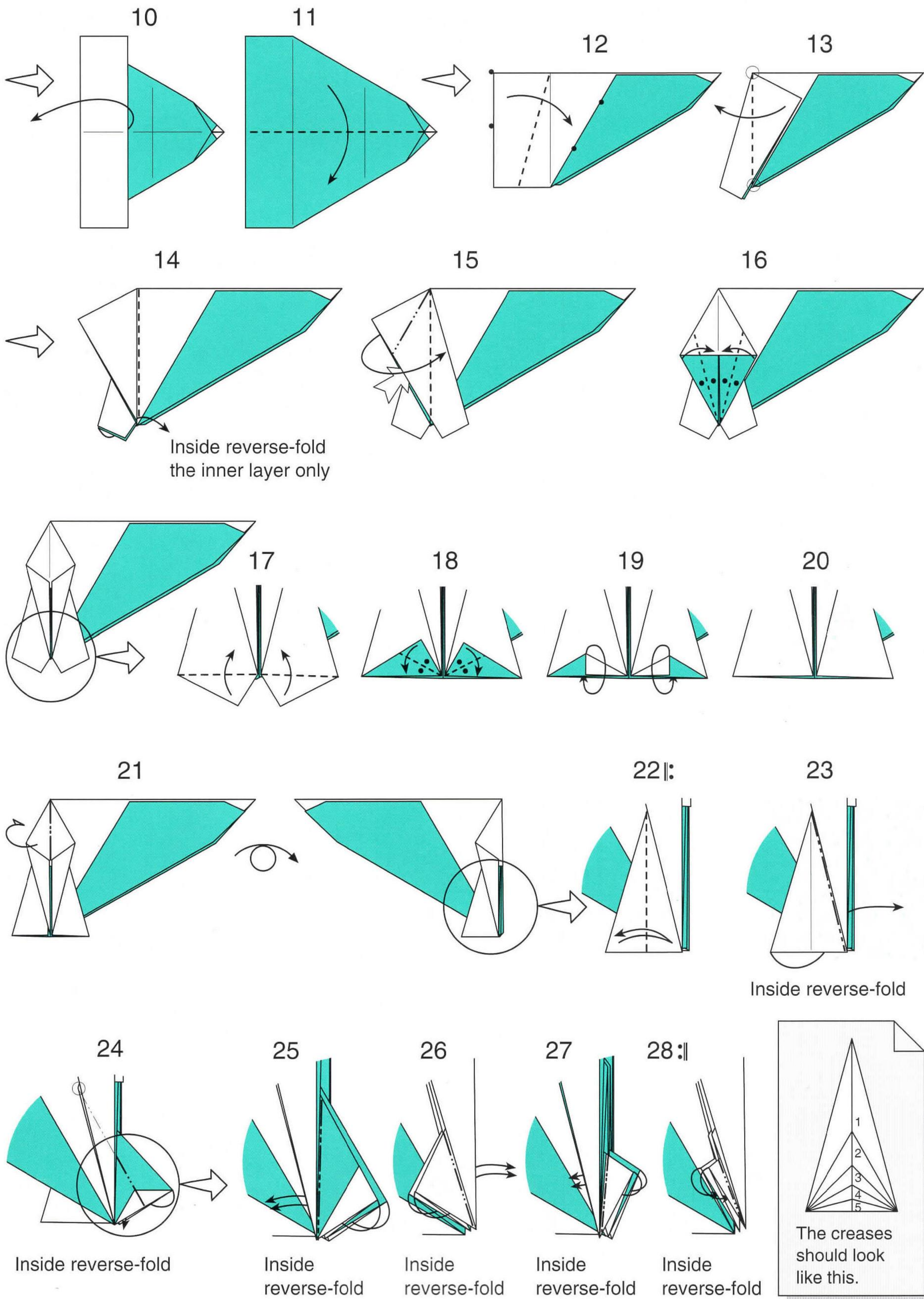


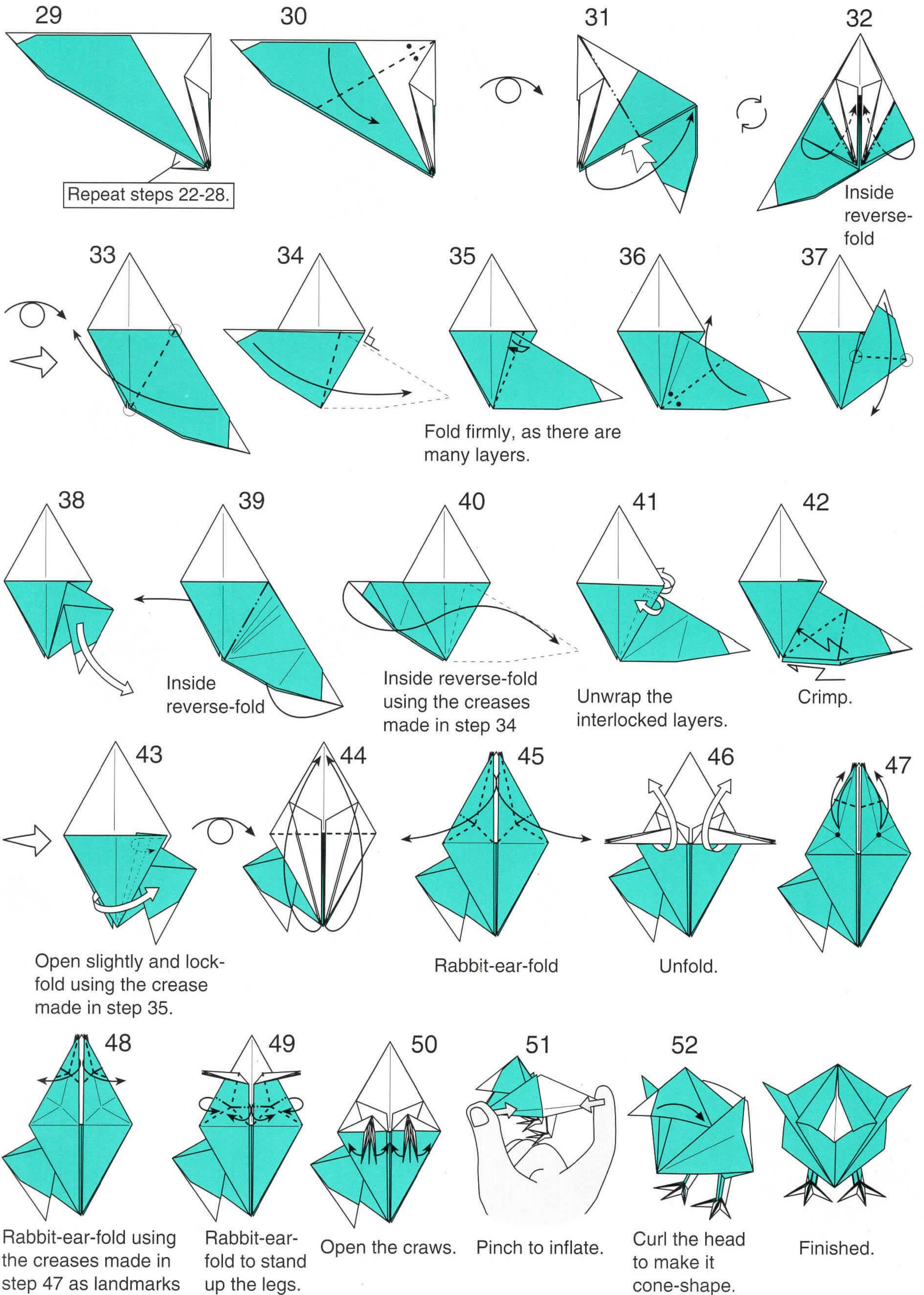
Regular polyhedra



Deltahedra



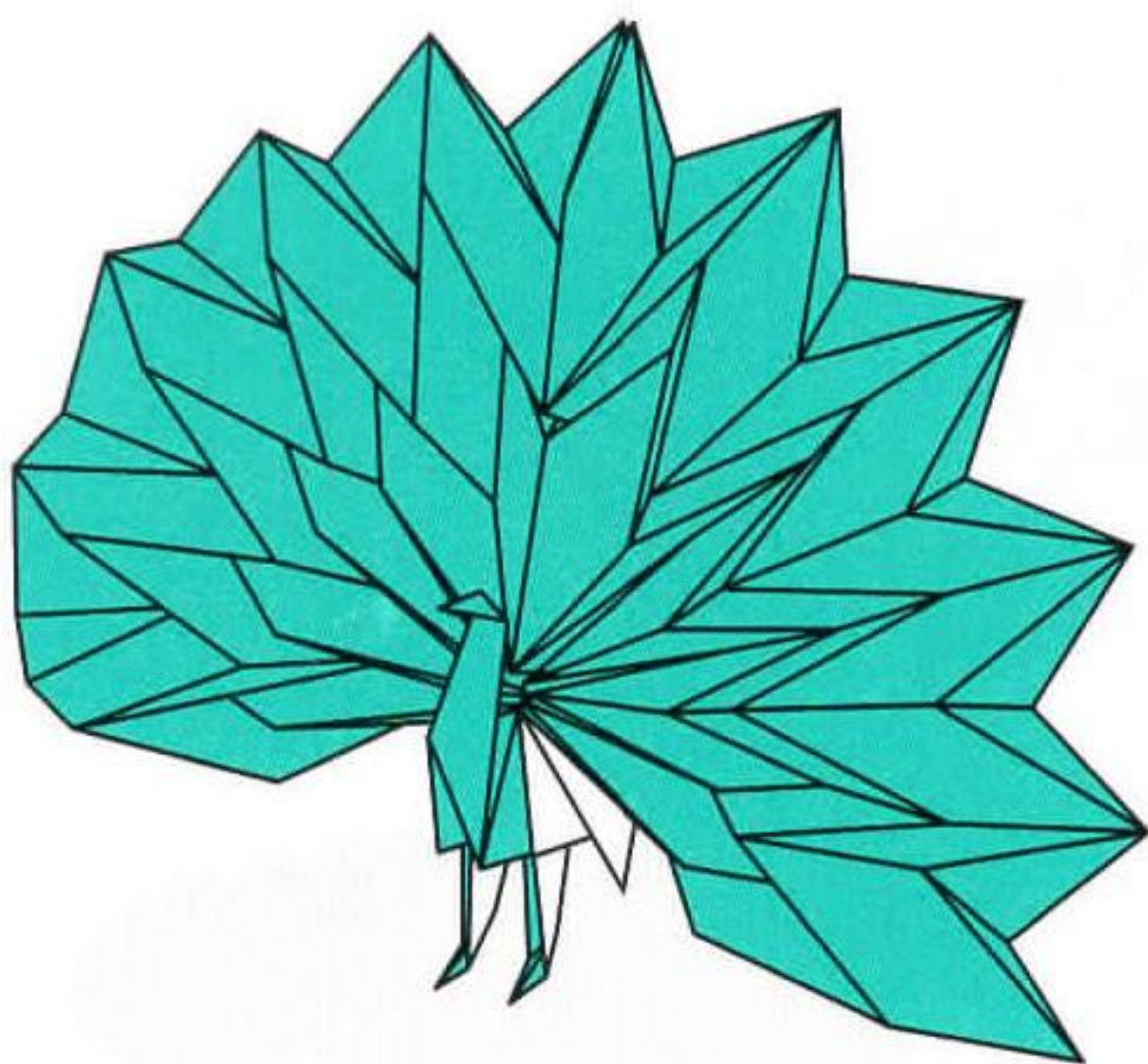




Peacock

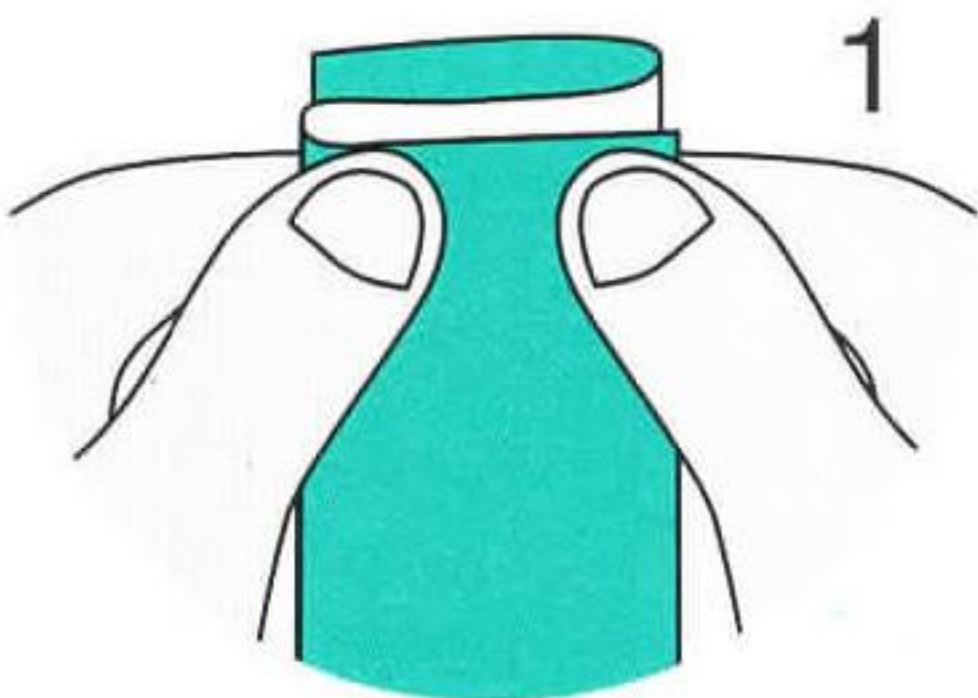
Theme: Miura-ori; Tessellation

Fold using 6" (15 cm) or preferably larger origami paper.

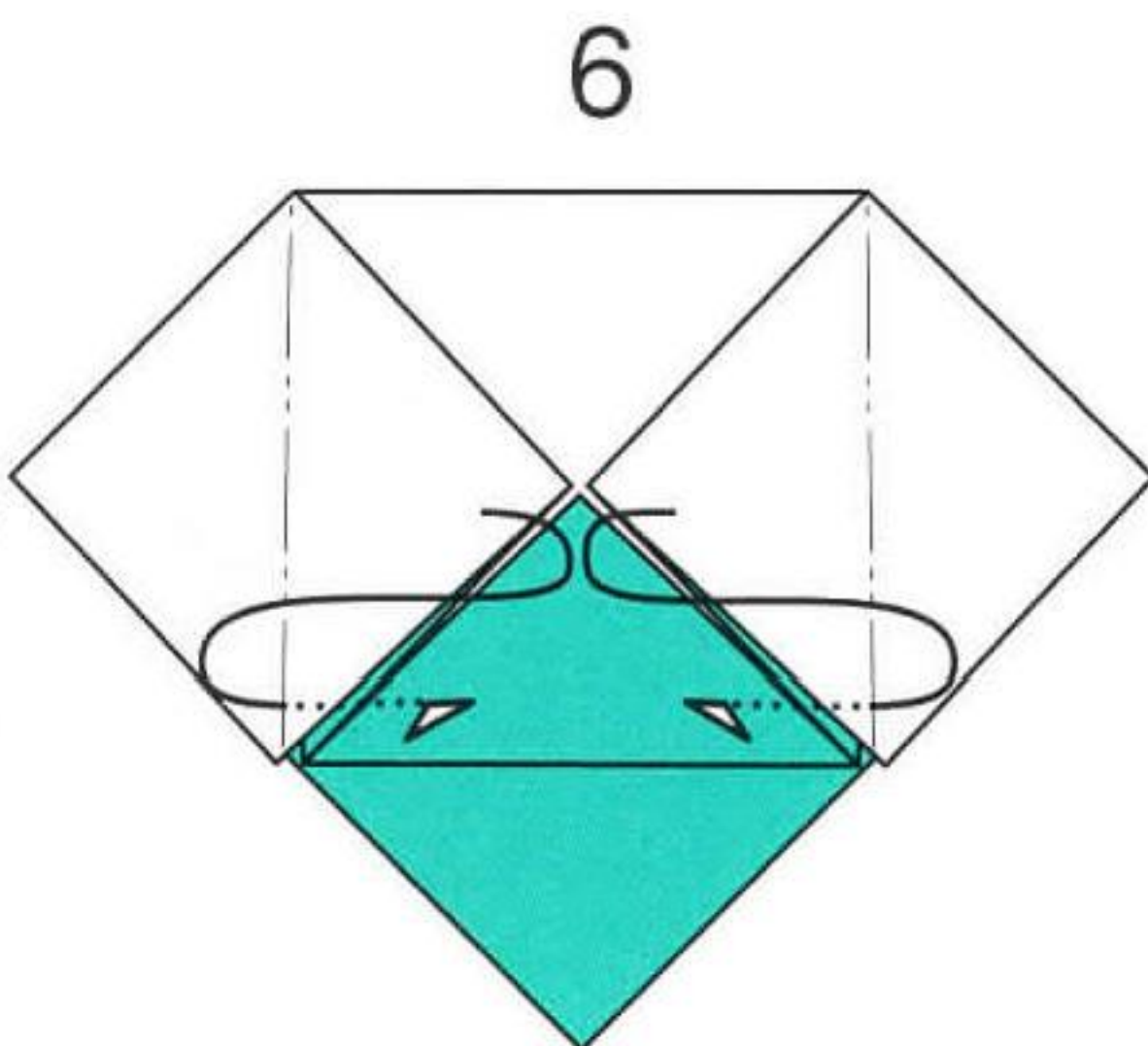
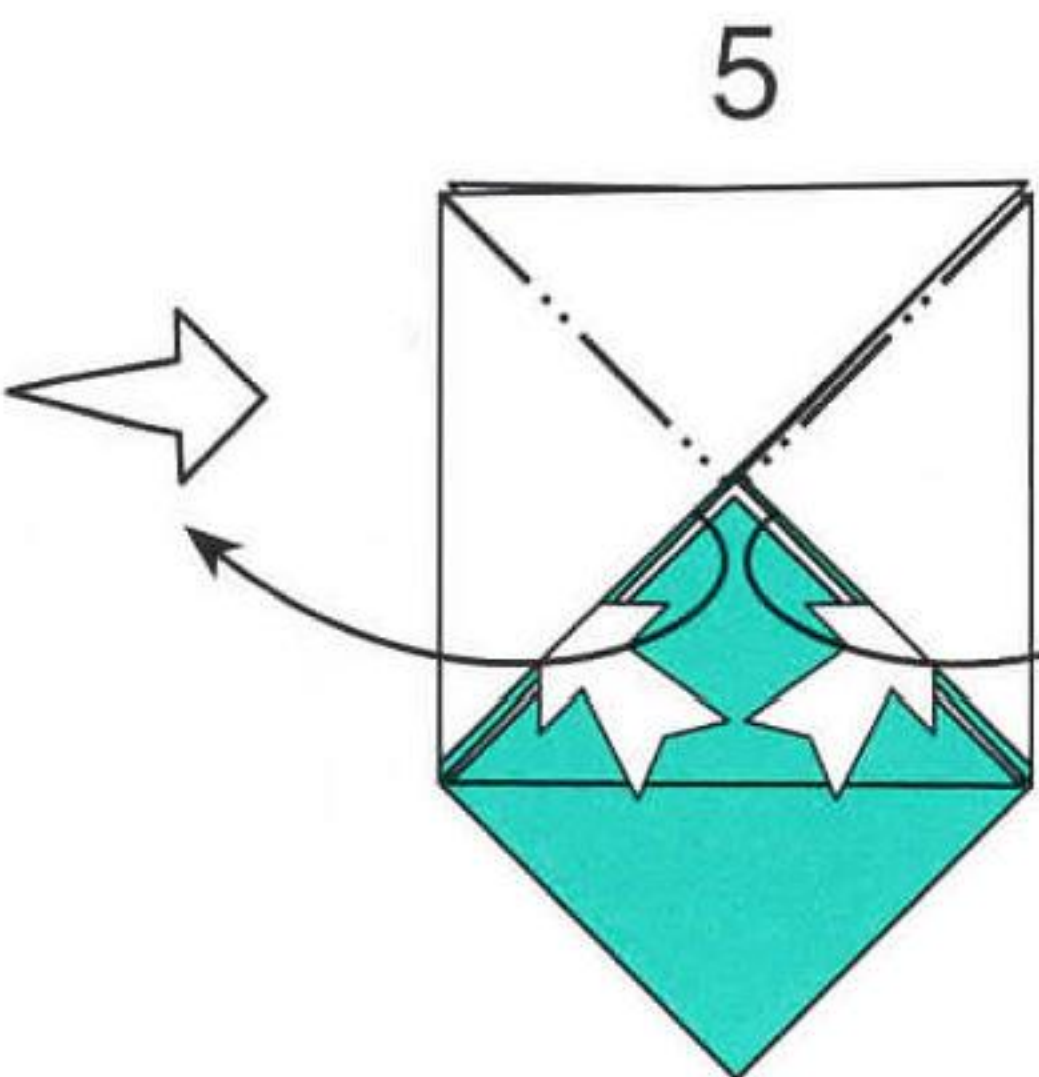
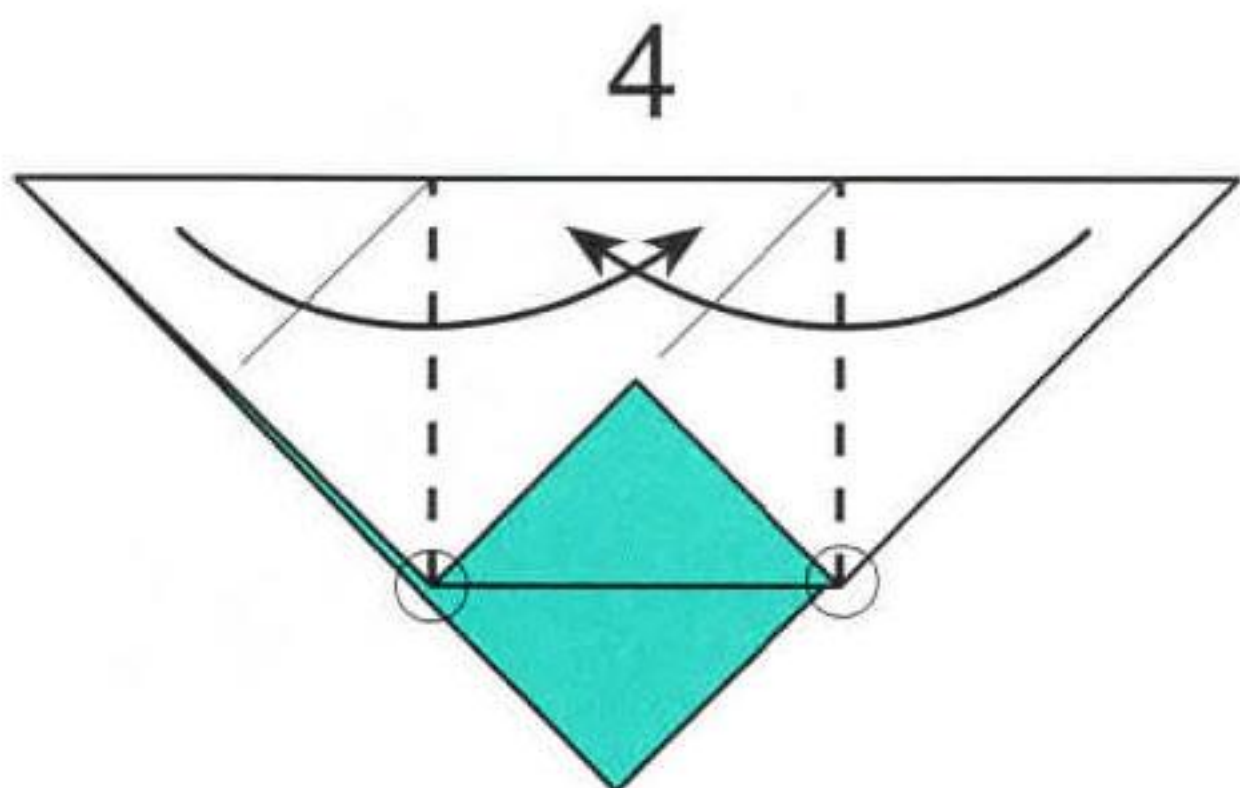
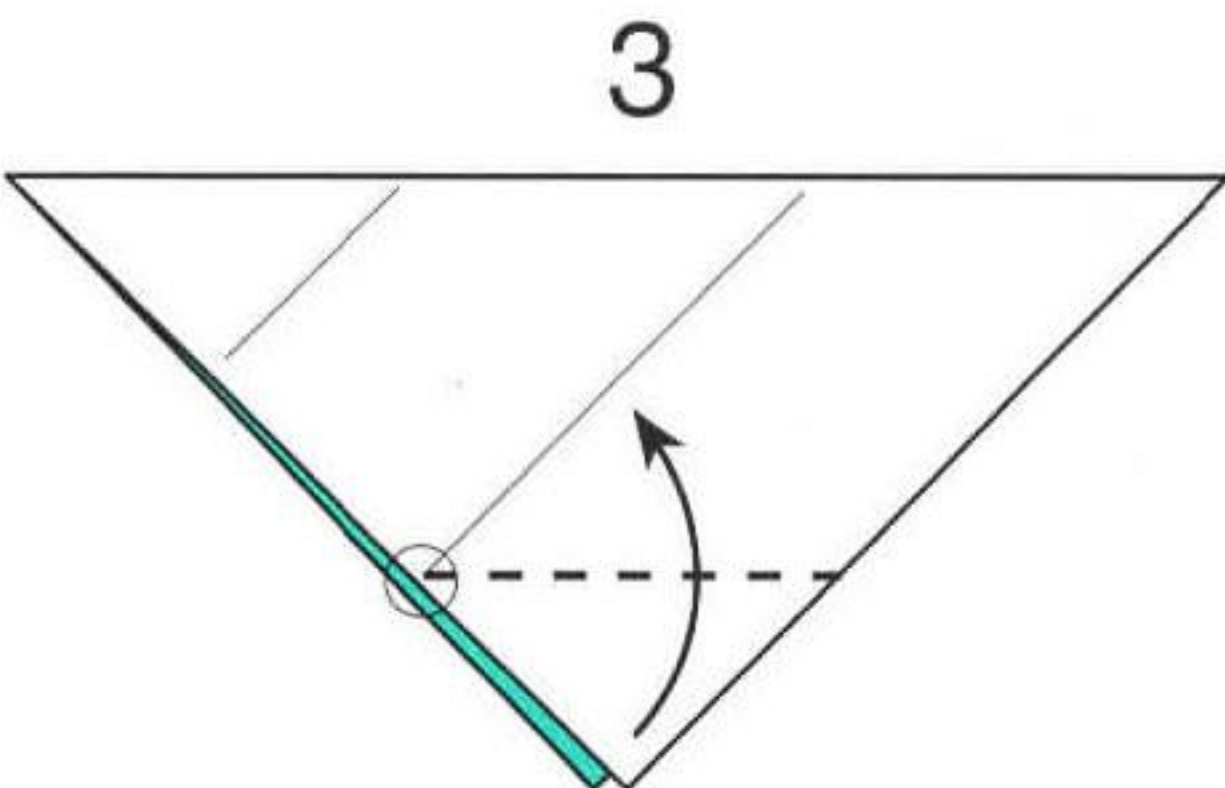
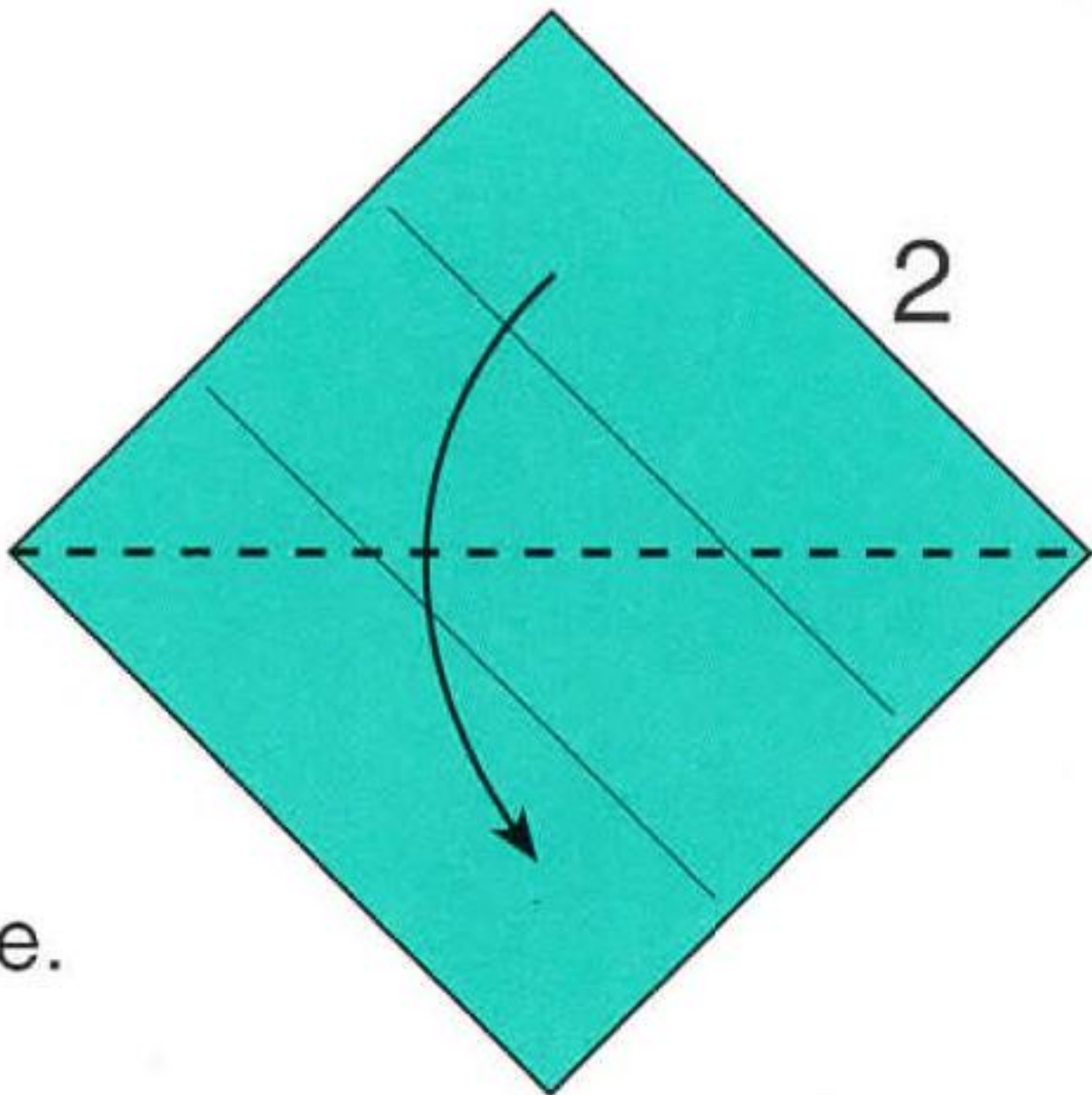


I present you two types of this model. First fold *Peacock 1*, with fewer pleats, as a warm-up, then proceed to *Peacock 2*, which is a more advanced model with twice as many pleats.

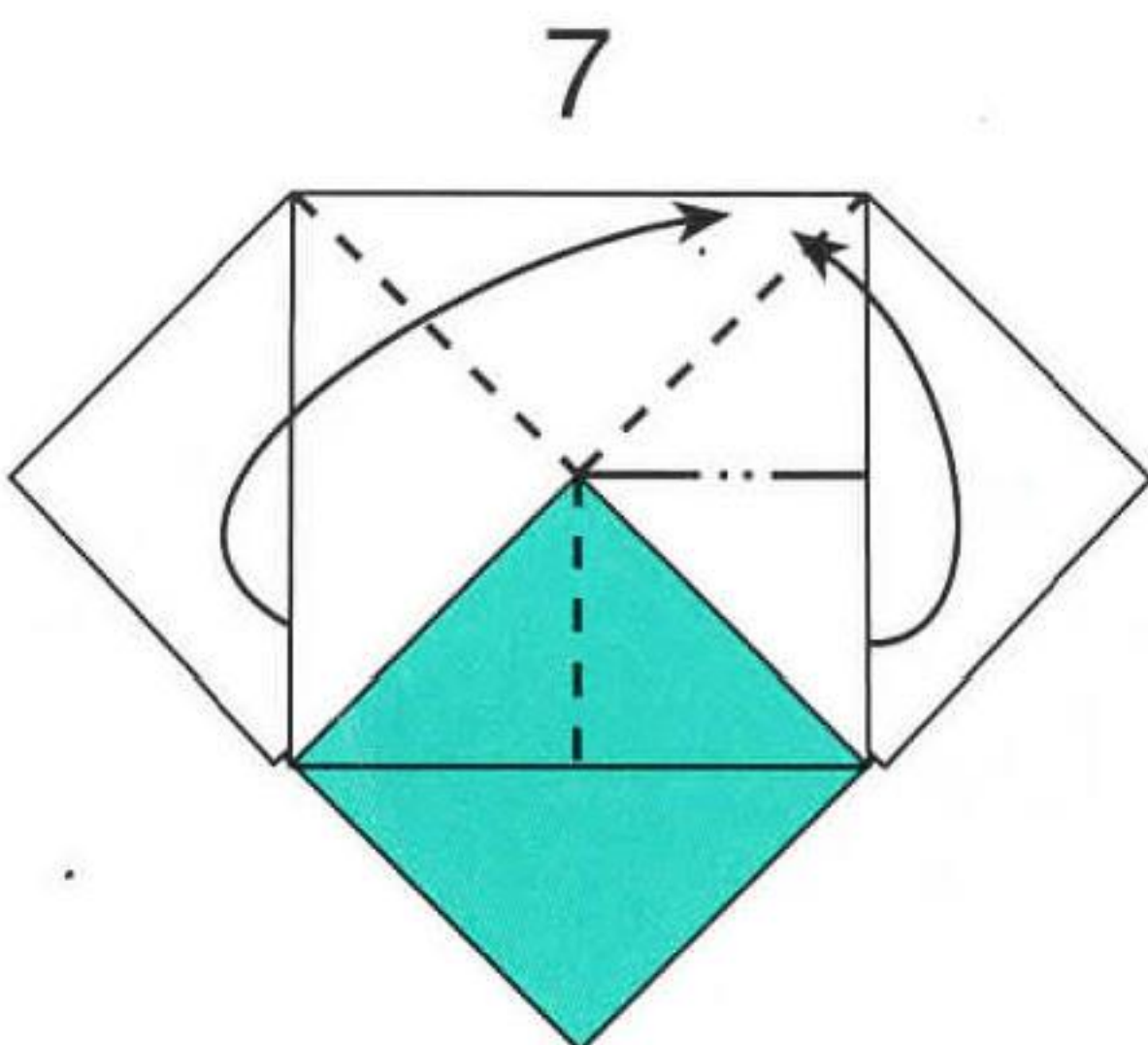
Peacock 1



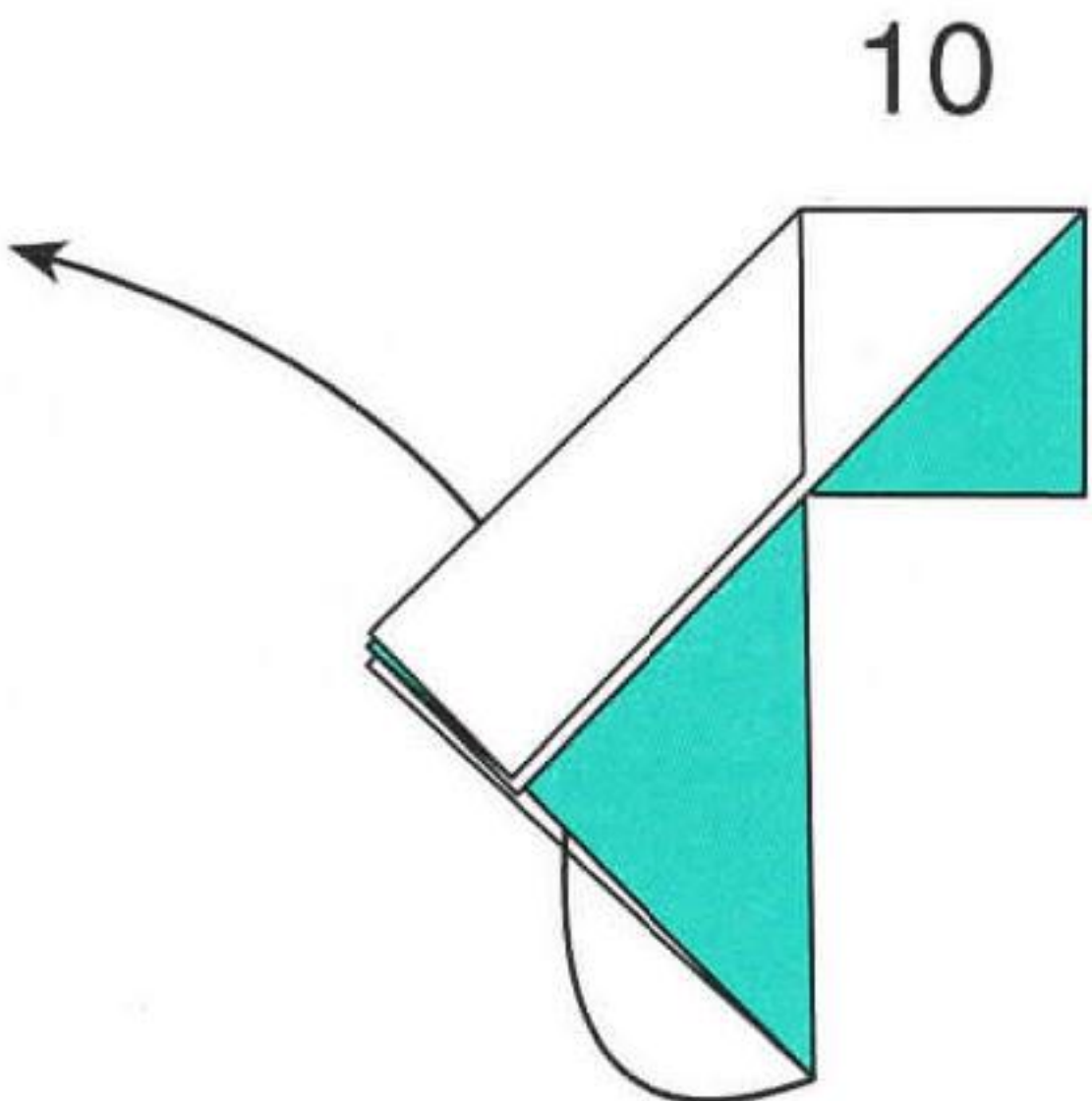
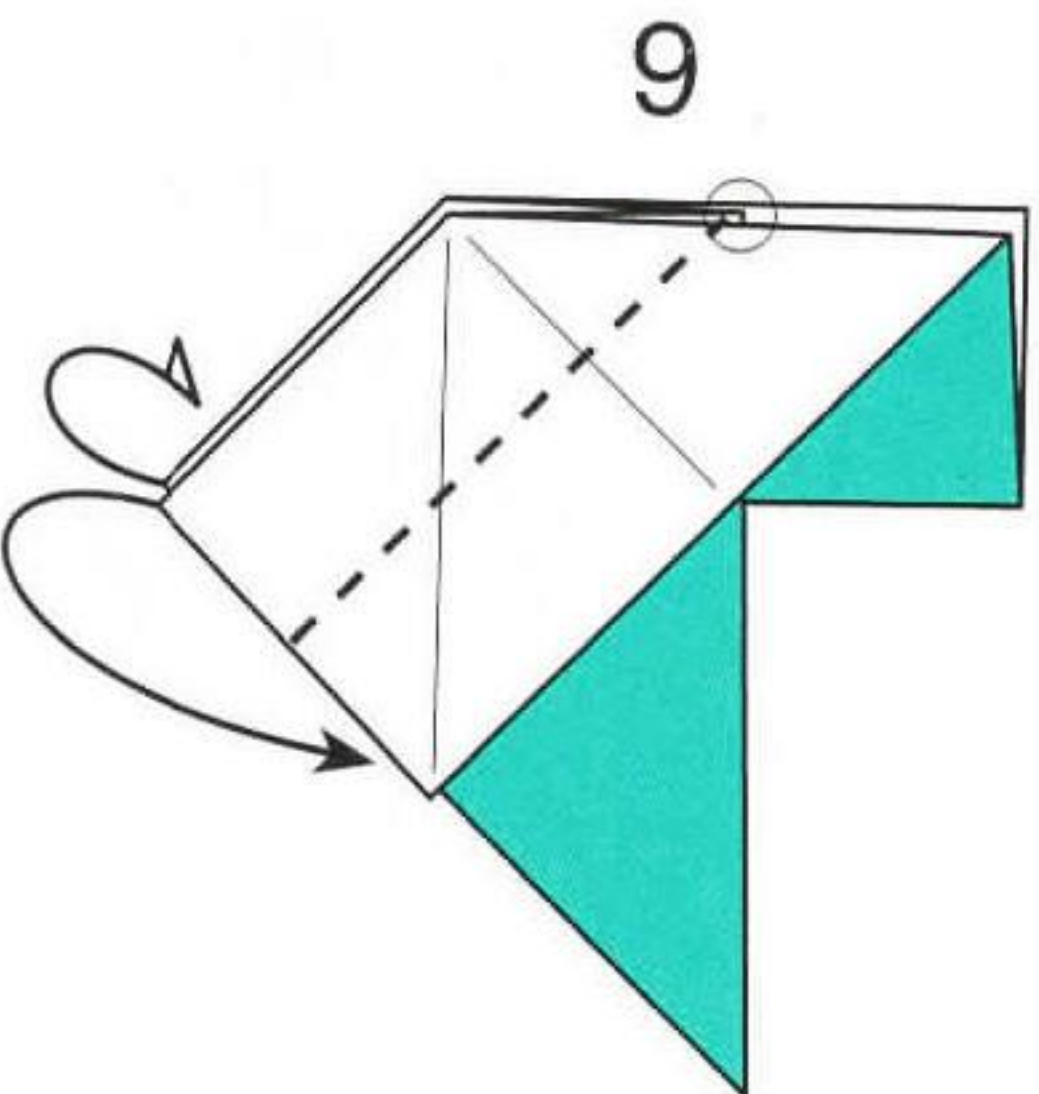
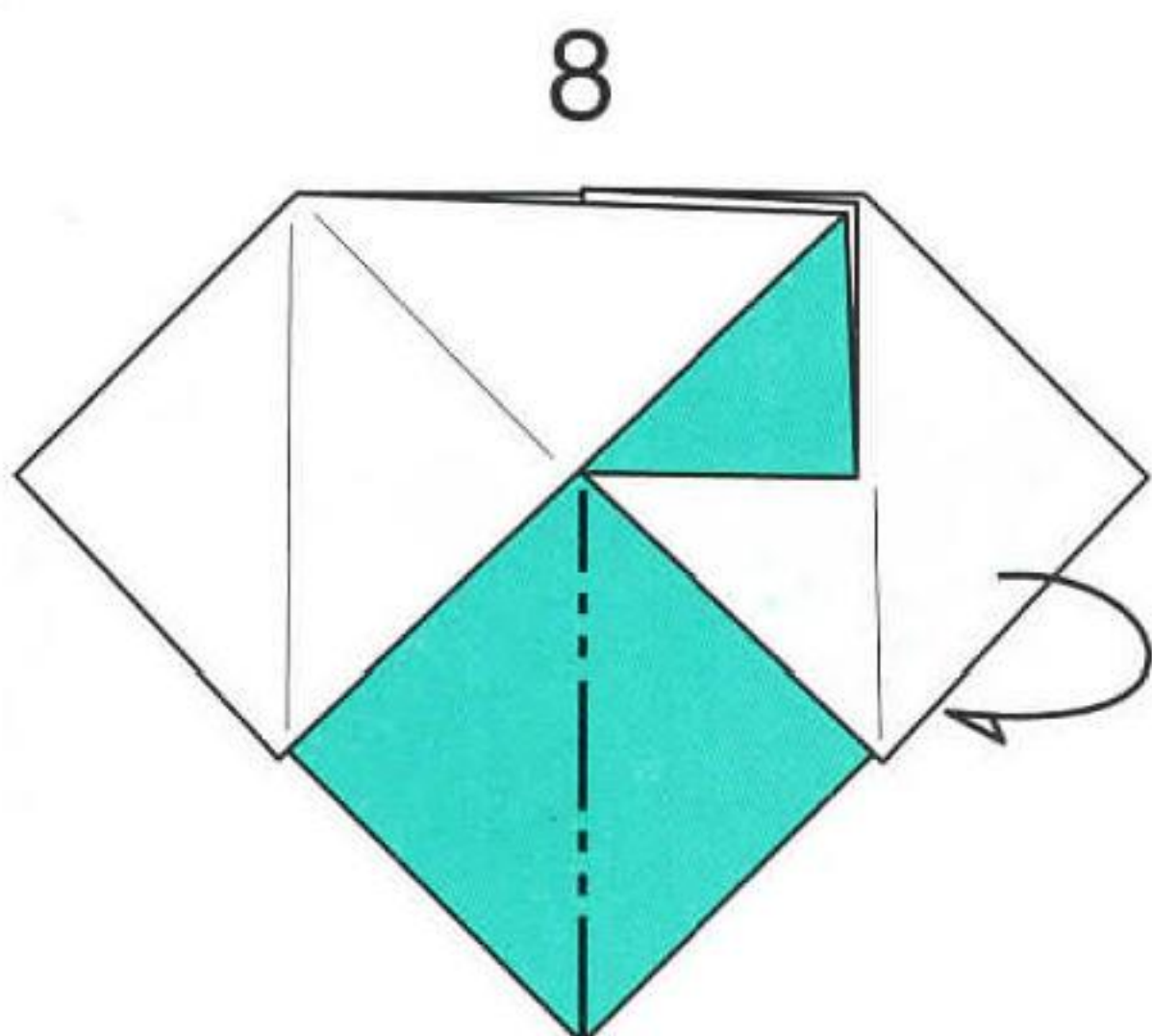
Divide the side into three.



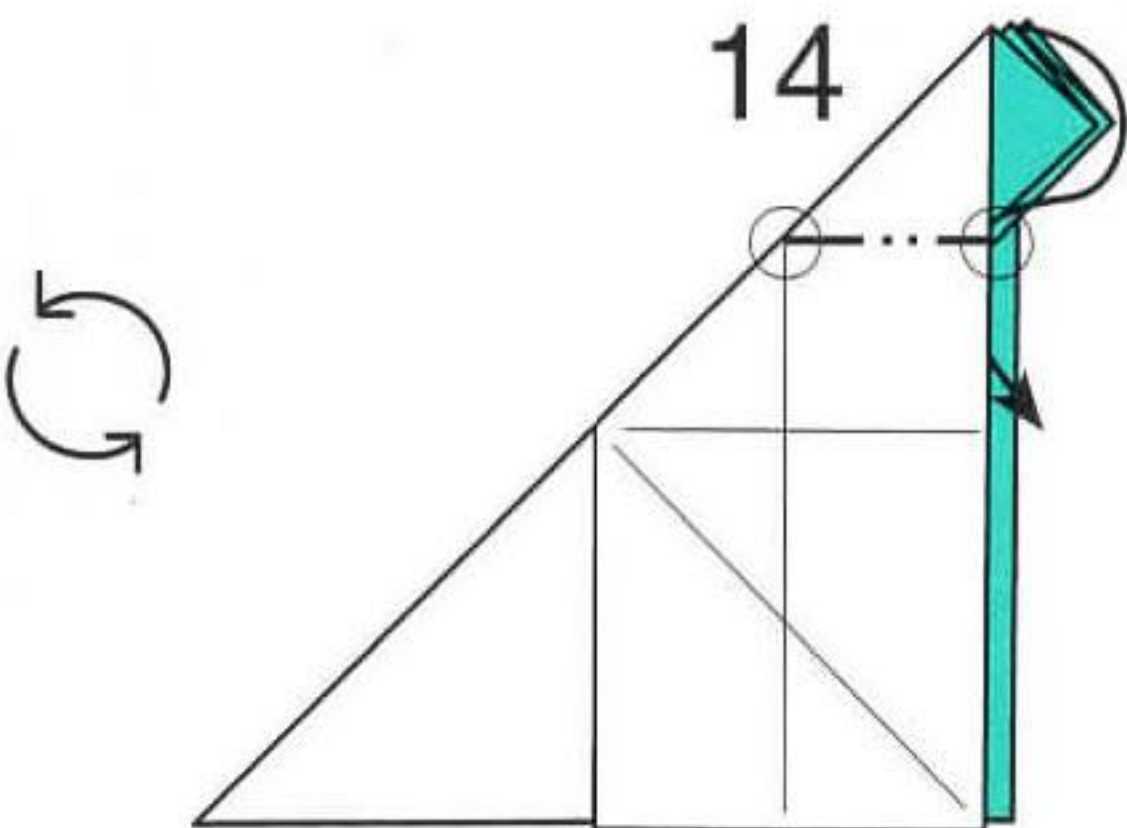
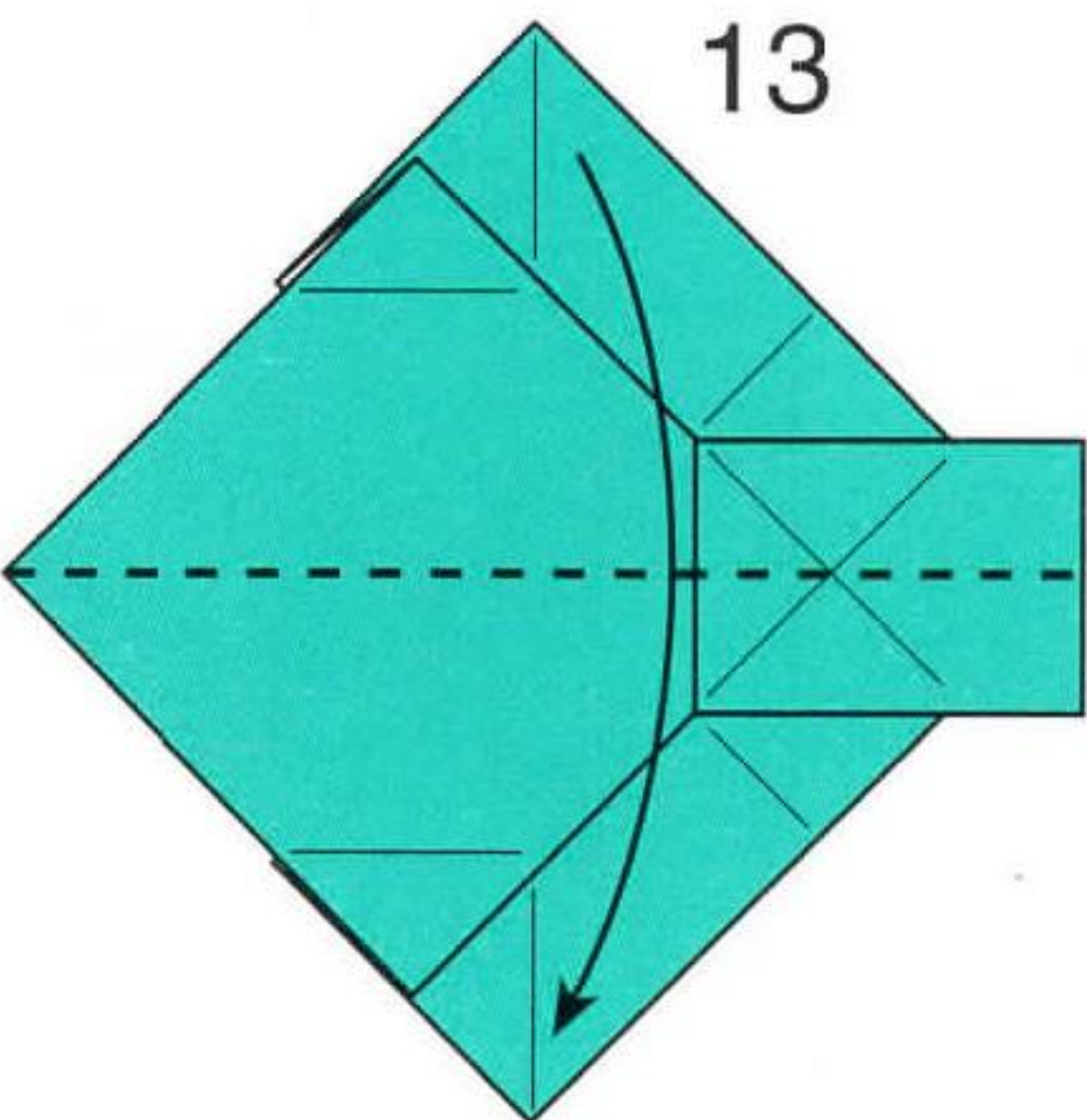
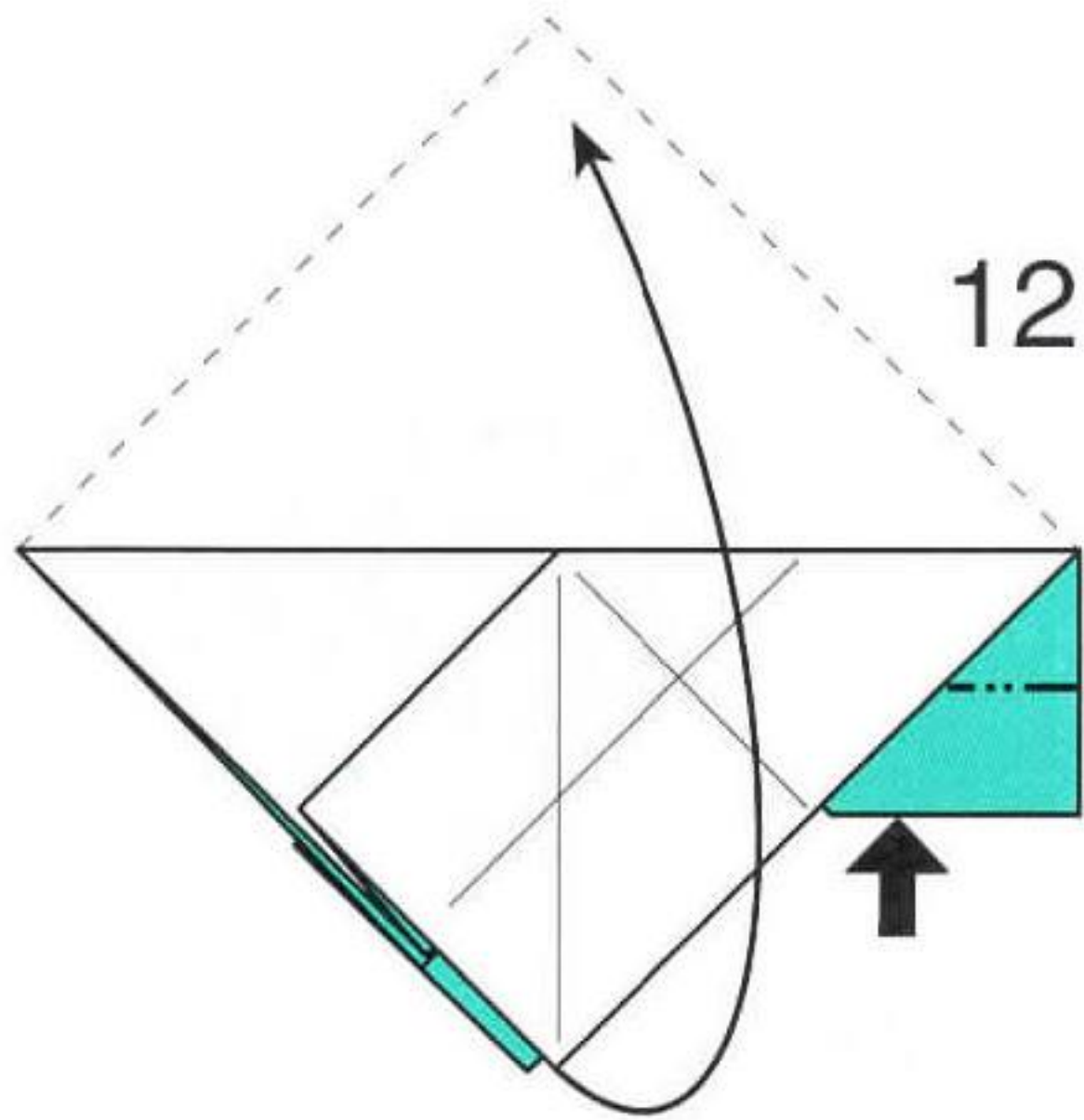
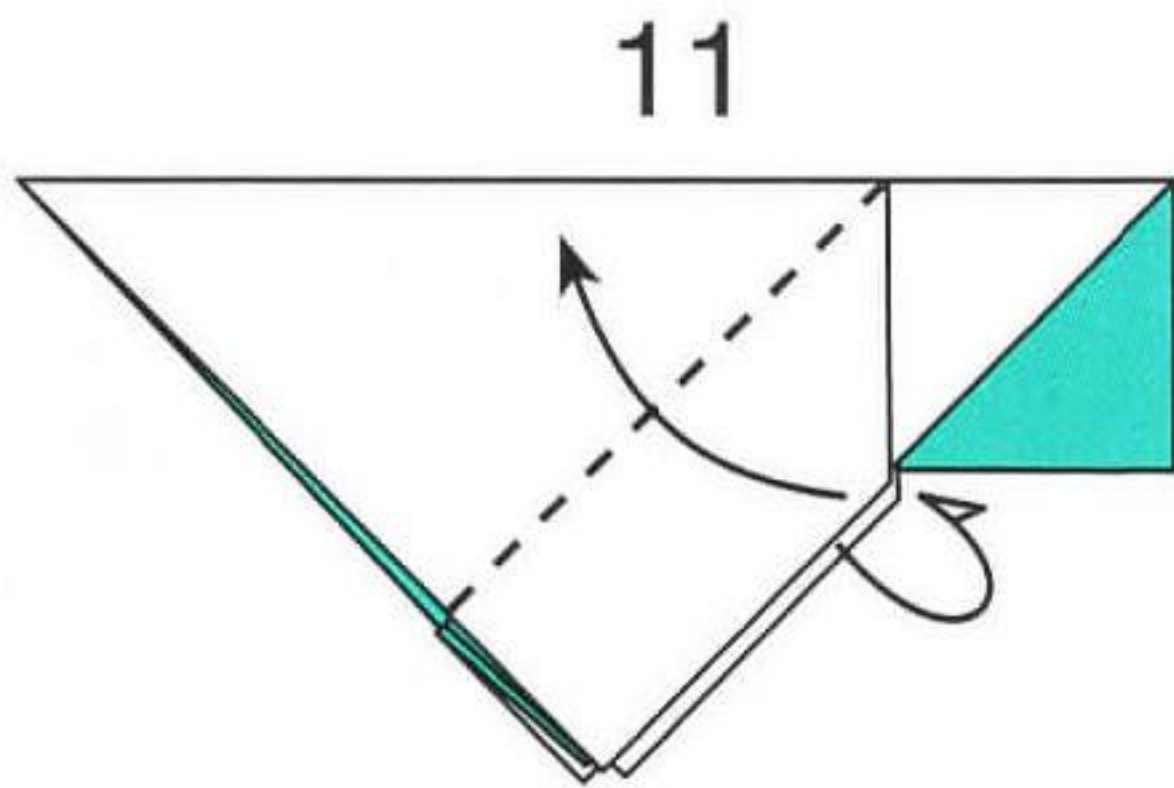
Reverse the mountain and valley creases.



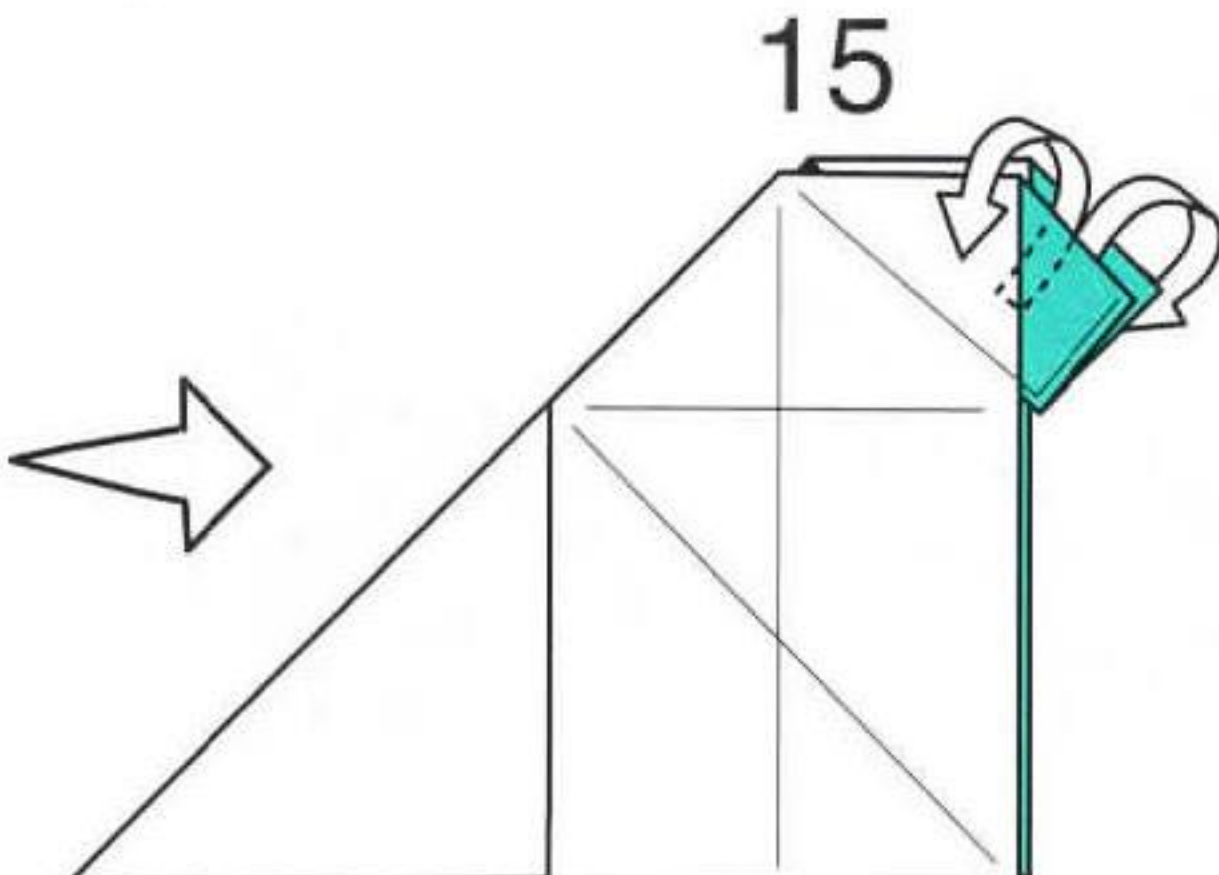
Rabbit-ear-fold



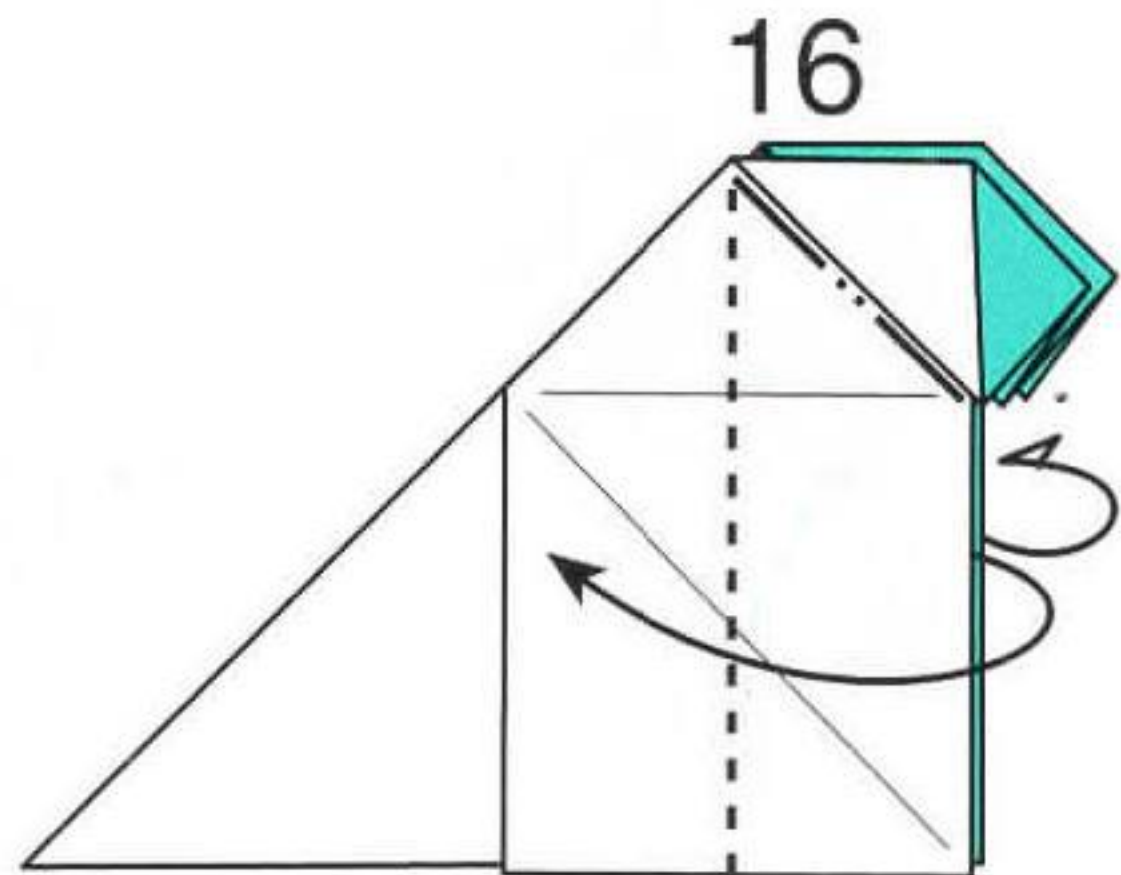
Inside reverse-fold

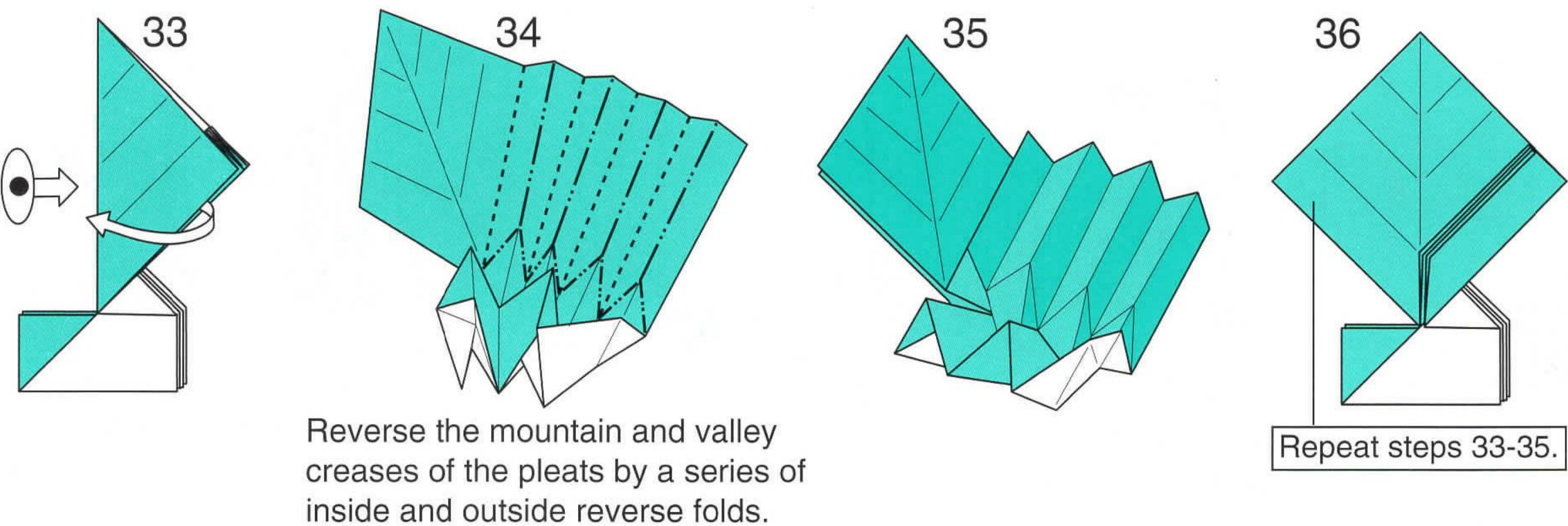
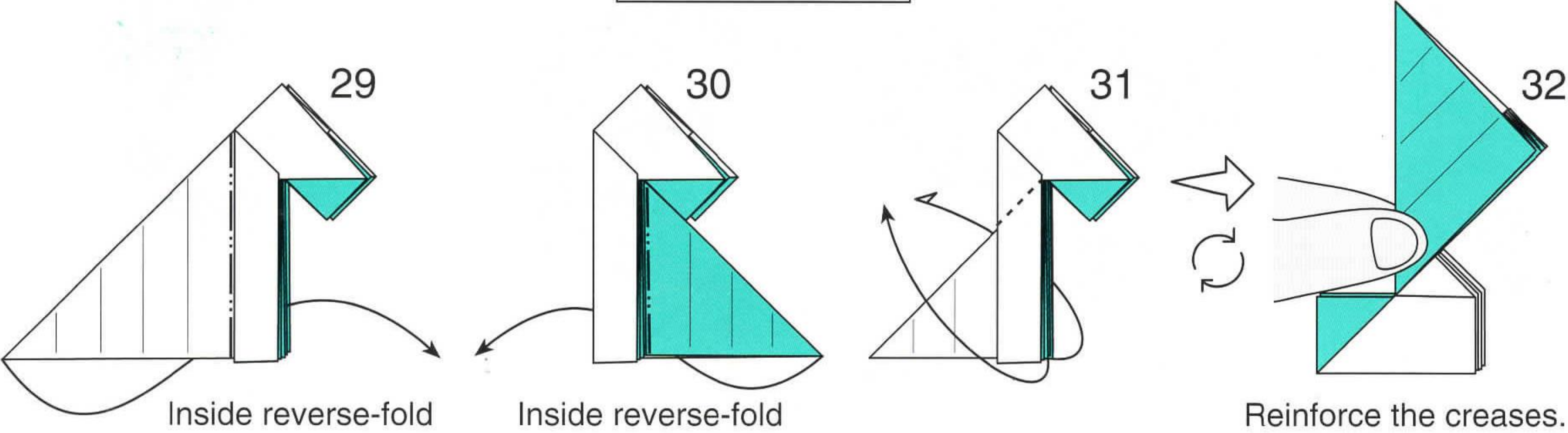
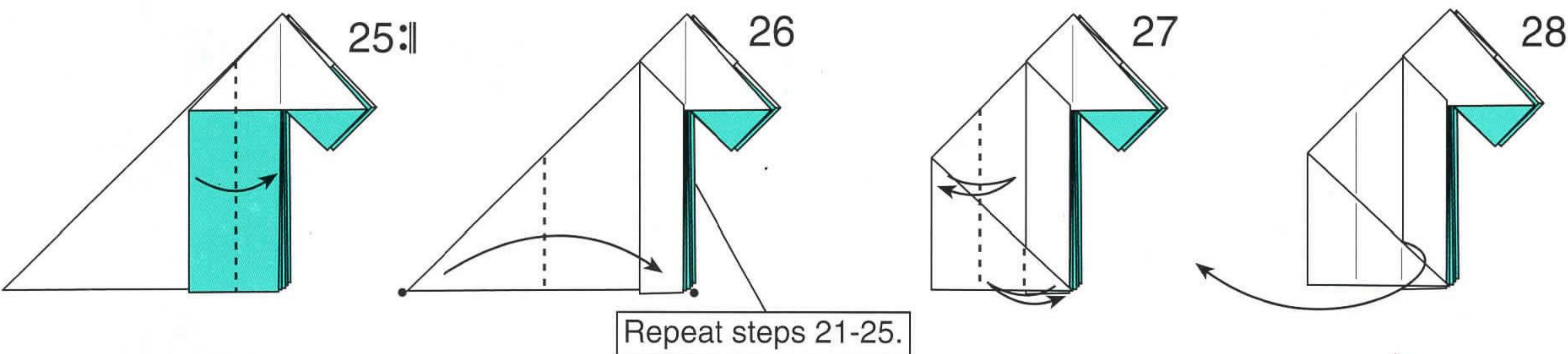
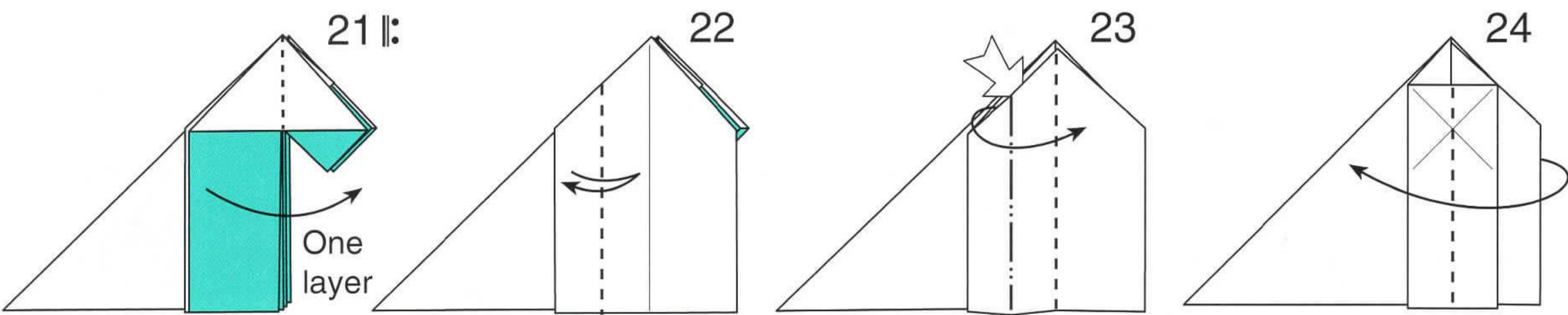
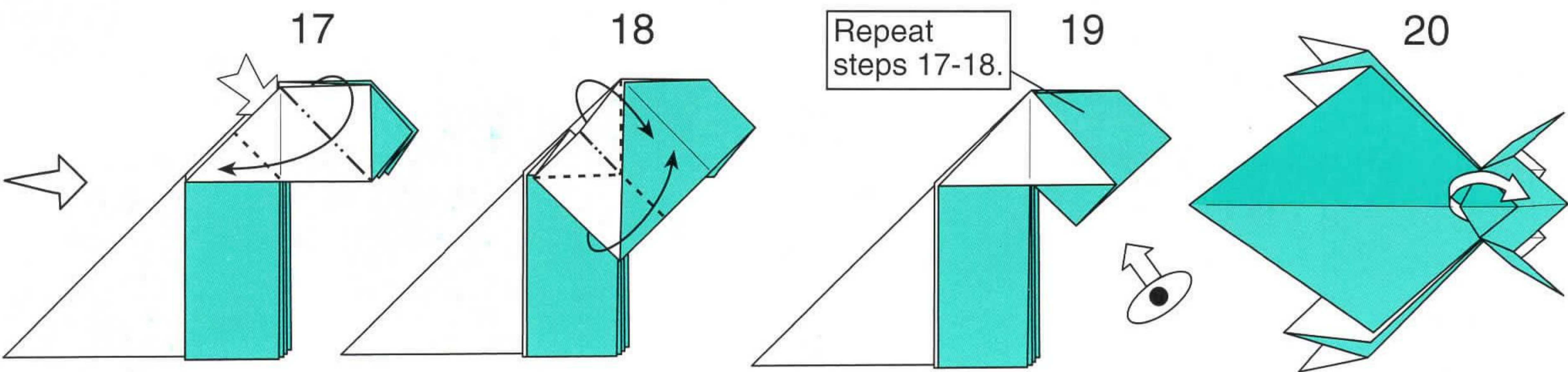


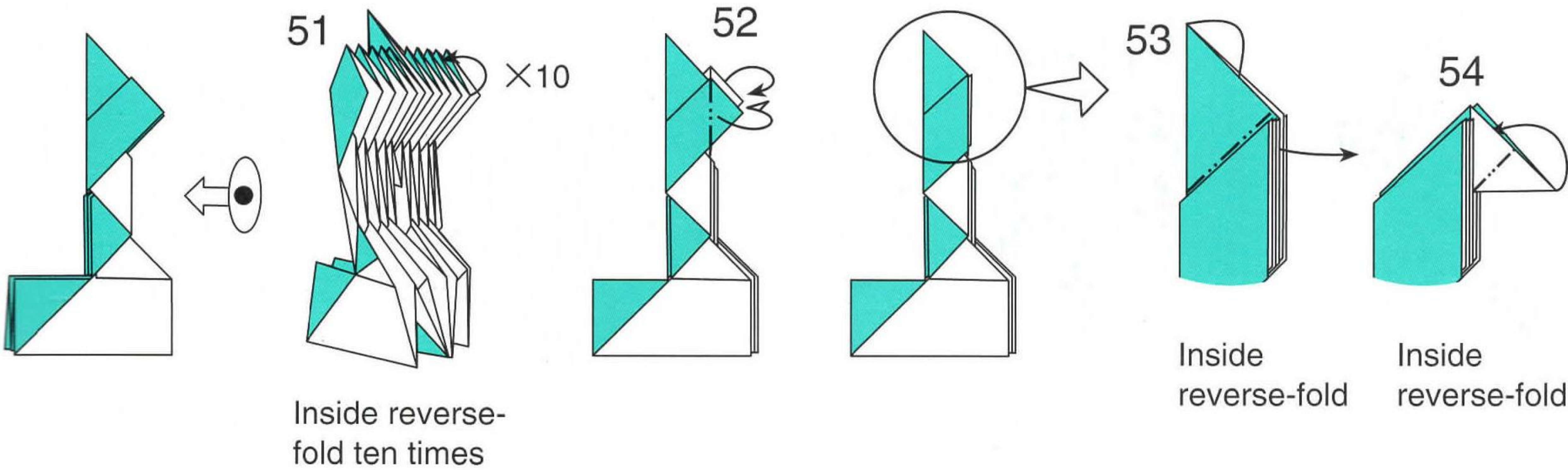
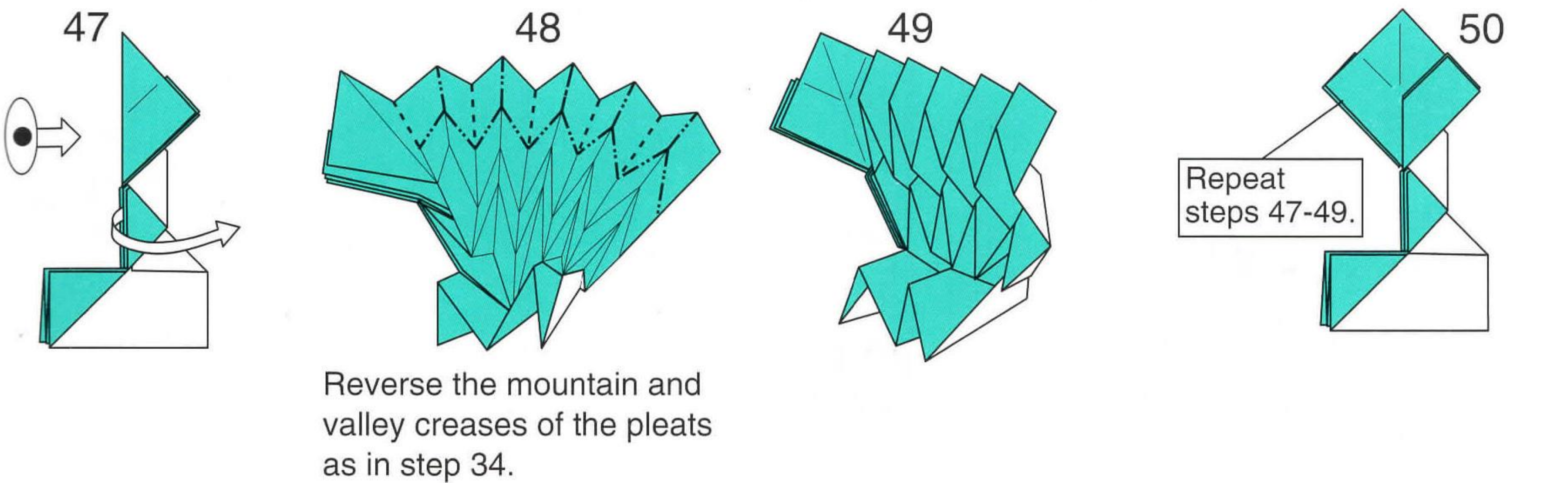
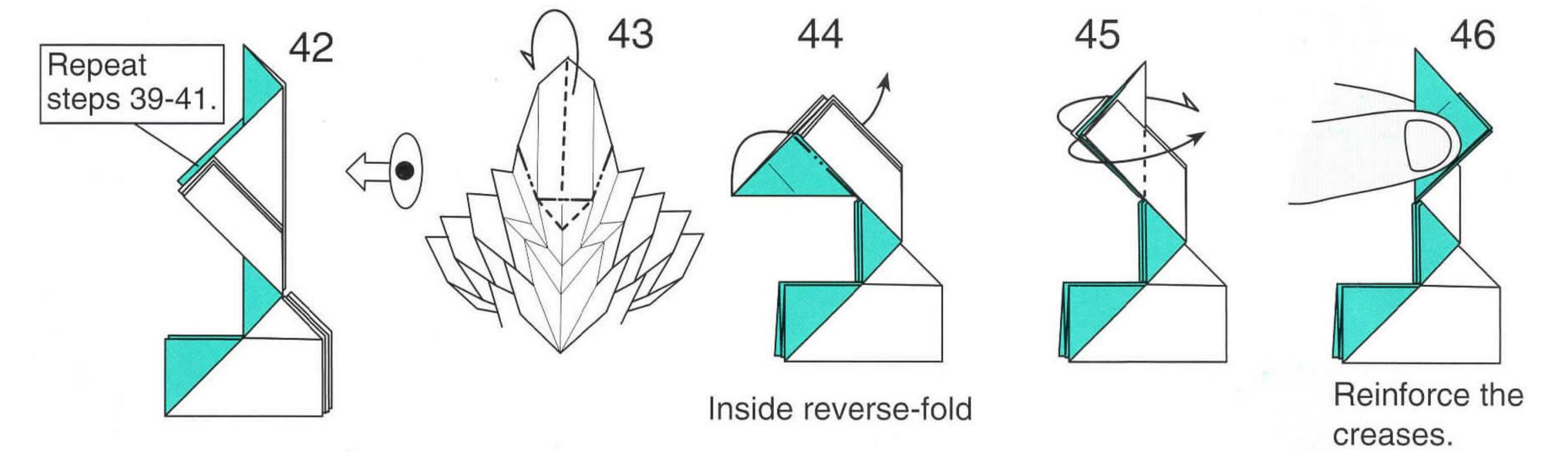
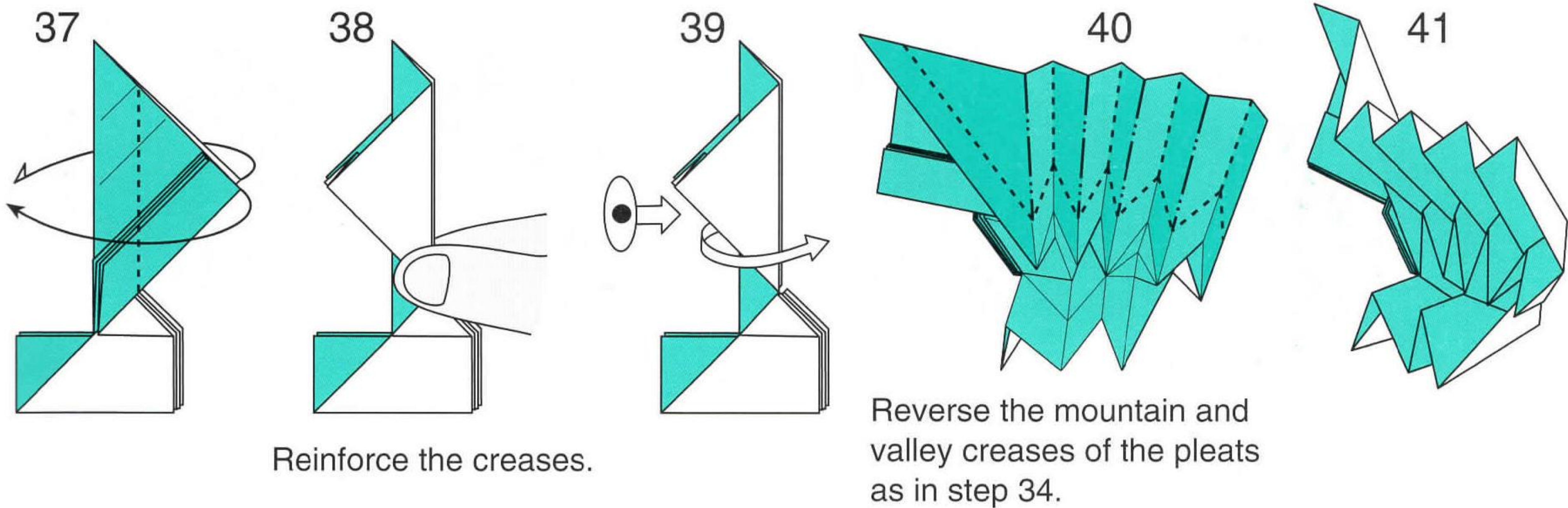
Inside reverse-fold

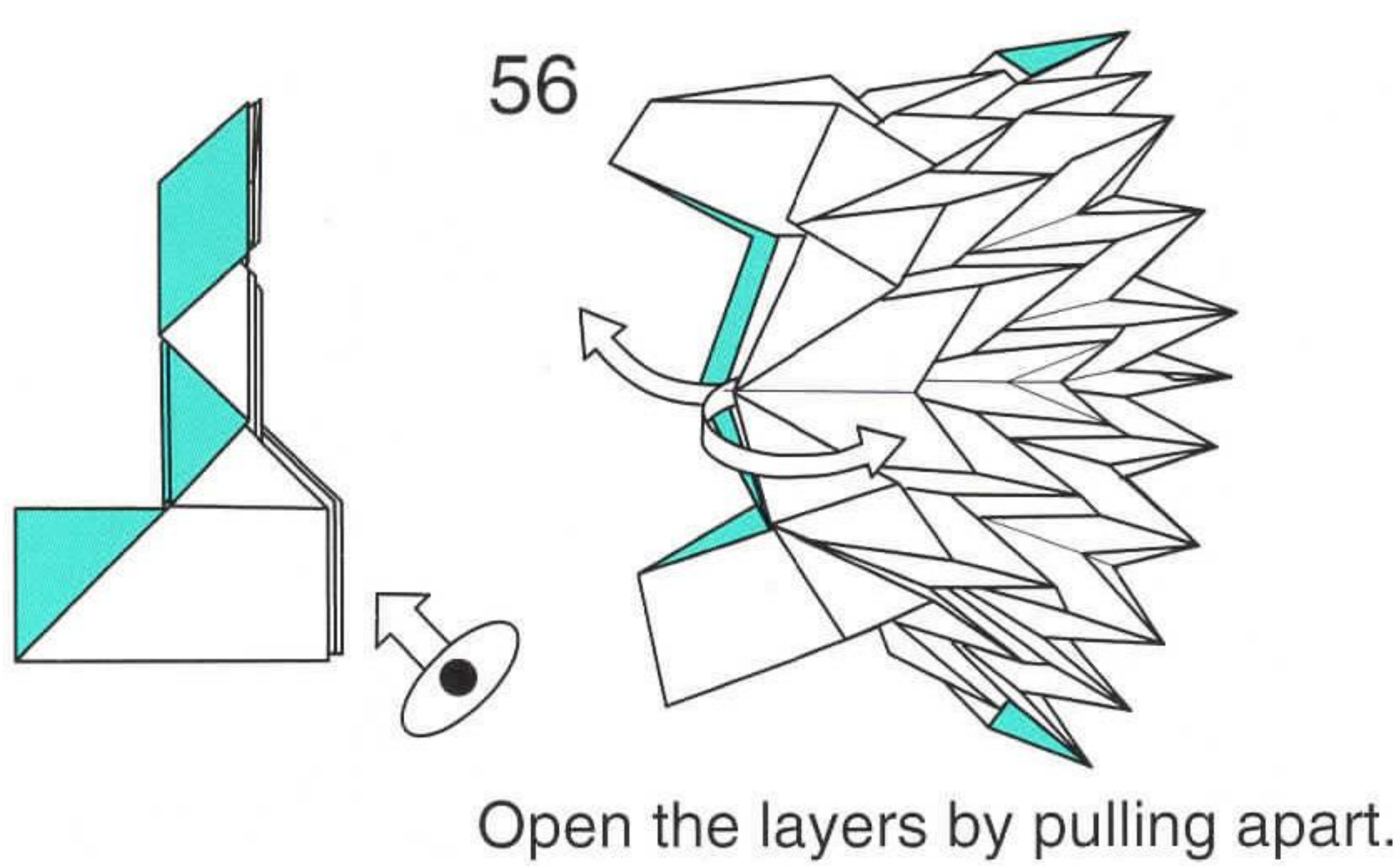
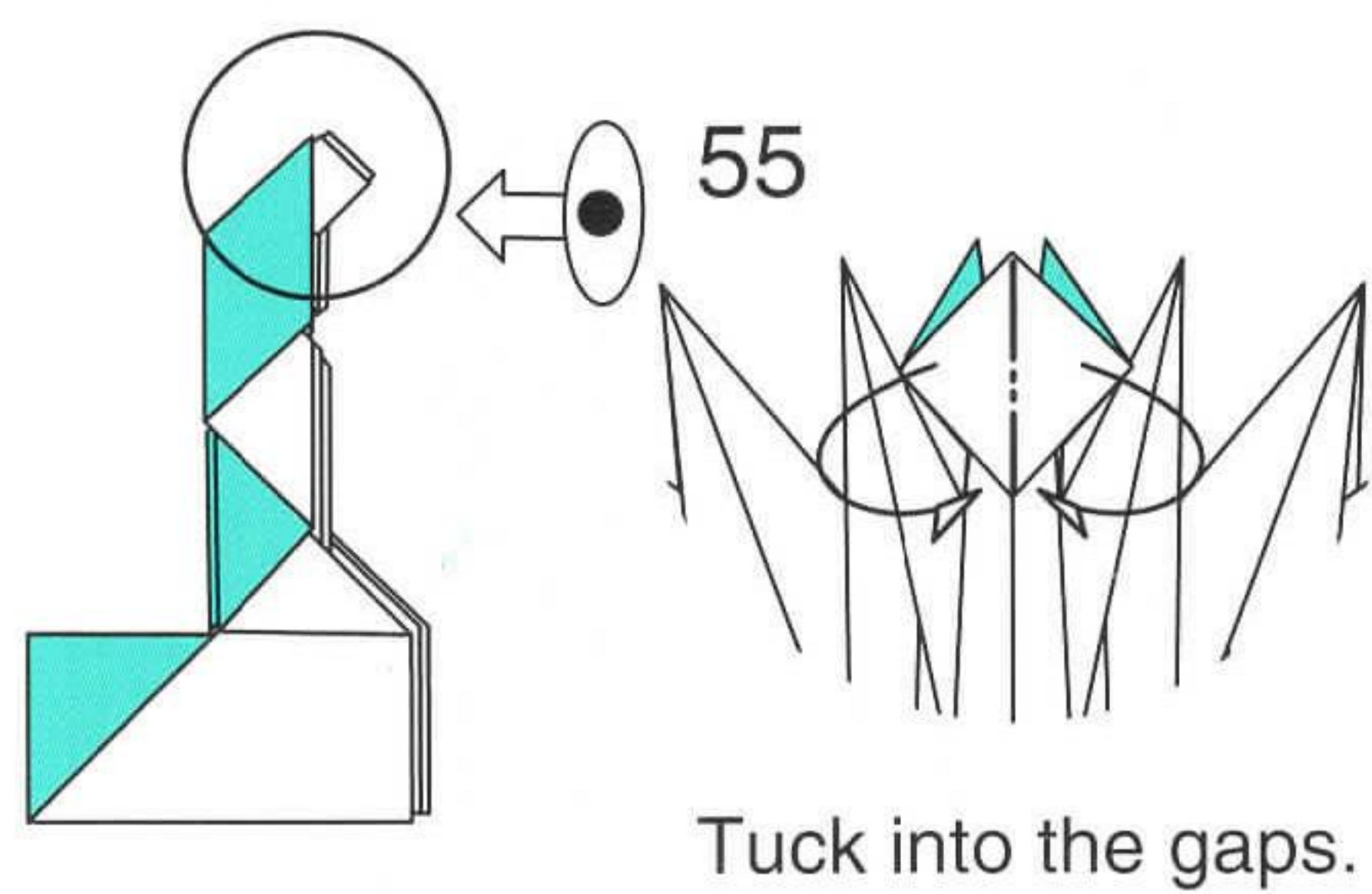


Reverse like an outside reverse fold.

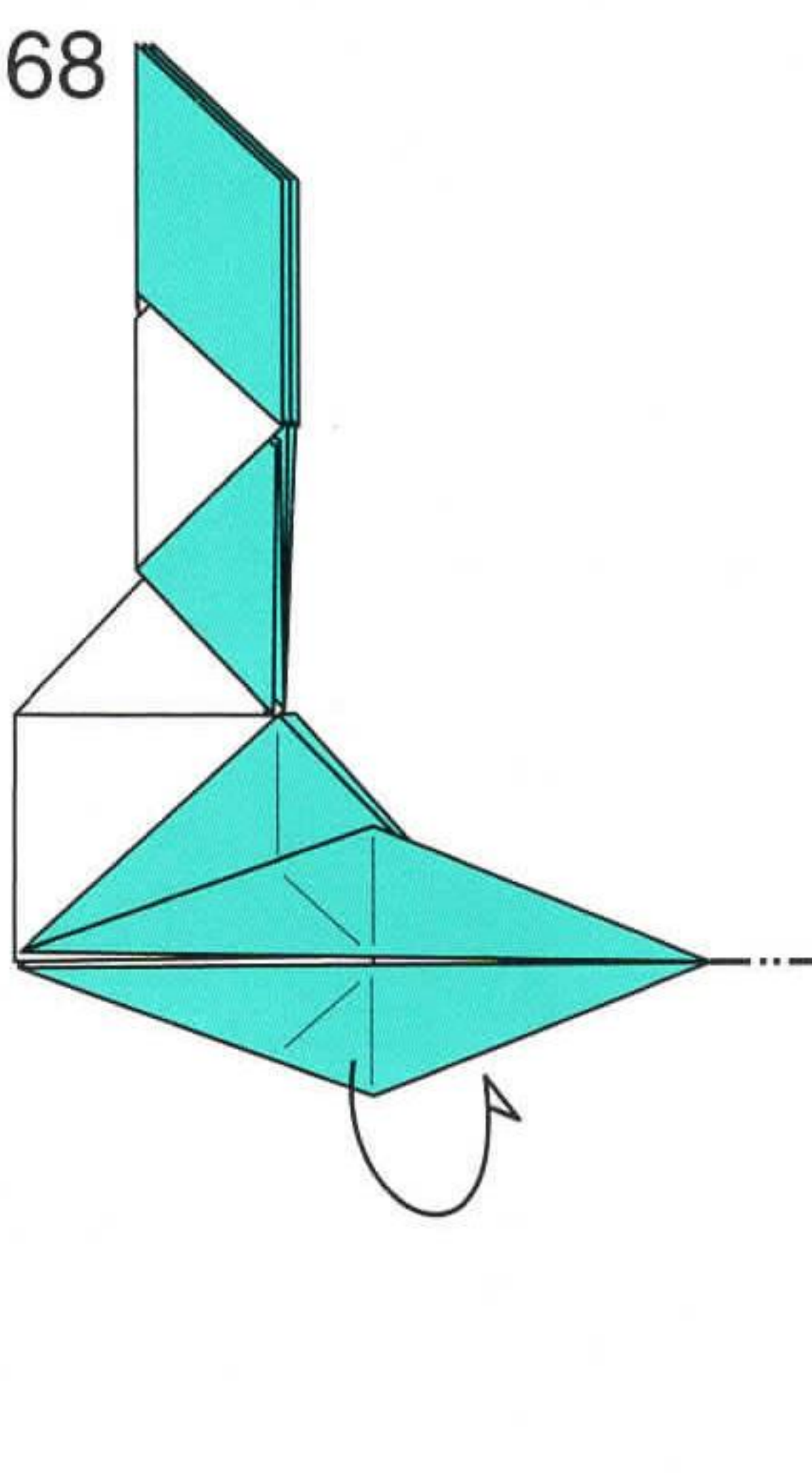
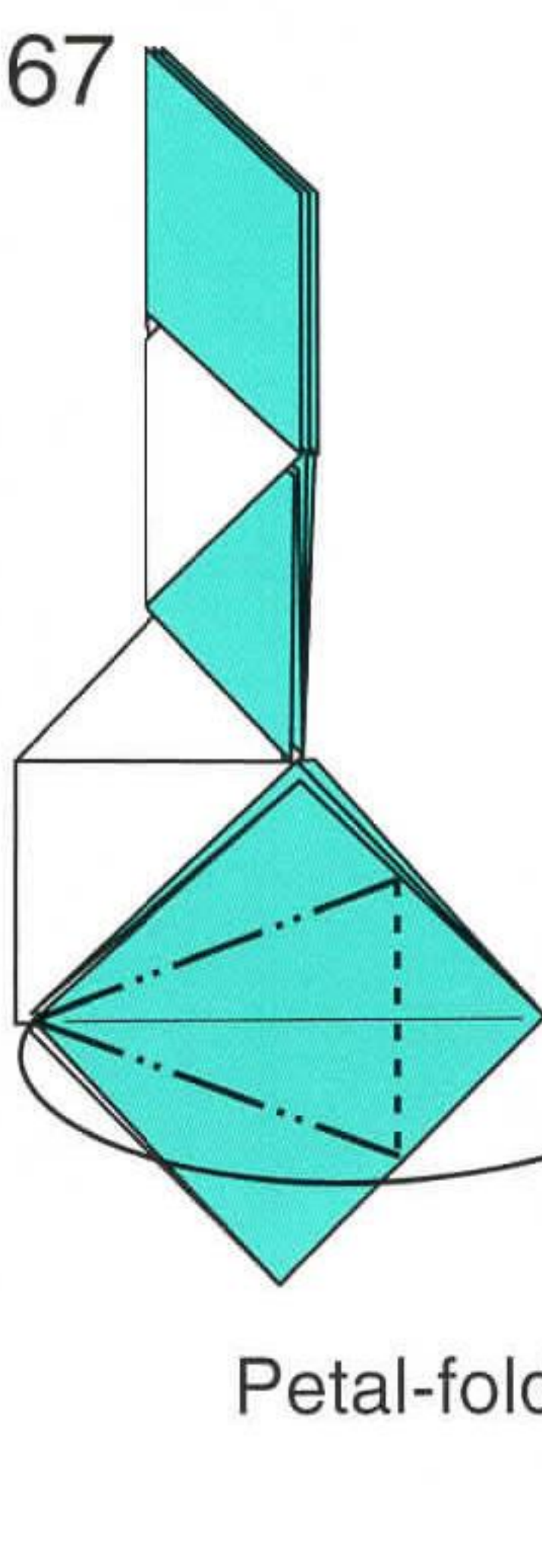
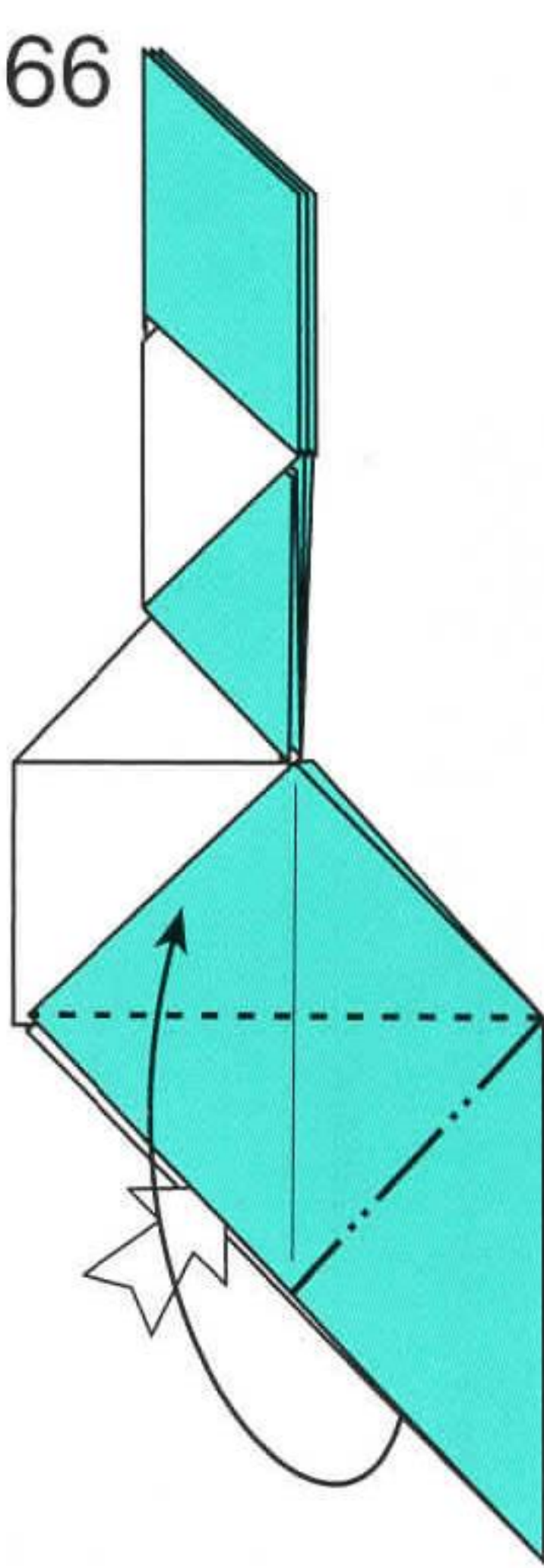
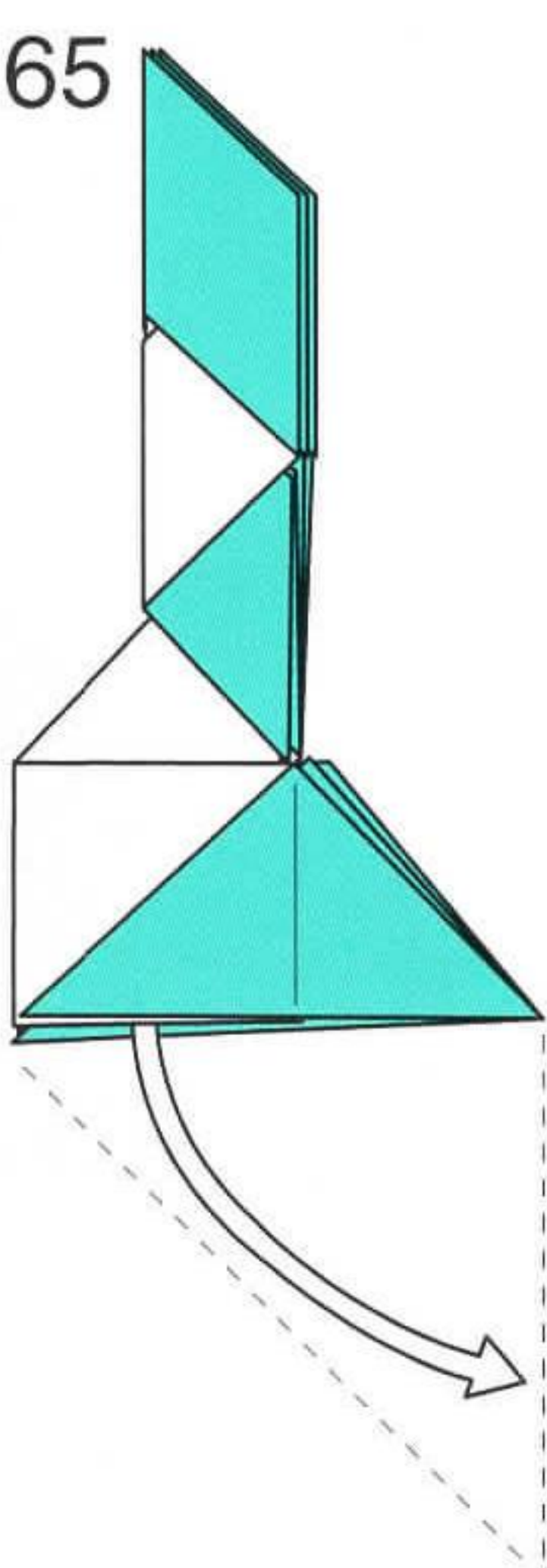
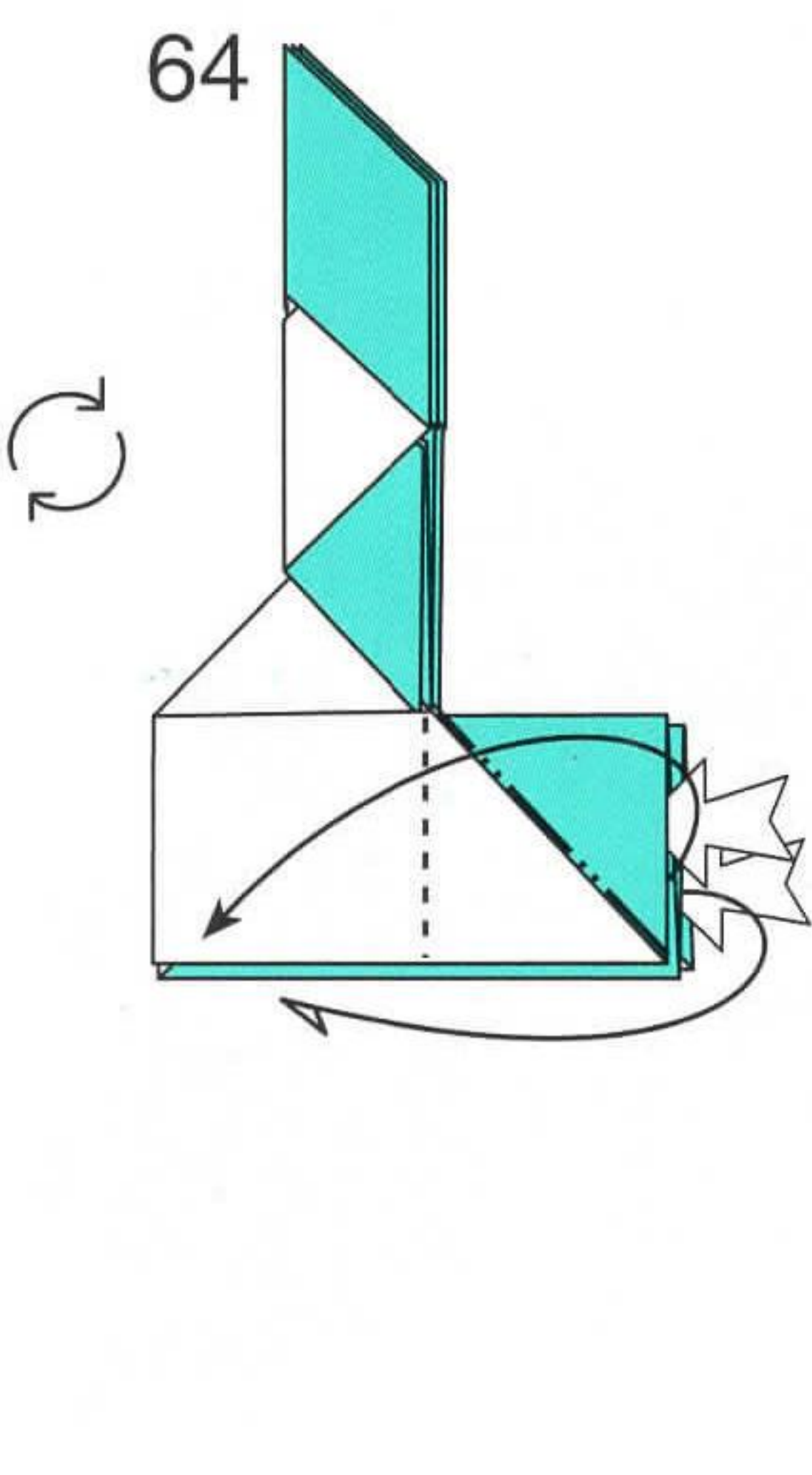
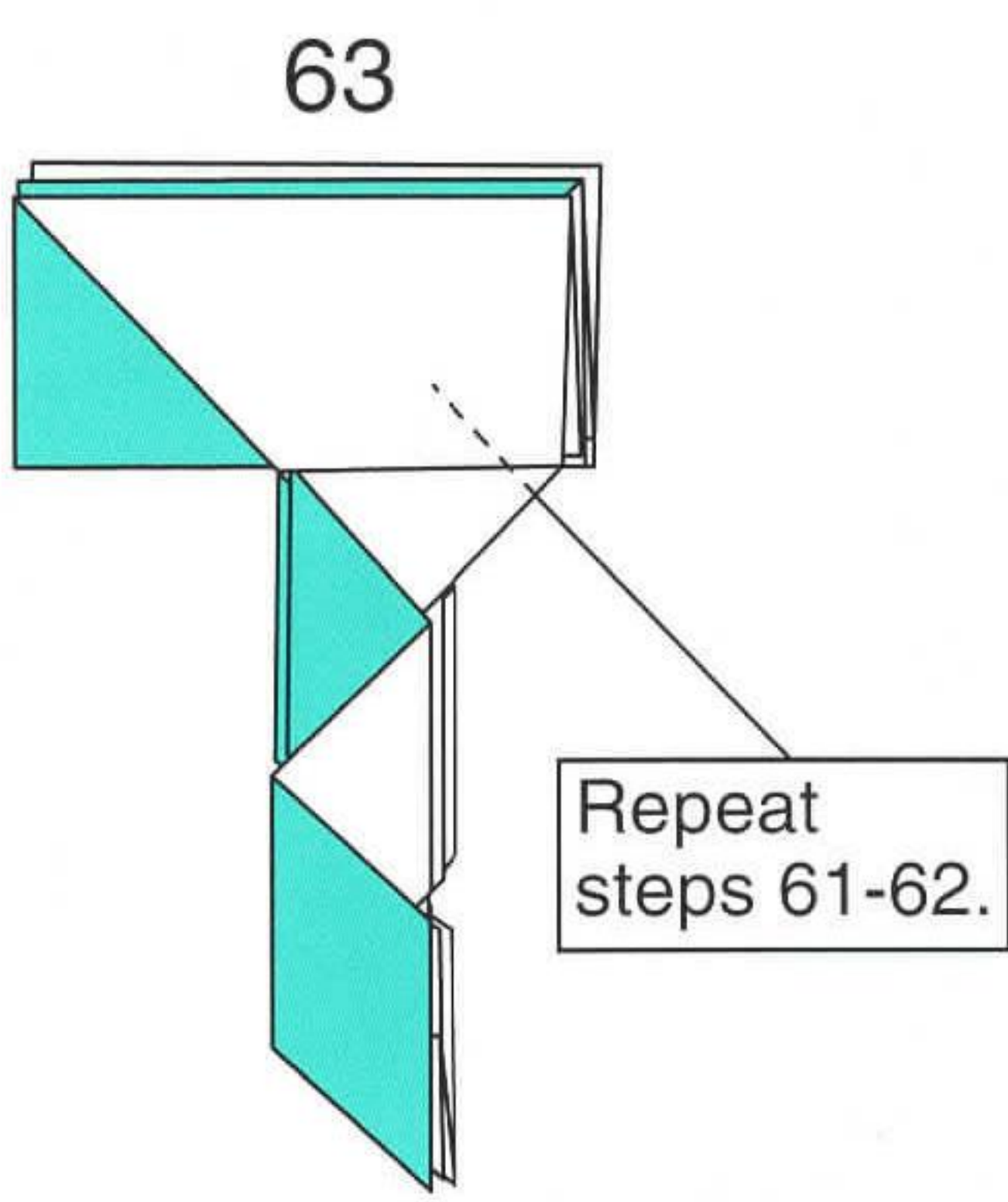
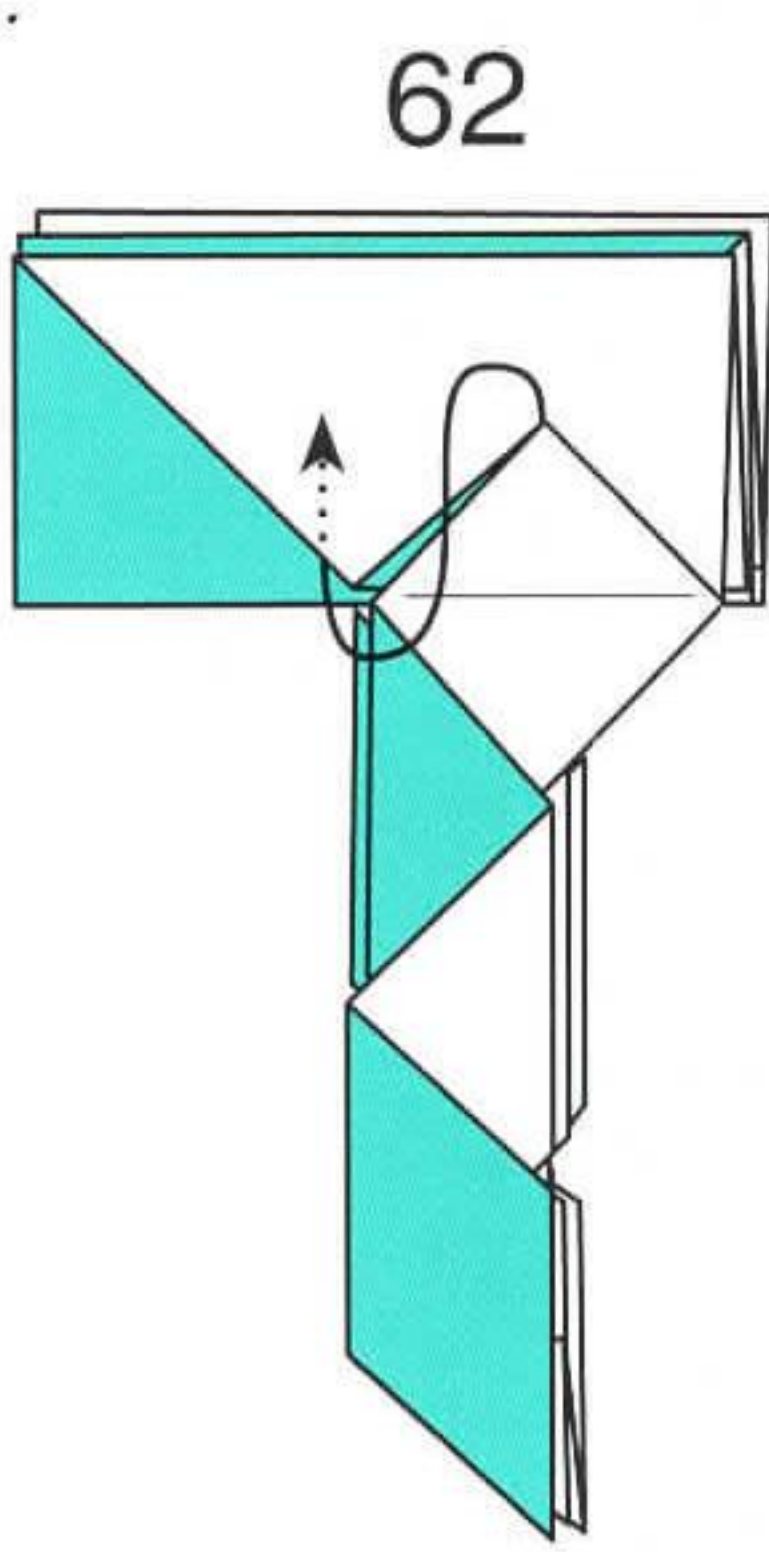
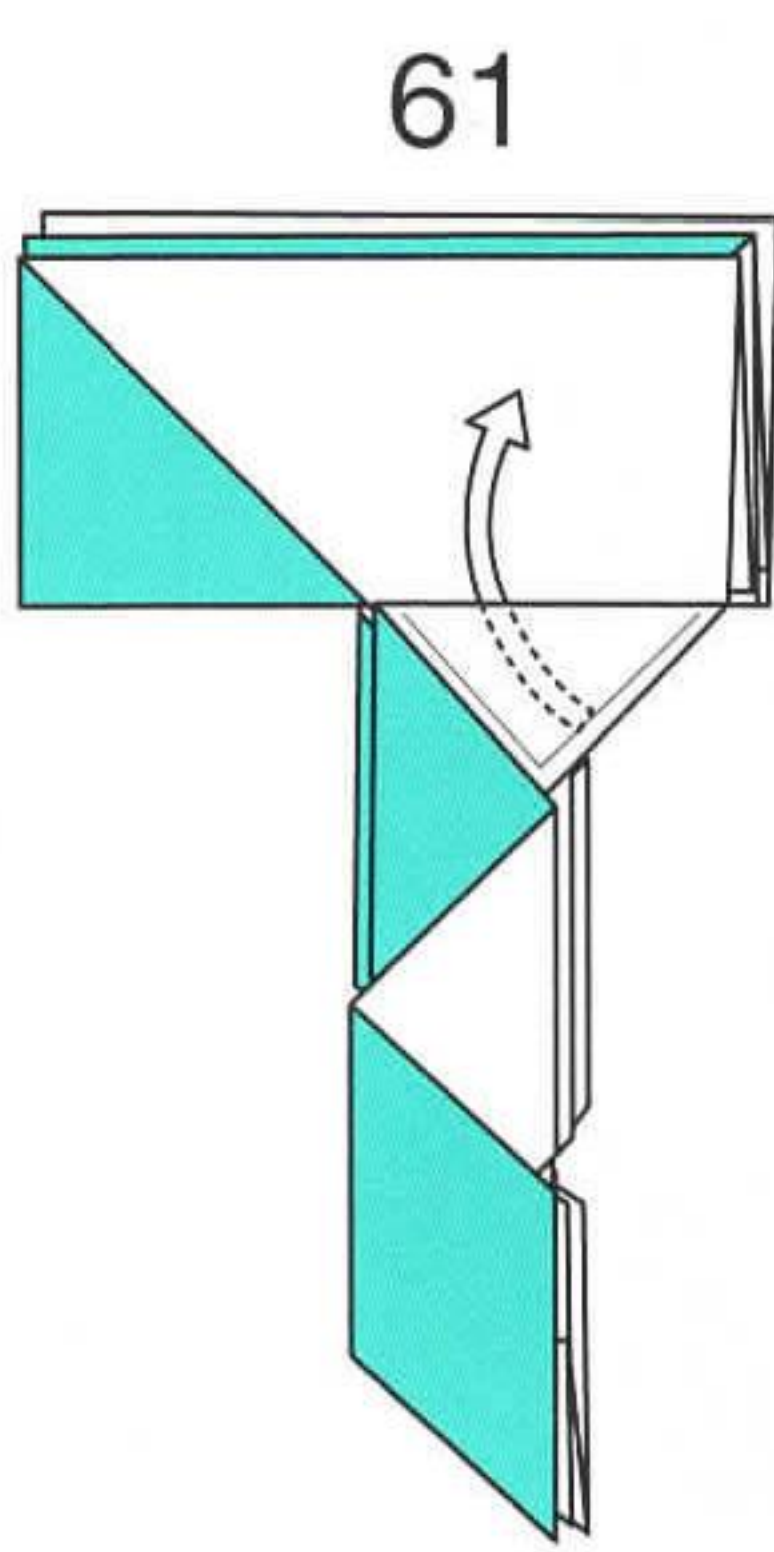
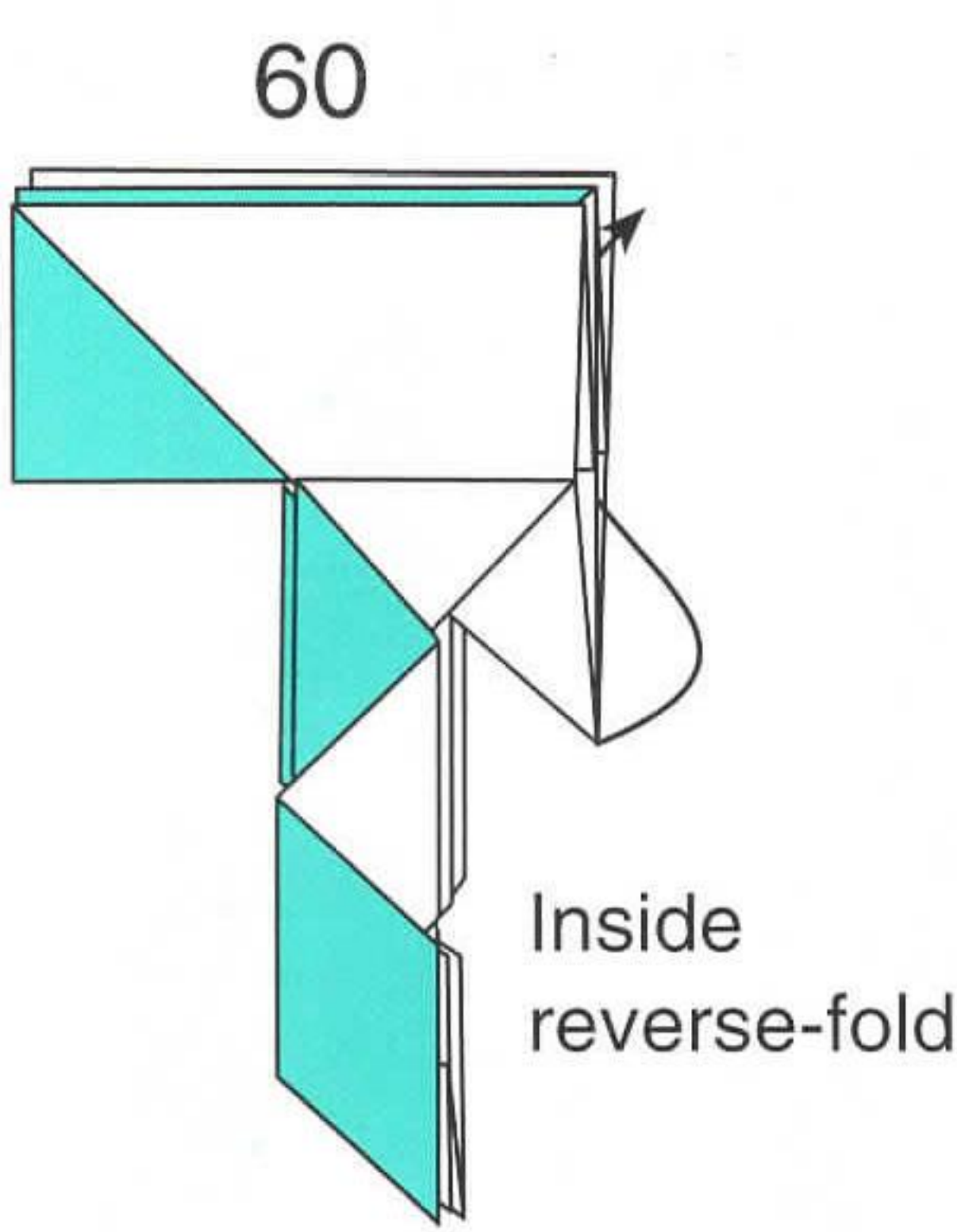
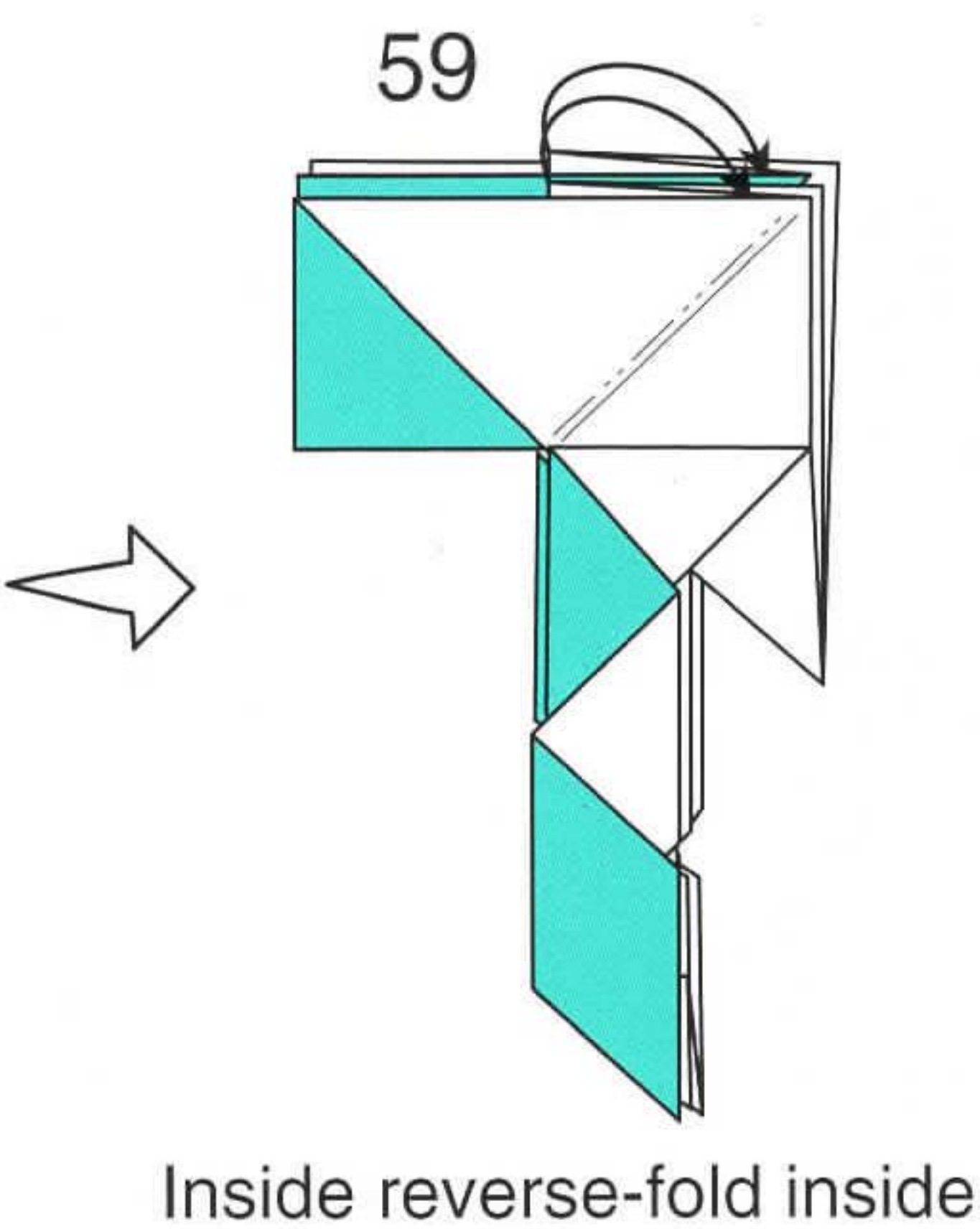
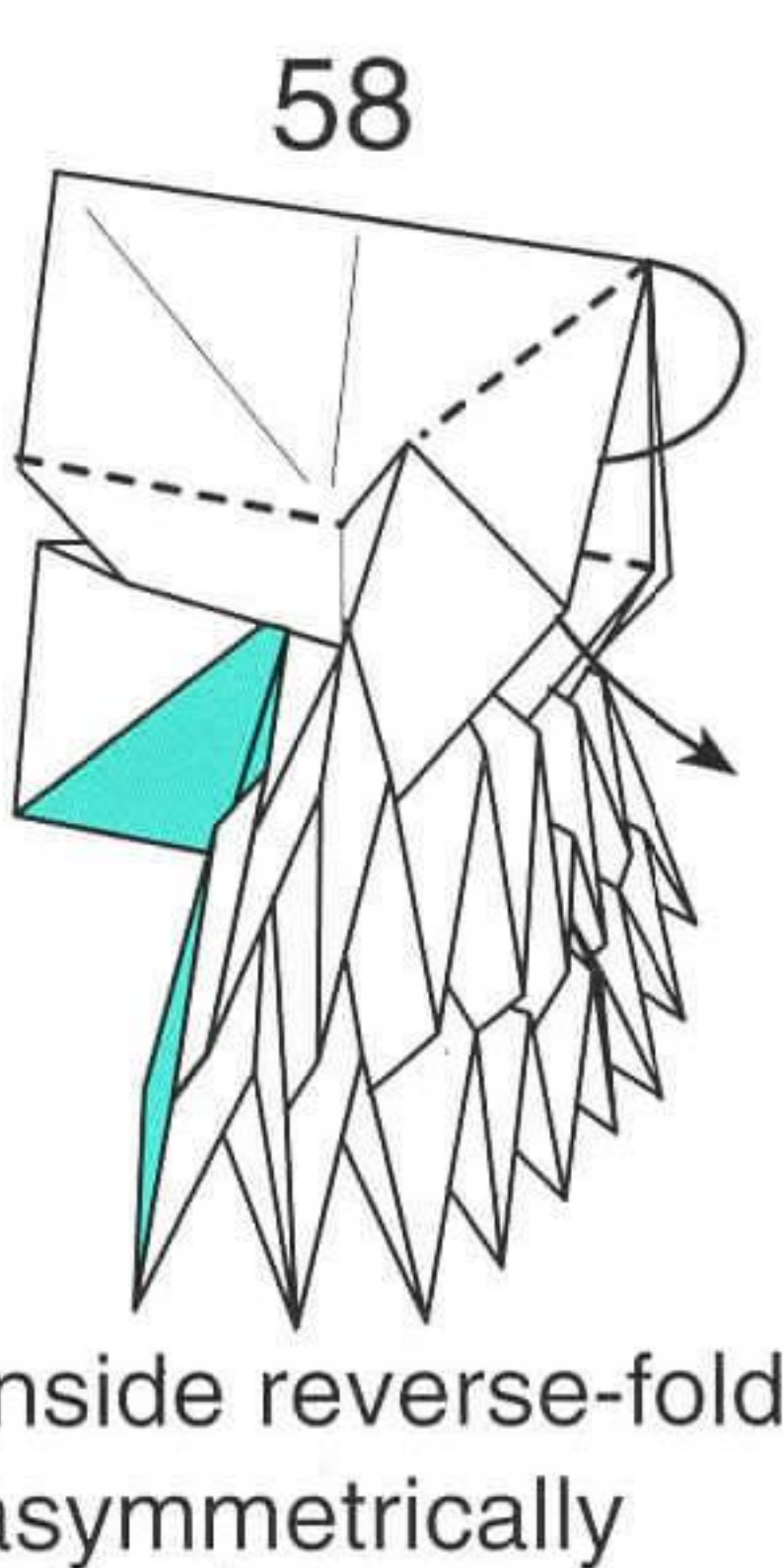
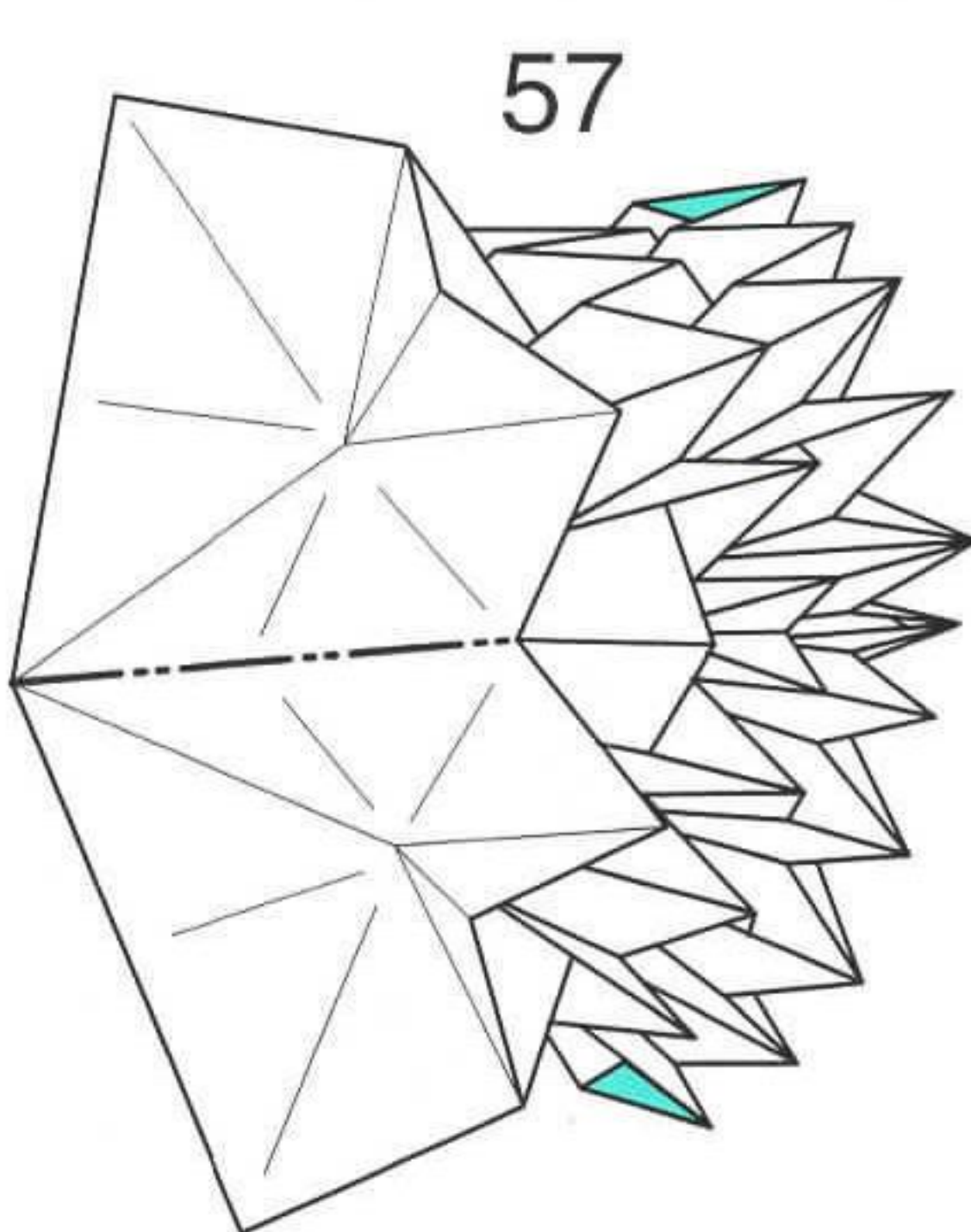


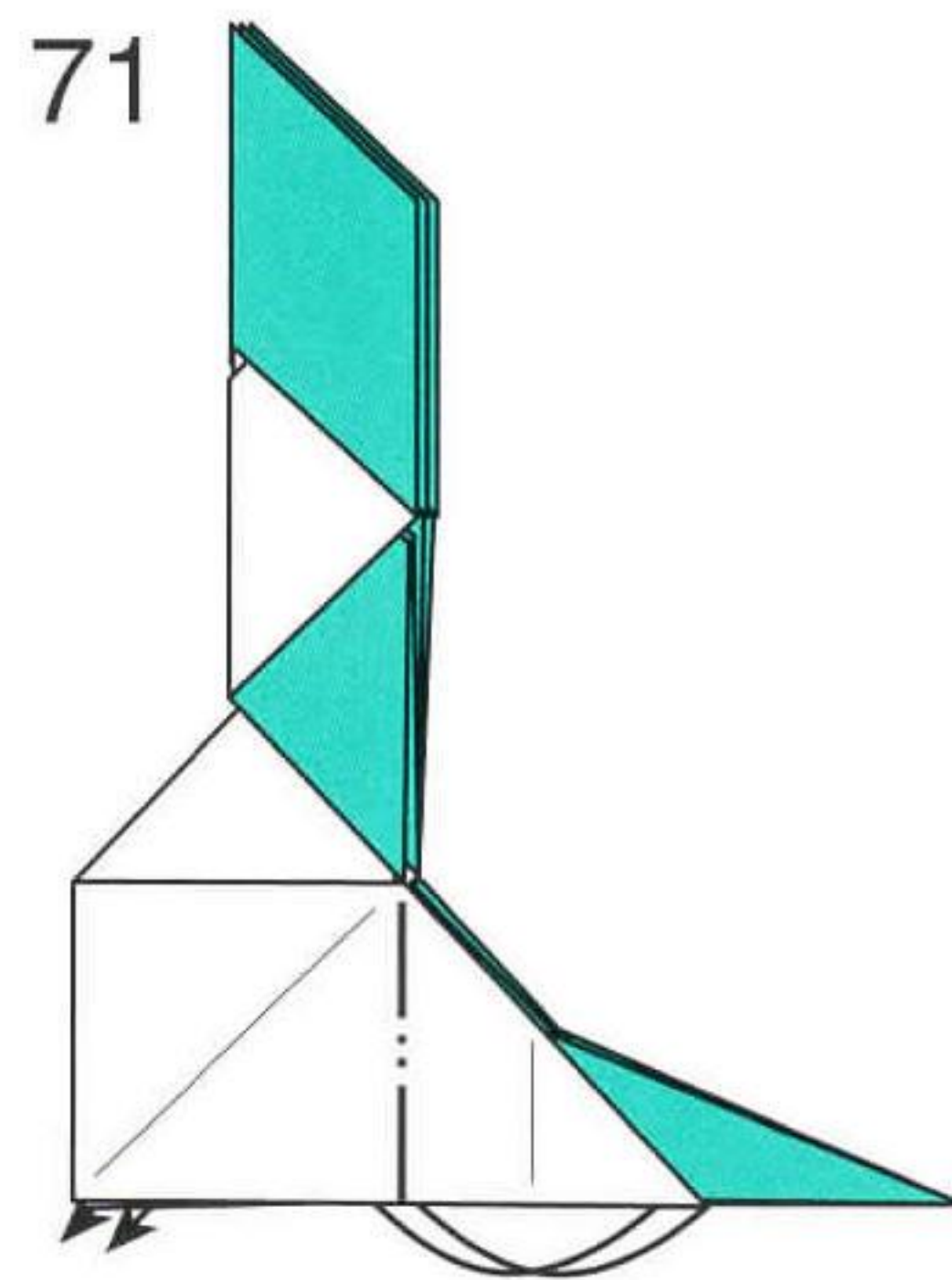
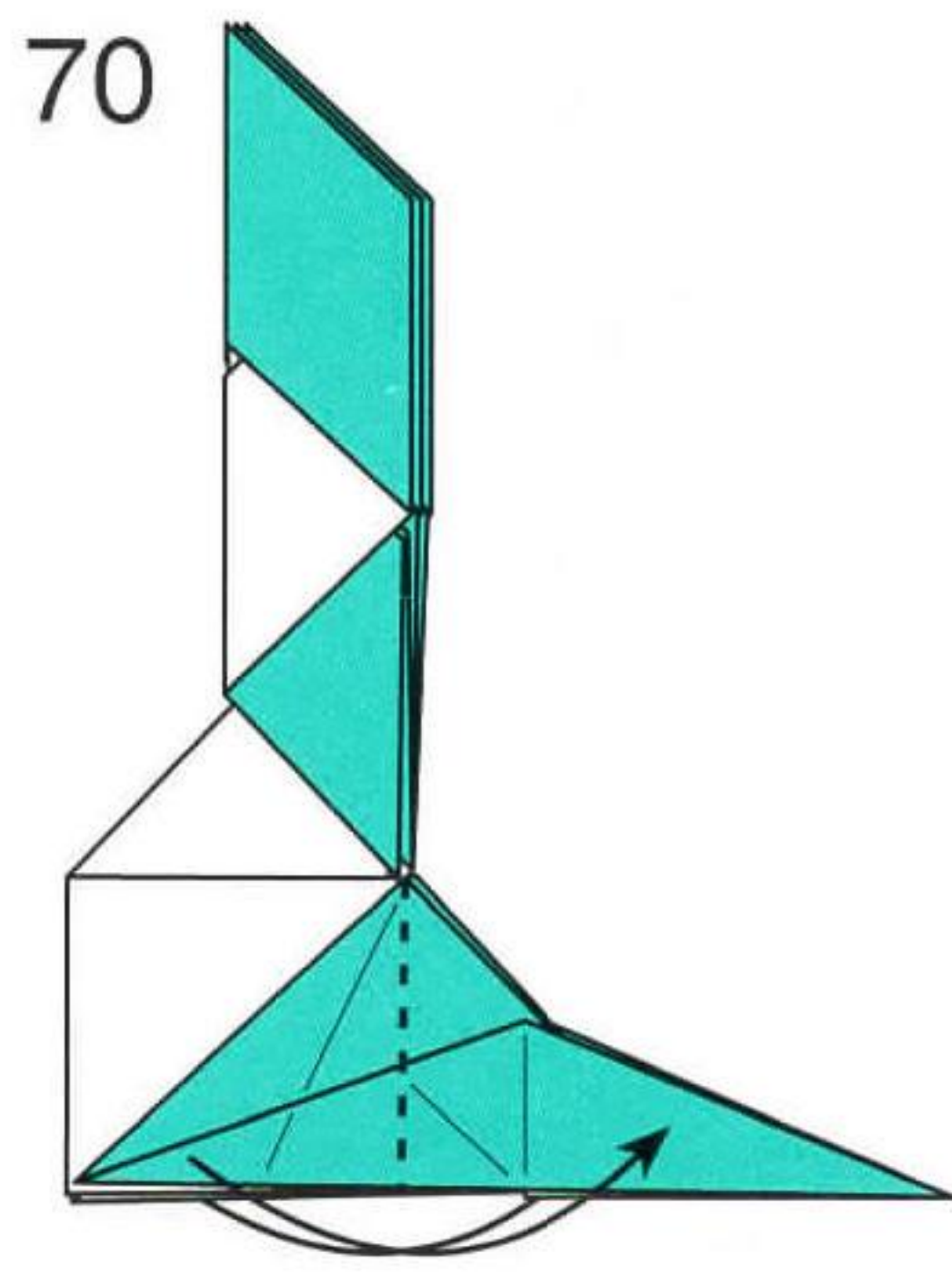
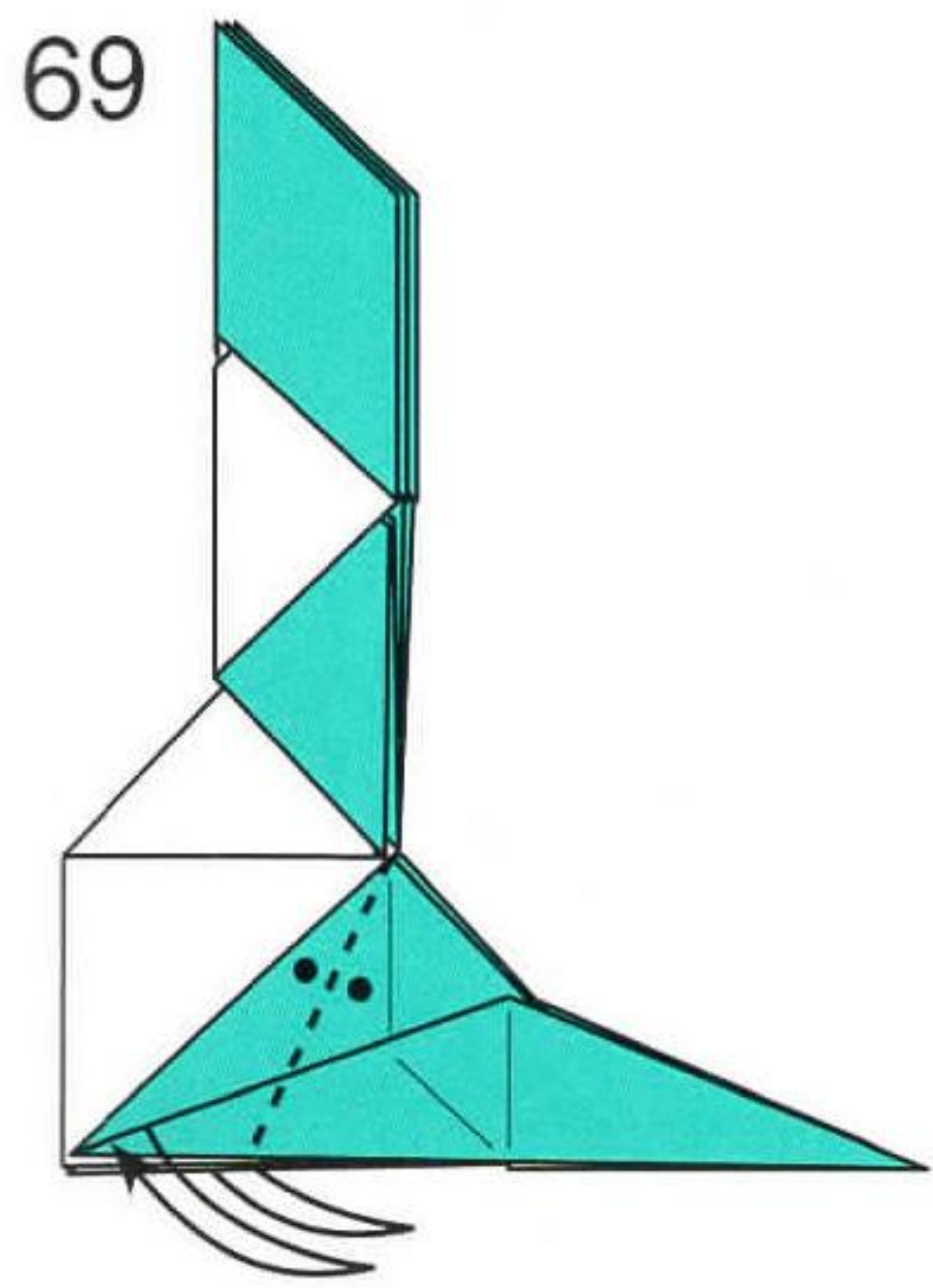




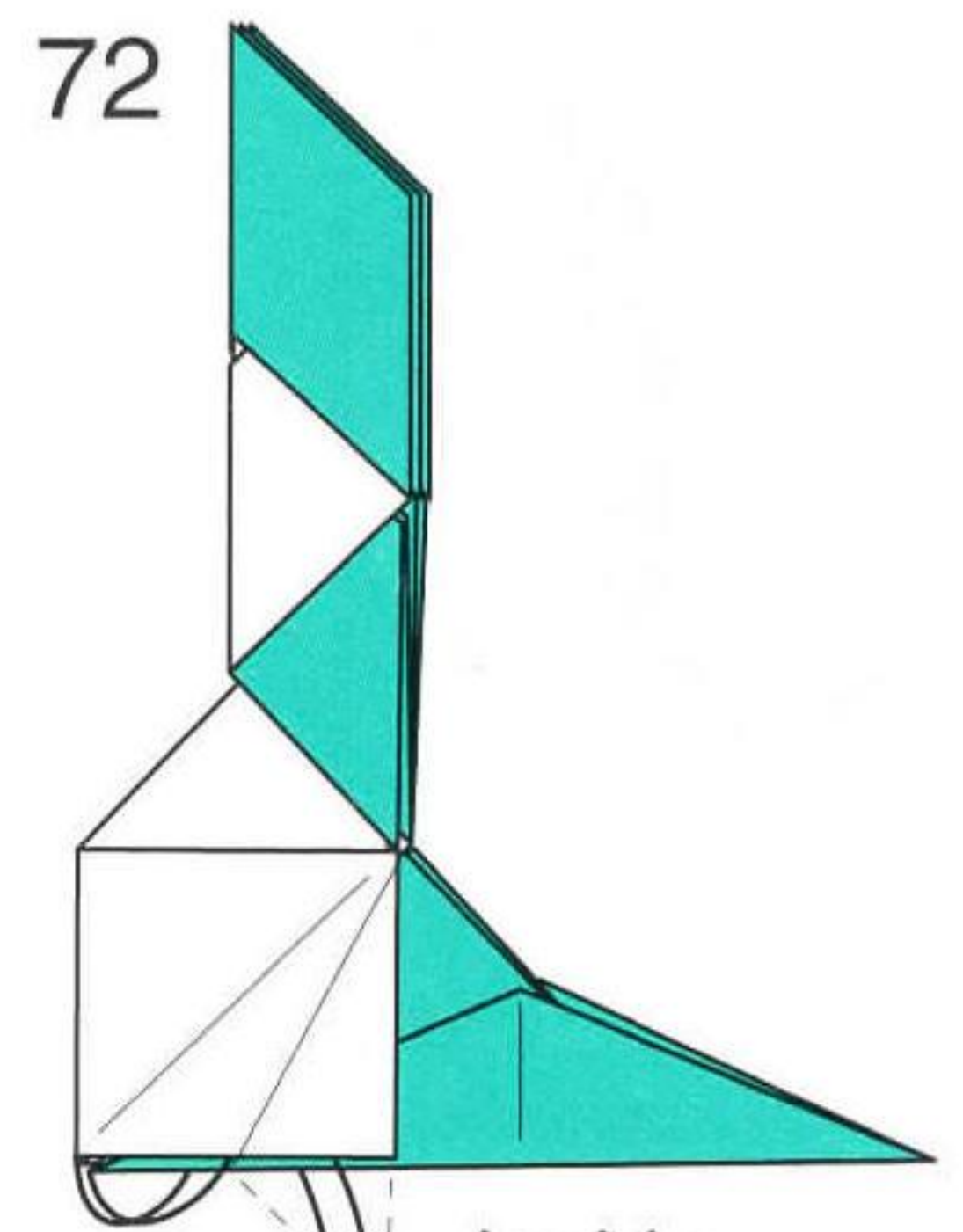


Lock the root of the fan in steps 56-58.

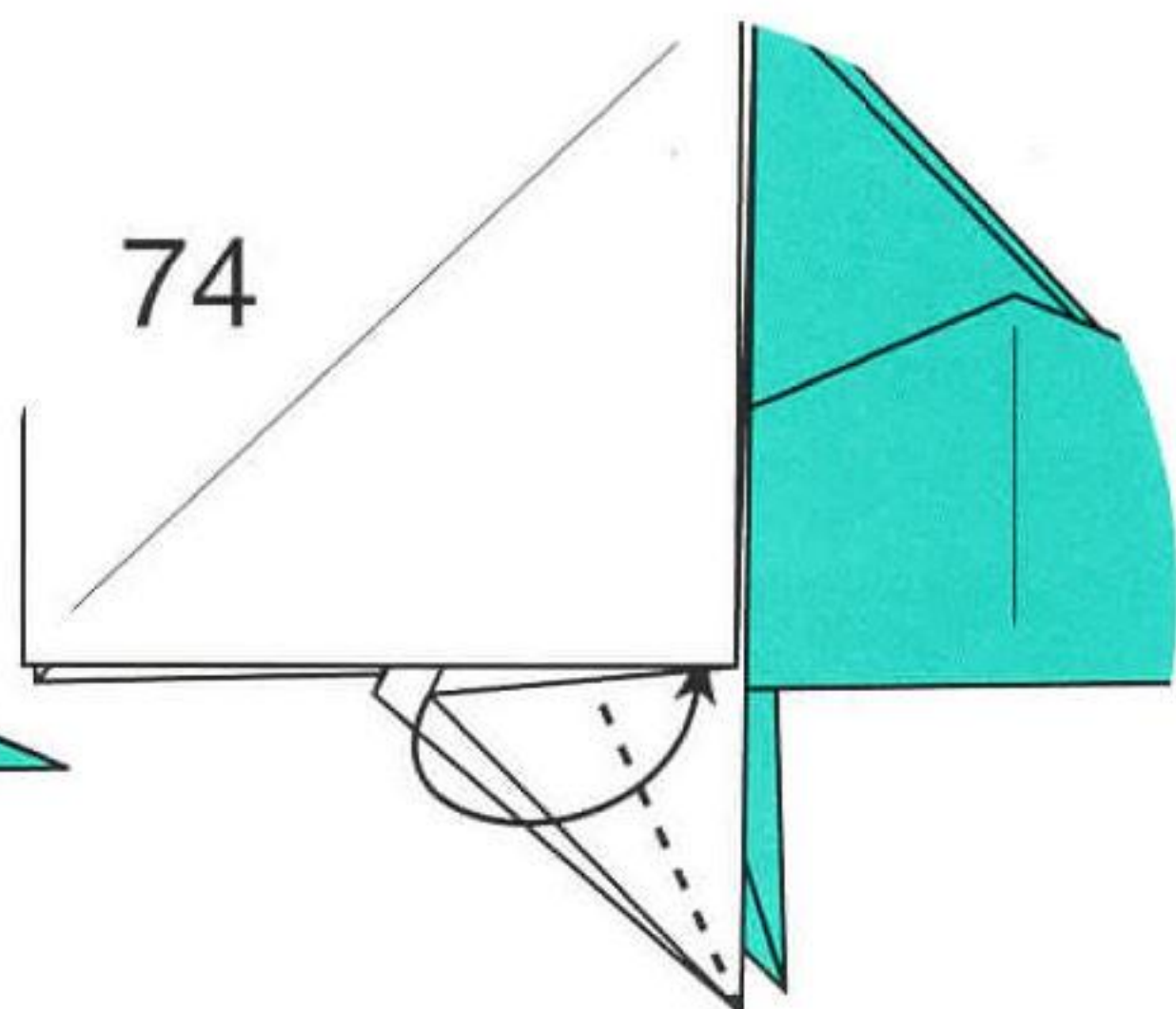
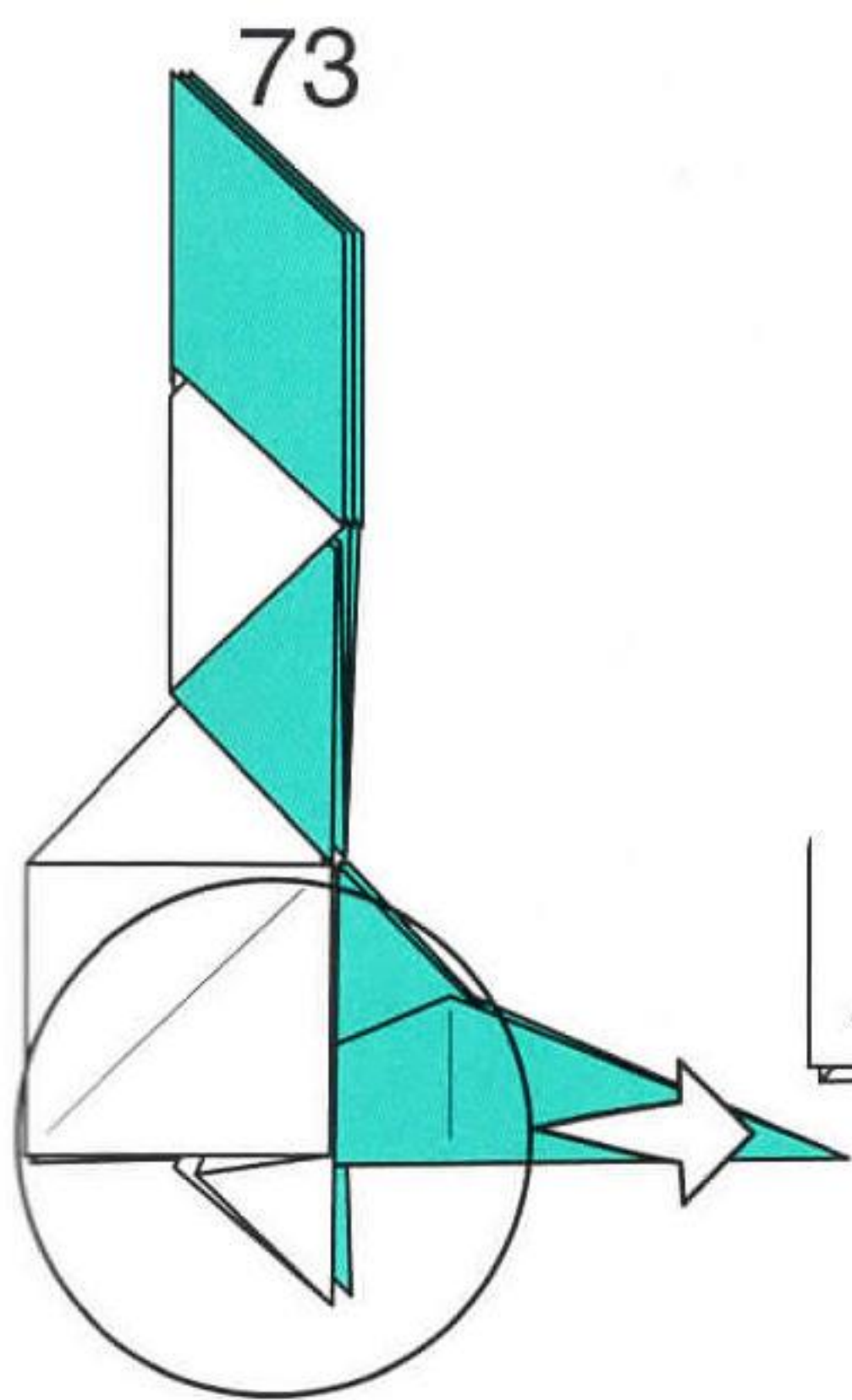




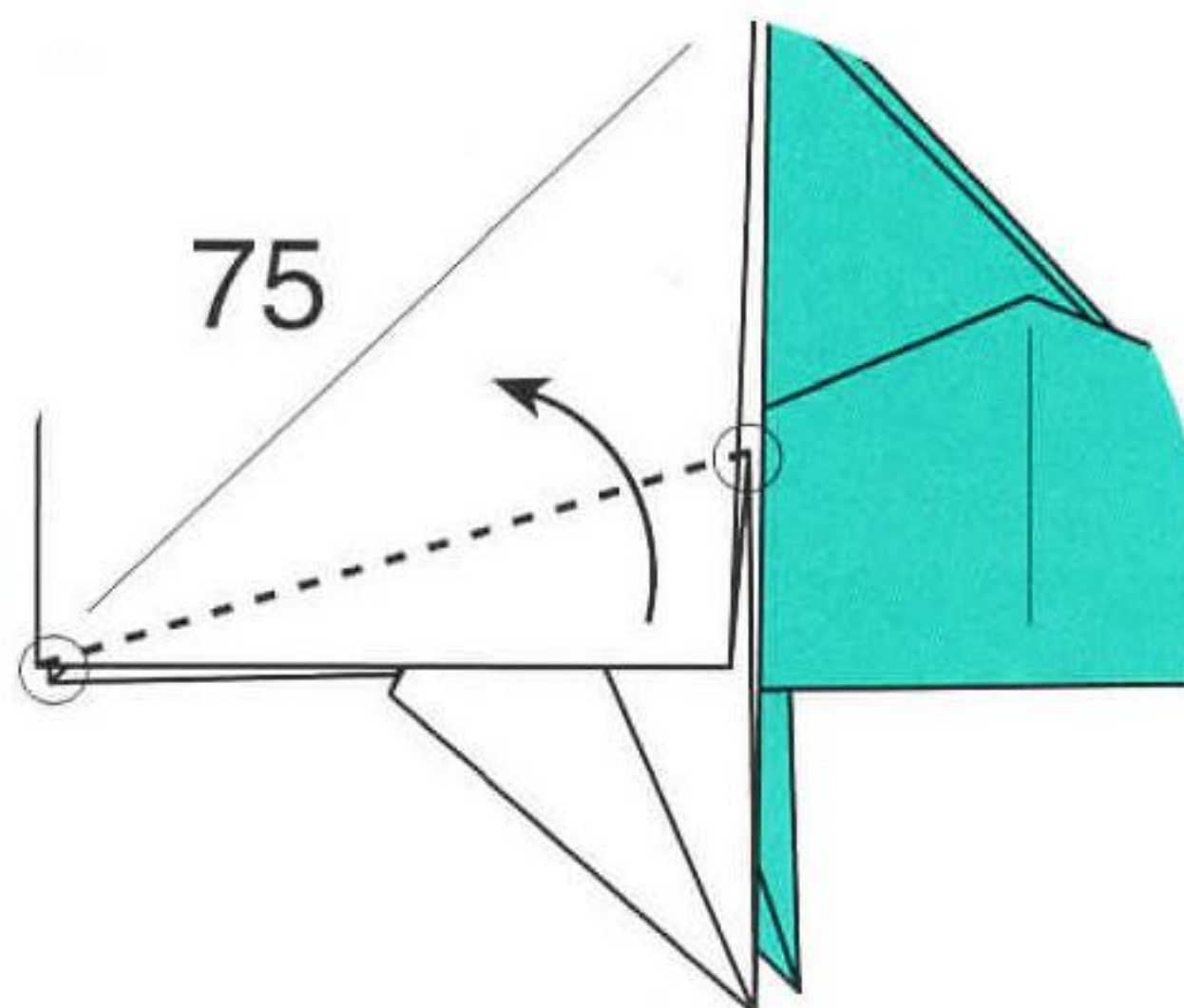
Inside reverse-fold



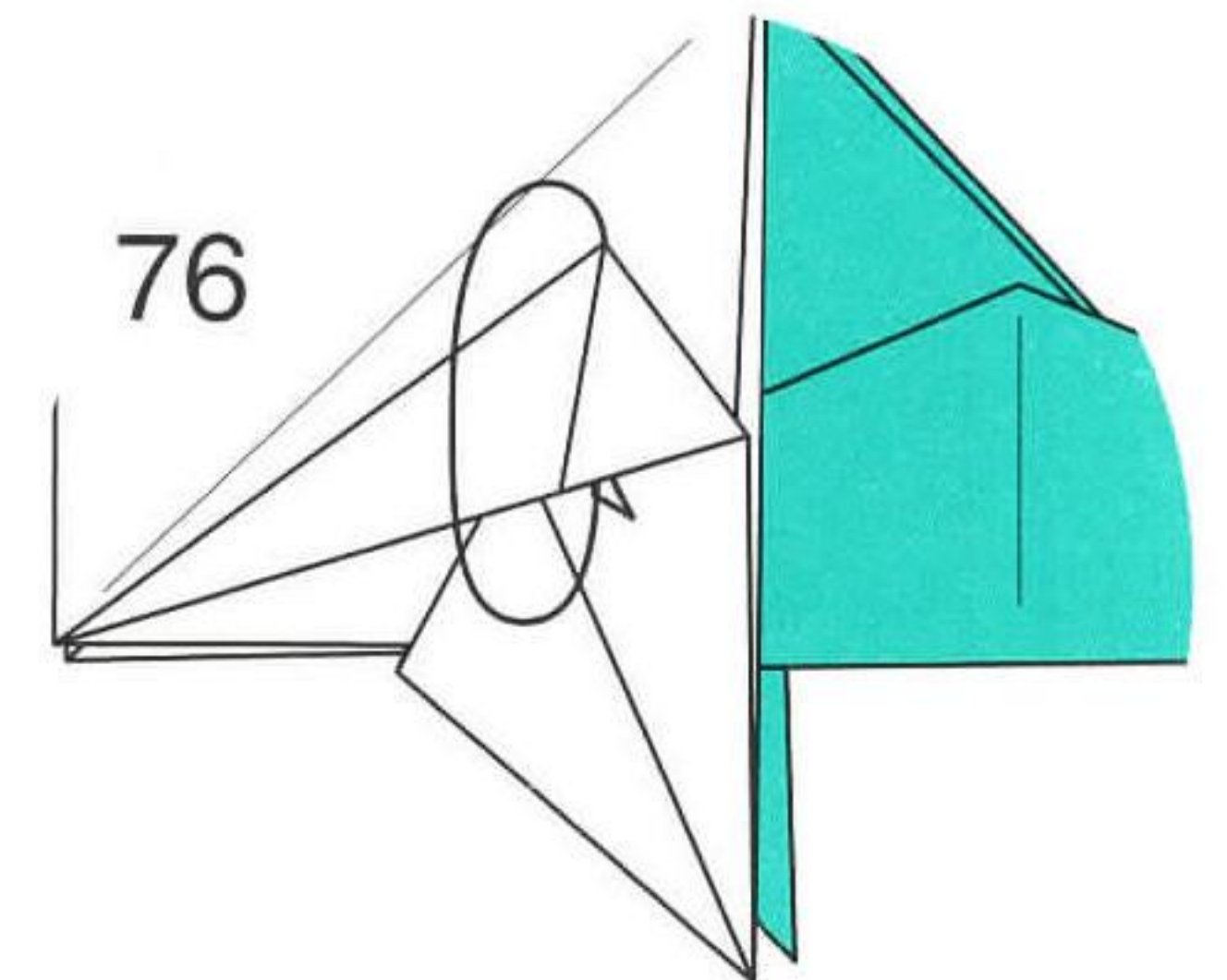
Inside reverse-fold



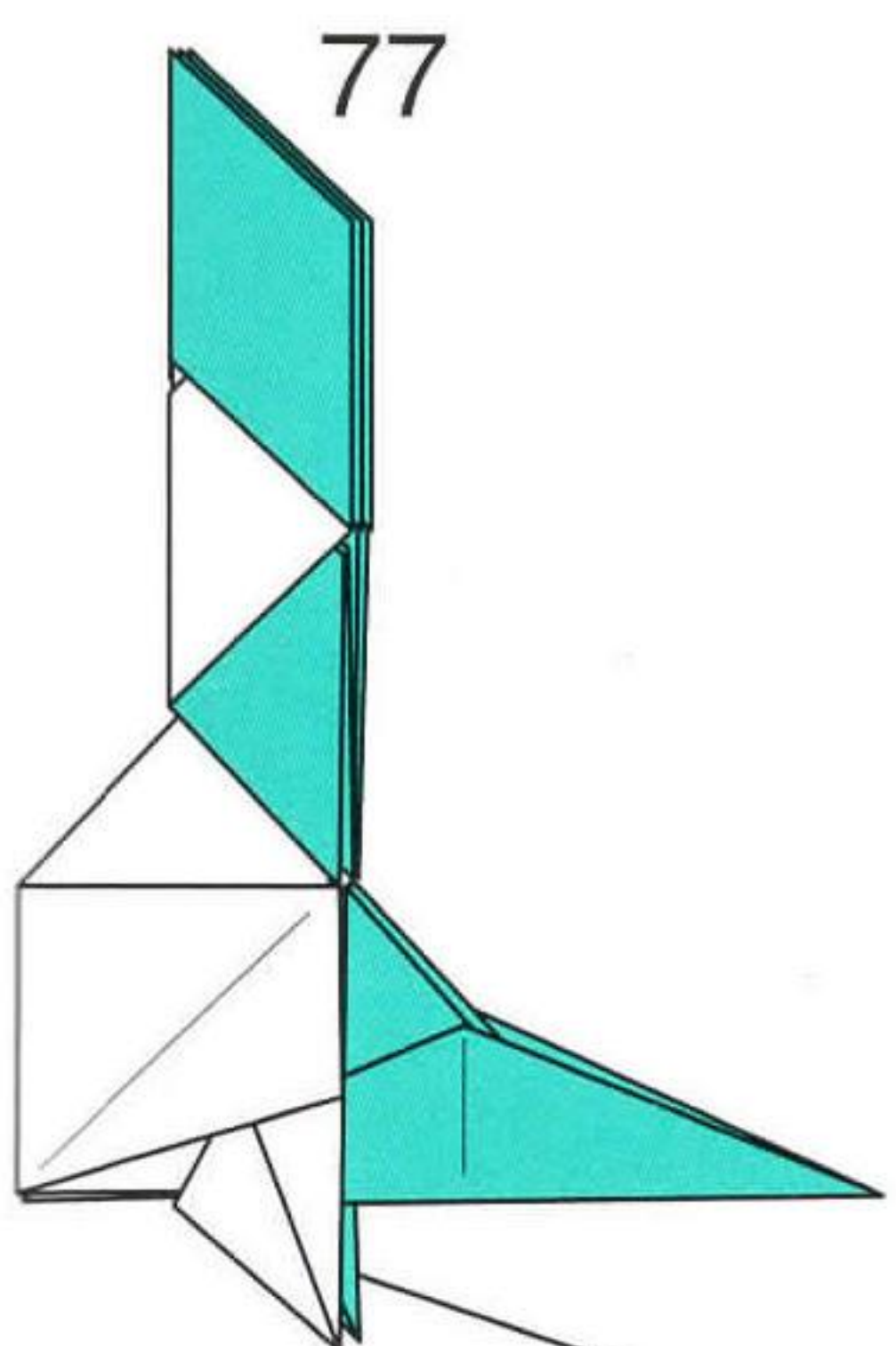
Inside reverse-fold



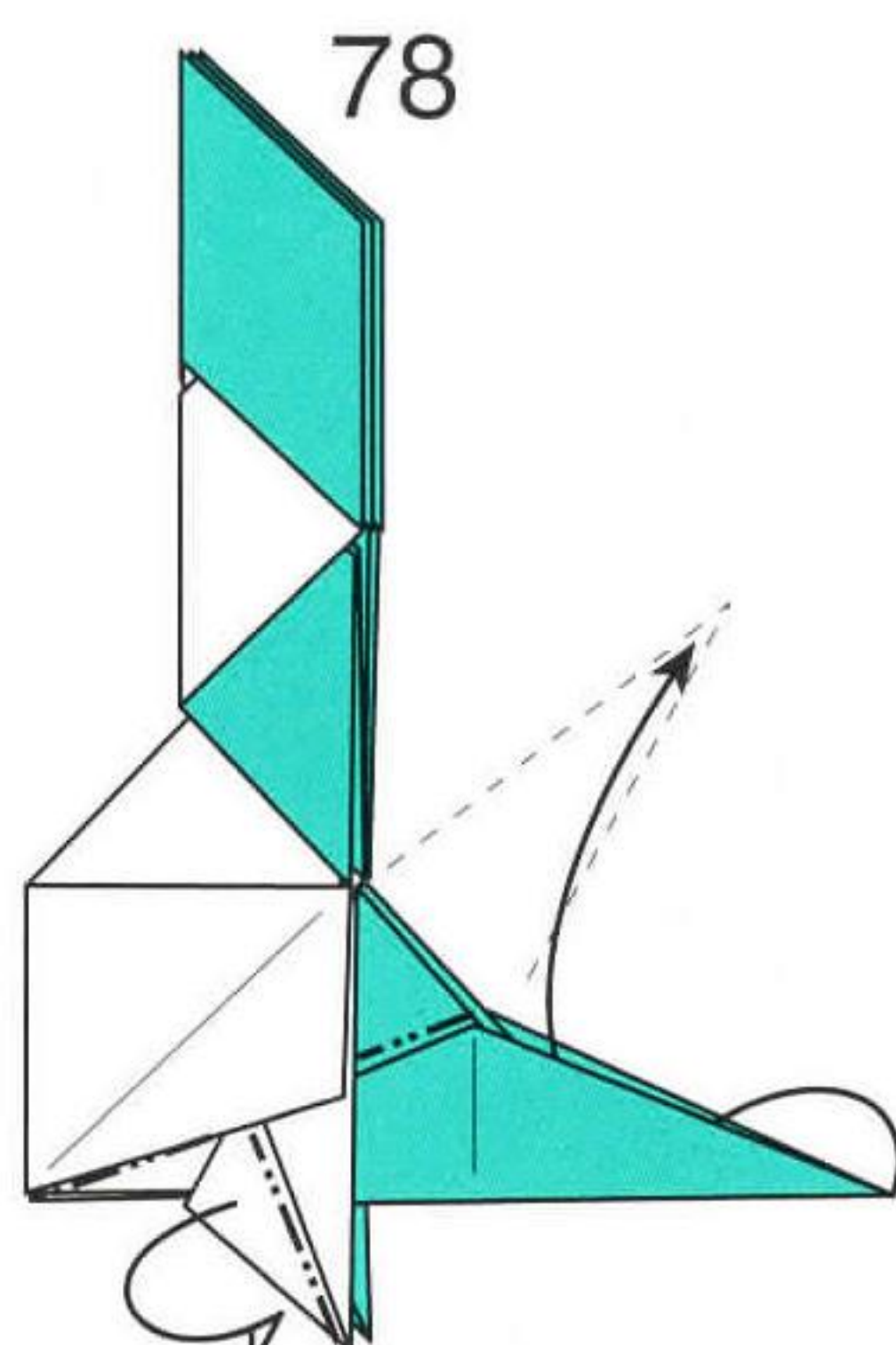
The crease does not bisect the angle.



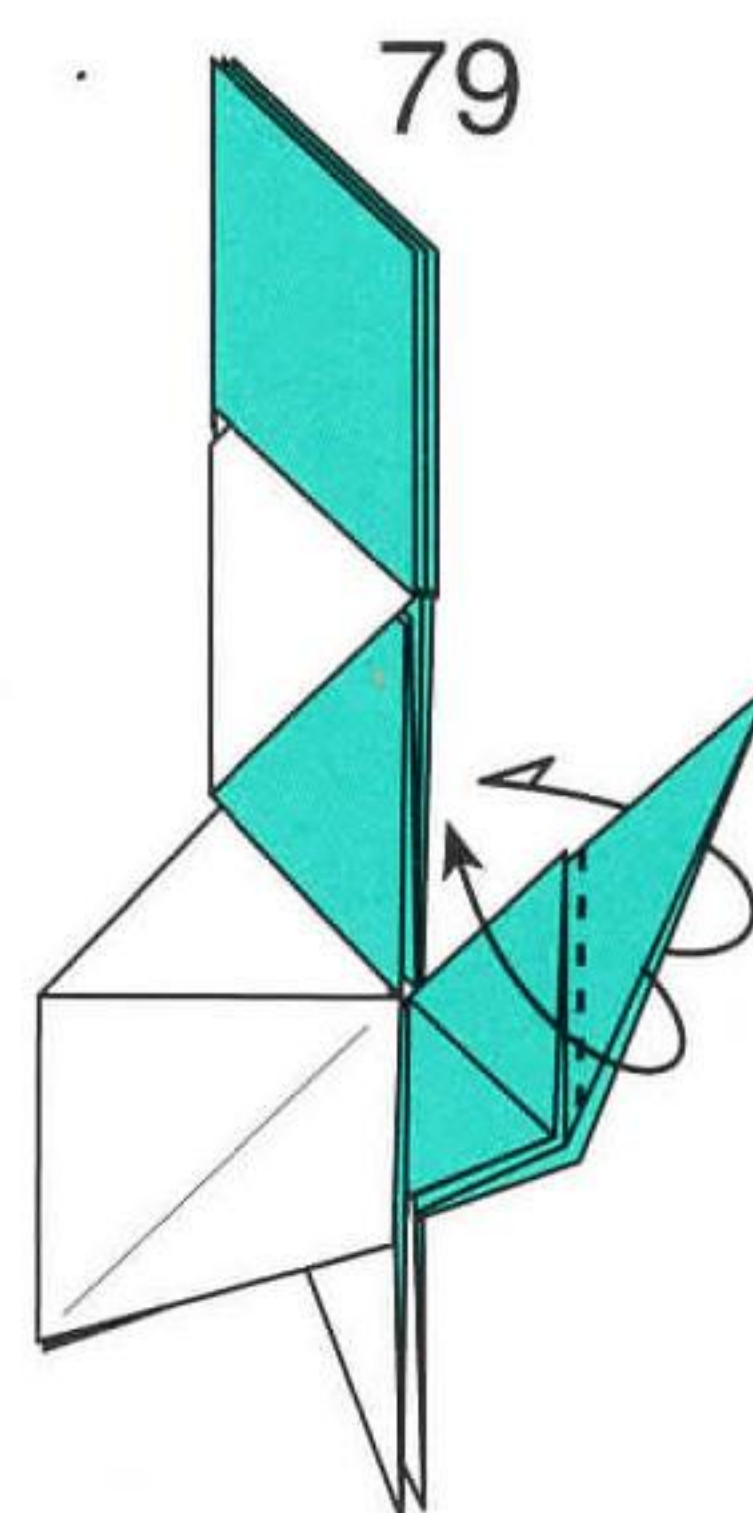
Reverse the valley fold made in step 75 to mountain.



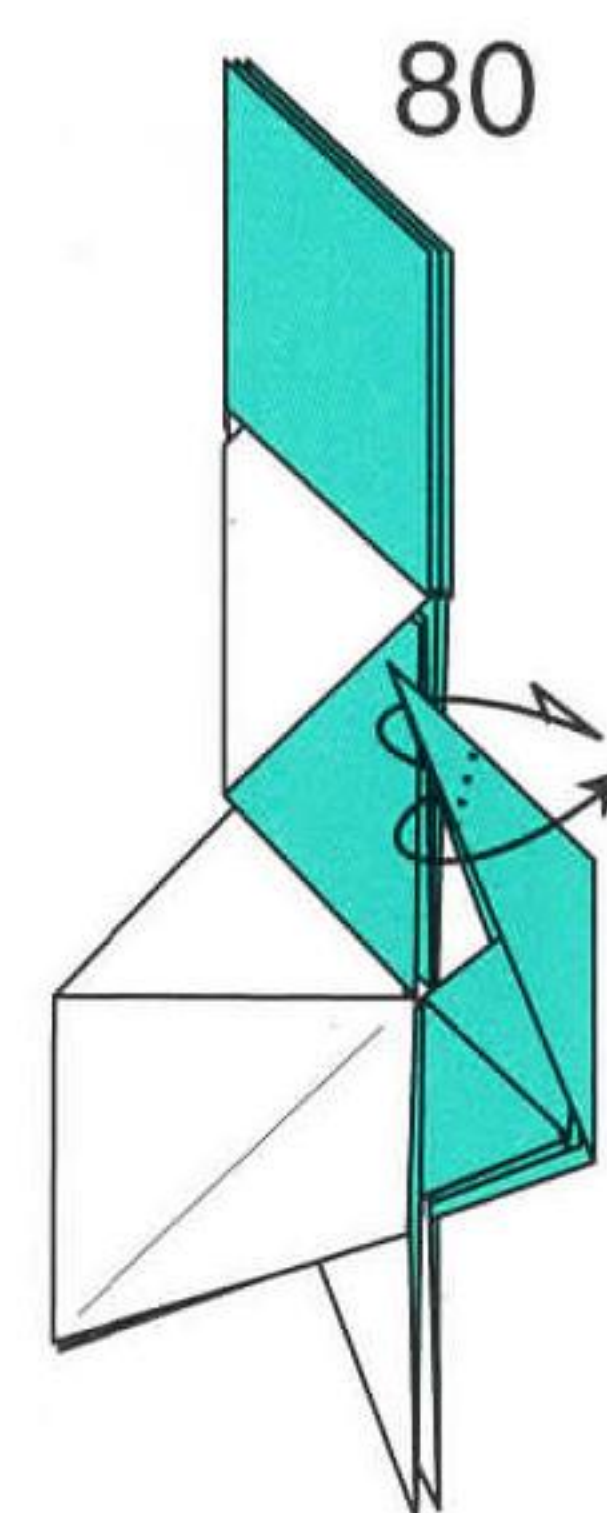
Repeat steps 74-76.



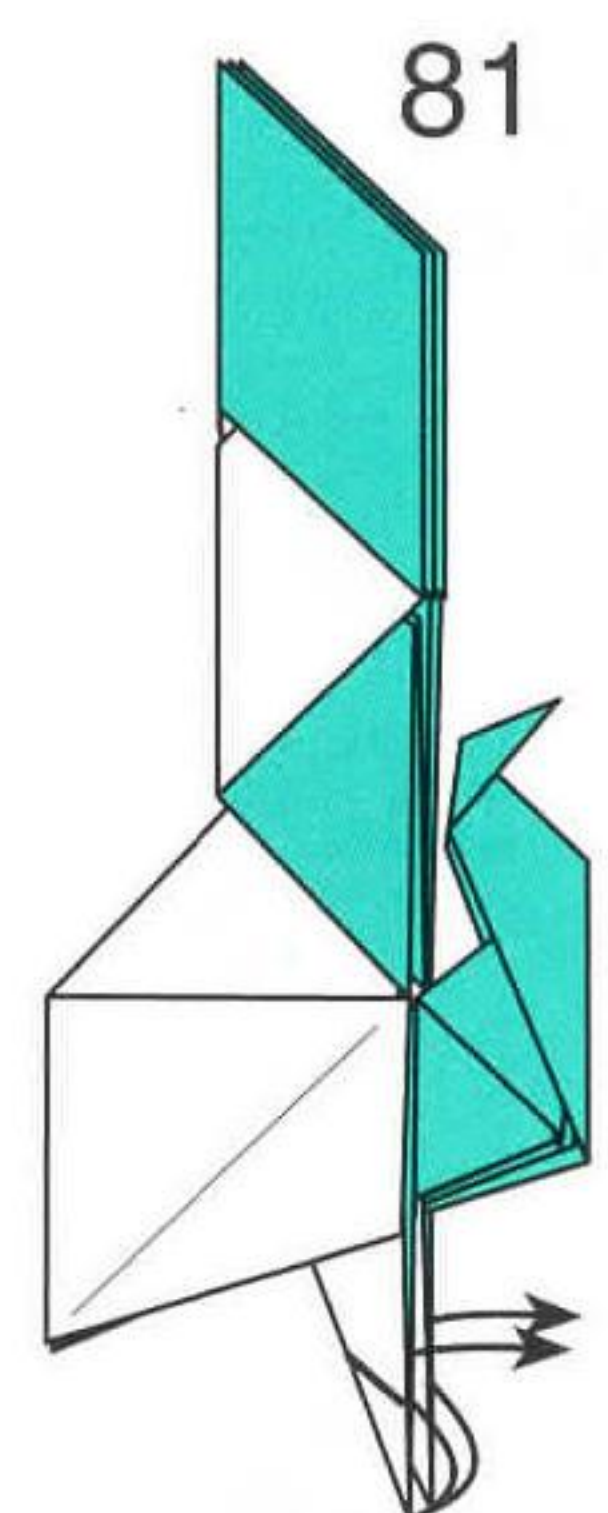
Inside reverse-fold



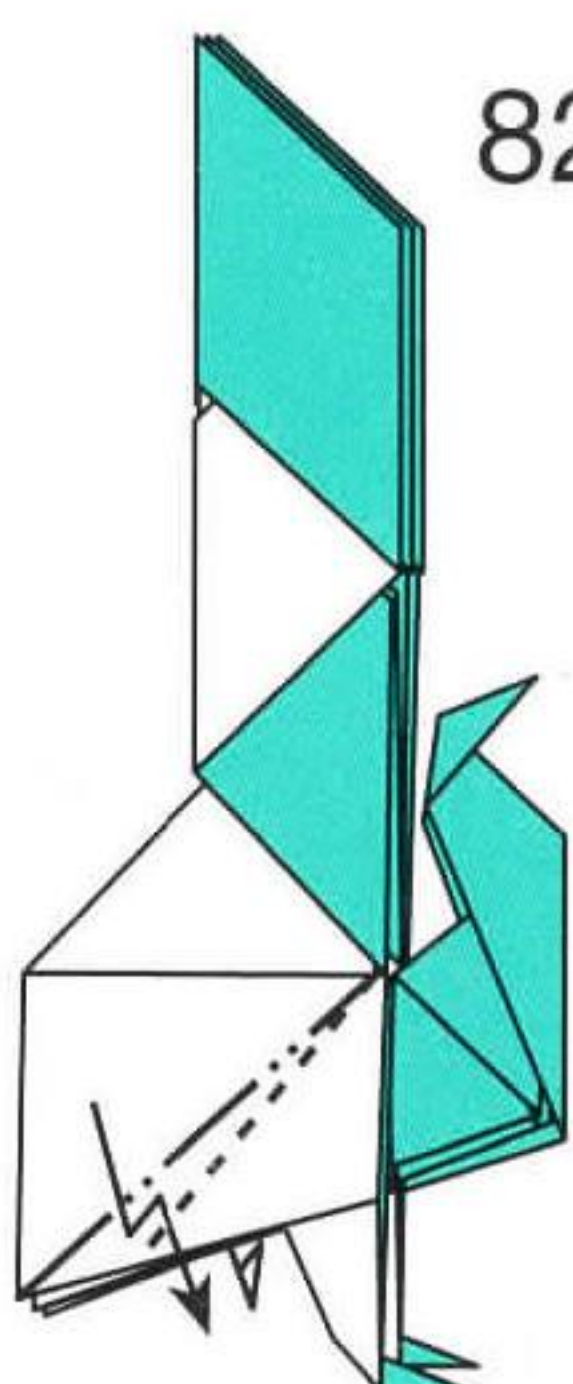
Outside reverse-fold



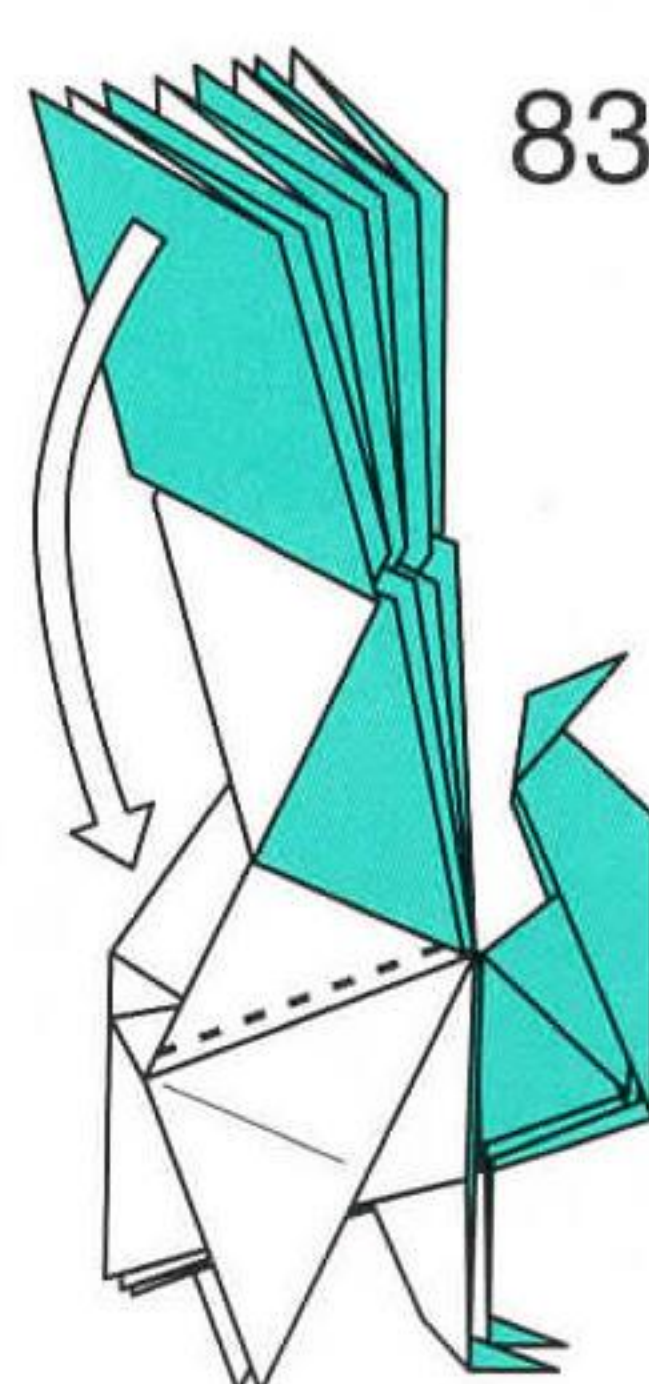
Outside reverse-fold



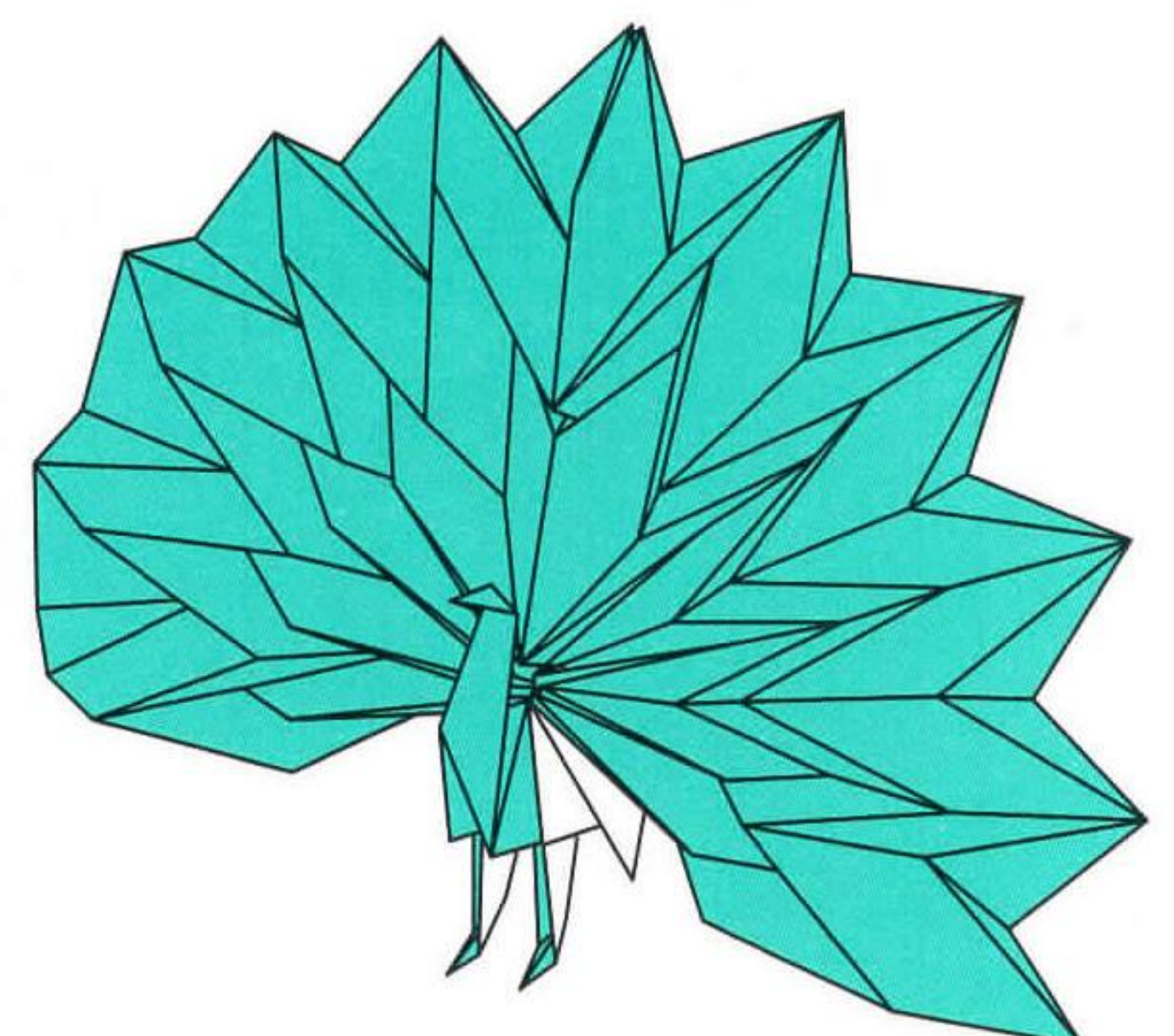
Inside reverse-fold



Crimp the outer layers only.

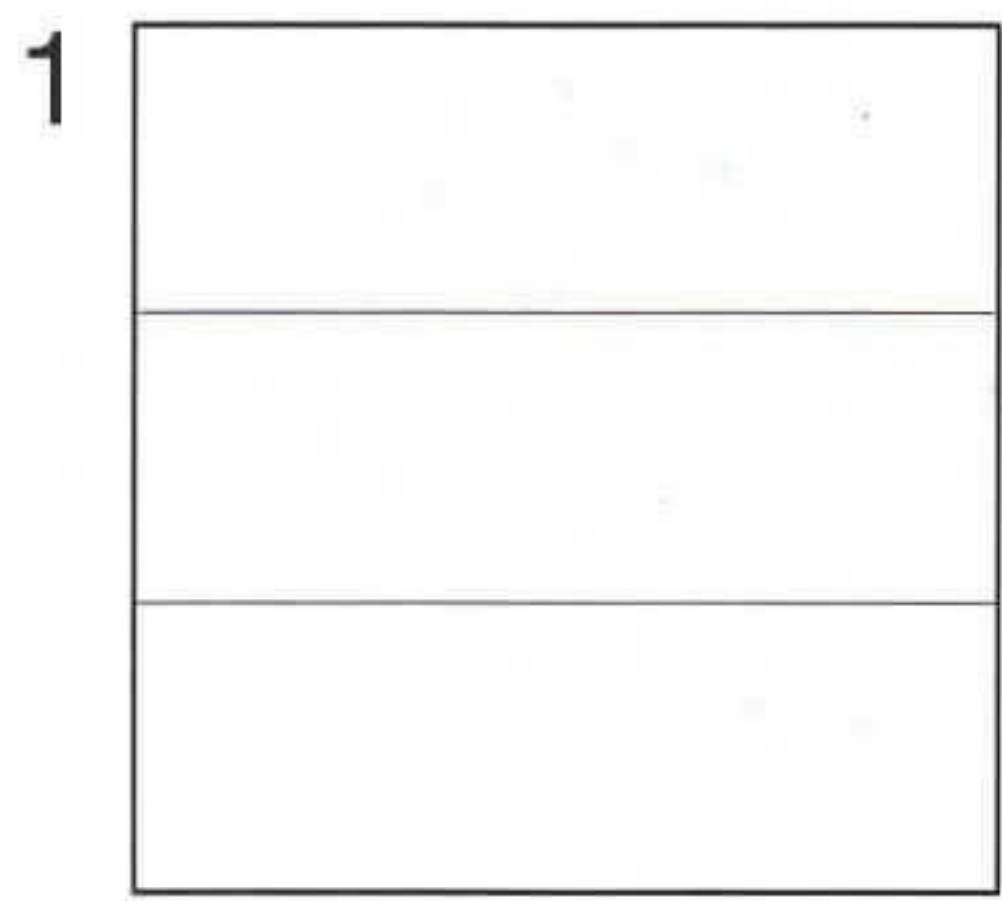


Make the model stand on its wings and legs.

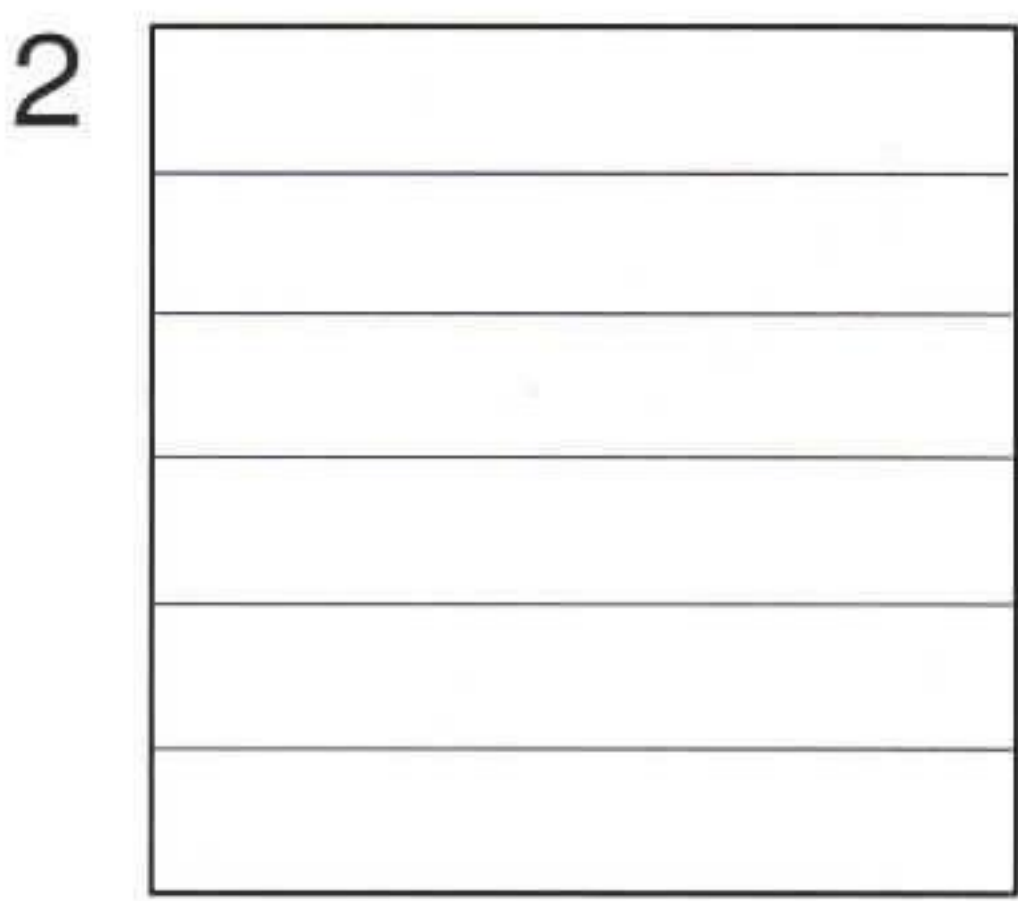


Finished.

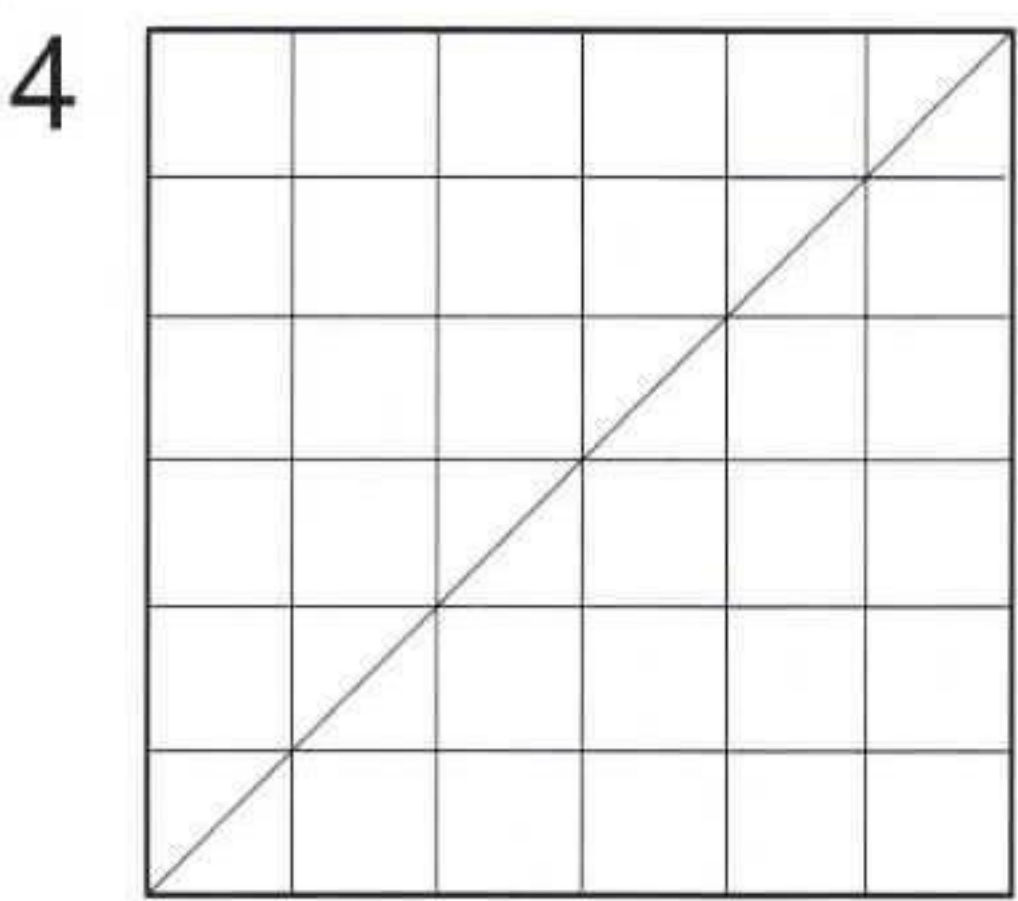
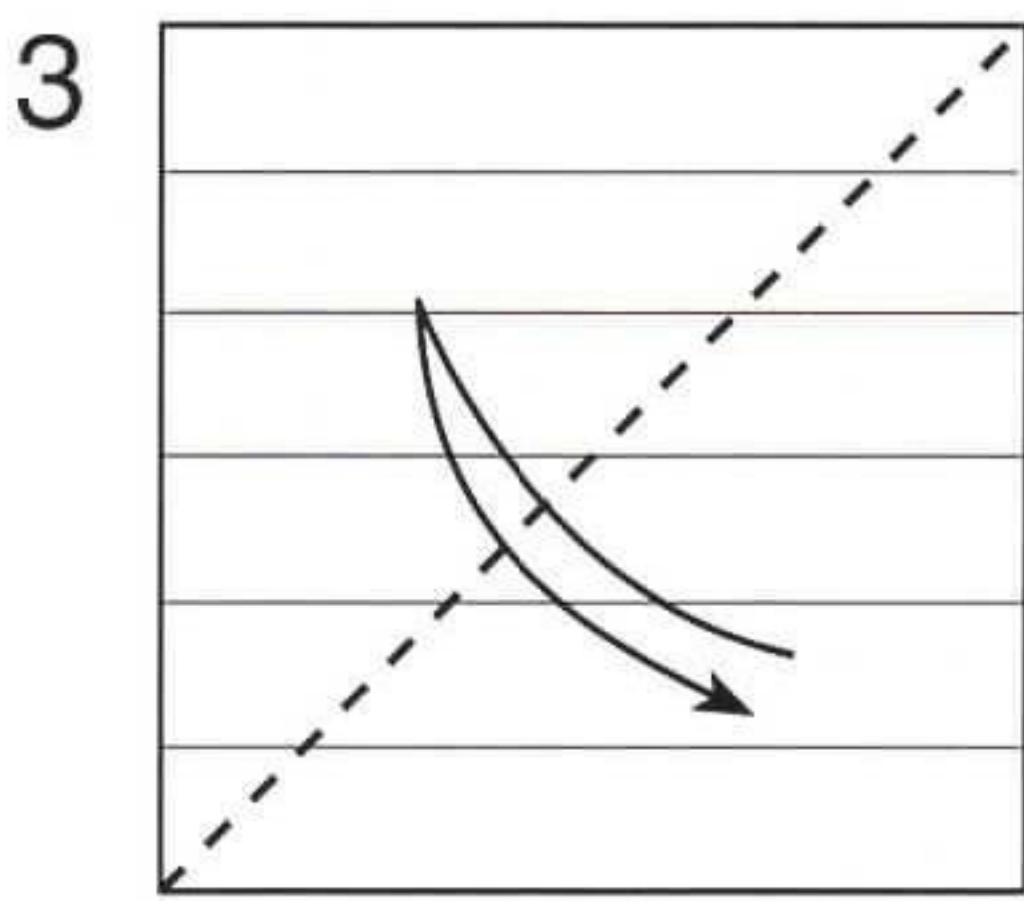
Peacock 2



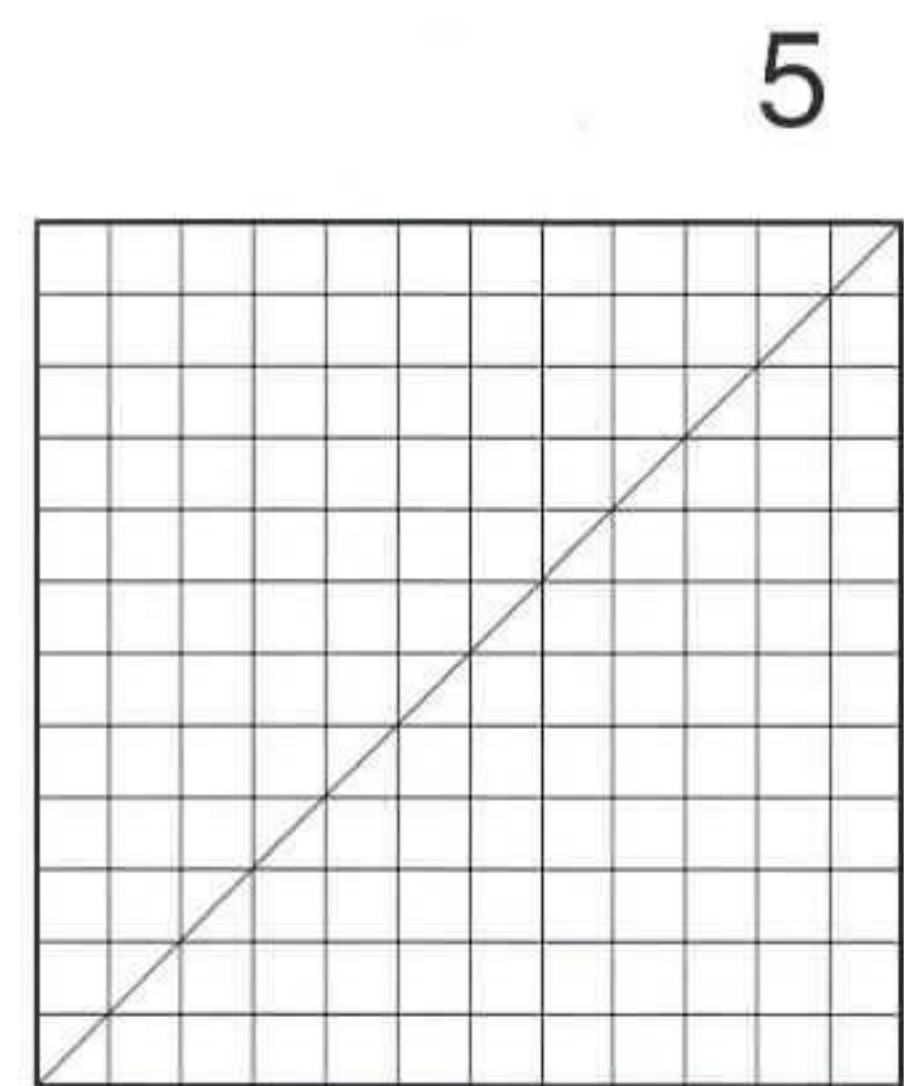
1
Divide the side into three.



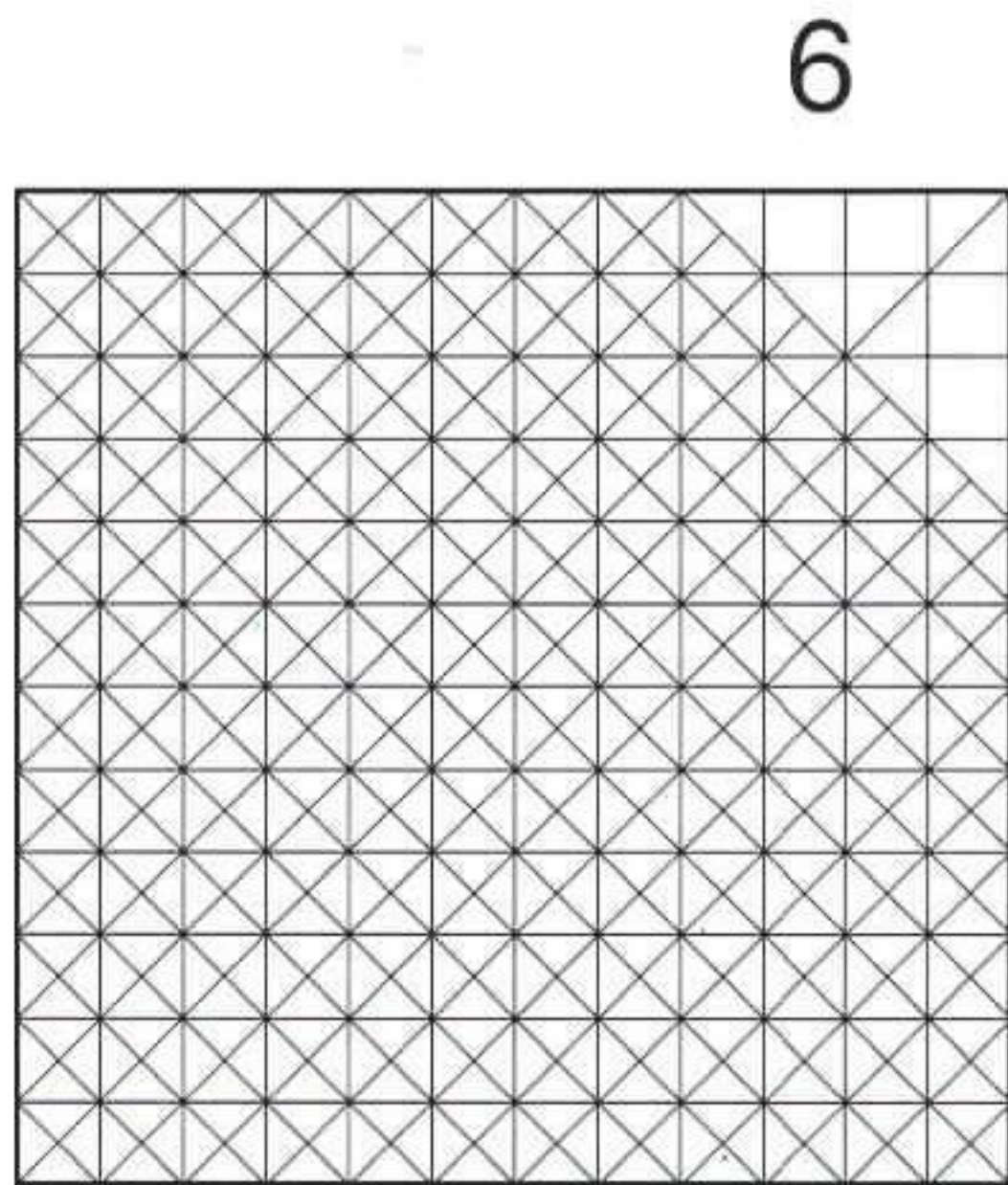
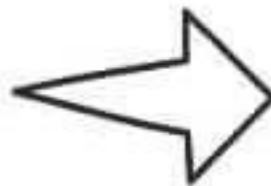
2
Divide the side into six.



4
Divide the other side into six.



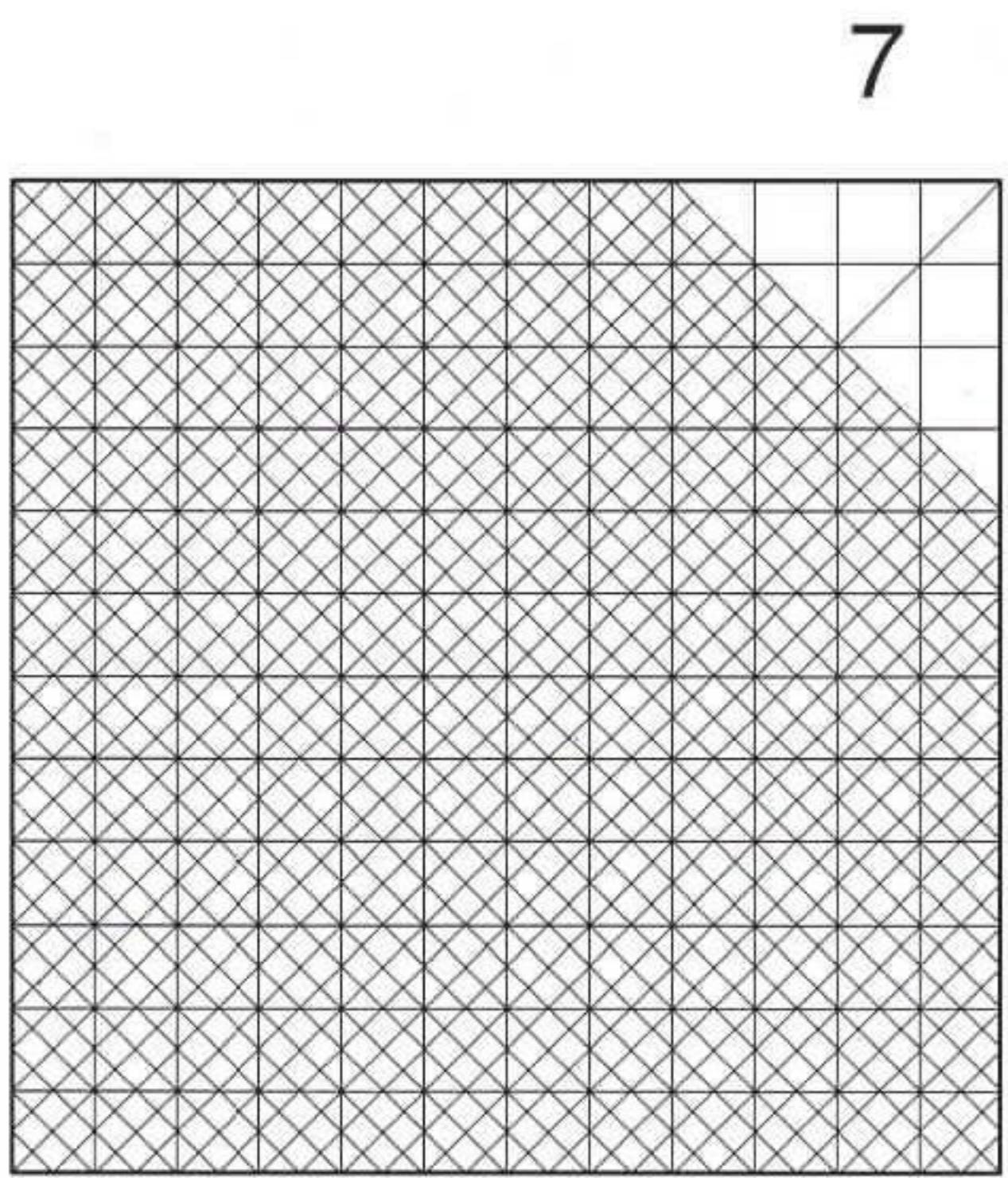
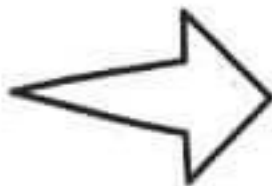
5
Divide both sides into twelve.



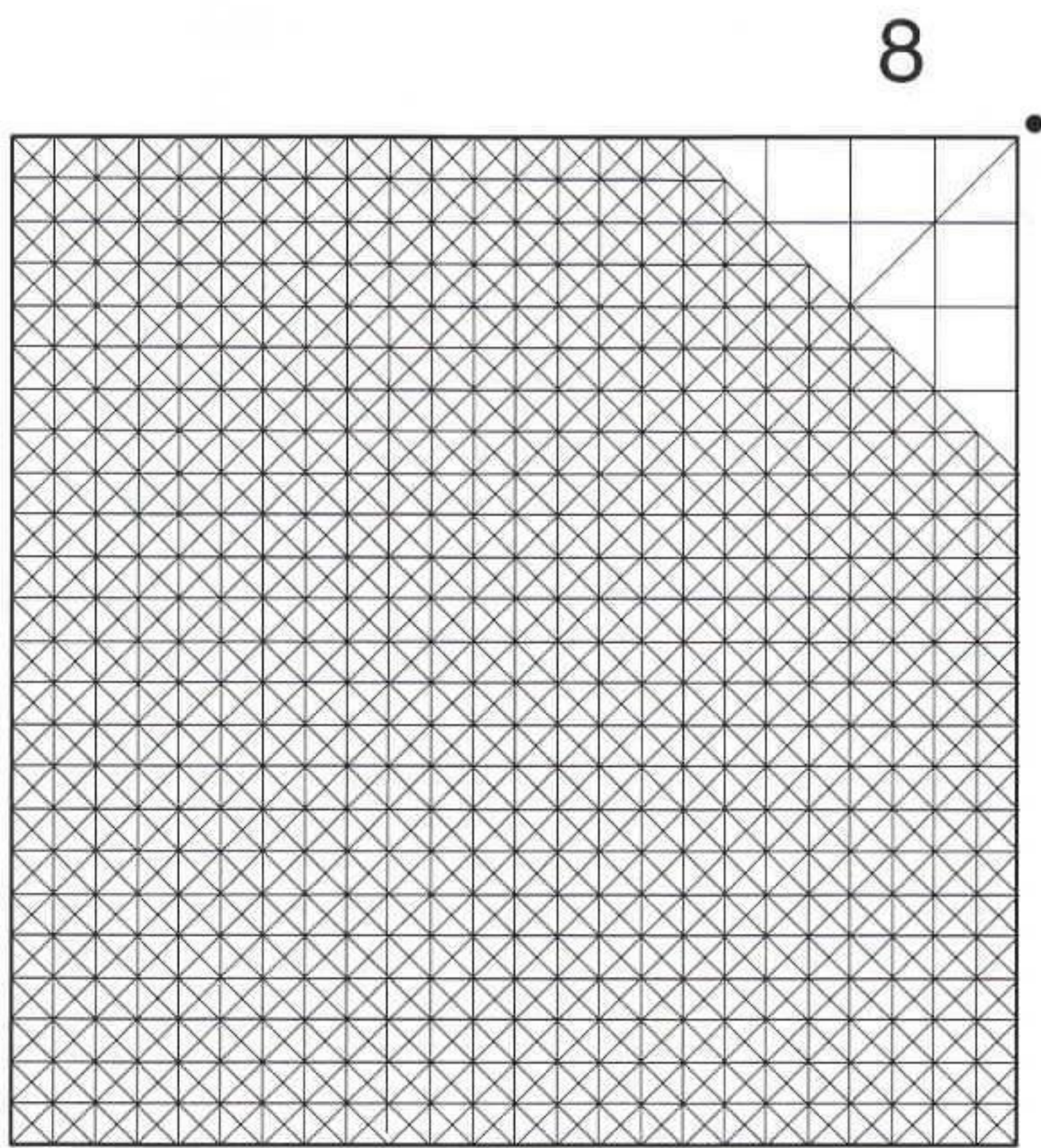
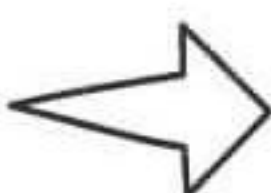
6
Fold and unfold the diagonals of small squares.



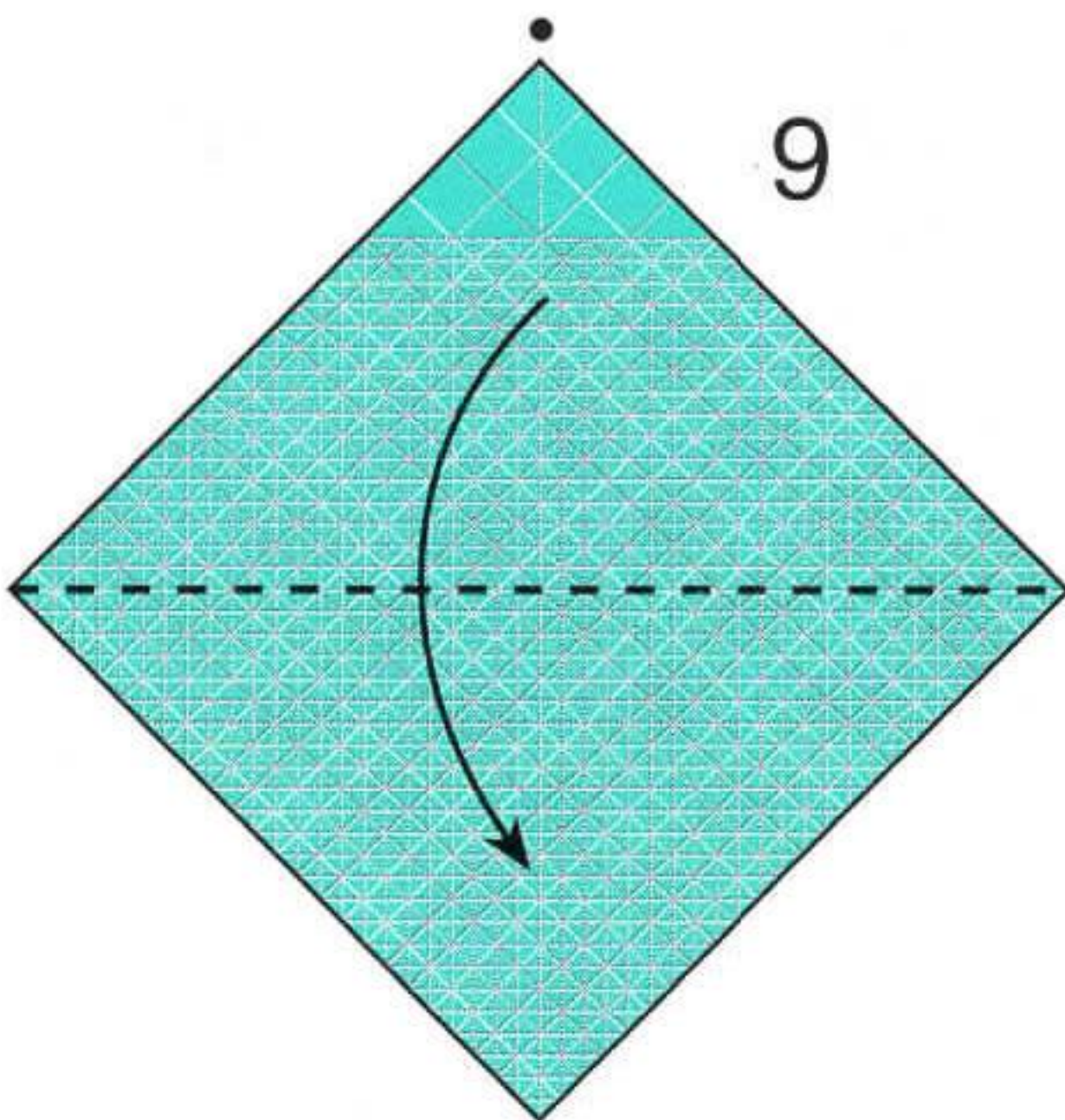
Don't crease in this area.



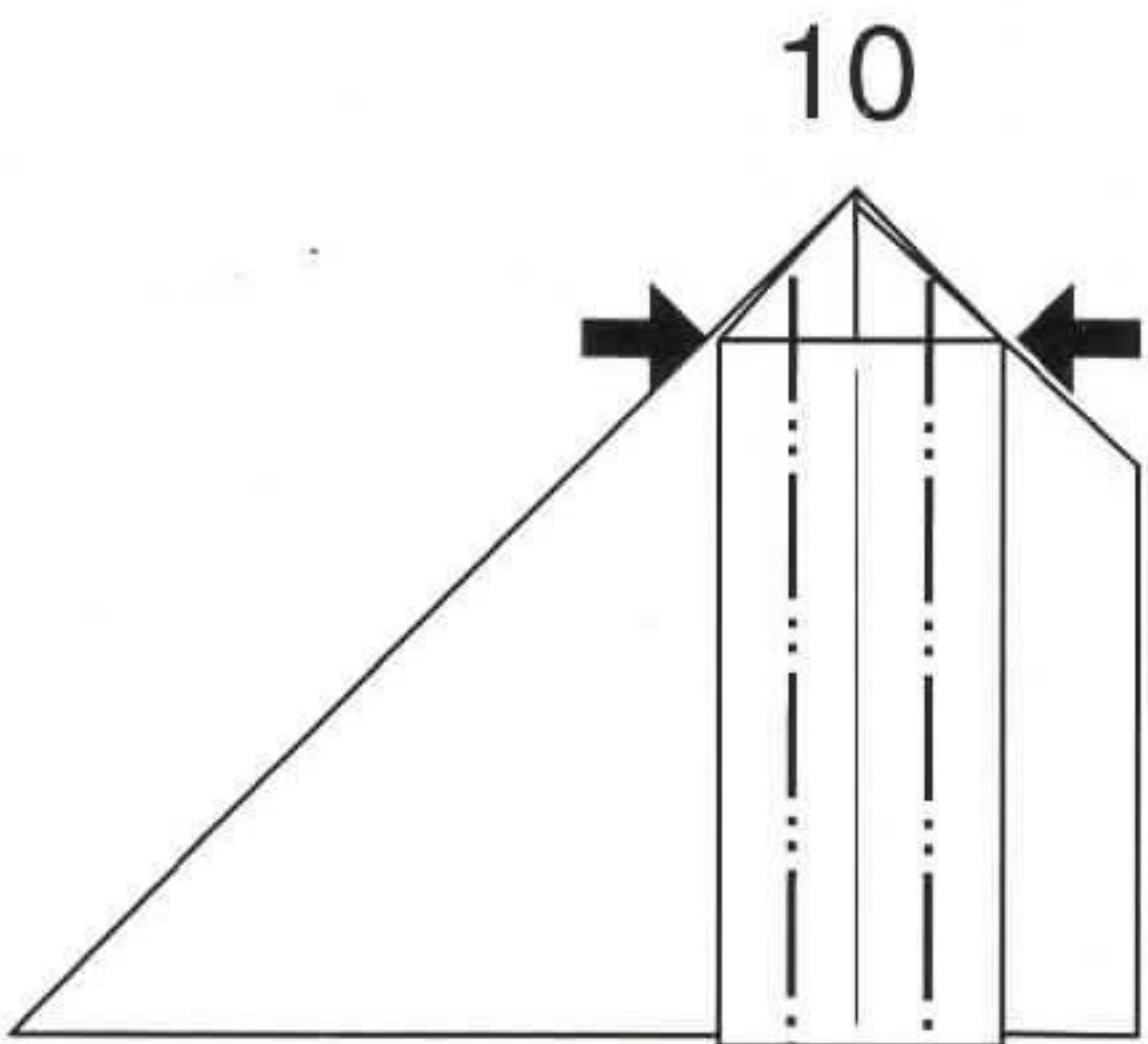
7
Fold and unfold more diagonals in half.



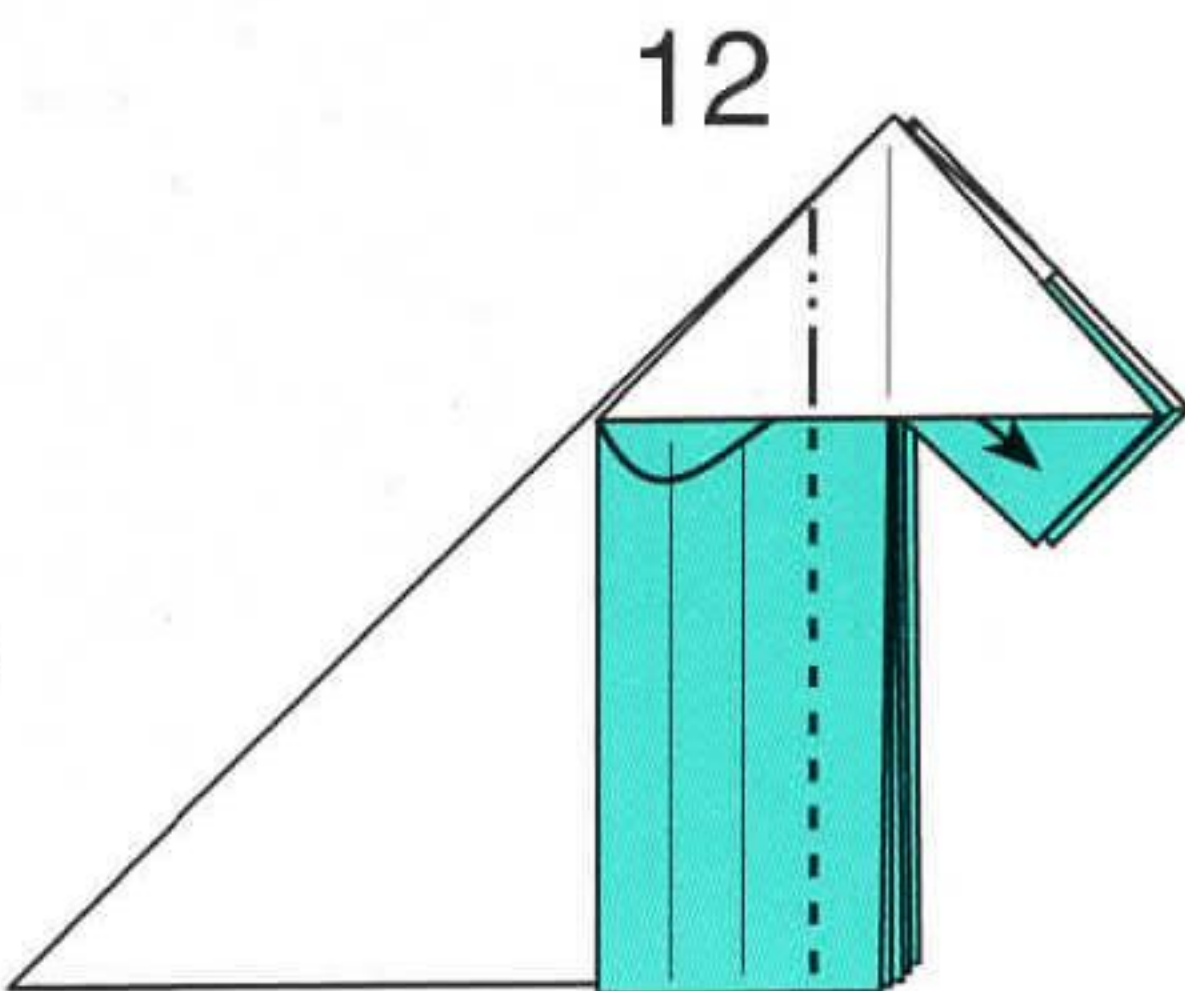
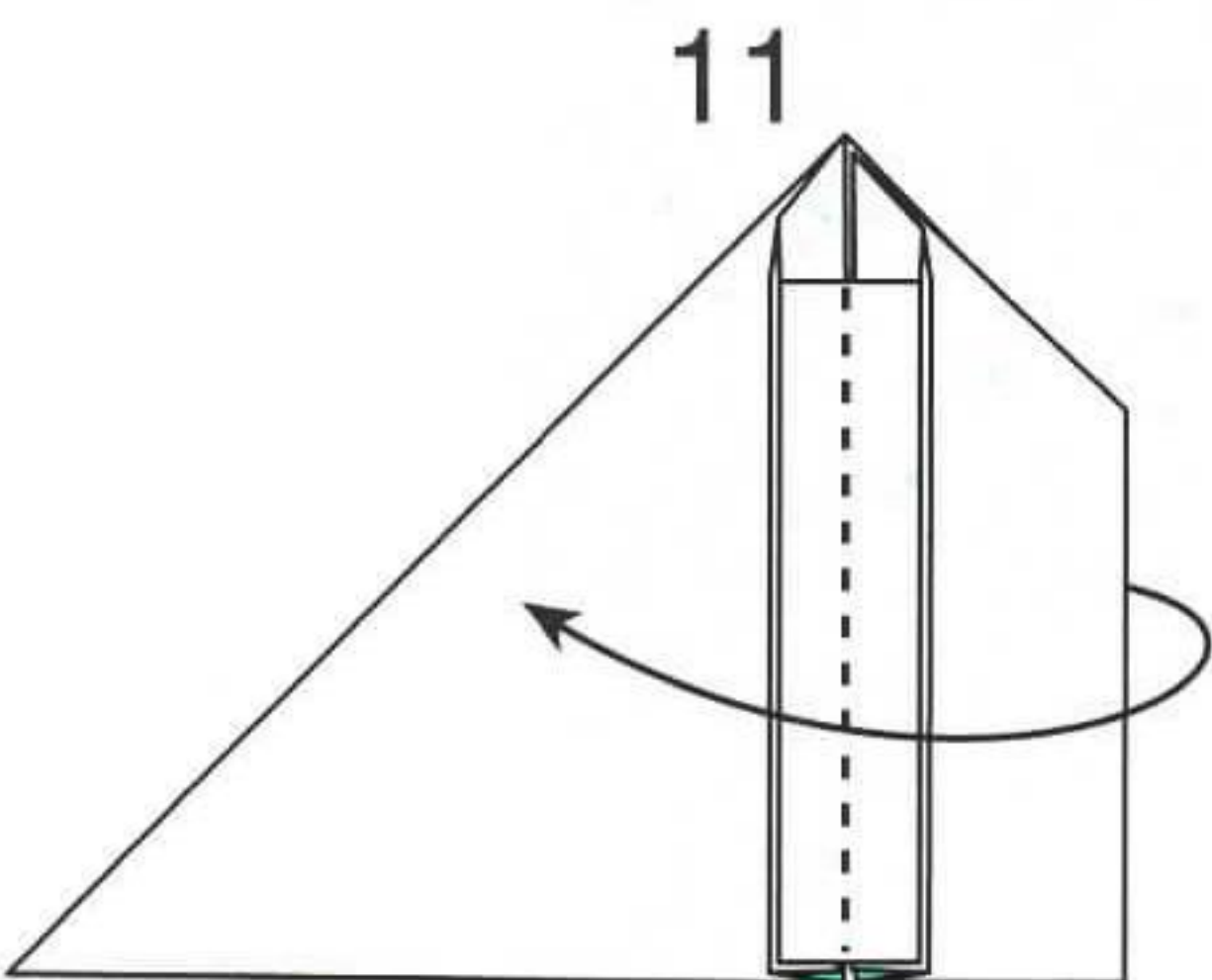
8
Fold and unfold horizontally and vertically in half.



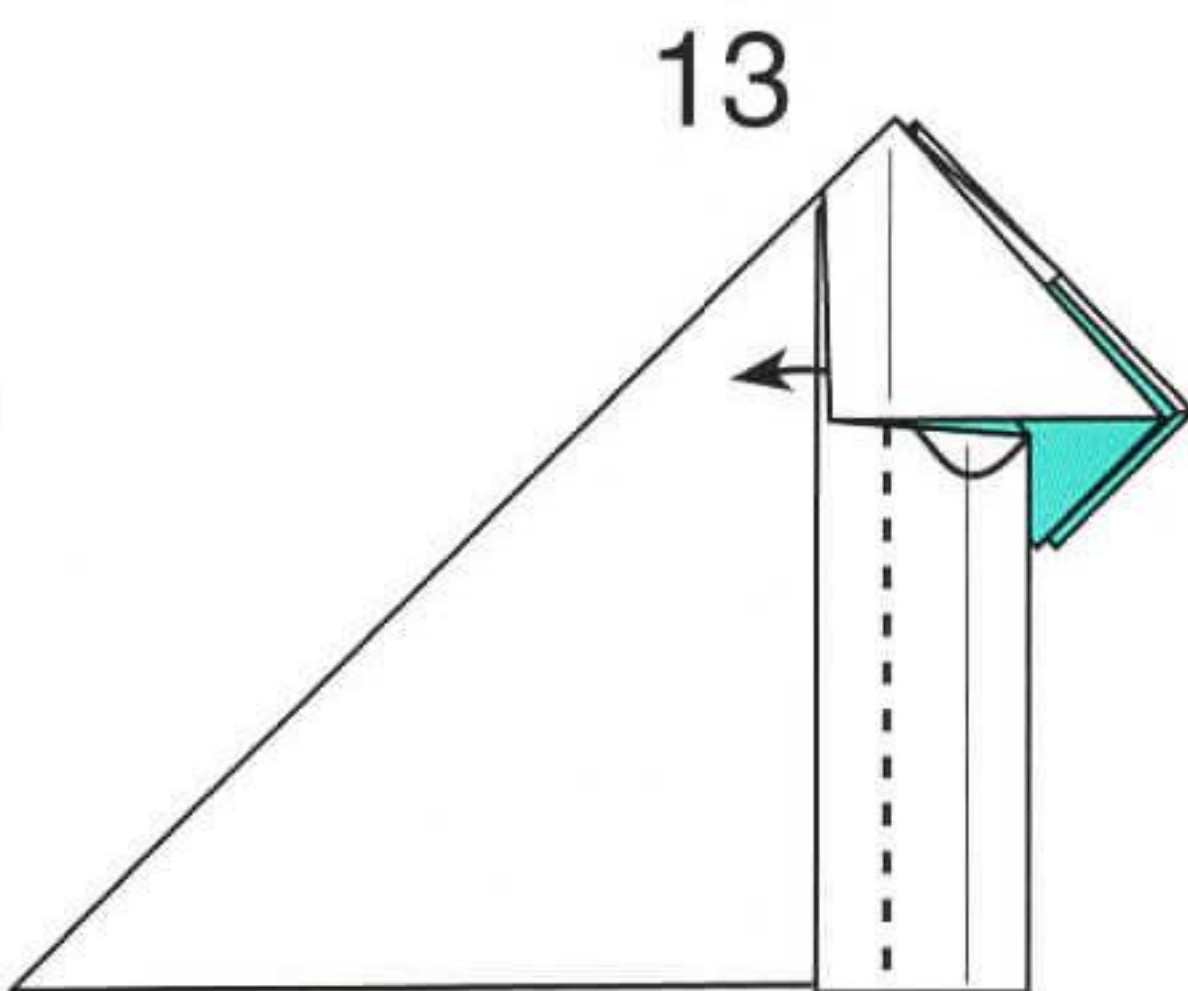
Repeat steps 2-24 of Peacock 1.



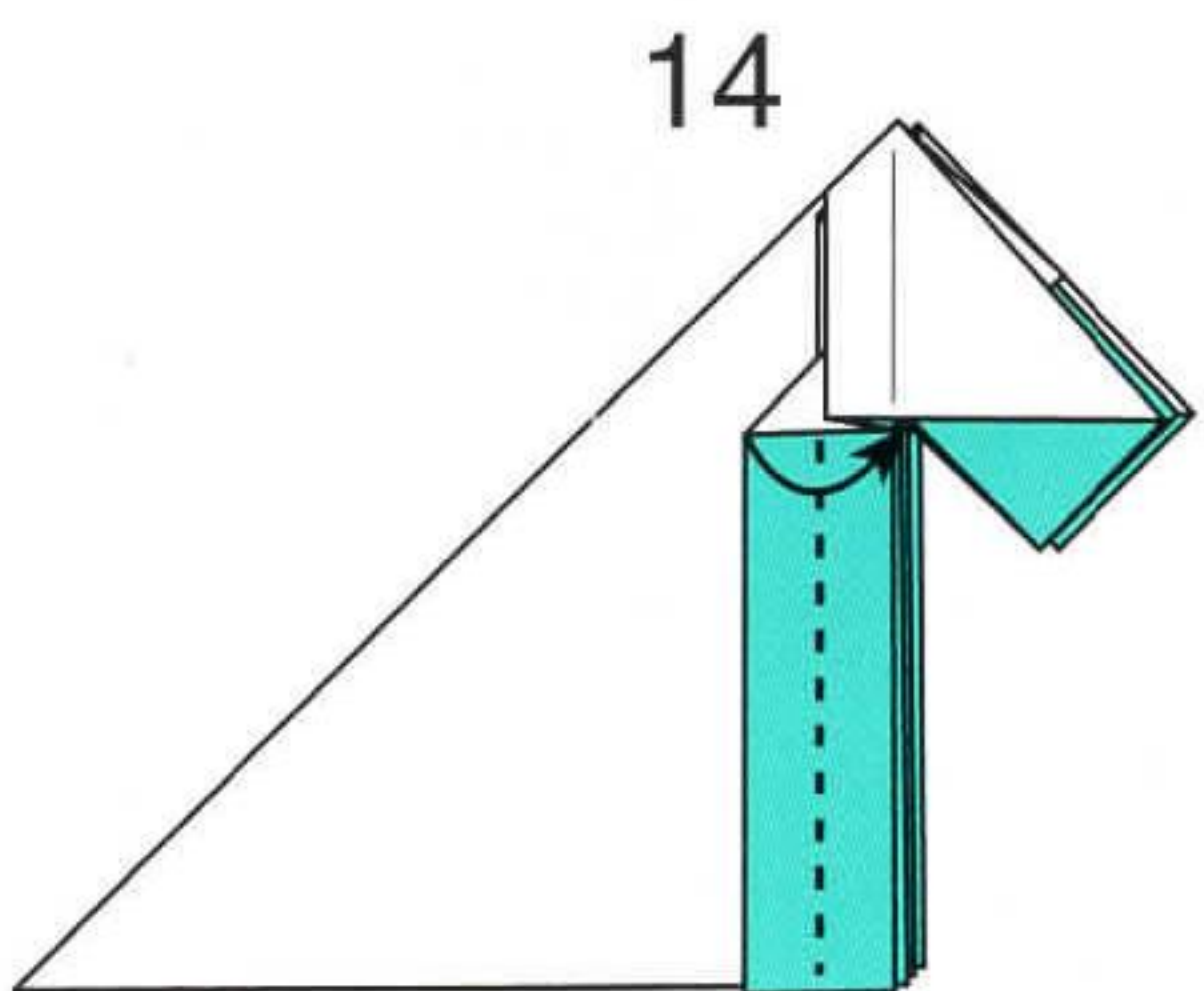
10
Closed-sink



12
Inside reverse-fold

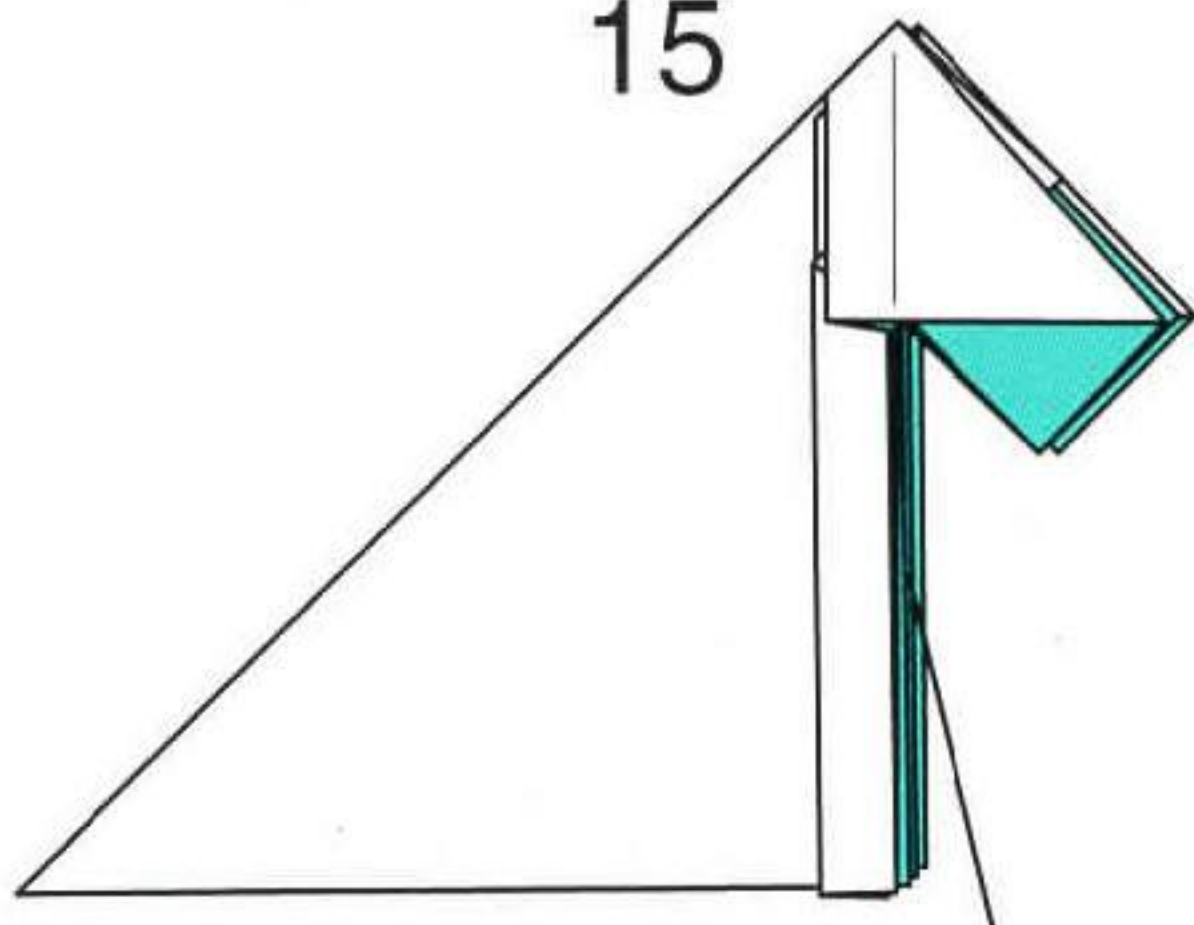


13
Inside reverse-fold



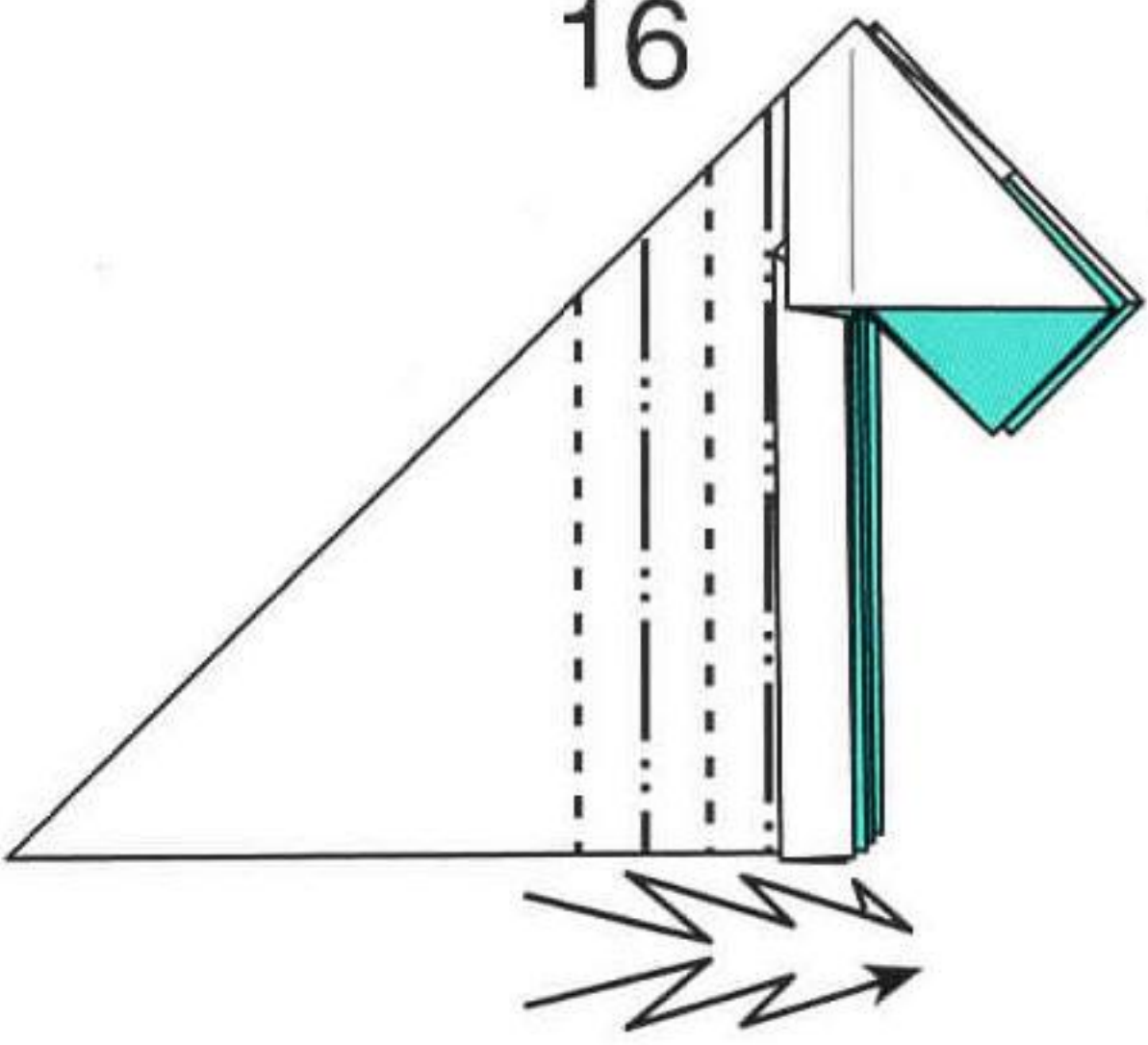
14
Inside reverse-fold

15



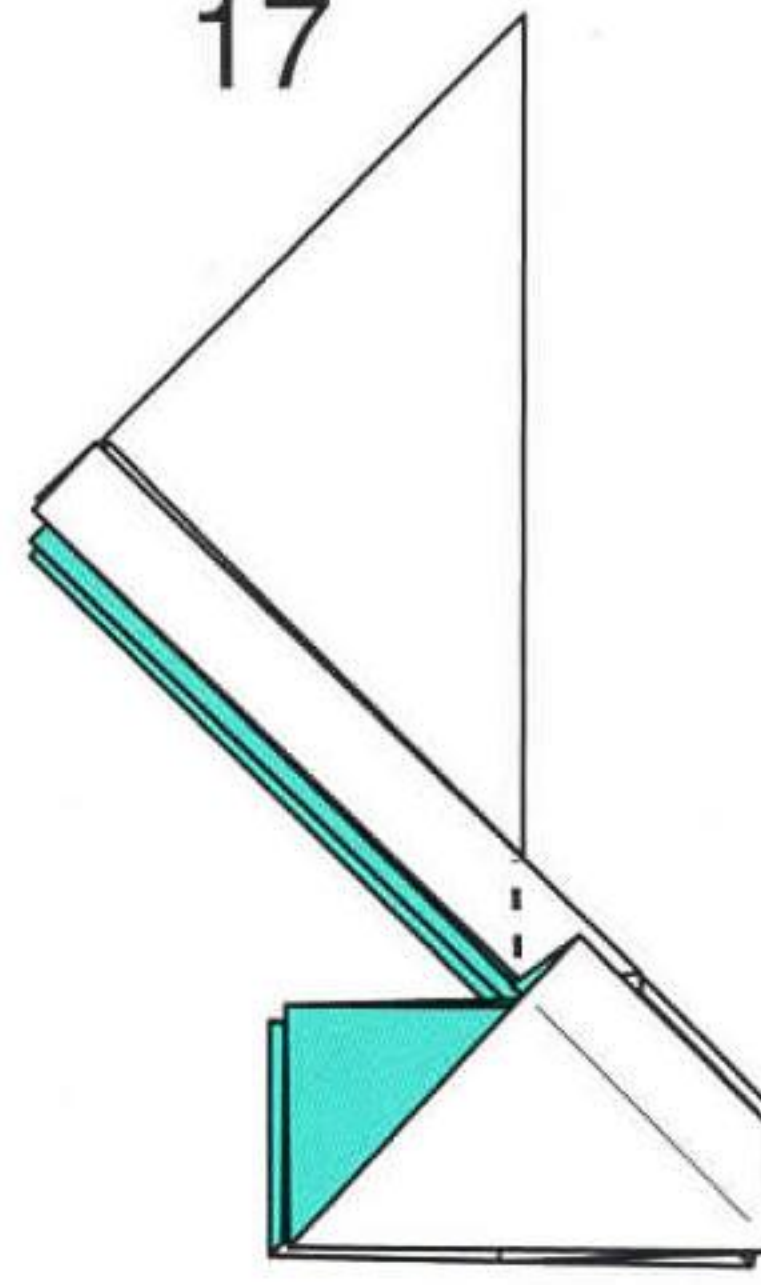
Repeat steps 10-14.

16

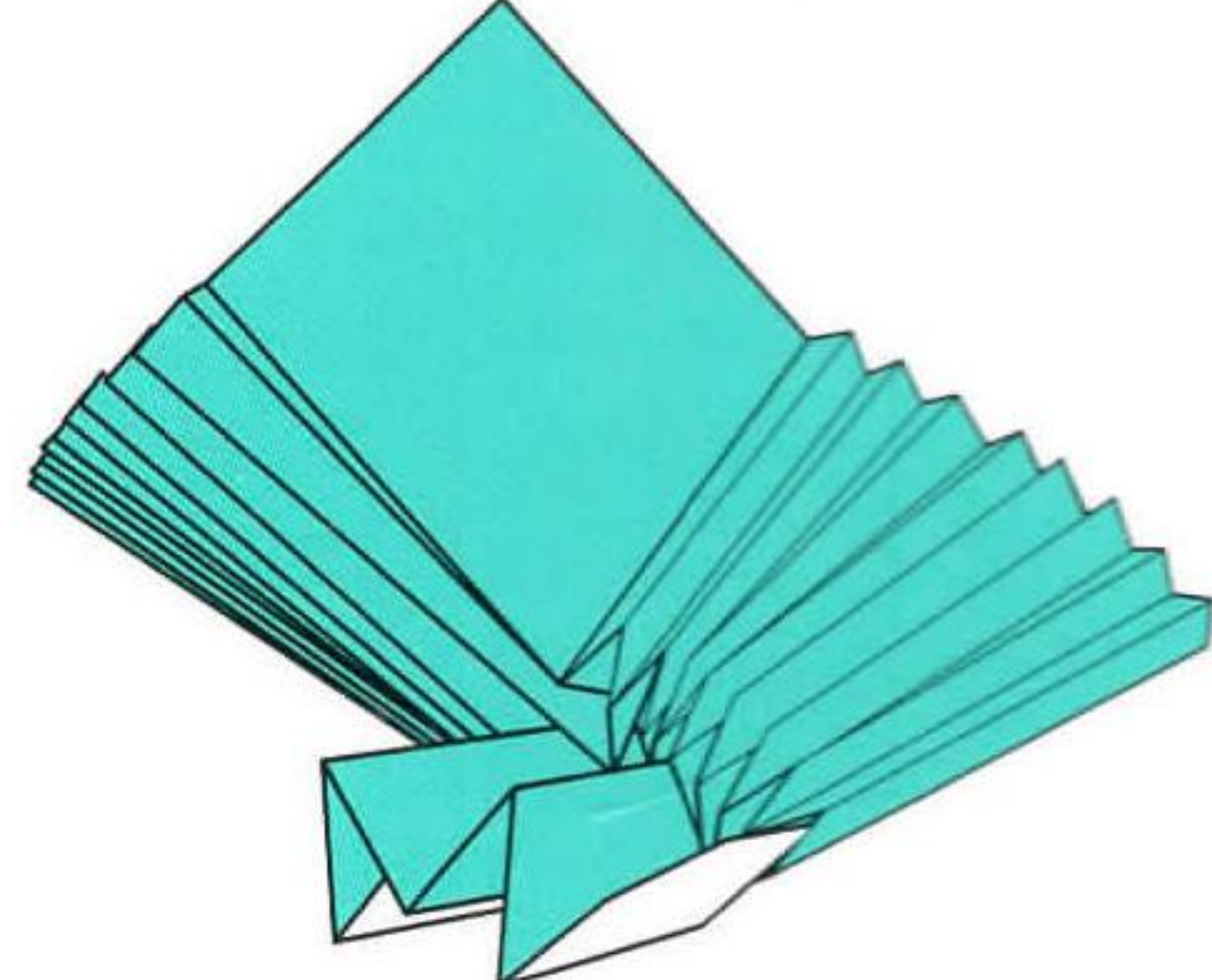


Inside reverse-fold four times

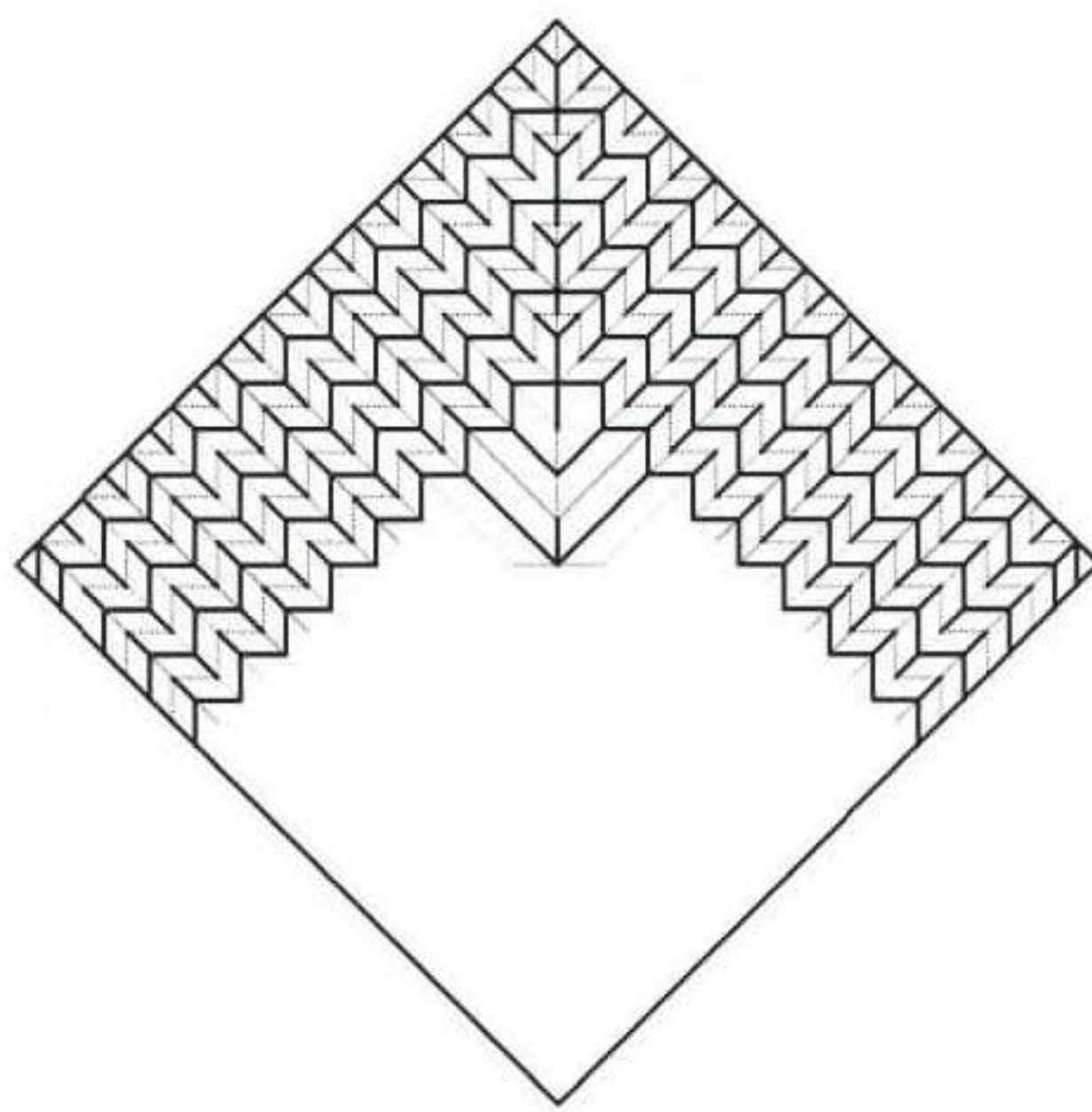
17



18

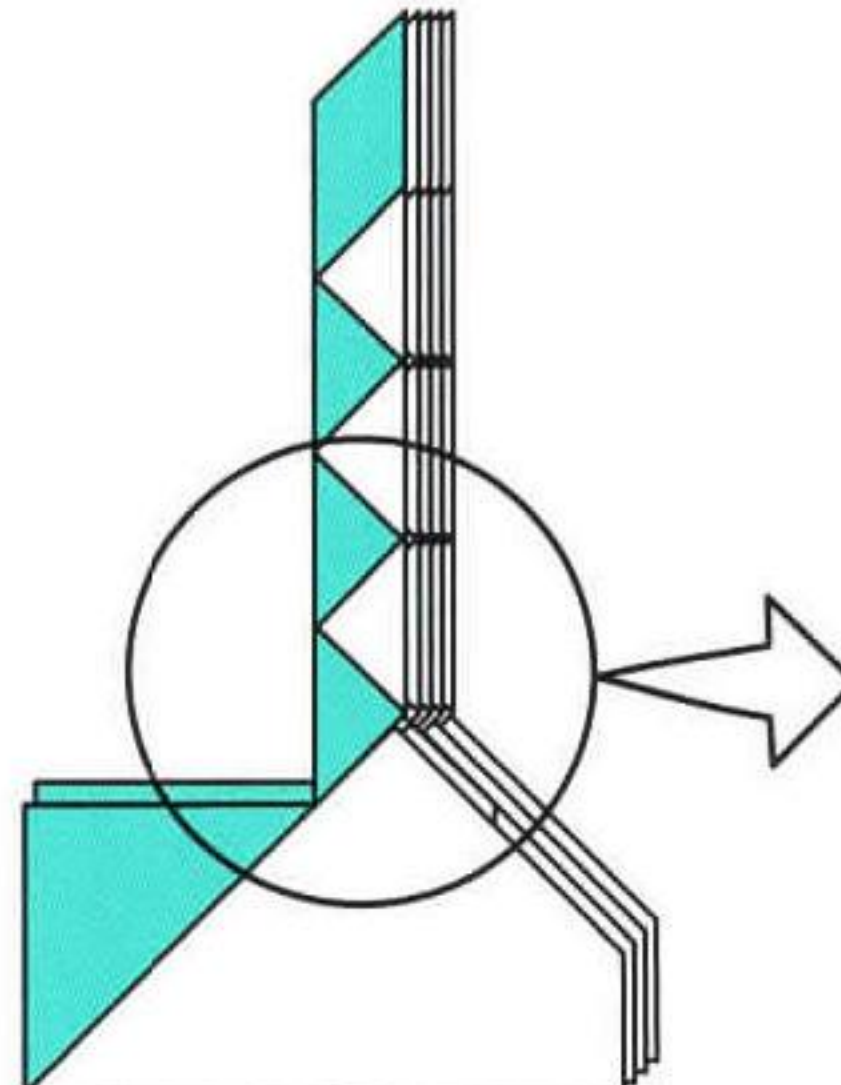


Repeat steps 34-55 of *Peacock 1*.

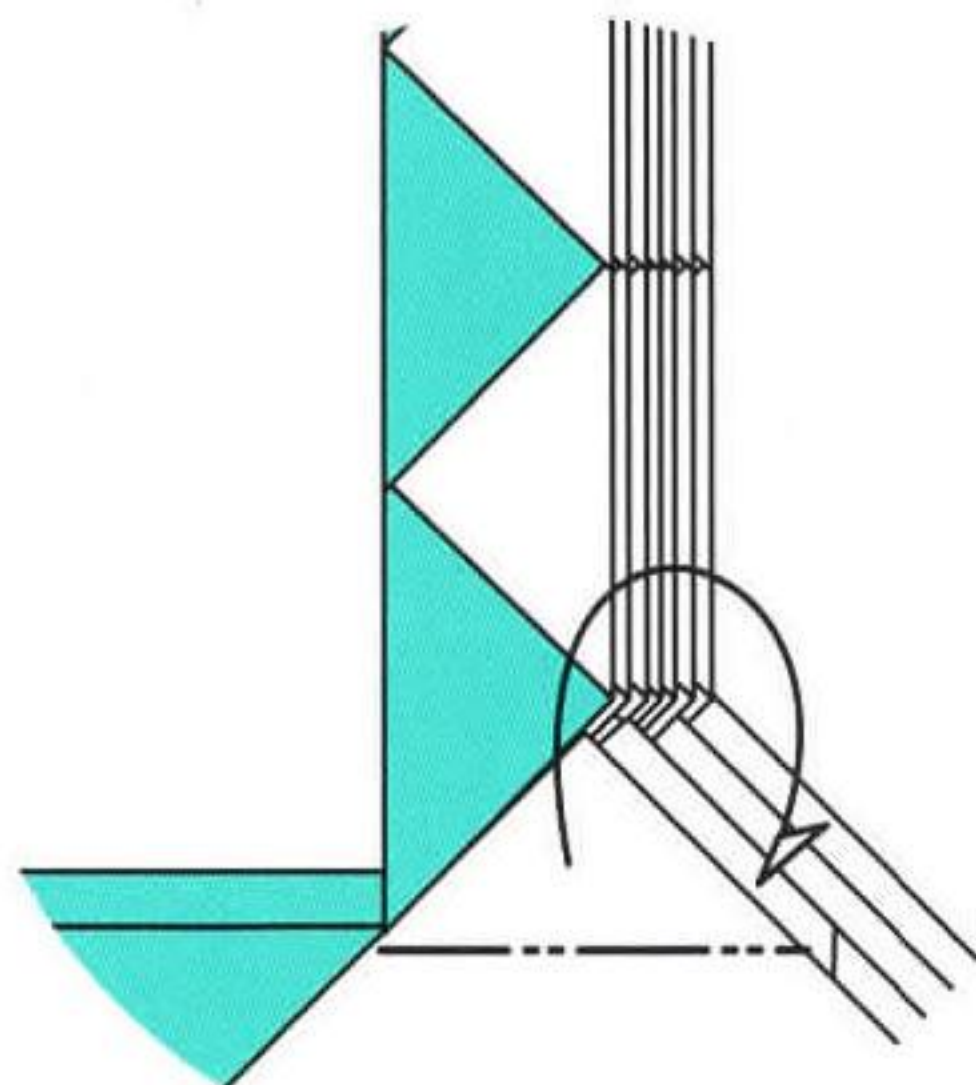


The crease pattern for steps 18-19

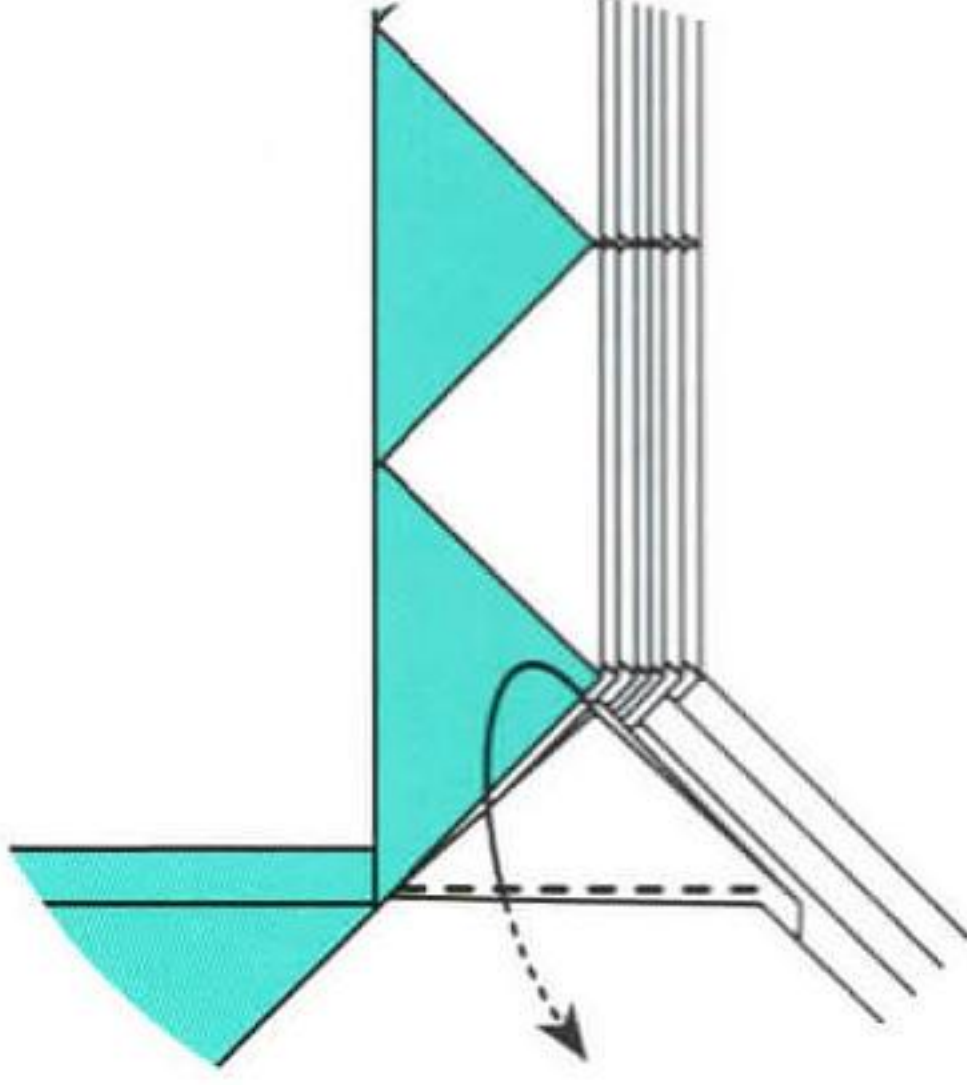
19



20

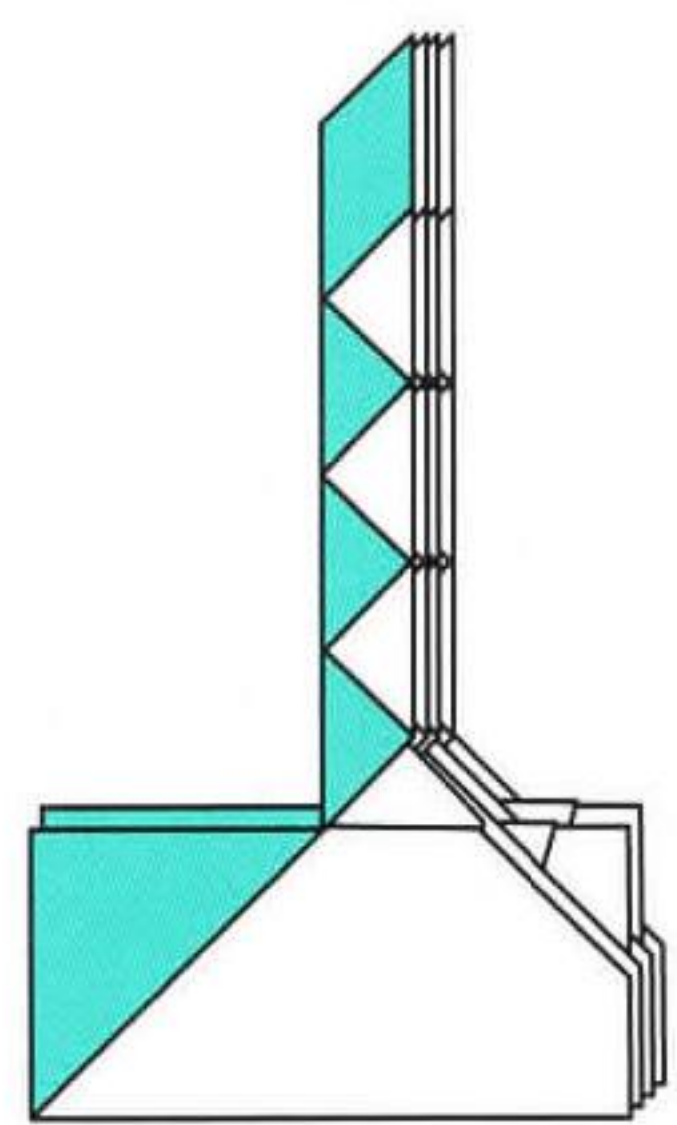


21



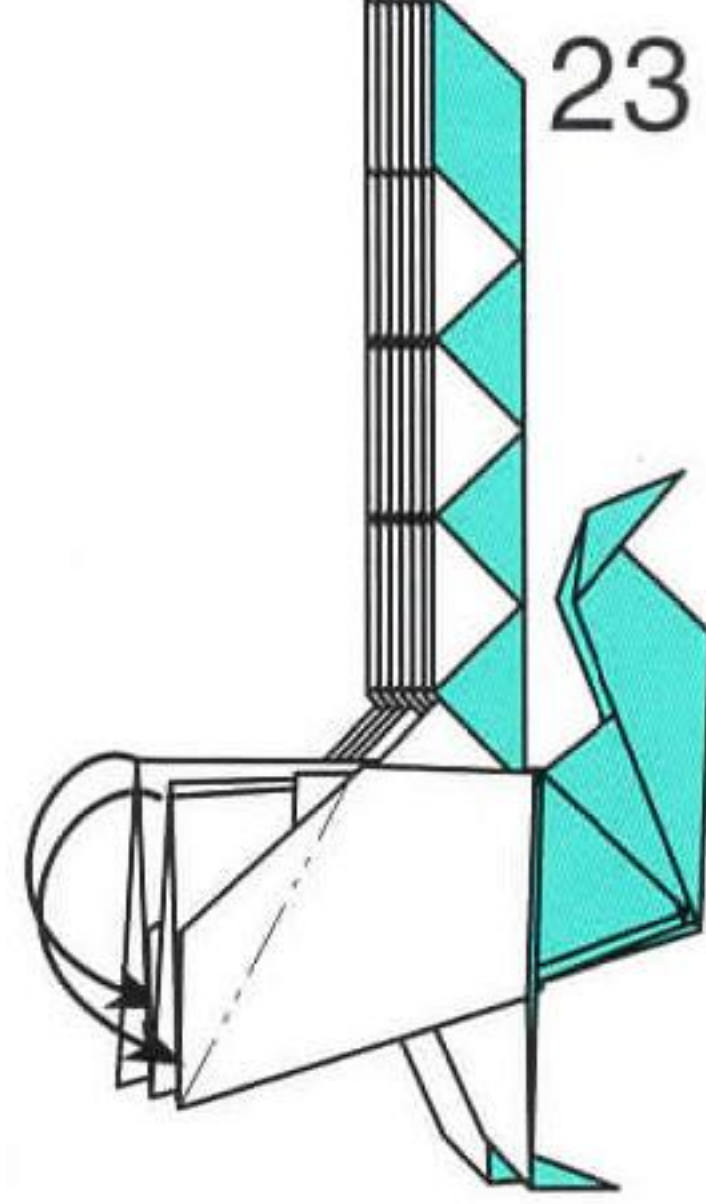
Repeat steps 56-60 of *Peacock 1*.

22



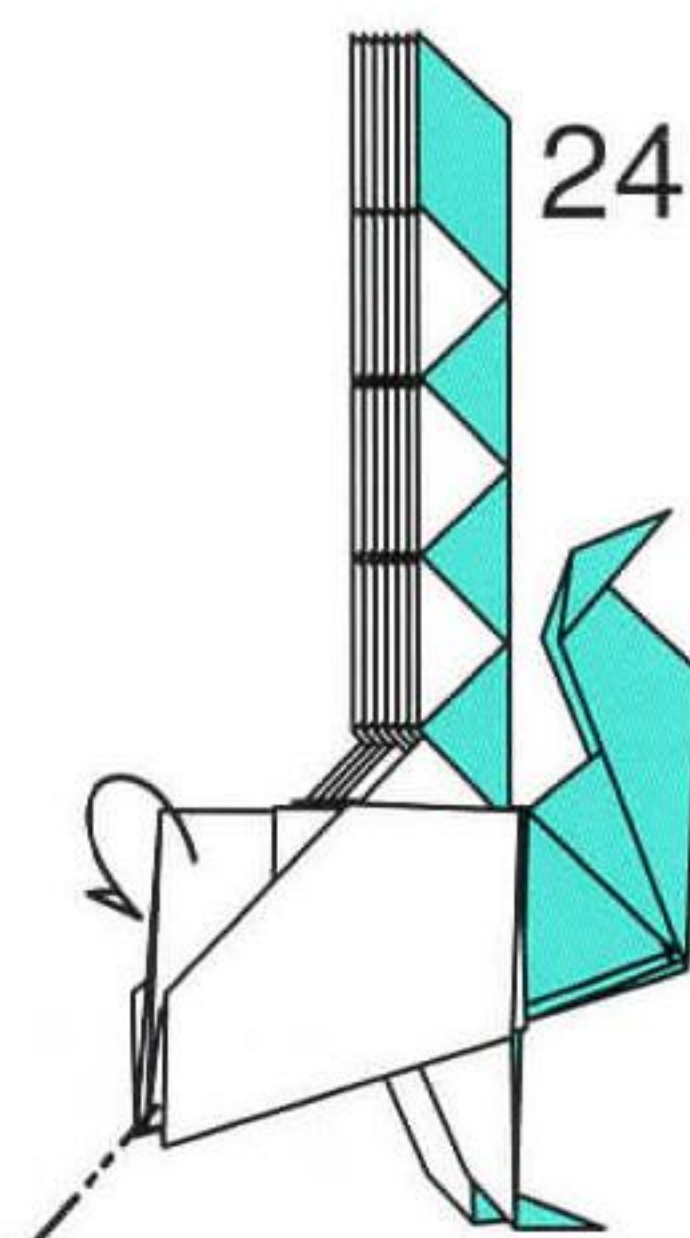
Repeat steps 64-81 of *Peacock 1*.

23



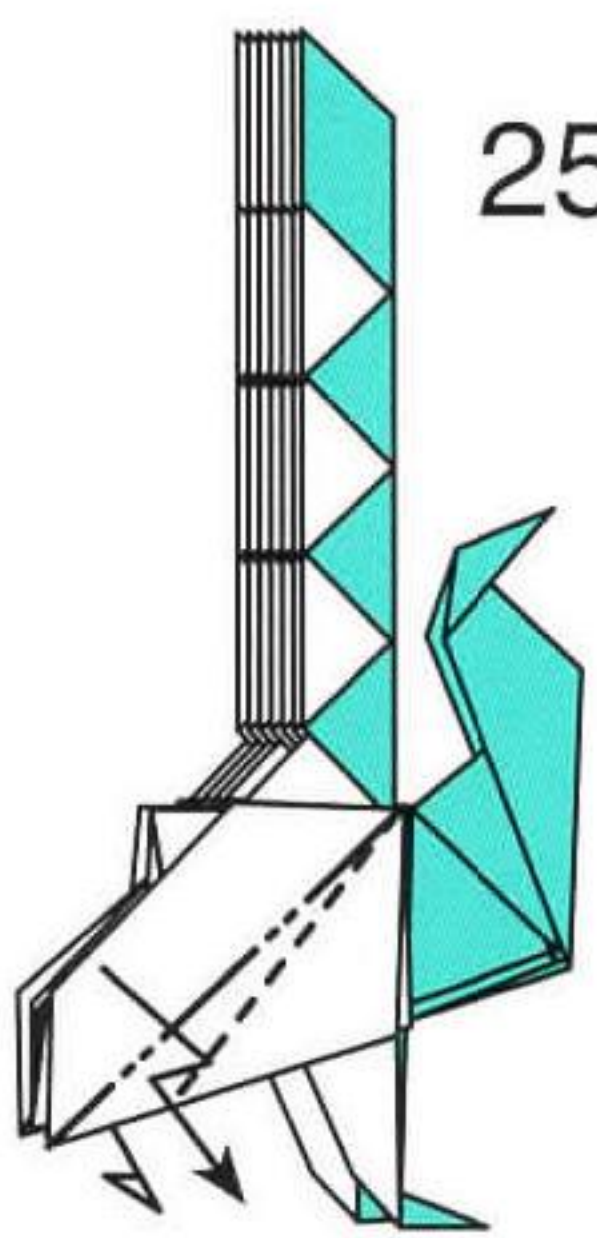
Inside reverse-fold the flaps on both sides

24

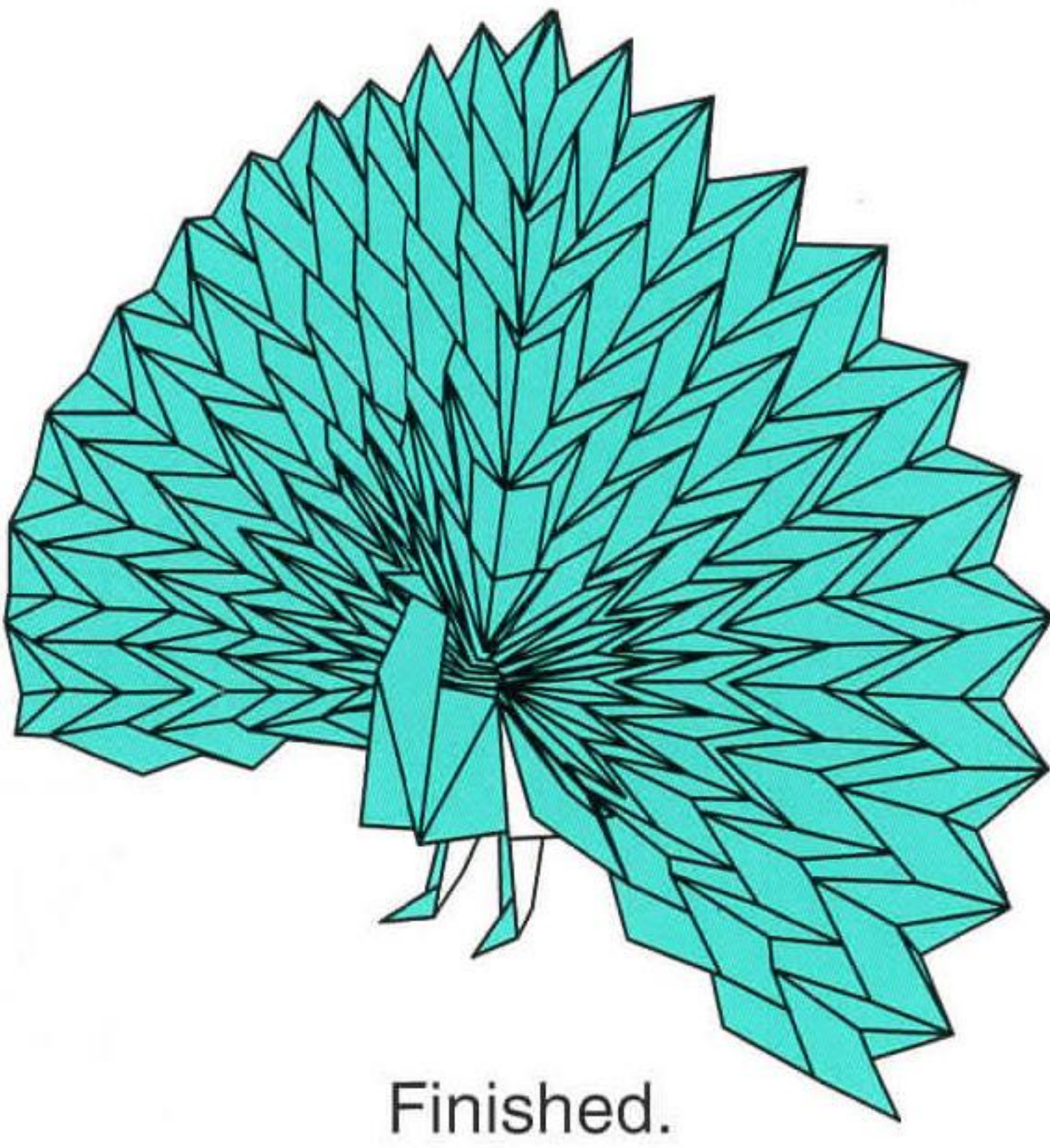


Tuck in the center layer.

25



Crimp the outer layers (wings) only, so that the model stands on its wings and legs.



Miura-ori and tessellation

The tail of *Peacock* has the same structure as **Miura-ori**, a crease pattern devised by Koryo Miura. Though the angles are different, compositions of mountain and valley creases are the same.

Although well known for map folding, Miura-ori was originally invented in space engineering technology to transport a large flat structure (such as an antenna, a solar panel, or a solar sail that receive the pressure of particles emitted from the Sun) into outer space. This structure is technically called **developable double corrugation surface** because it can be easily developed onto a plane.

This crease pattern itself had been used in lampshades and other designs before Miura started studying it and revealed its significance in engineering technology.

I designed, without the knowledge of Miura-ori, an earlier version of *Peacock* that has a similar crease pattern in its tail. It was folded from a rectangle. After learning and analyzing the Miura-ori, I came up with the idea of placing two sets of Miura-ori in different orientations within the square and connecting them at the right angle, thus resulting into this model.



As I discussed about the use of cuts in origami at the end of **Varieties of Origami**, models that use crease patterns that can be repeated infinitely, as with Miura-ori, are the ones that we can call true origami “with no cuts.”

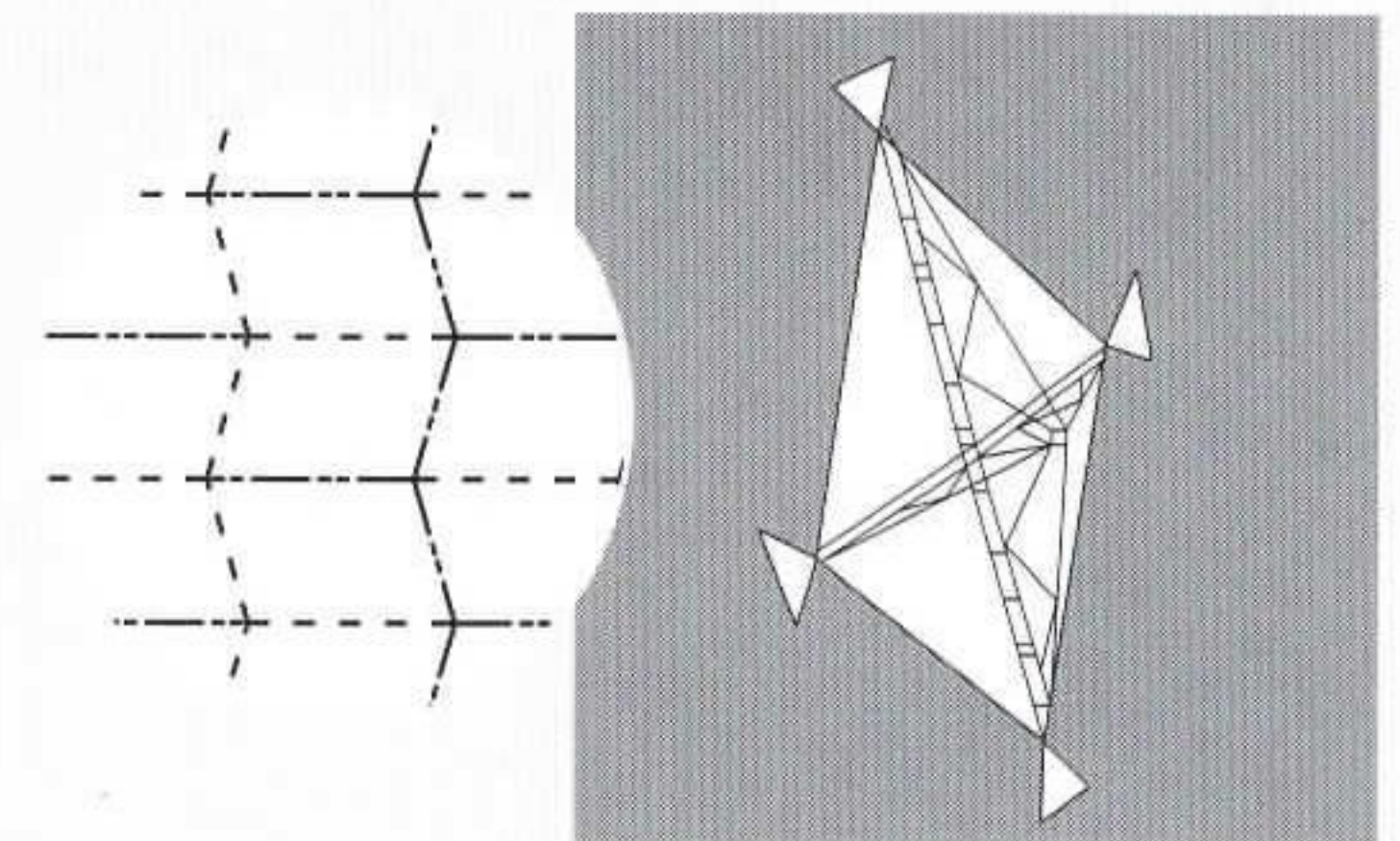
So, what will happen if we fold an infinitely large sheet in Miura-ori? The structure is called “double corrugation” because of the combination of horizontal and vertical pleats. But those two types of pleats are different. As you can see in the tail of *Peacock*, the sheet will be narrowed in one direction but become only slightly shorter in the other. When applied in engineering, it will be packed more compactly because the angles are closer to the right angle than 45° and 135° of *Peacock*. Still, because of the difference between the directions, the sheet becomes oblong when folded.

The difference also appears on the crease pattern. That can be eliminated by using two types of parallelograms, instead of one as in original Miura-ori. The first modeling of such extended Miura-ori is, as far as I know, **MARS** by Paulo Taborda Barreto.

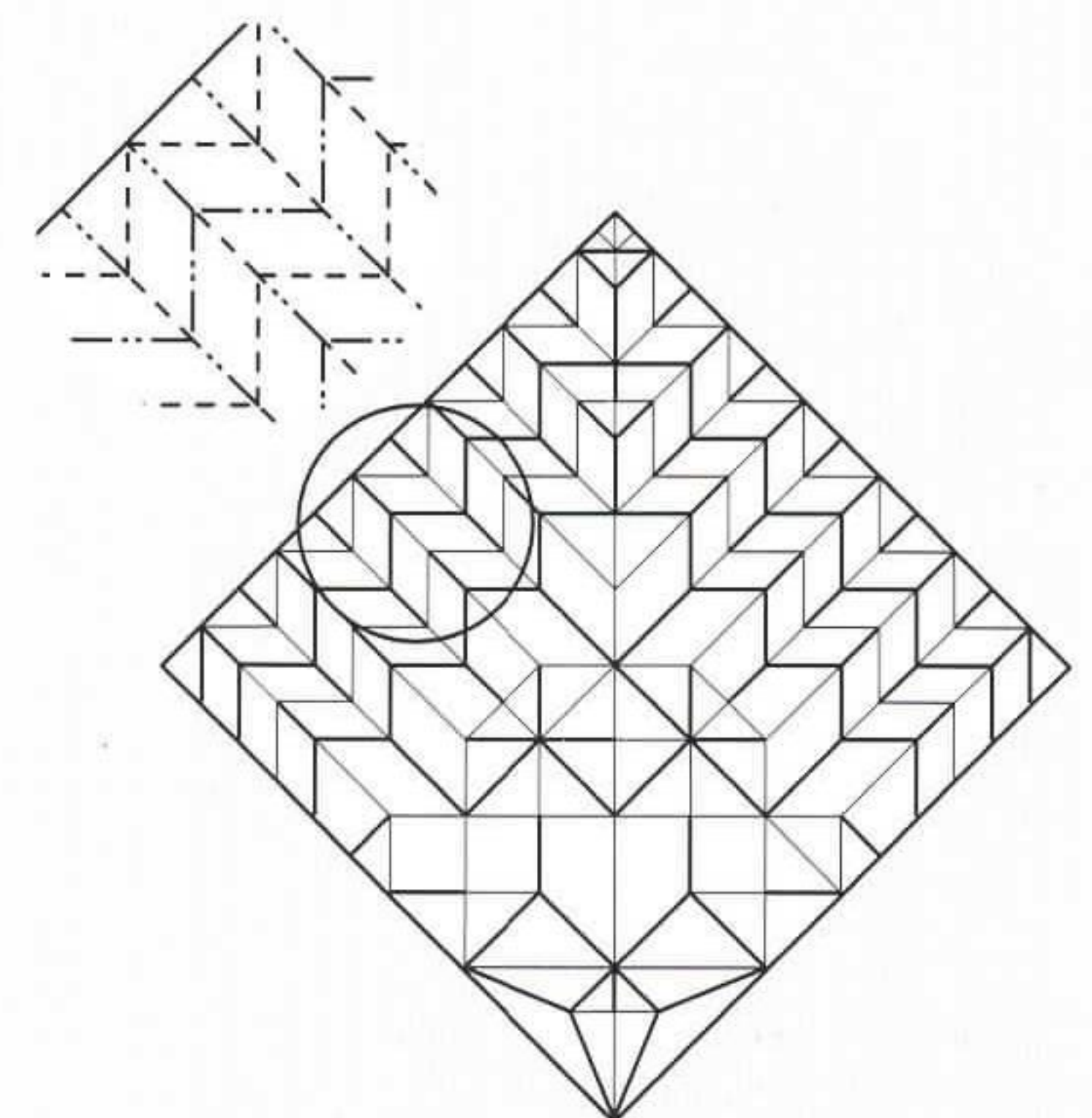
For example, we can use squares and parallelograms whose angles are 60° and 120° . Then the folded pattern extends in all directions, though there is still a little difference between directions.

A pioneer of such tiling crease pattern, or **origami tessellation**, is Shuzo Fujimoto. He calls it “hira-ori”, or flat-weaving, because folded patterns look as if it is woven. Recently it is also applied to the design of scales and other patterns.

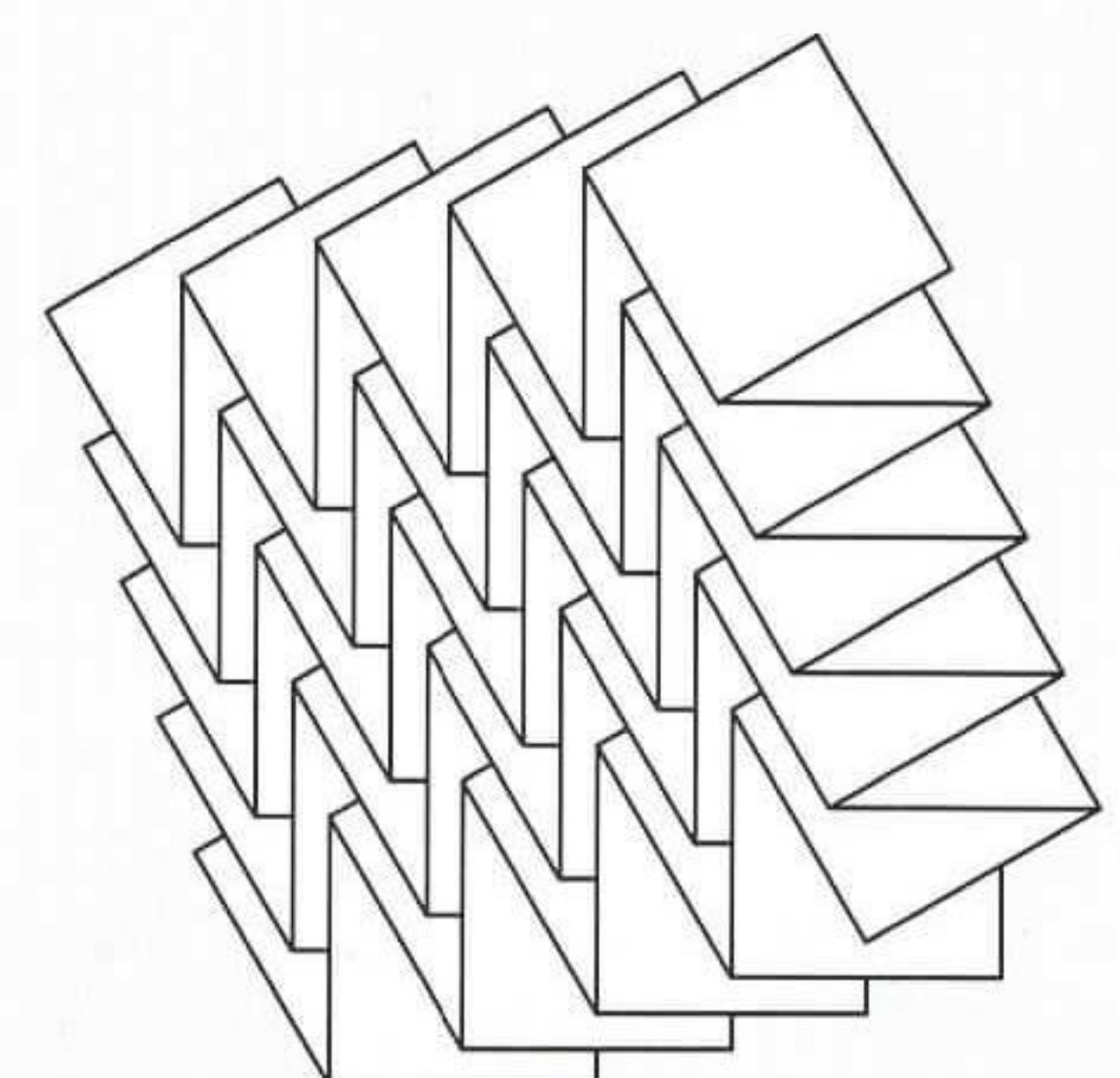
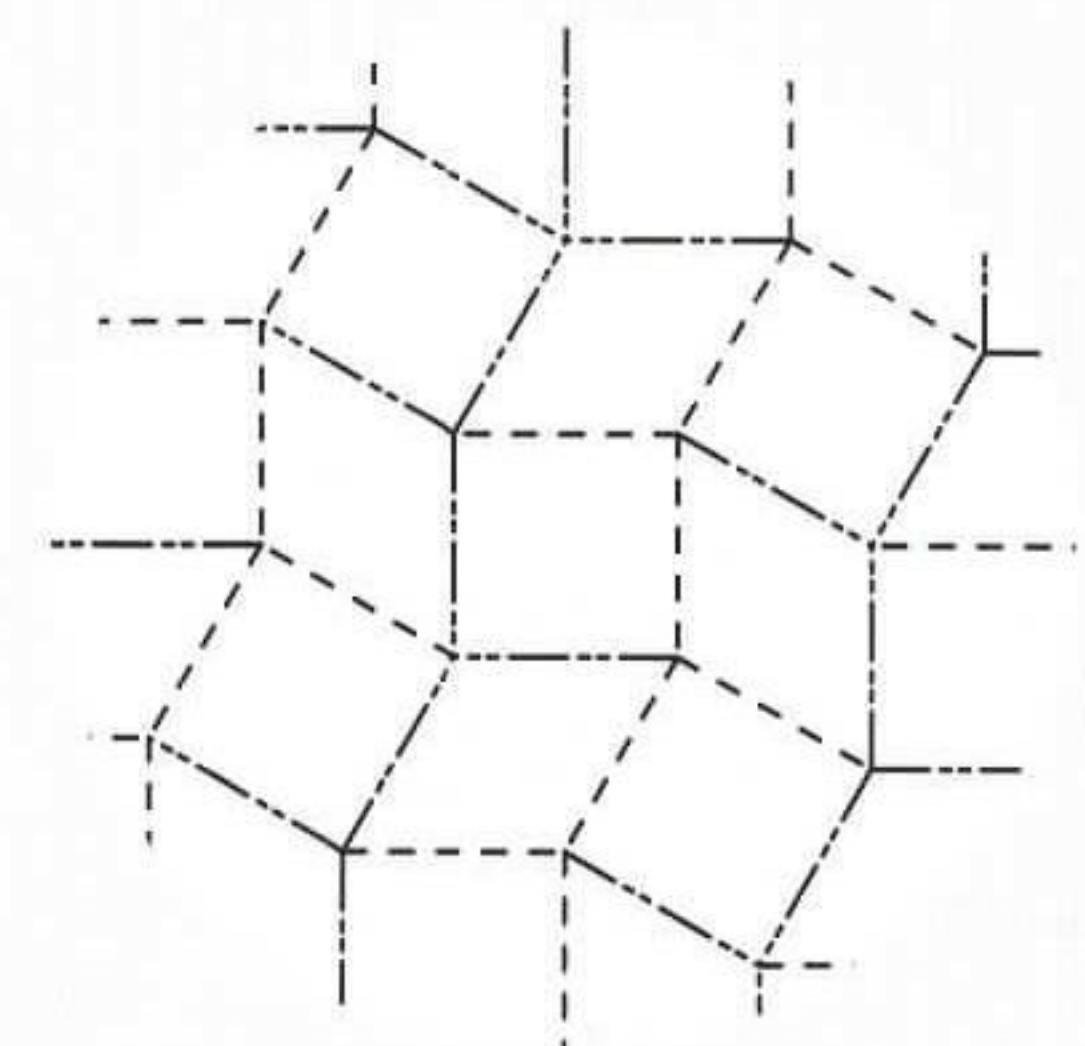
Note that Miura-ori is also iso-area (see *Gift Box*).



Miura-ori by Koryo Miura



Peacock

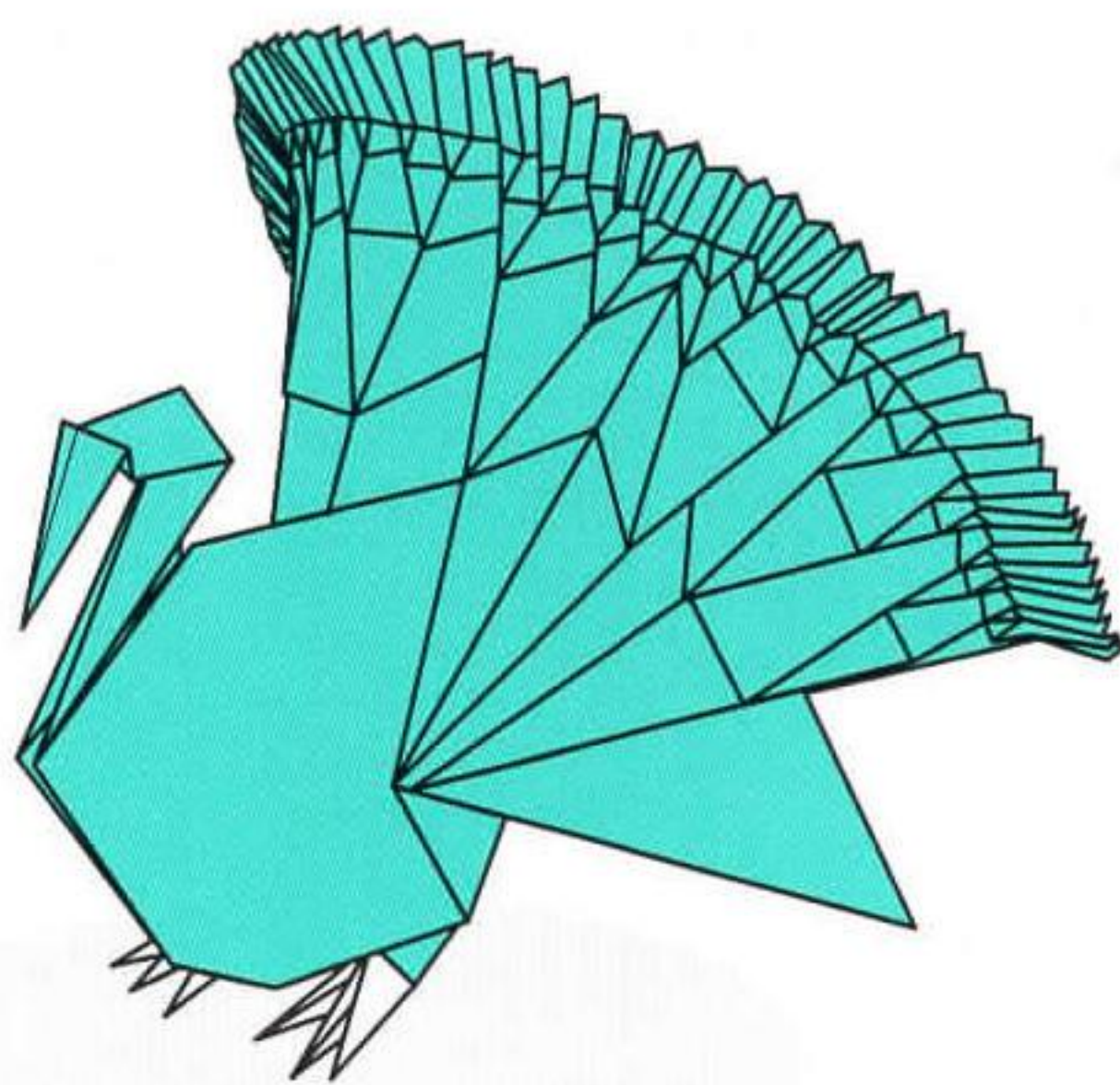


Extended Miura-ori: MARS by Paulo Taborda Barreto

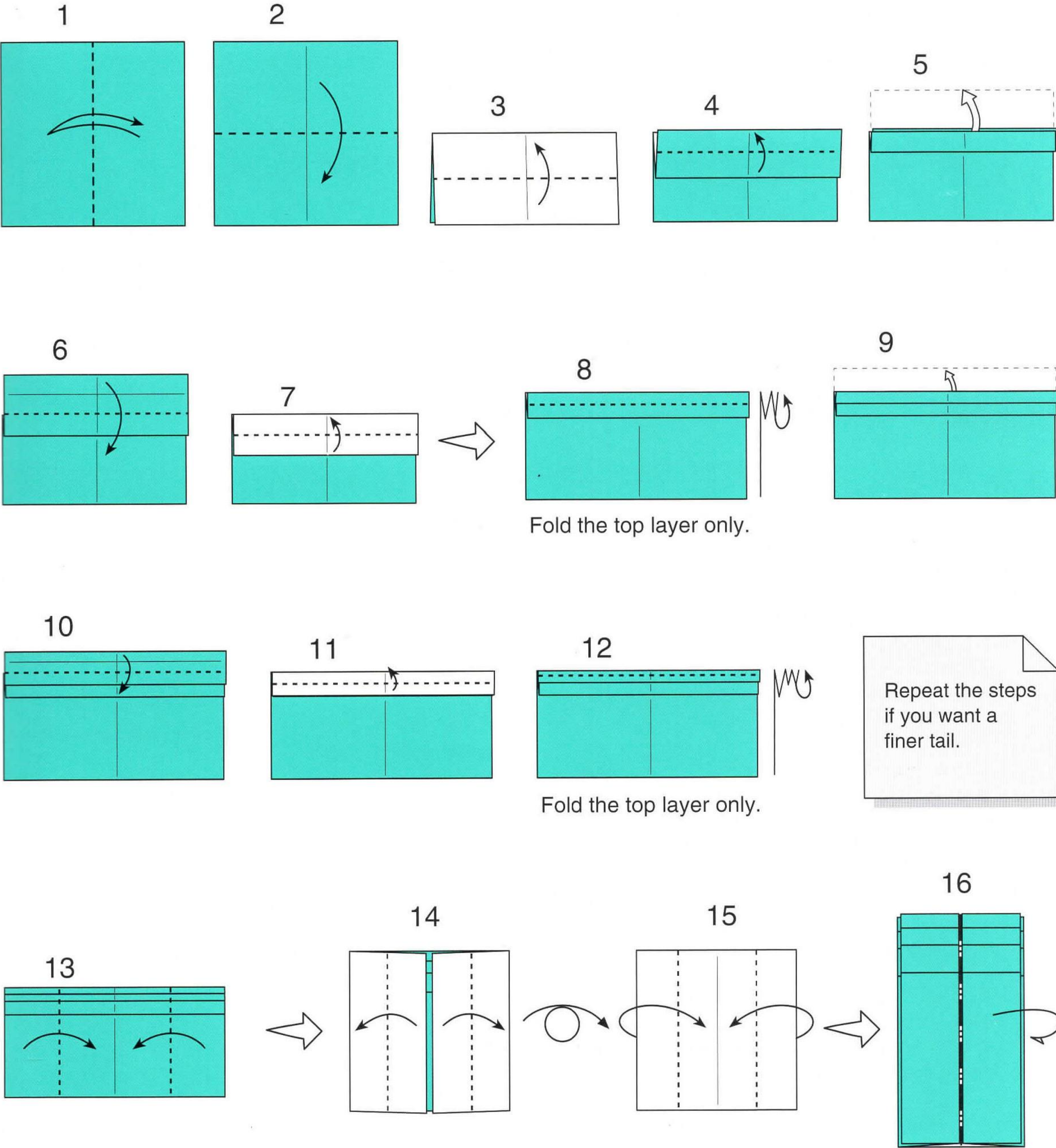
Turkey

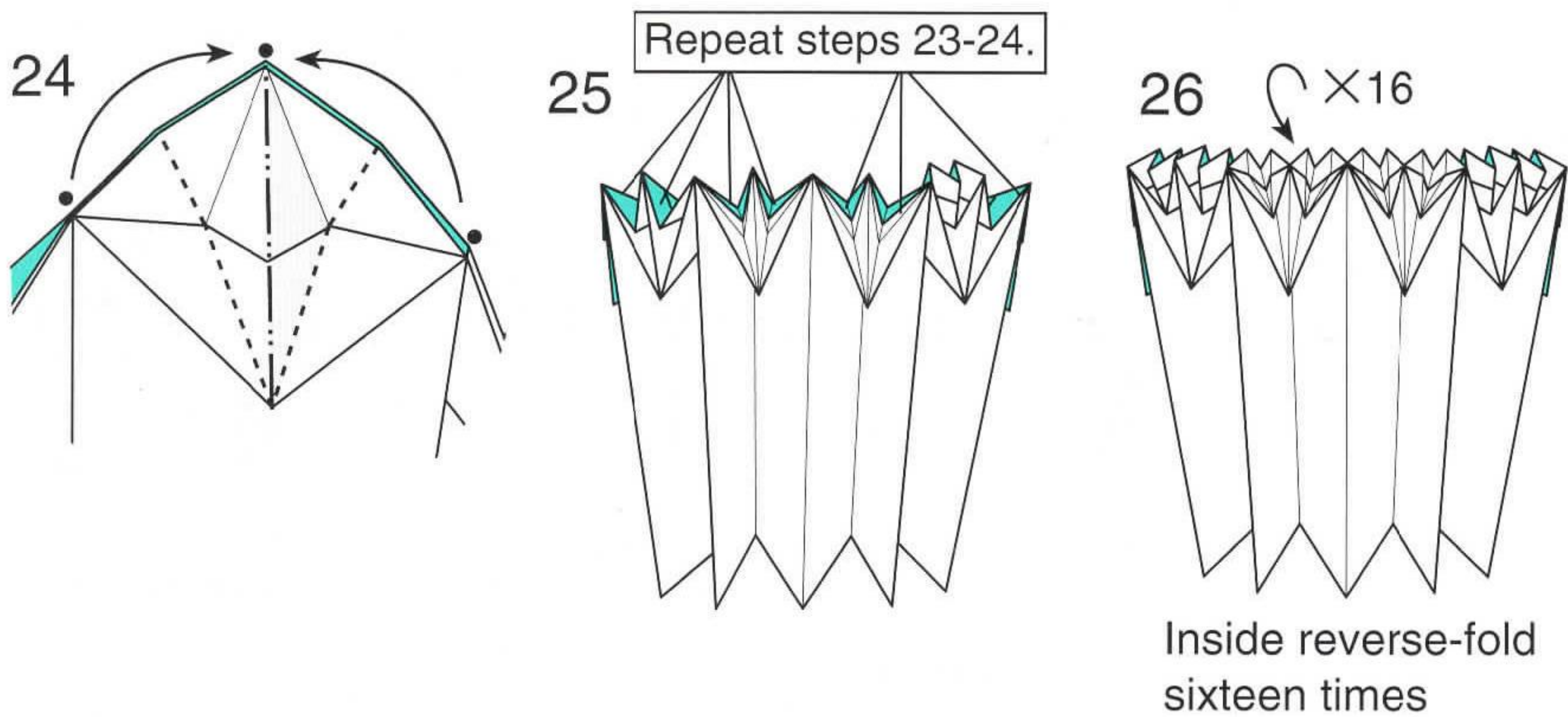
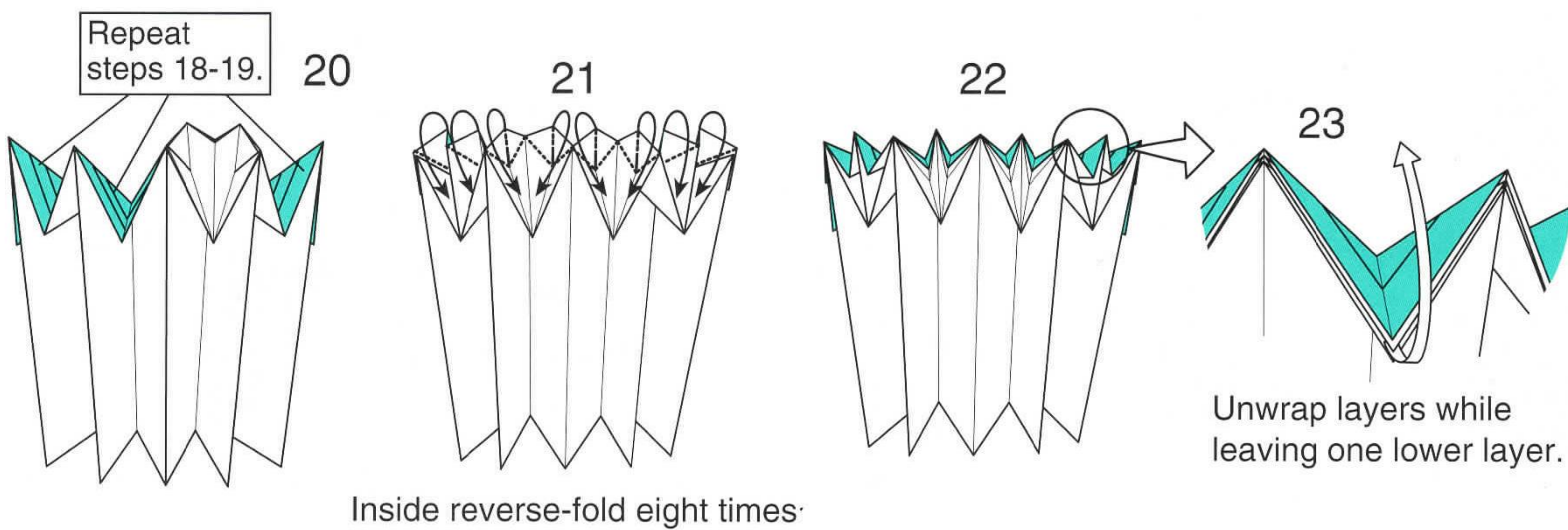
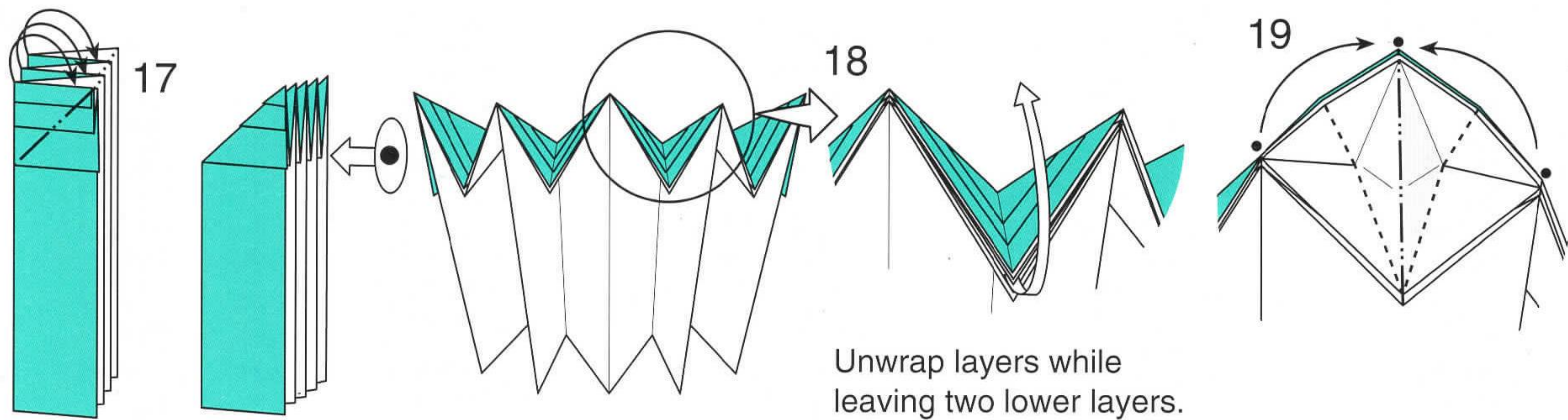
Theme: Self-similar

Difficult to fold using 6" (15 cm) origami paper. 10" (25 cm) to 12" (30 cm) very thin paper is suggested.

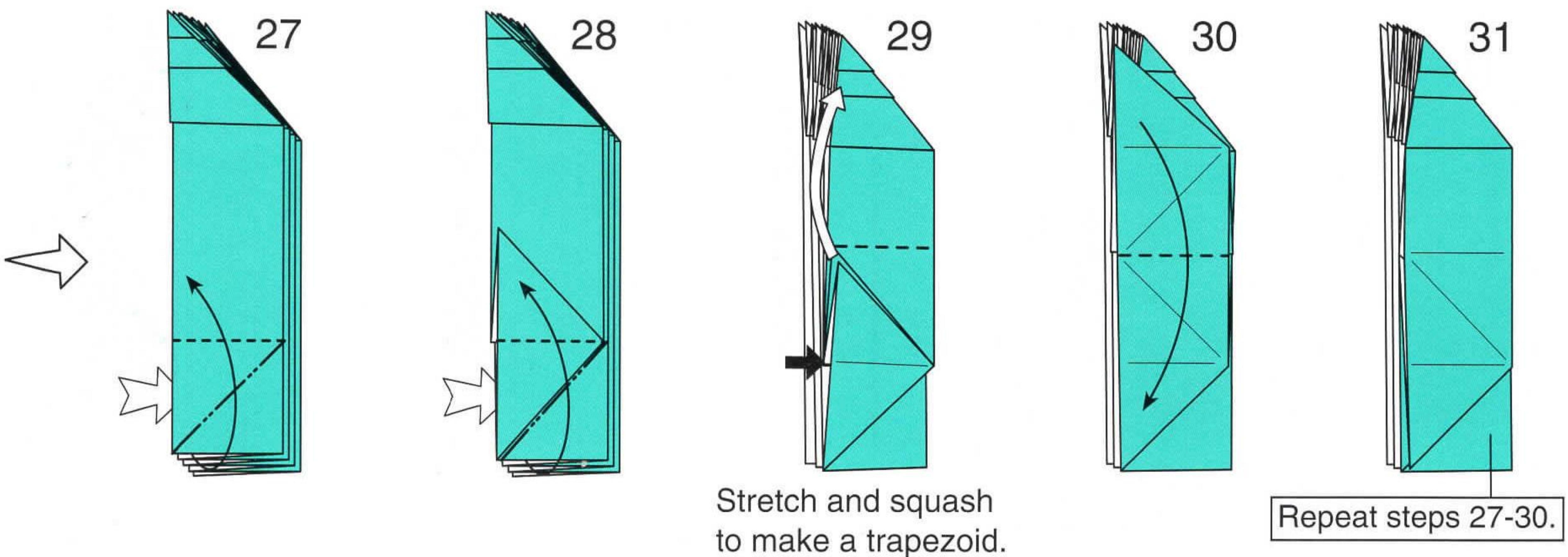


First, you need to decide how fine you would like to make the tail. That defines how many times you have to repeat the steps. Repeat five times for the picture on the left and in the beginning of this book, though the diagram instructs to repeat three times.





If you have repeated more times at step 13, repeat these steps as well.
You can also unwrap the edge of the paper to make rectangles, as in the picture in the beginning of the book.



32||

33

34

35

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43

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50

Swivel-fold

Repeat steps 32-46.

Pull out the hidden flap.

Repeat steps 48-49.

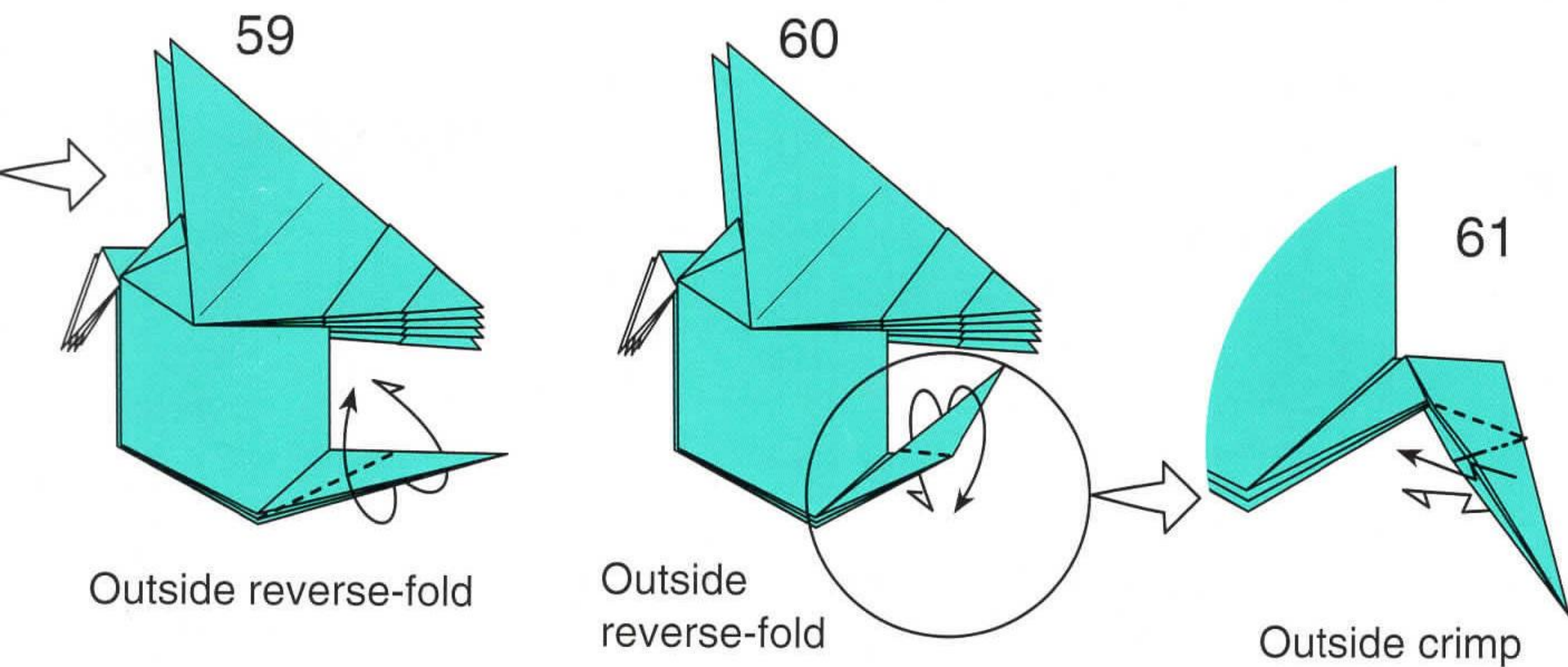
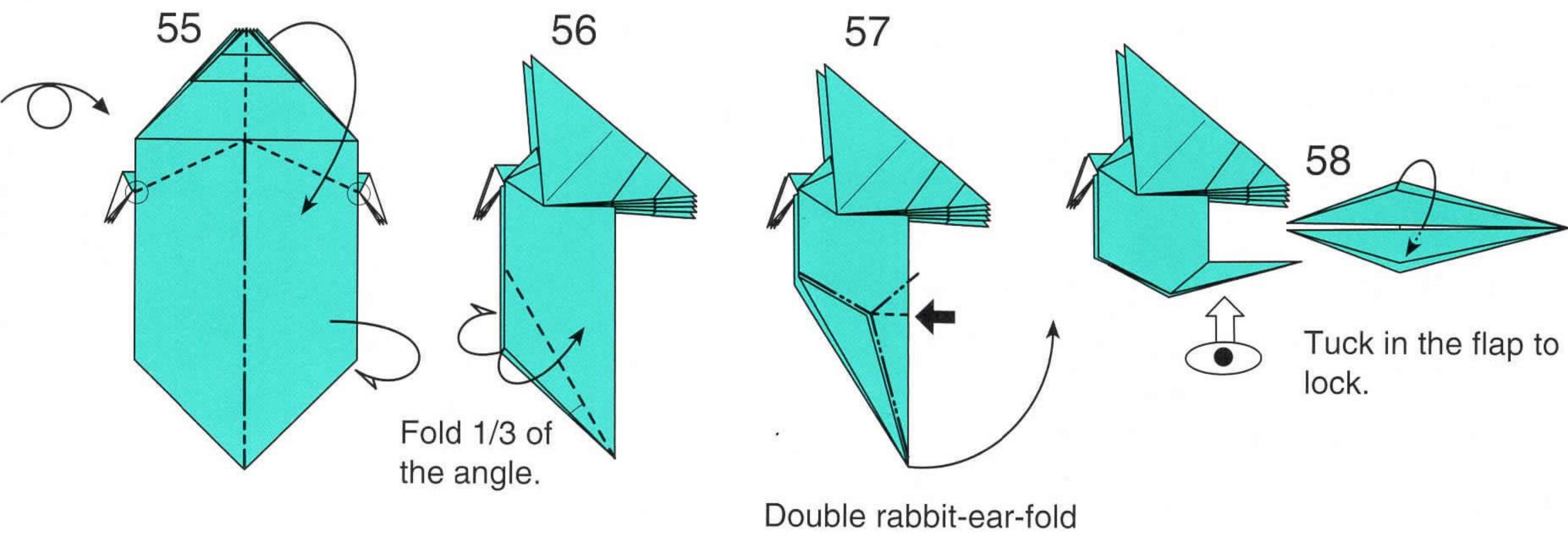
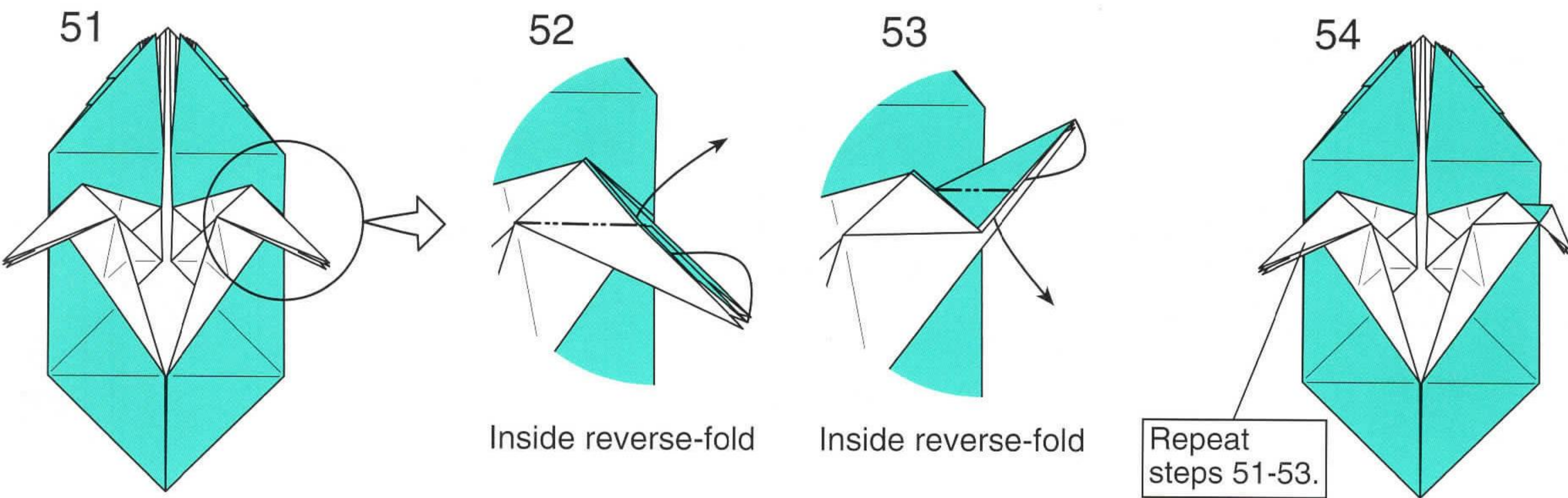
Inside reverse-fold

Inside reverse-fold

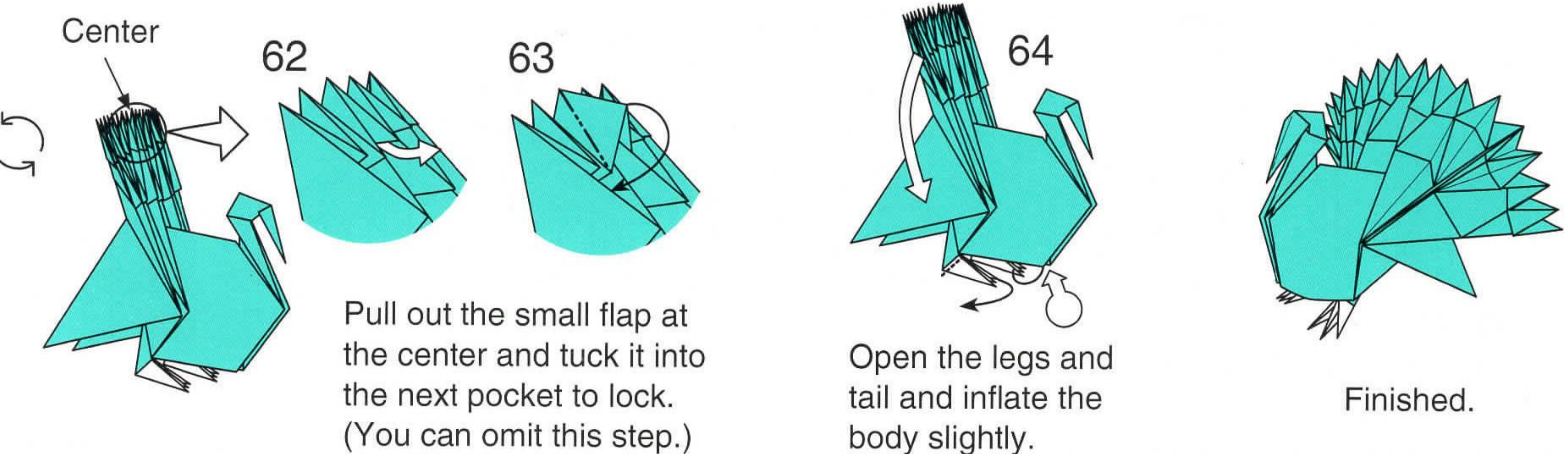
Inside reverse-fold

Inside reverse-fold

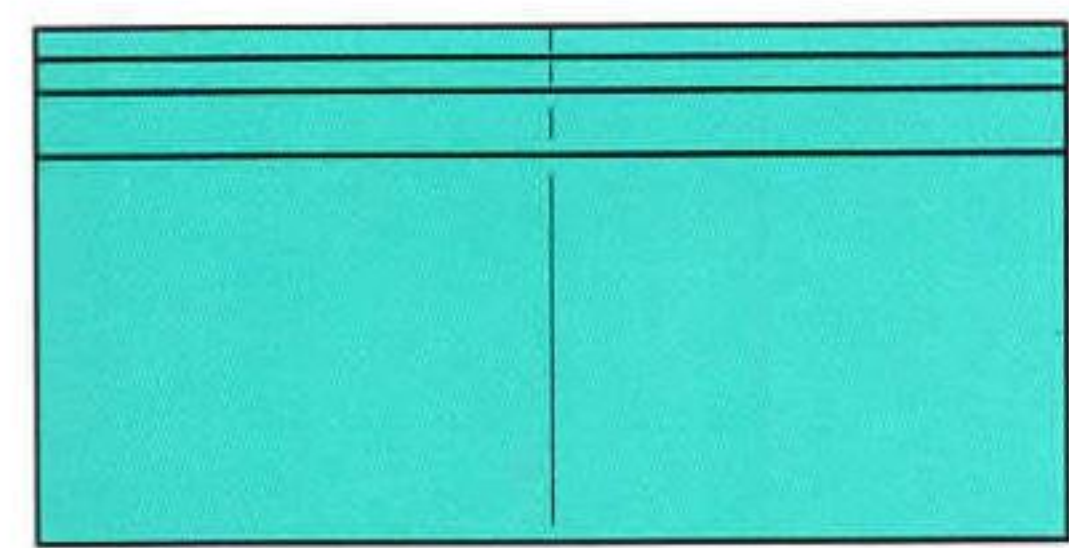
Inside reverse-fold



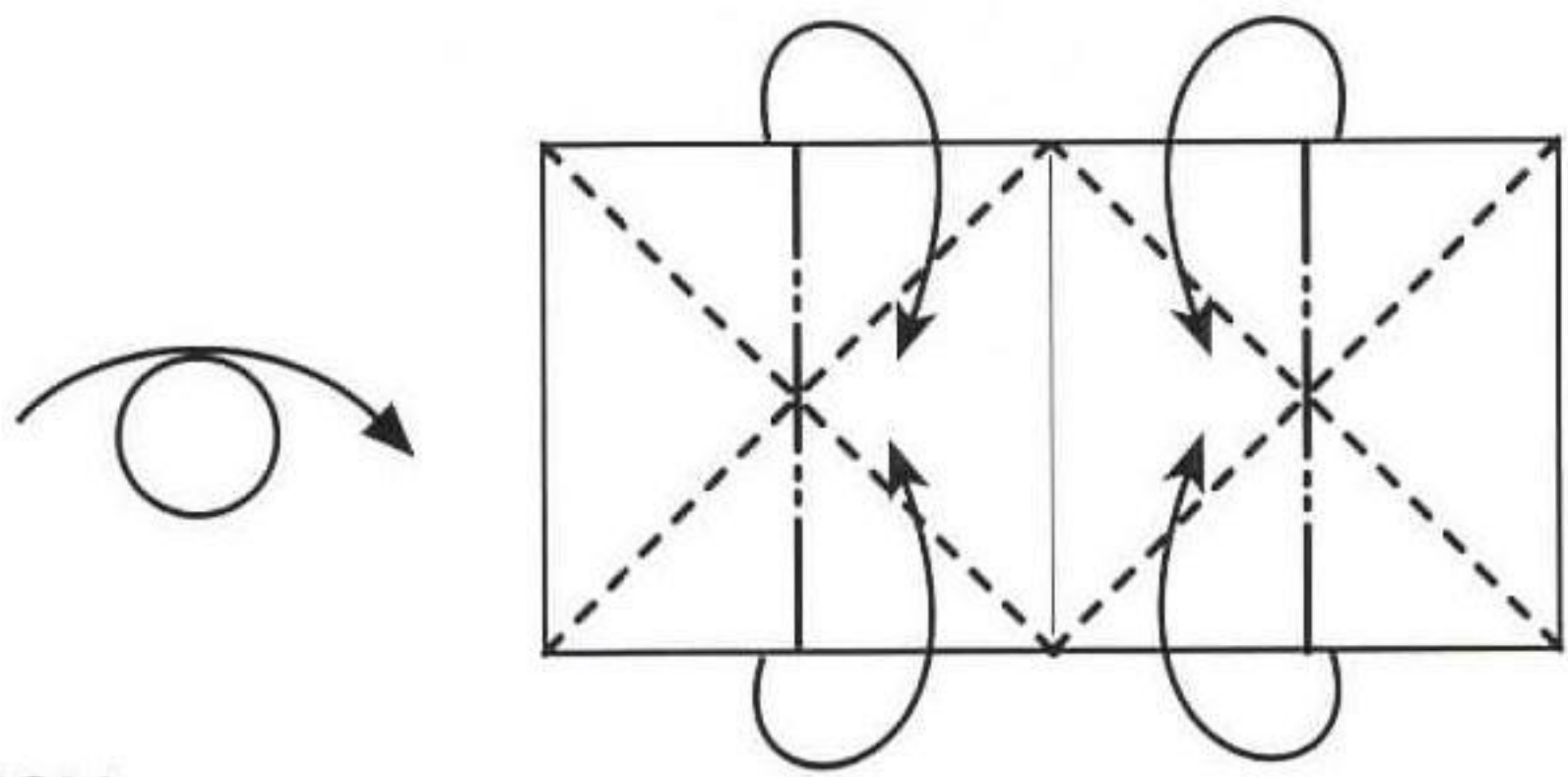
Fold the point so that it becomes a wattle, not a beak.



Related model: *Surf*

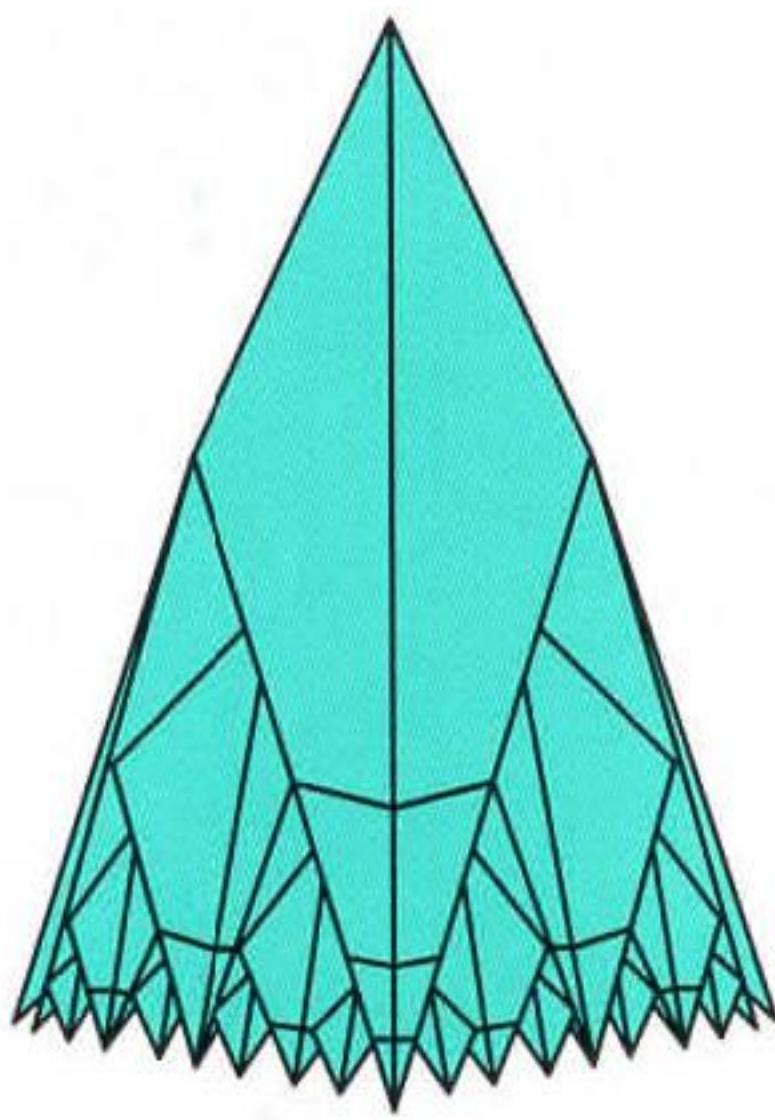


Start from step 13 of *Turkey*.



Fold two Water-bomb bases.

Repeat steps 18-26 of *Turkey*.



Self-similar and fractal

The main design aspect of *Turkey* is its repeating pattern at the tail. This pattern came from another model *Surf*, which is shown above.

I designed *Surf* not with an intention to design waves, but with a geometric interest in the crease pattern that repeat itself to branch infinitely.

Its basic structure is composed of the branches halving in the length and dividing into two, as shown on the right. The crease pattern is shown below. You can repeat the creases infinitely until the physical limitations of the paper.

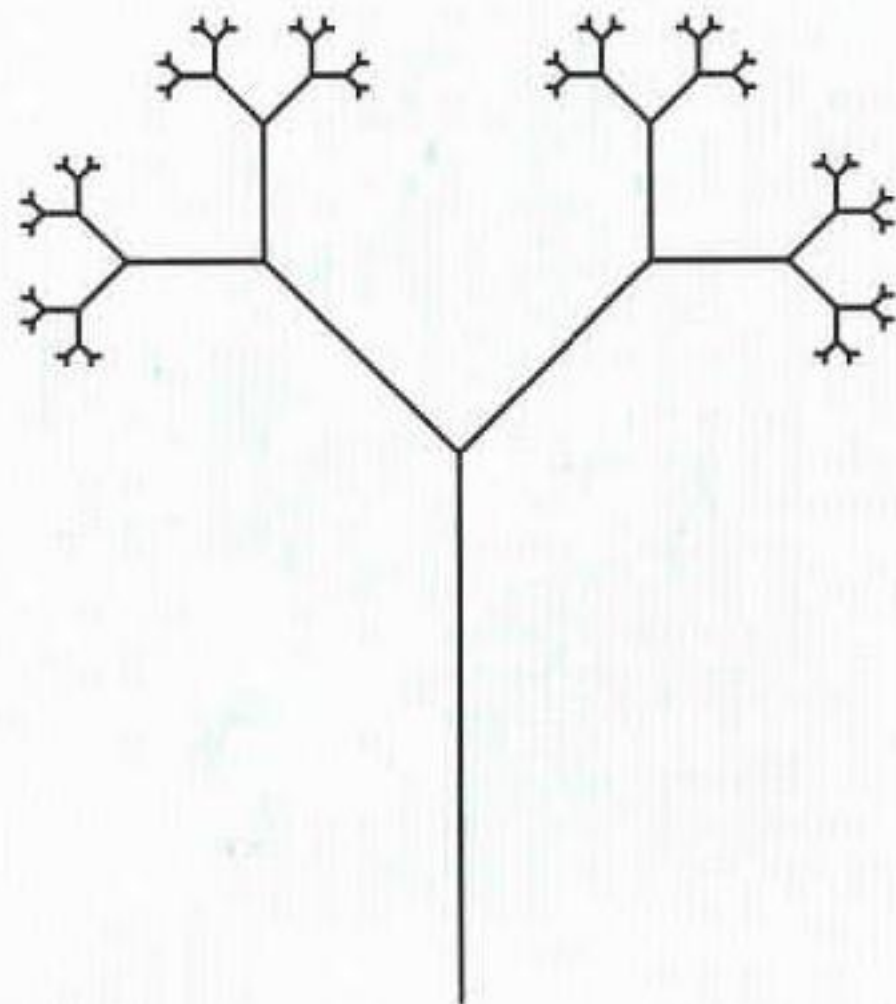
This figure is an example of self-similar shape, which is a shape whose part is similar in proportion to the whole. The patterns of *Tree* and *Pyramid* are also self-similar. While those patterns are self-similar at one point, the pattern of this model is self-similar at an area with some length, that is, the ends of branches.

The notion of self-similar is one of the most important elements of fractal geometry.

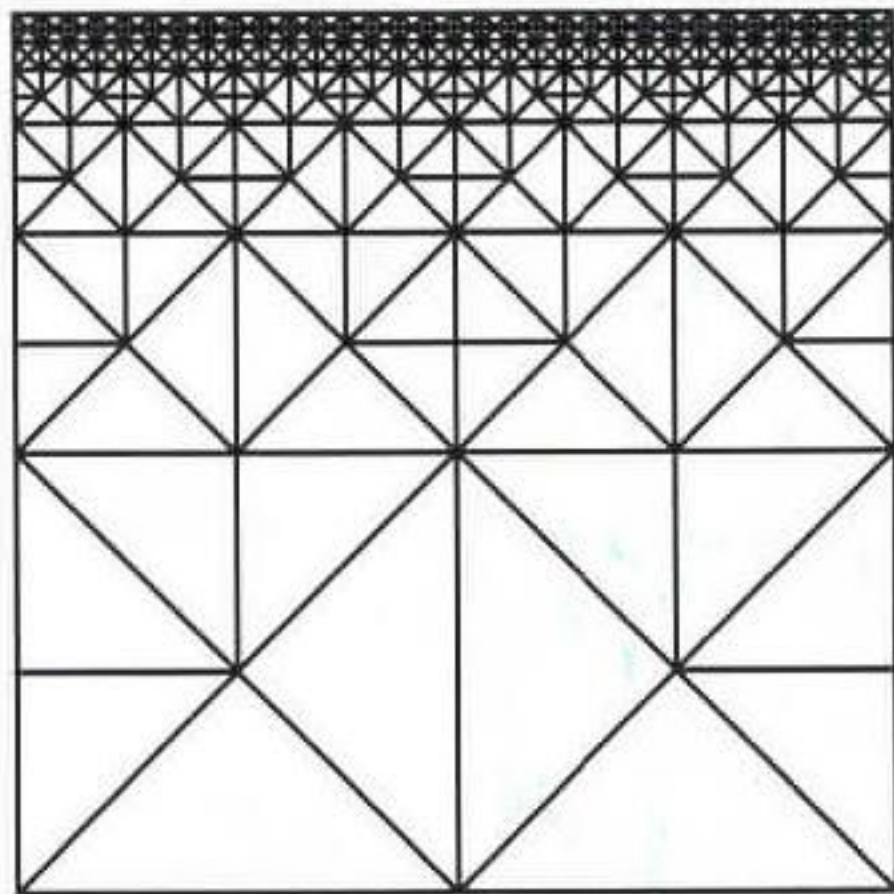
In the crease patterns of *Surf* and *Turkey*, the total length of creases increases by the same amount at each step, because the number of creases becomes twice and the length of each one becomes half. Such “nested” branching structure is called sub-fractal in fractal geometry. This quasi-fractal structure is common in nature, plants like trees and cauliflowers, branches of rivers, and ramification of blood vessels.

Fractal geometry is not just a field of geometry but also a new viewpoint to recognize the nature, as the title of the book written by Benoît Mandelbrot, who is the advocator of fractal geometry, is *The Fractal Geometry of Nature*.

While the father of the modern painting Paul Cézanne said, “treat nature by the cylinder, the sphere, the cone,” Mandelbrot wrote that “Clouds are not spheres, mountains are not cones, coastlines are not circles, and bark is not smooth, nor does lightning travel in a straight line.” I am not saying that Cézanne was wrong. In fact, I privately call my own cone-based model *Penguin* “Cézanne origami” and am arrogantly self-satisfied. But it is also true that the design with self-similar repeating patterns is wonderfully interesting, in a little different way from the design with solid bodies such as with cylinders and cones. And some of such designs are truly “origami-like.”



The basic structure

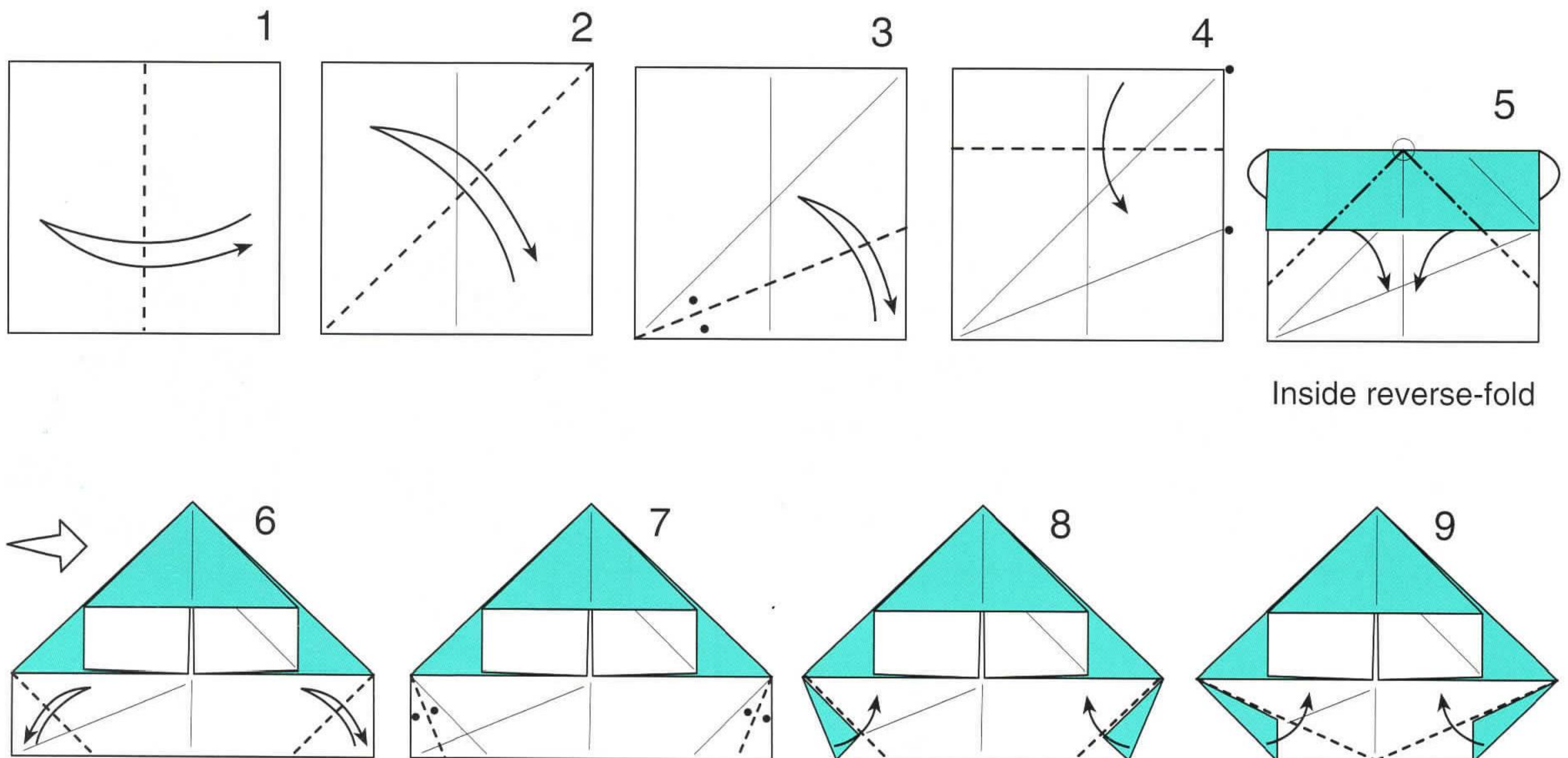
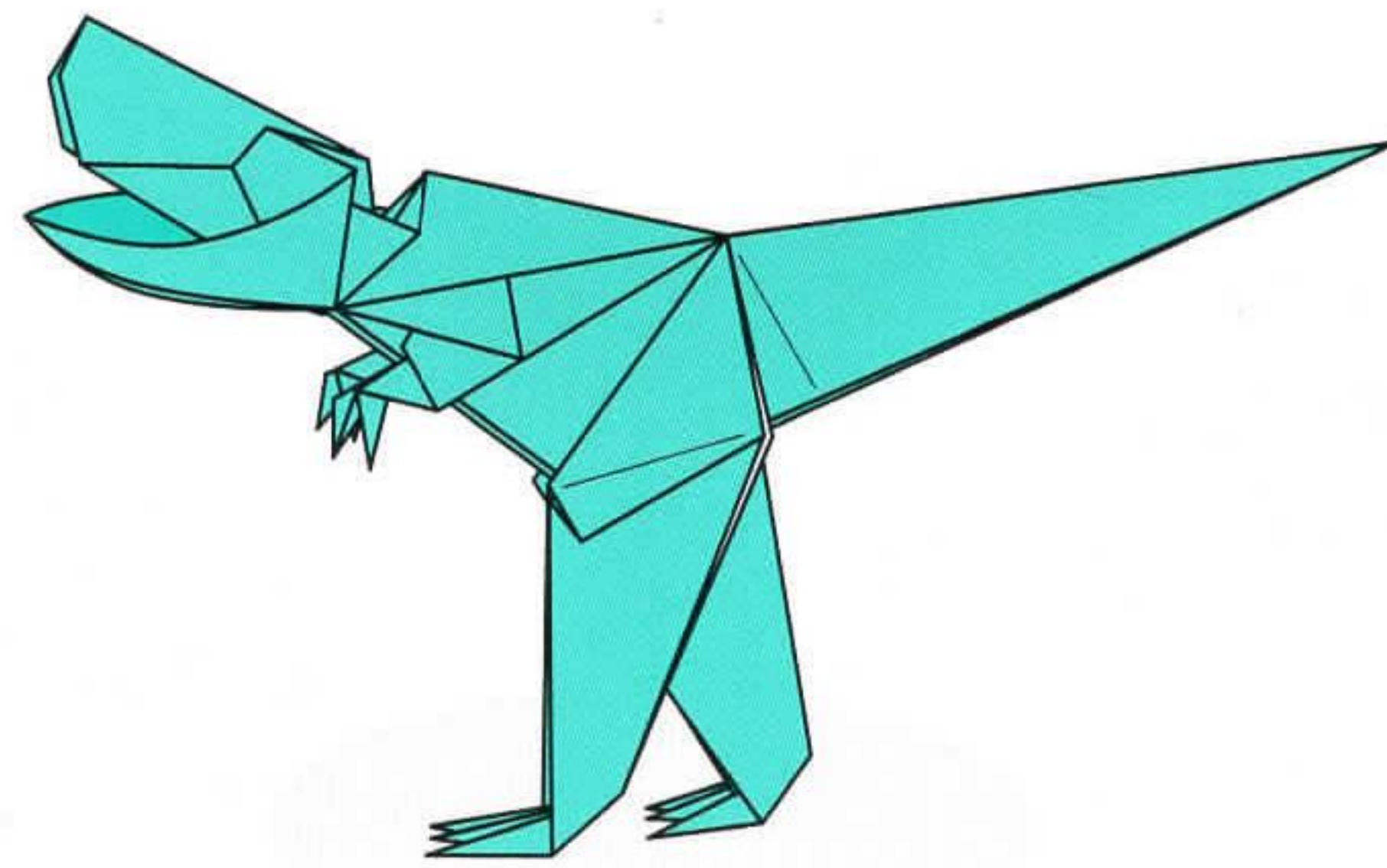


The crease pattern of *Surf* (mountain and valley folds are not shown).

Tyrannosaurus

Theme: Realism

Difficult to fold using 6" (15 cm) origami paper.
10" (25 cm) or larger paper is suggested.



Realism in origami

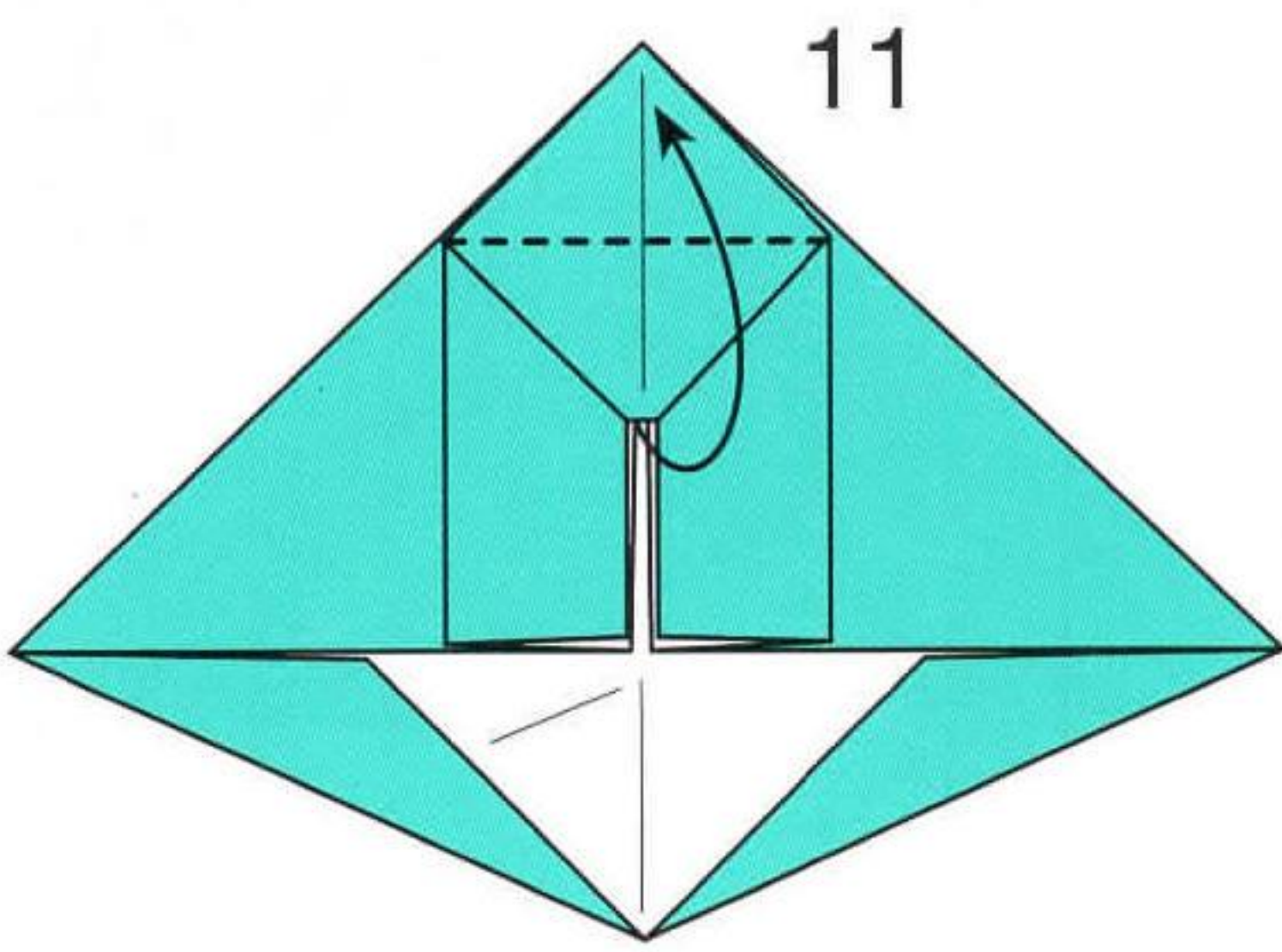
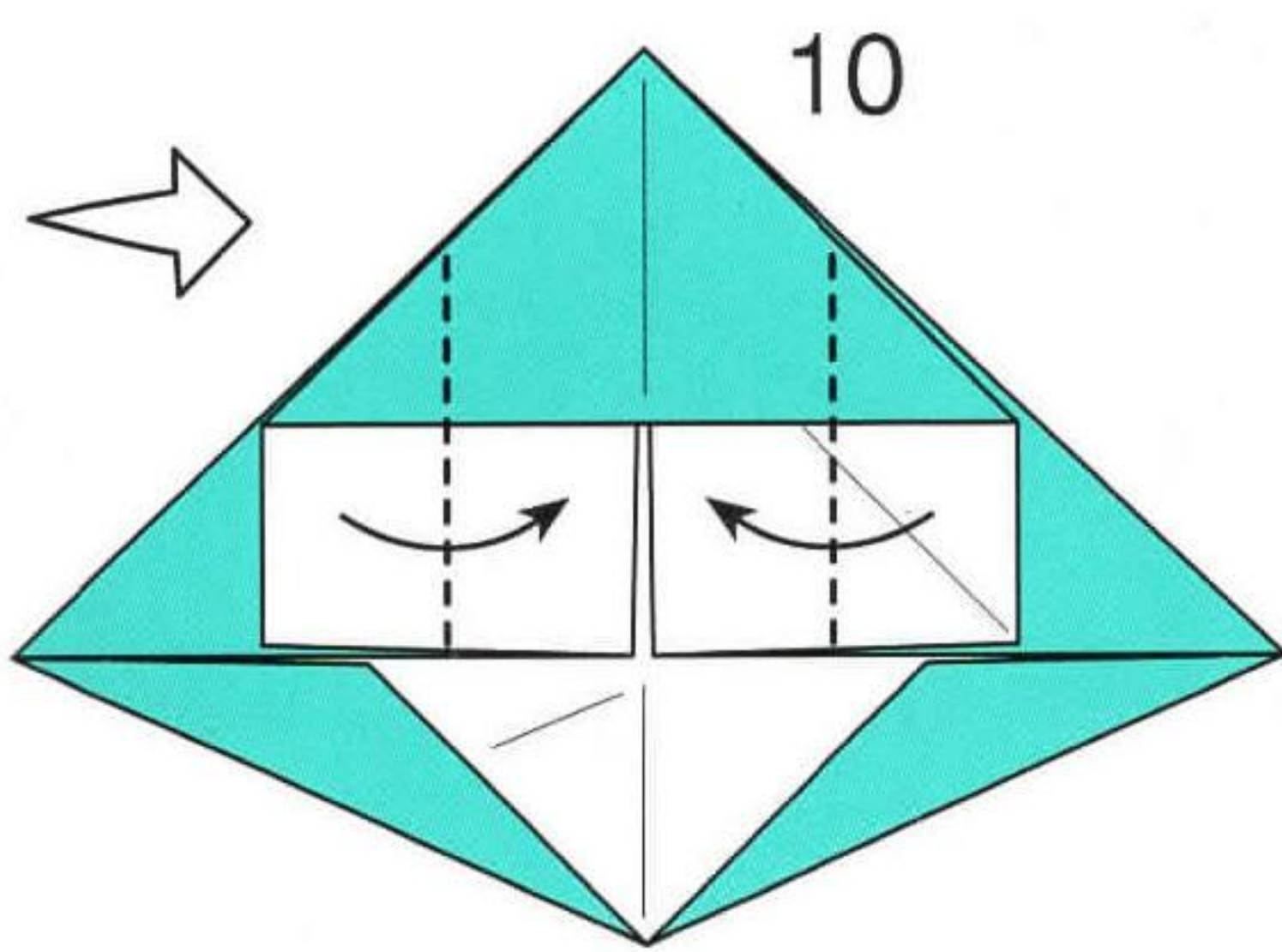
I published a *Tyrannosaurus* in the past. But now I am ashamed of that model. It is partly because I failed to adopt the knowledge of current paleontology, but also because I made many mistakes that are just out of the question. Although it may have been inevitable that the model has the tail dropping down like a kangaroo, I would say it is a model of another species of dinosaur because it had three fingers at each foreleg, which was even emphasized in that design. In this version of *Tyrannosaurus*, I aimed for realism, though somewhat deformed.

Living creatures is the most popular theme in origami. One cannot deny that, in addition to the richness of geometry, the diversity of forms in the creatures and natural world is an inexhaustible source of origami design.

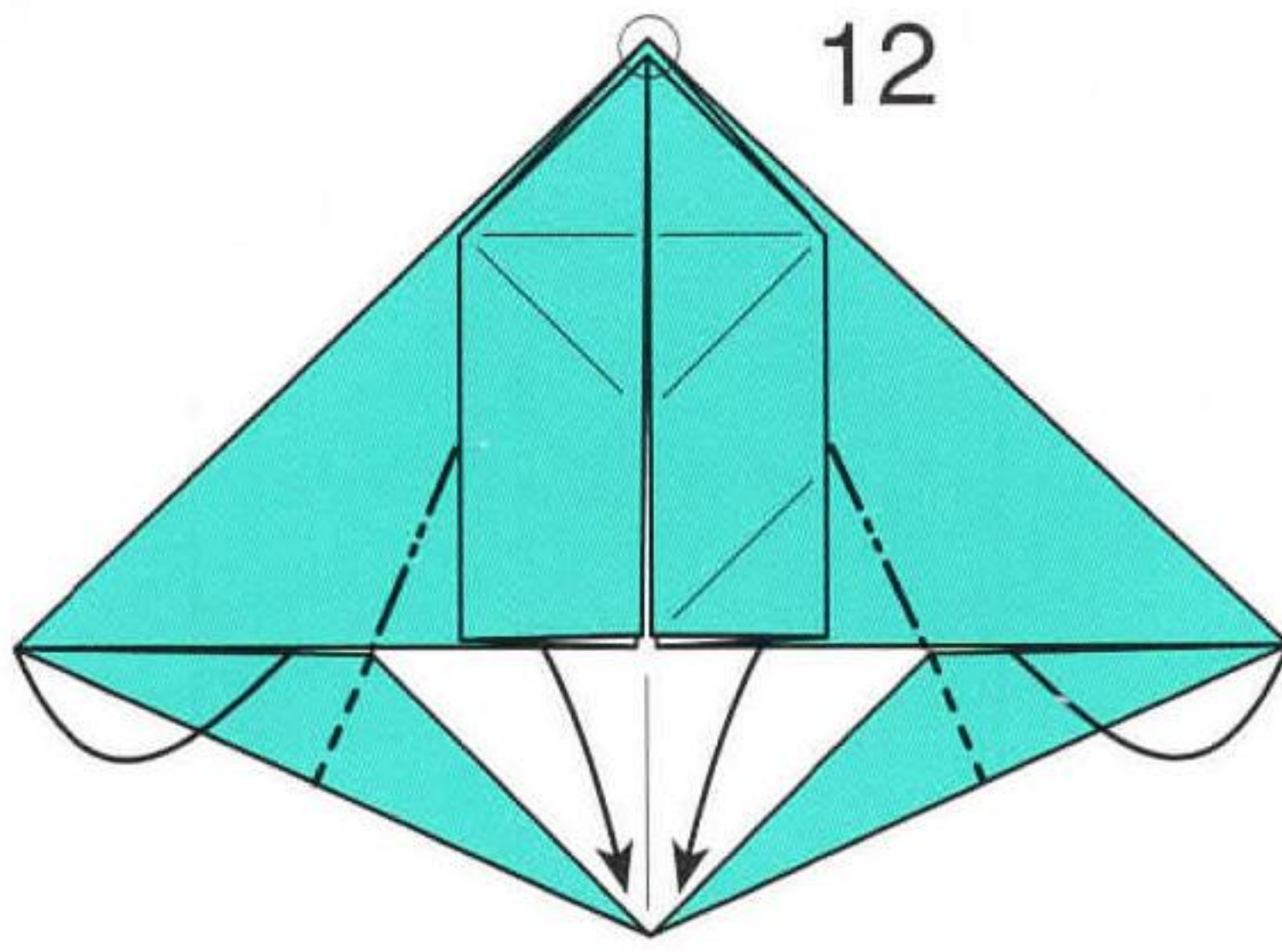
However, I always feel that the important thing is not only to pursue realism using techniques and skills. I personally give priority to the ideas of geometric design over the intention of making realistic models. My main priority for design is to achieve balance between "mitate" and geometry. That may be the definition of the notion of "origami-like" for me.

At the same time, I think other factors also define "origami-like." For example, capturing the characteristics of the subject with only one or two strokes, as in sketches, is also one of the ideals of origami design. But such models inevitably contain many "judgment folds" that decrease the geometric interest. That is annoying for me.

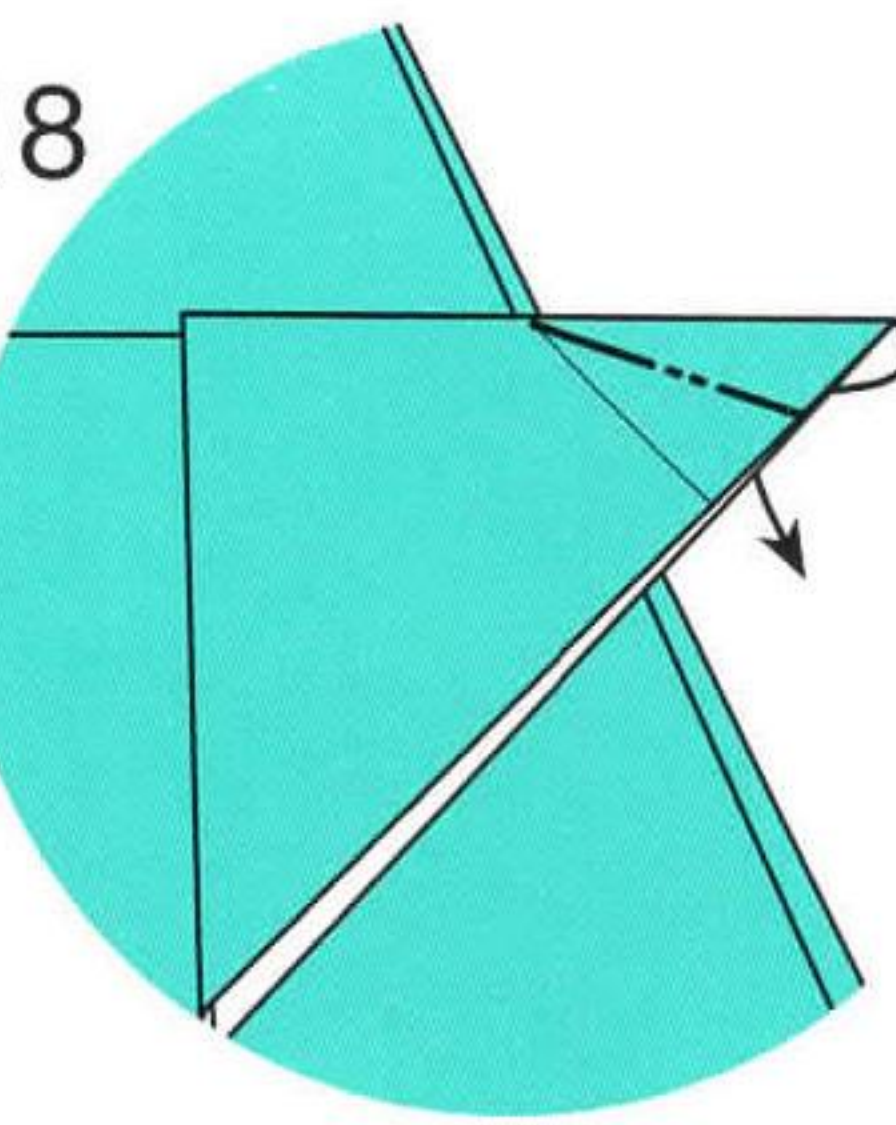
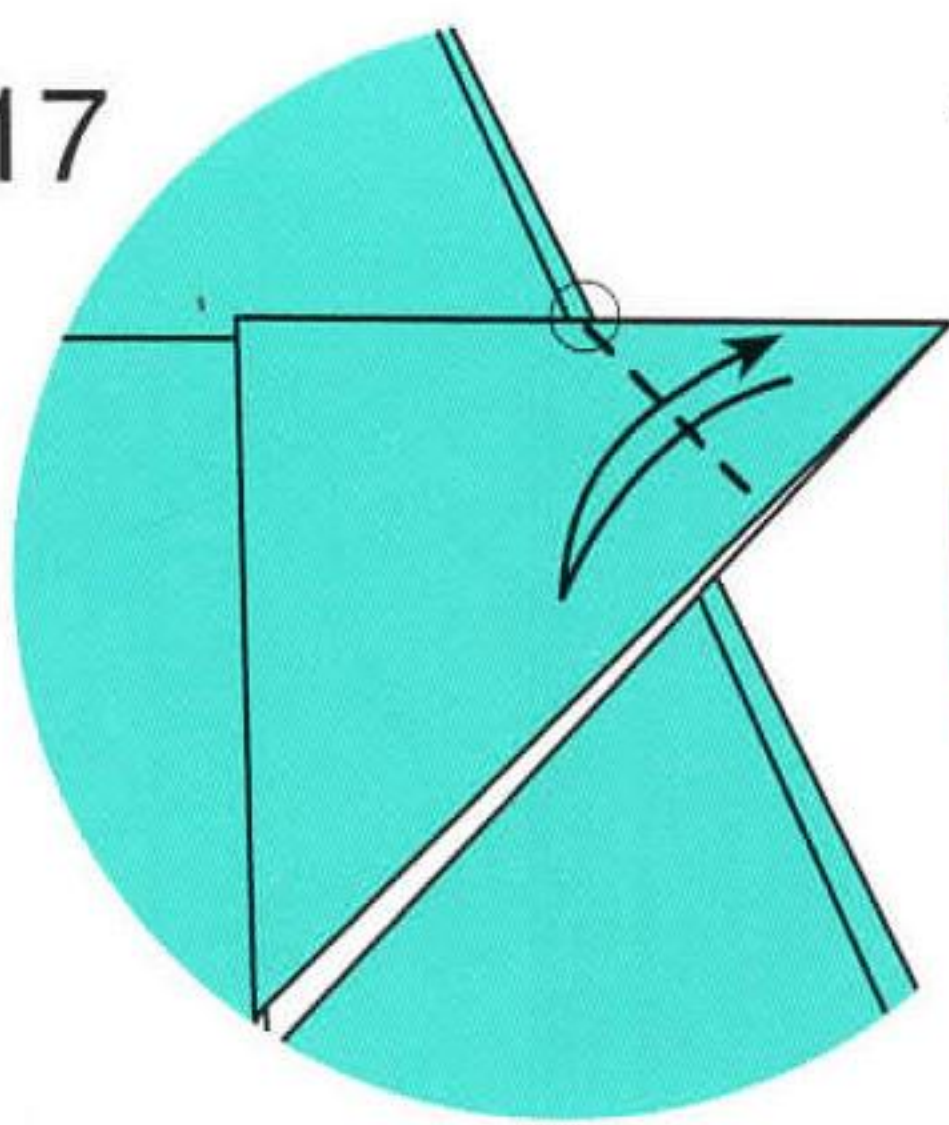
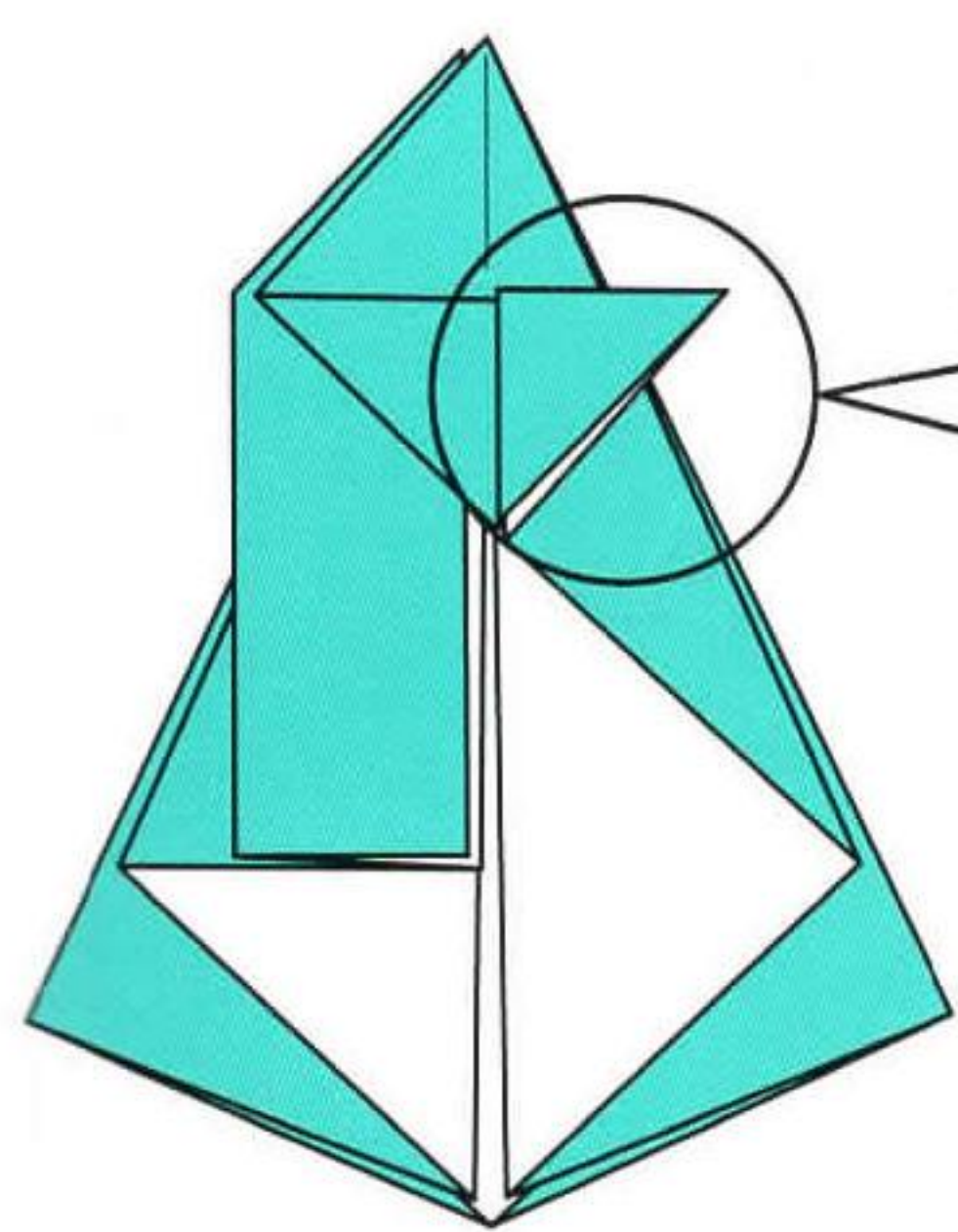
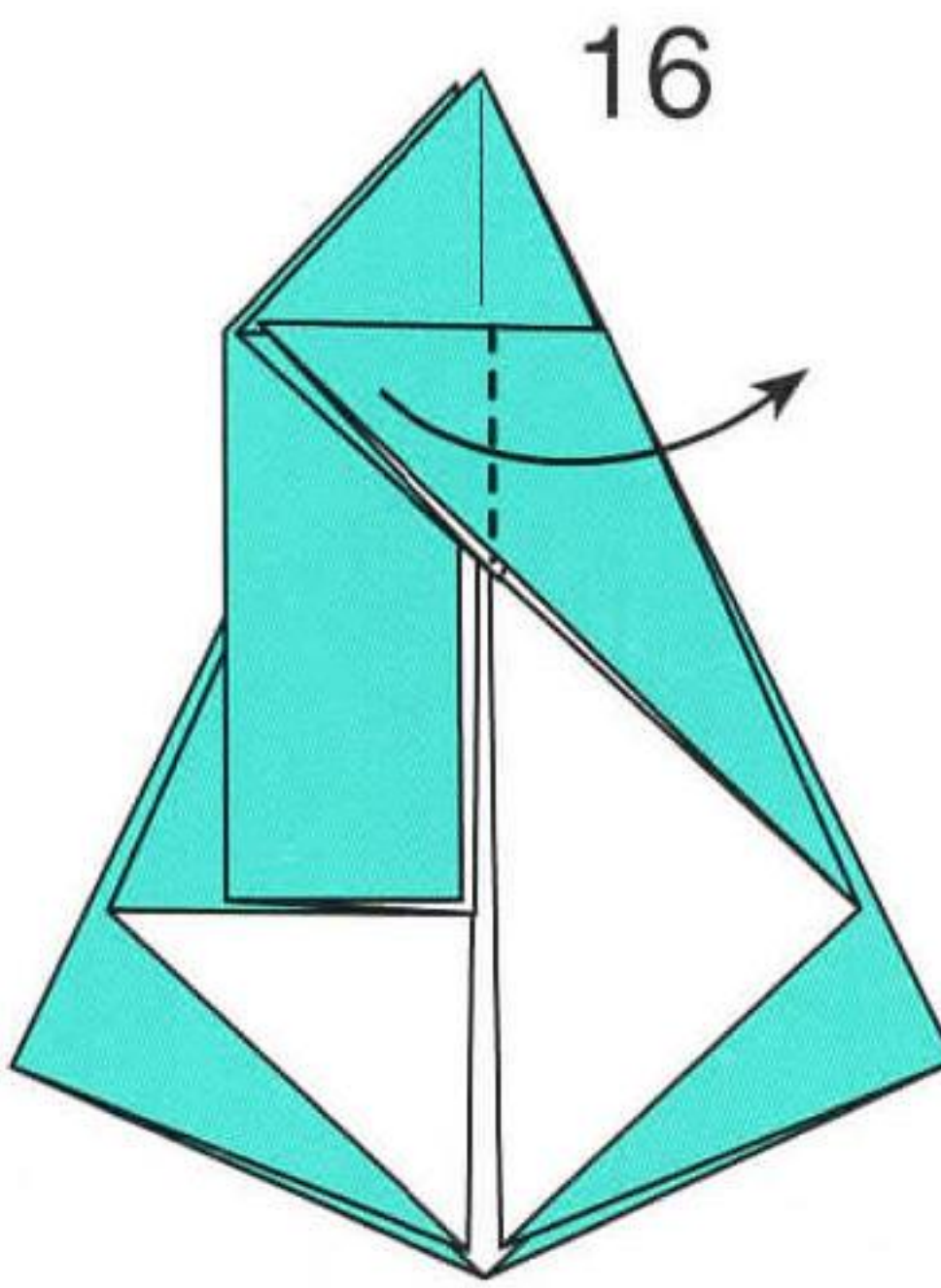
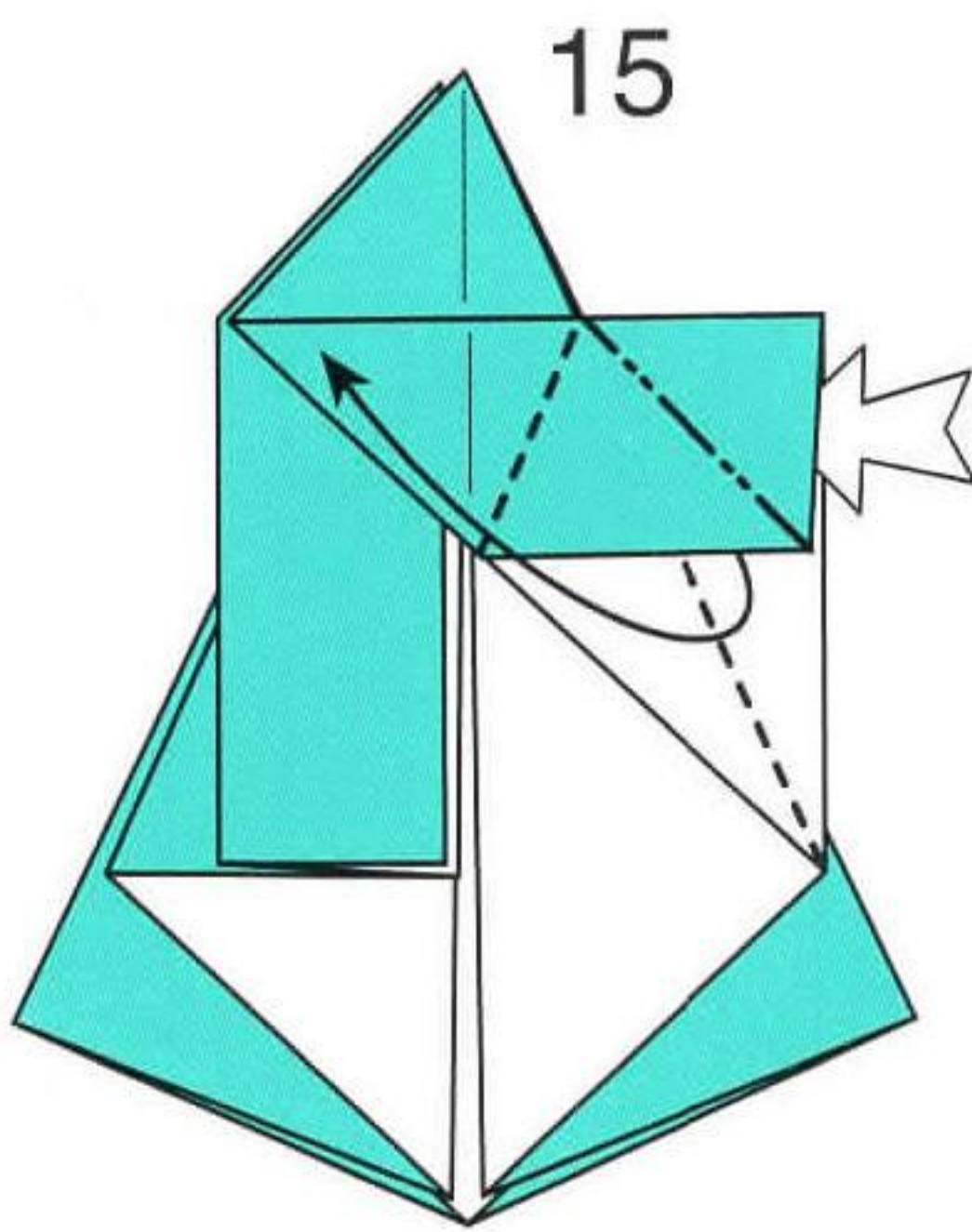
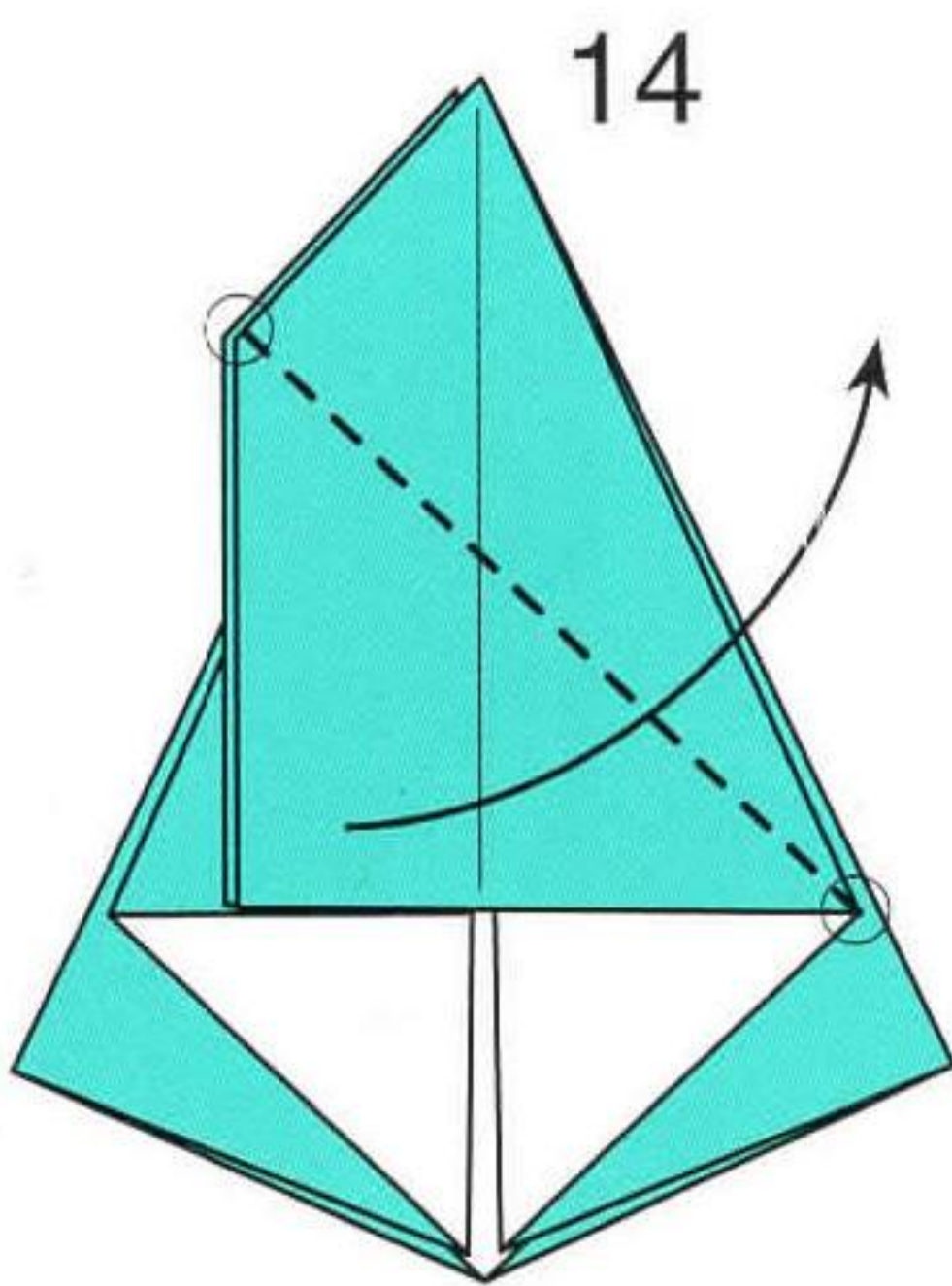
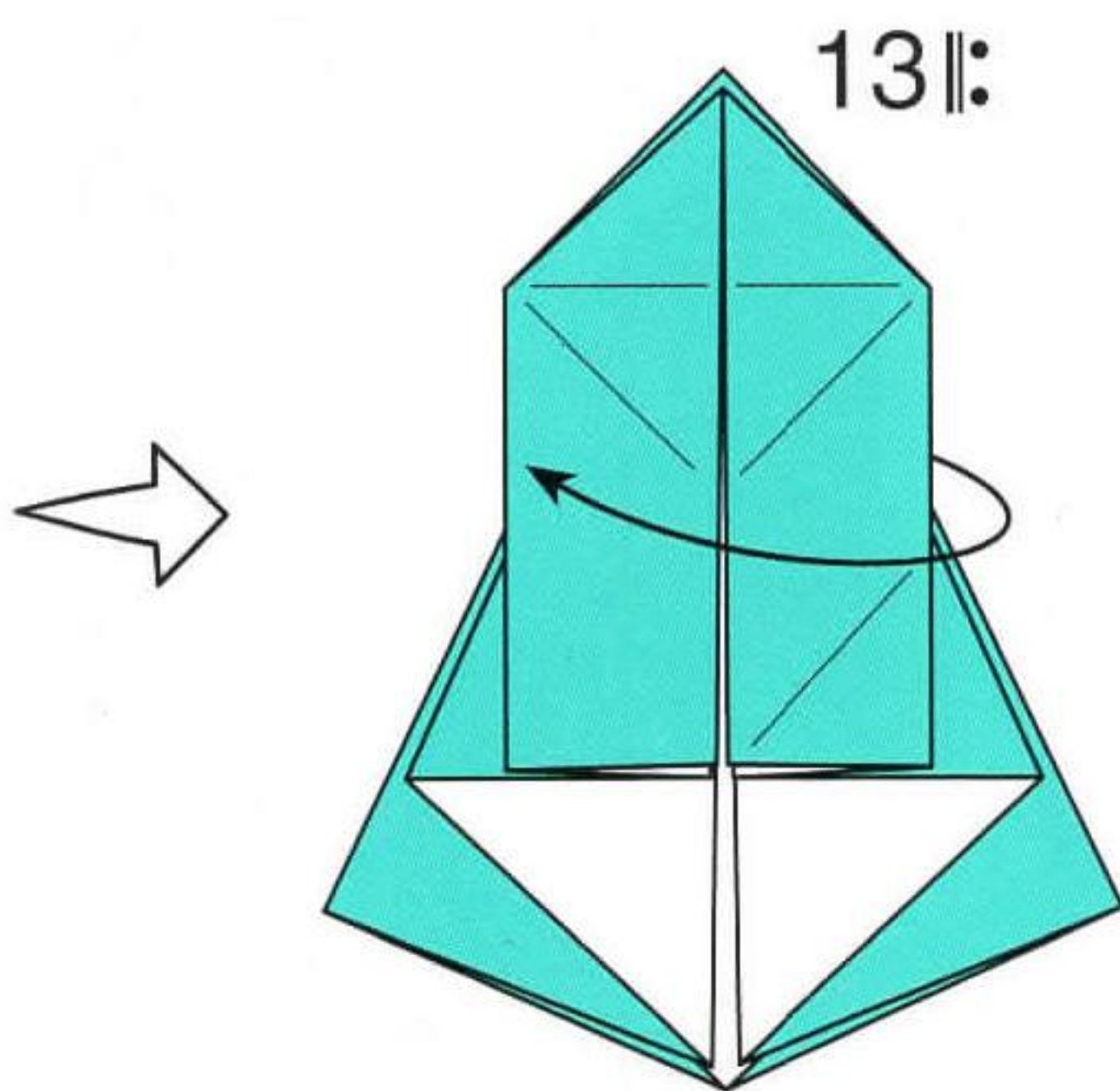
Another factor that defines origami design is the diagramming. I prefer such a design that folders can reproduce obtaining the same result by following the diagrams. This condition often enhances the quality of design rather than compromises it.



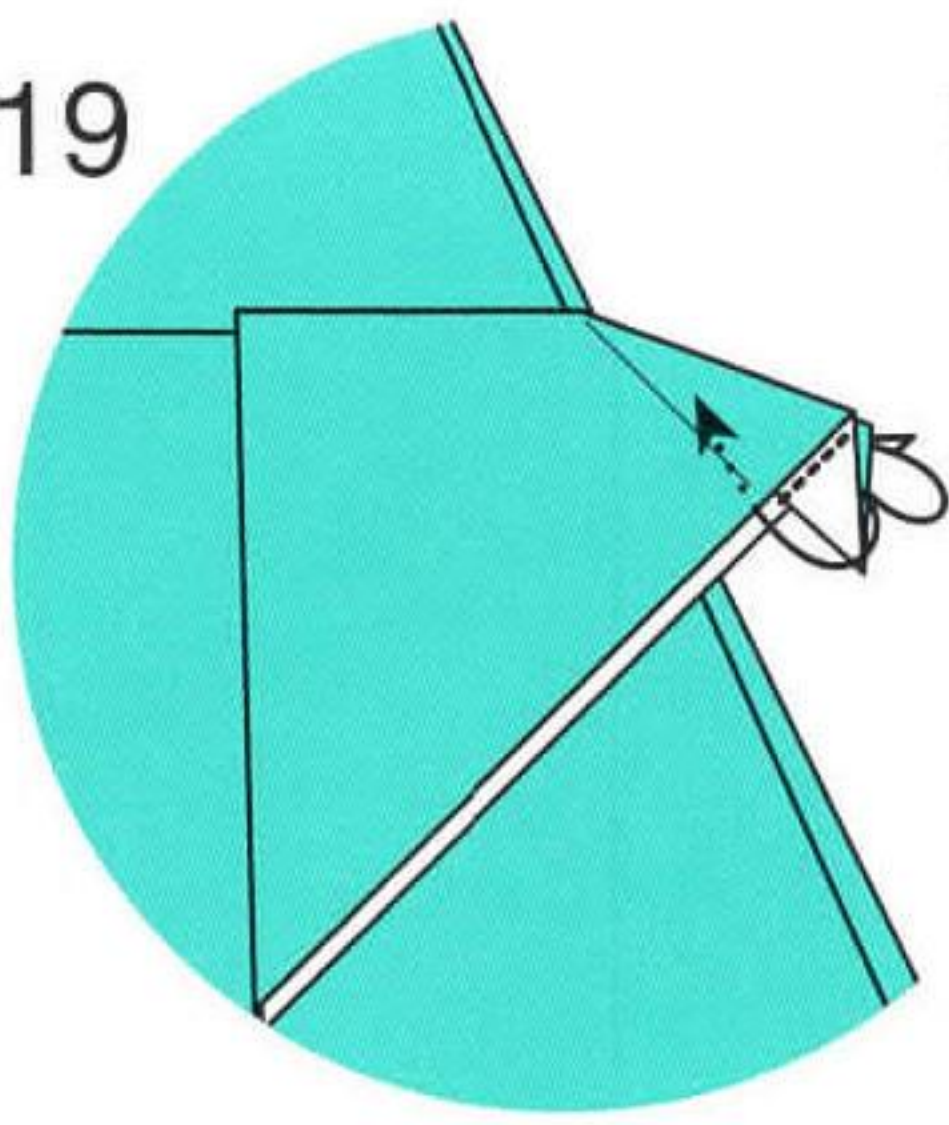
Petal-fold



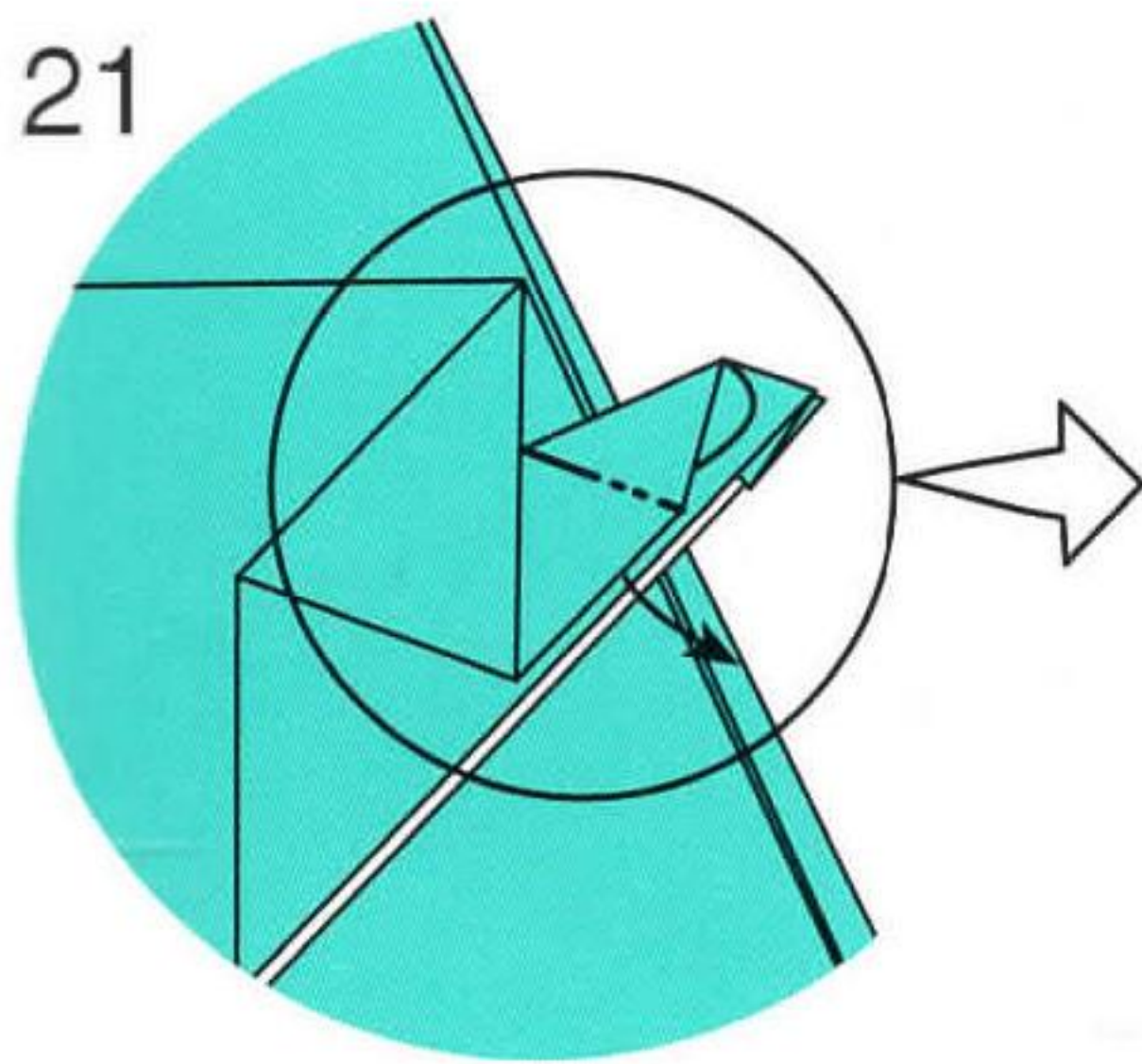
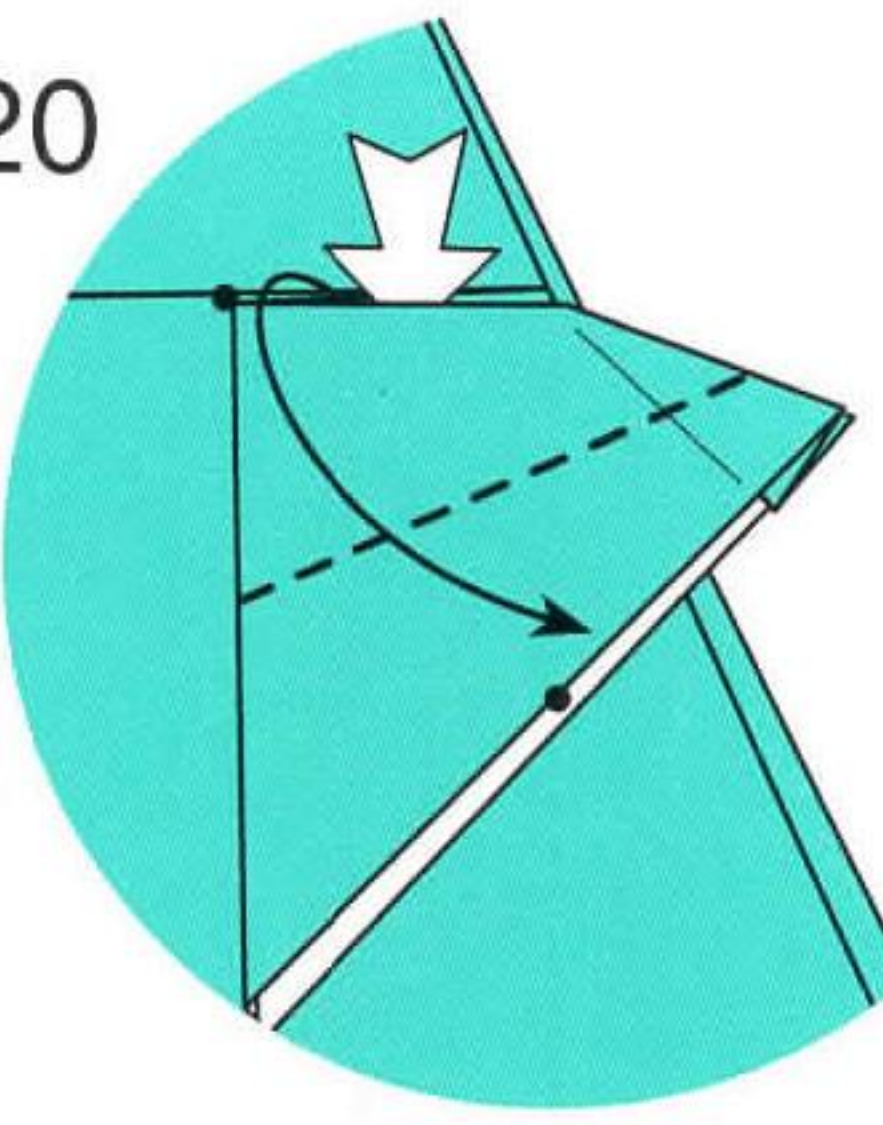
Inside reverse-fold



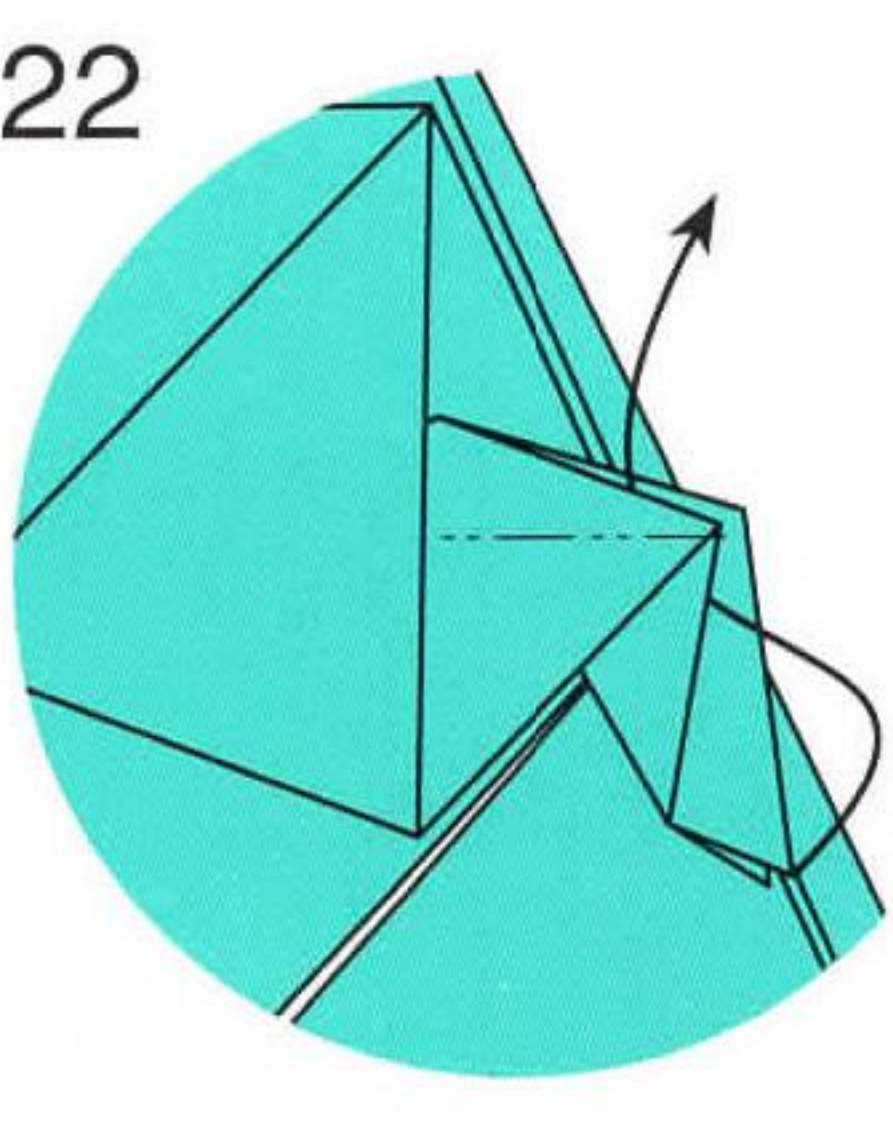
Inside reverse-fold



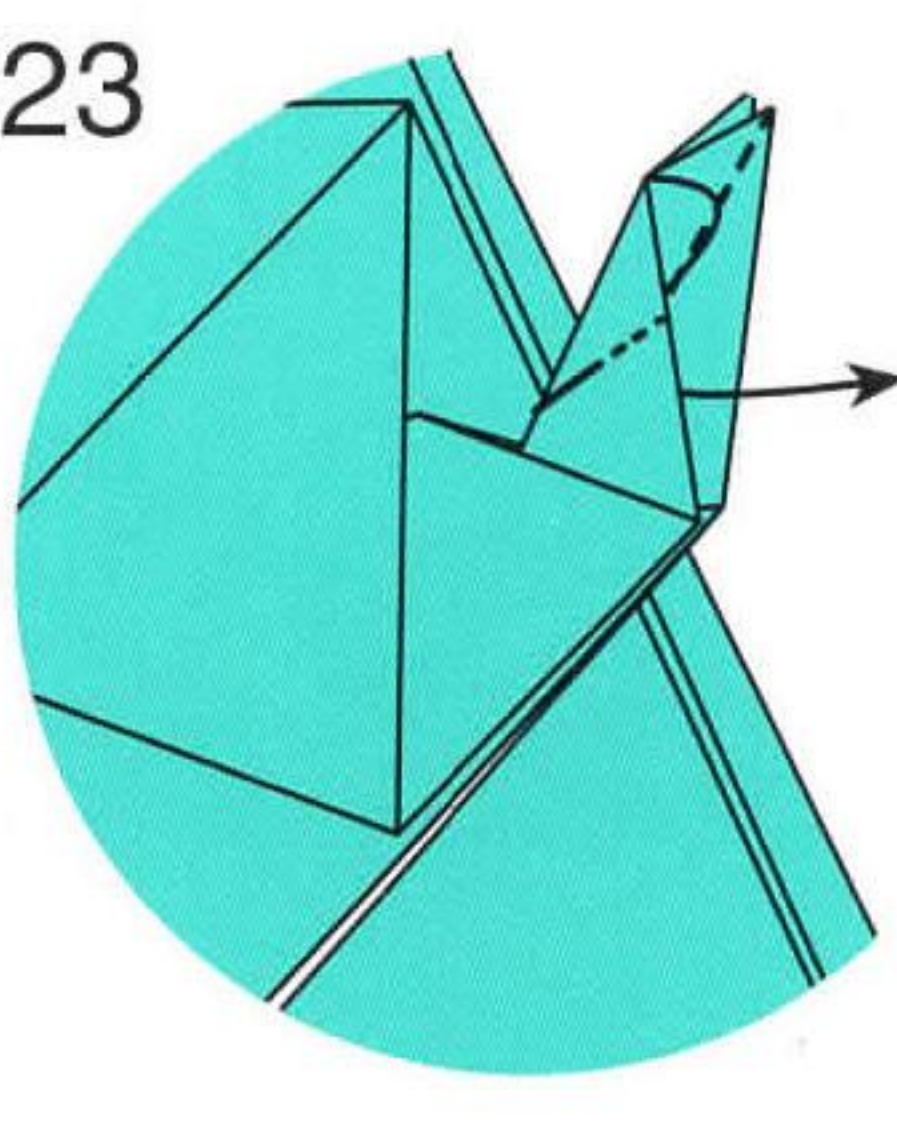
Outside reverse-fold inside



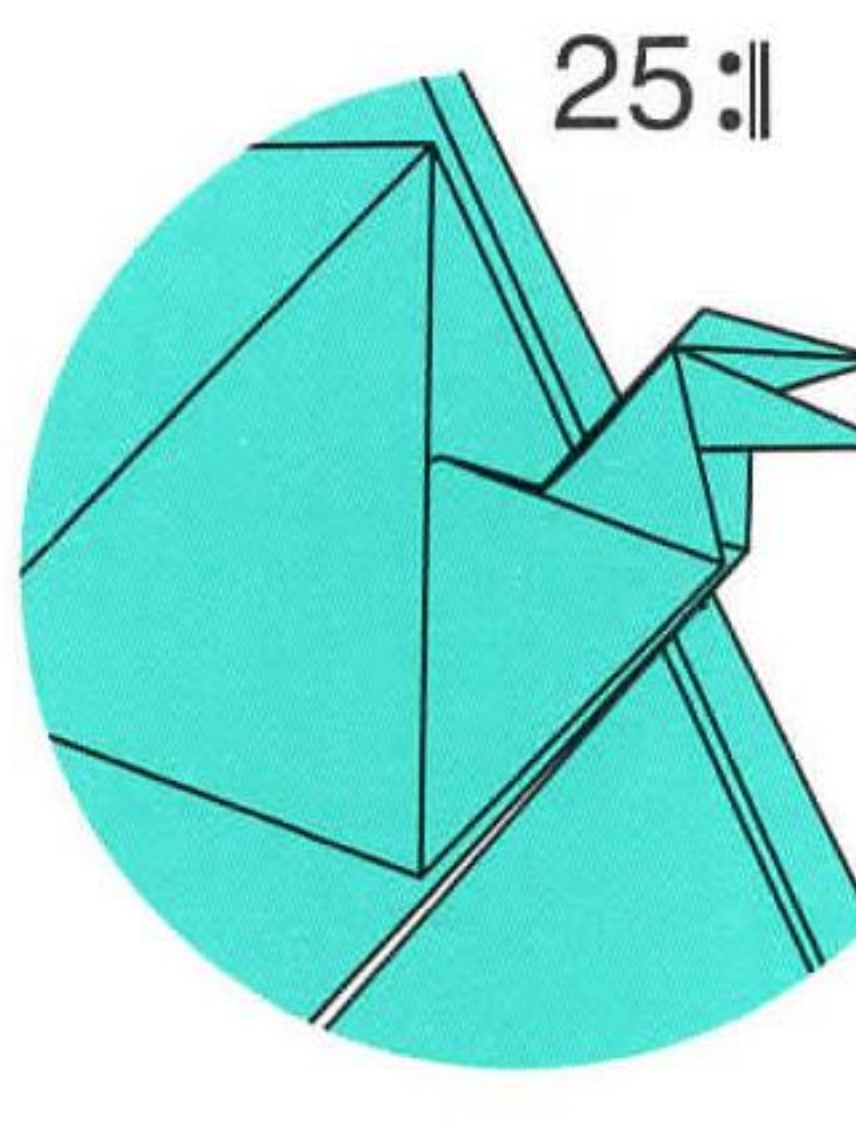
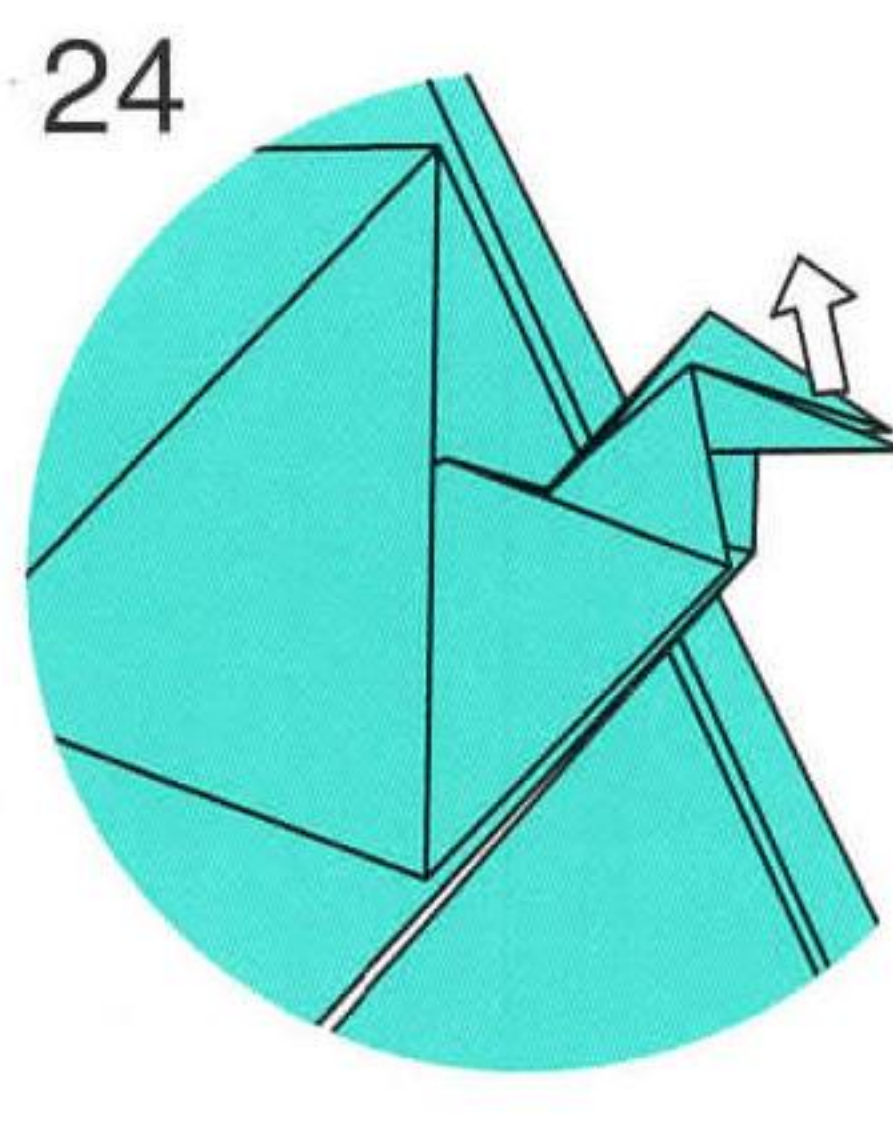
Inside reverse-fold

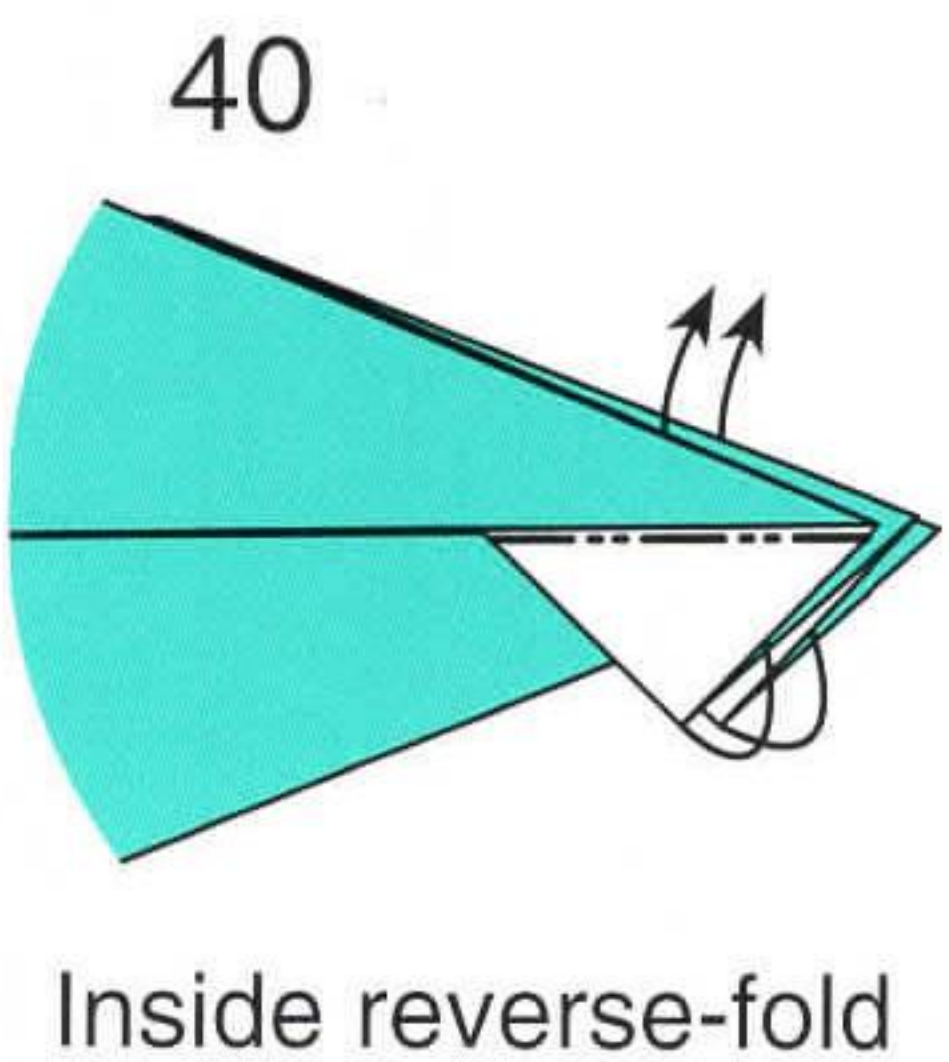
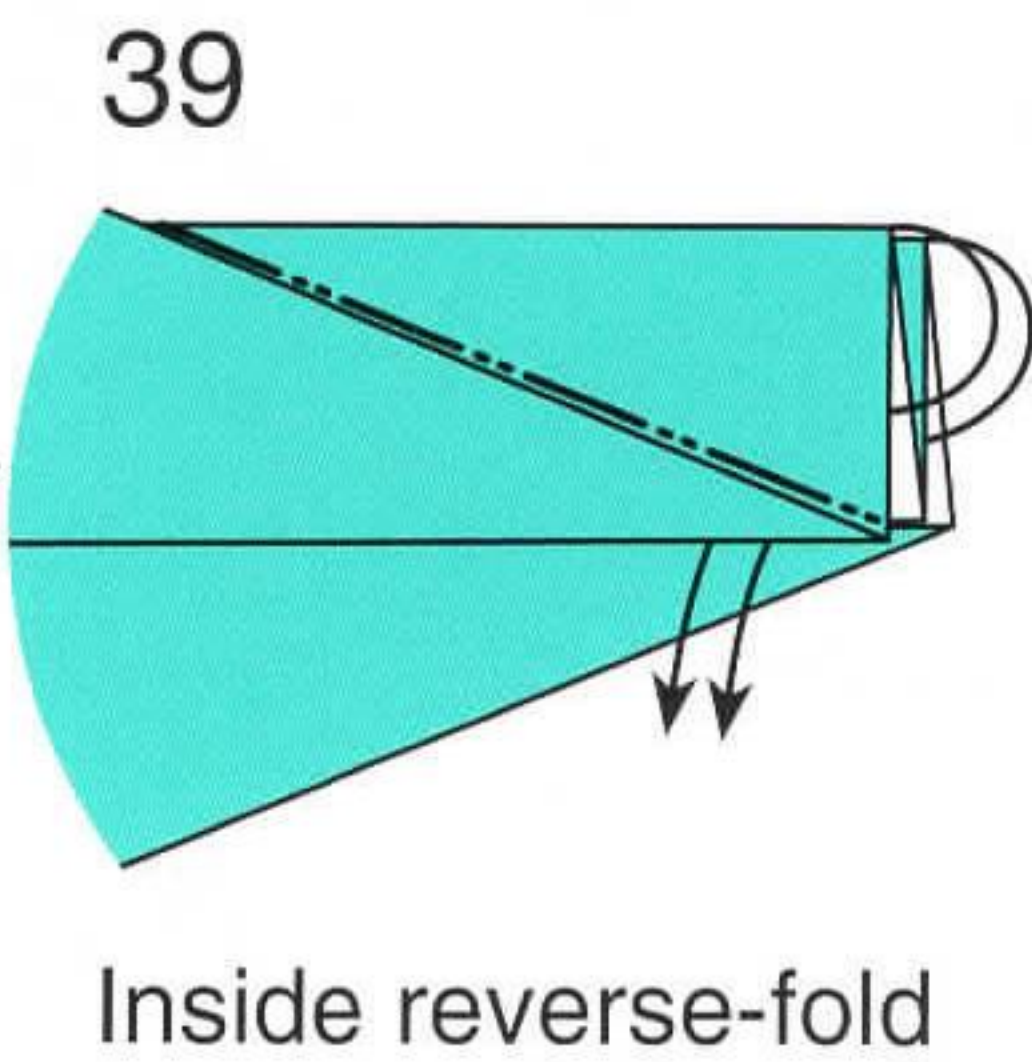
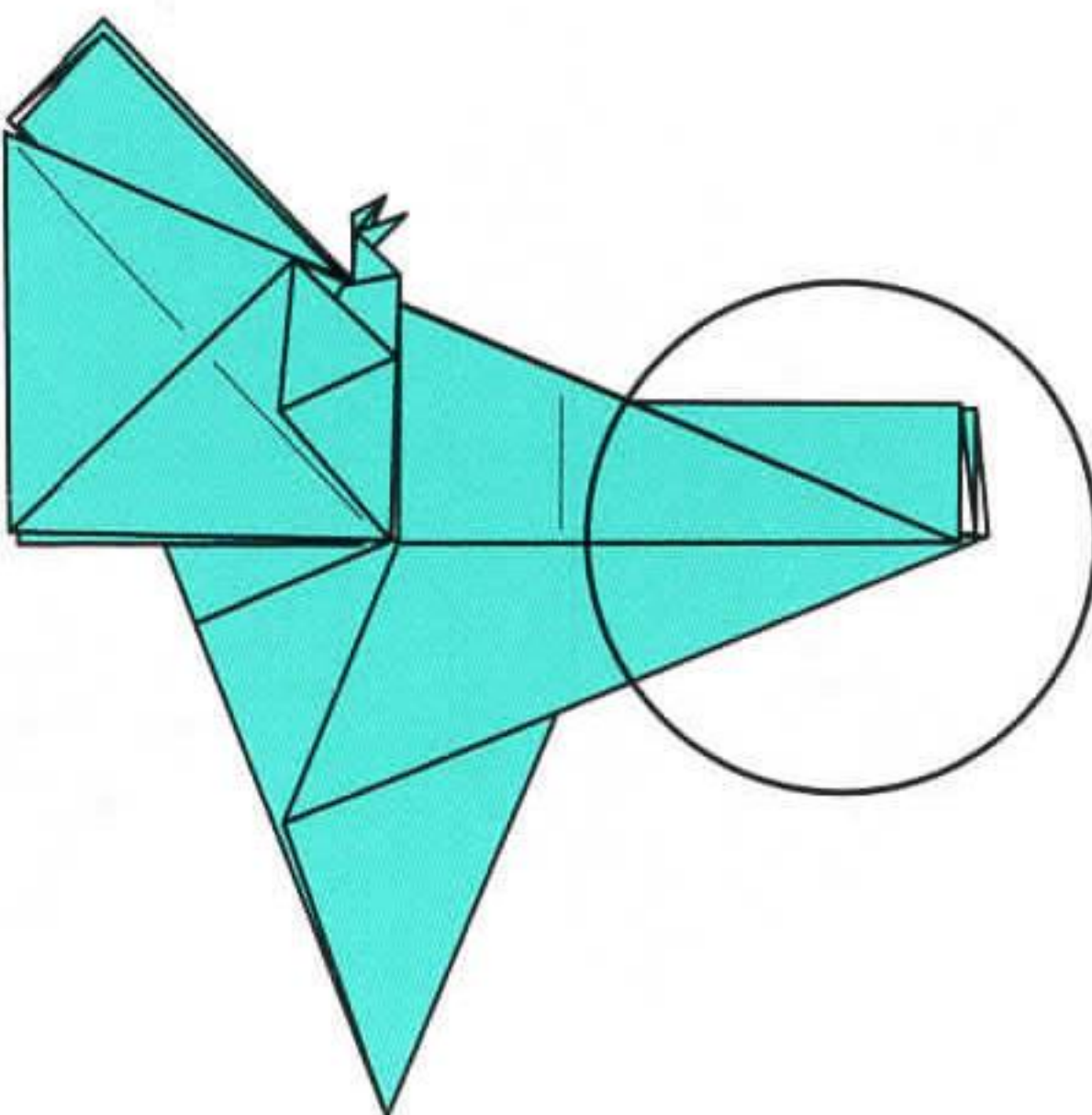
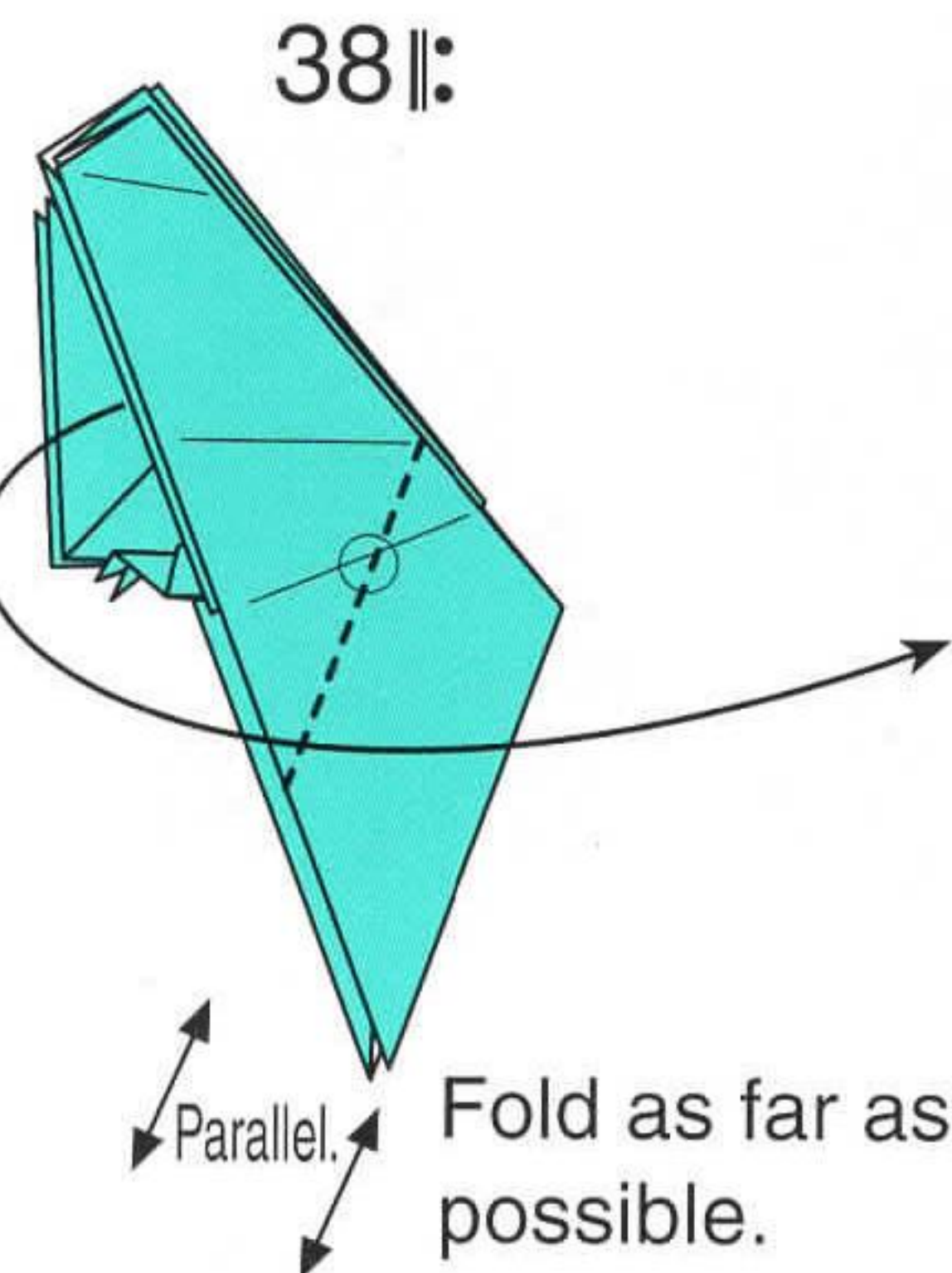
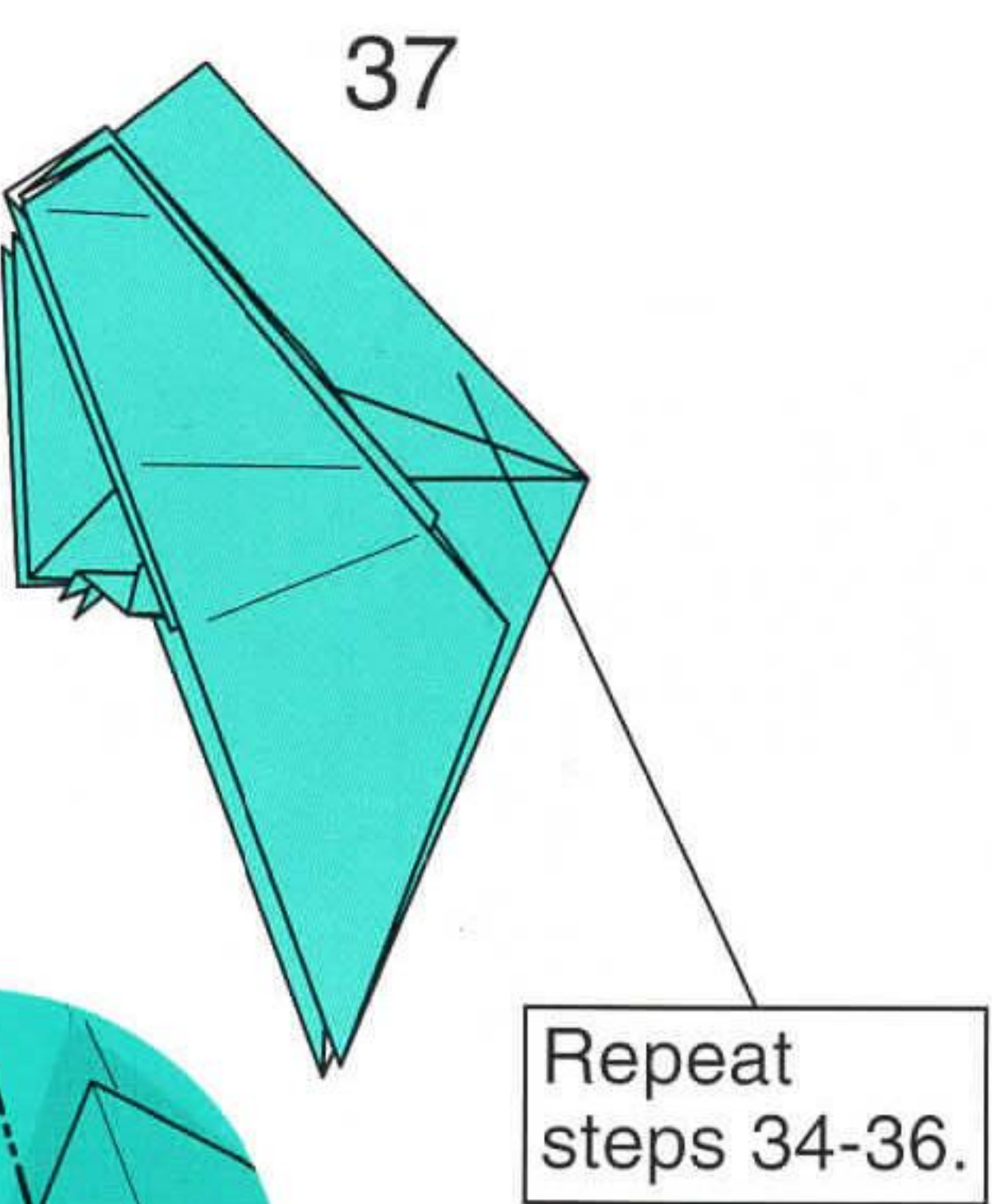
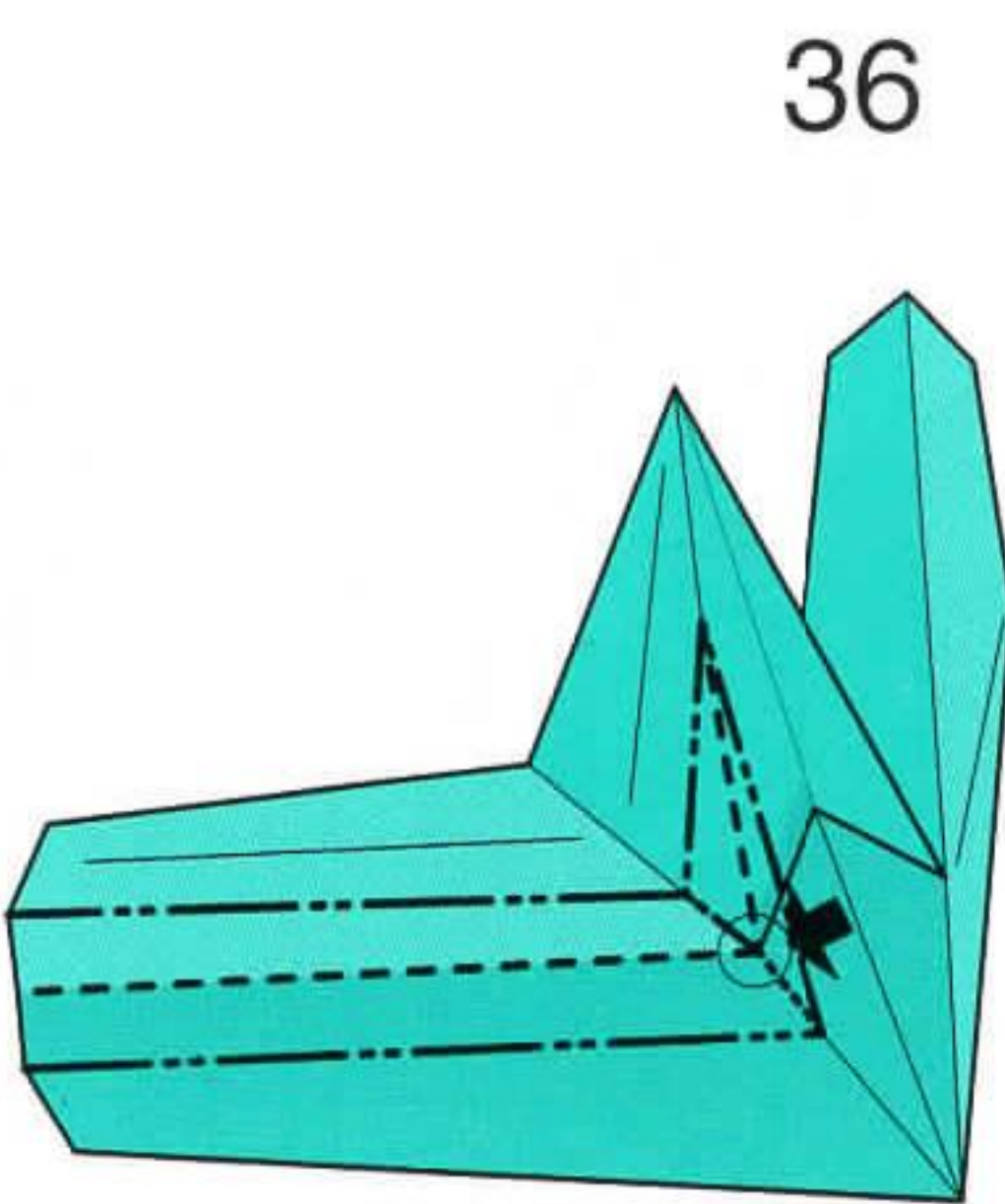
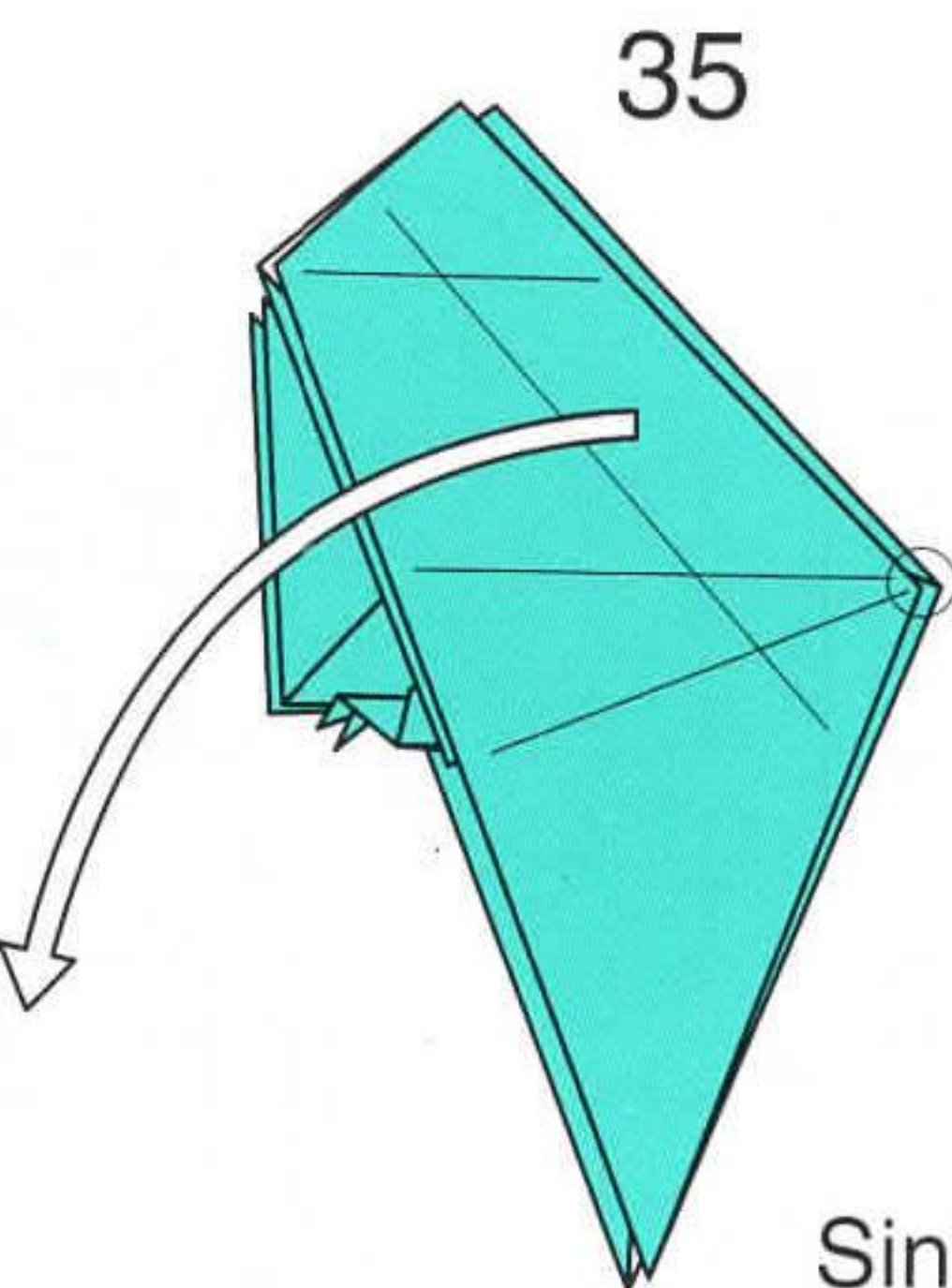
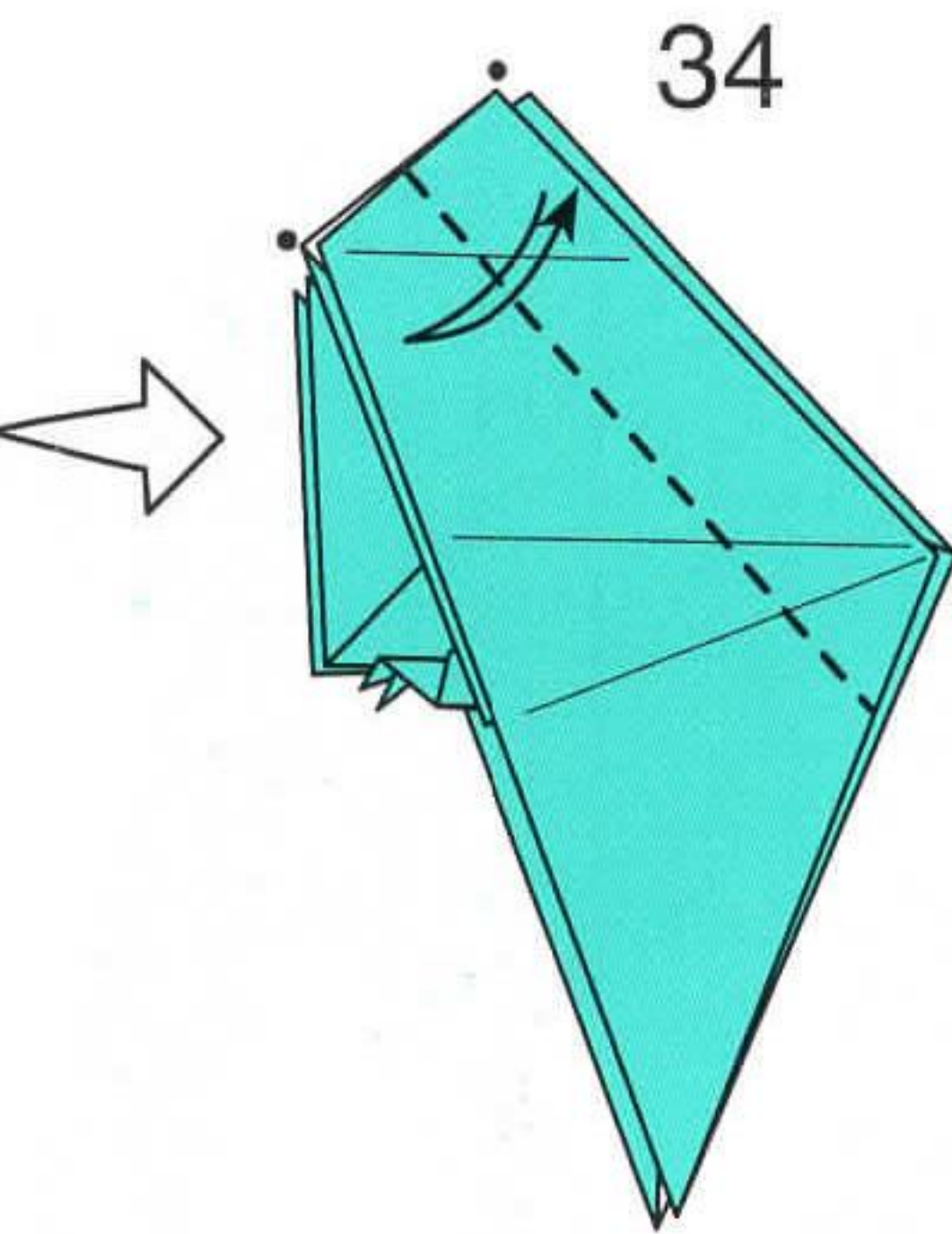
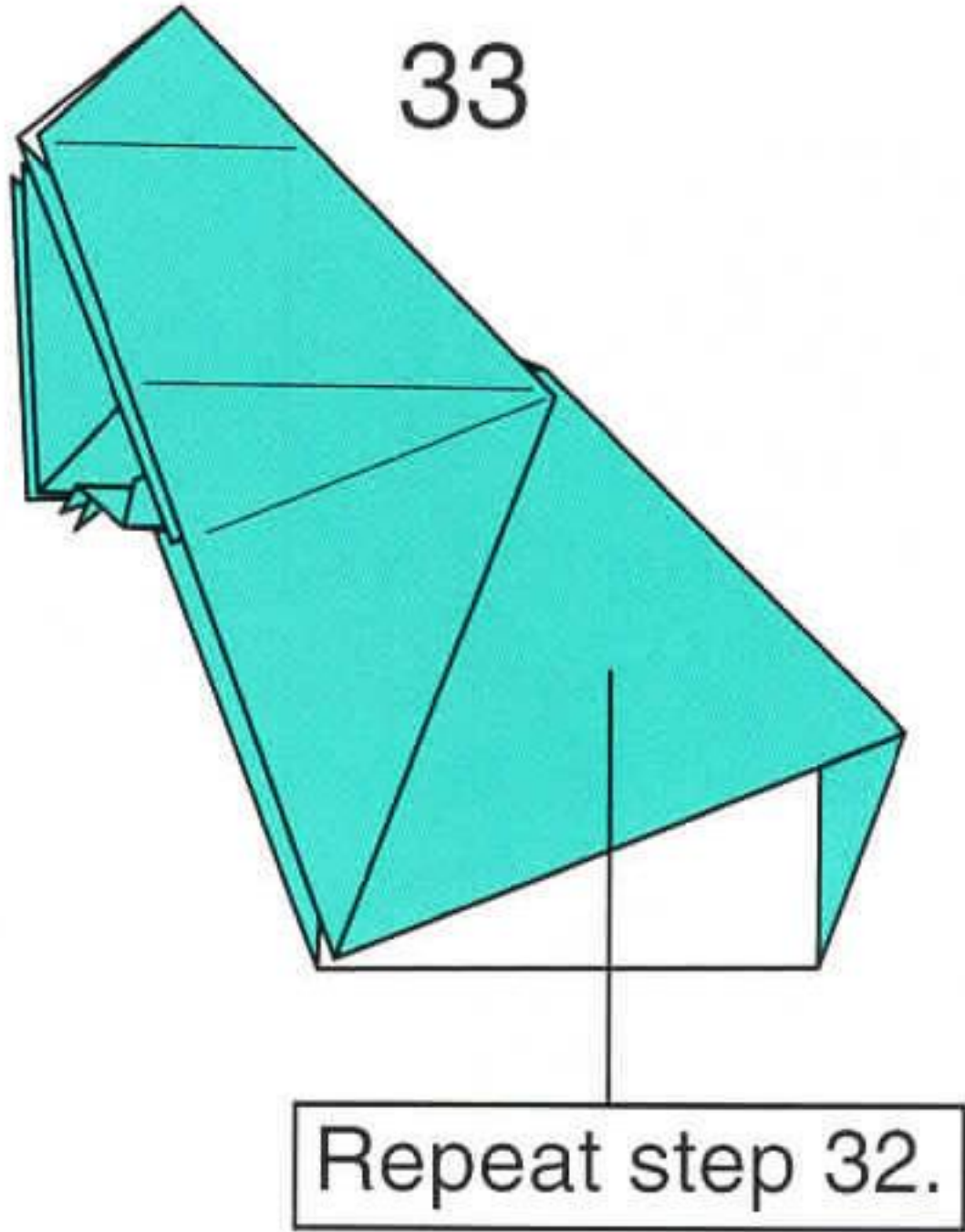
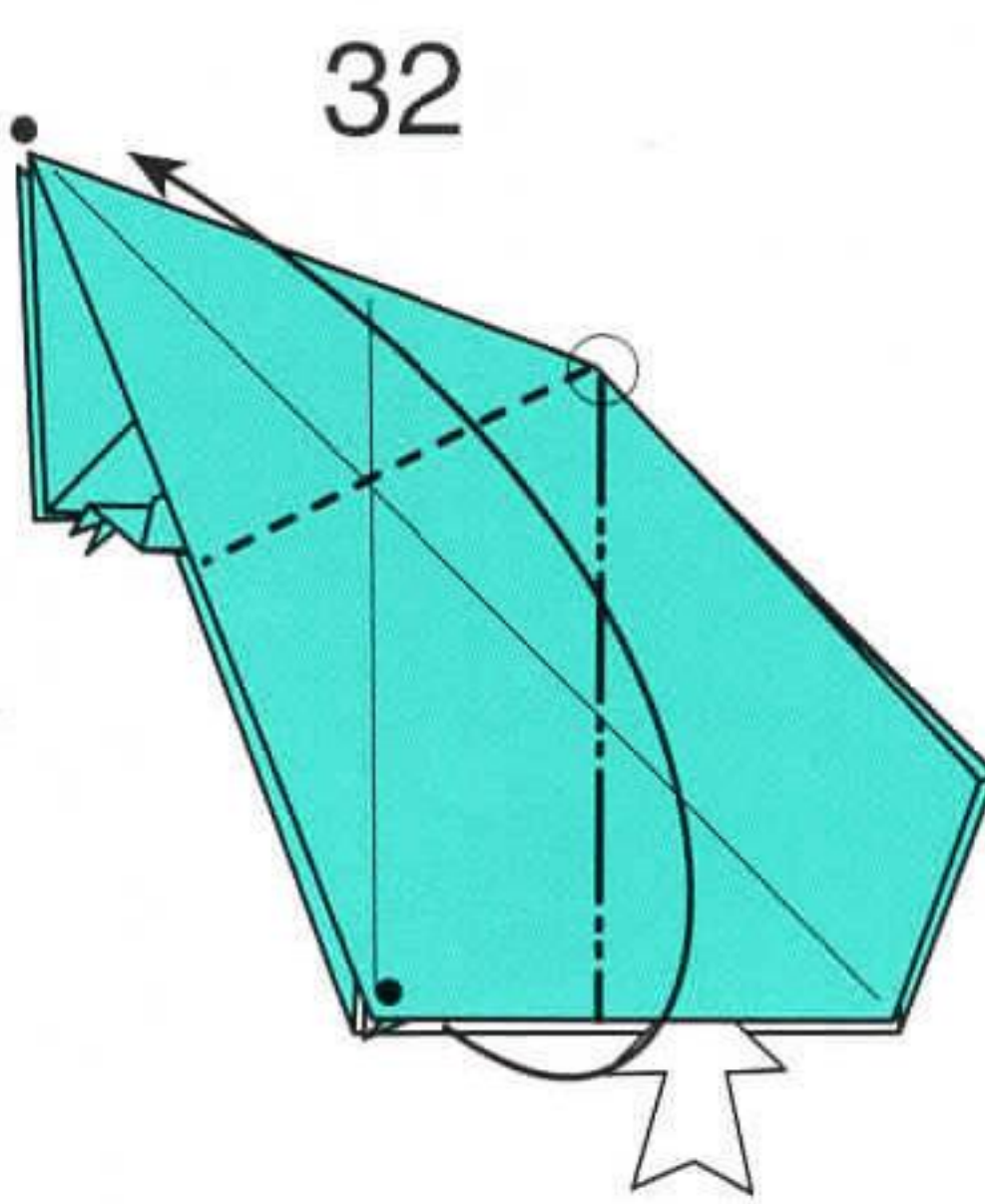
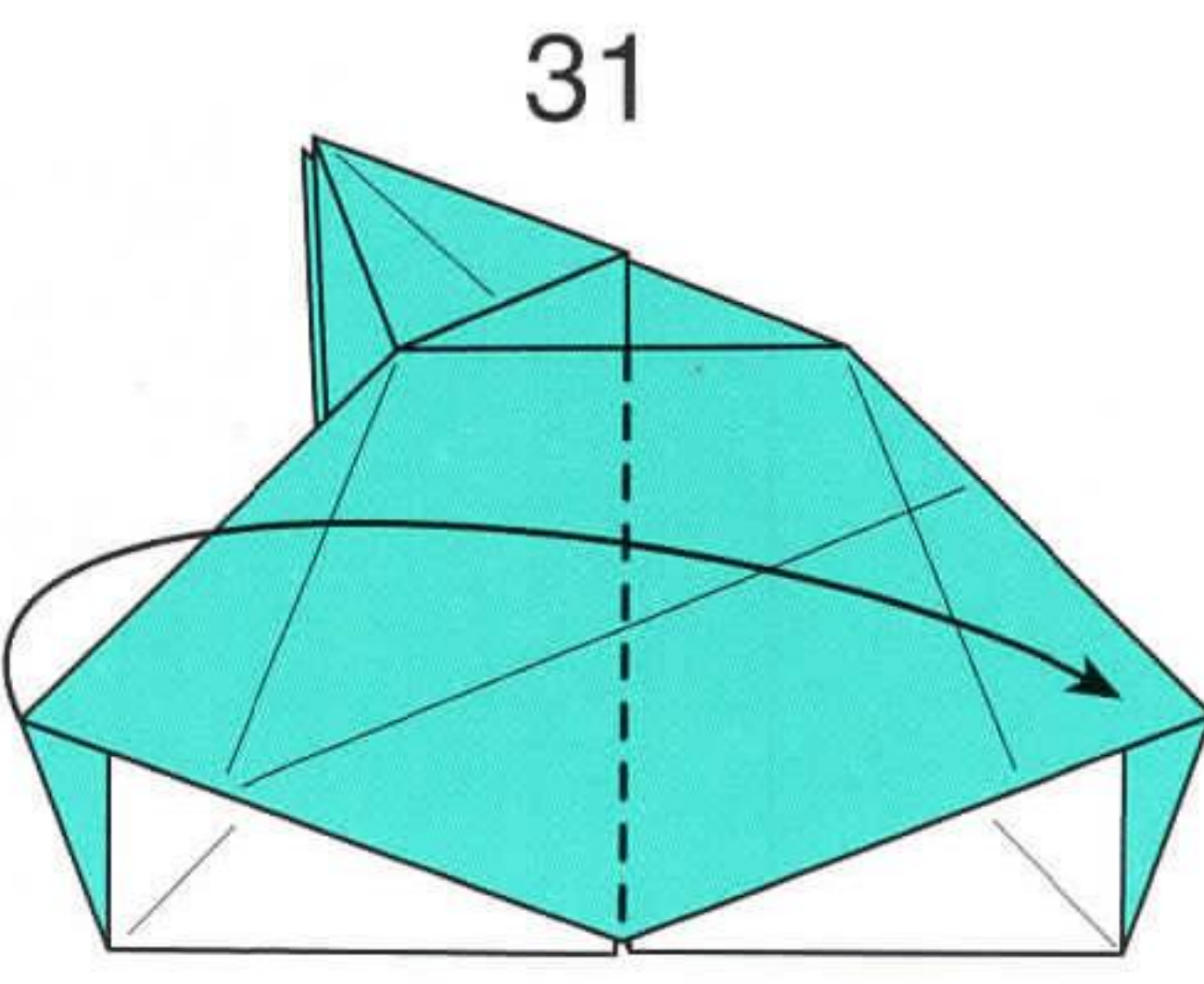
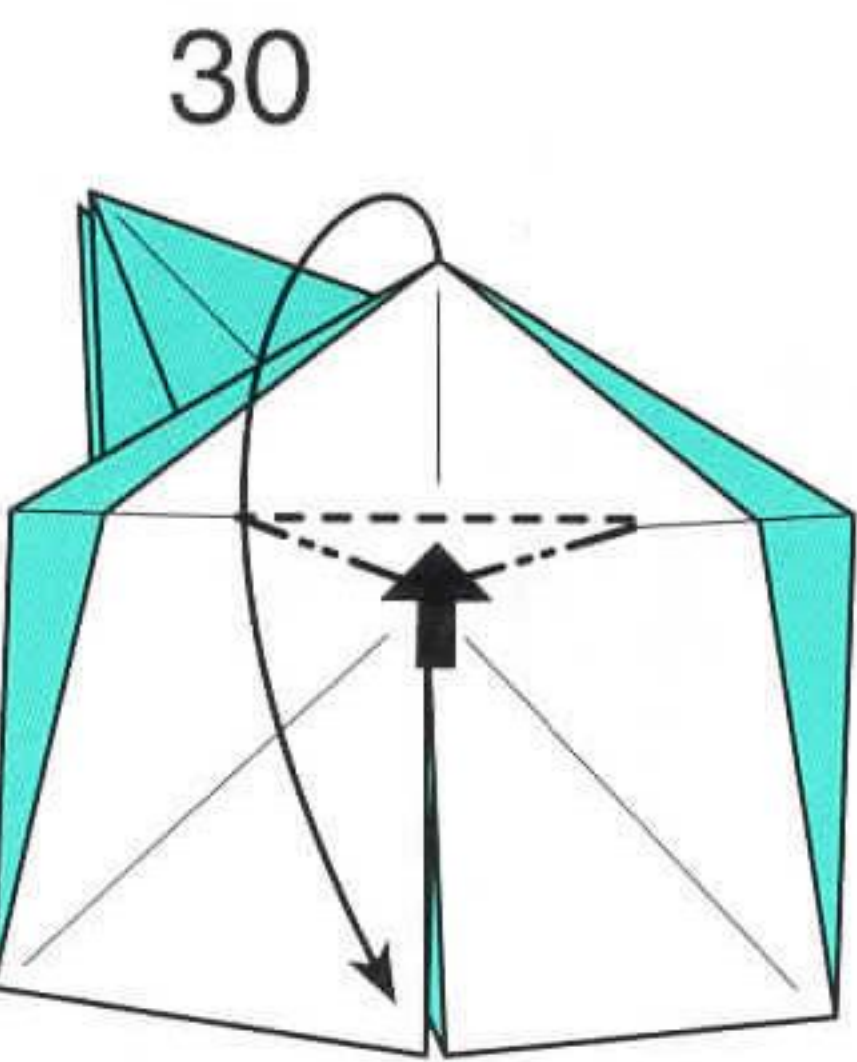
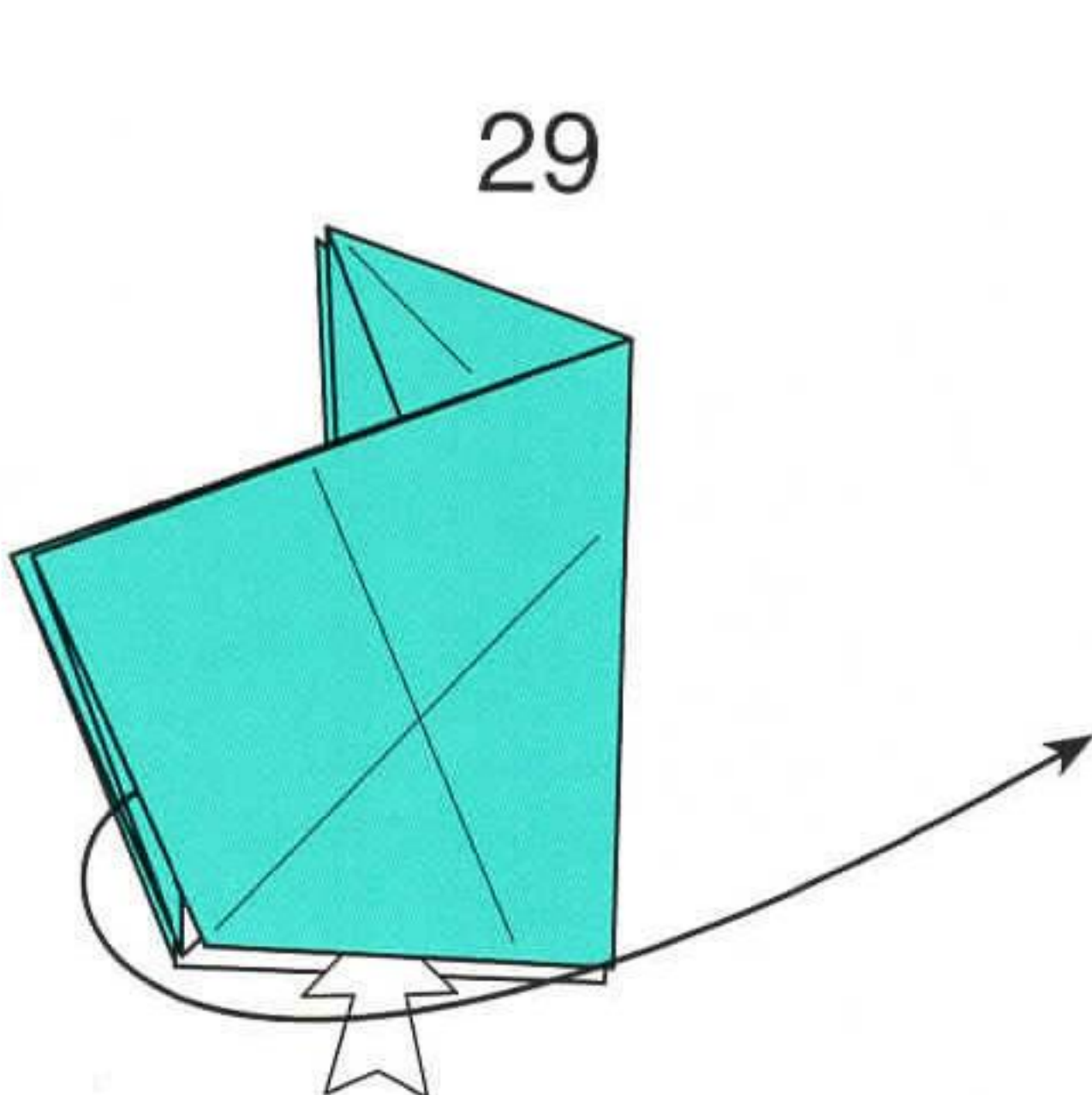
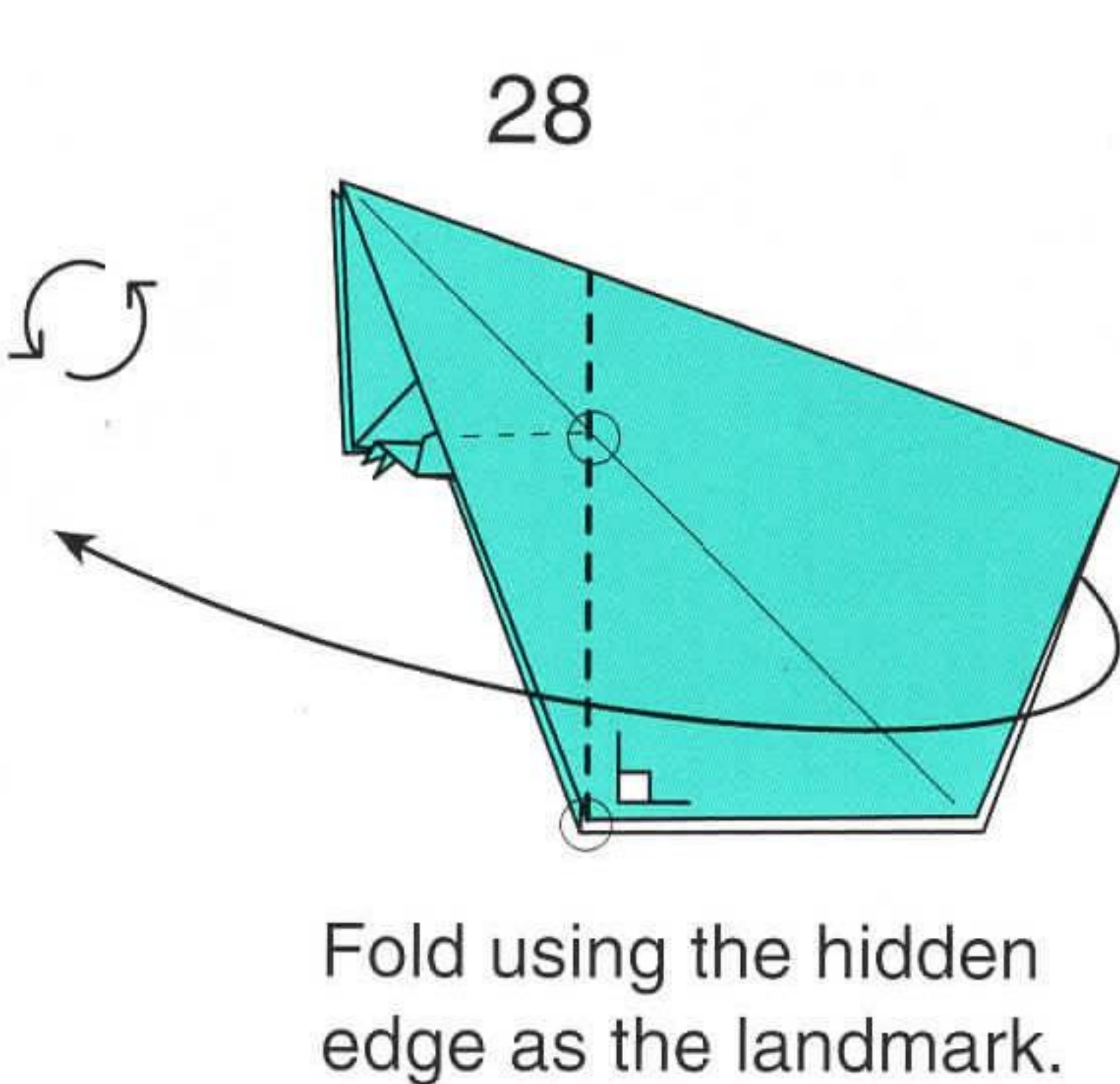
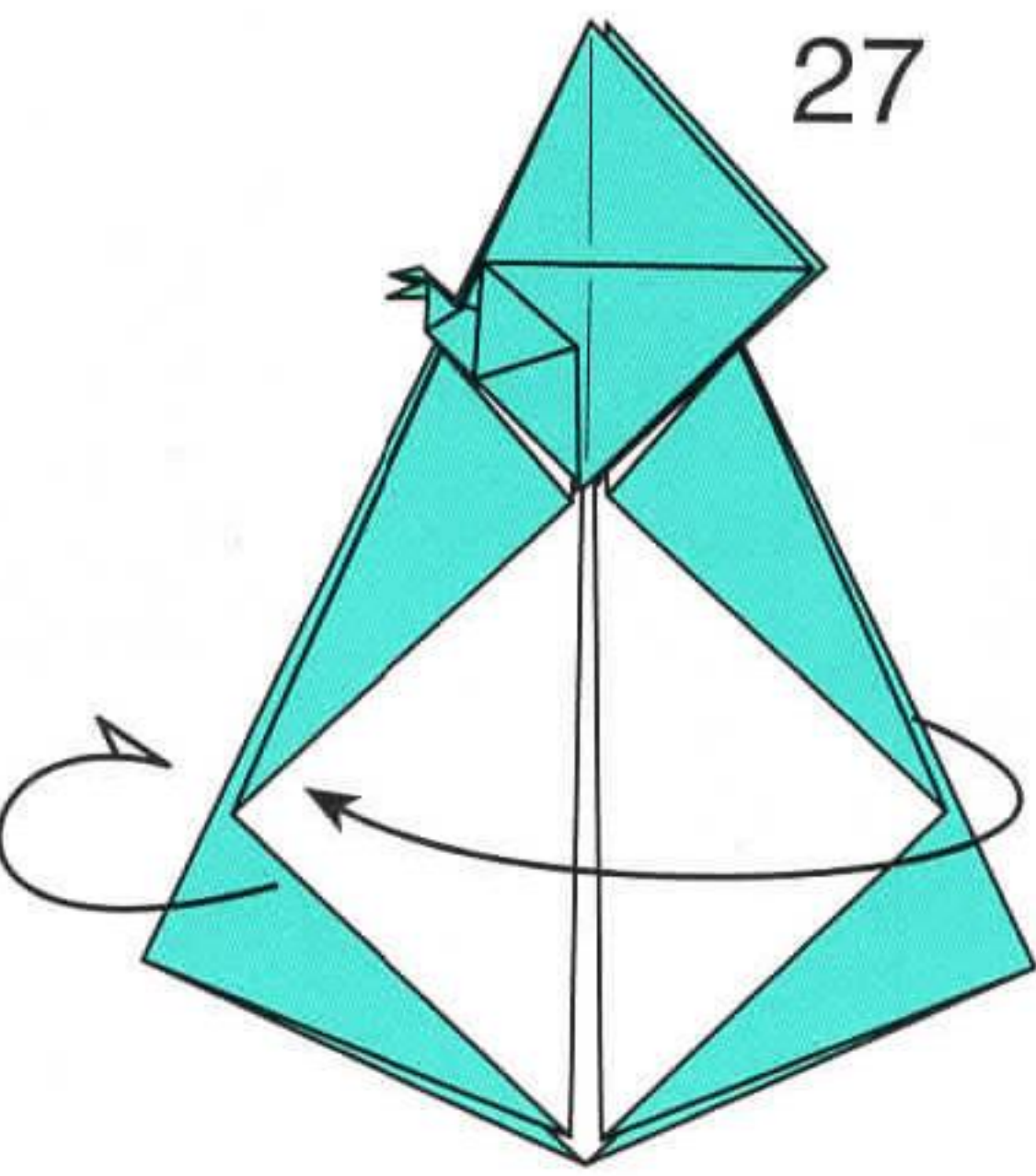
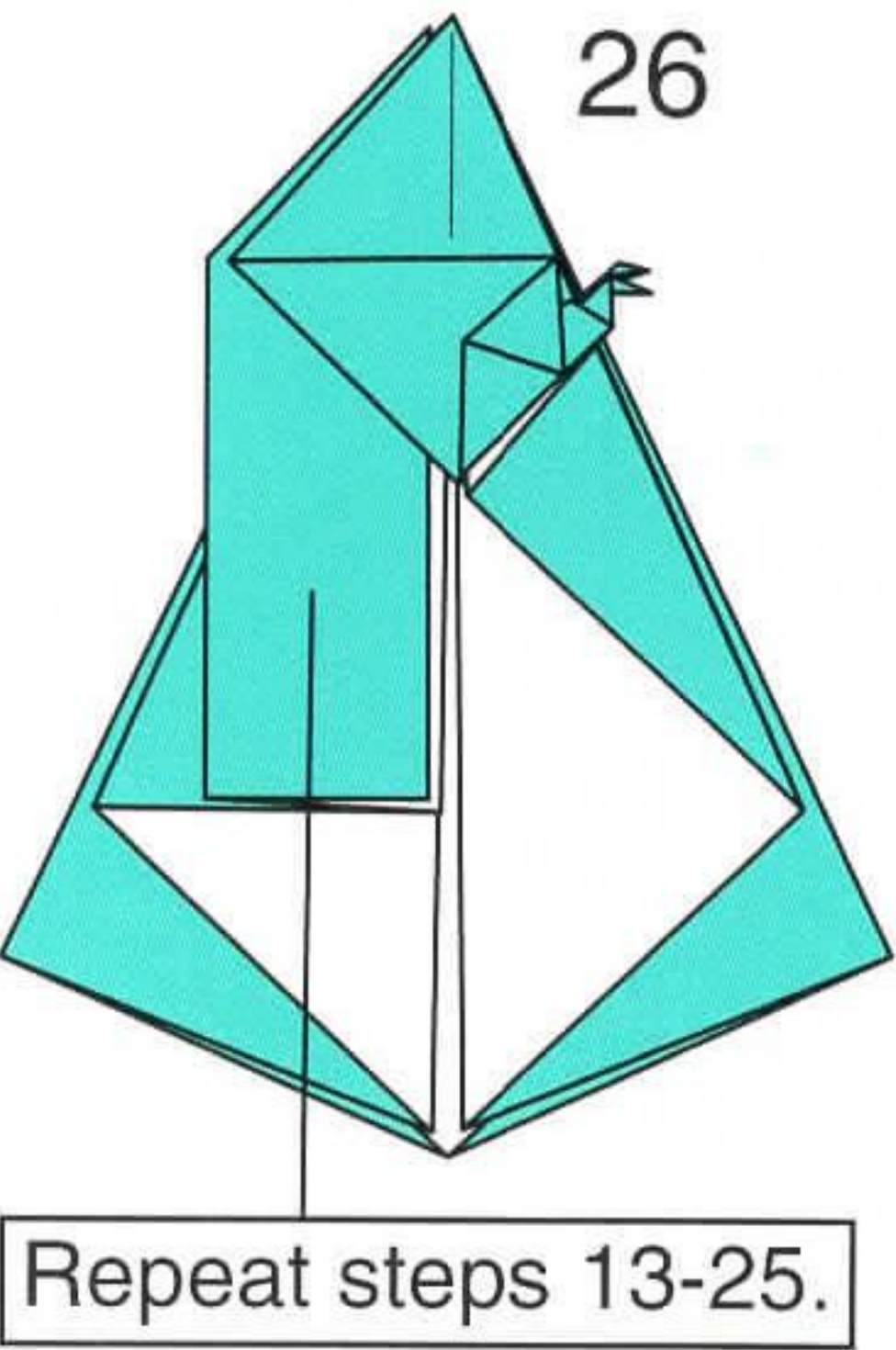


Inside reverse-fold



Inside reverse-fold to make sharp points





41:|

Inside reverse-fold

42

Repeat steps 38-41.

43

Swivel-fold

44

Swivel-fold

45

Reverse the valley crease into mountain.

46

Tuck into the bottom pocket.

47

Repeat steps 43-46.

48

49

50

51

52

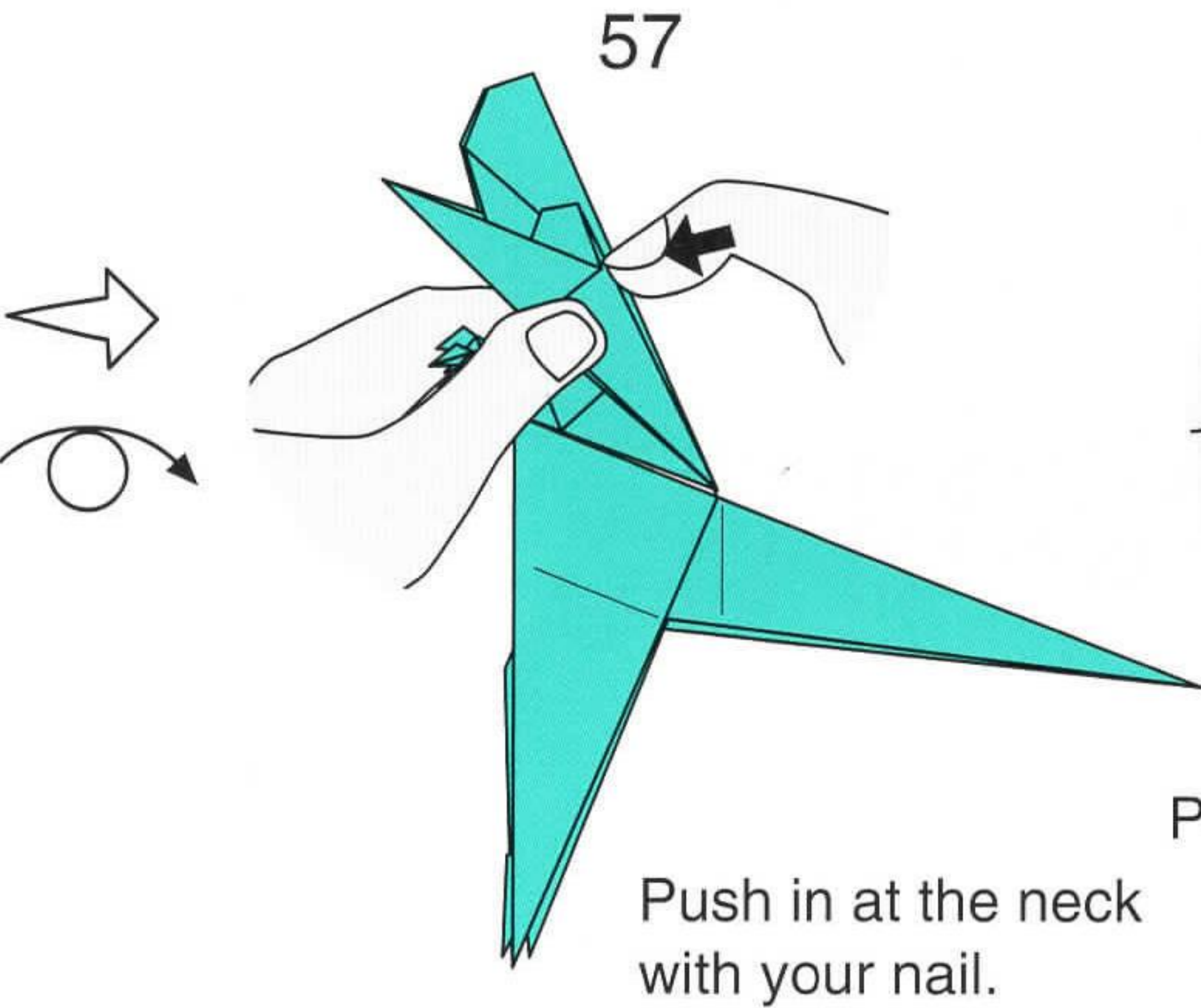
Release the interlocked layers.

53

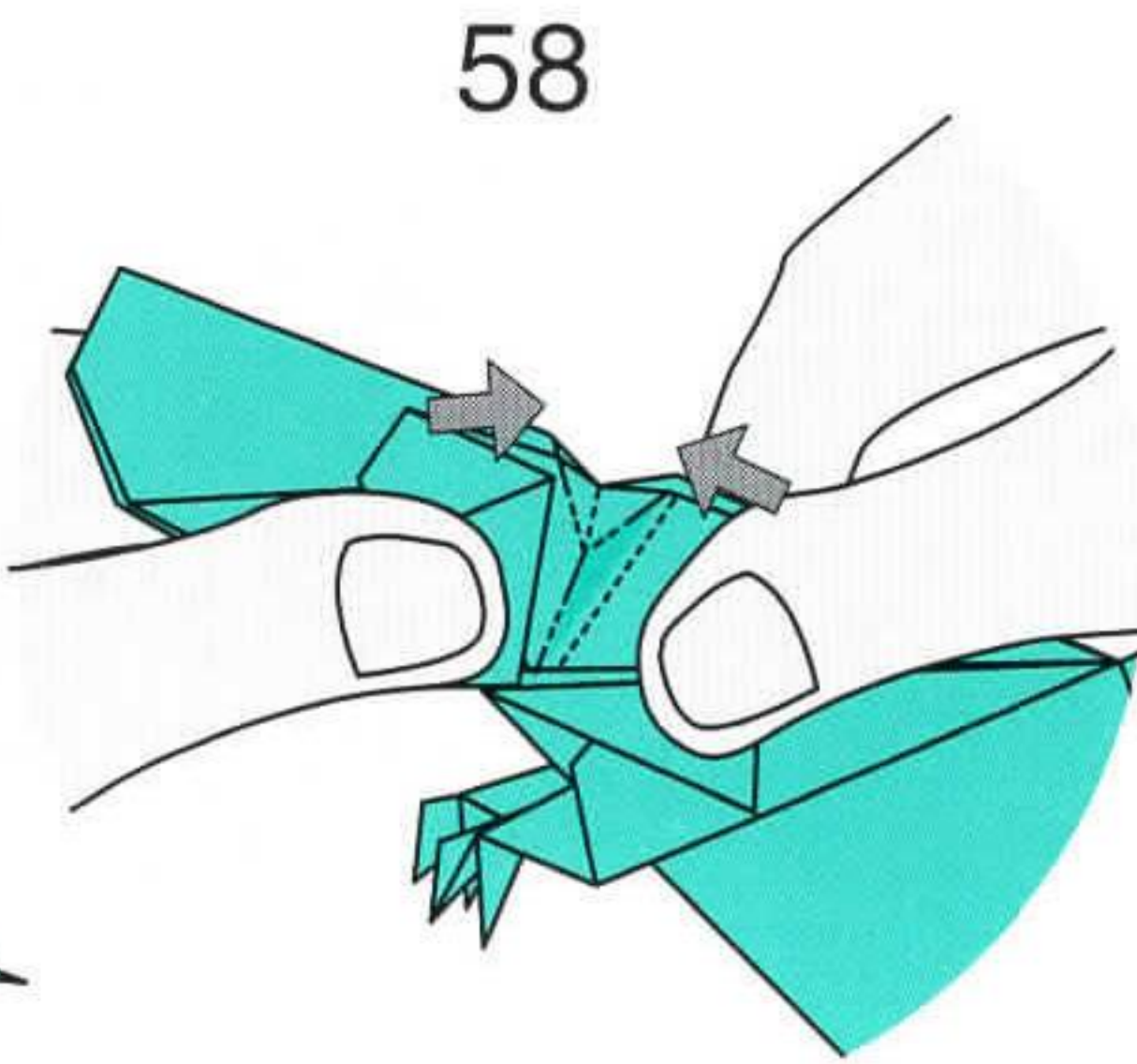
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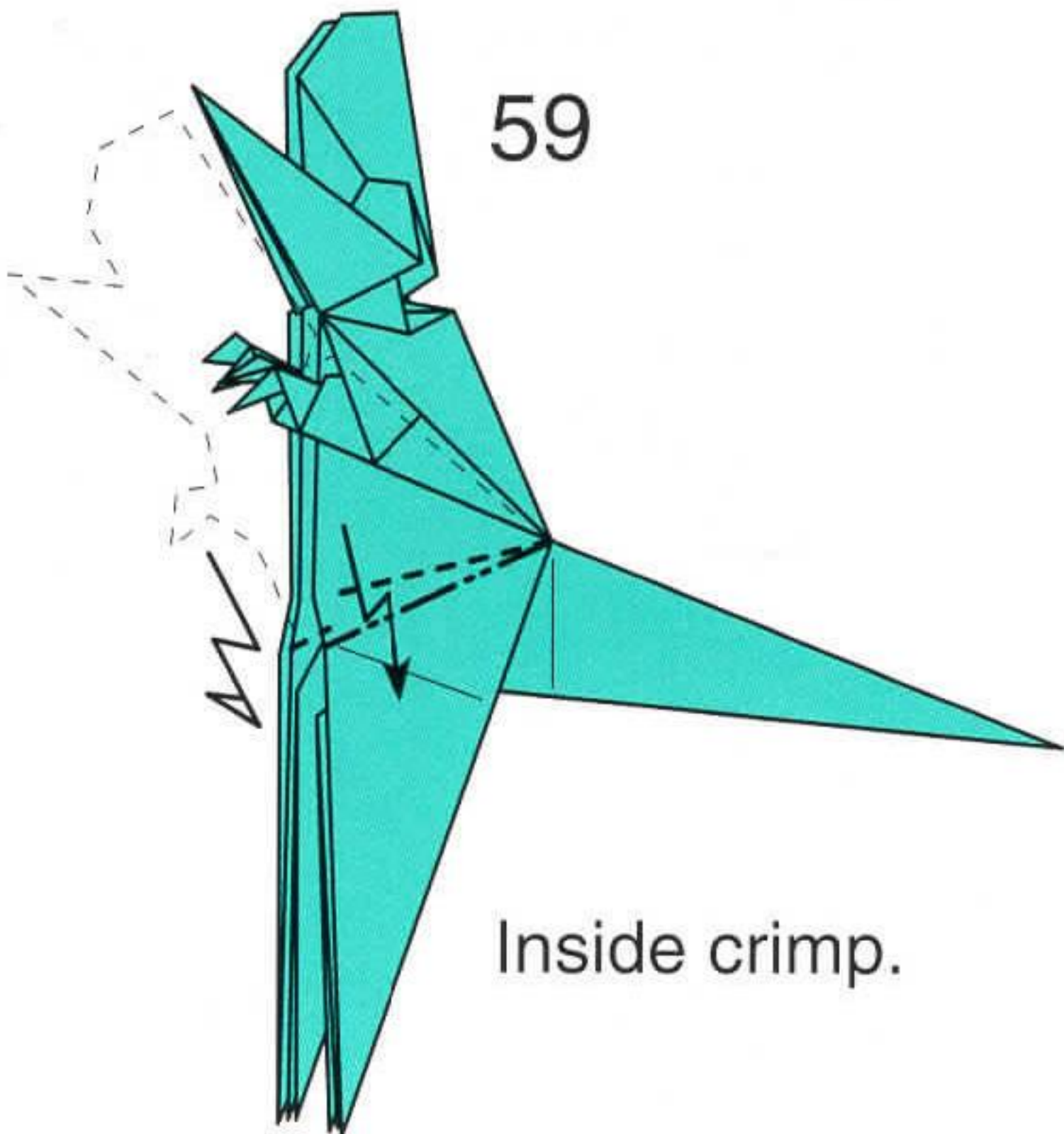
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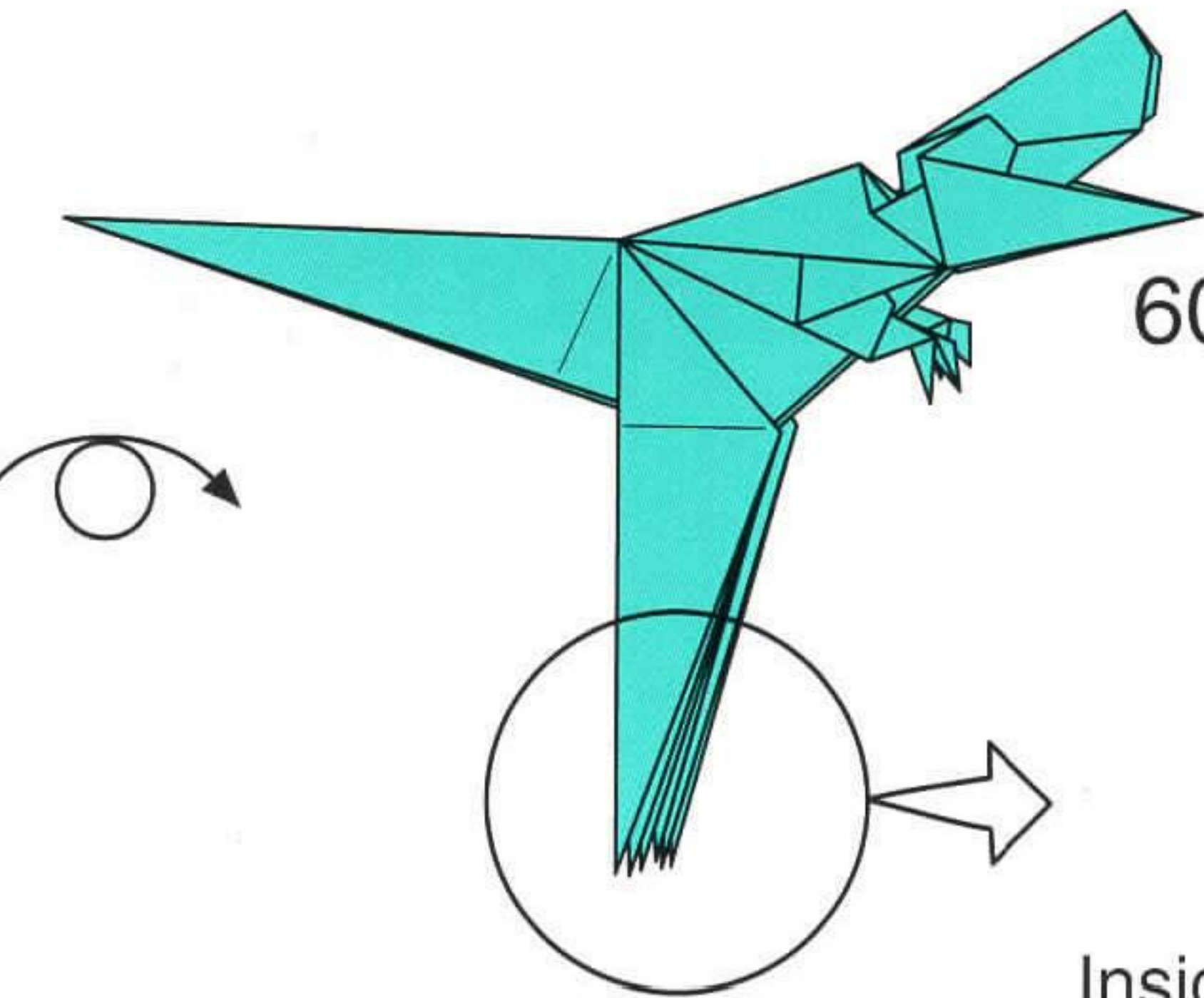
Push in at the neck with your nail.



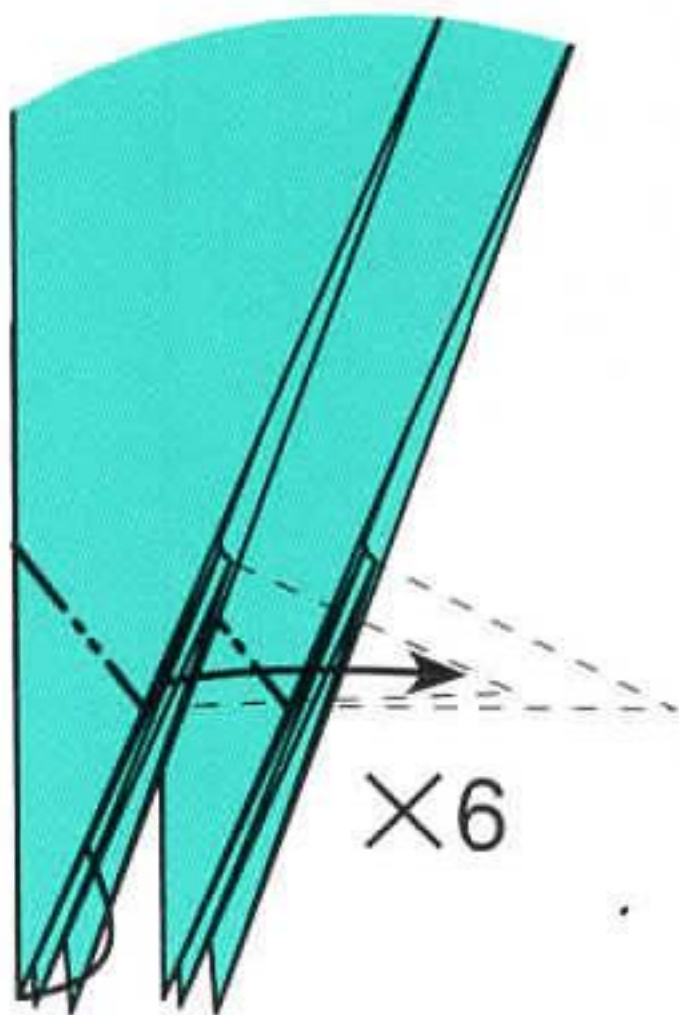
Push to crimp on both sides.



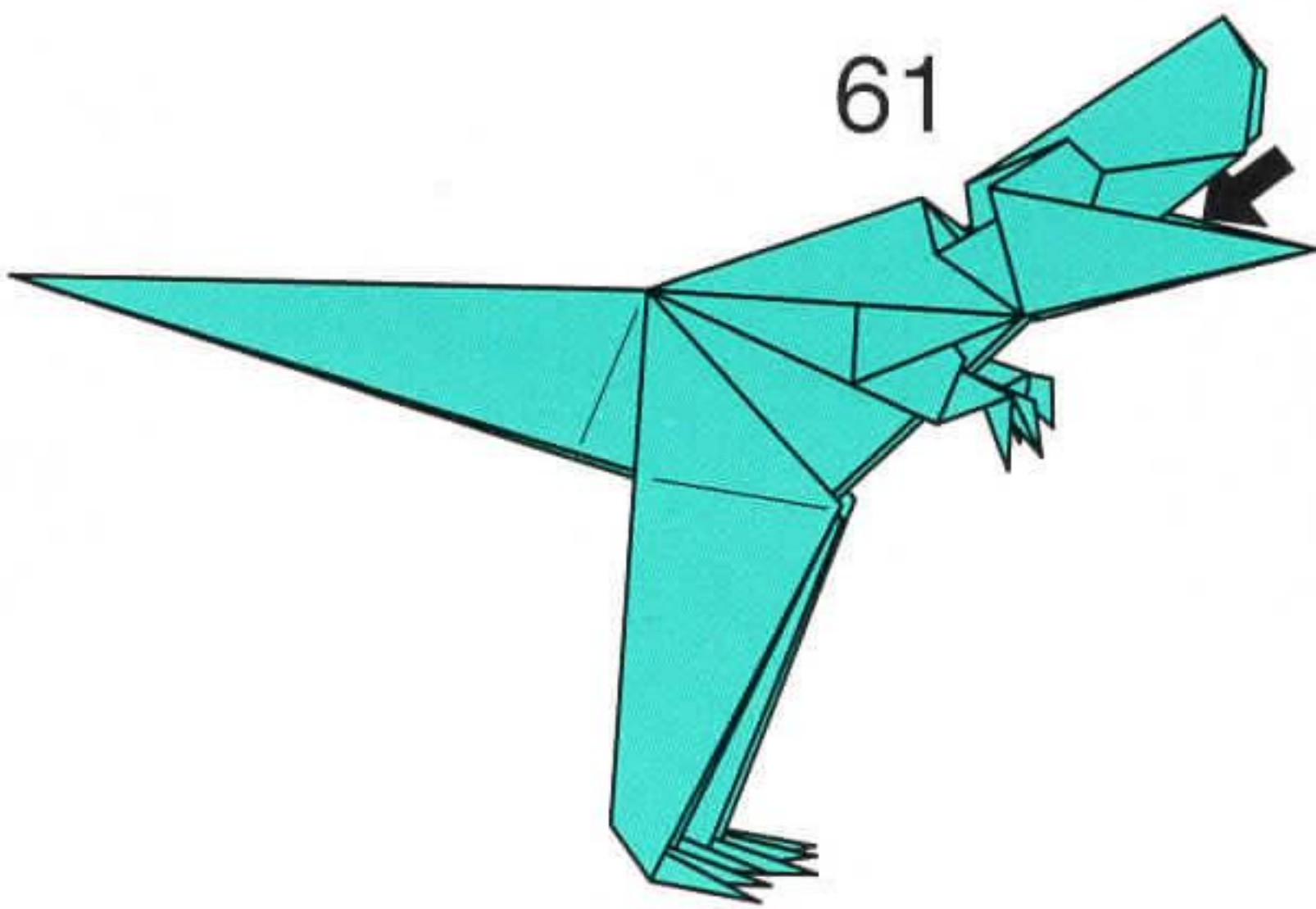
Inside crimp.



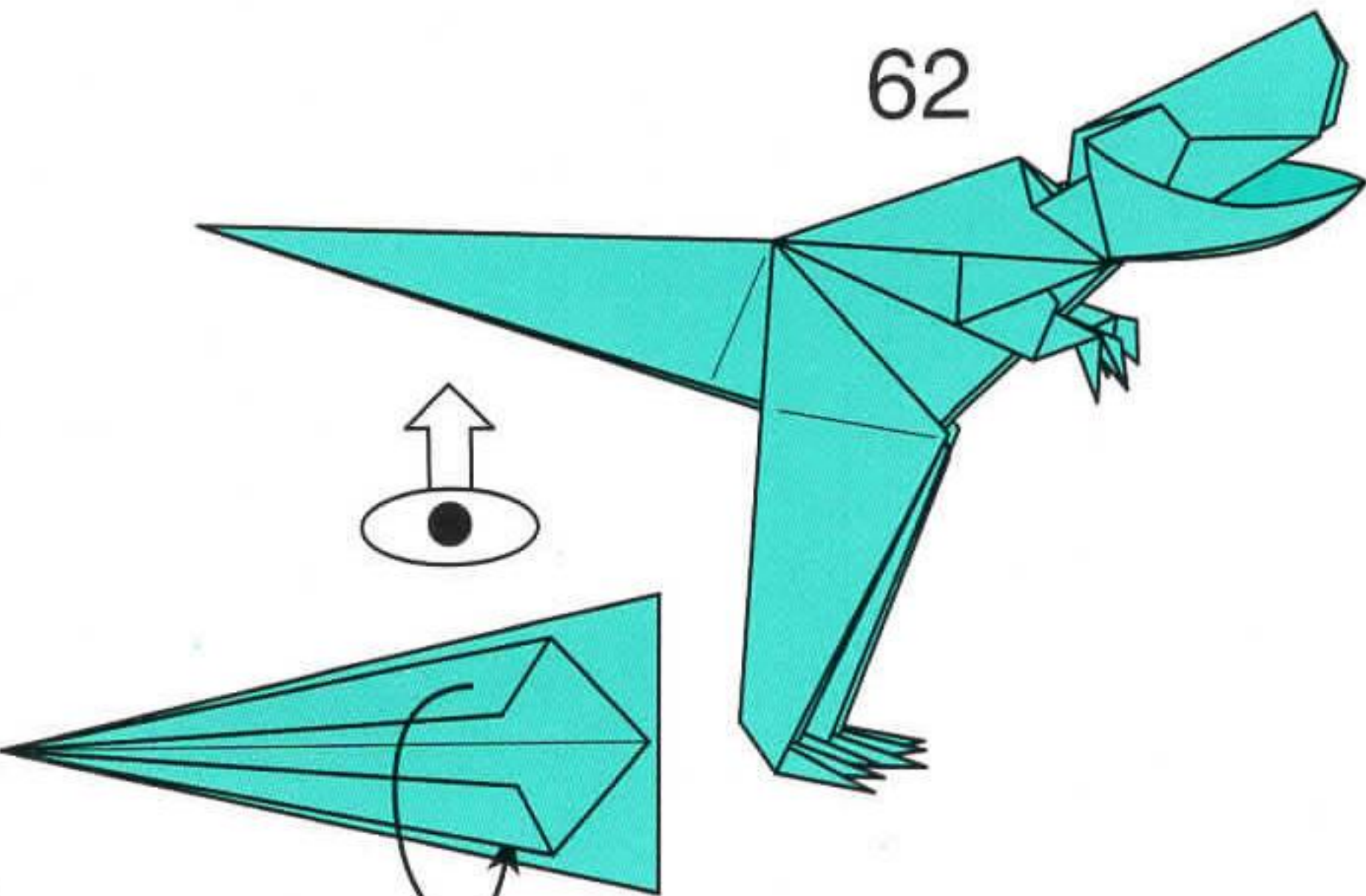
Inside reverse-fold six times



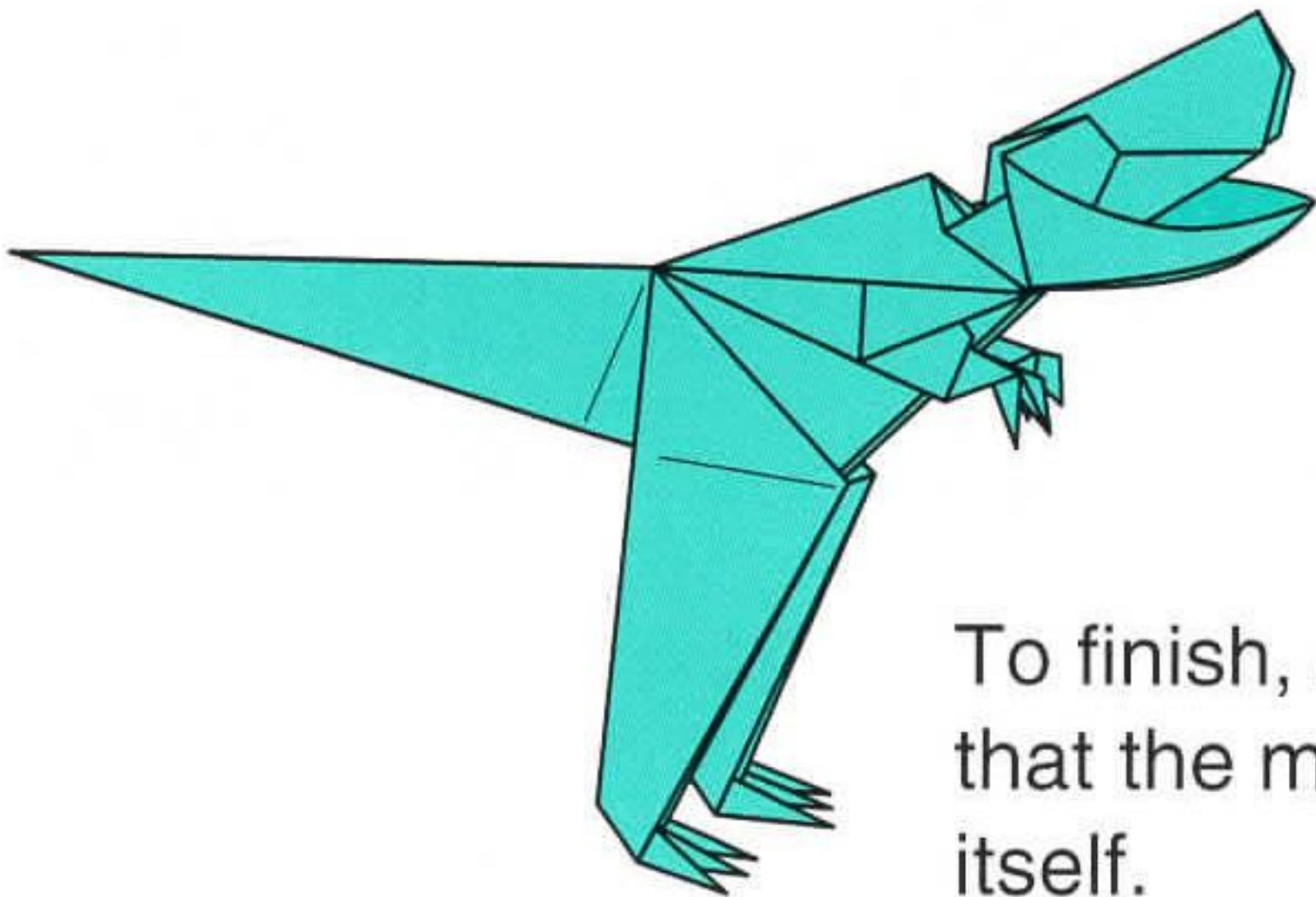
X6



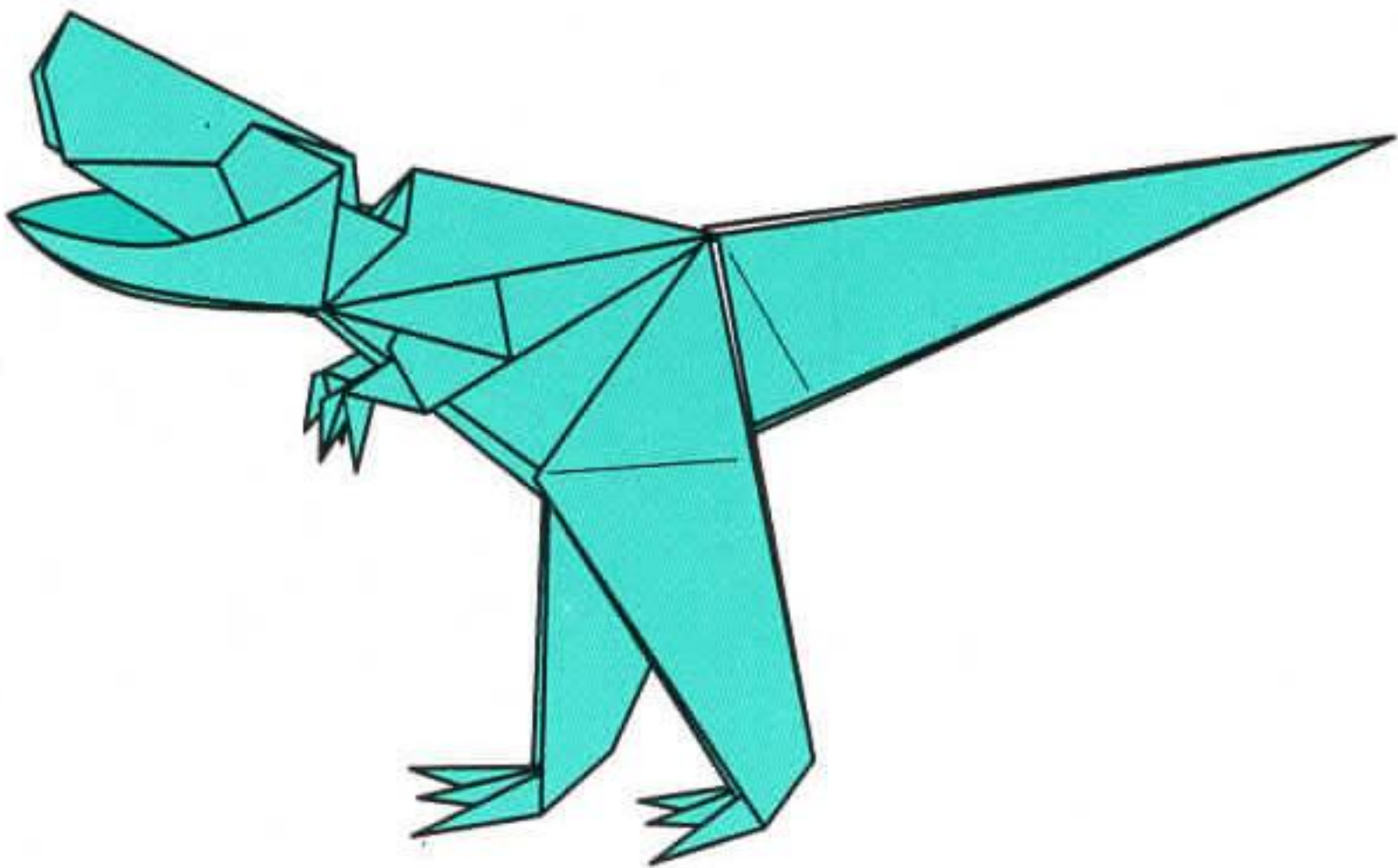
Push in to make the lower jaw 3D.



Lock-fold



To finish, adjust the toes so that the model stands by itself.



If you shape the legs, the model becomes alive but difficult to stand by itself.

You can add some more shaping, such as pinching the legs, to make the model three-dimensional. But I prefer stopping here.

It is very difficult to decide where to stop folding. That may be an eternal problem in origami design.

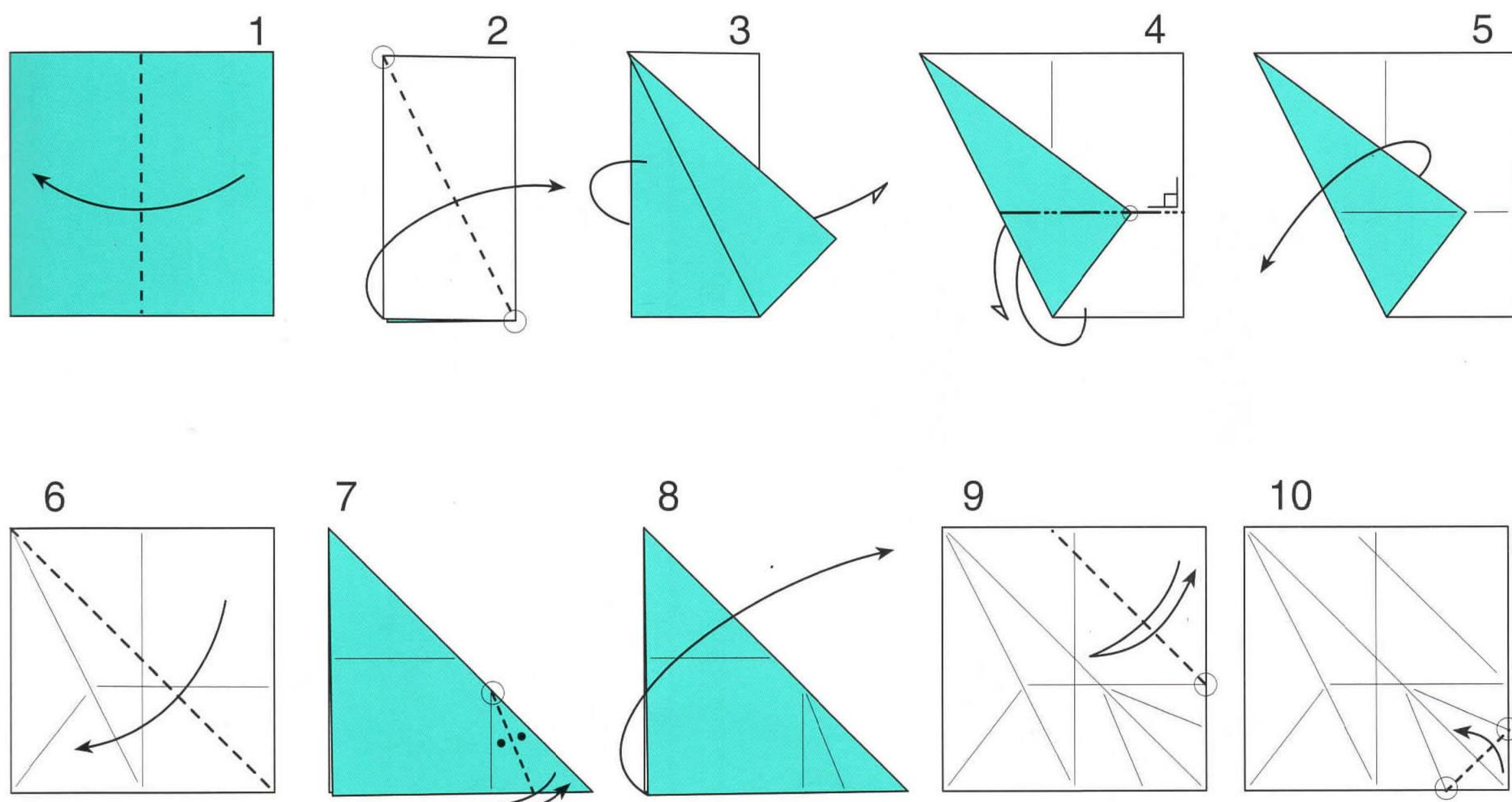
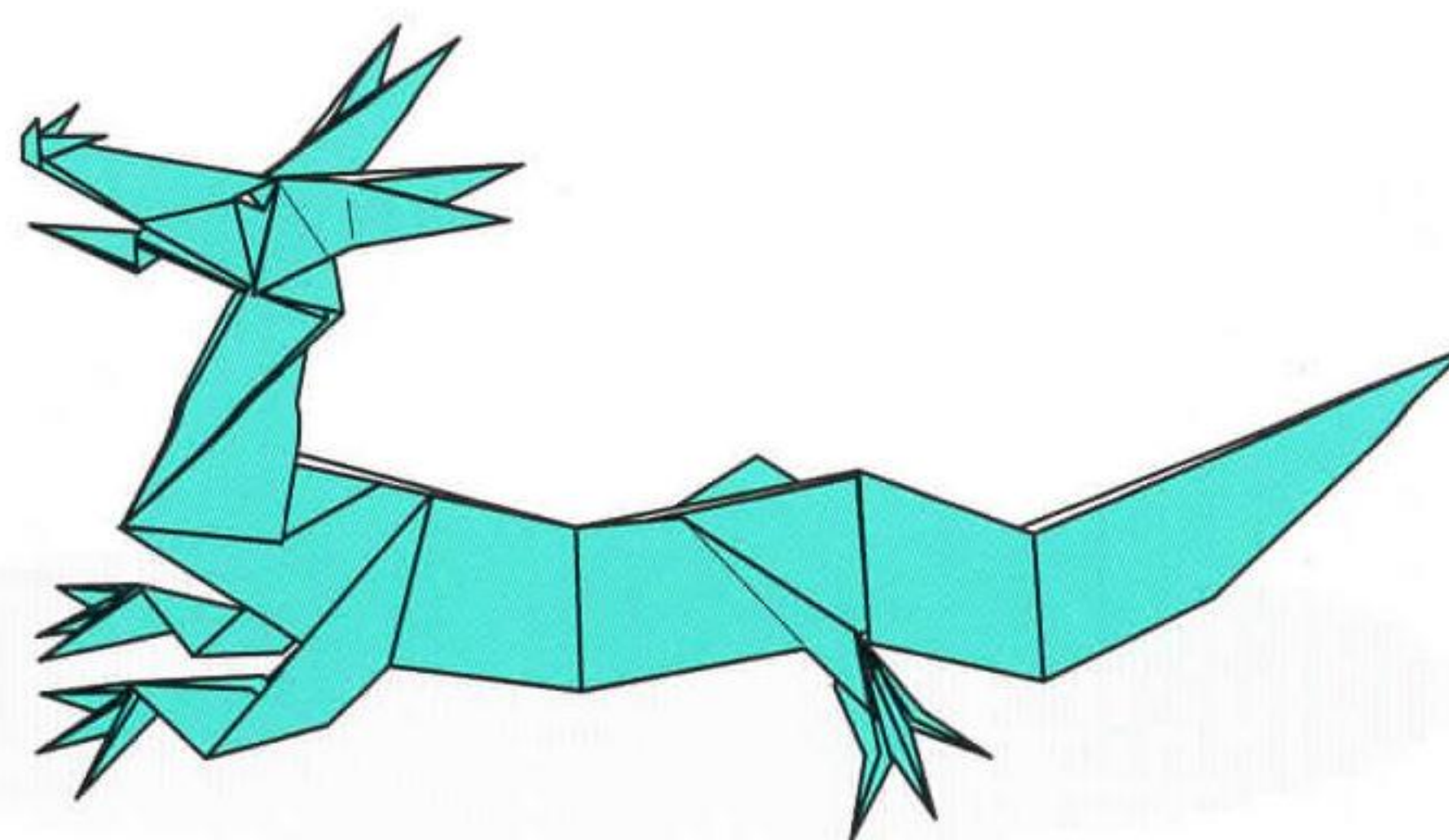
Anyway, I think it is more important to make the model stand by itself than to shape it well.

Eastern Dragon

Theme: Grafting

Not impossible to fold using 6" (15 cm)

origami paper. 10" (25 cm) or larger thin washi (Japanese handmade paper) is suggested.



Grafting technique

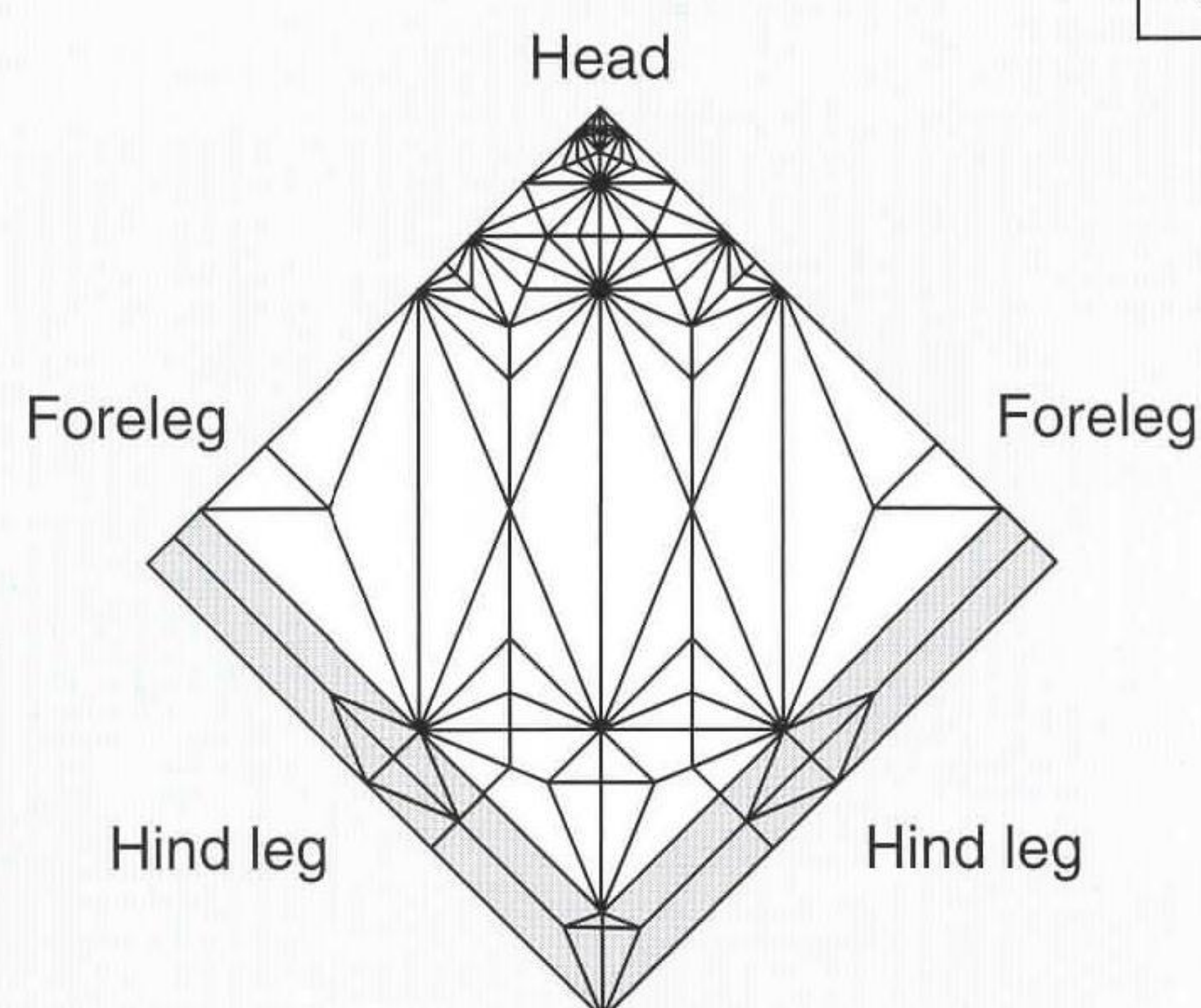
I designed this *Eastern Dragon* by adding craws to my previous design. This technique is a kind of **preparation** explained in *Three-headed Crane*.

The gray area in the crease pattern shown on the right indicates the grafted part. I added a "gusset" while leaving the original crease pattern intact.

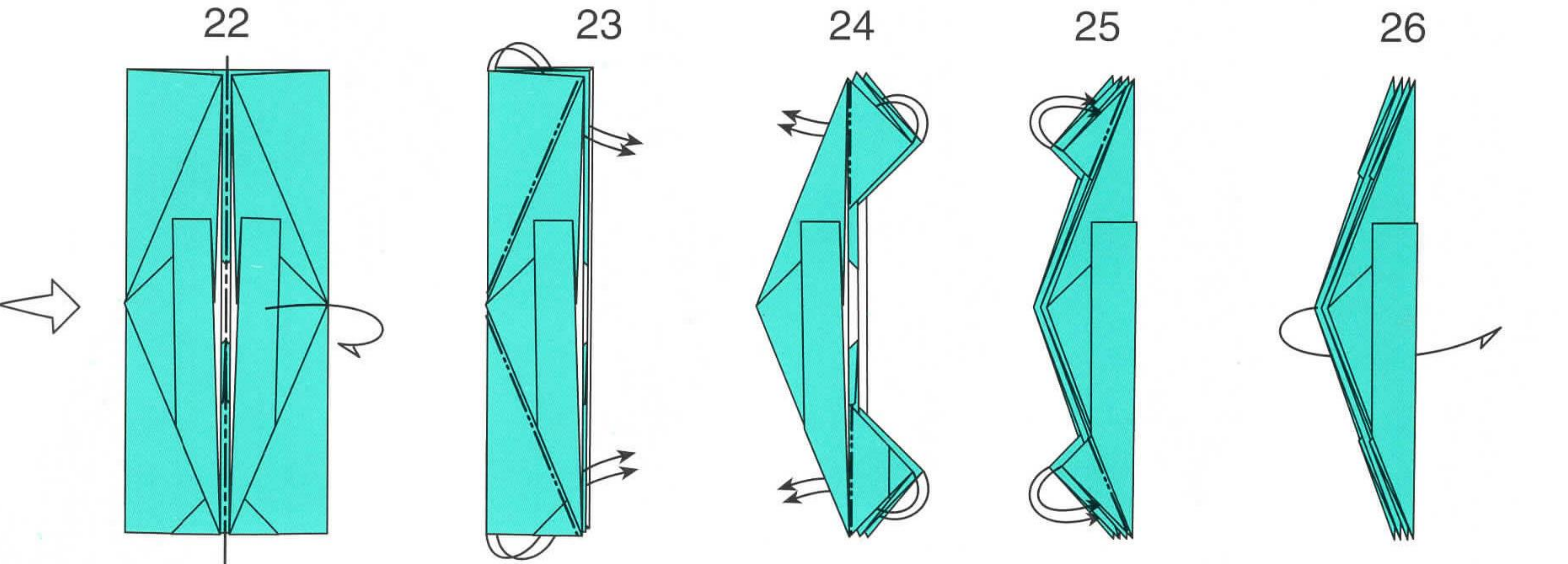
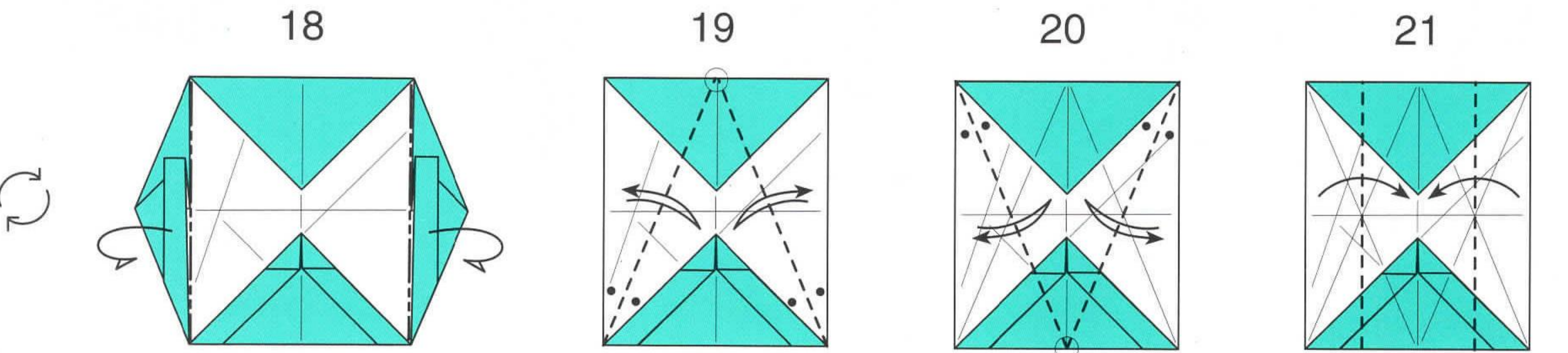
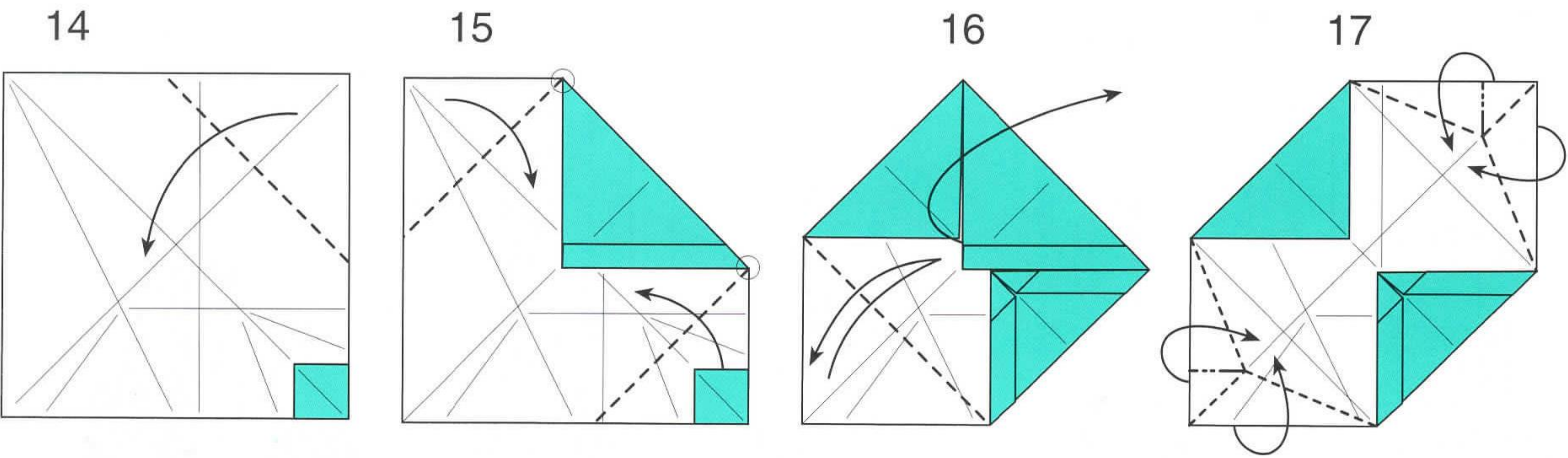
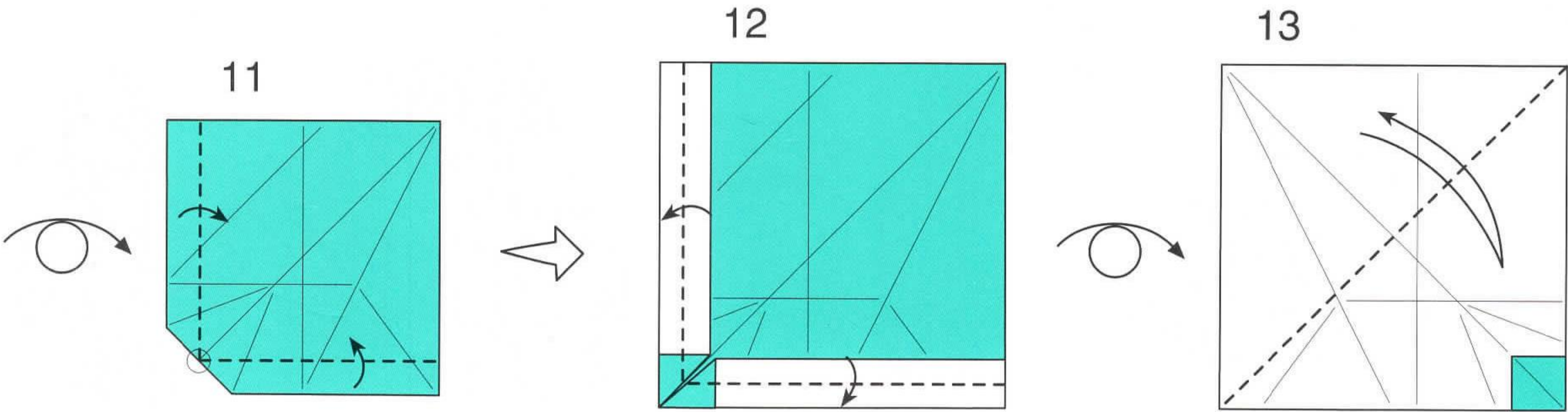
As a side effect of adding the craws, I also obtained a longer body.

Note that an area can be grafted not only along the sides of the square, as in this model, but also in different parts.

You can divide an existing crease pattern and insert a gusset between them. *Devil* is an example, where fingers are grafted into the original model.



The crease pattern of *Eastern Dragon* (mountain and valley folds are not shown).



Inside reverse-fold Inside reverse-fold Inside reverse-fold

There are more layers on the upper half.

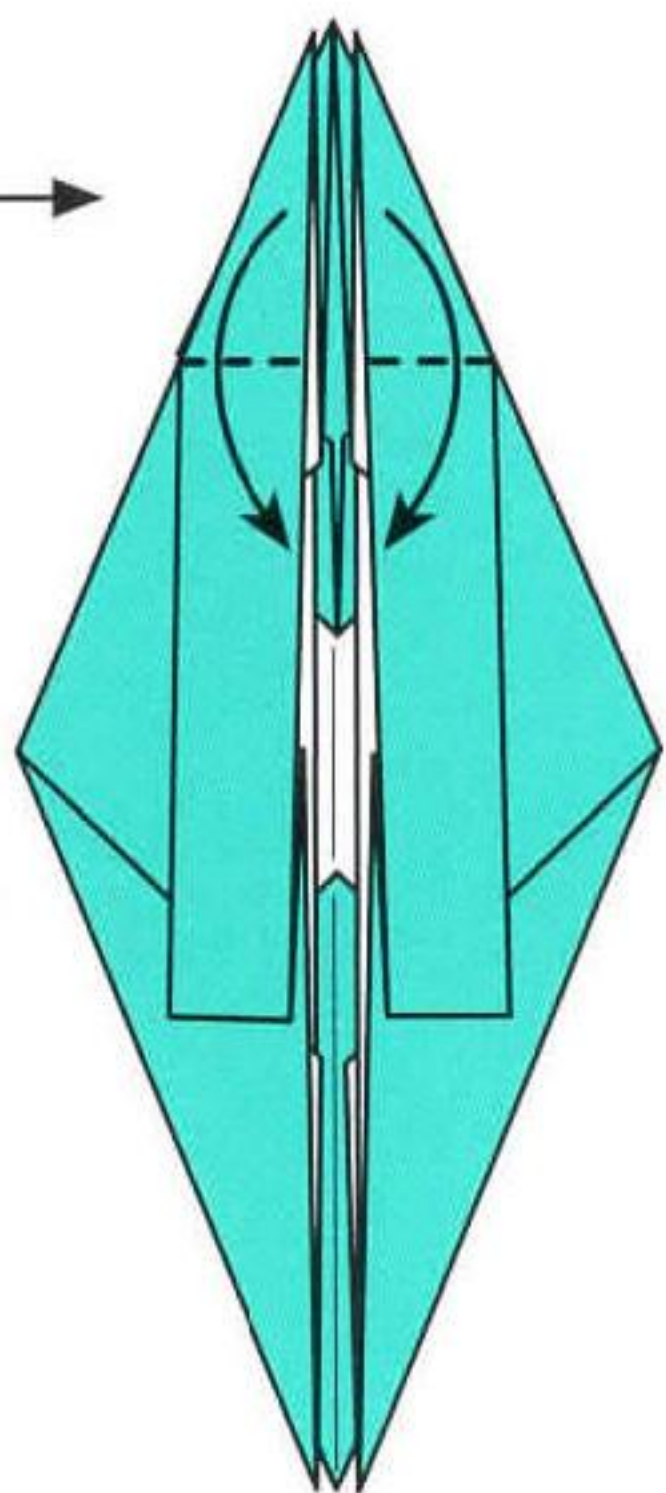


Diagram 28: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.

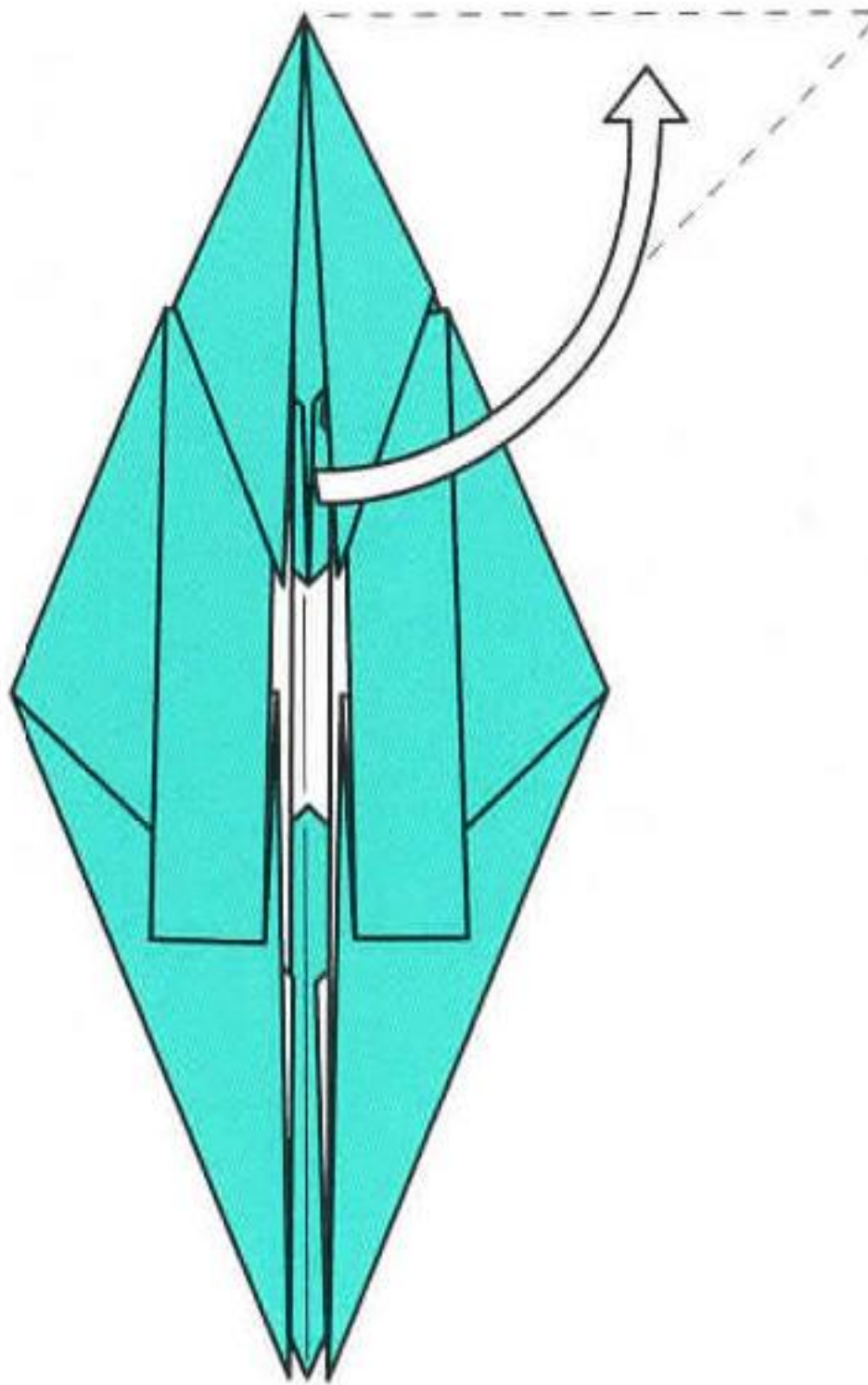


Diagram 29: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.

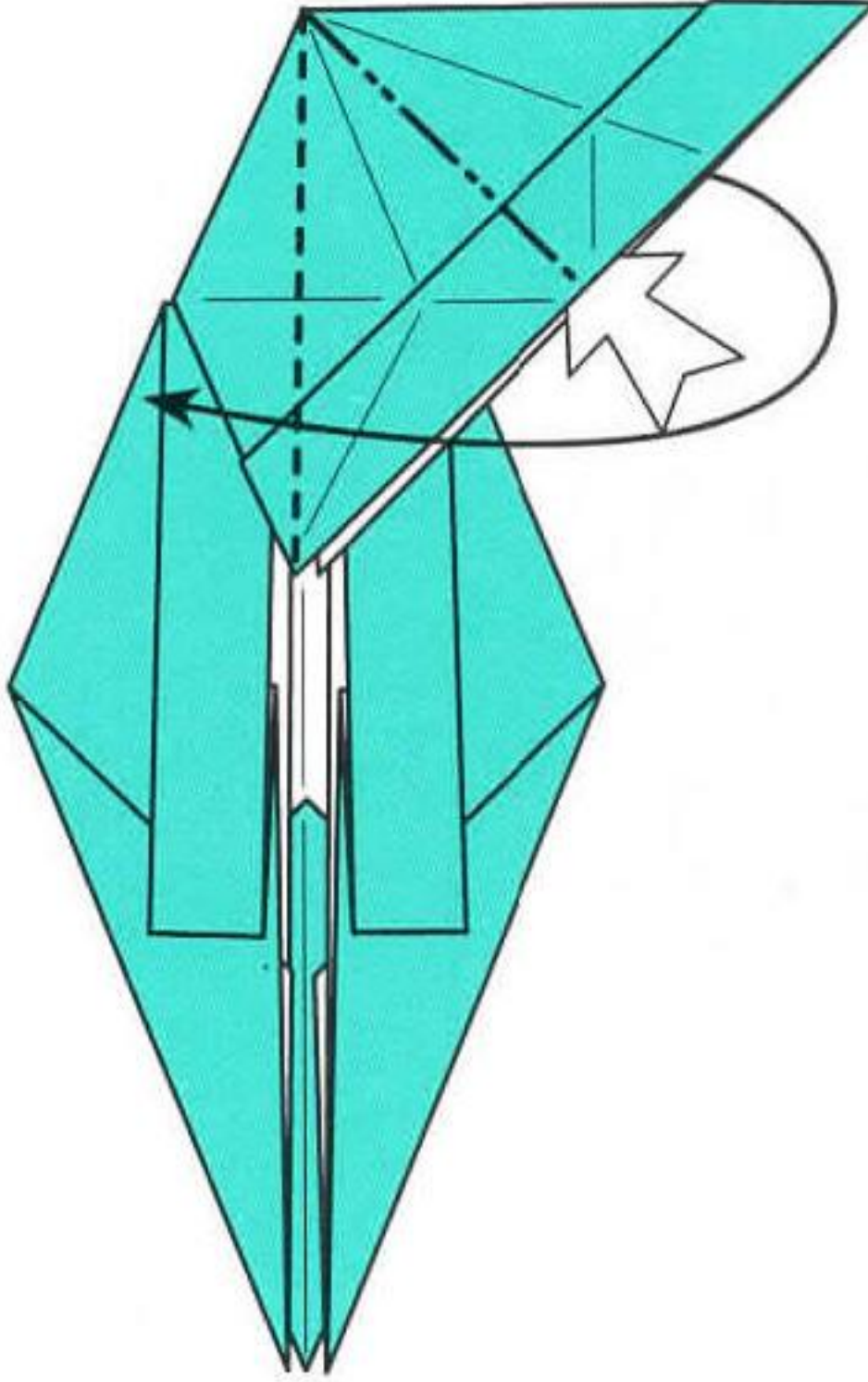
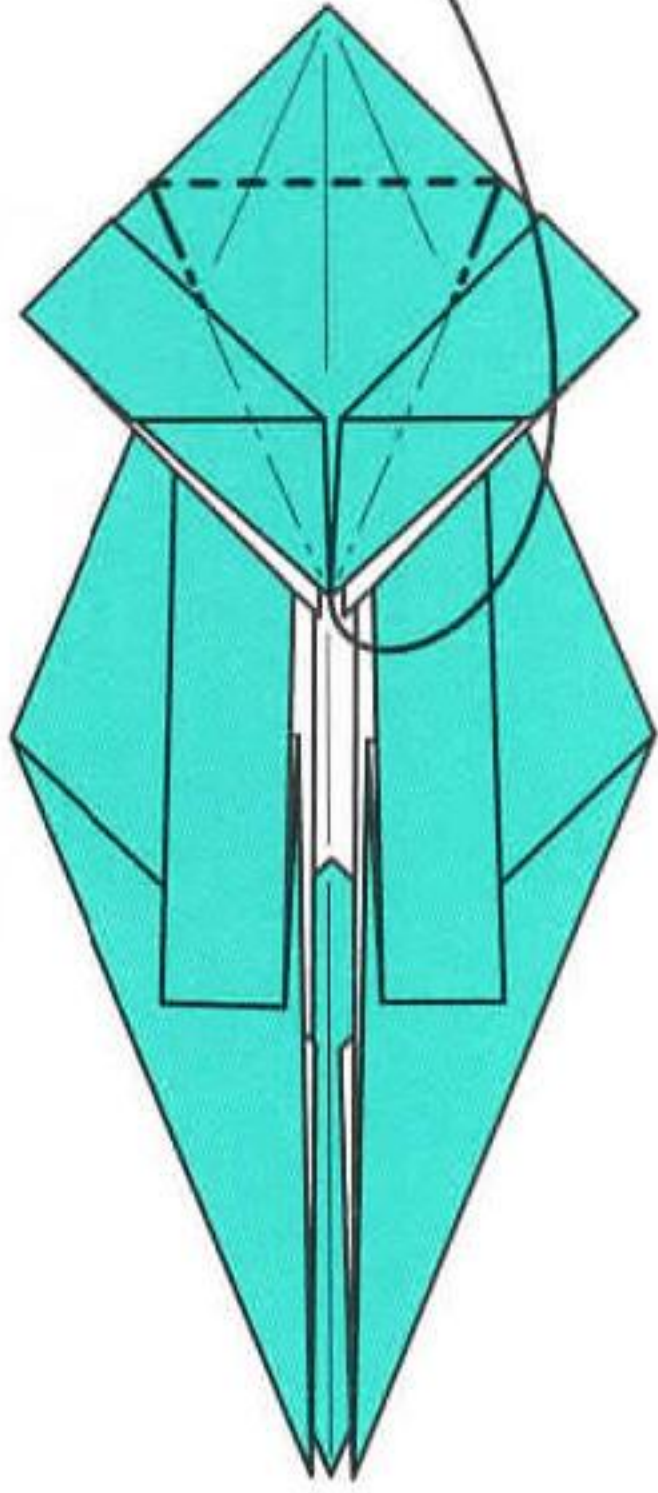


Diagram 30: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.



Petal-fold

Diagram 31: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.

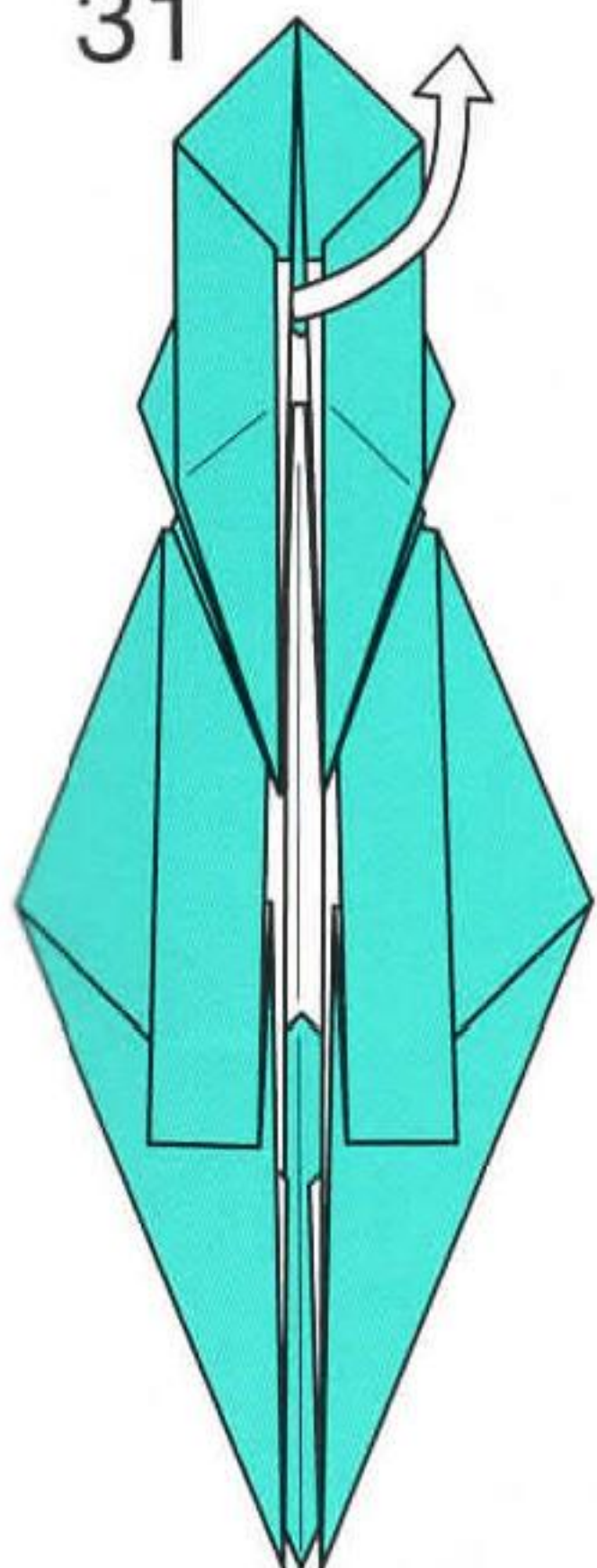


Diagram 32: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.

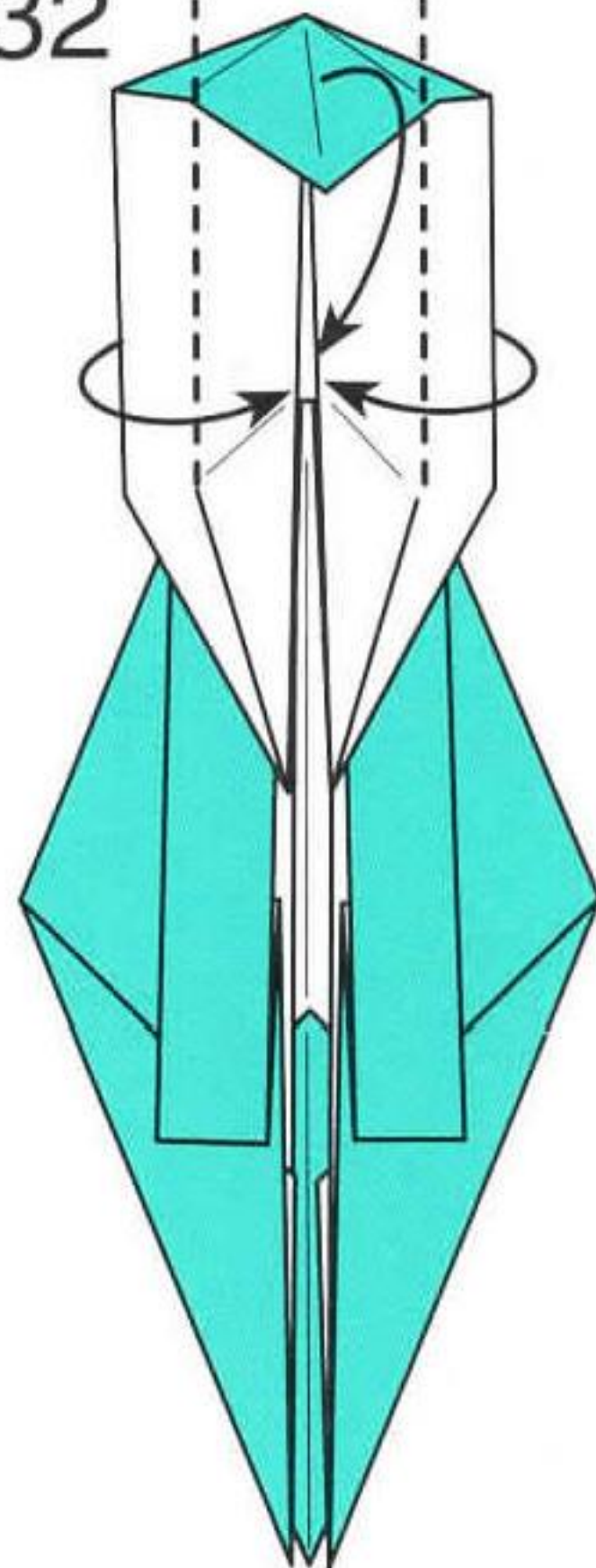
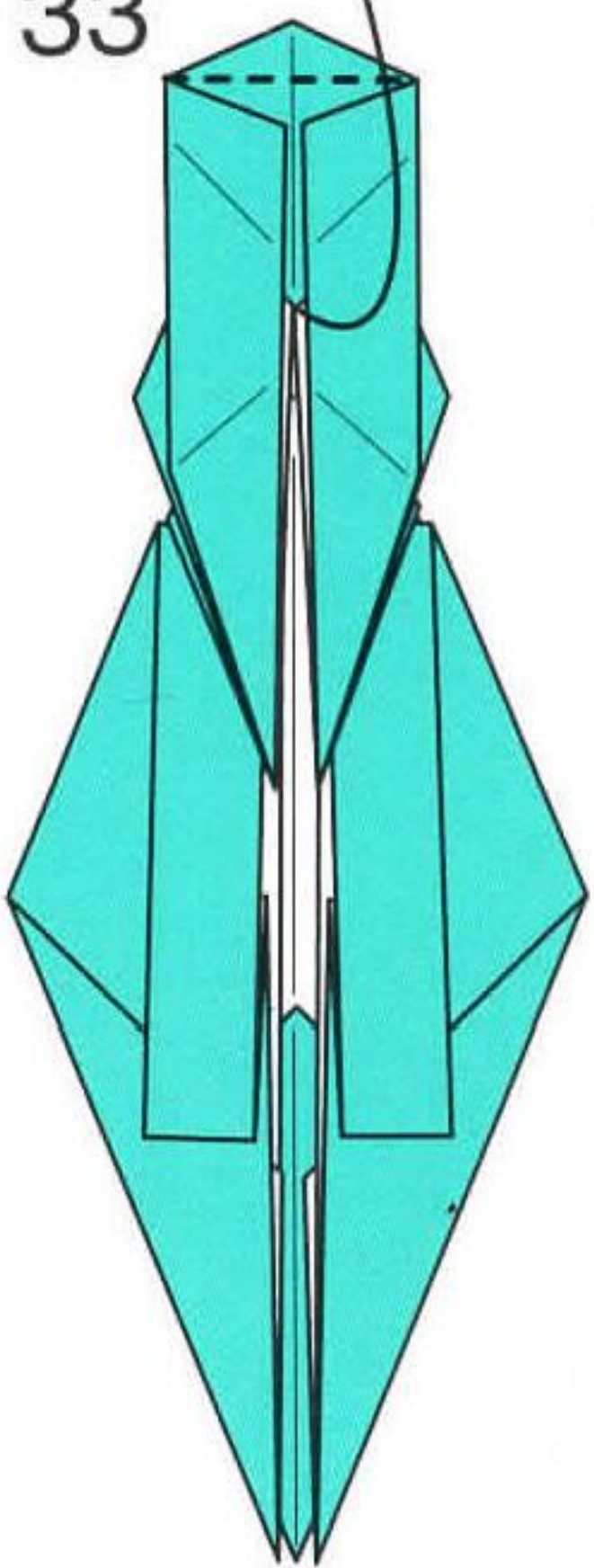


Diagram 33: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.



Petal-fold

Diagram 34: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.

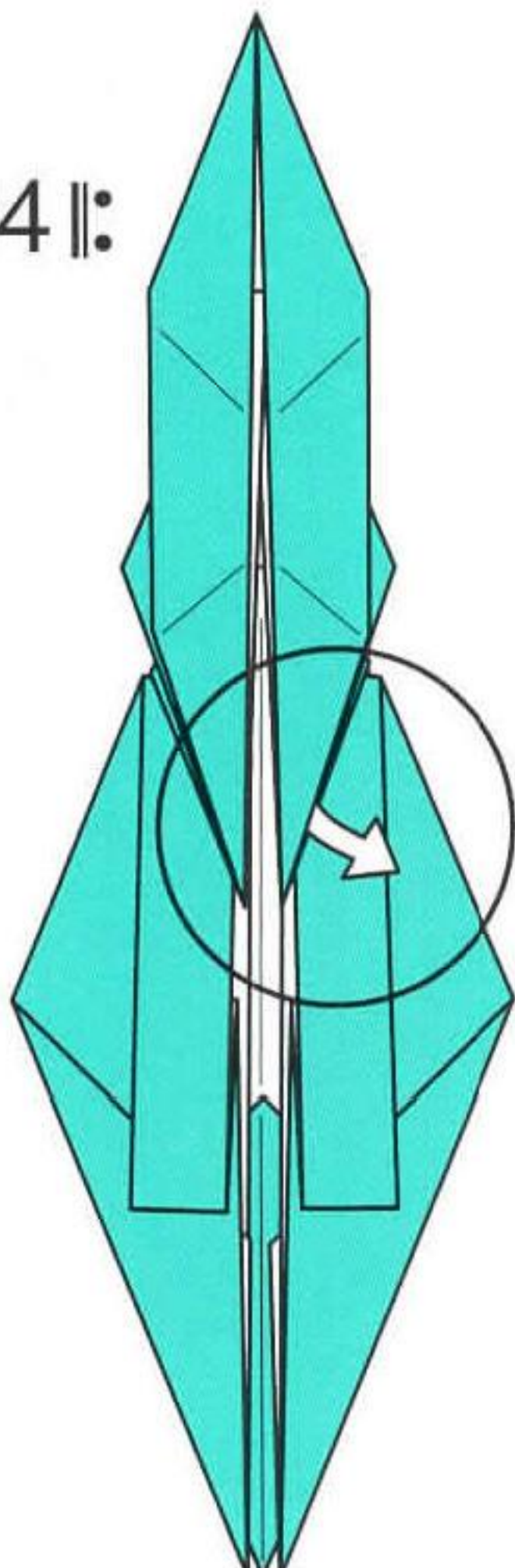


Diagram 35: A circular inset showing a close-up of the fold in diagram 34.

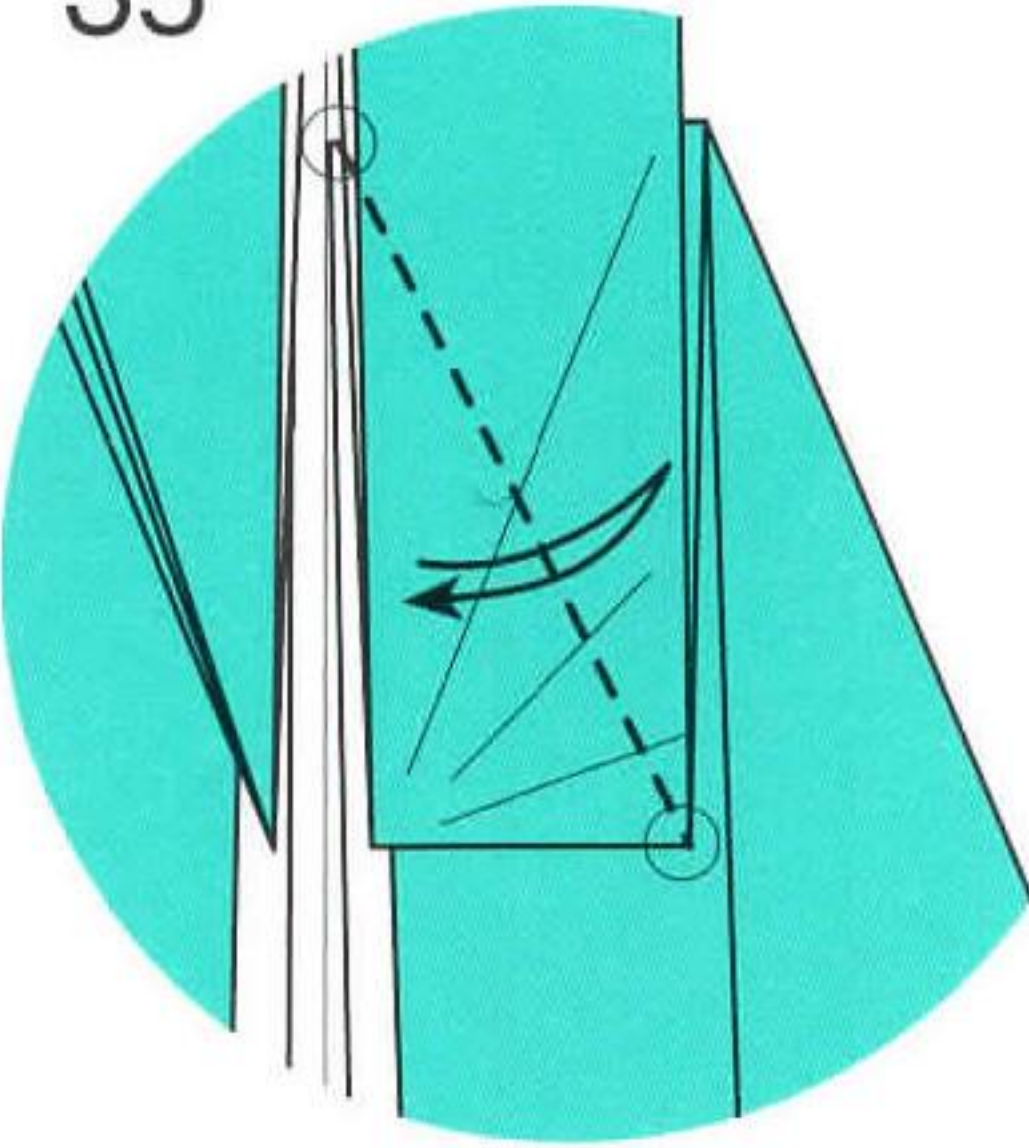
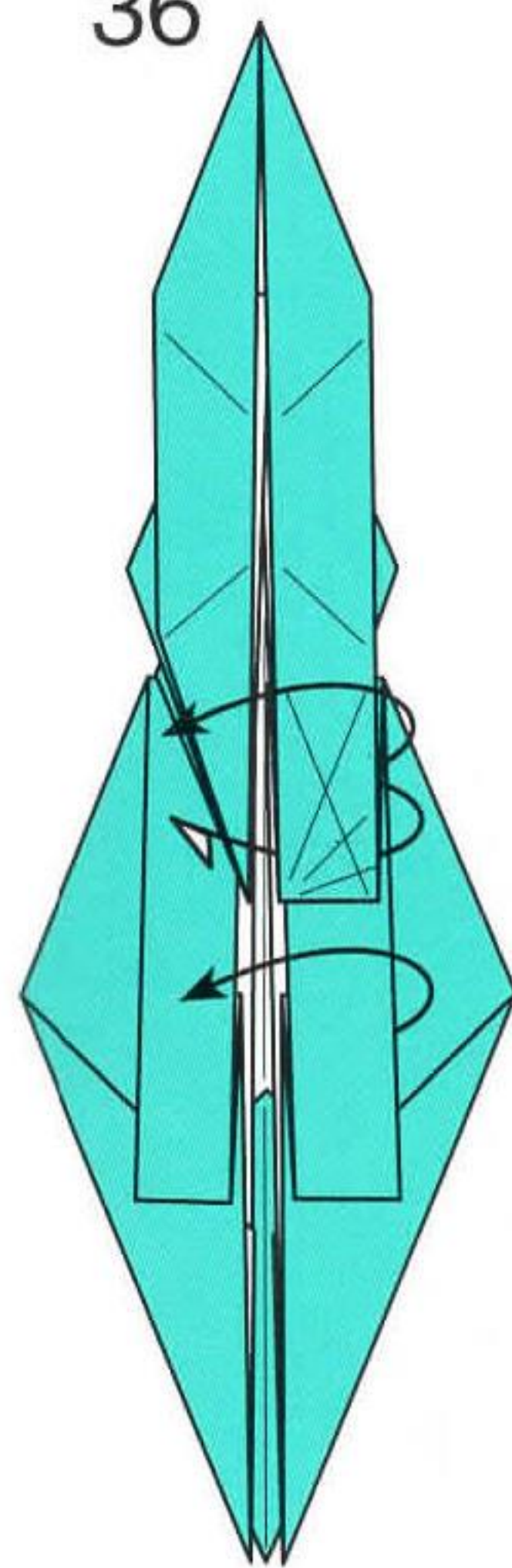
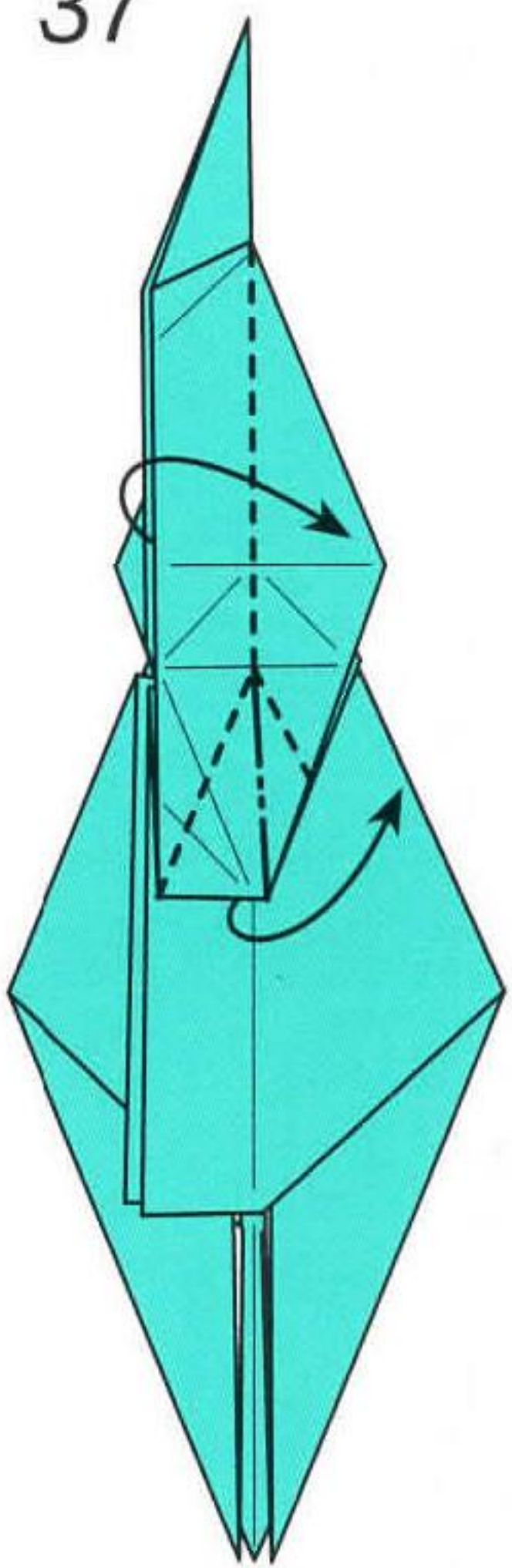


Diagram 36: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.



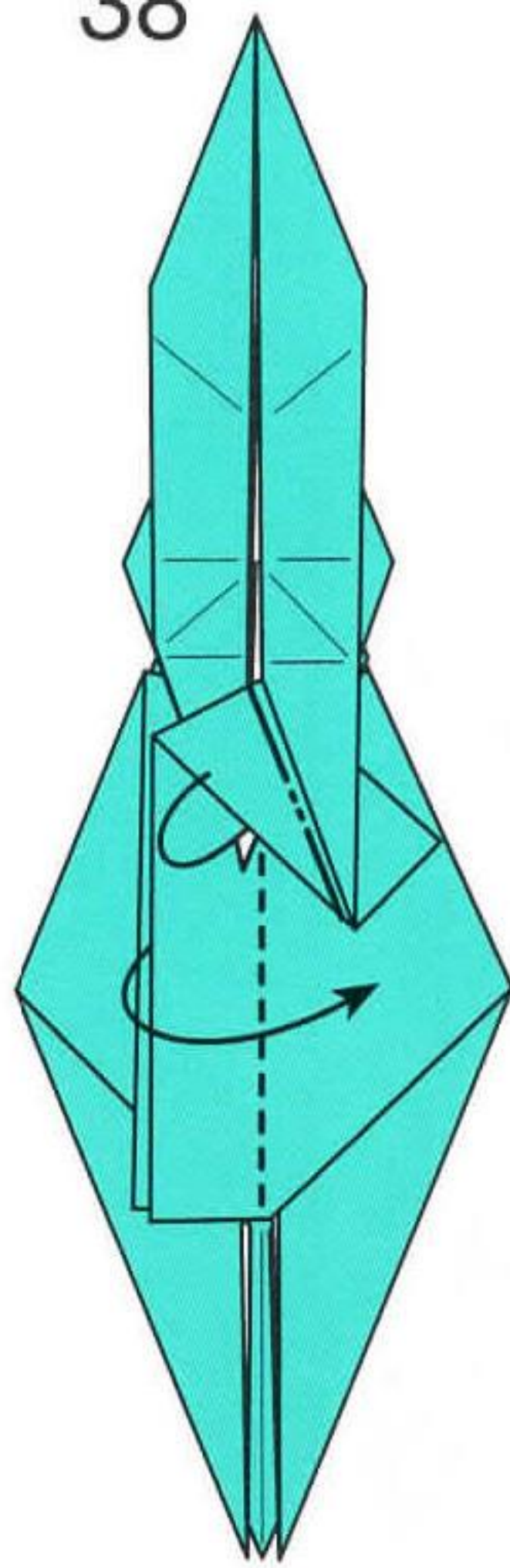
Outside reverse-fold

Diagram 37: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.



Fold like an inside reverse fold.

Diagram 38: A diamond-shaped paper with a vertical crease. An arrow indicates a fold from the top edge towards the center crease.



Swivel-fold

Diagram 39: A circular inset showing a close-up of the fold in diagram 38.

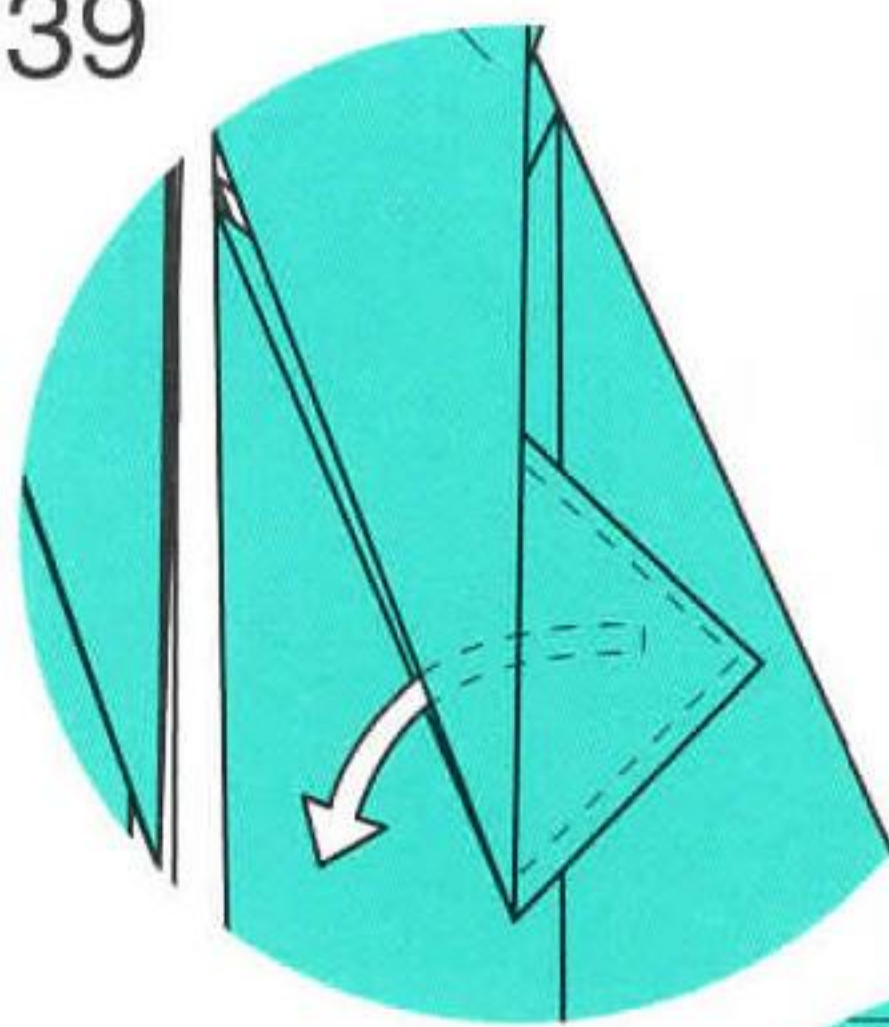
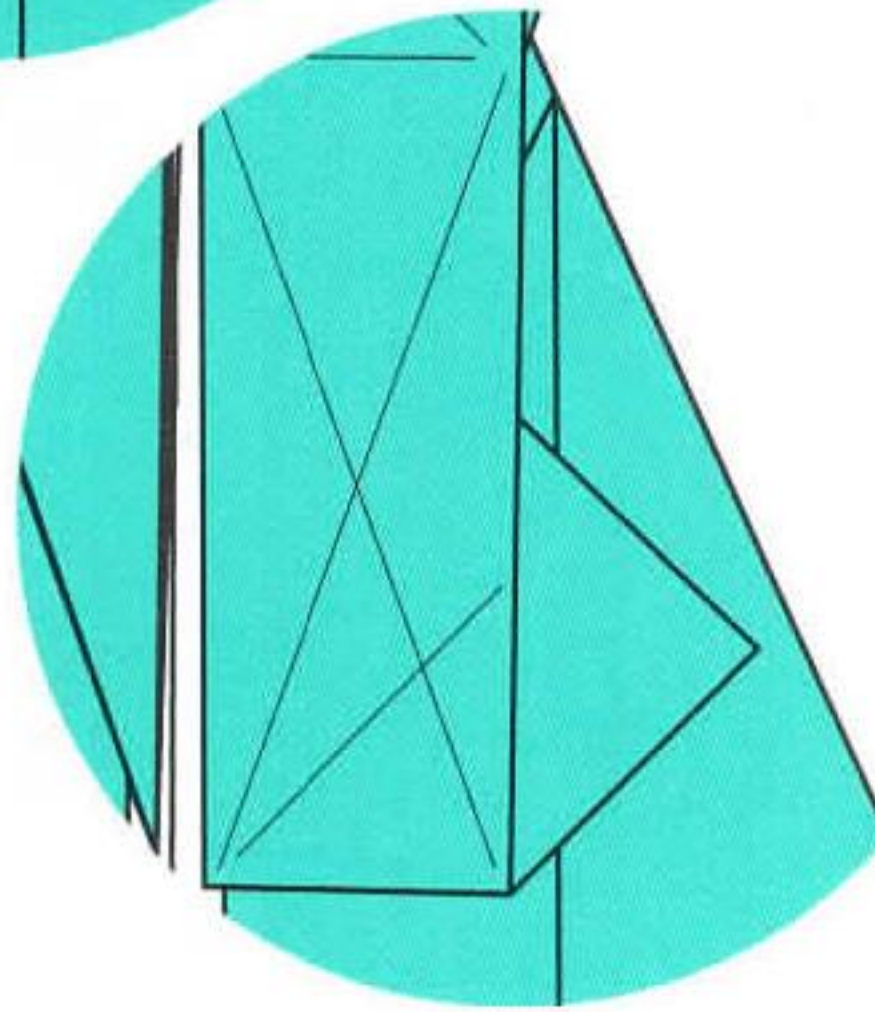
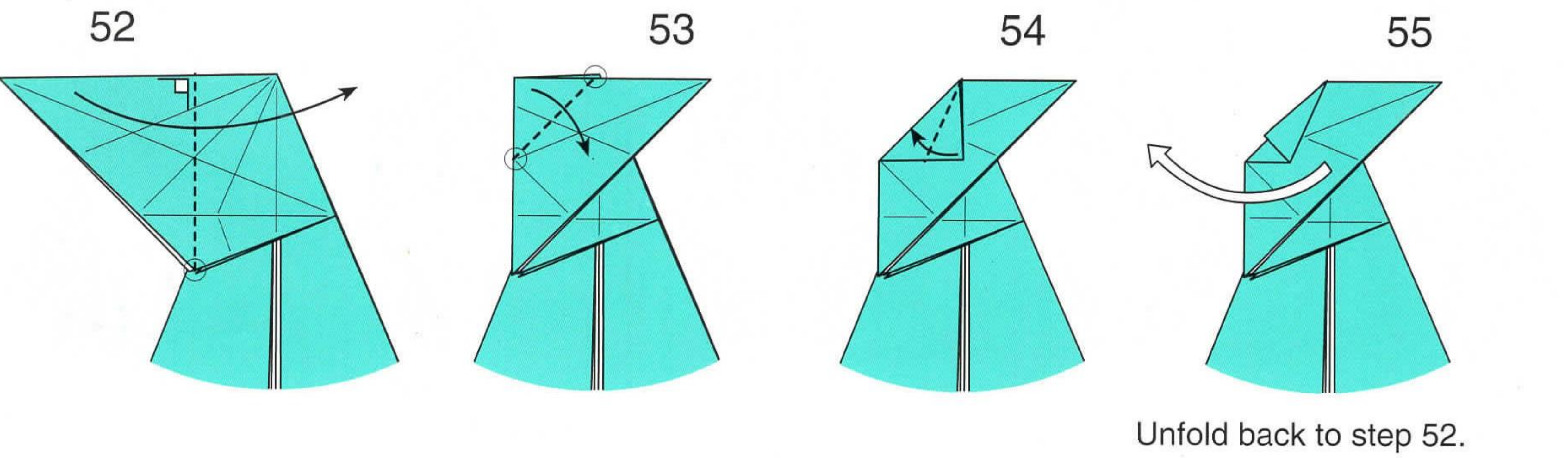
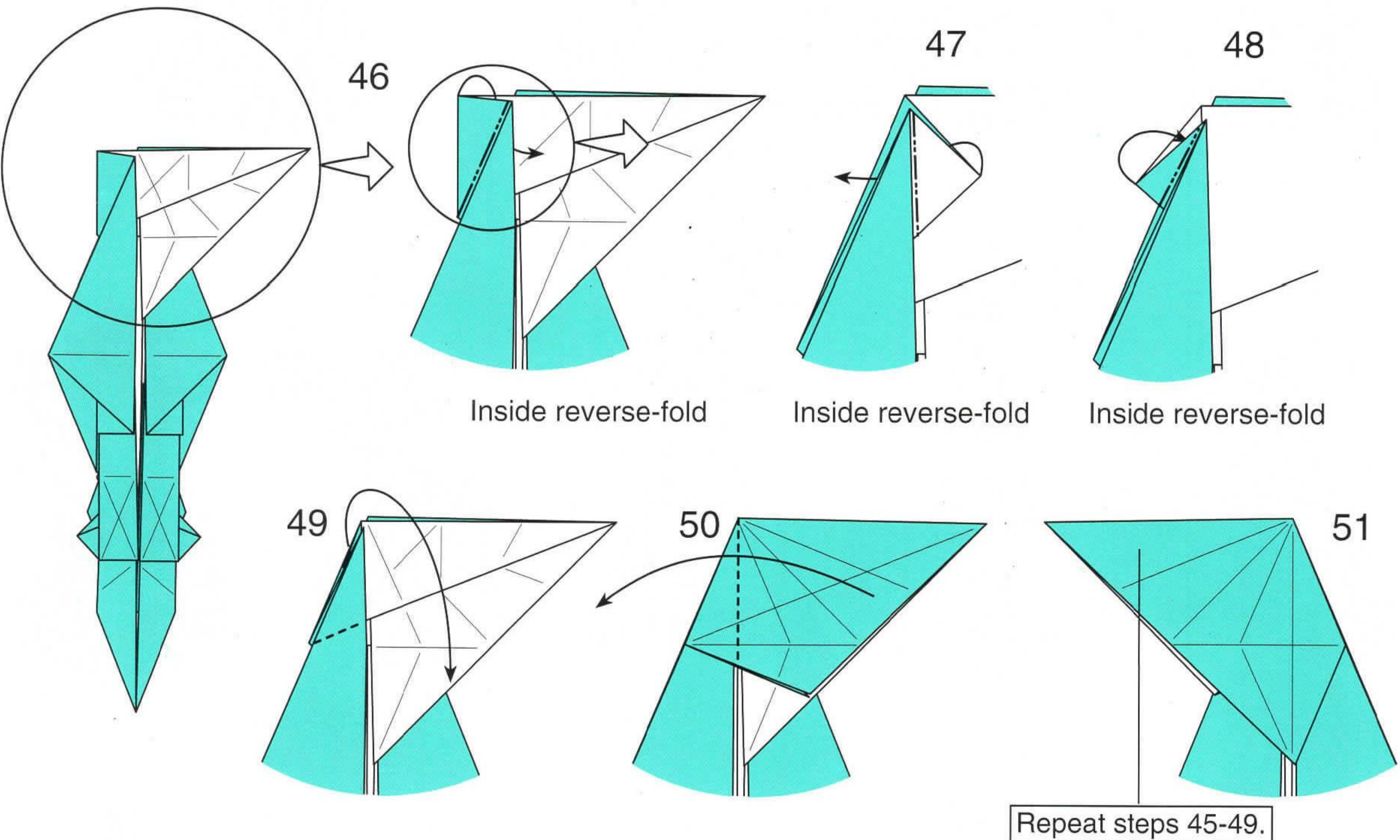
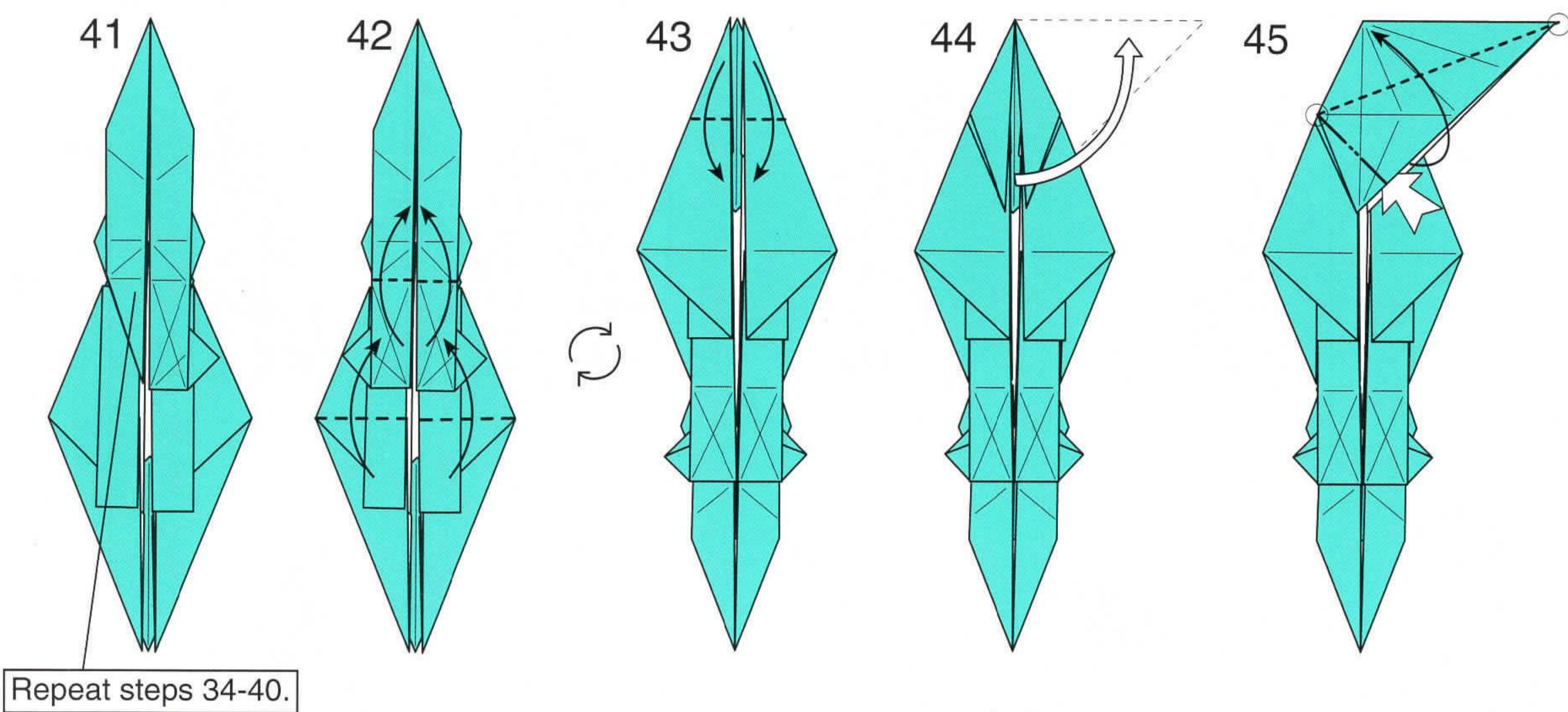
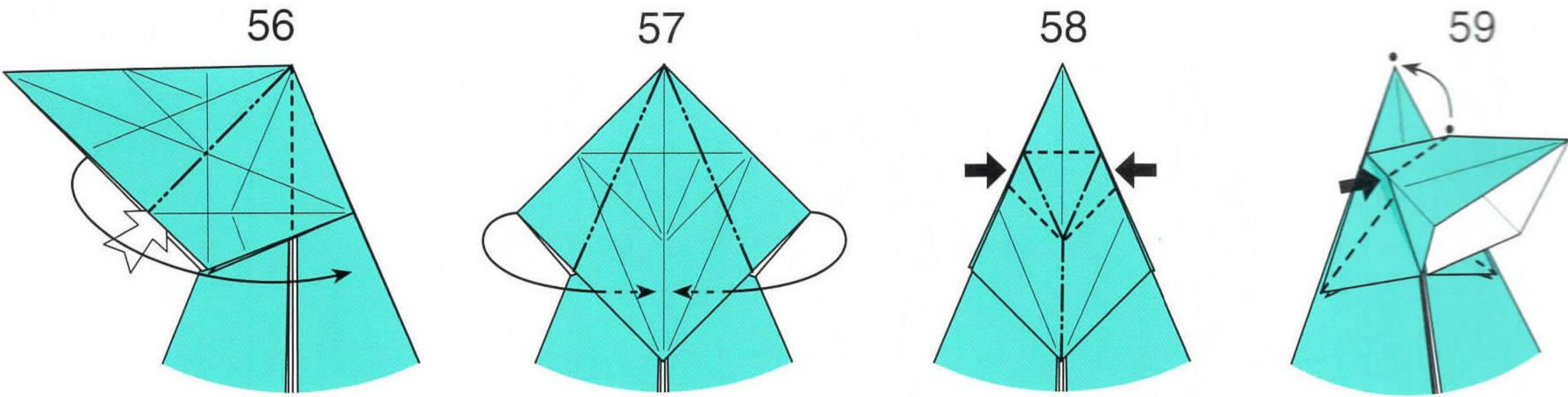


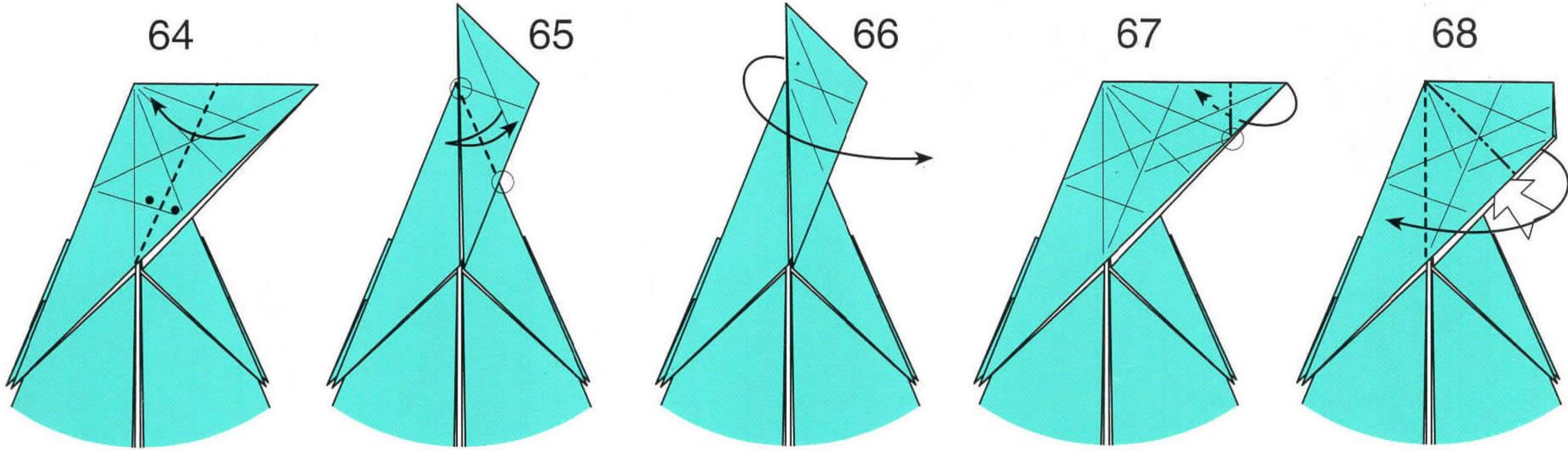
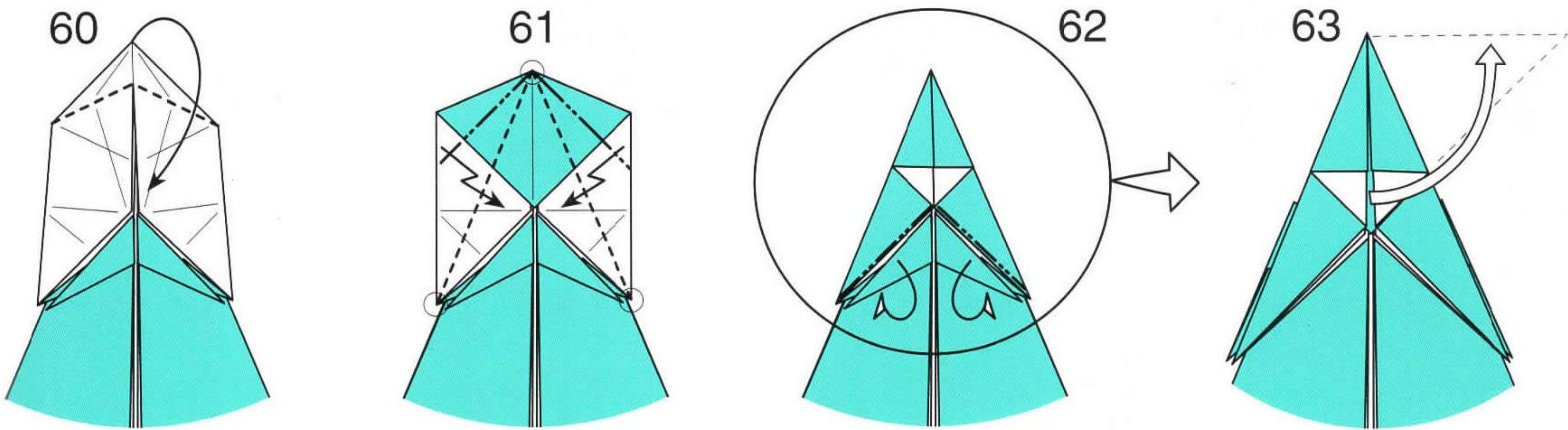
Diagram 40: A circular inset showing a close-up of the fold in diagram 38.



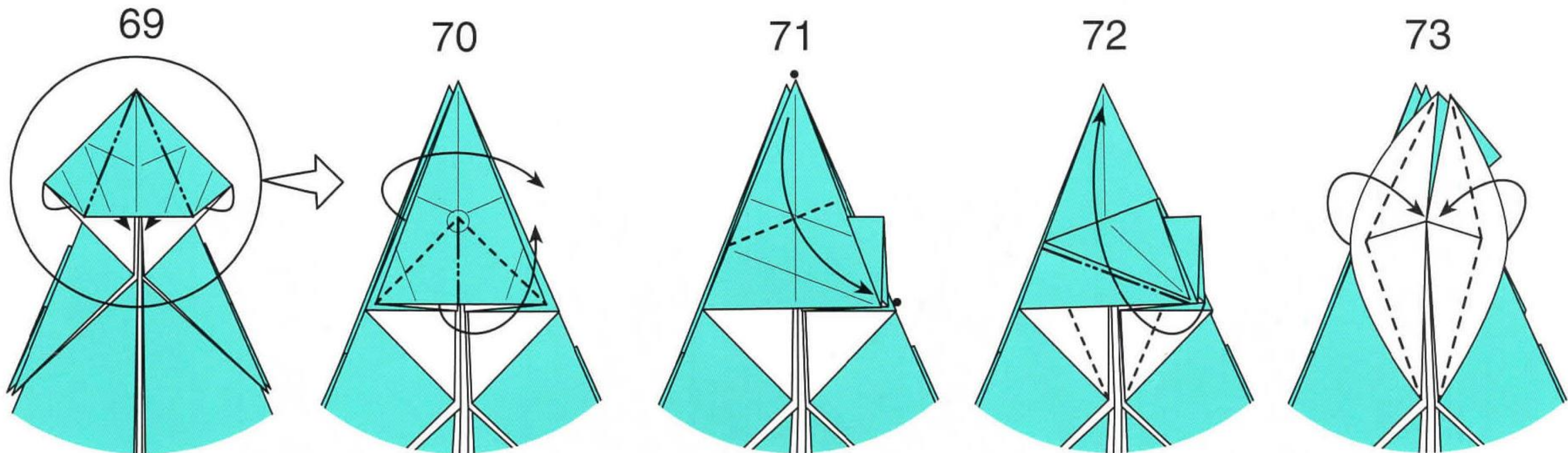




Inside reverse-fold

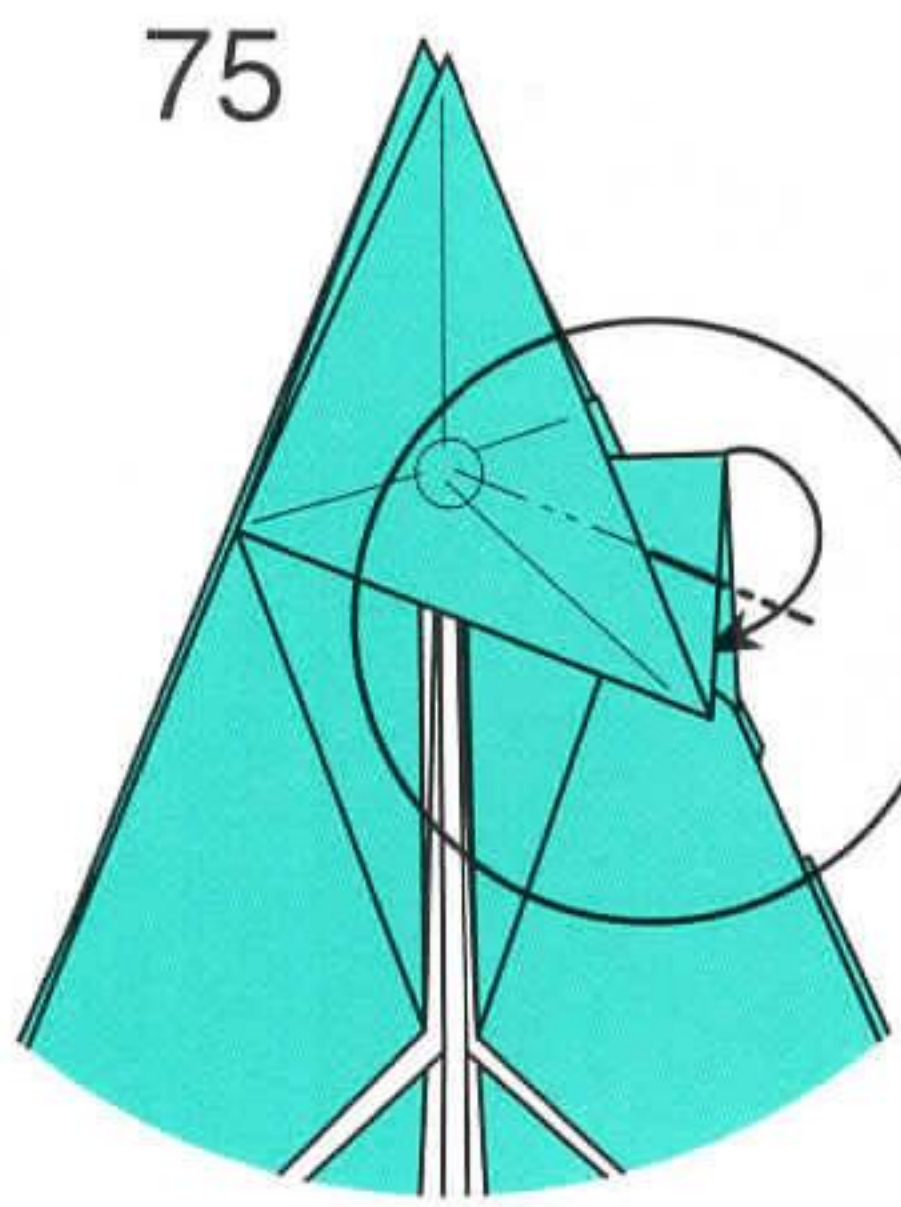
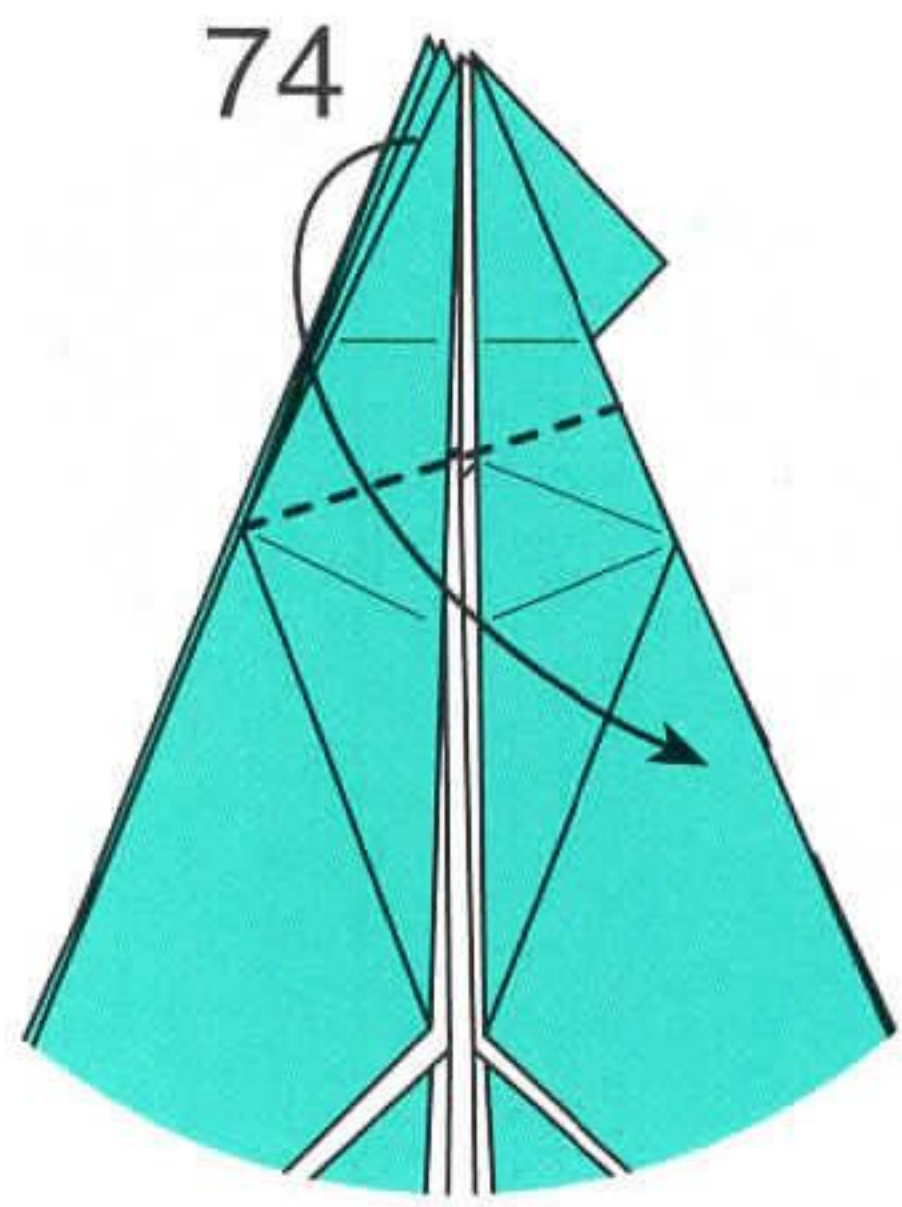


Inside reverse-fold

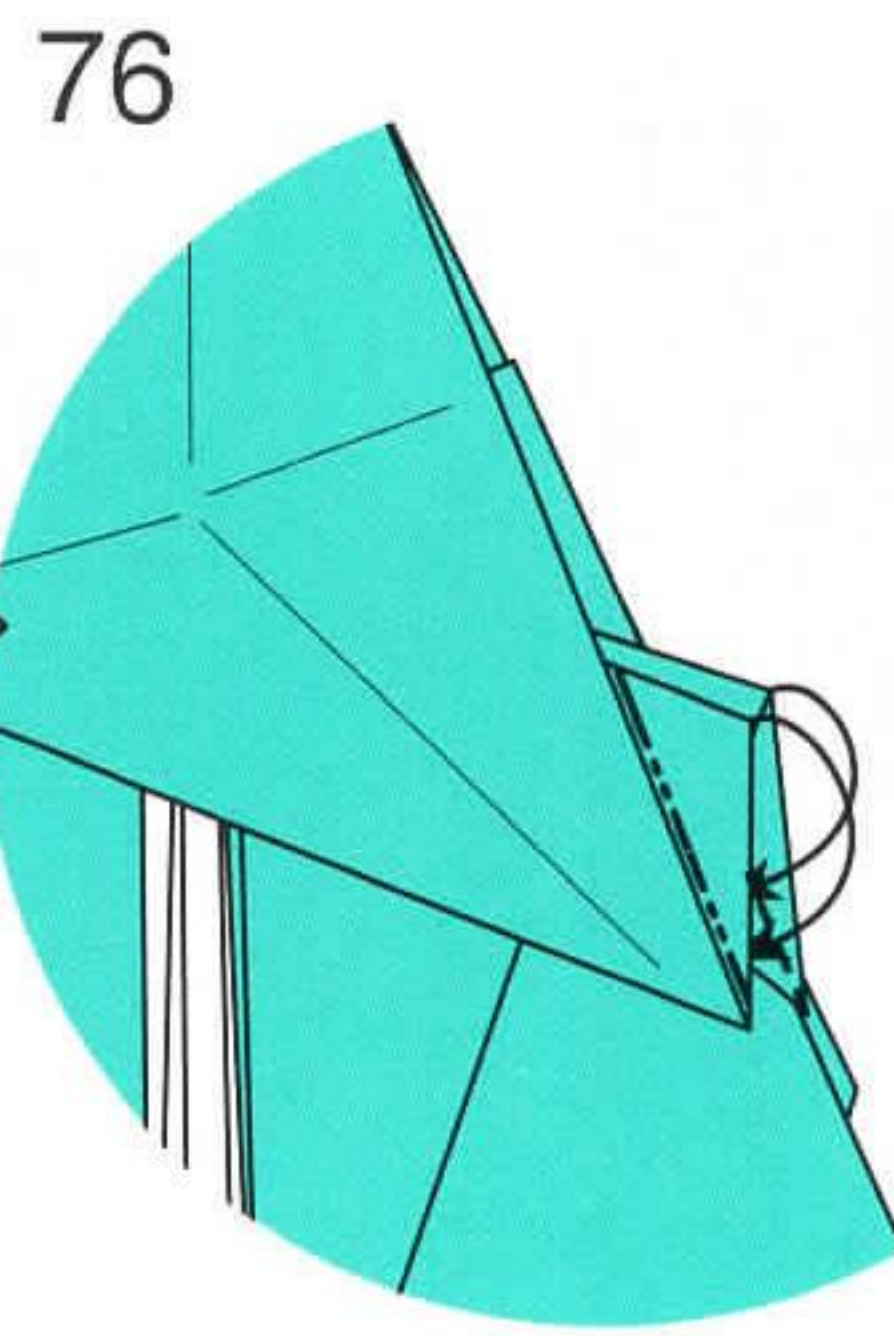


Inside reverse-fold

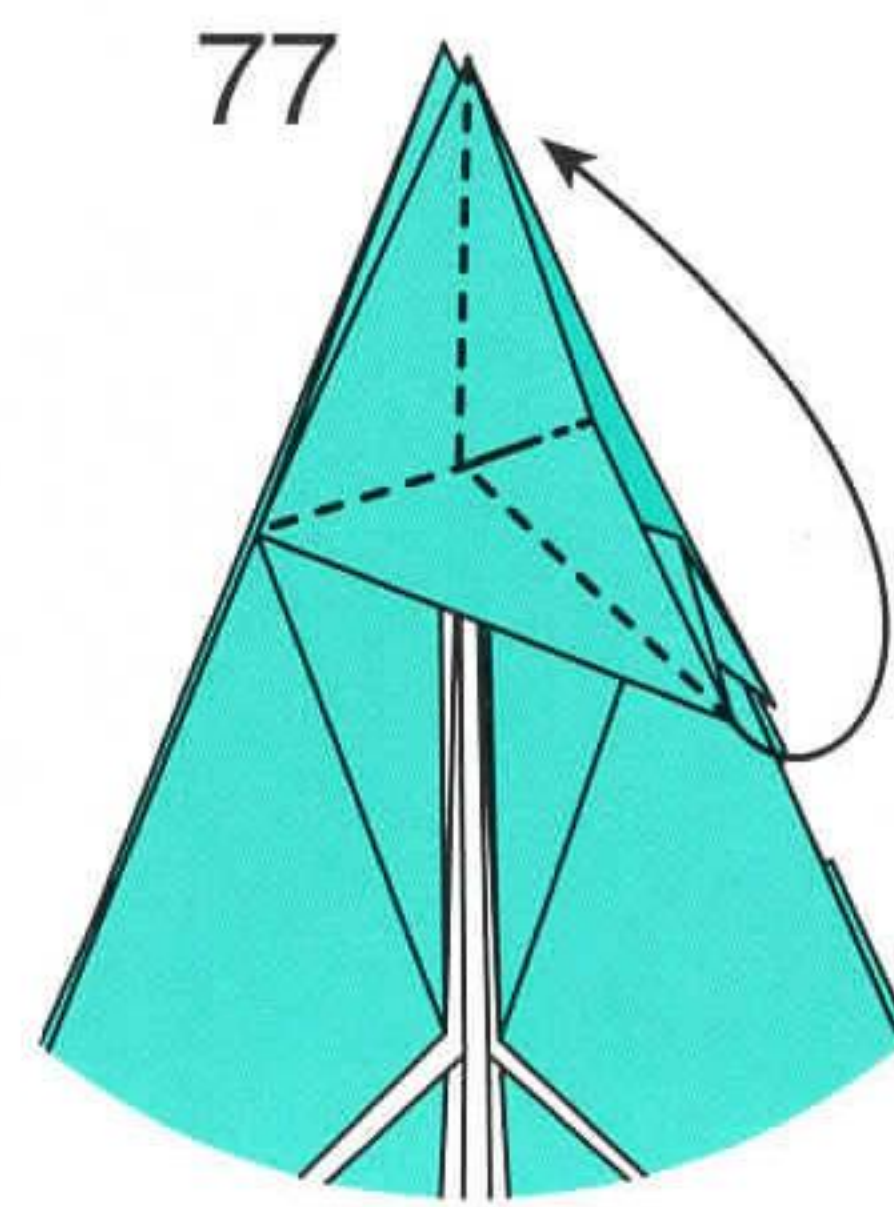
Fold all the layers together.



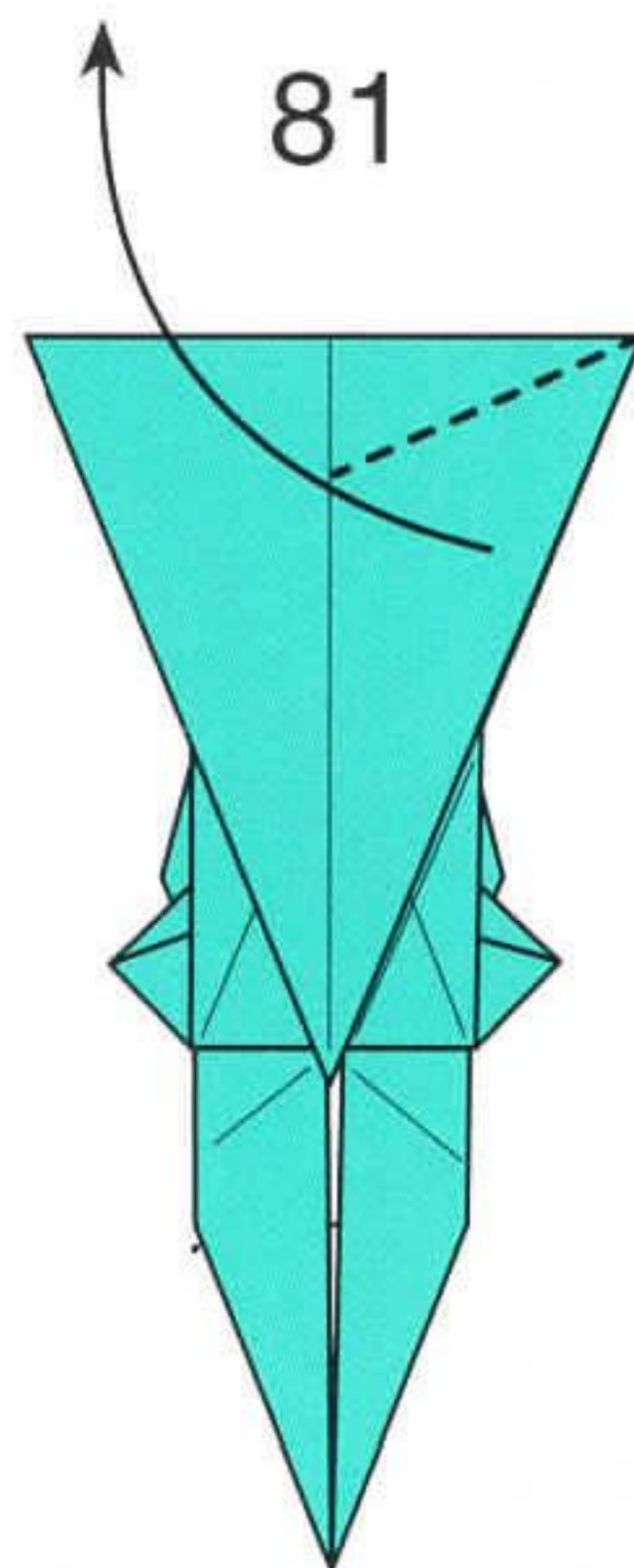
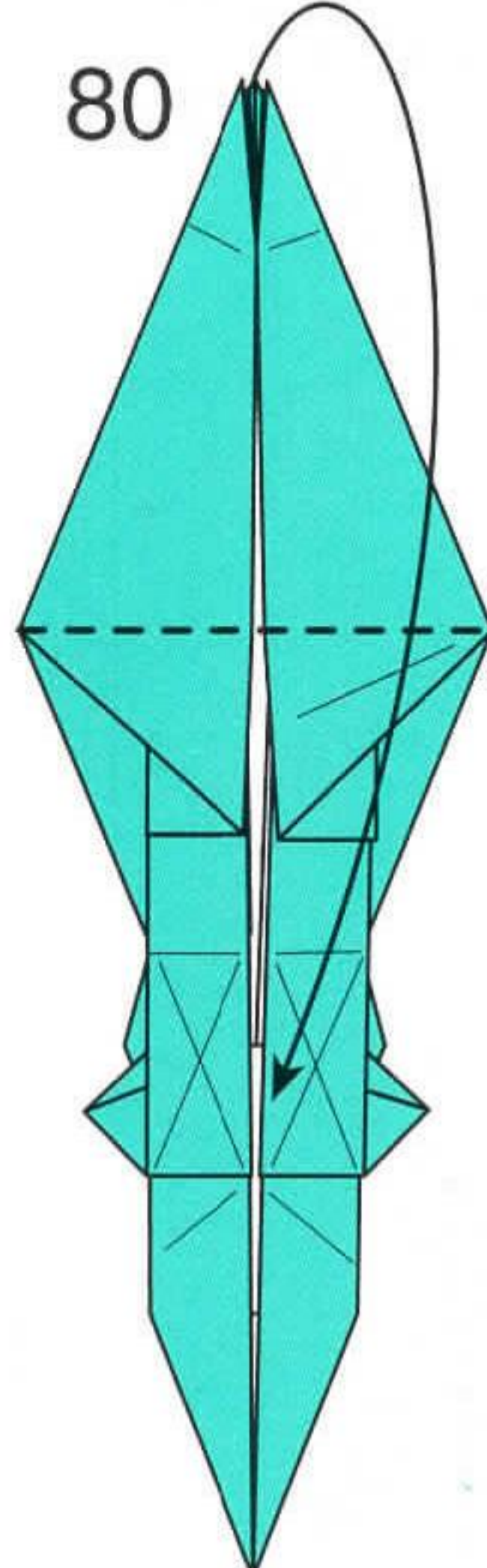
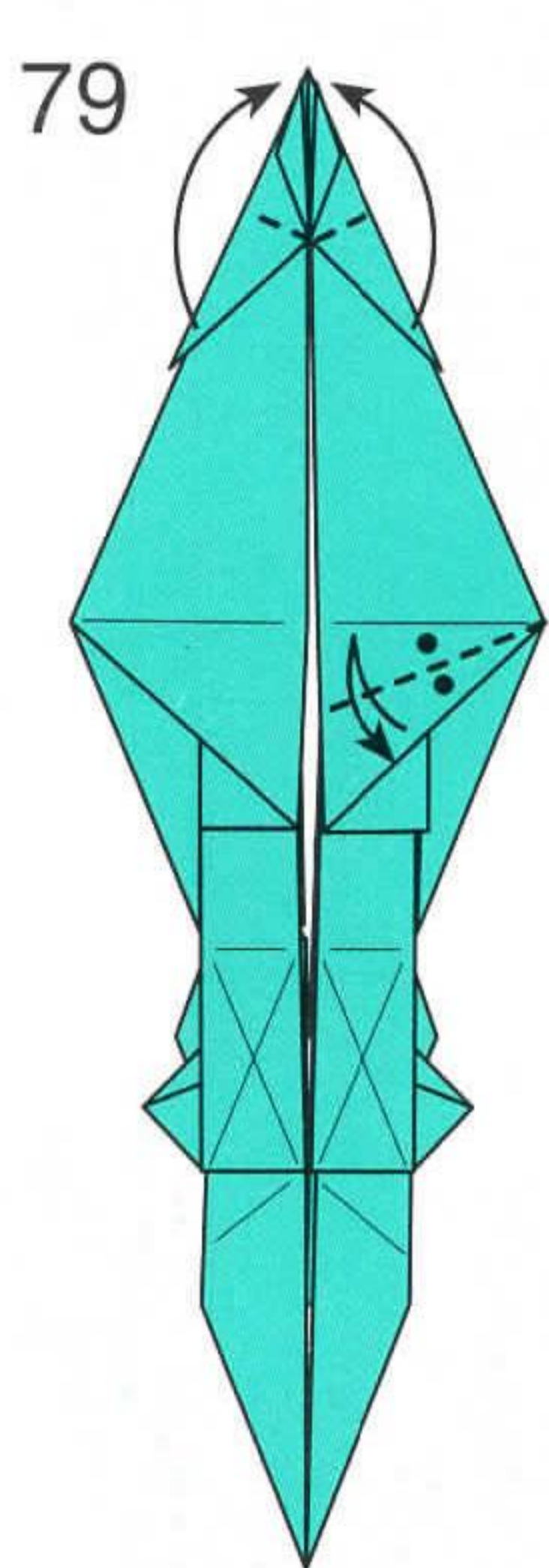
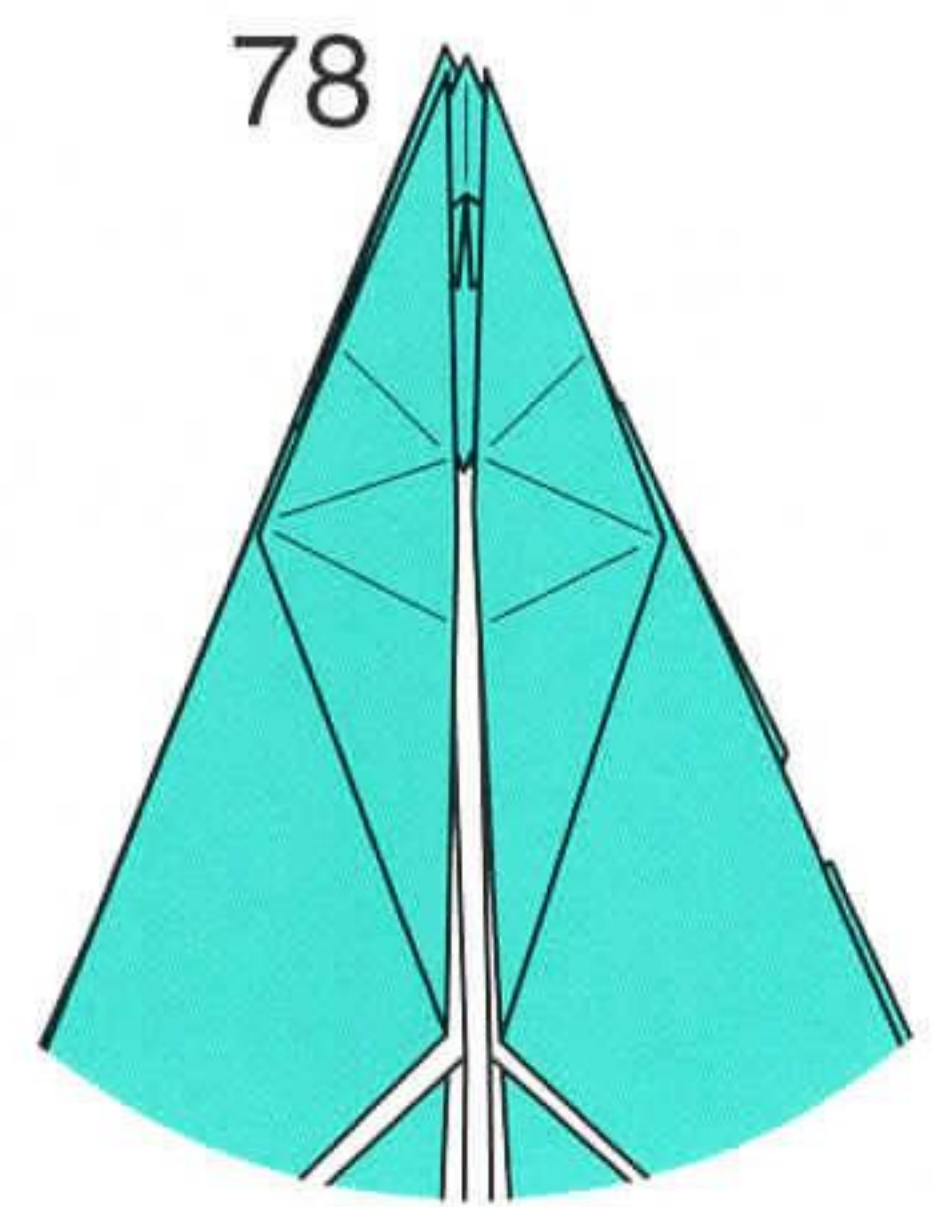
Inside reverse-fold



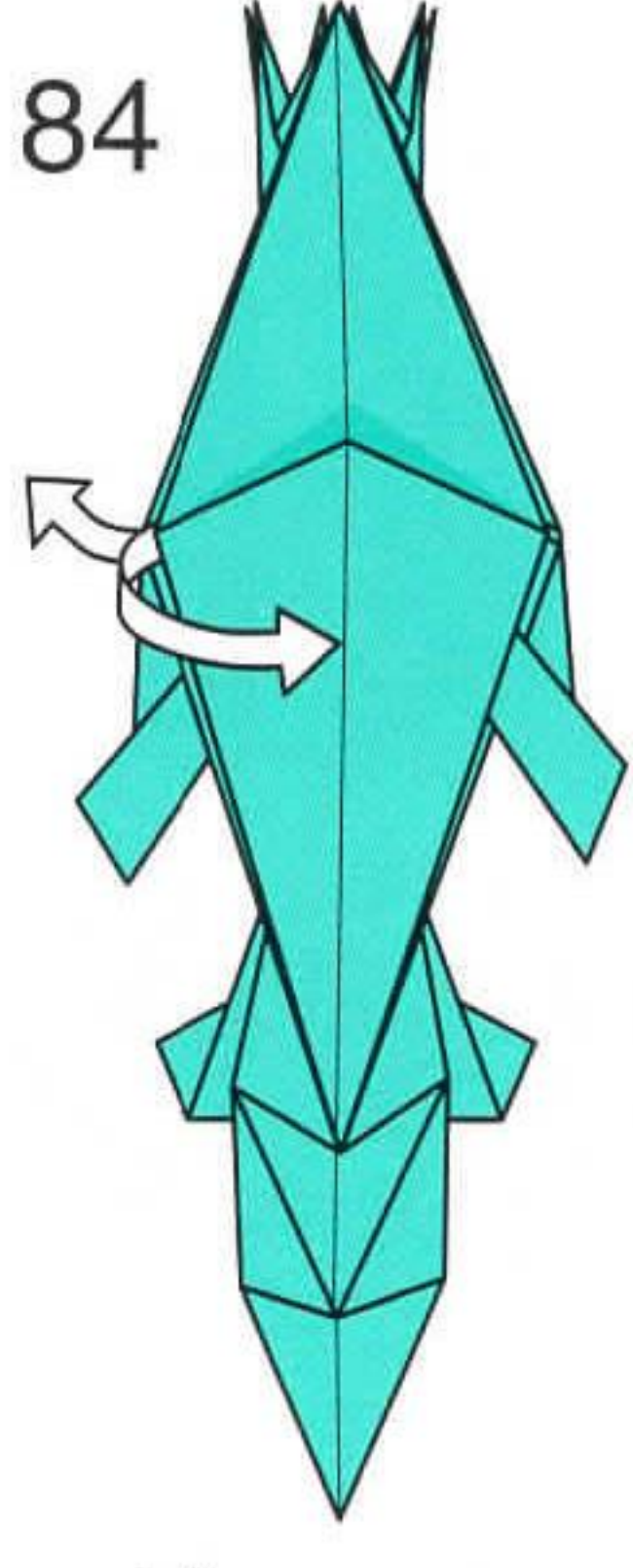
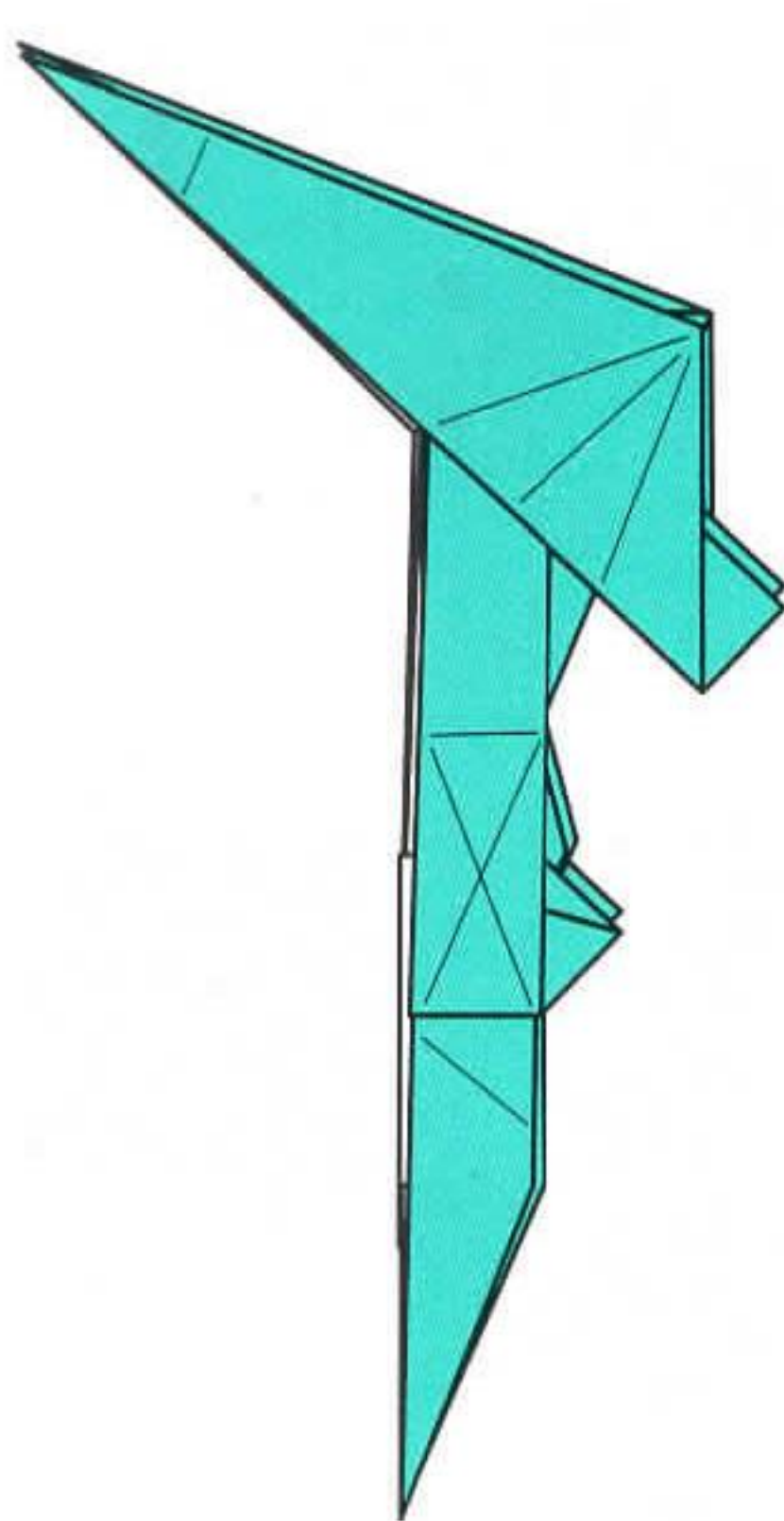
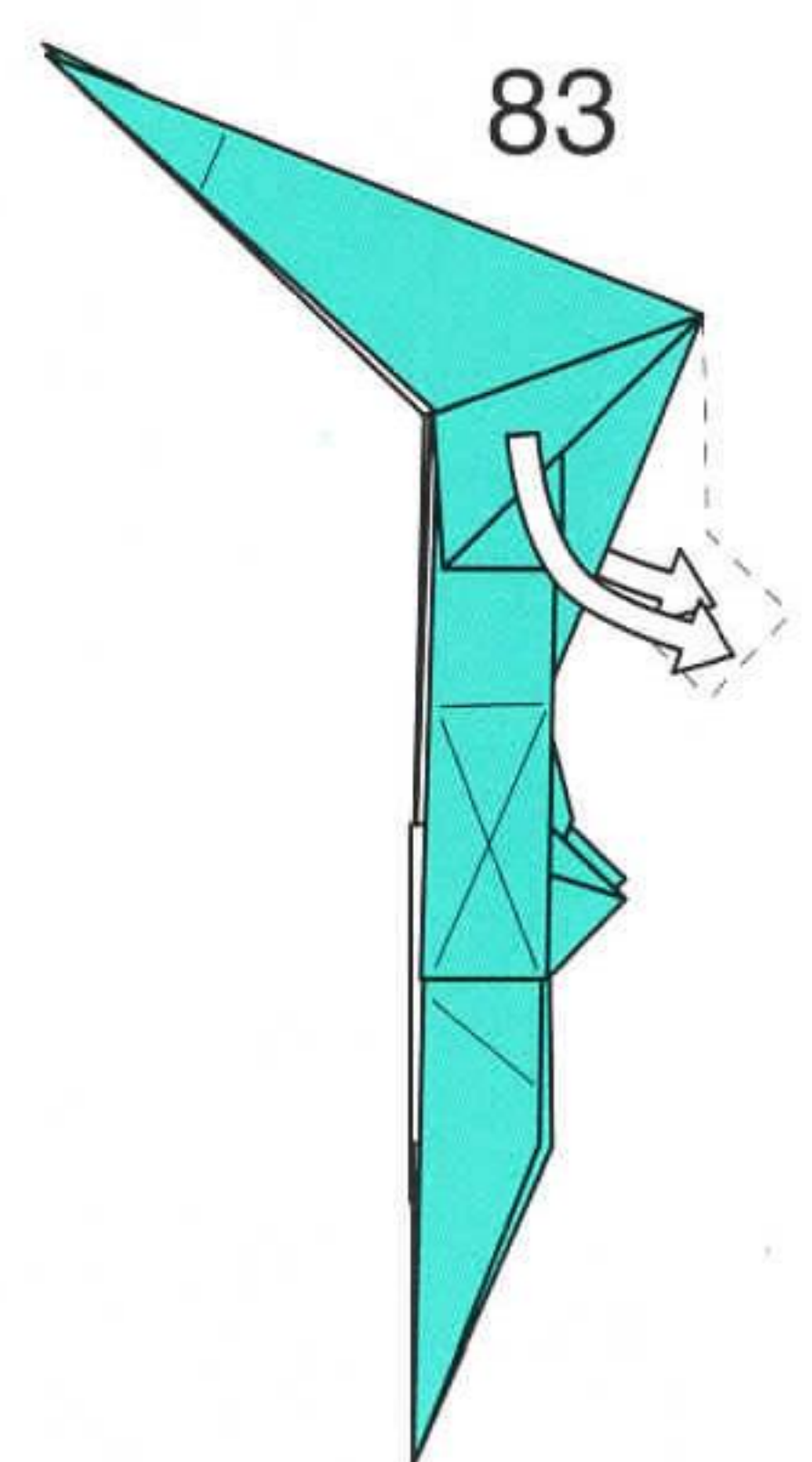
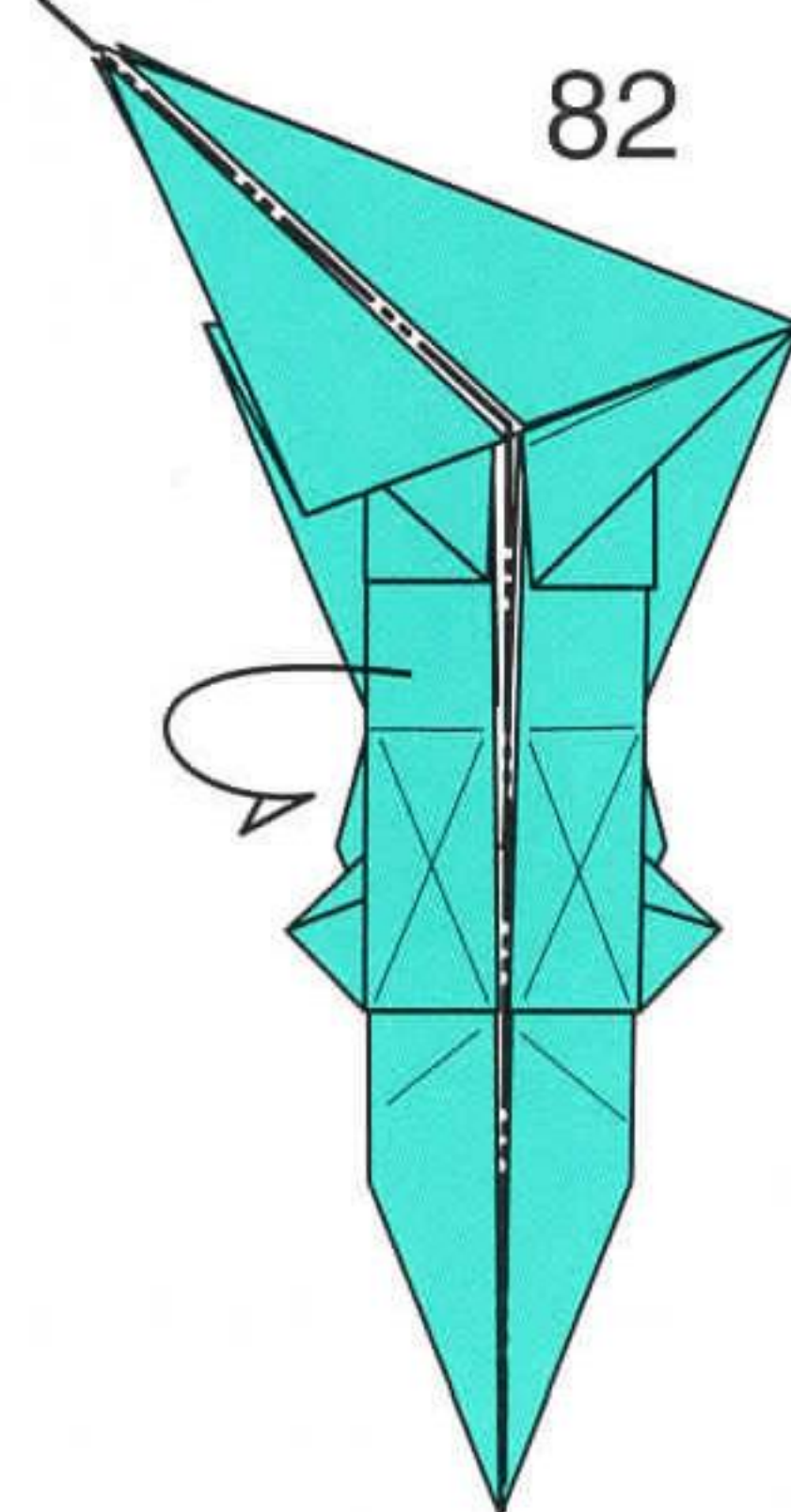
Inside reverse-fold



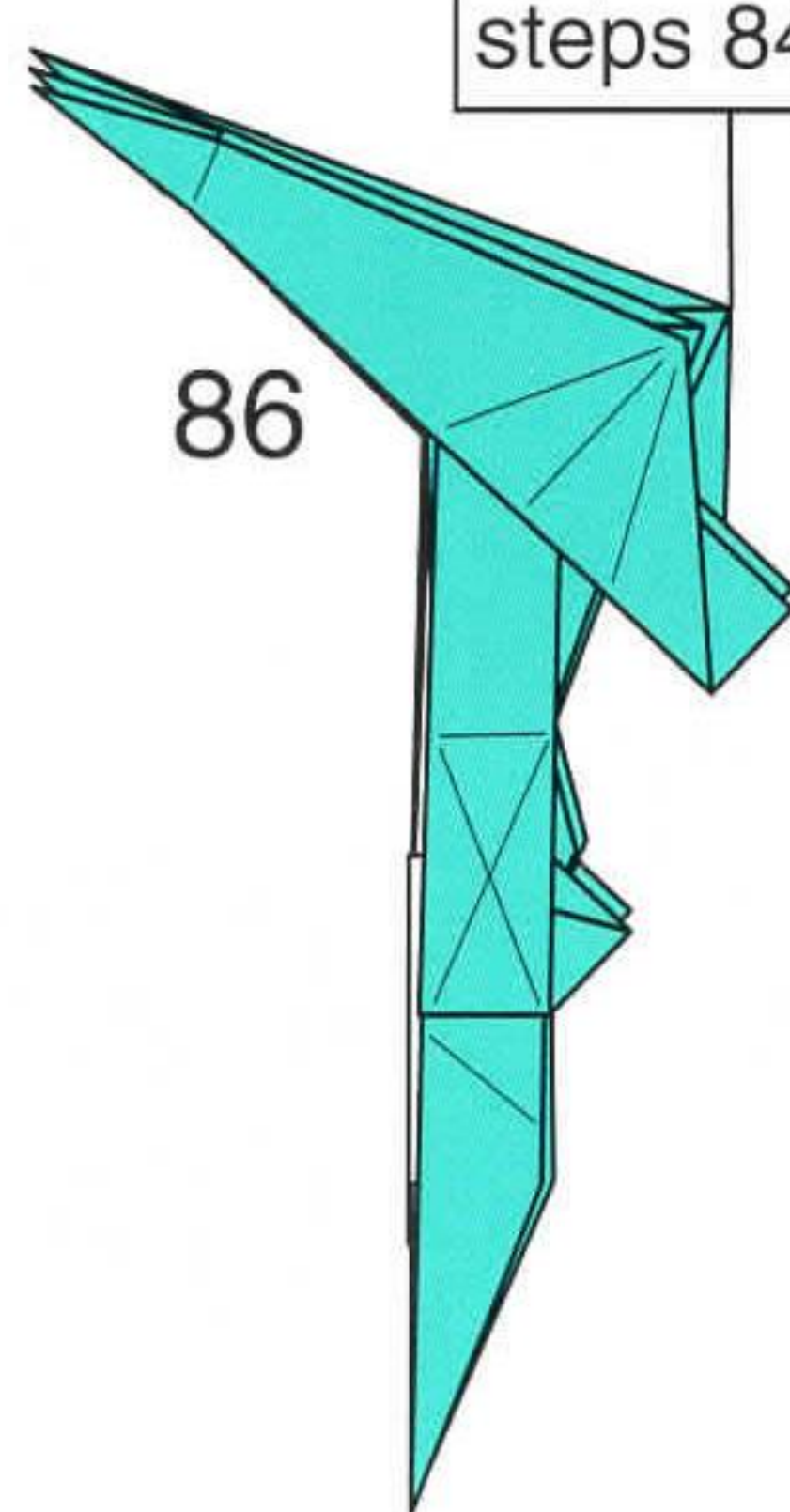
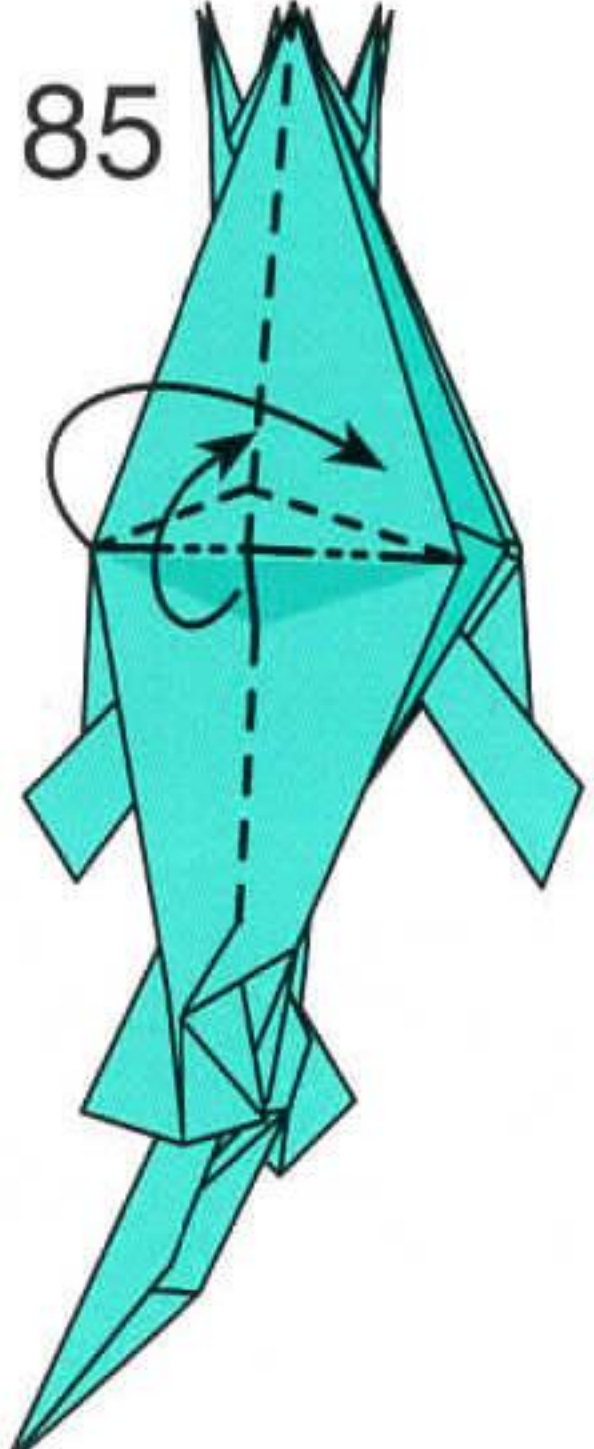
Make the model symmetrical.



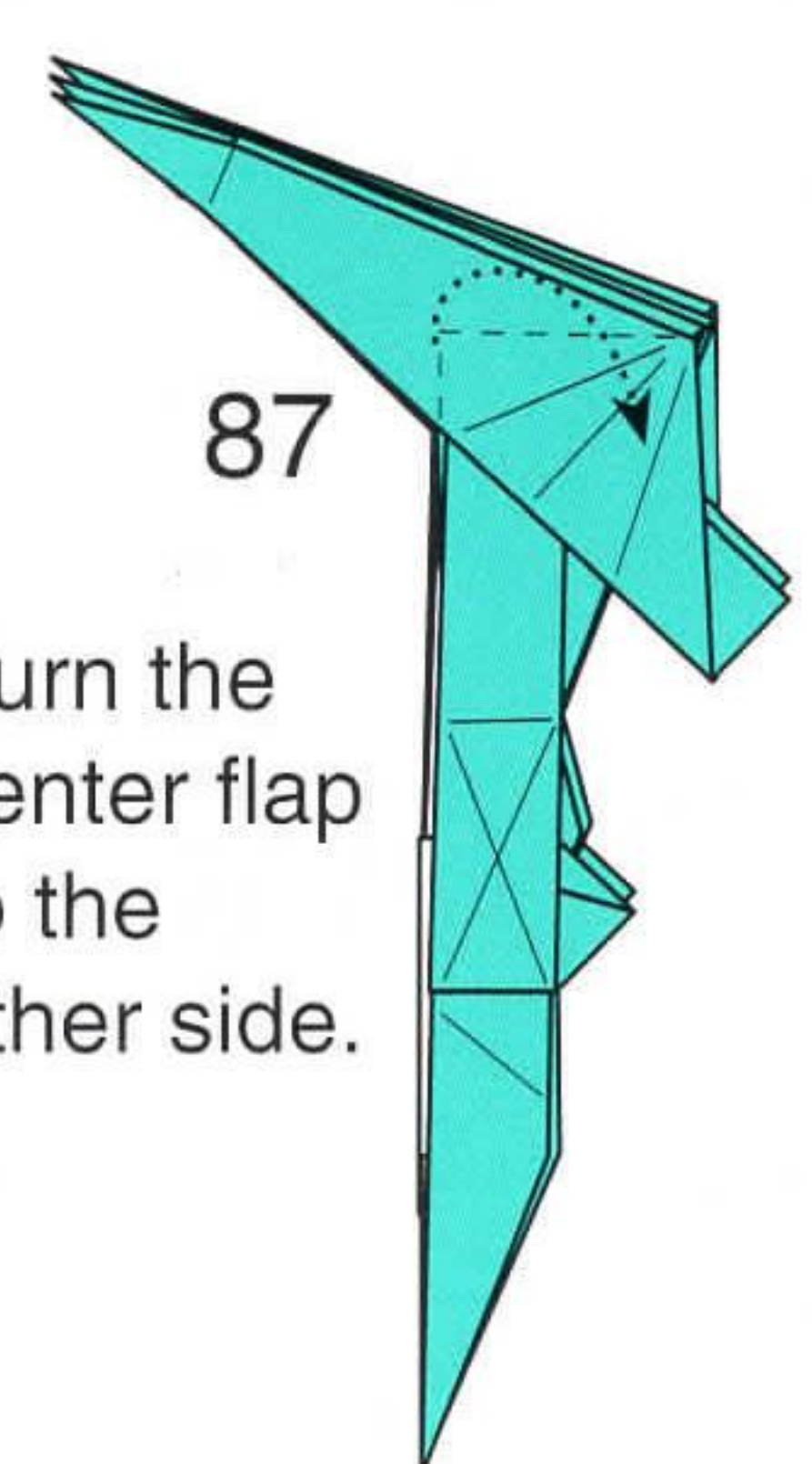
Fold along the crease made in step 79.



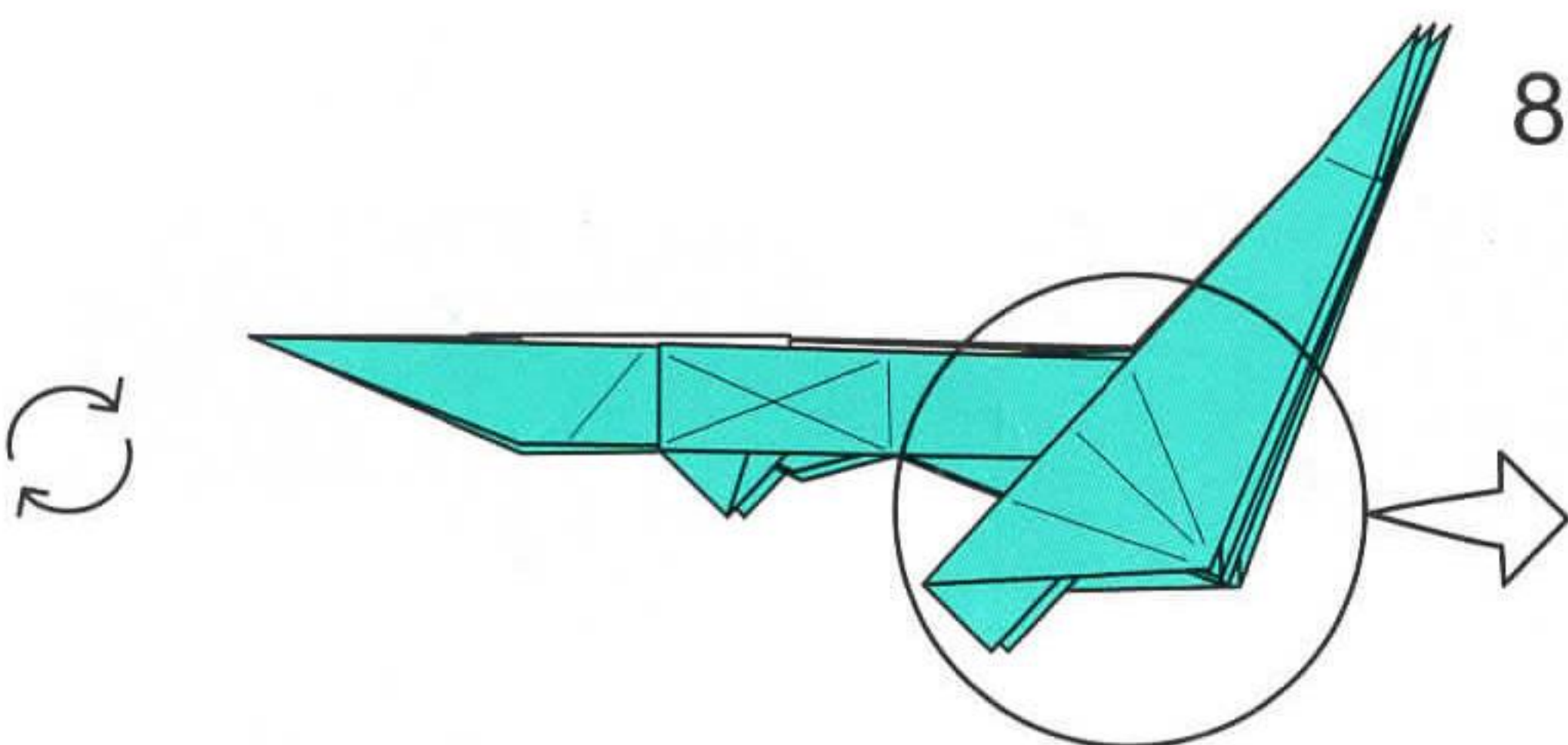
Unwrap.



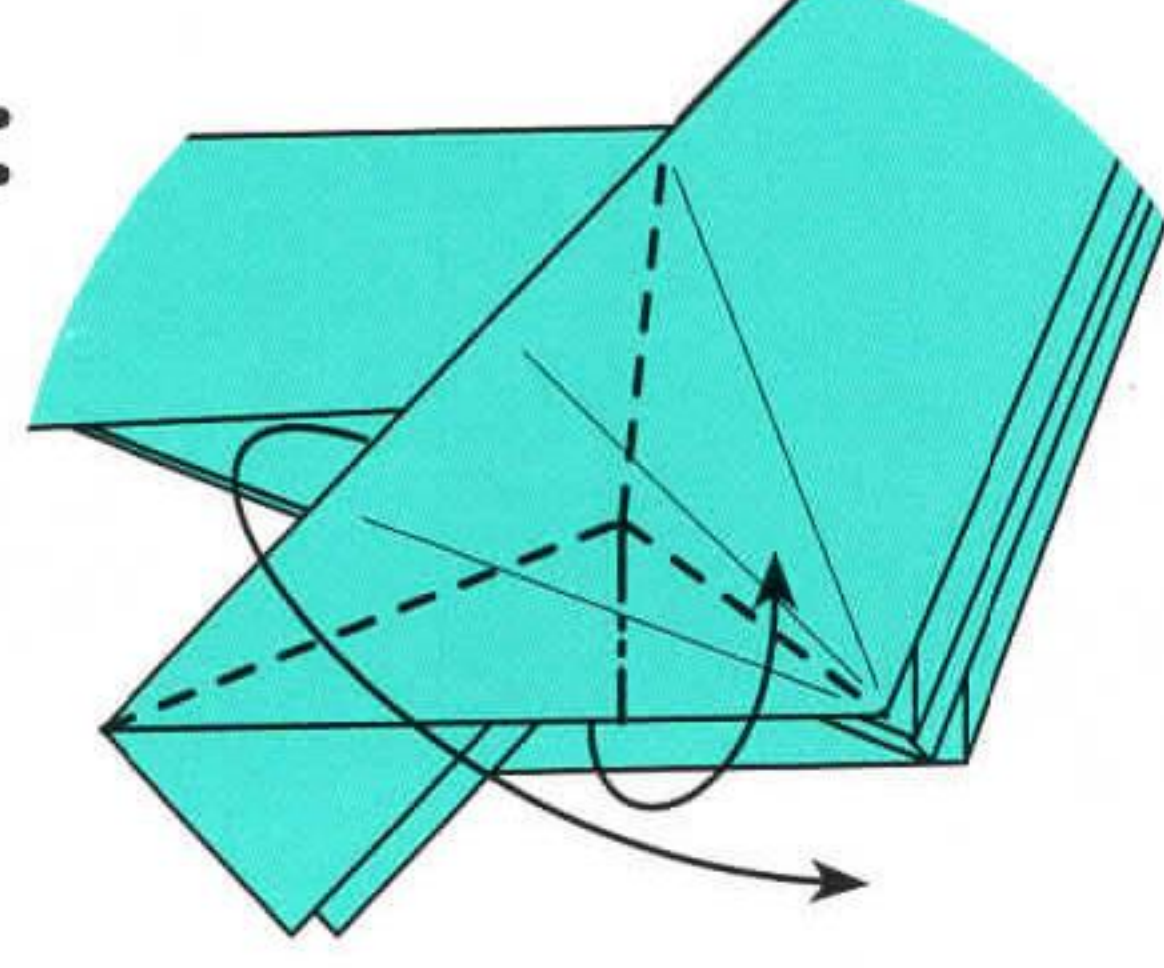
Repeat steps 84-85.



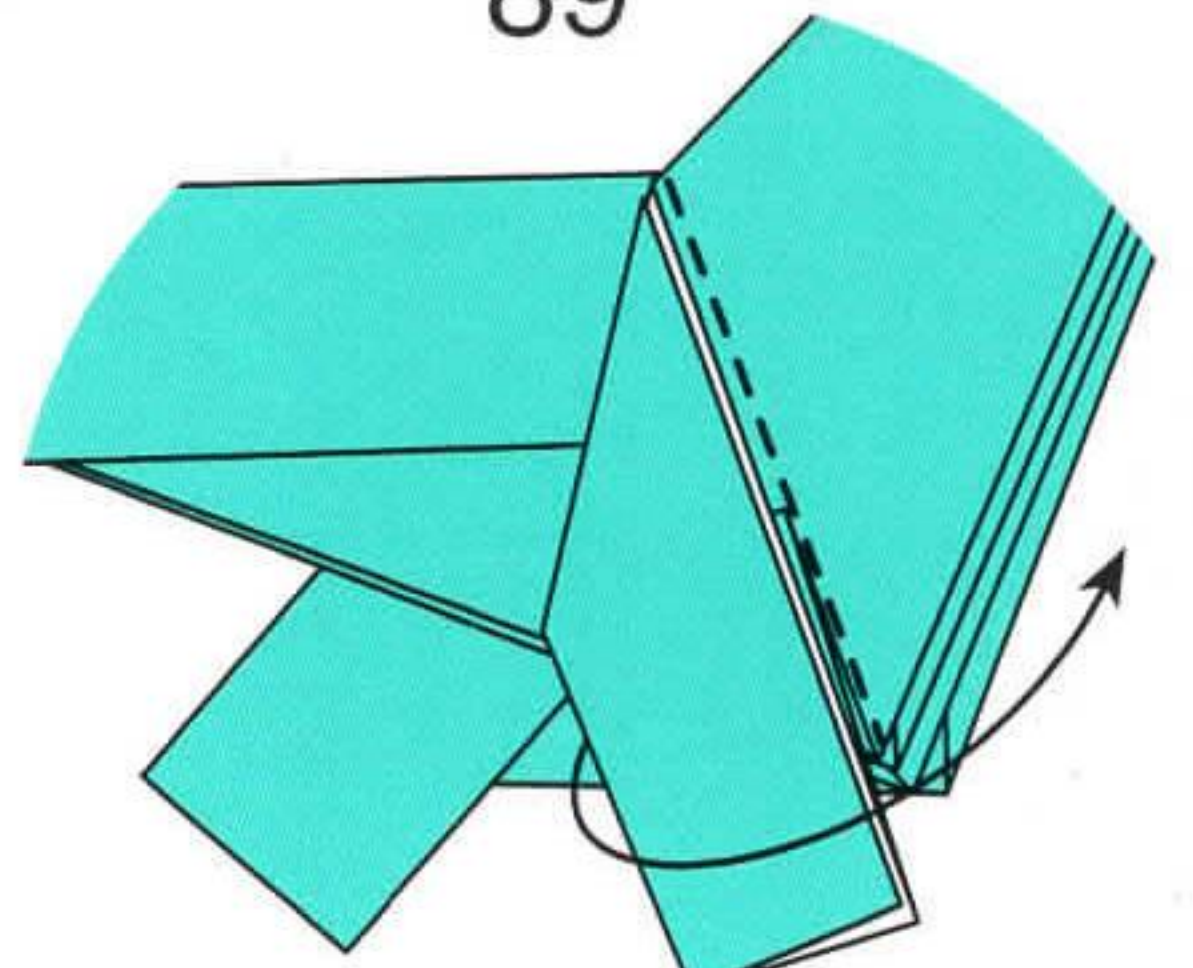
Turn the center flap to the other side.



88||:

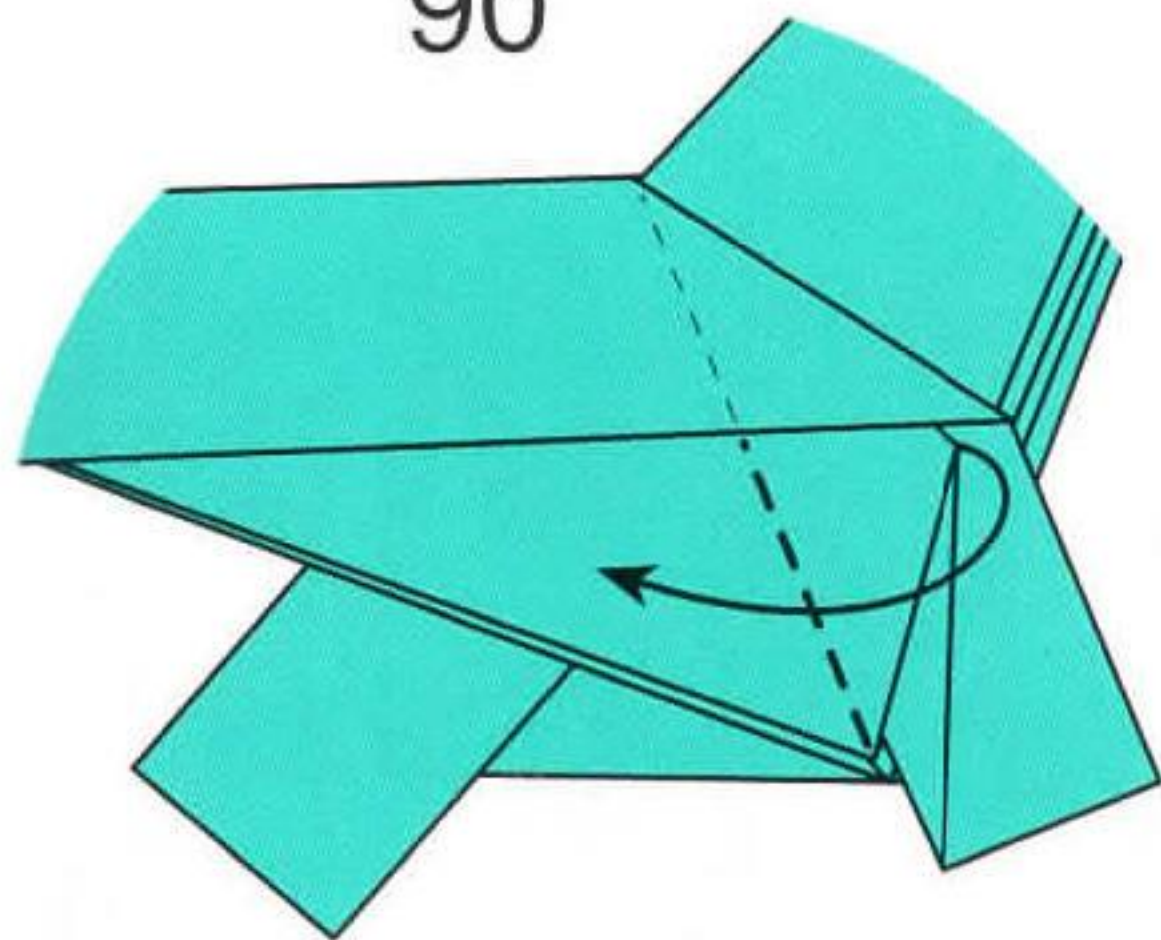


Rabbit-ear-fold

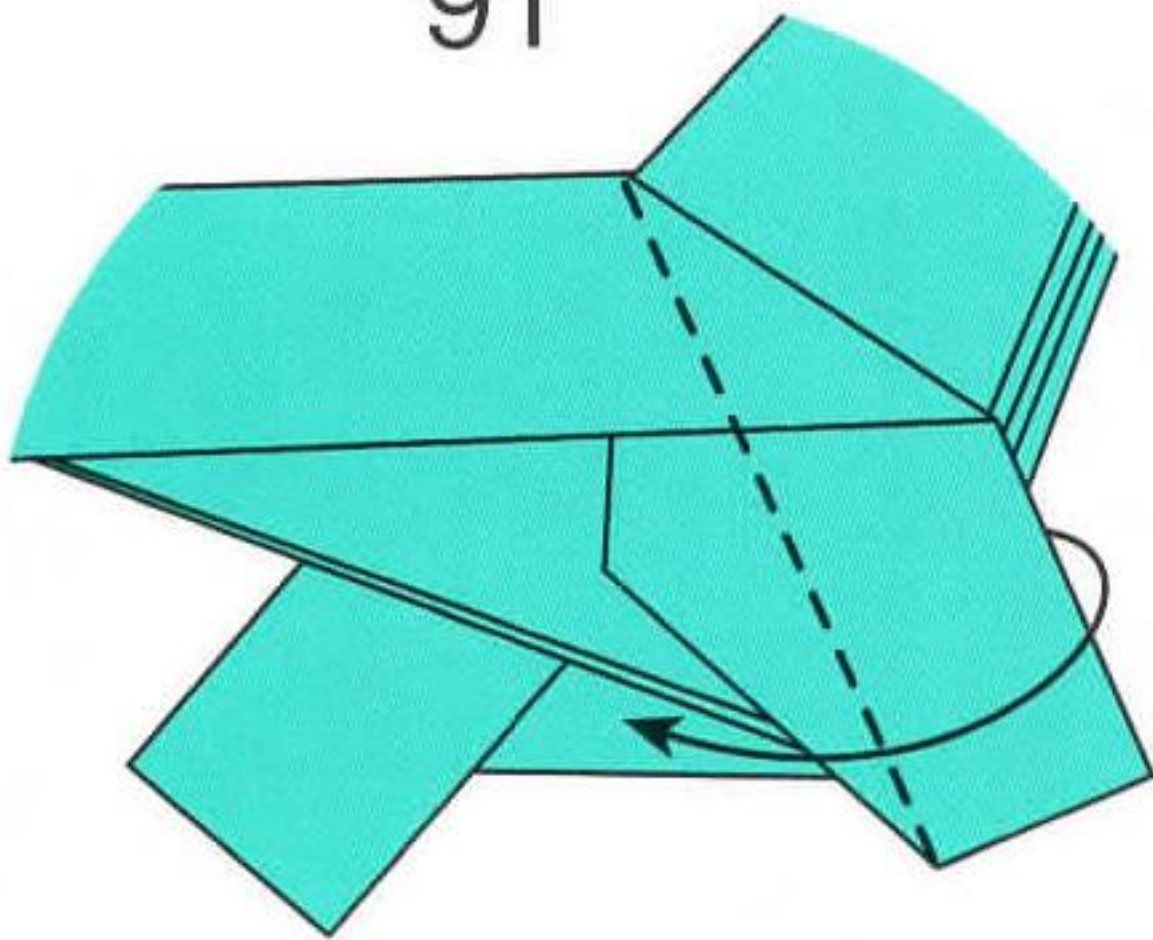


89

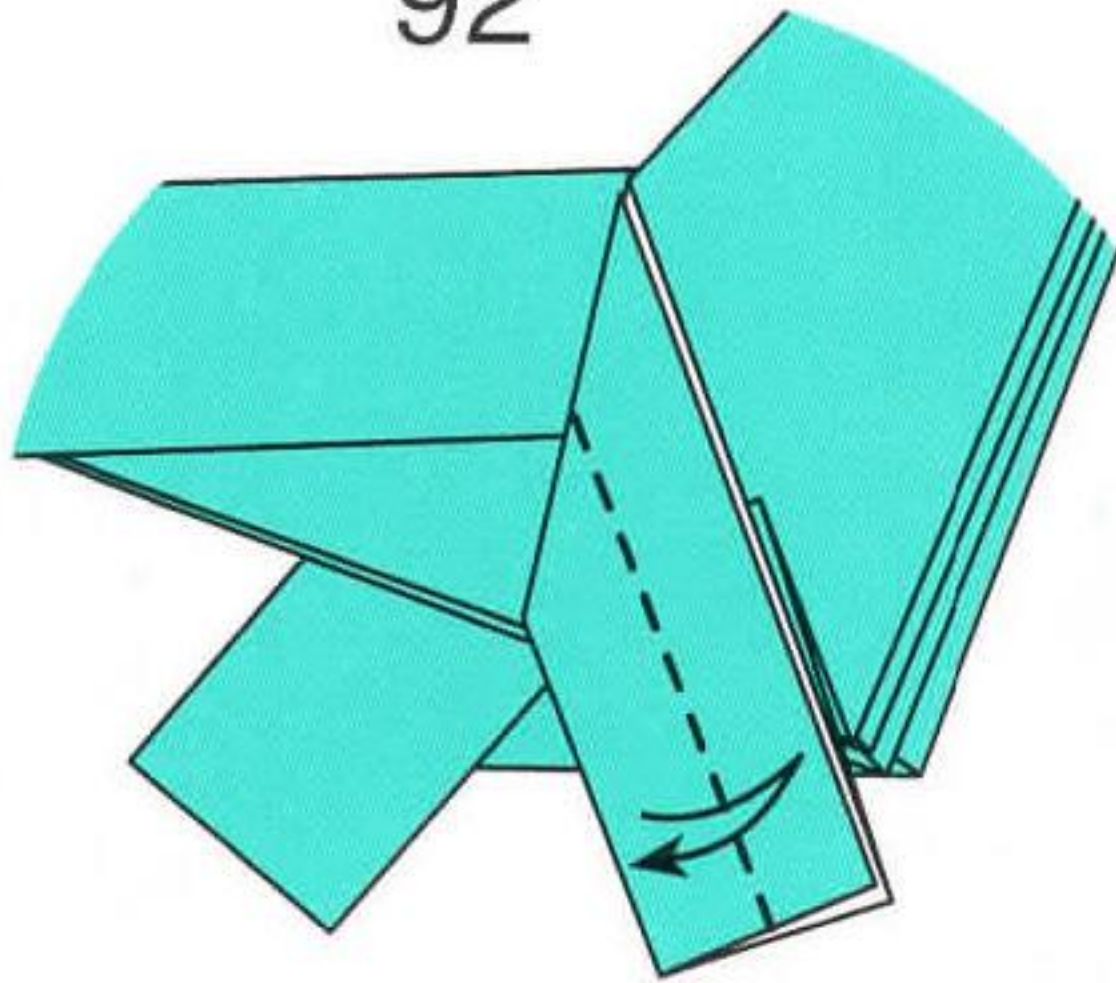
90



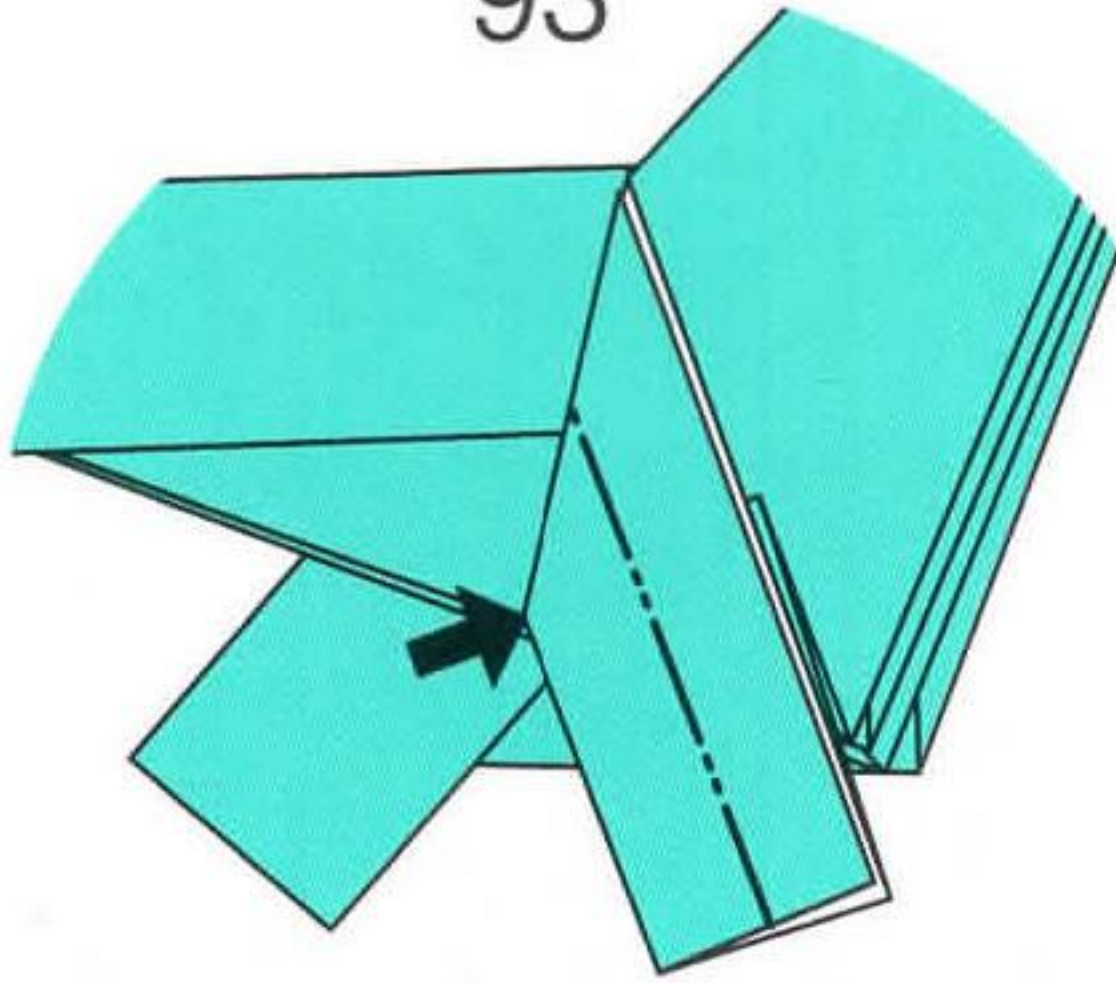
91



92

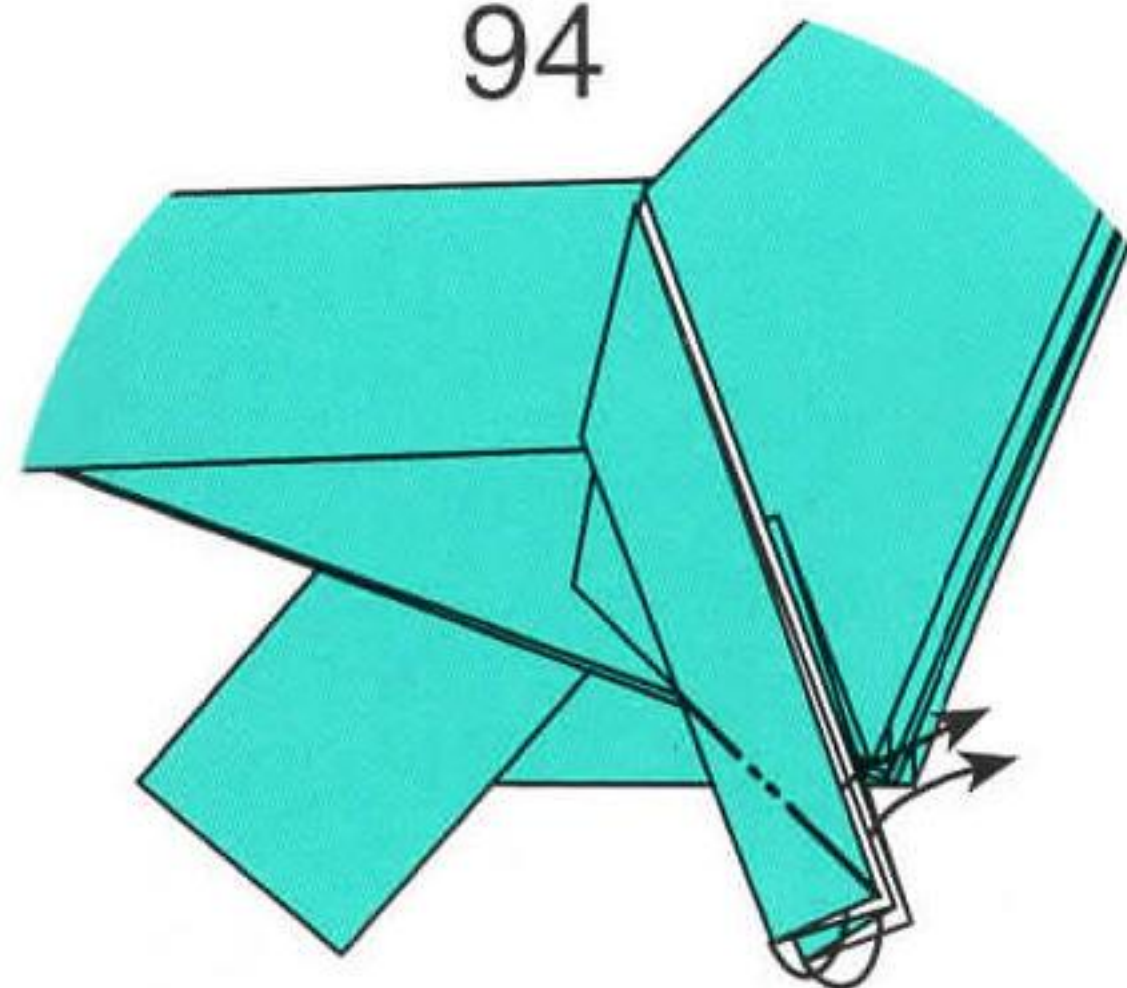


93



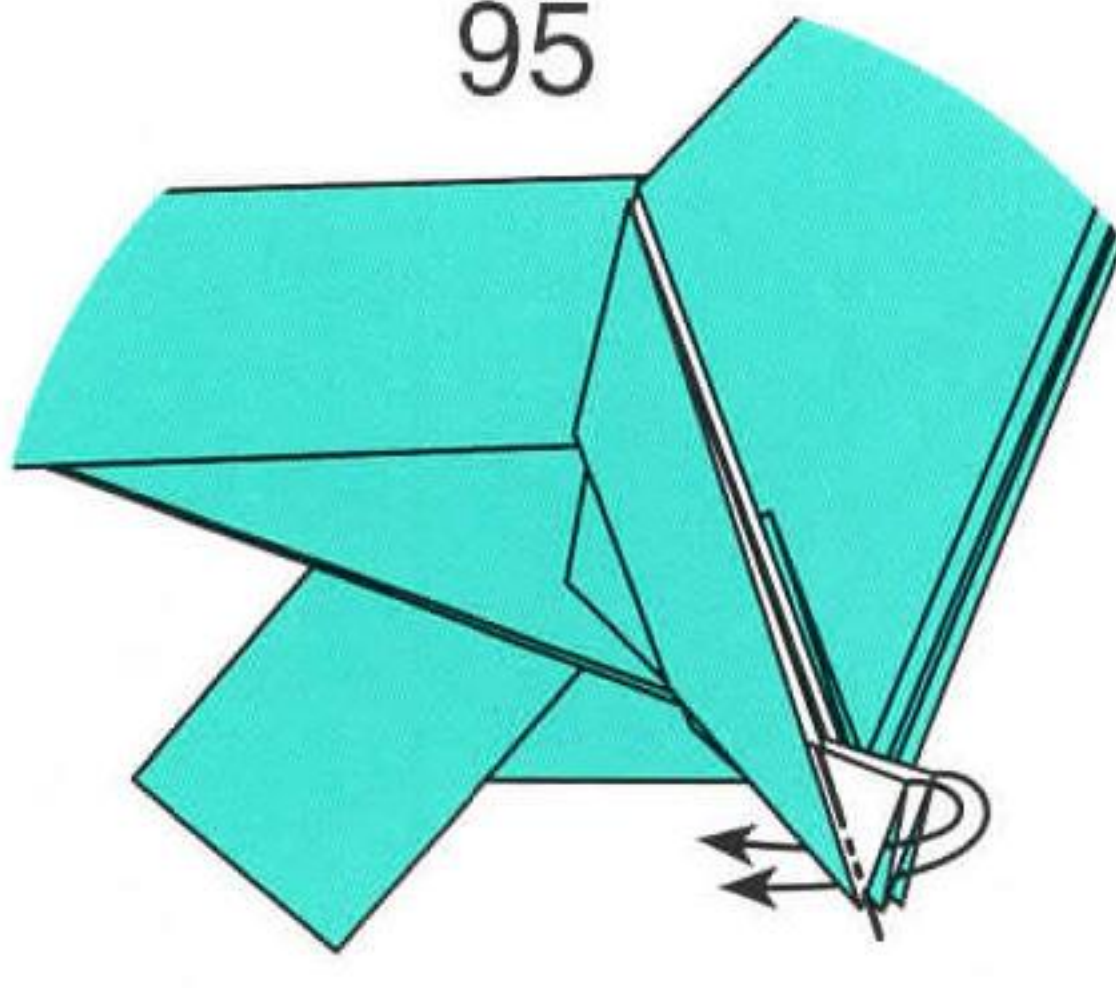
Closed-sink

94



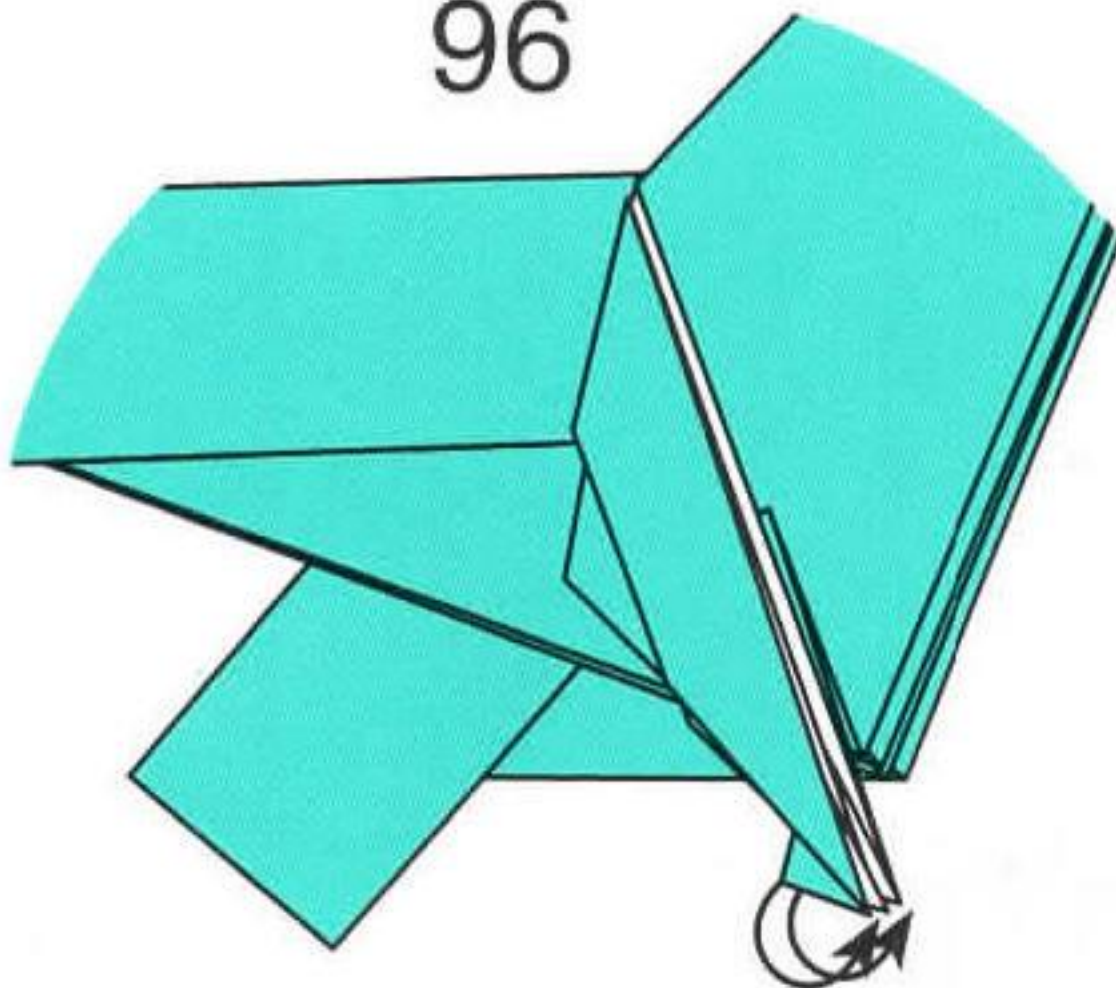
Inside reverse-fold

95



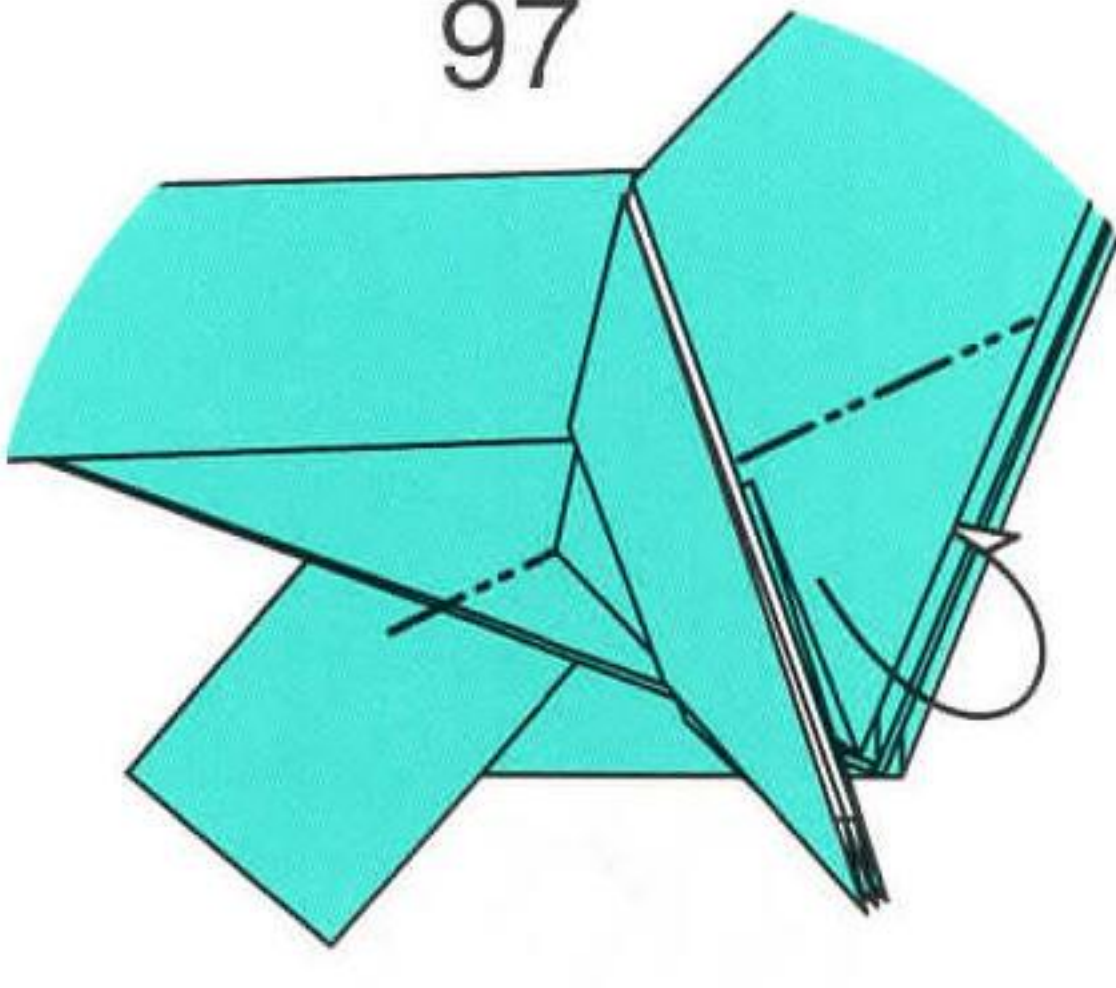
Inside reverse-fold

96



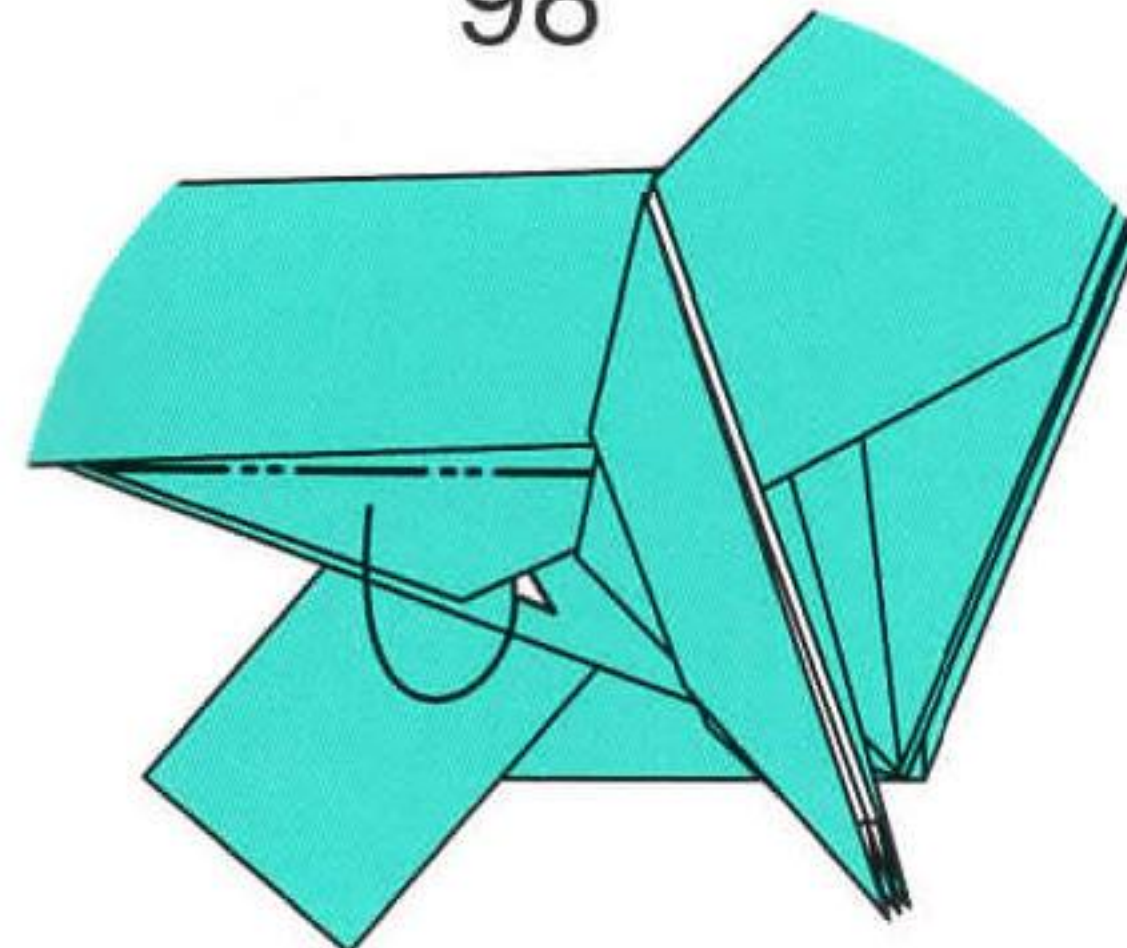
Inside reverse-fold

97

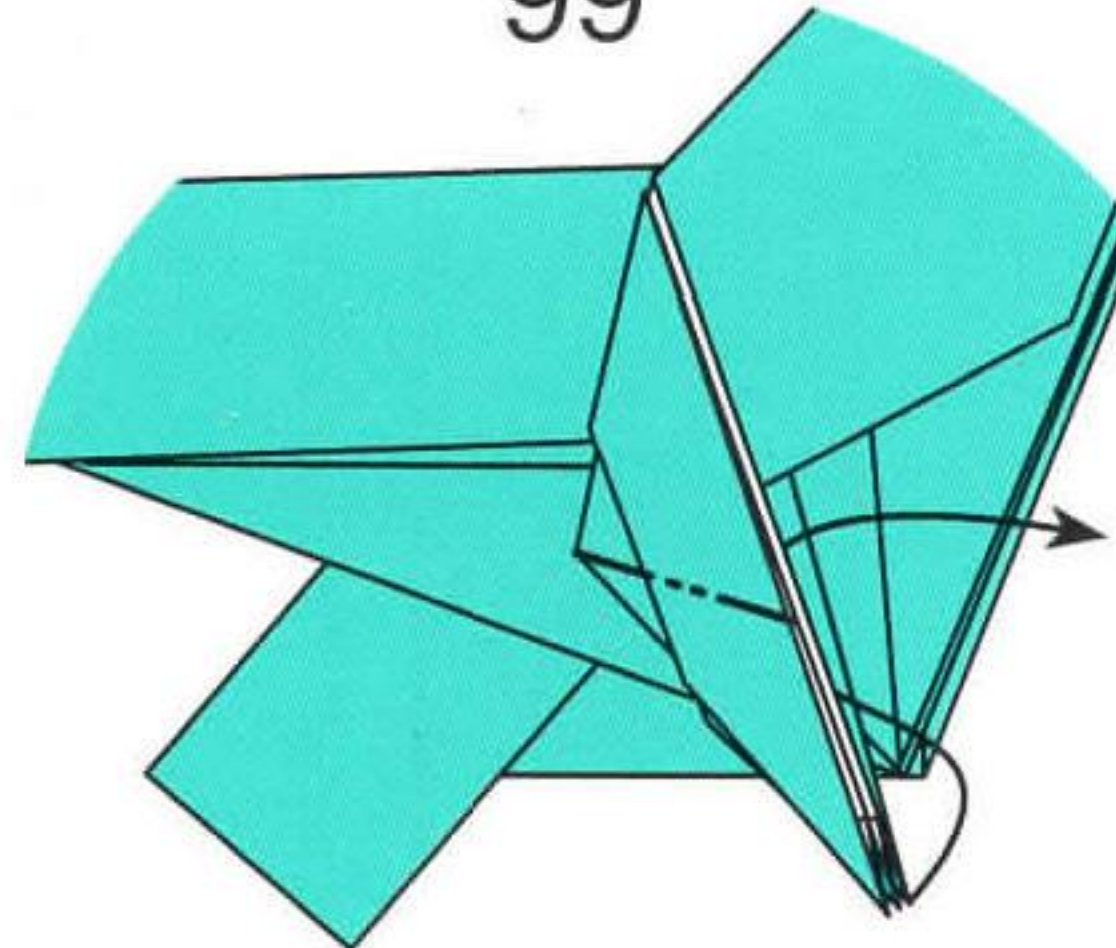


Fold the top layer only.

98

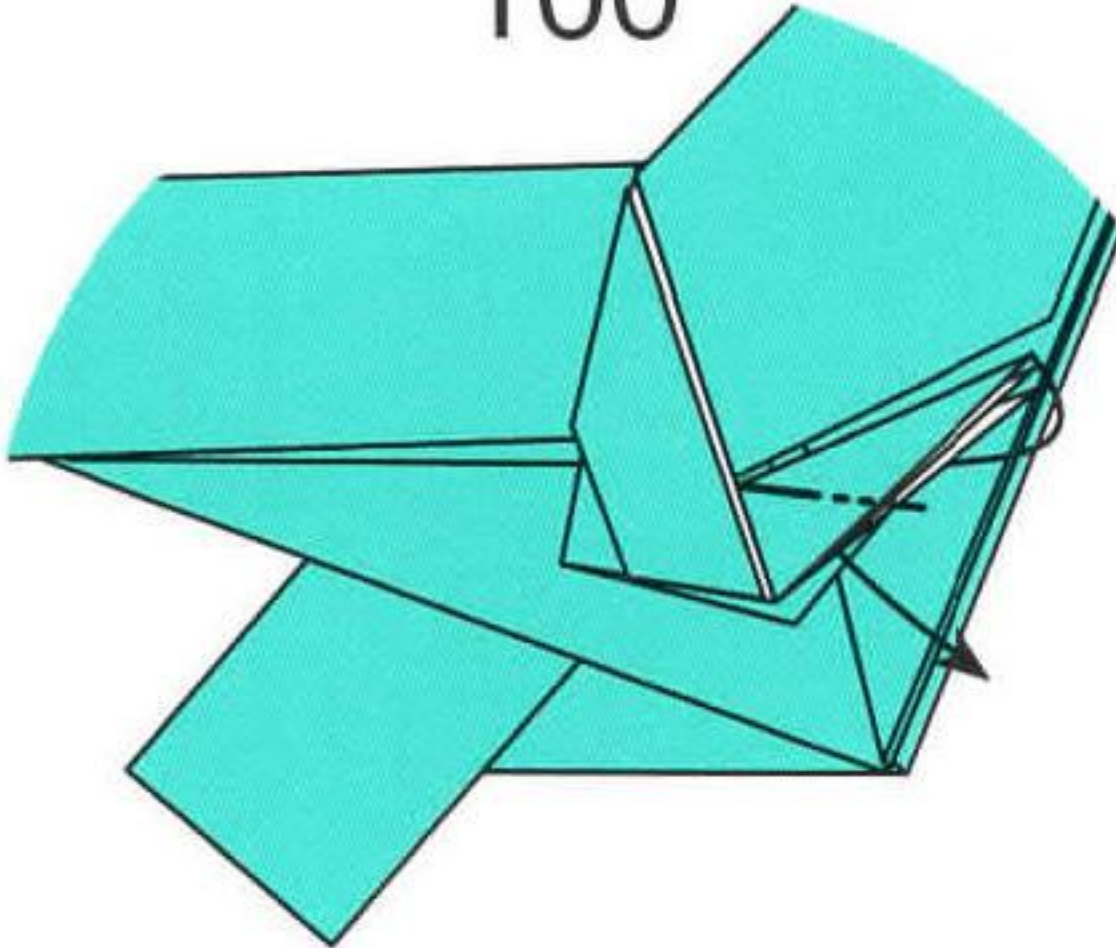


99



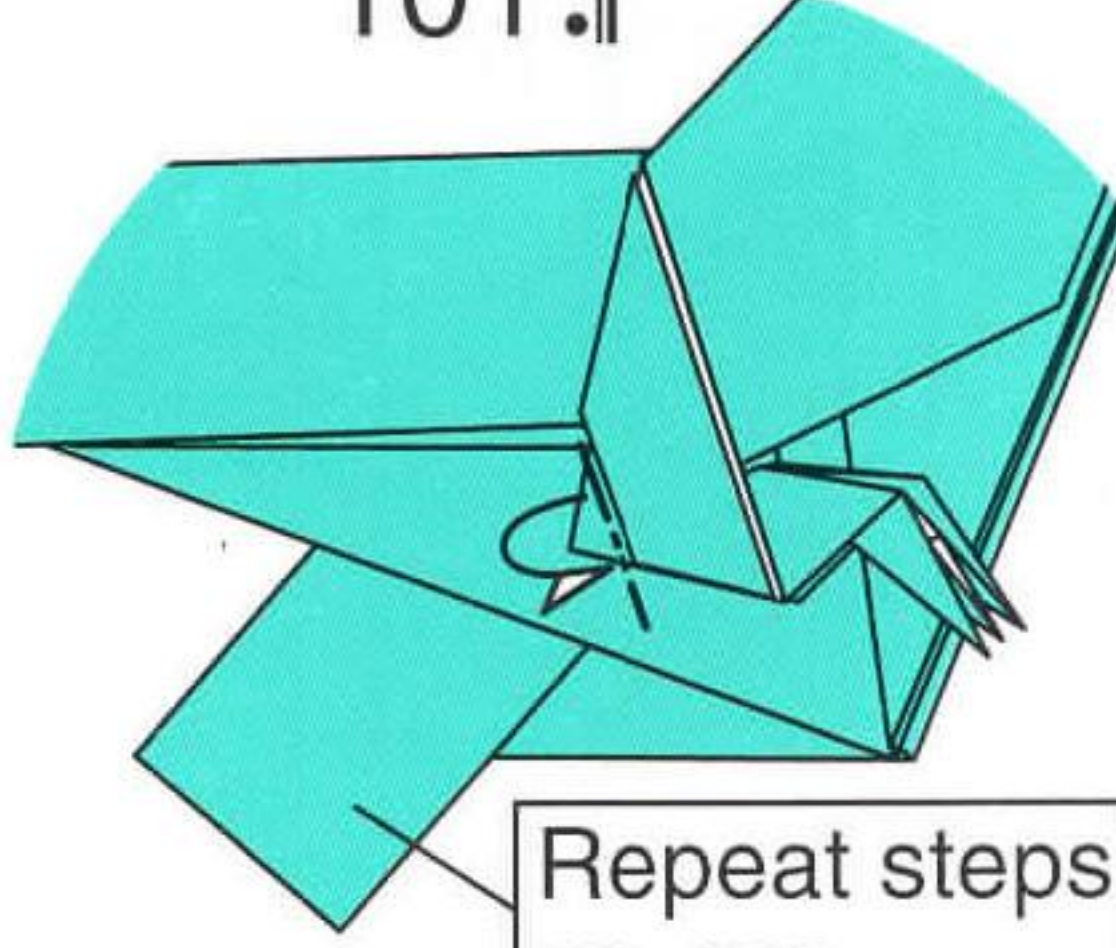
Inside reverse-fold
through the bottom gap

100

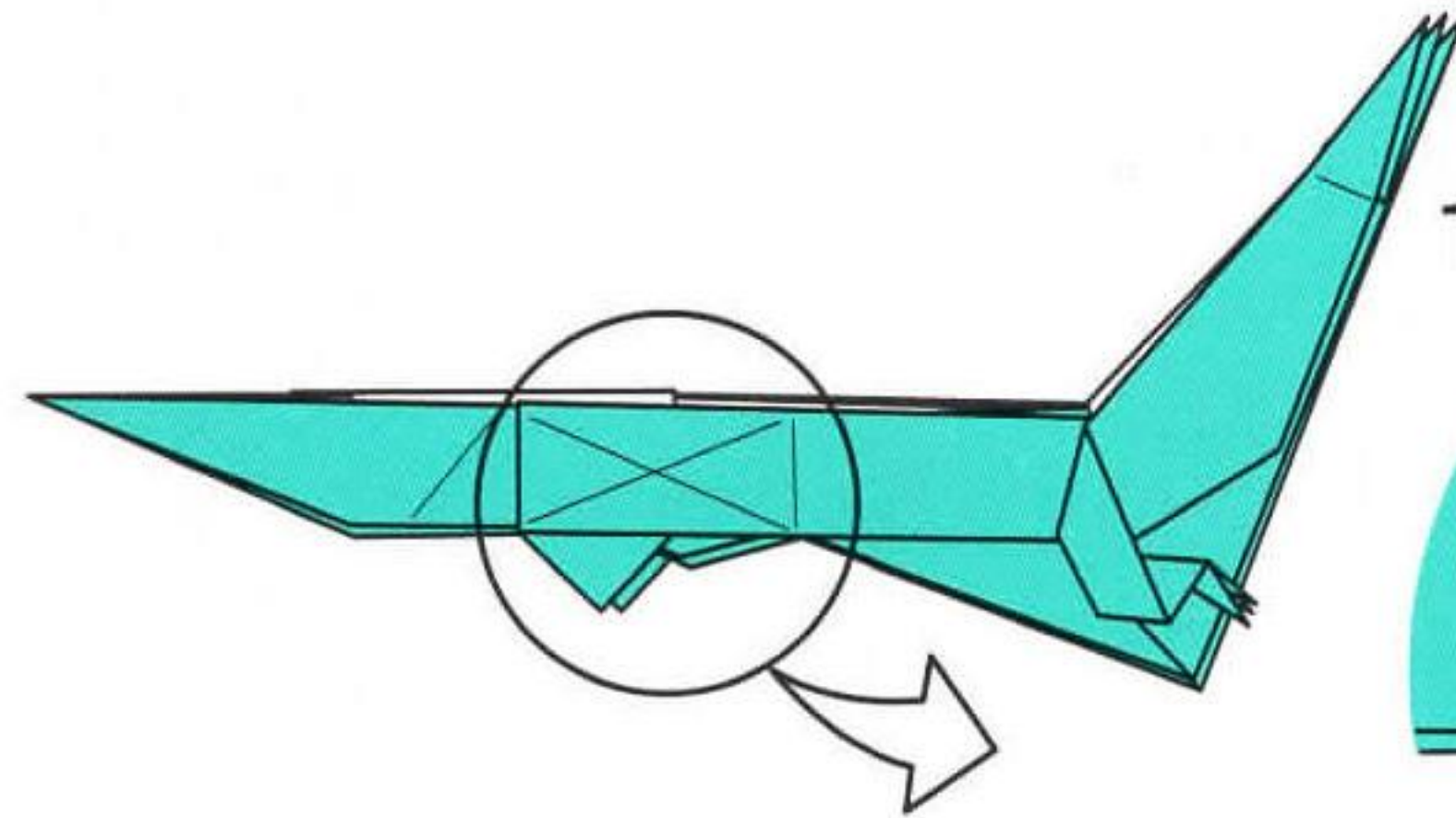


Inside reverse-fold

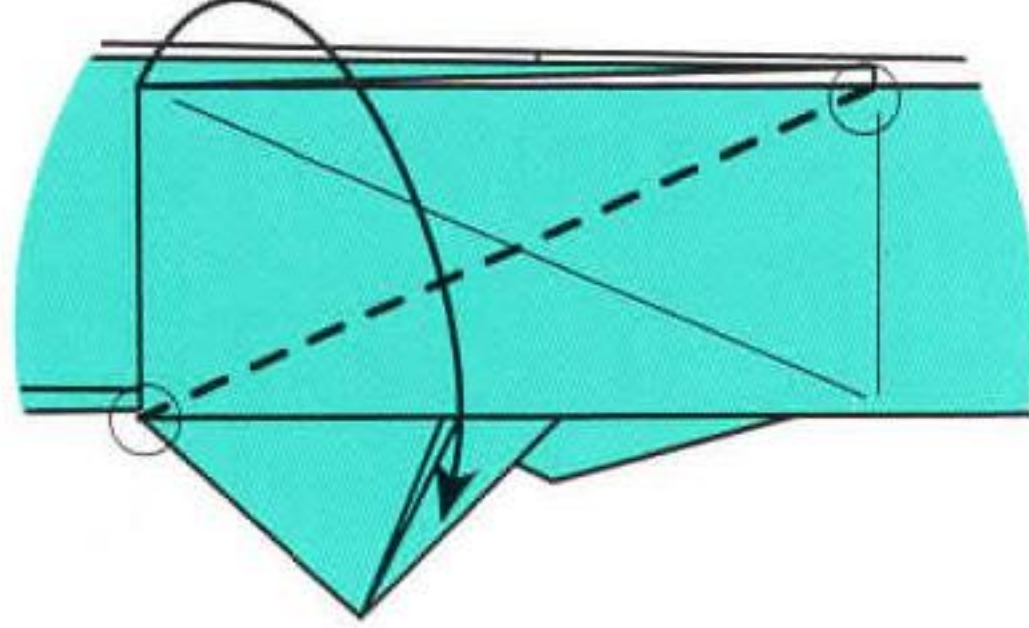
101:||



Repeat steps
88-100.



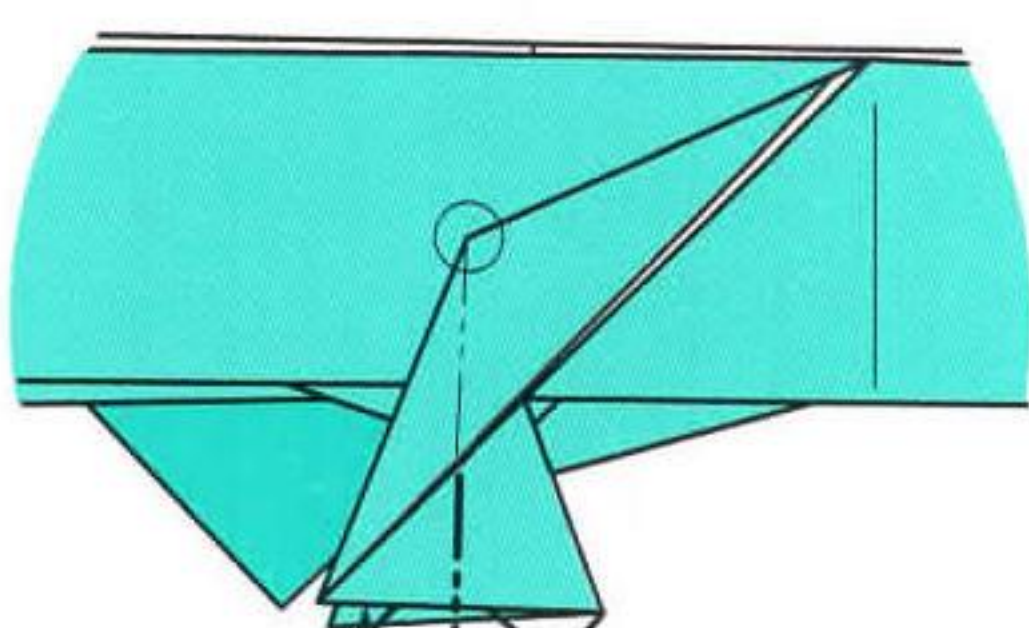
102:||



103

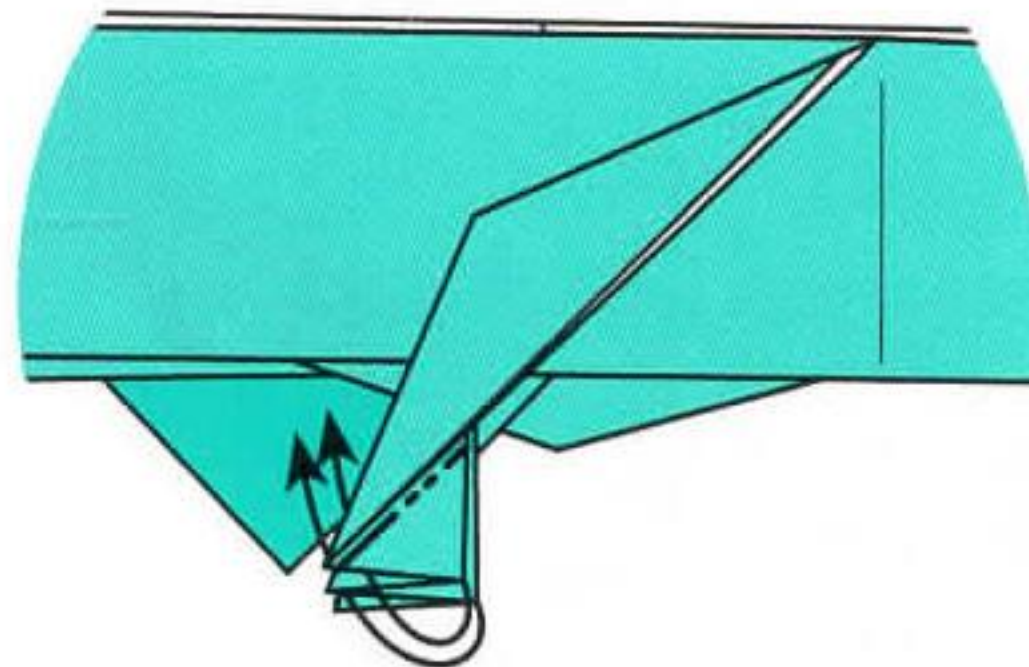
Inside reverse-fold

104



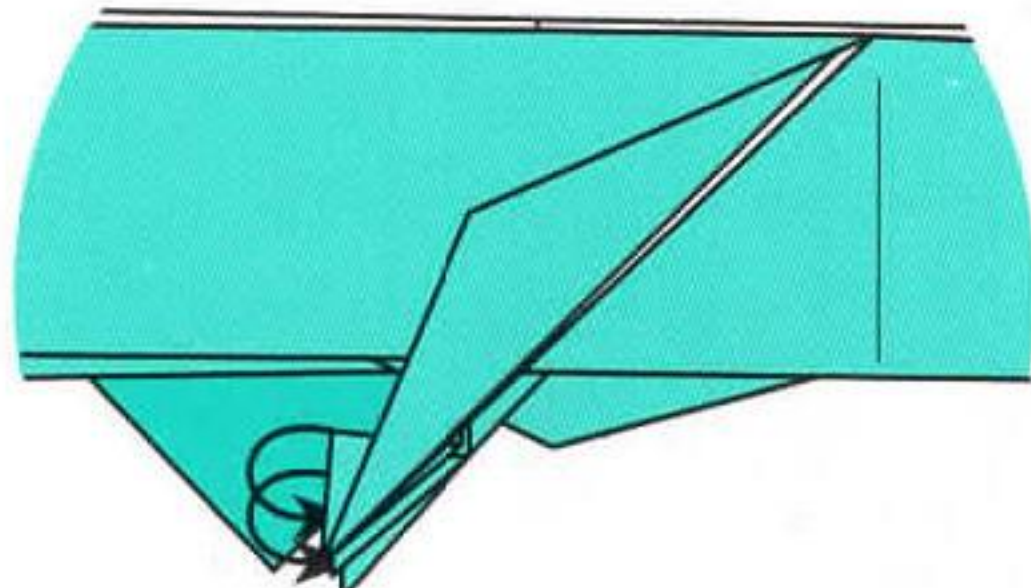
Inside reverse-fold

105



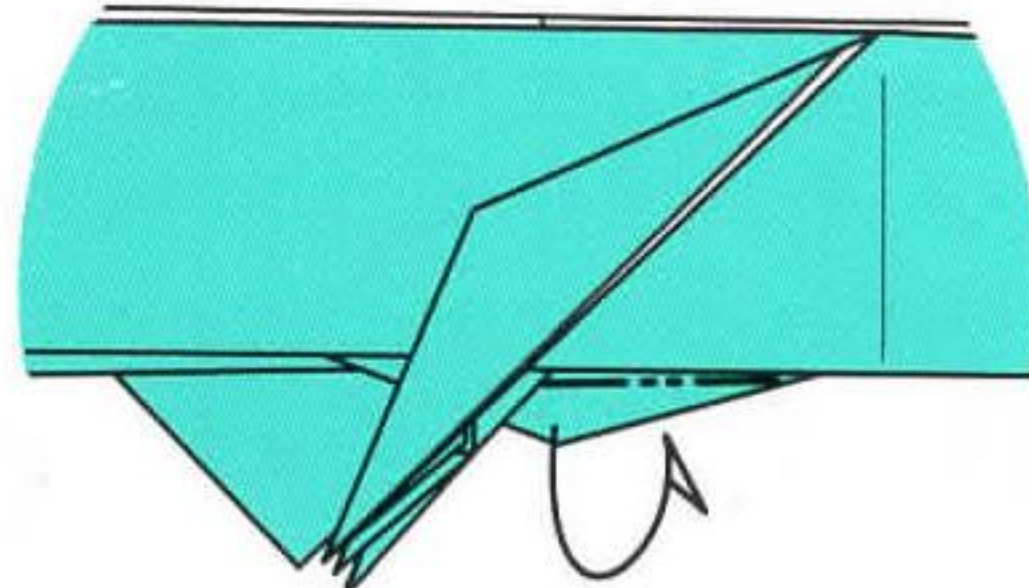
Inside reverse-fold

106

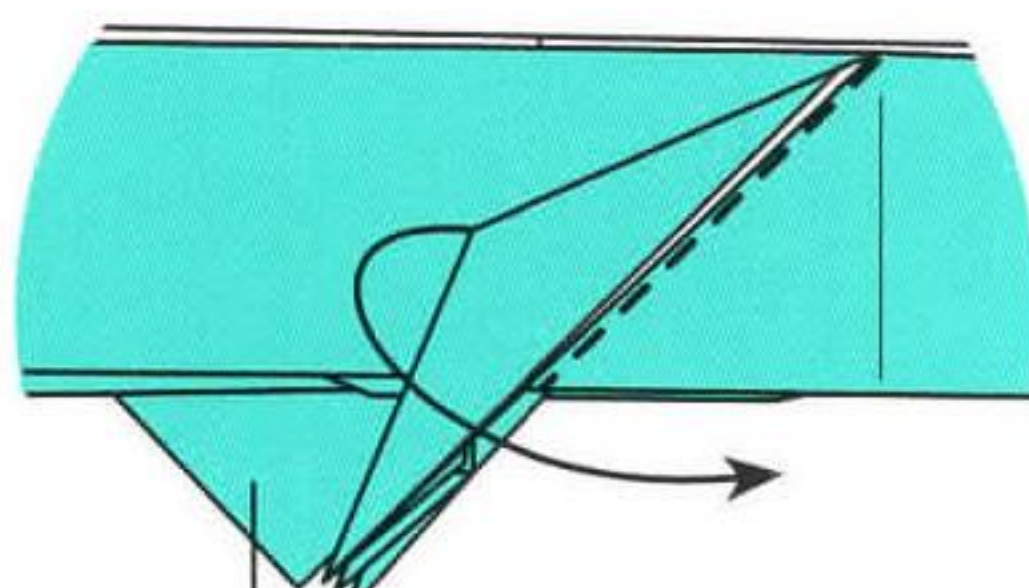


Inside reverse-fold

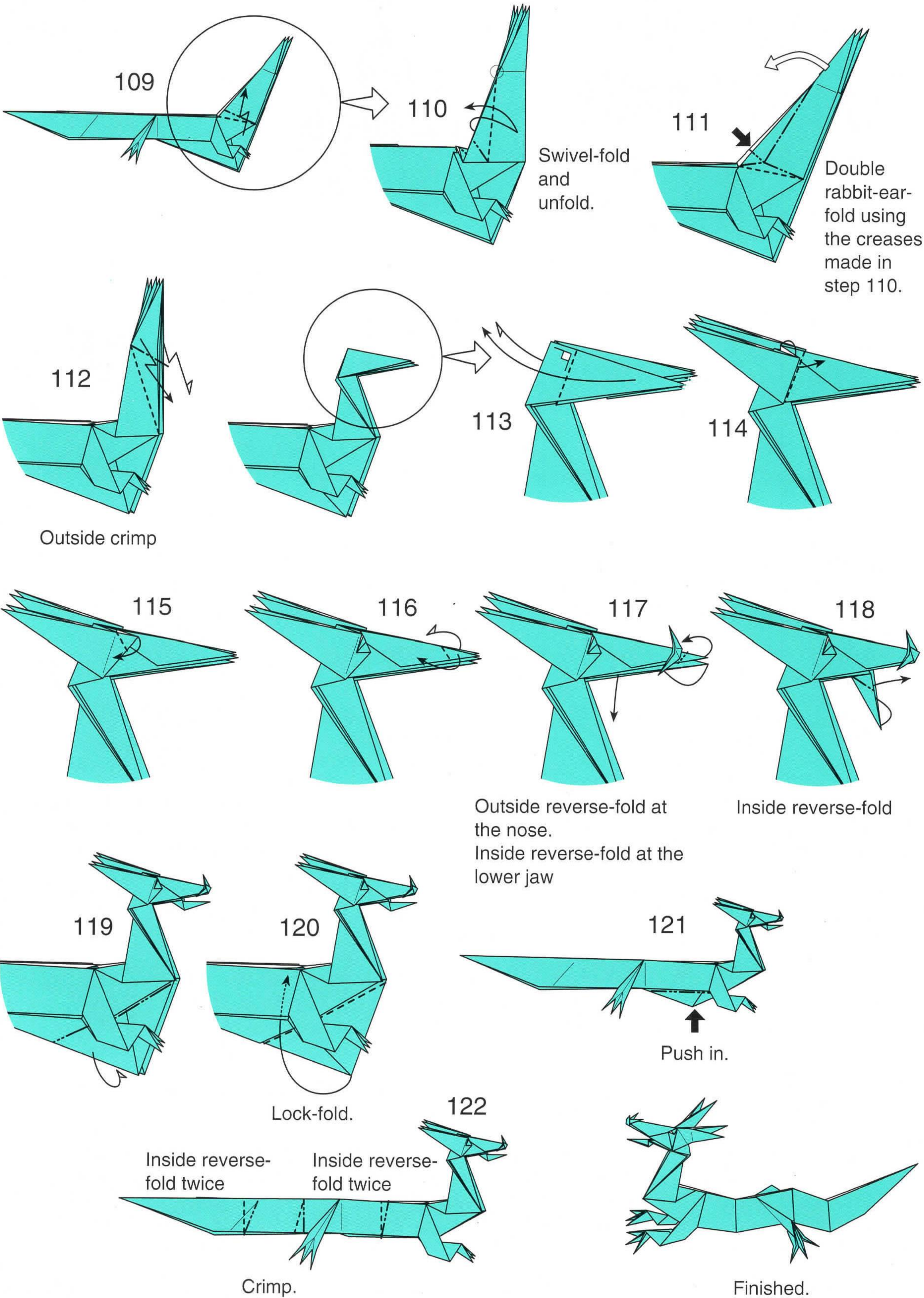
107



108:||



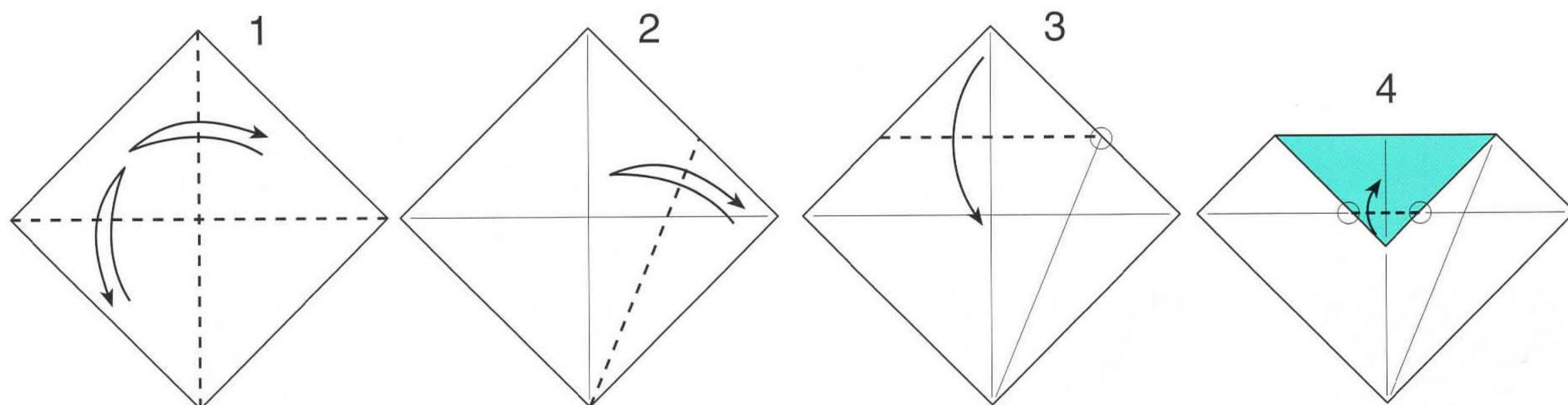
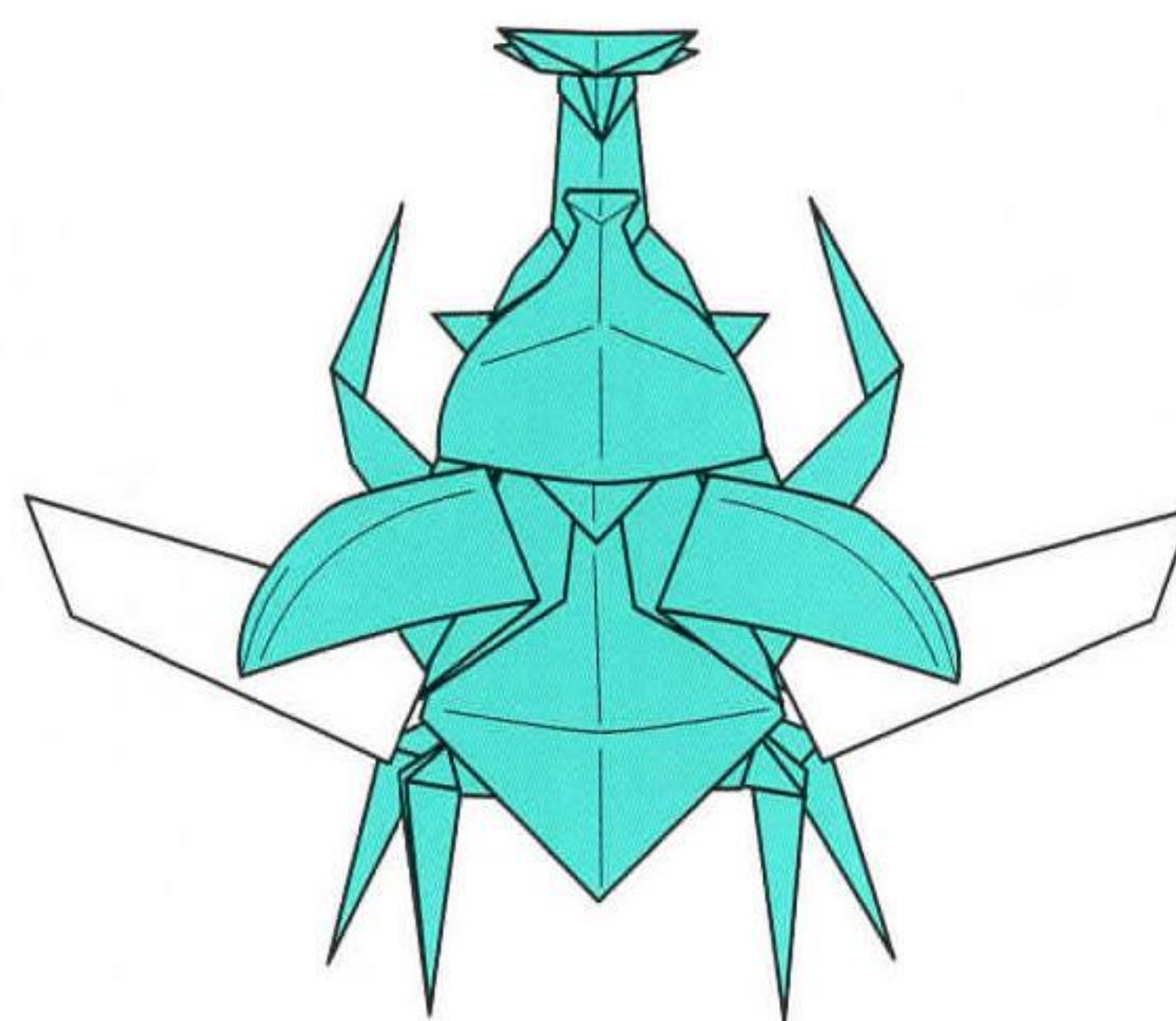
Repeat steps 102-108.



Samurai Helmet Beetle

Theme: No glue, no cuts

Difficult to fold using 6" (15 cm) origami paper. 12" (30 cm) paper is suggested.



Symbolism of the "glue"

This model is a modified version of my *Flying Samurai Helmet Beetle*, which was designed about 10 years ago for an informal competition known as the "Bug Wars." At that time I intended it as a negative Mannerism or a kind of joke, using excessive techniques, artificiality, and exaggeration. But now I think it was not a bad model at all.

In fact, the model did not require extremely thin paper to fold as long as the sheet was large enough, nor did it require glue to keep its shape. In improving the model, I paid more attention to in addition not to require glue also not to tear easily.

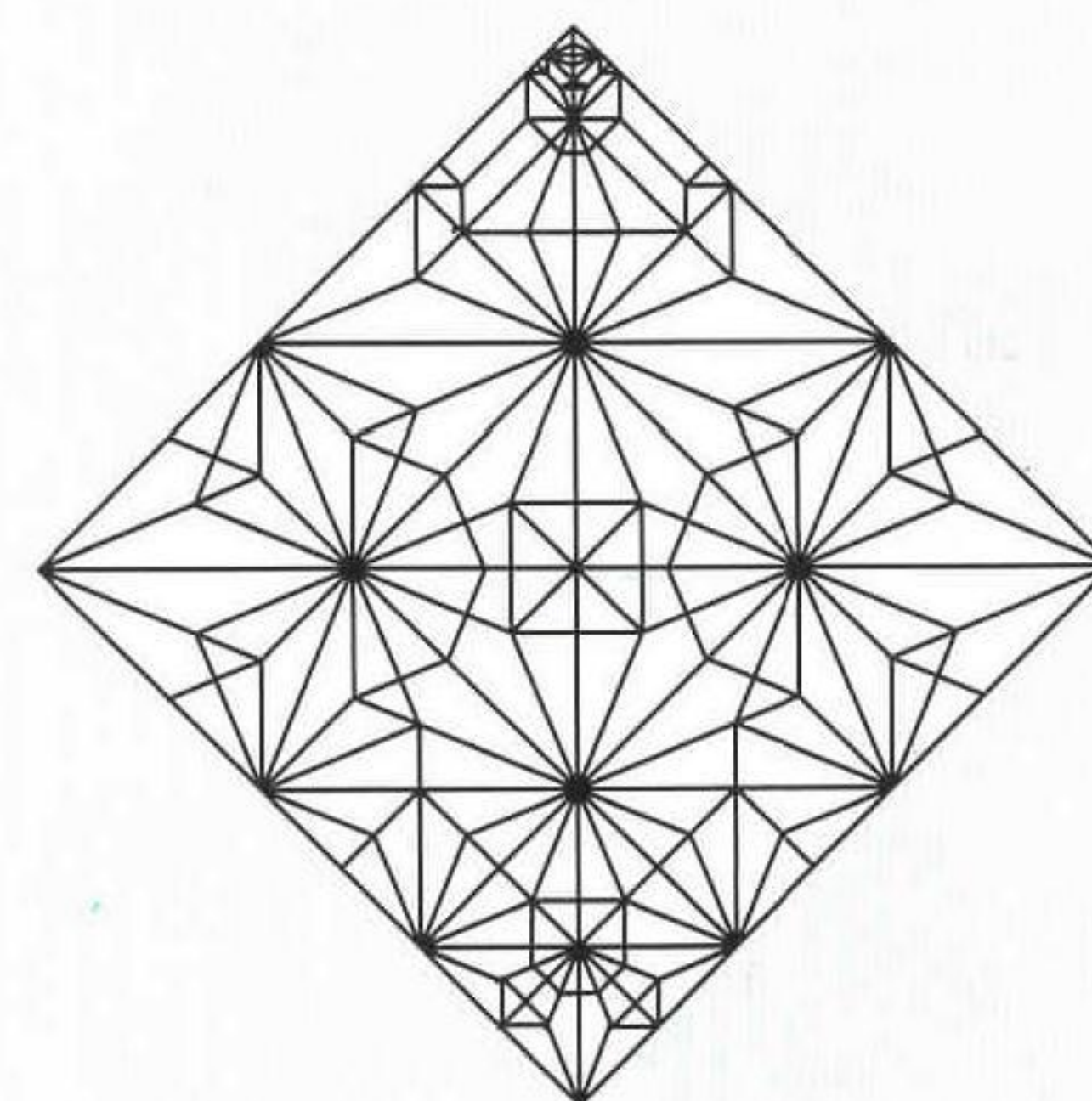
I deliberately avoid glue with the models in this book, as I used lock folds in some models.

Sometimes the selling point of an origami model is "folded without cuts or glue." Setting aside cuts, "no glue" appears to imply that the model is not folded from multiple sheets. However, requiring no glue to keep its shape is one of the ideals even for a model folded from one sheet.

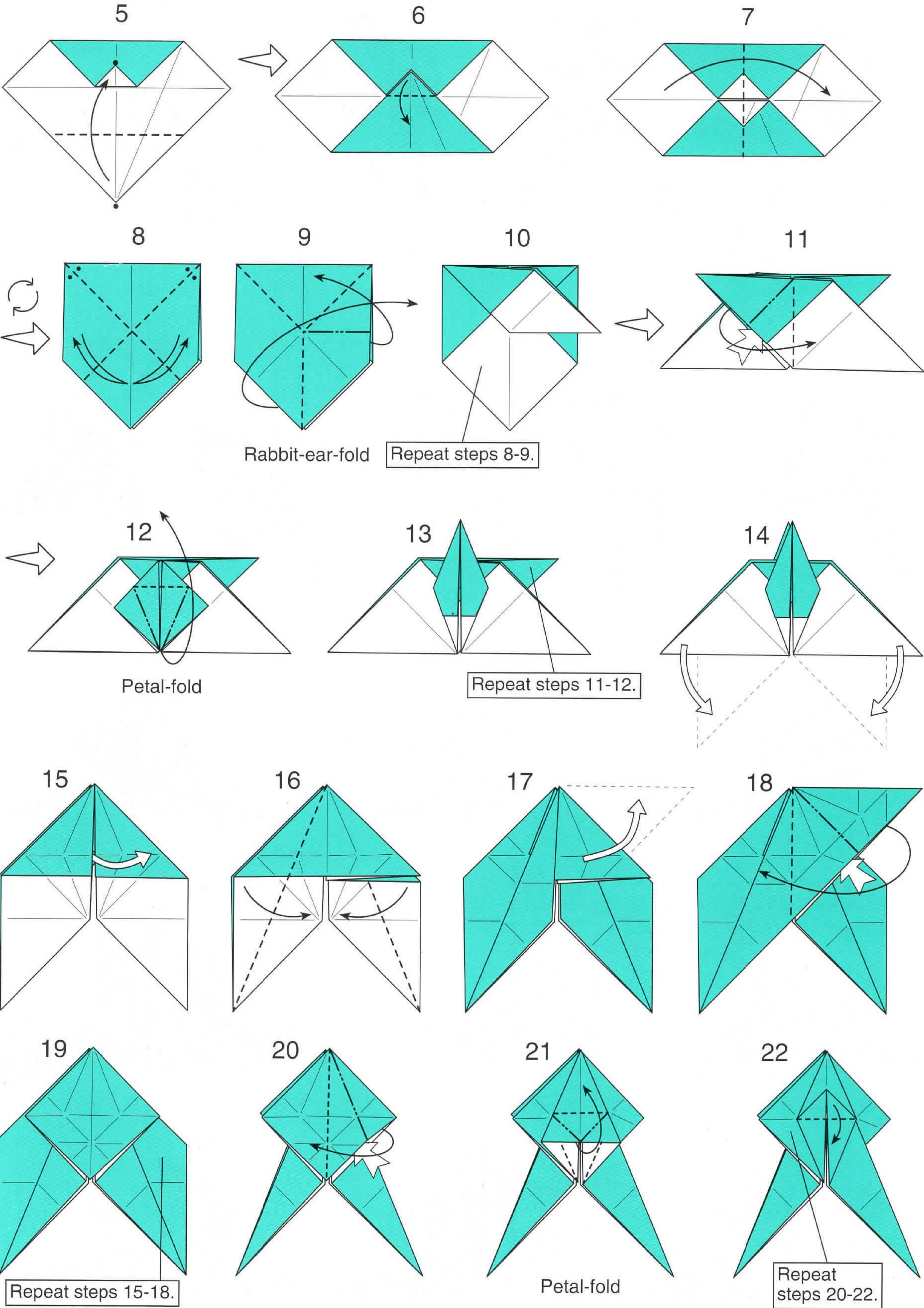
If you do not use glue, you can unfold a finished model completely to show that it is folded from a single sheet. That may seem to be an unnatural reasoning. But the fact that the origami model can be restored anytime to a plain sheet symbolizes "openness" of the wonder of how it was made, which is one of the fascination in origami.

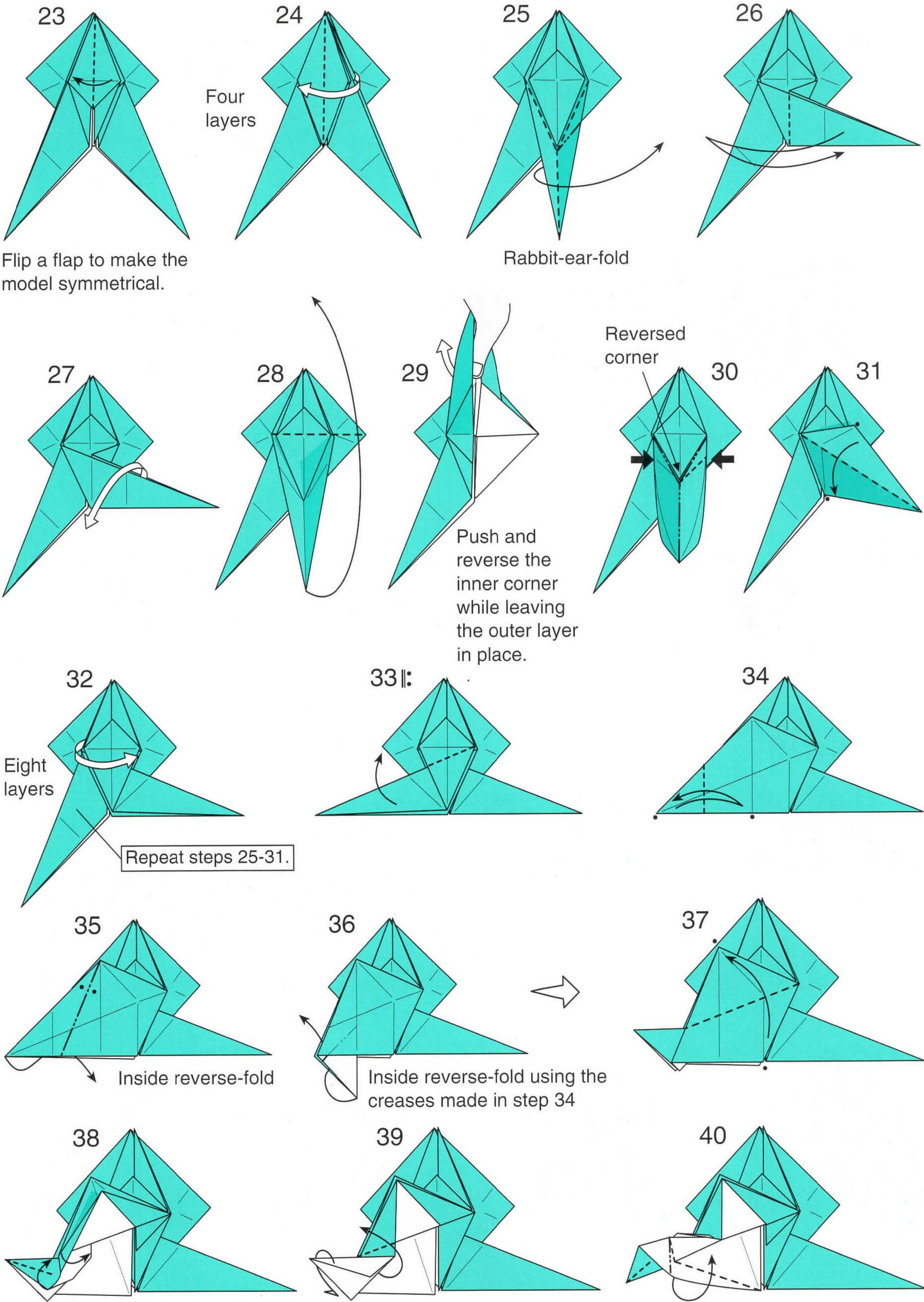
Moreover, creases on paper have a natural tendency to unfold. "No glue" means try to keep creases just by folding. It also symbolizes the recognition of the physical nature of the paper.

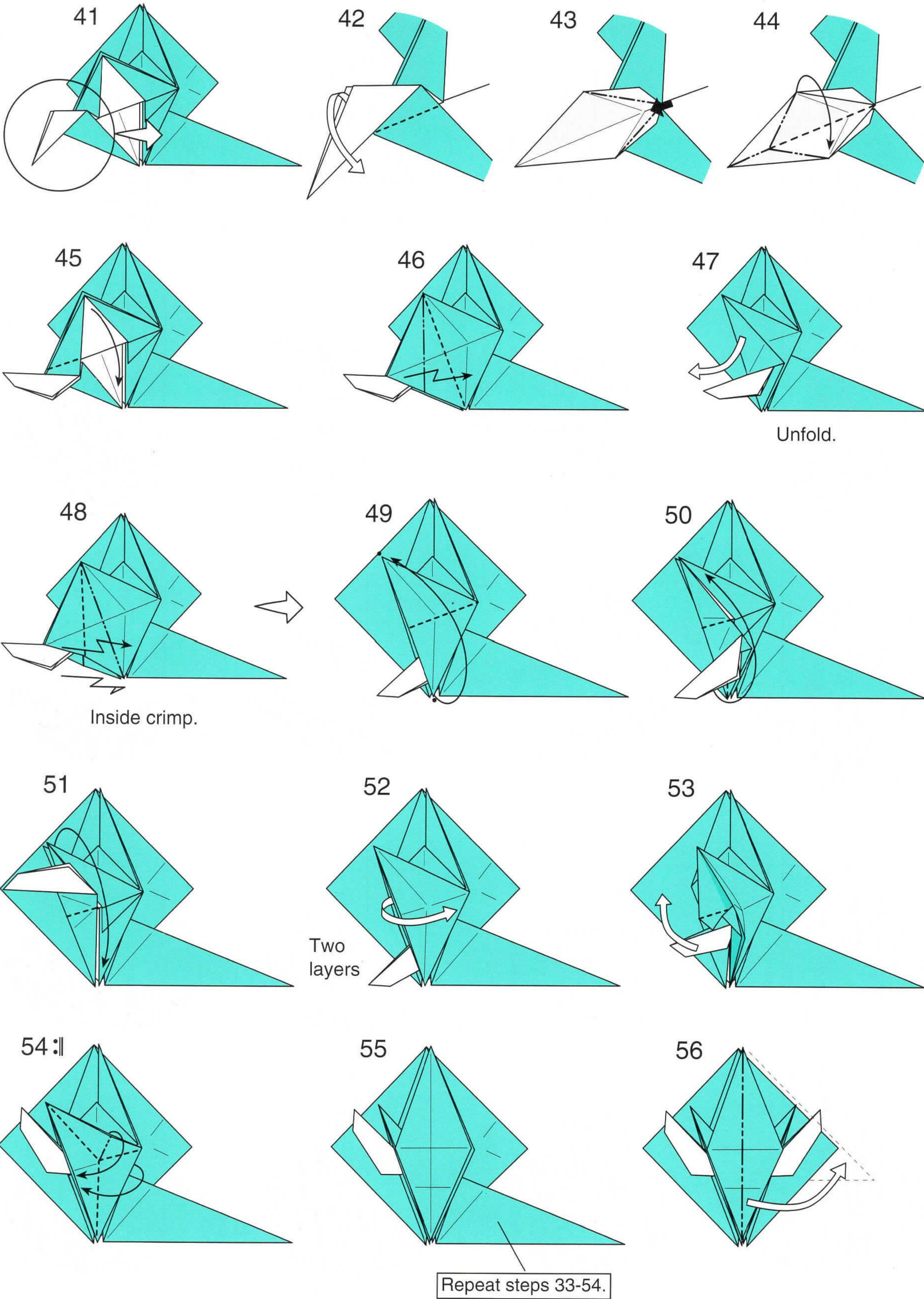
However, using glue does not always compromise origami designs. What is important is that the design centers on the "folded shape" or "bended surfaces emerged from a plane". Speaking of bended surfaces, when we design an origami model according to the composition of points, as in this *Samurai Helmet Beetle*, most of the surfaces are folded inside and hidden from the outline of the model. Therefore, one can say that the point of such model is in its folding, or unfolding, sequence rather than the finished shape.

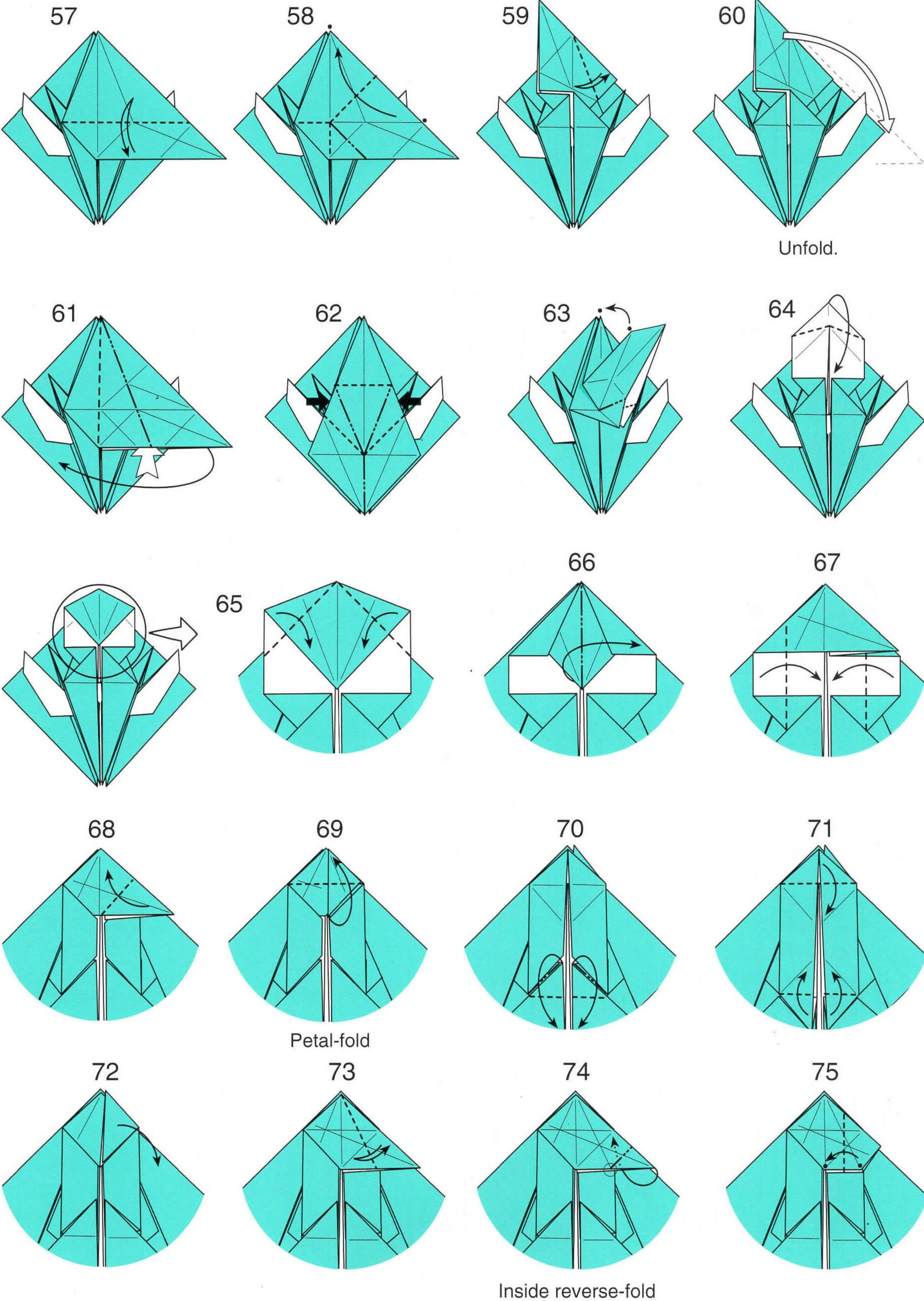


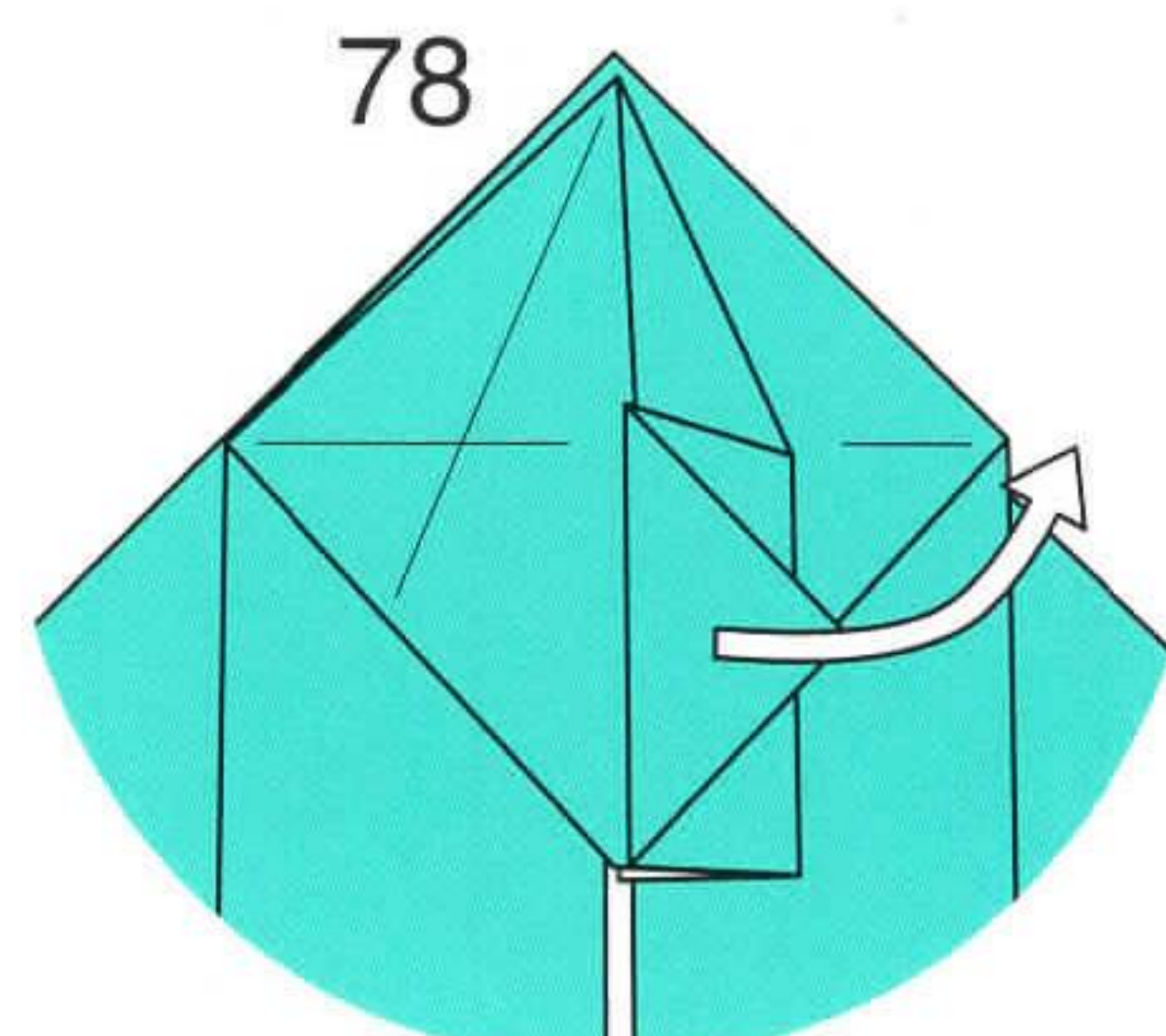
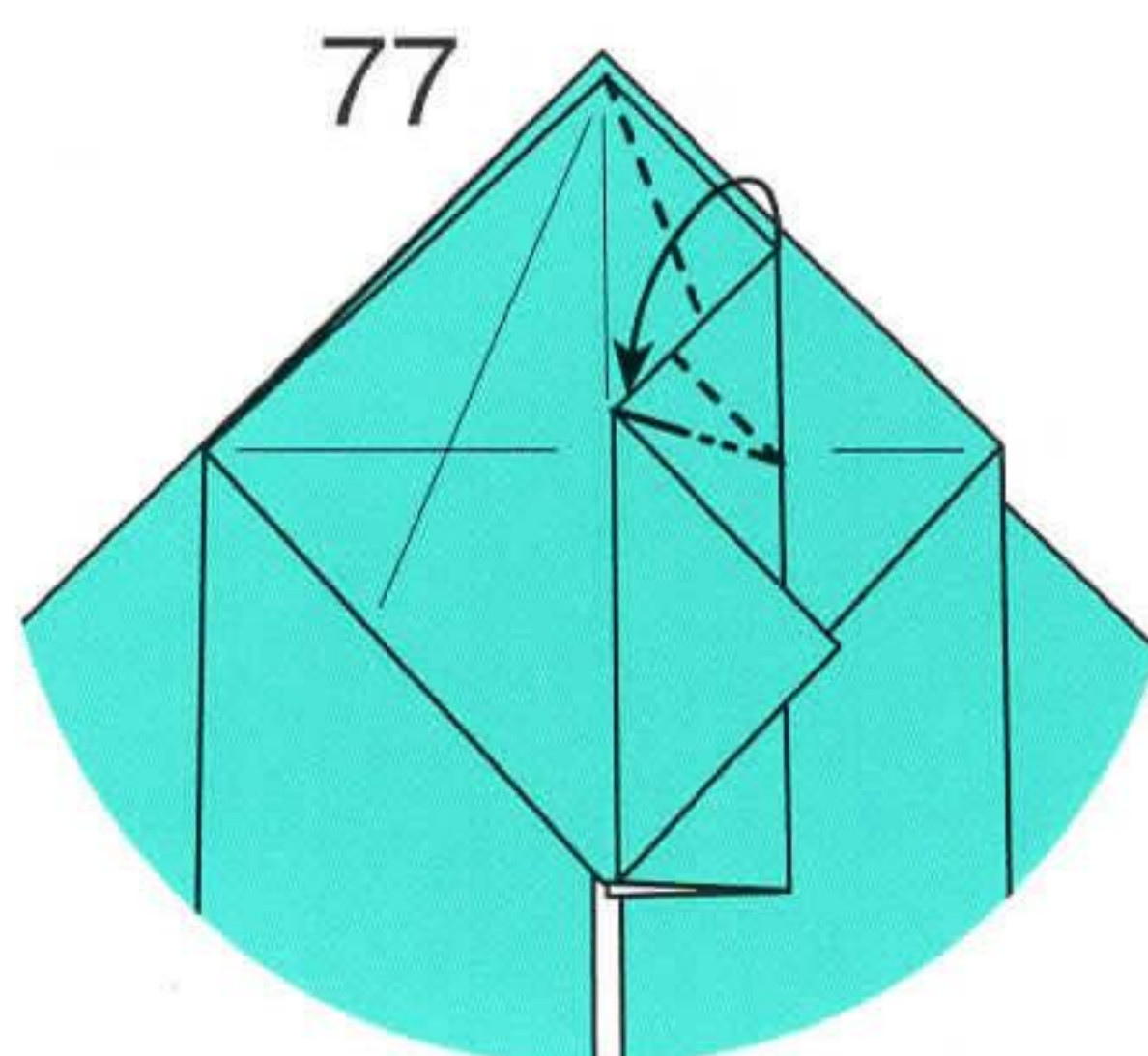
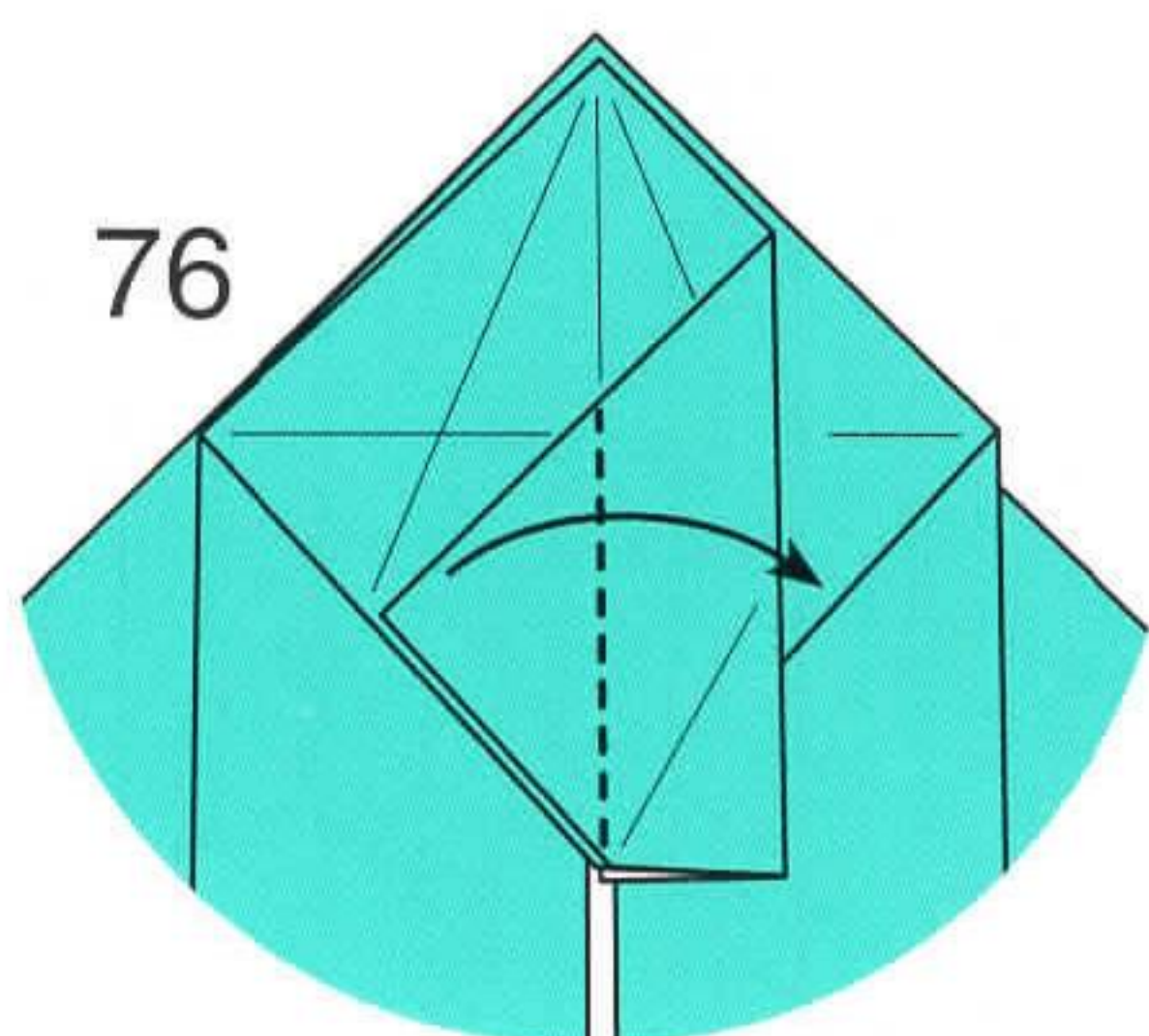
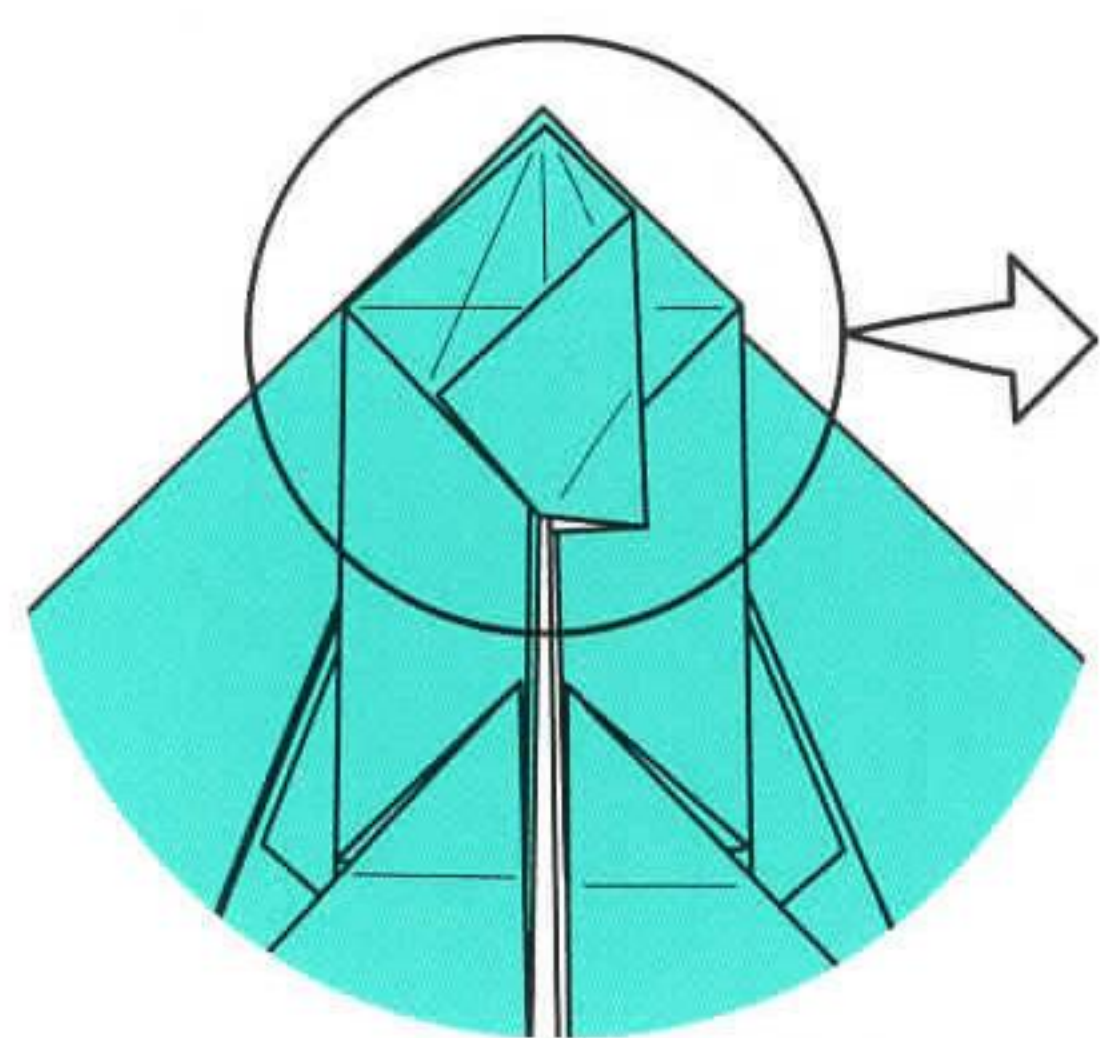
The crease pattern of Samurai Helmet Beetle (mountain and valley folds are not shown).



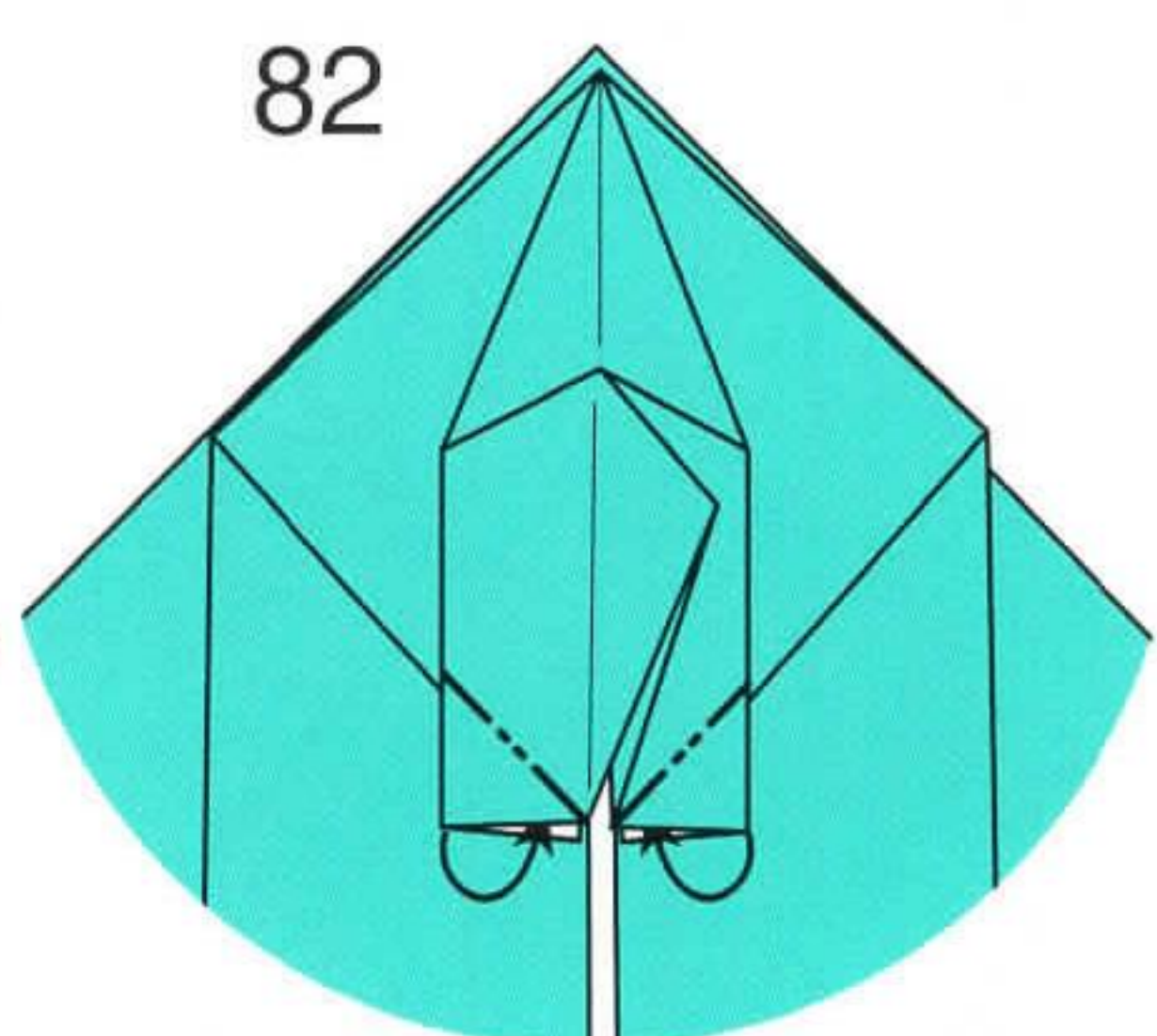
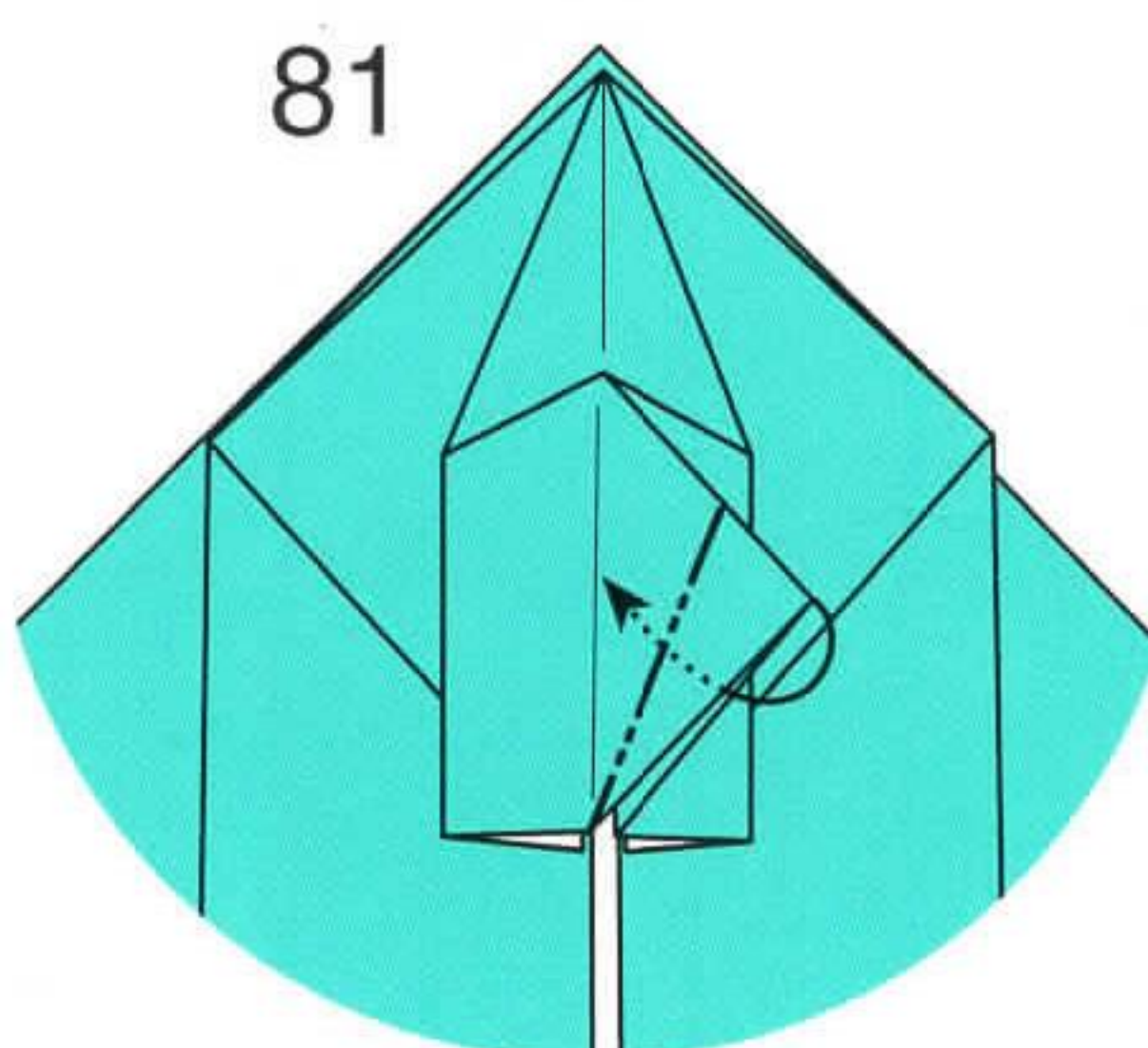
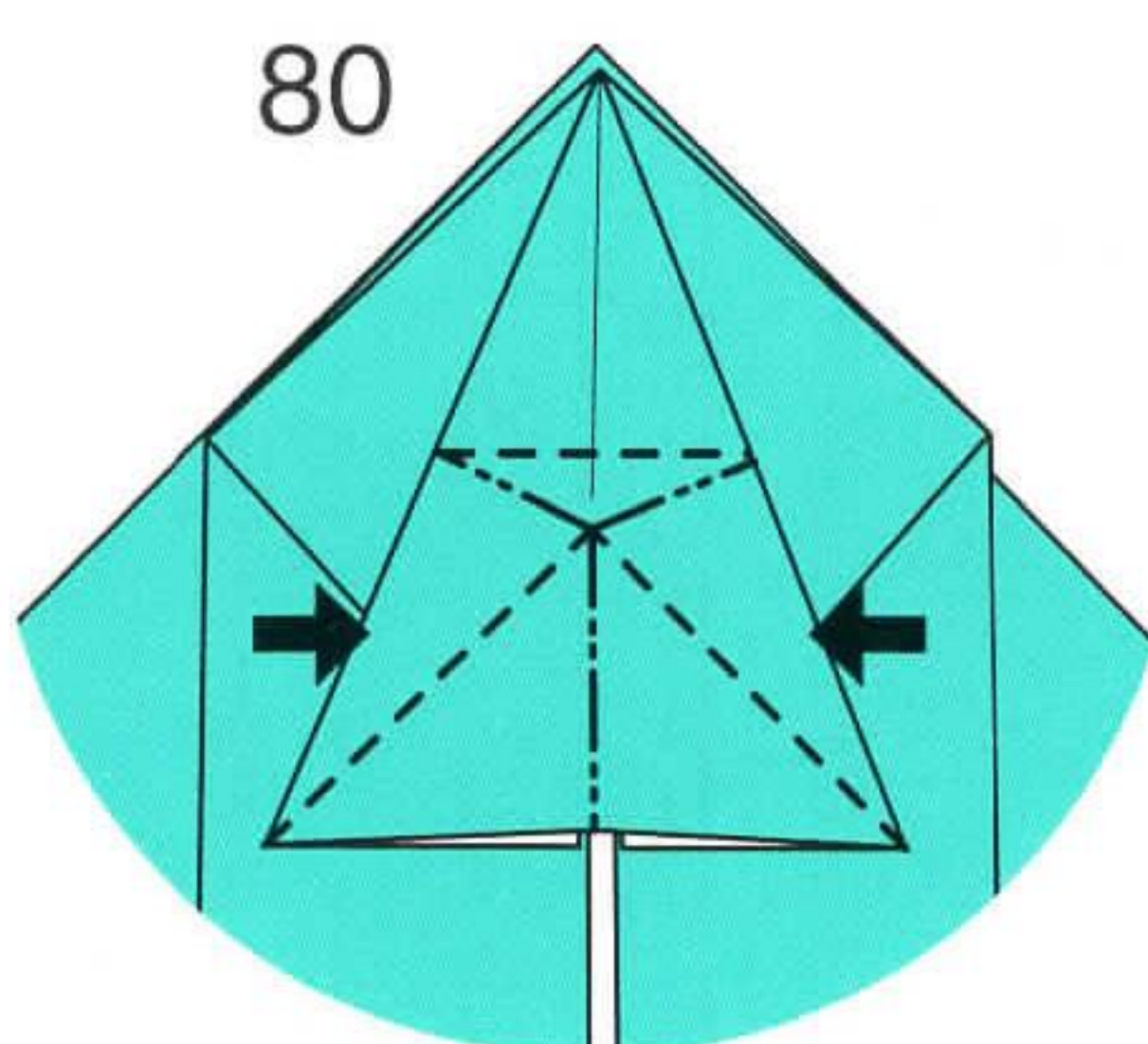
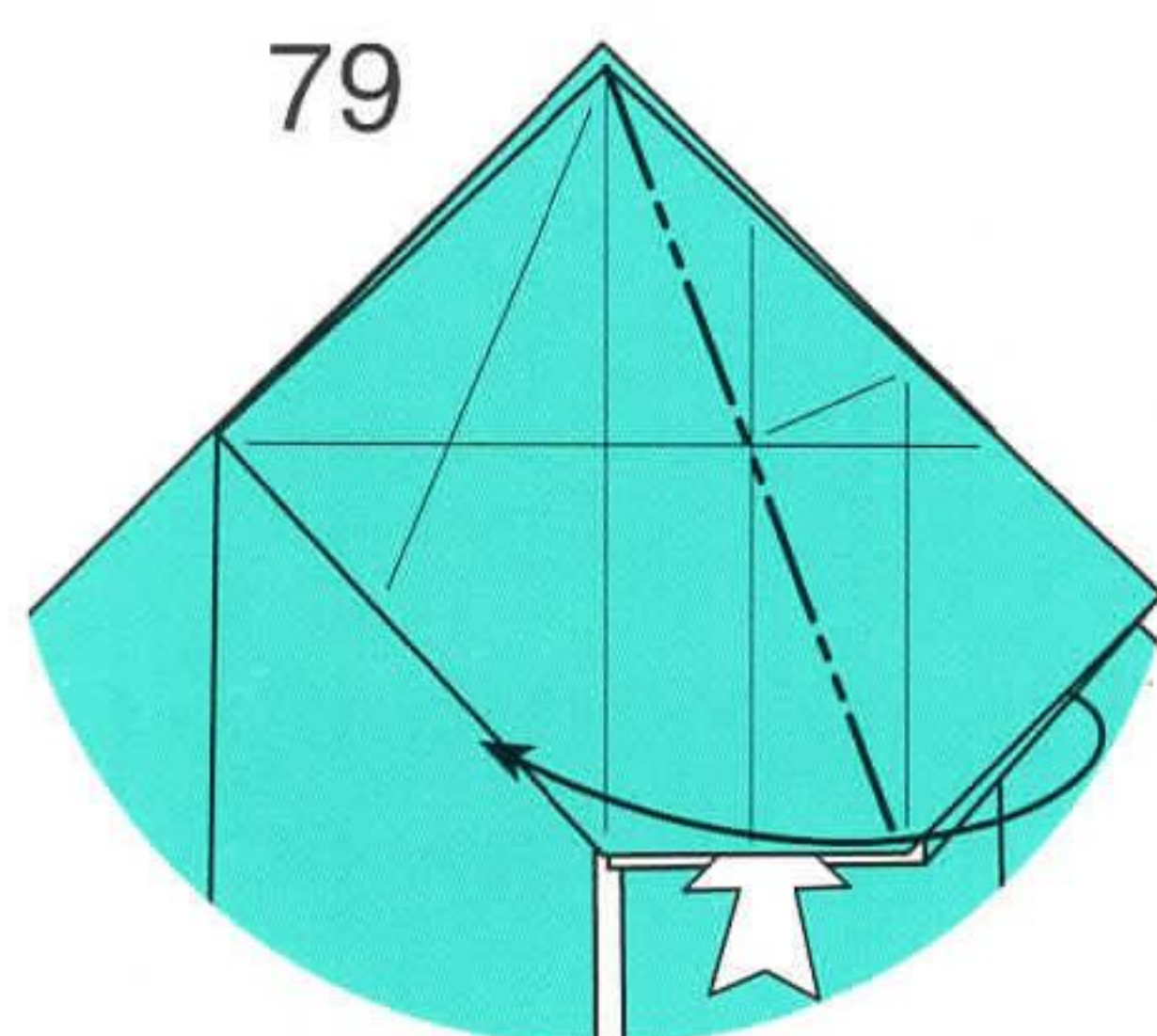






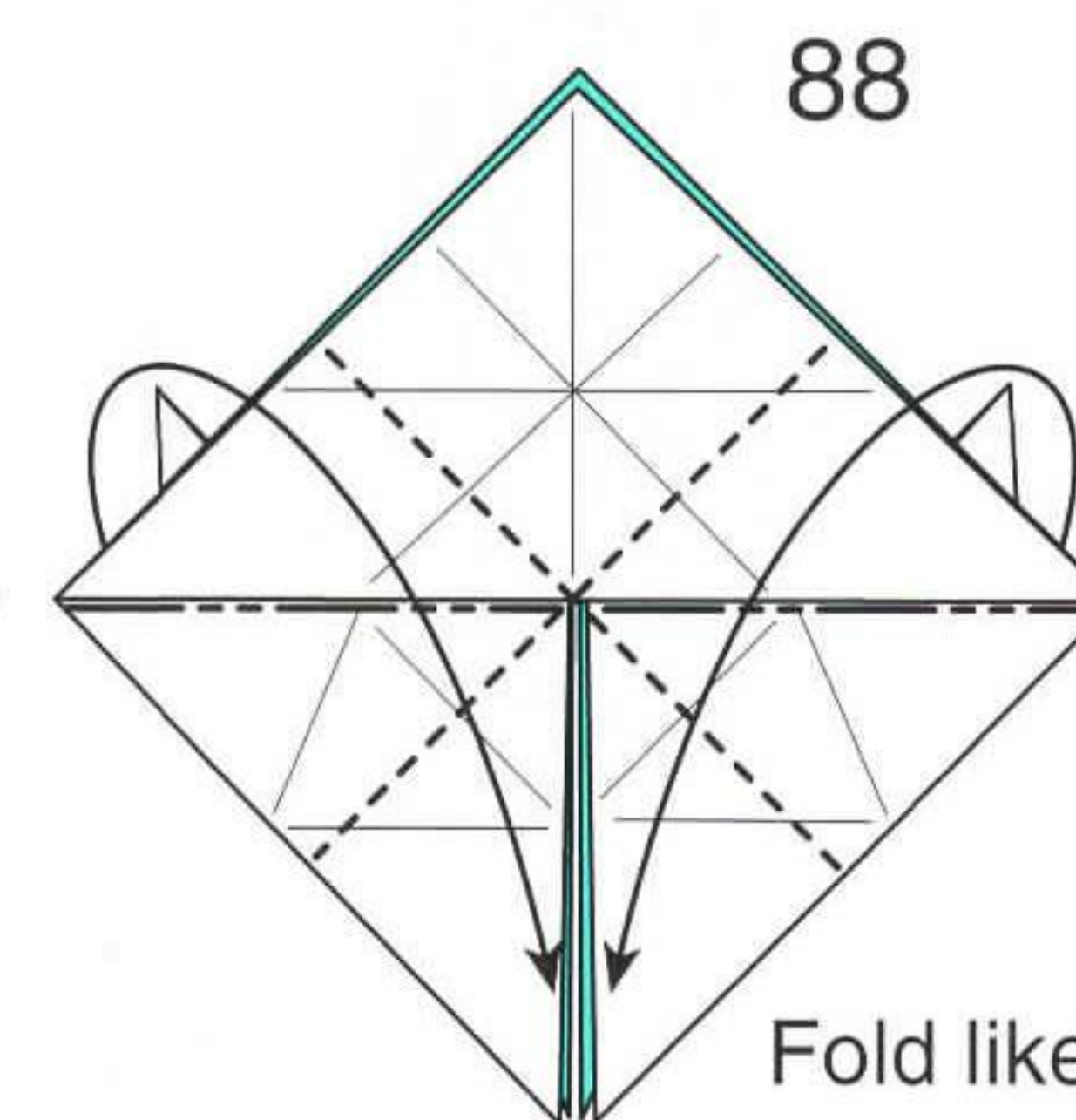
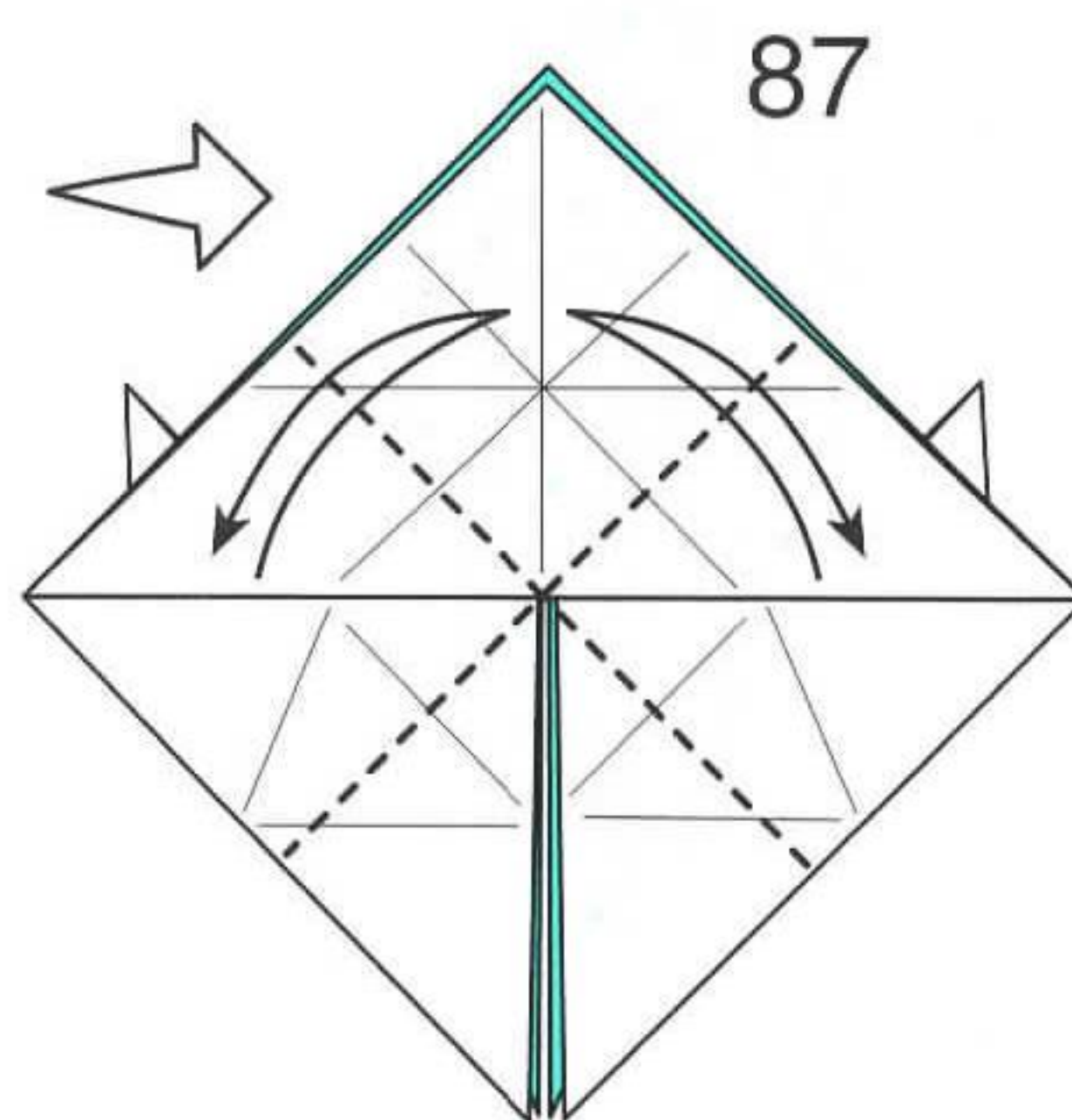
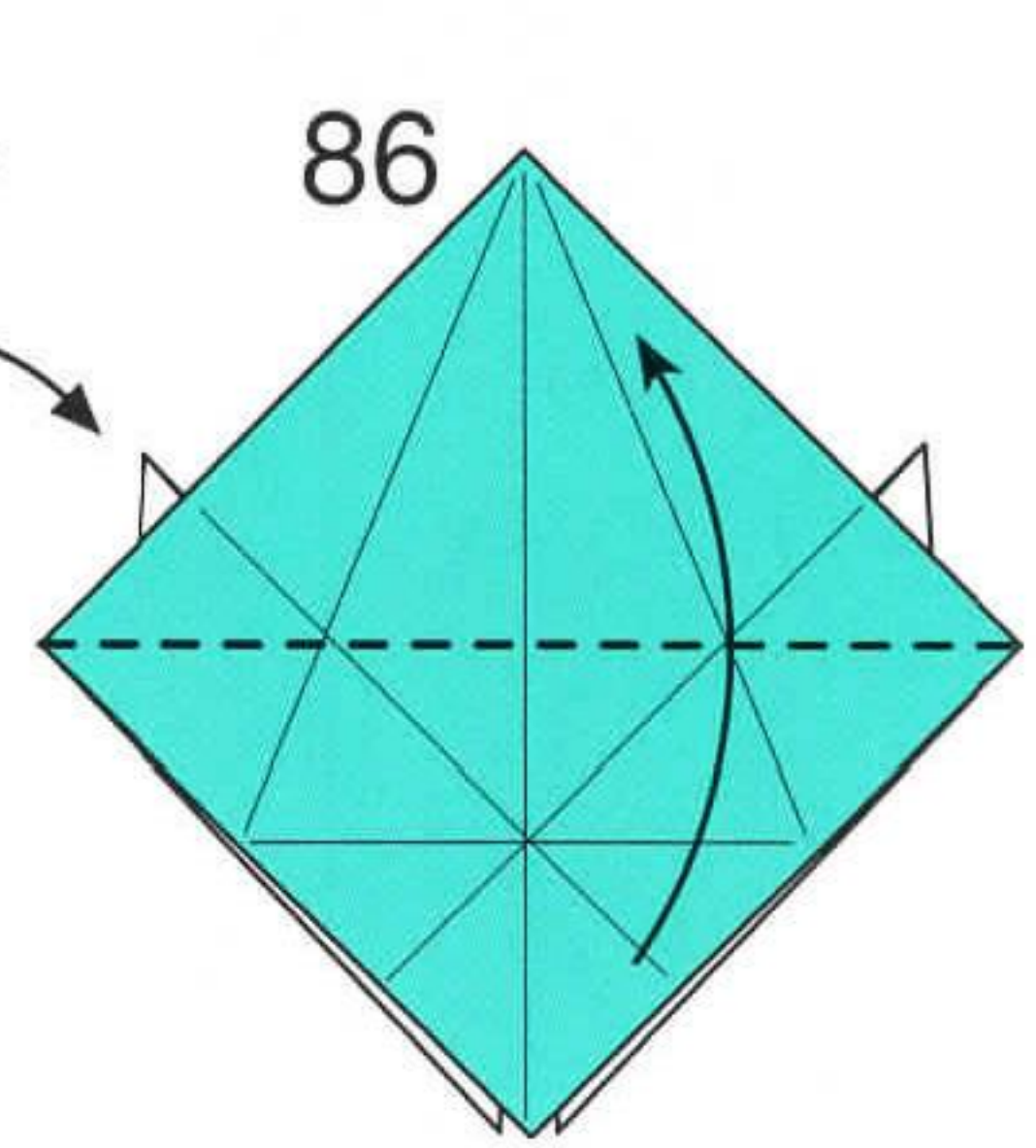
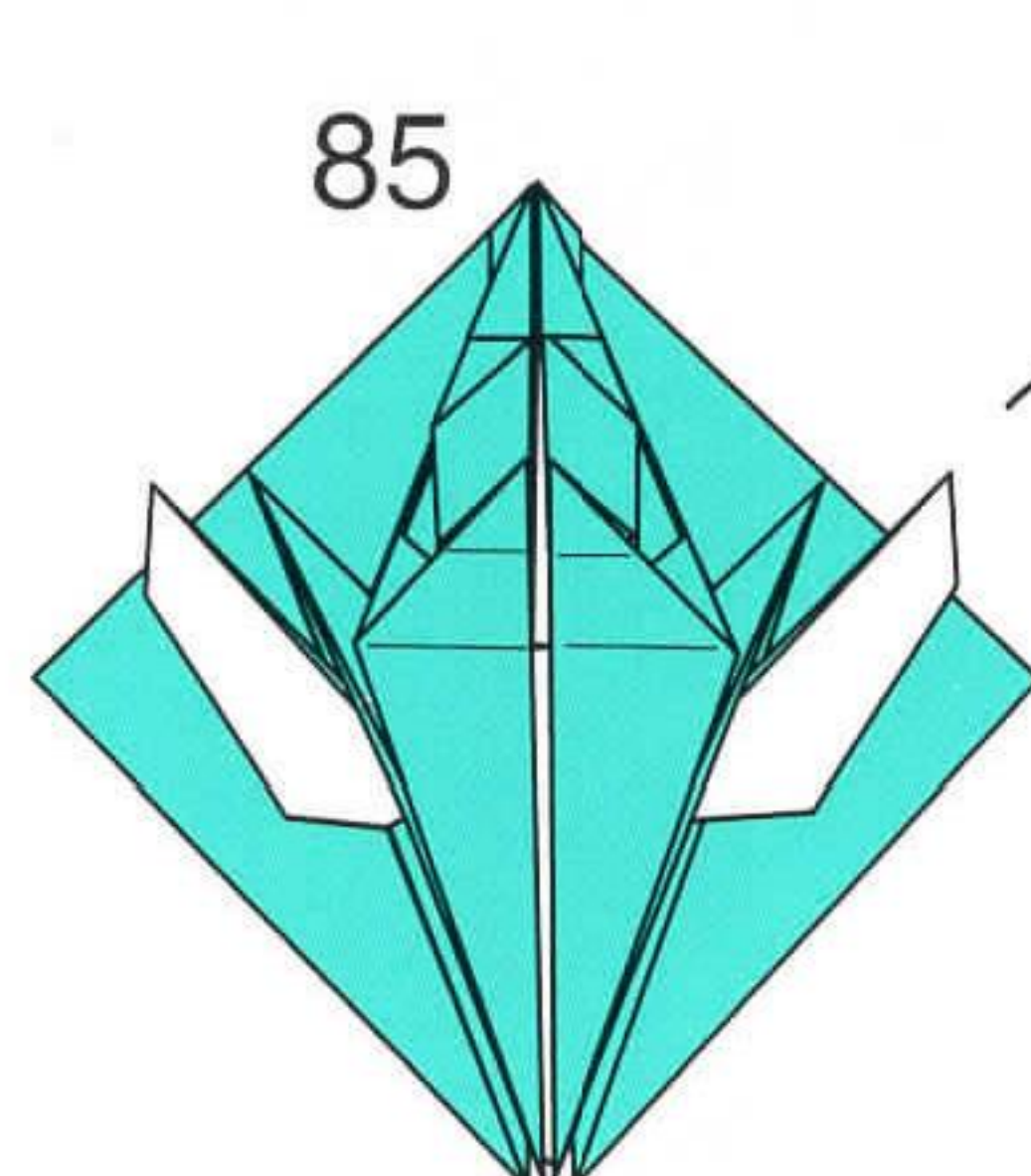
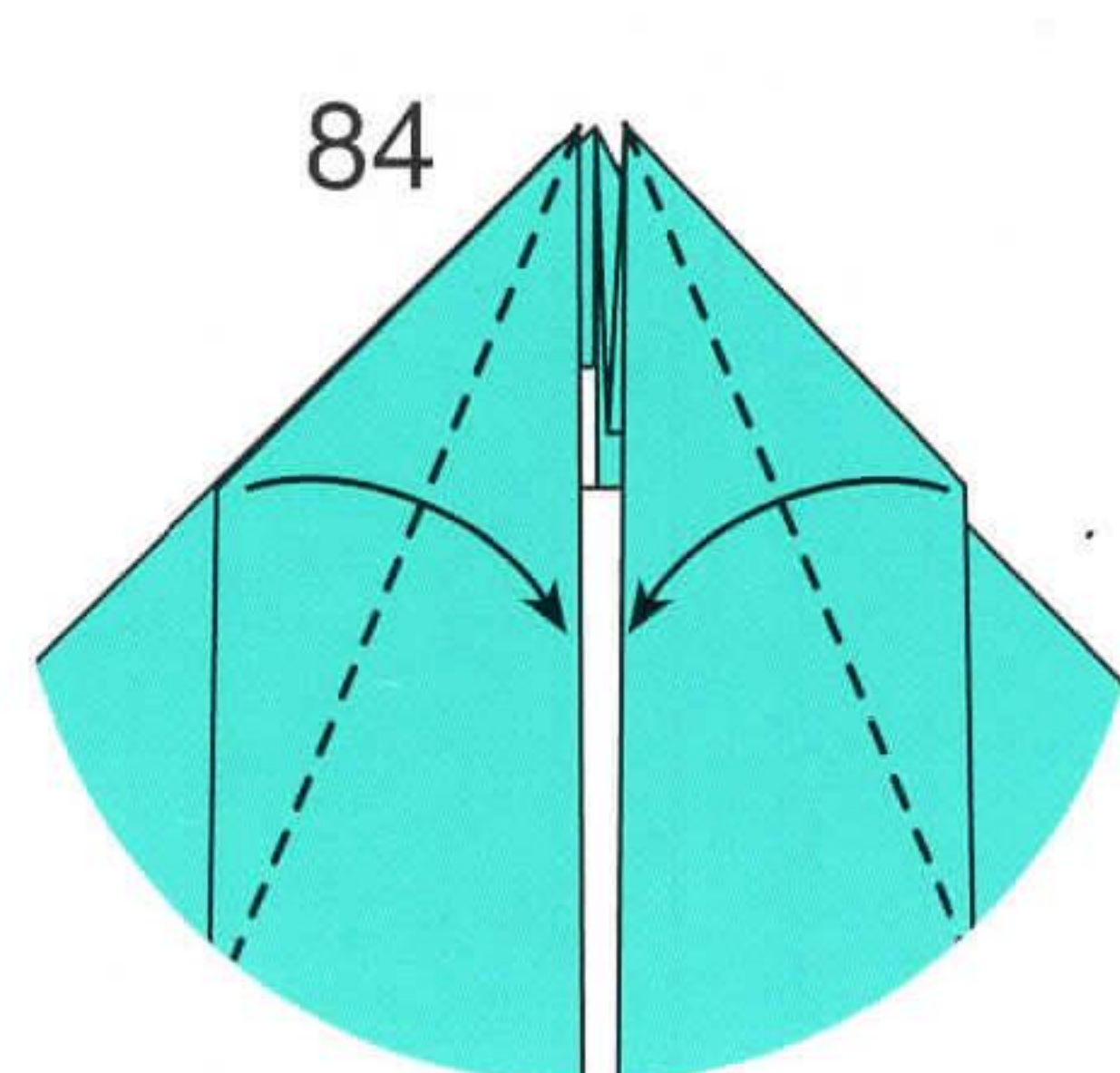
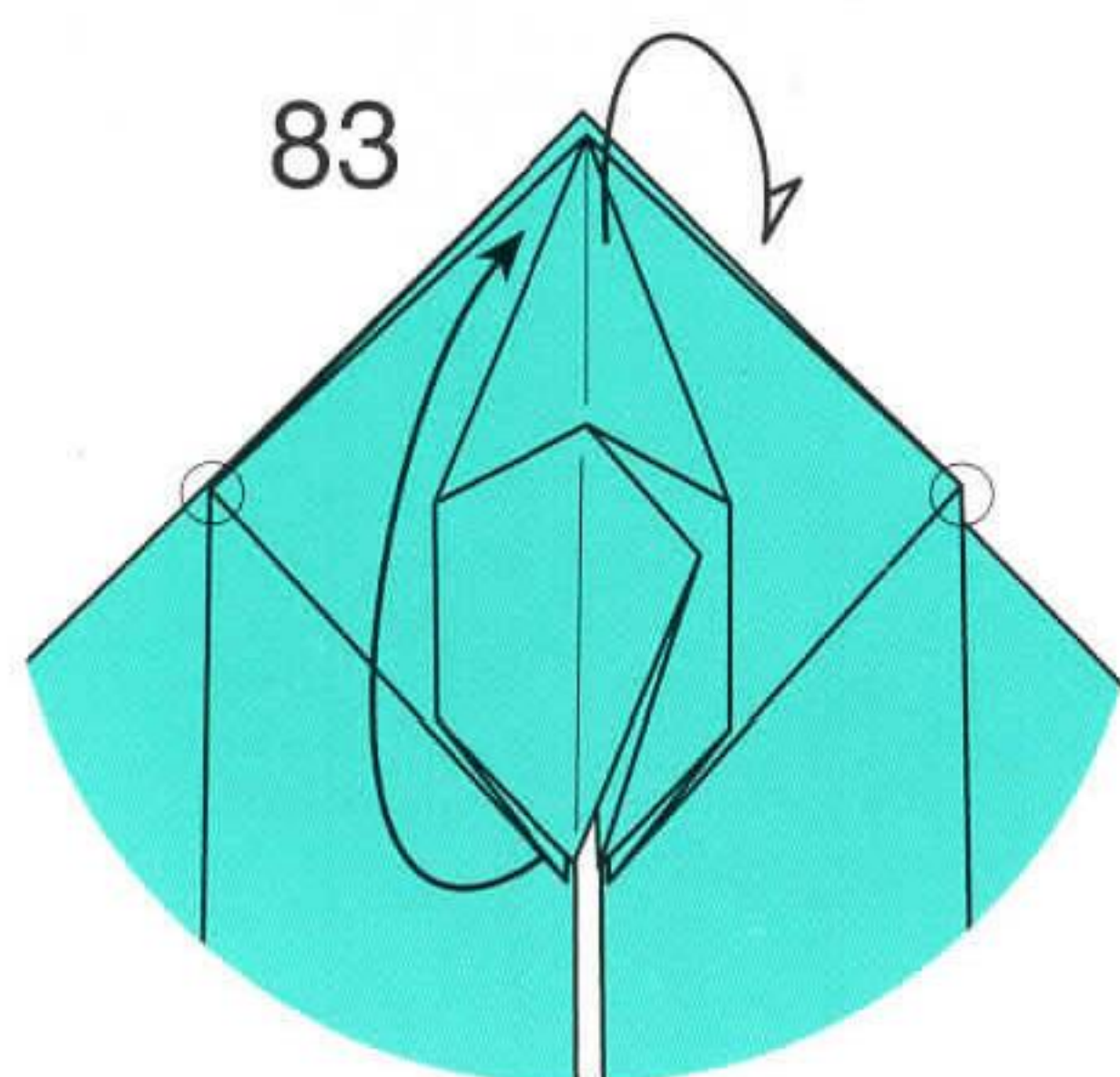


Unfold back to step 75.

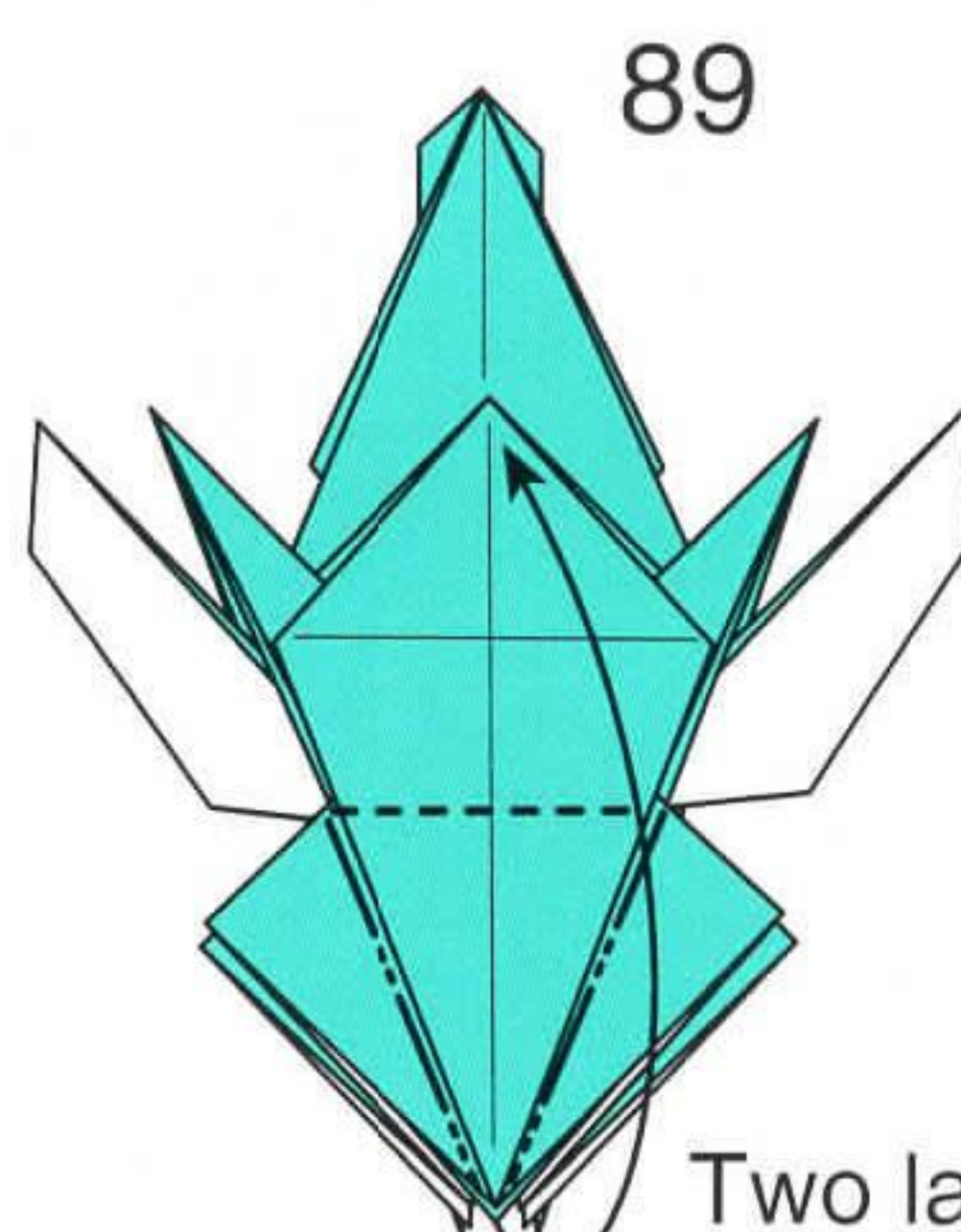


Inside reverse-fold

Inside reverse-fold

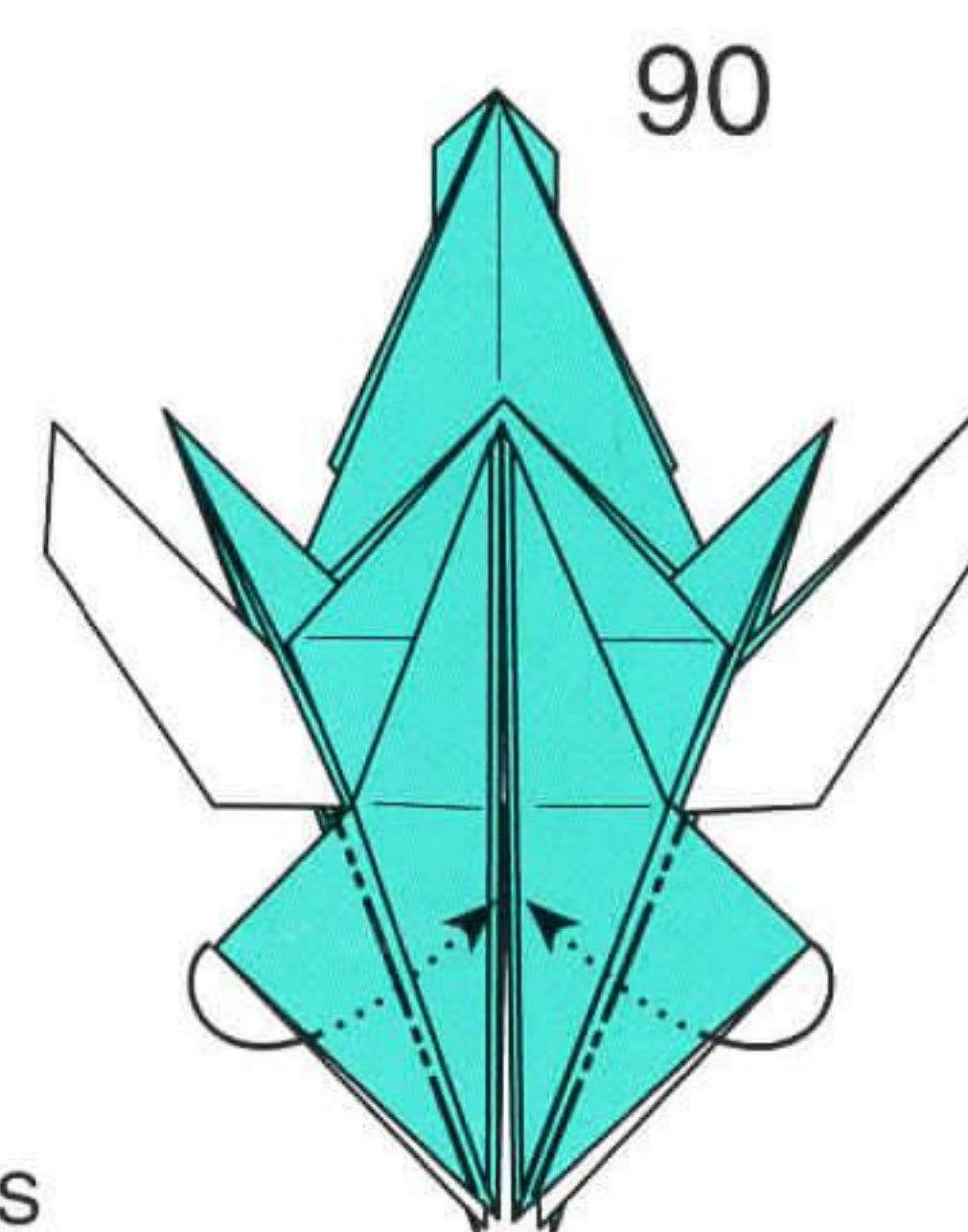


Fold like a Preliminary base.

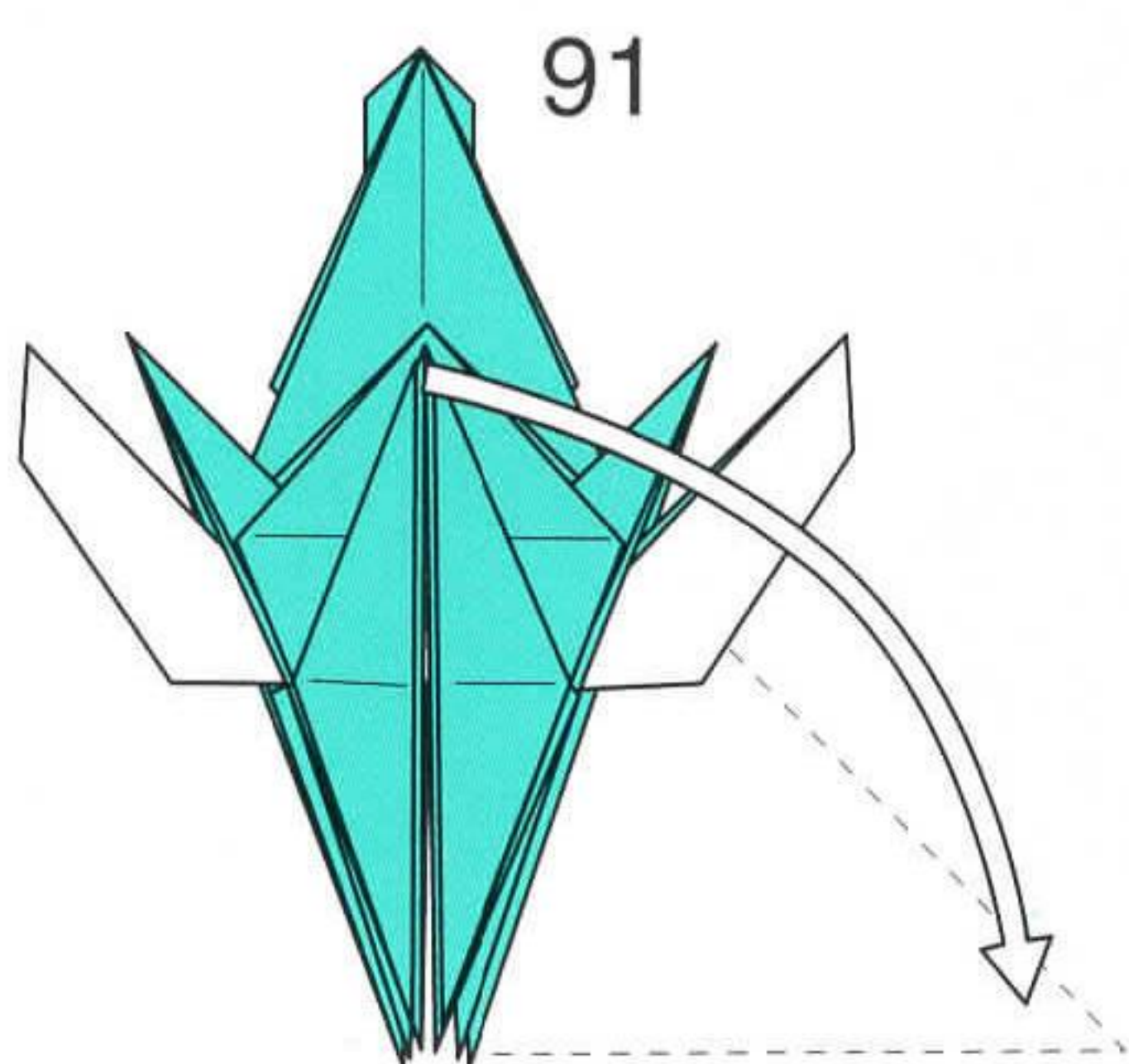


Petal-fold

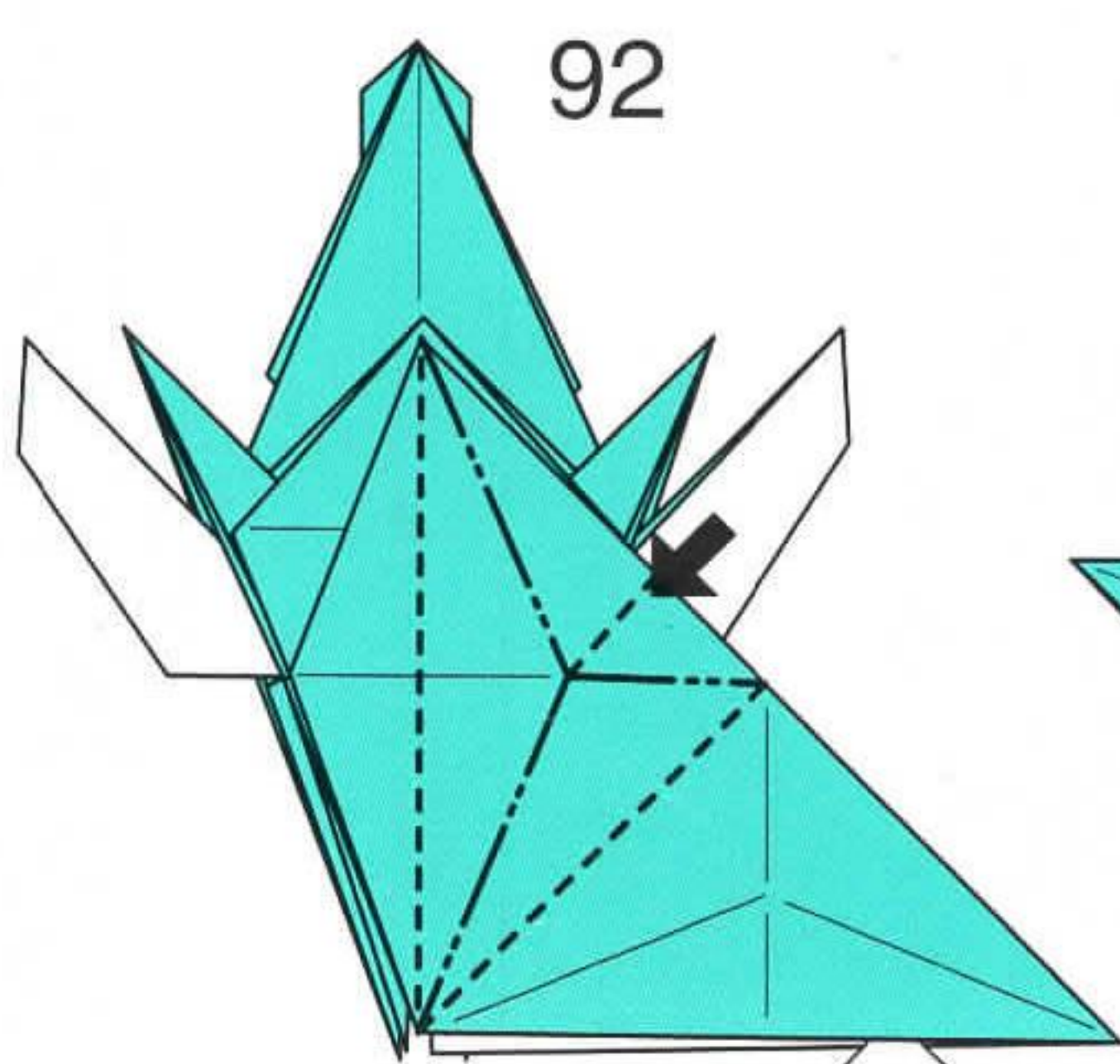
Two layers



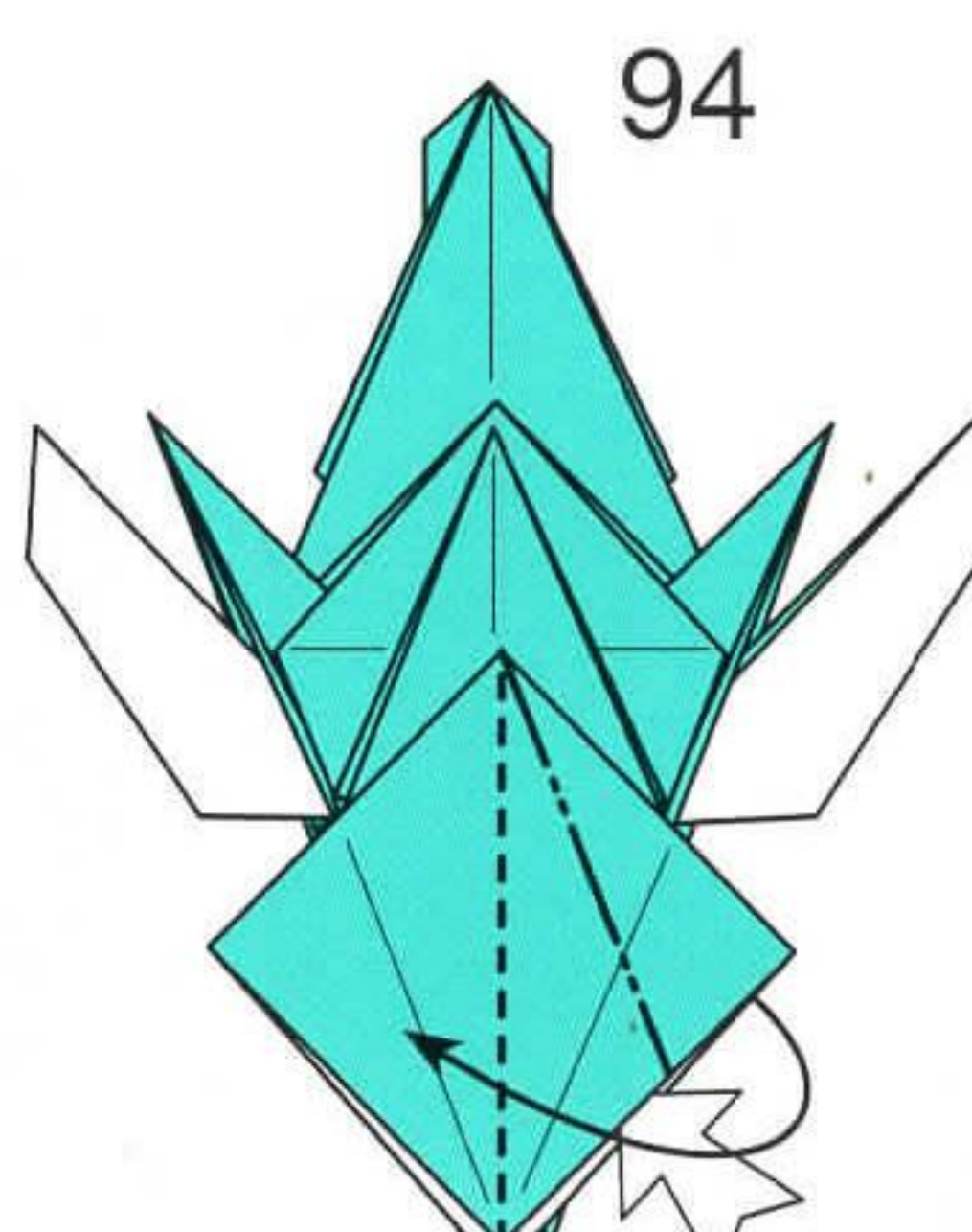
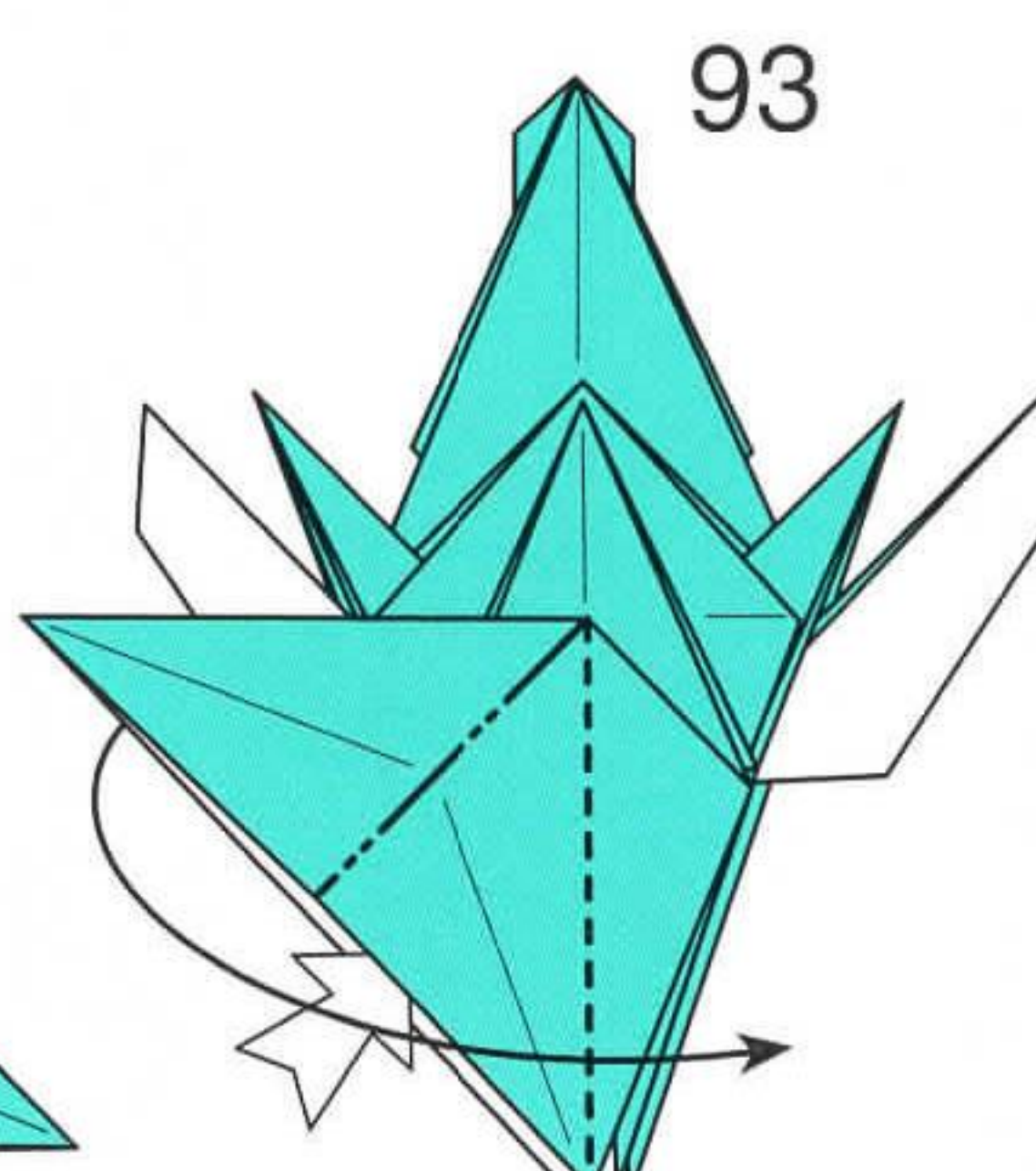
Inside reverse-fold

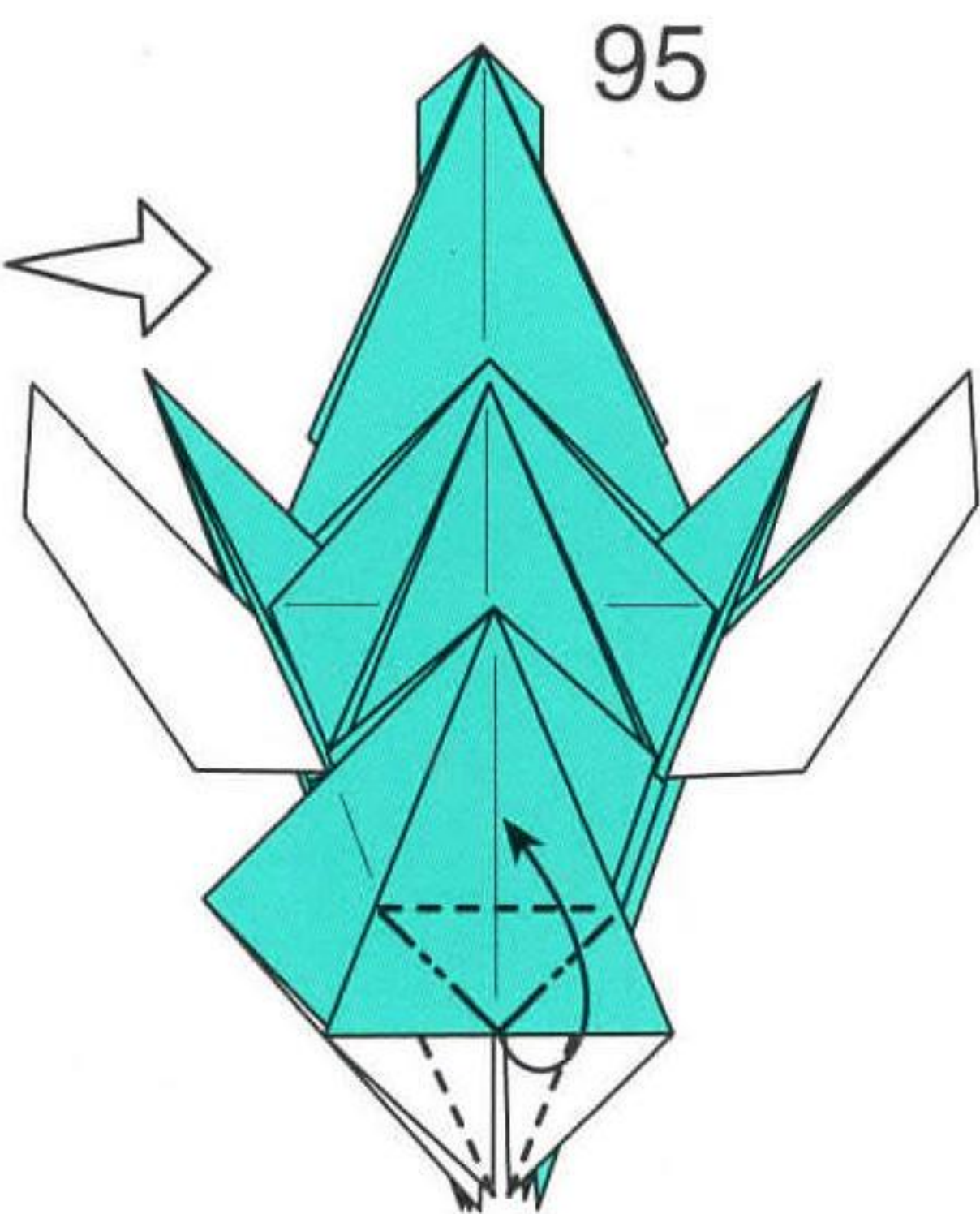


Pull out the inner corner while leaving the outer petal fold in place.

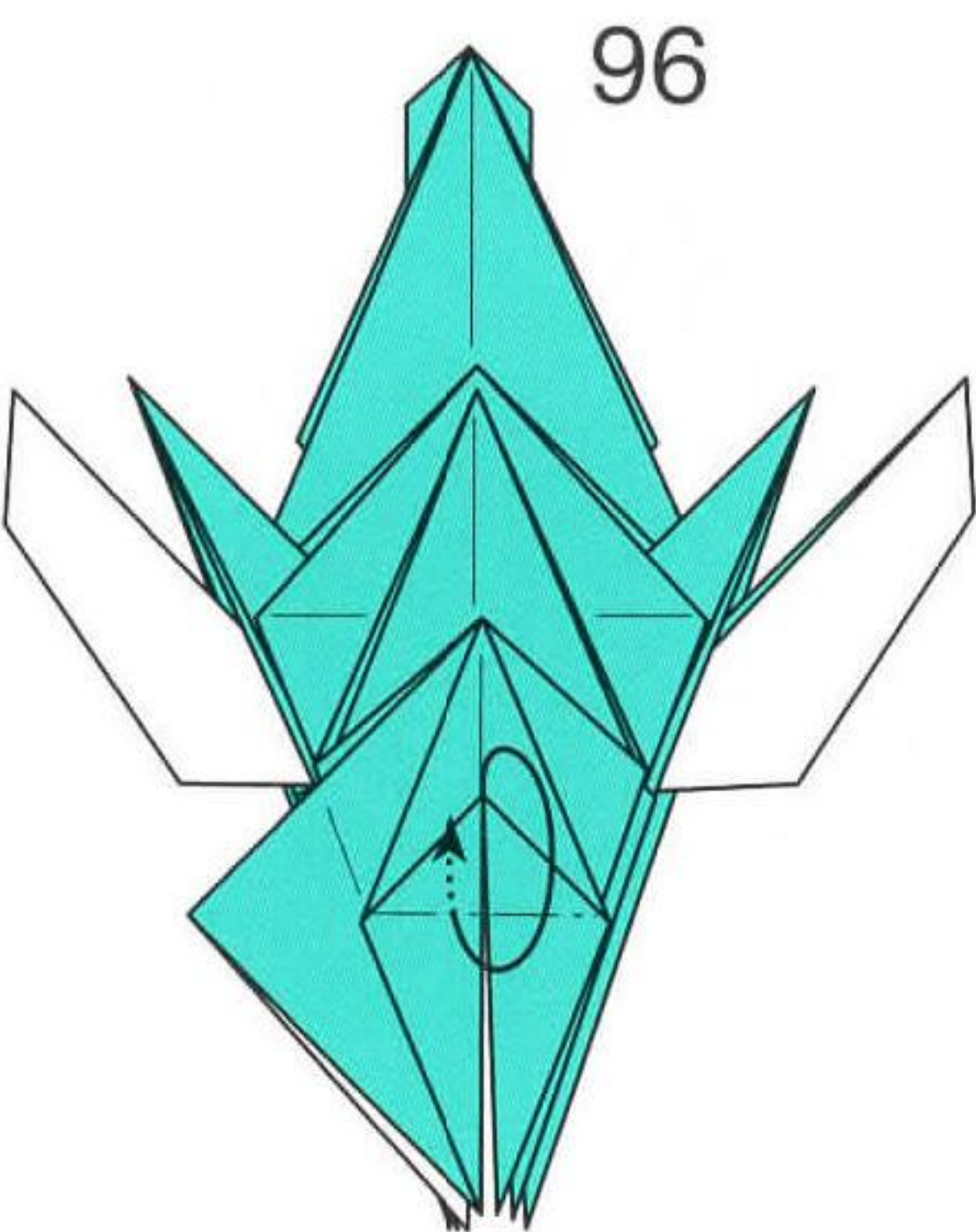


Fold like a Bird base.

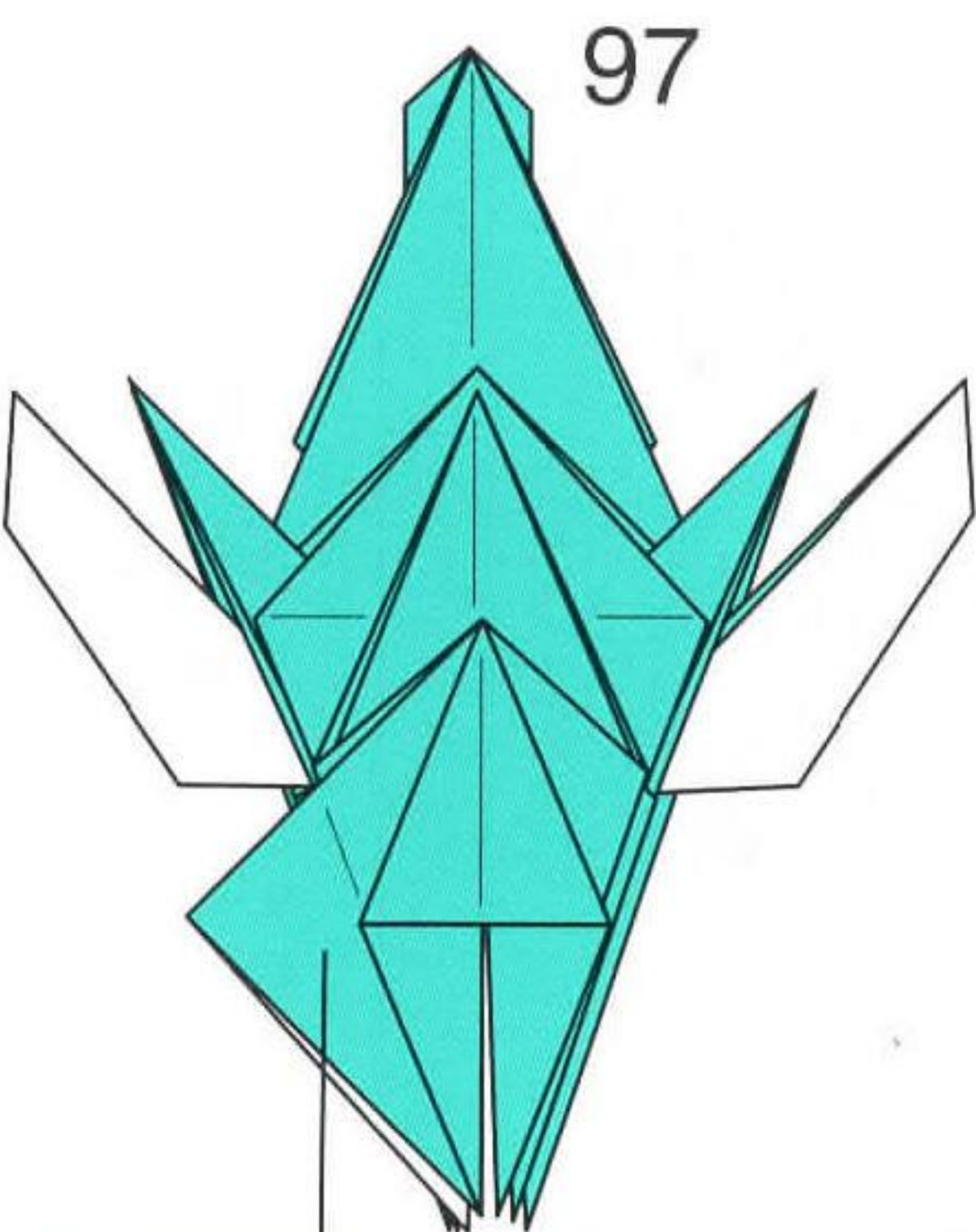




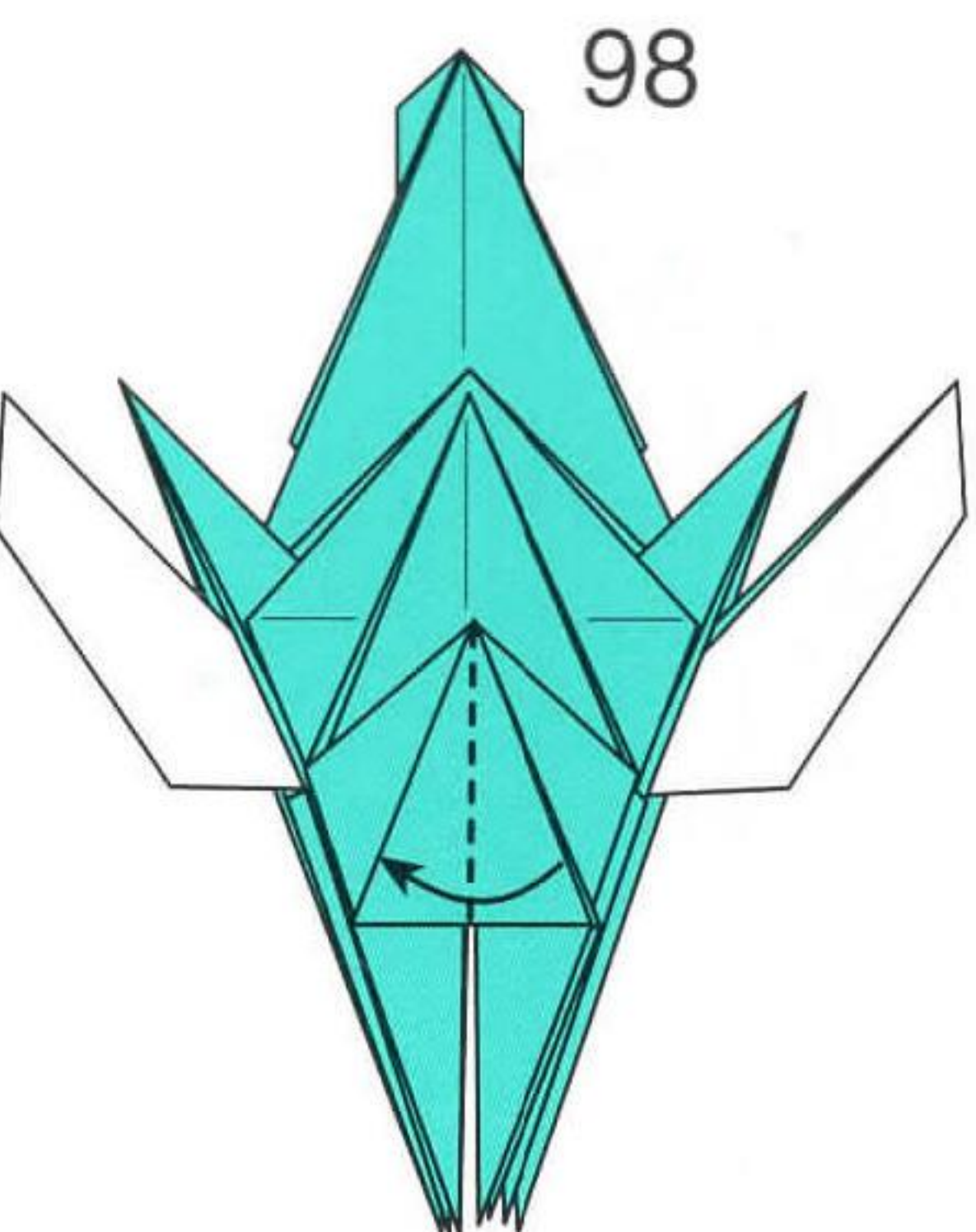
Petal-fold



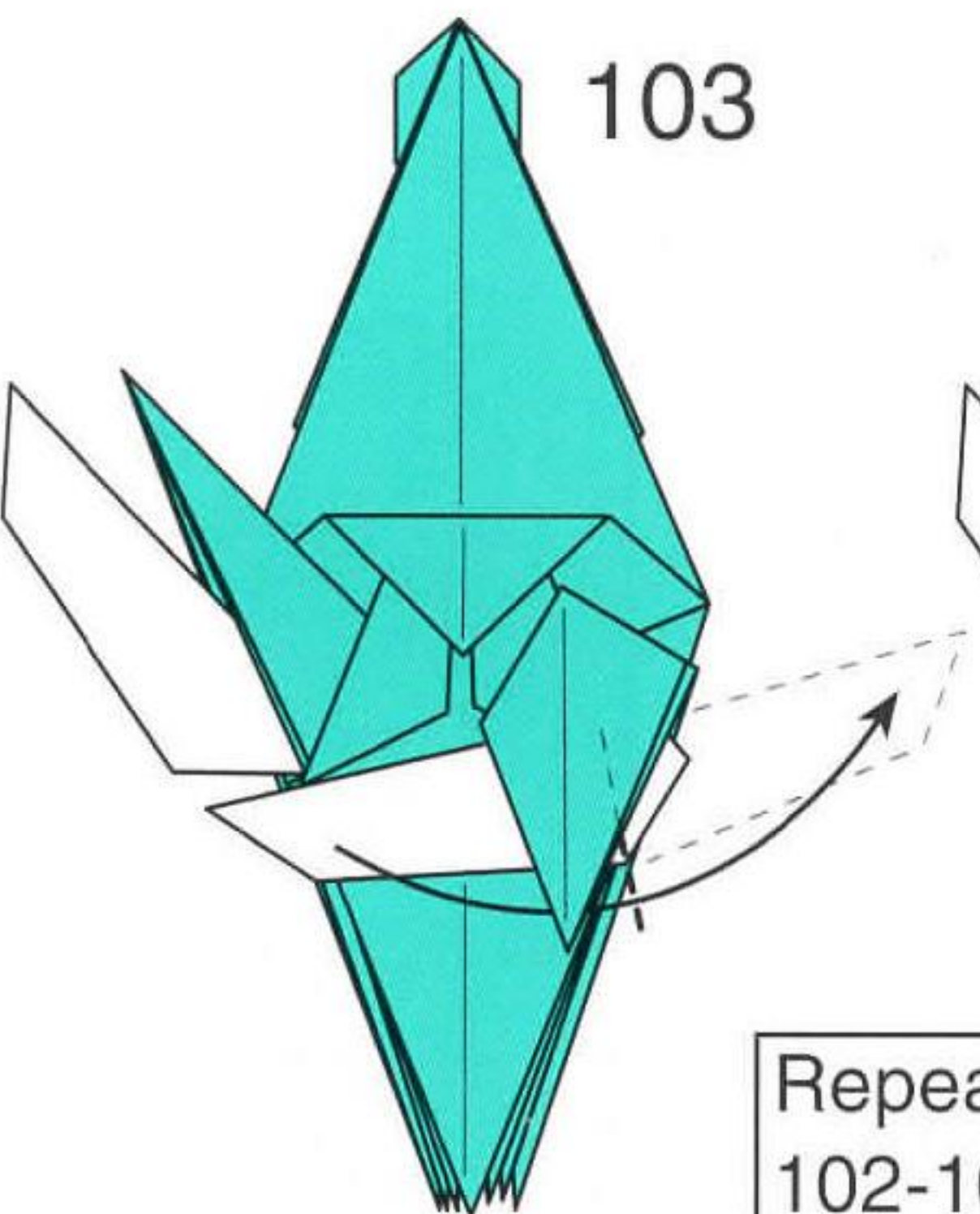
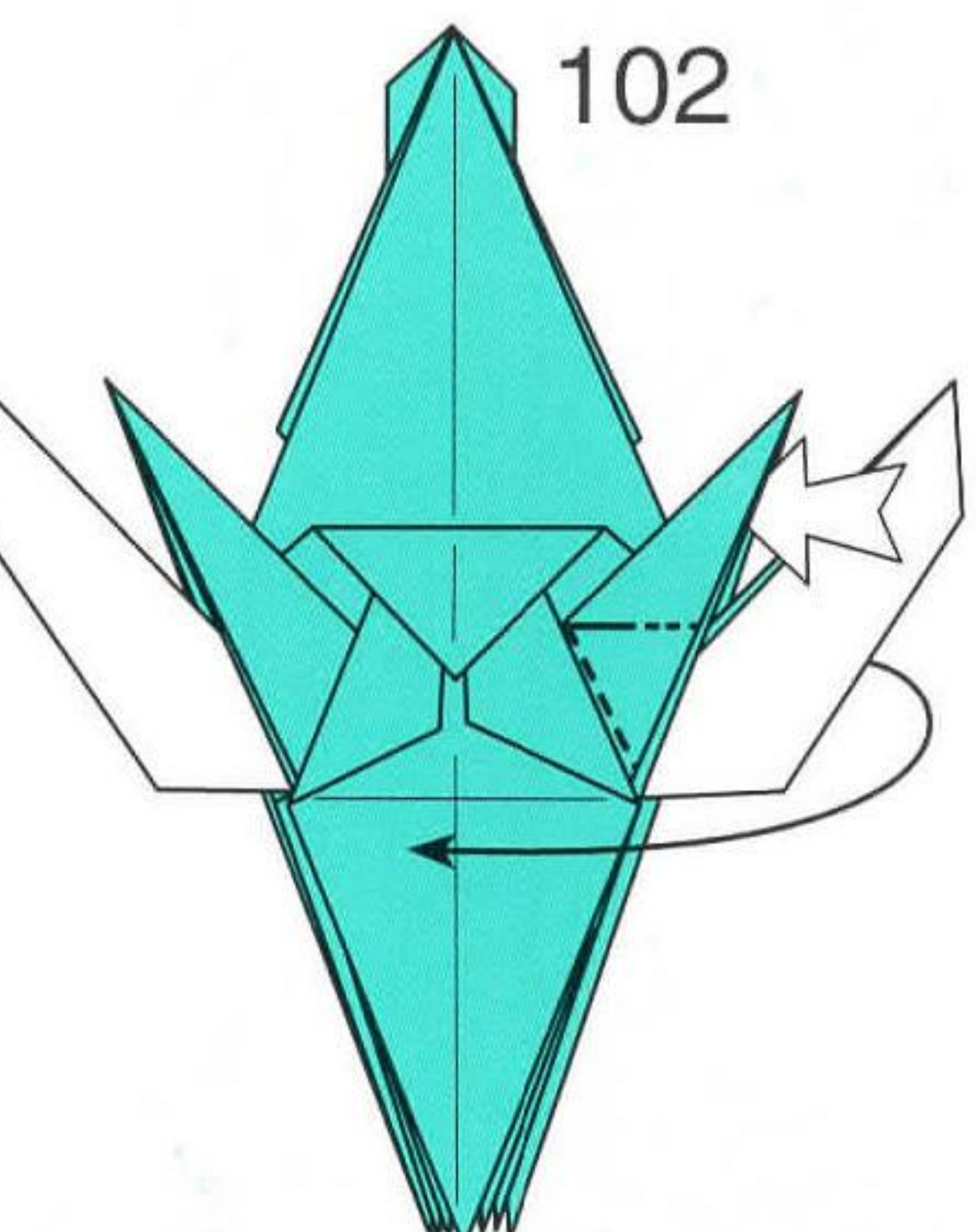
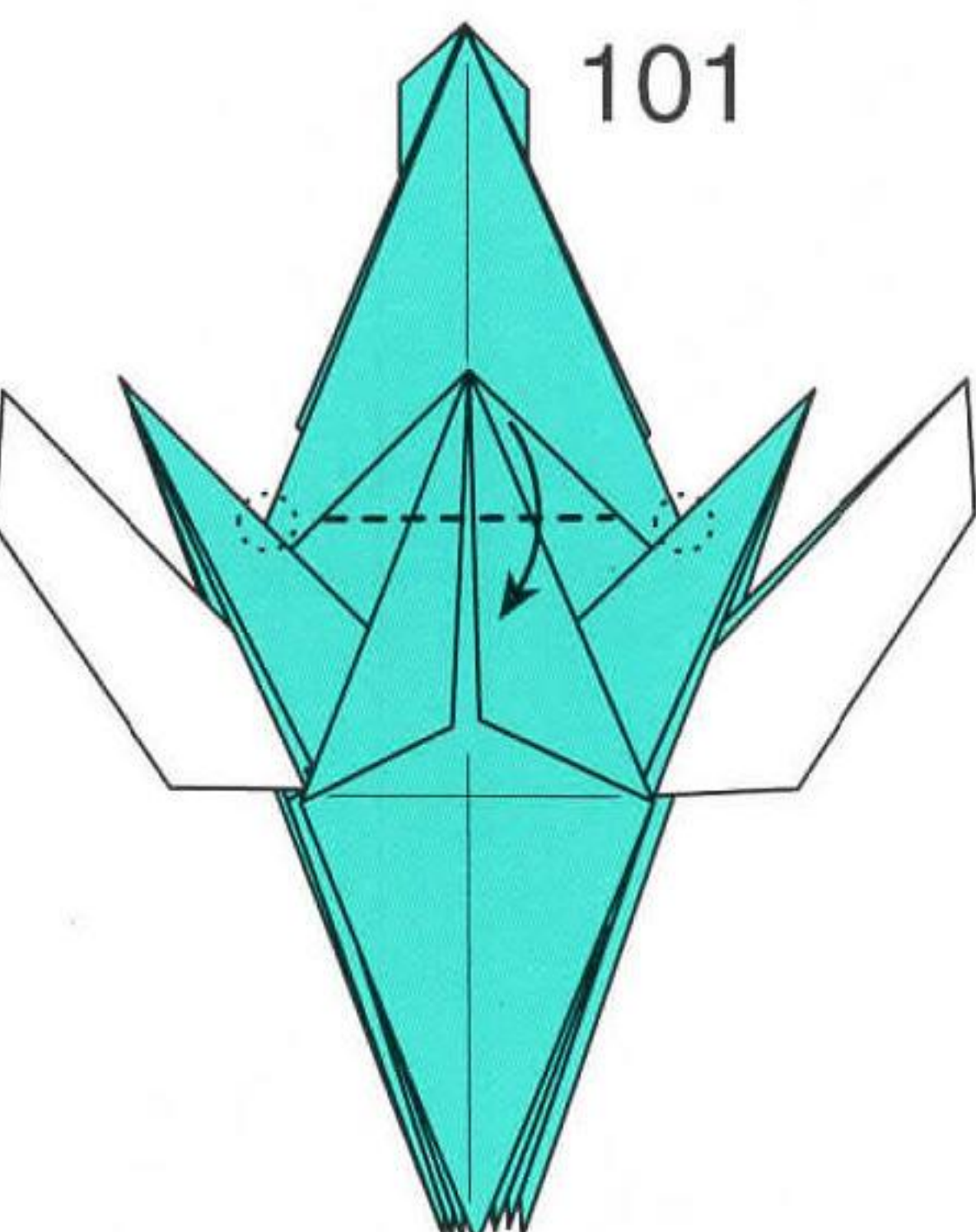
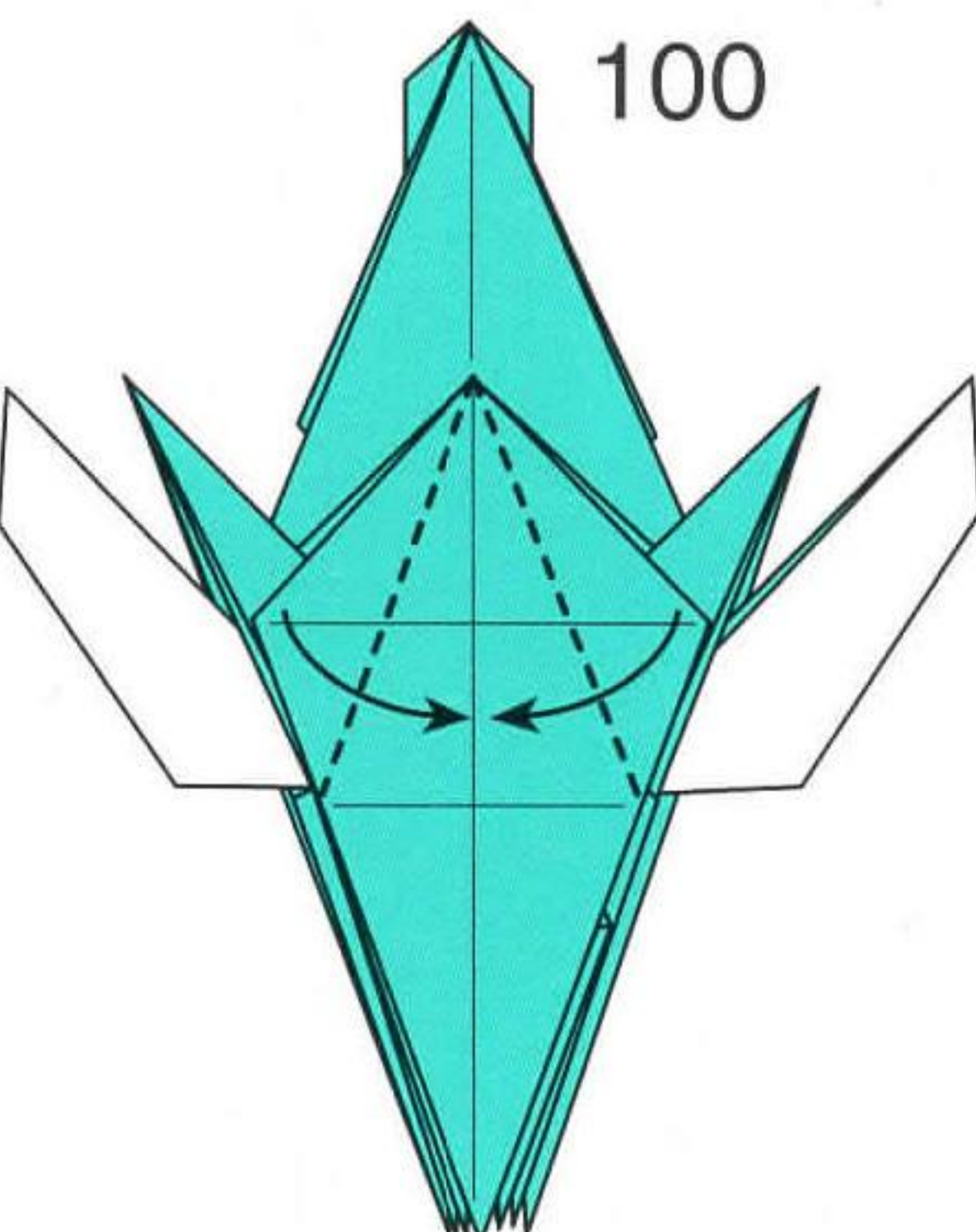
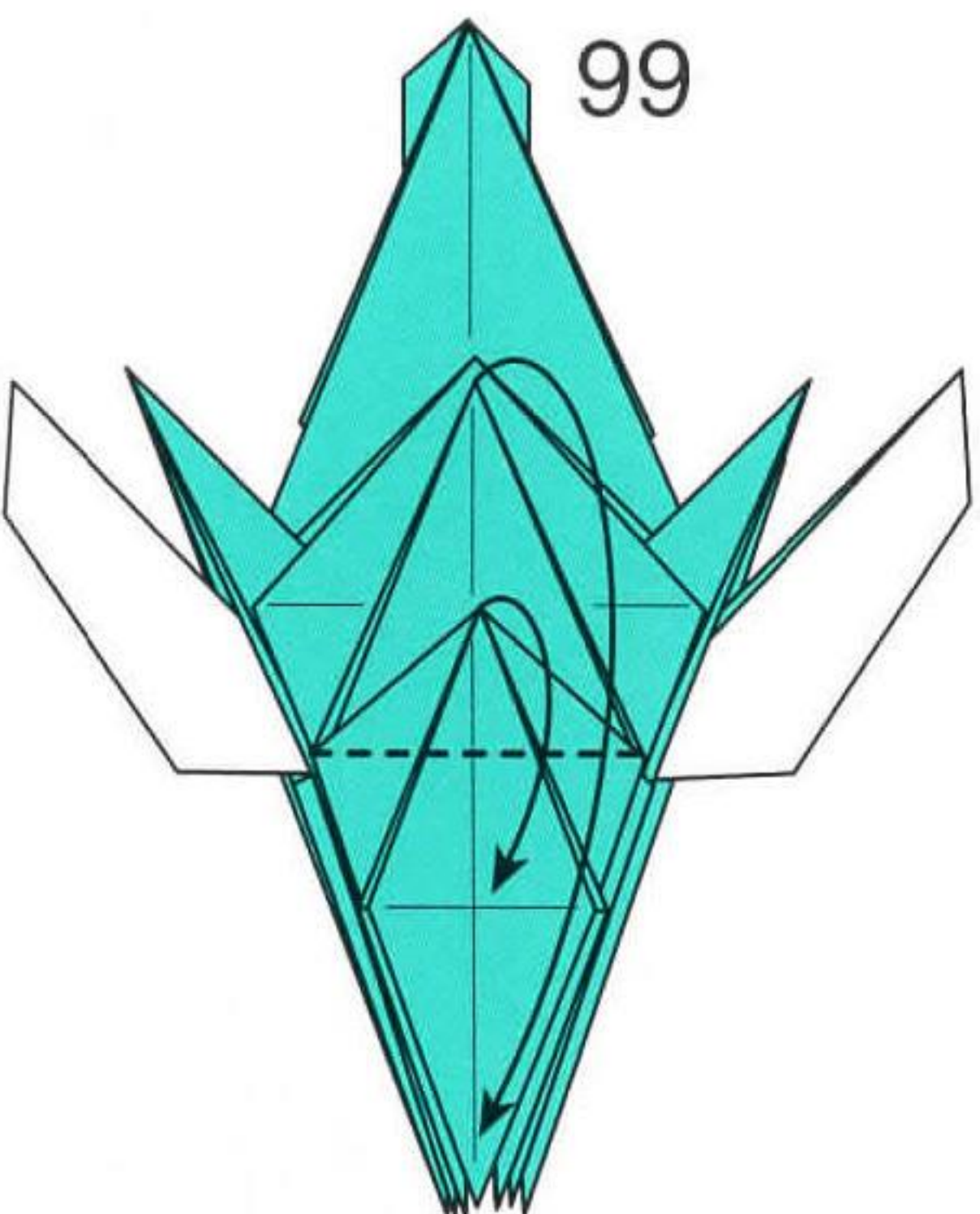
Reverse the flap inside.



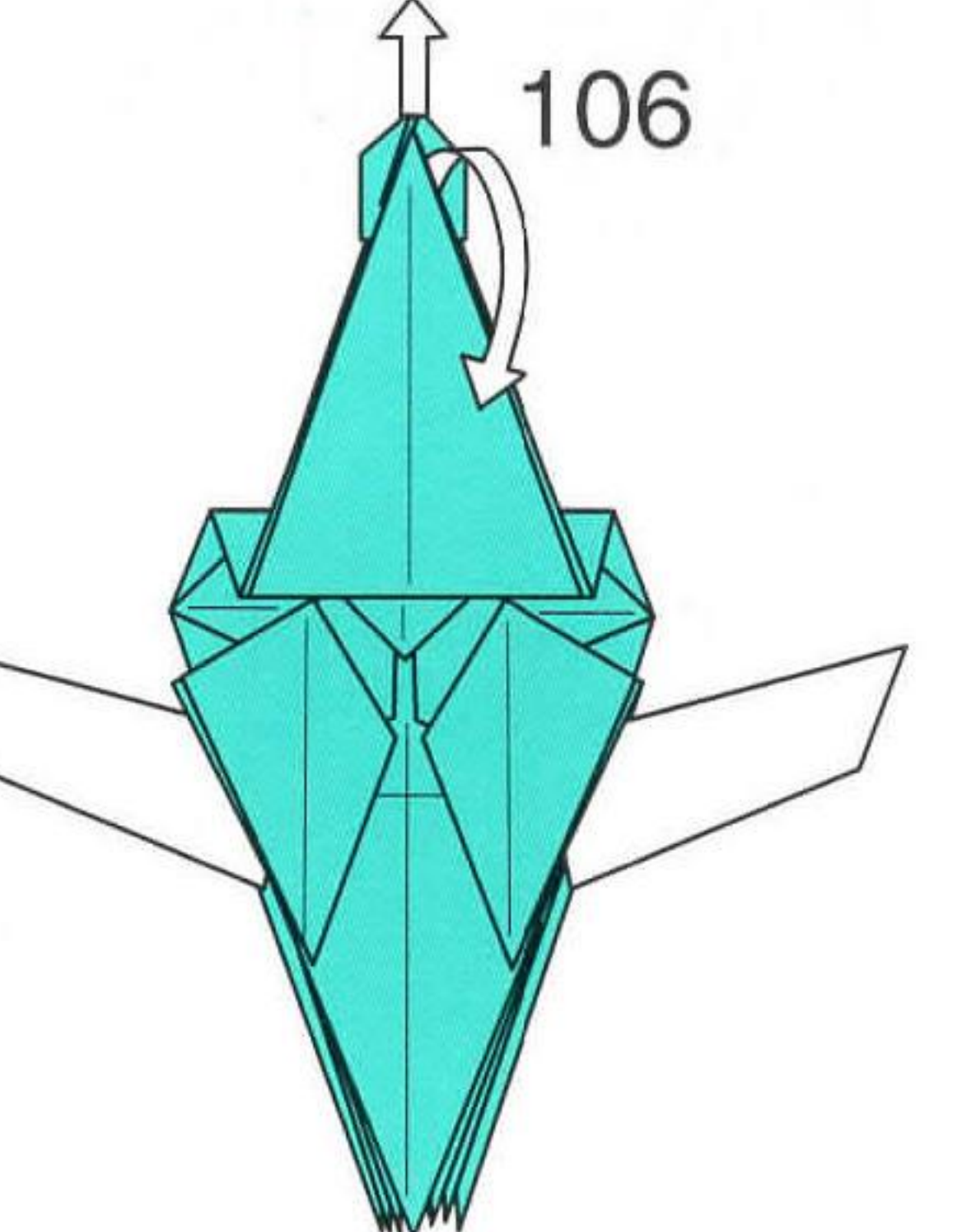
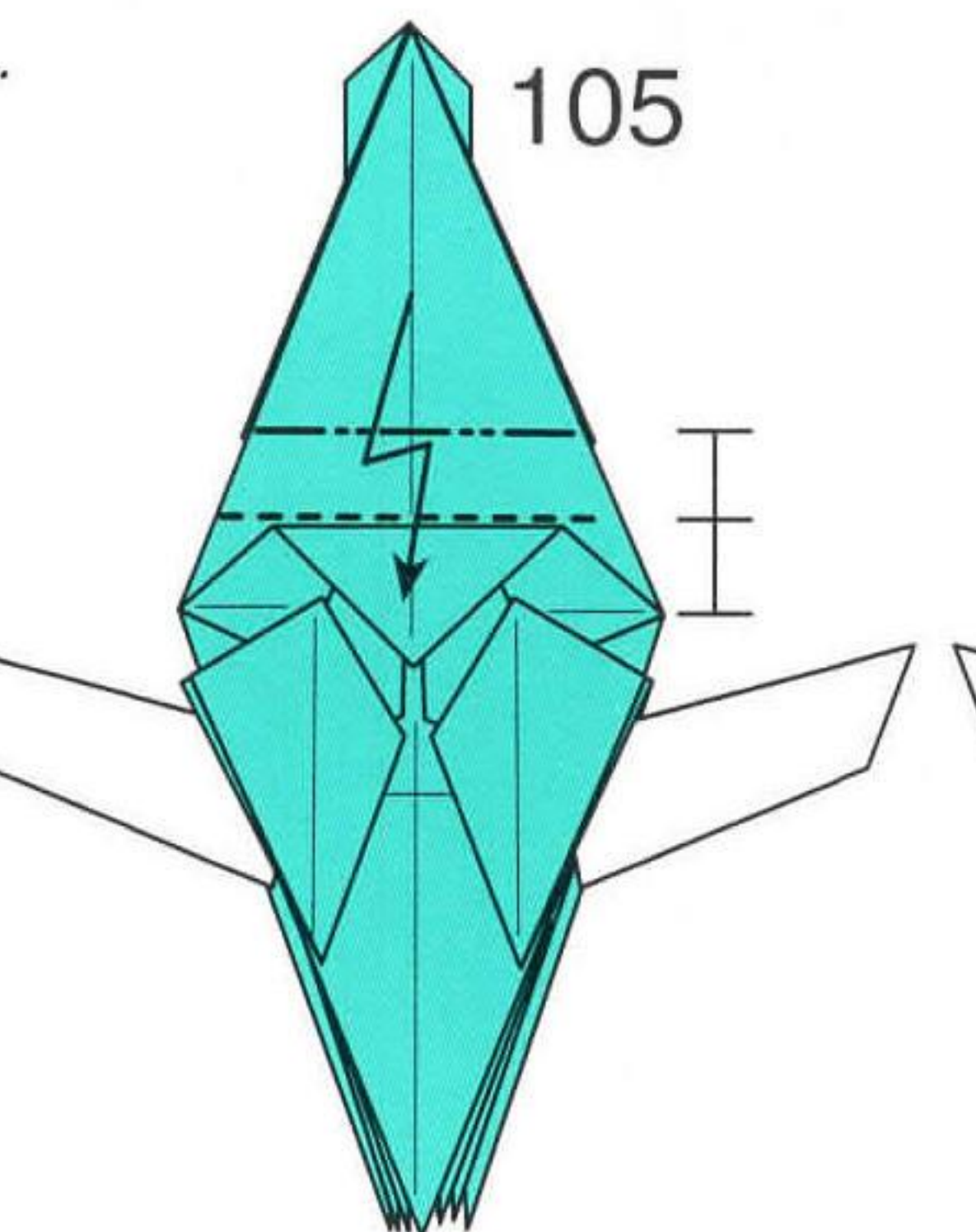
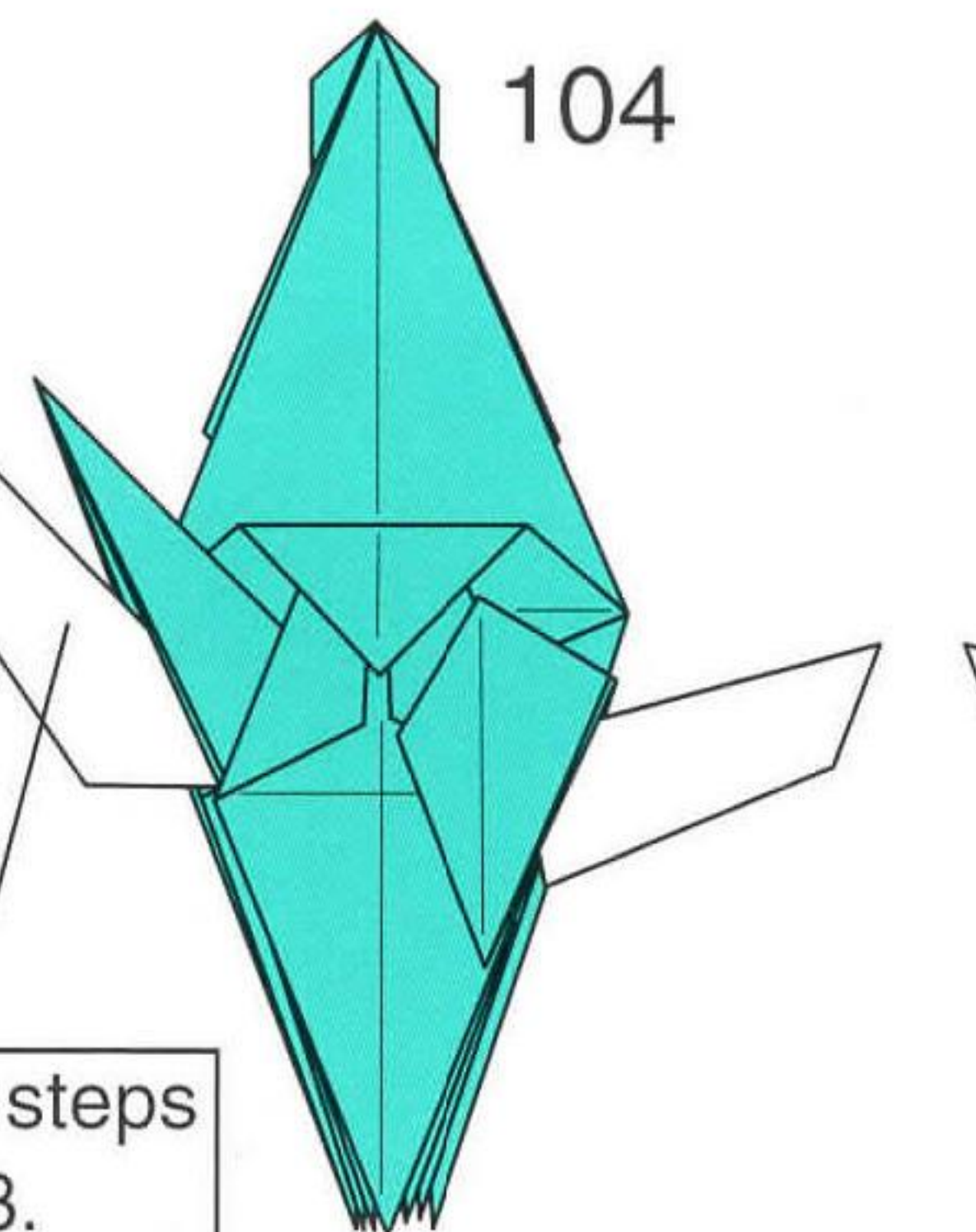
Repeat steps 95-97.



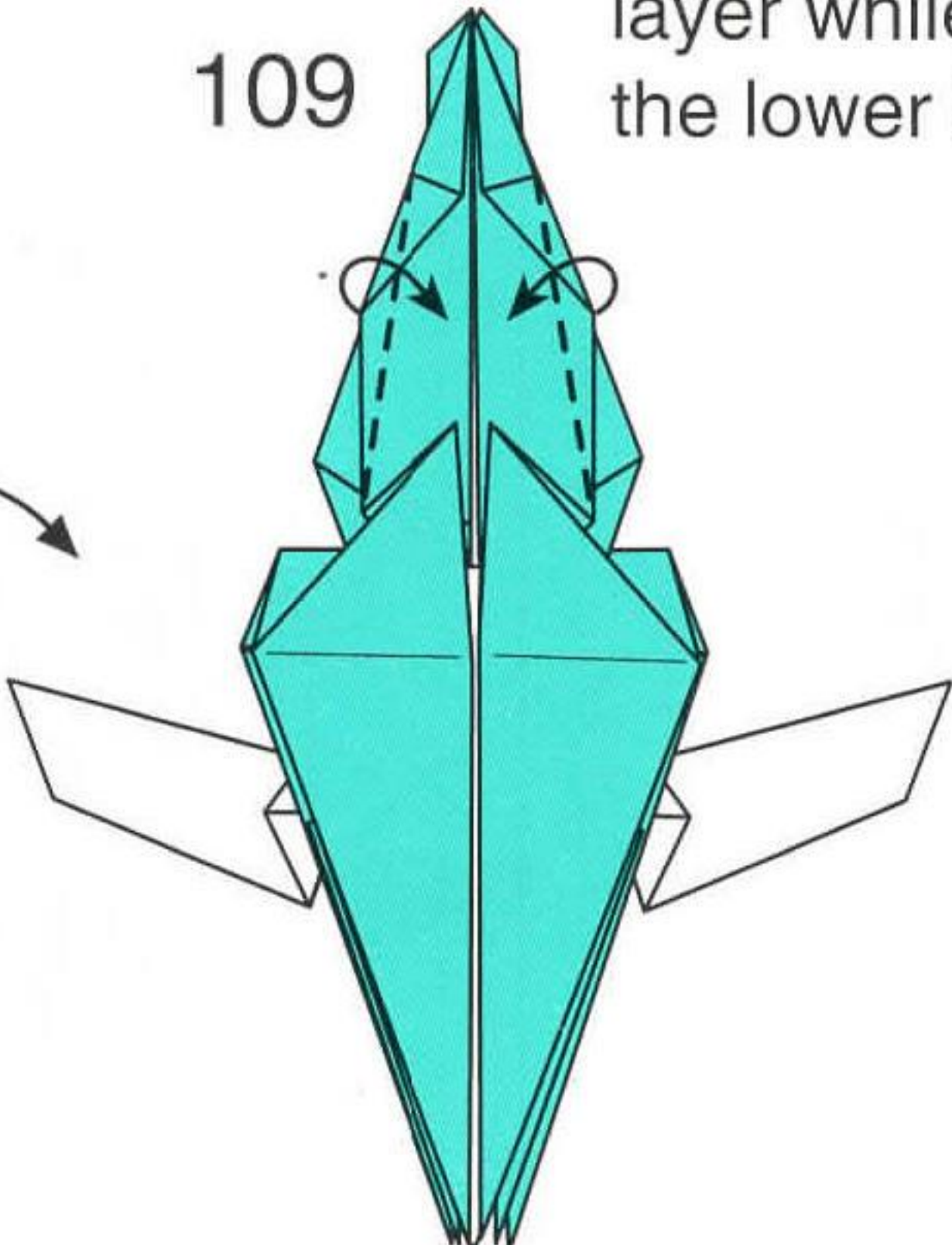
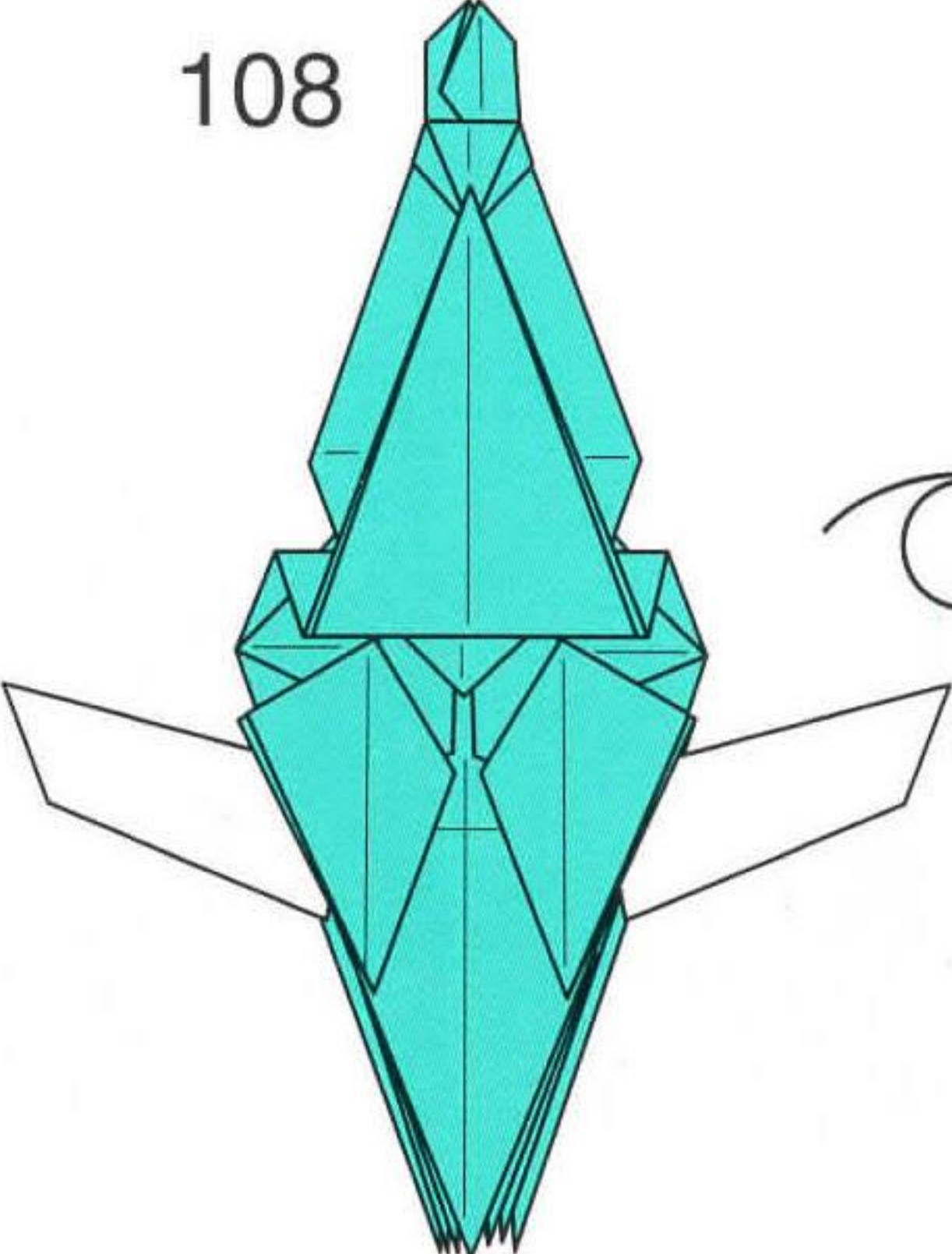
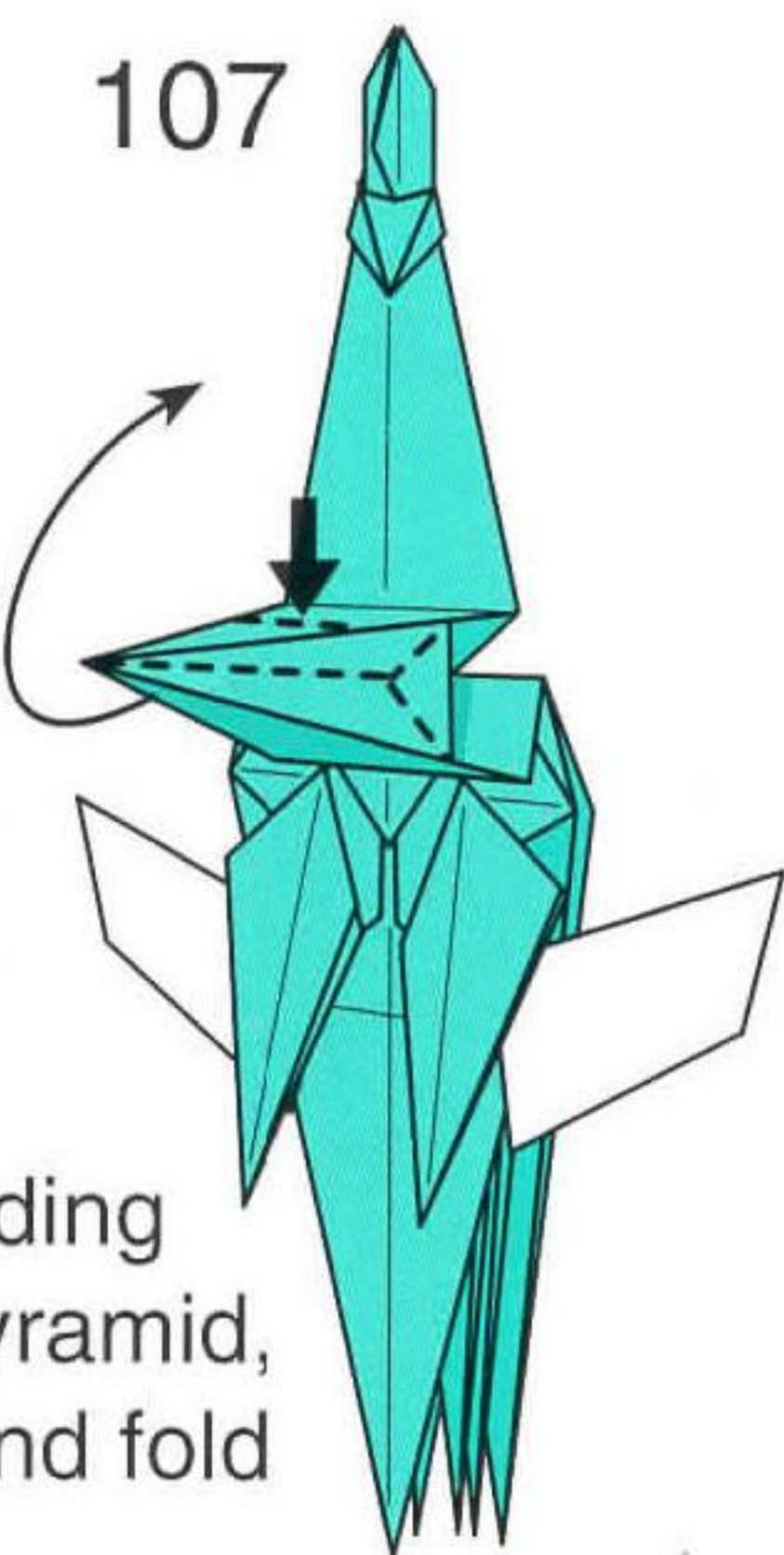
Flip a flap to make the model symmetrical.



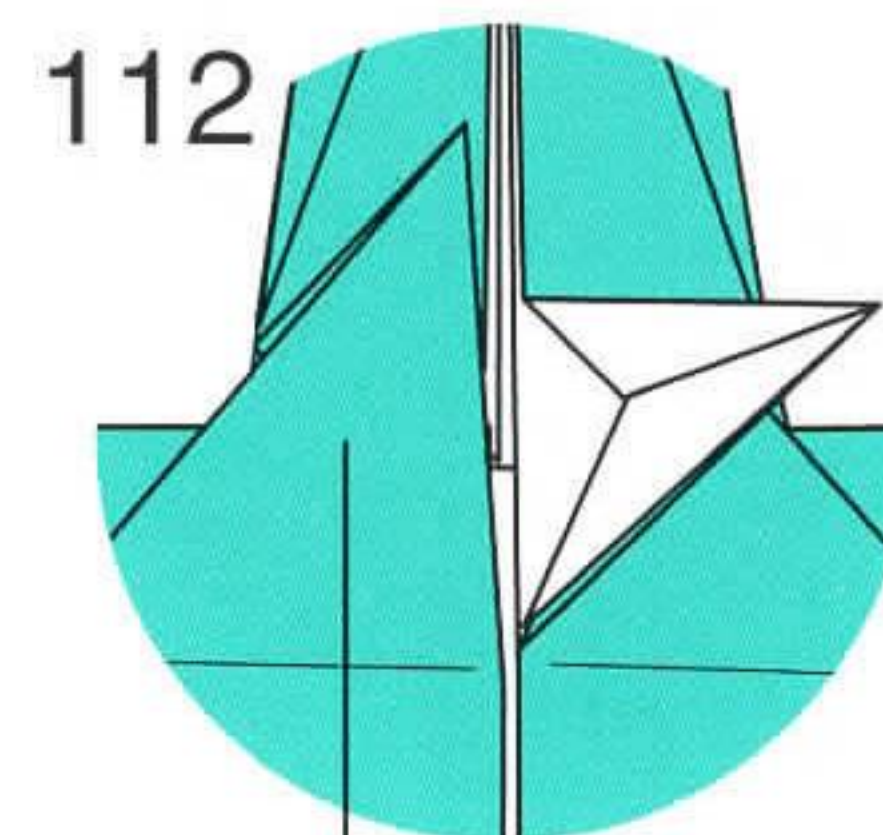
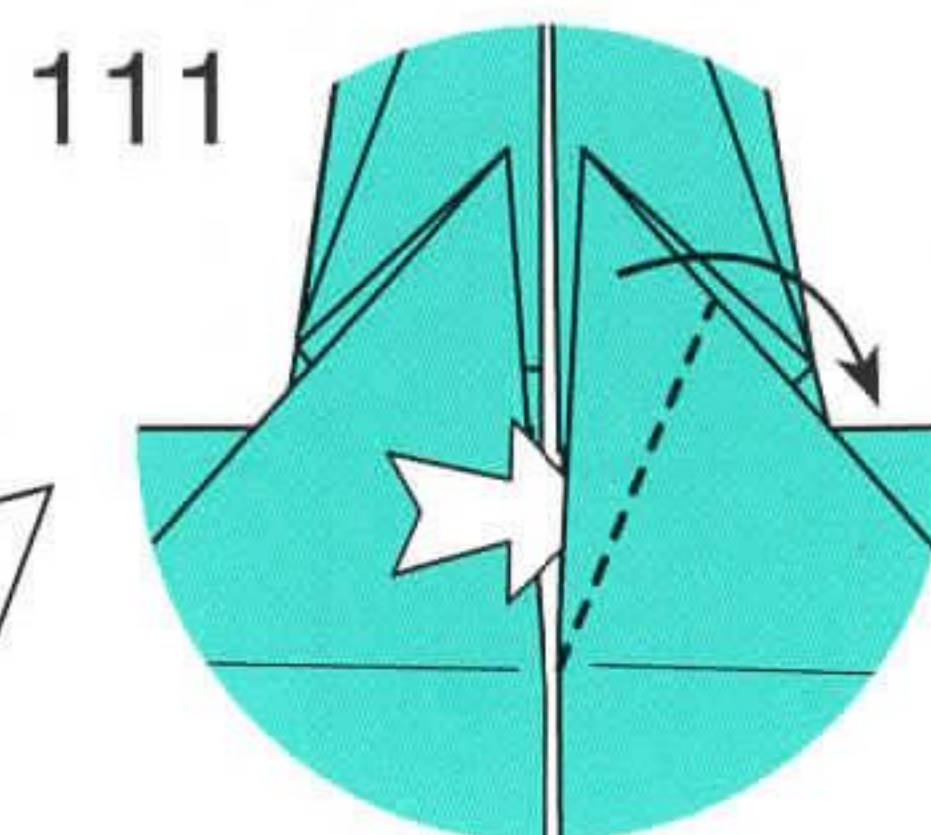
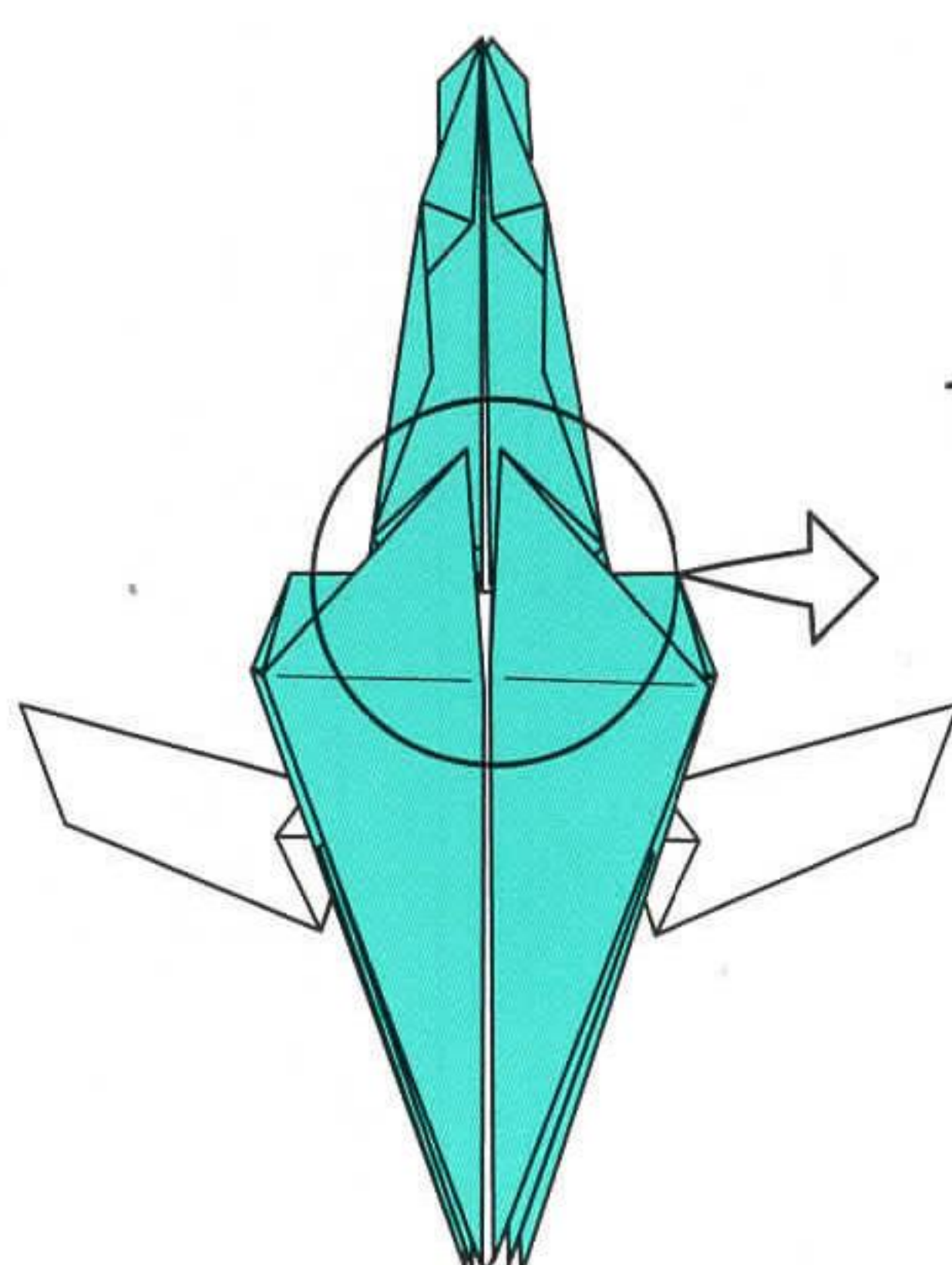
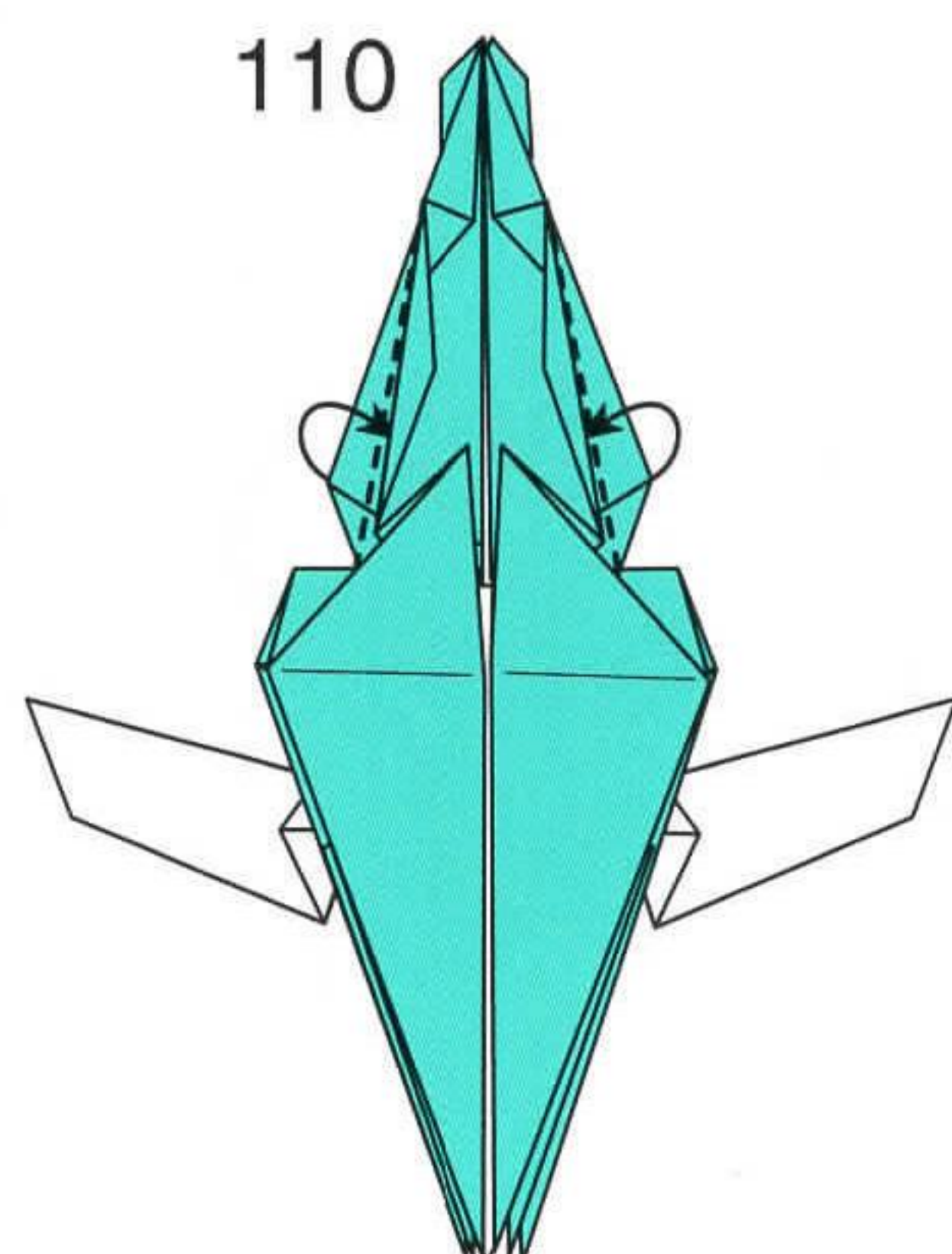
Repeat steps 102-103.



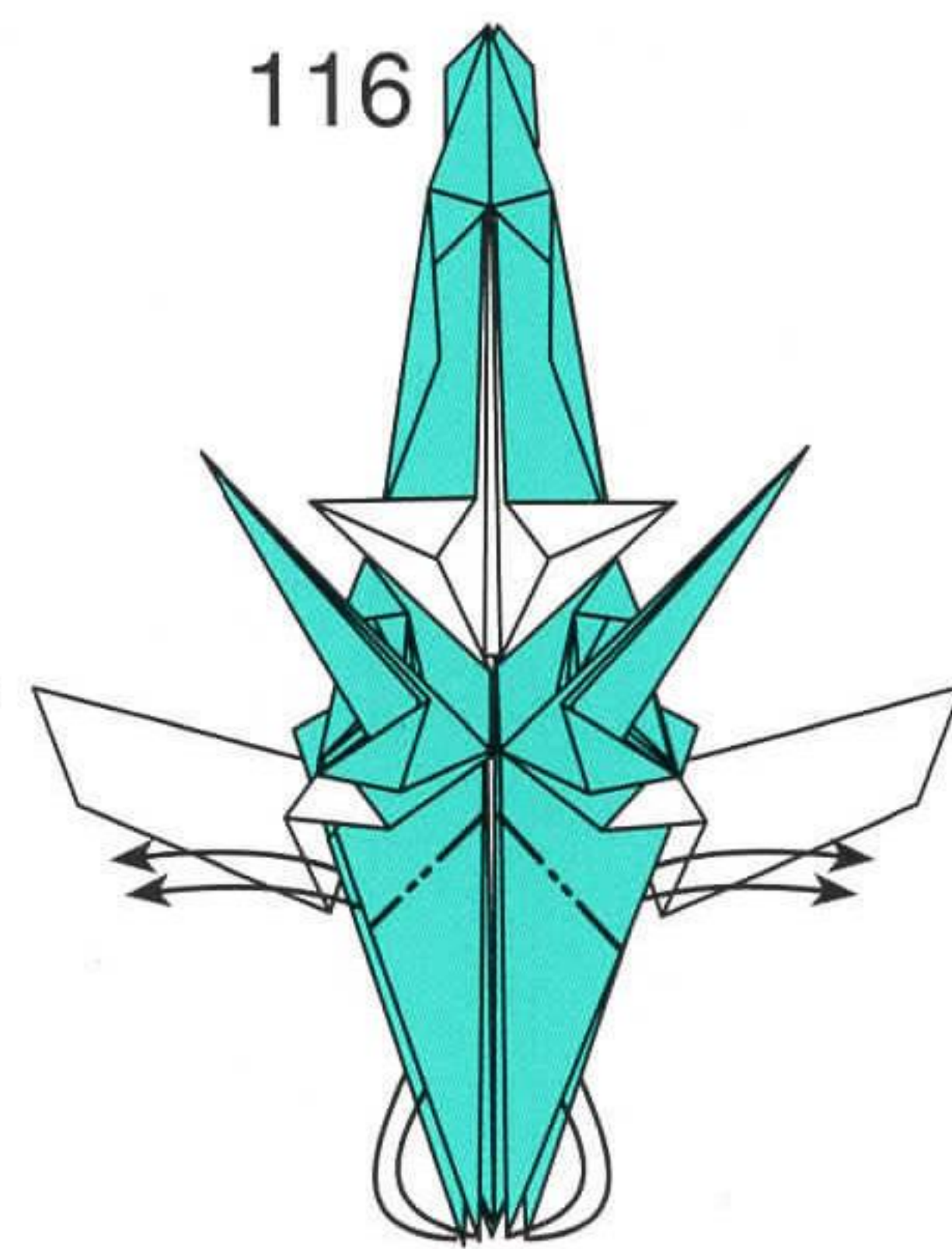
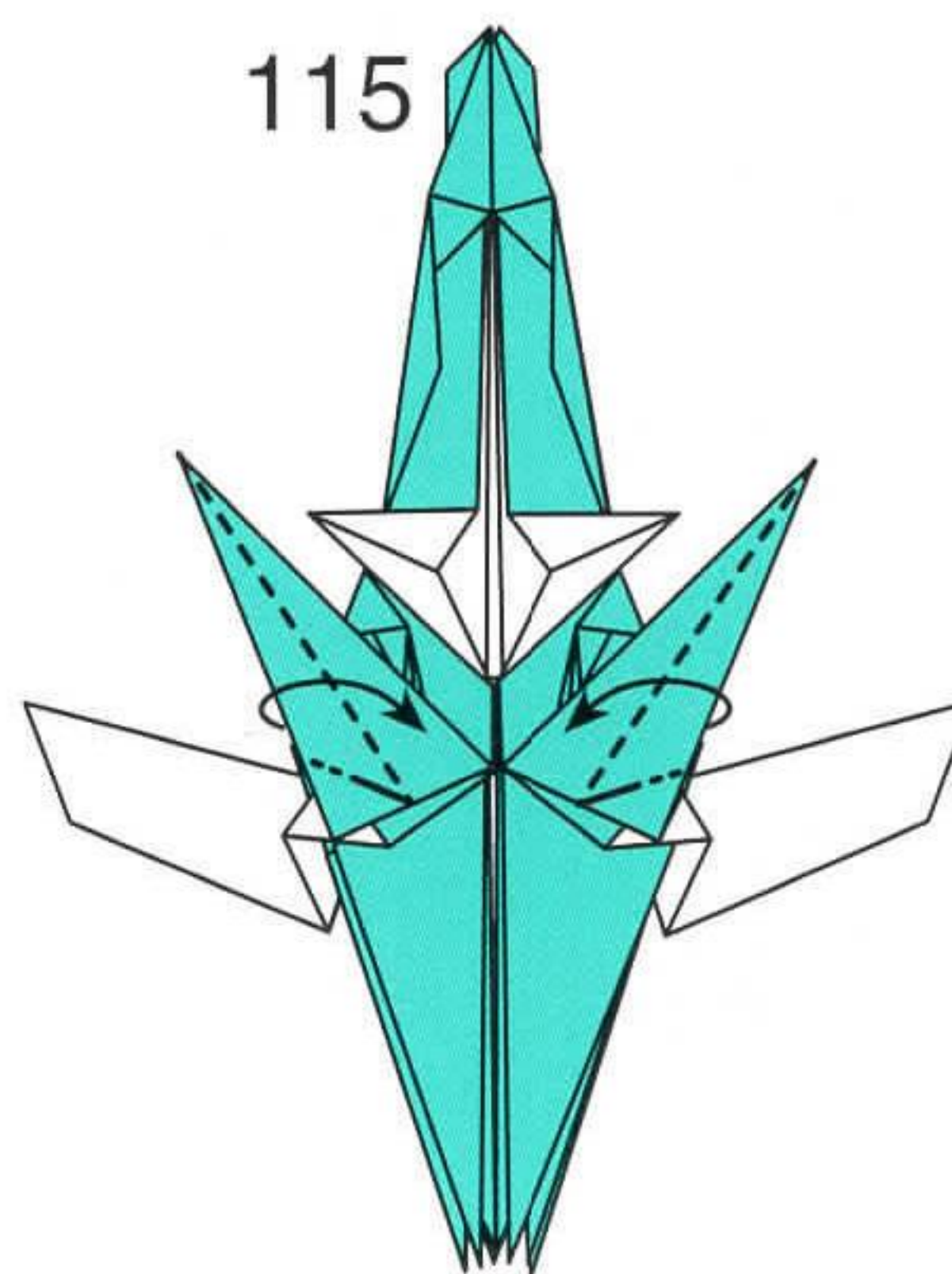
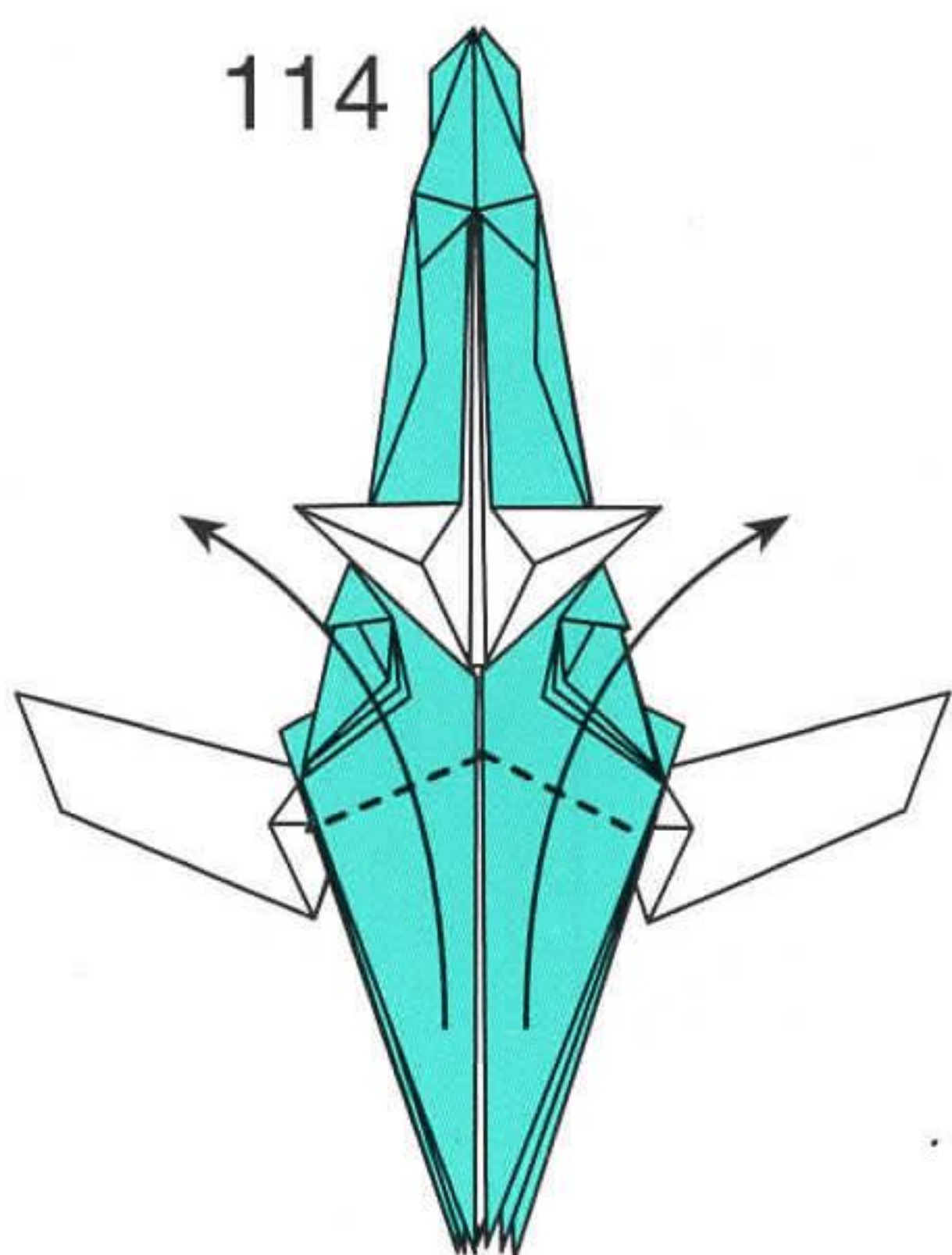
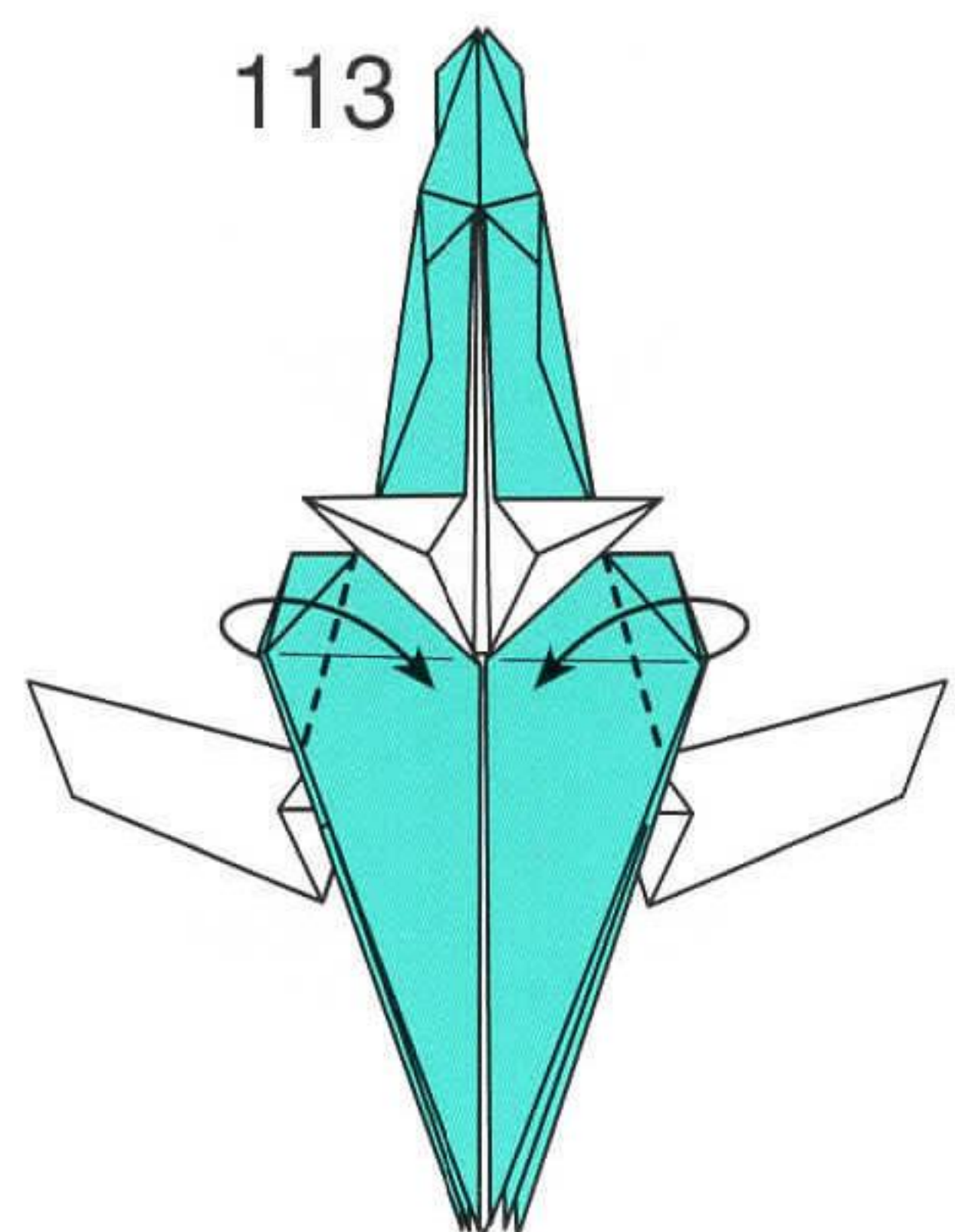
Stand up the top layer while stretching the lower layer.



Inflate the standing layer to be a pyramid, then flatten it and fold down.

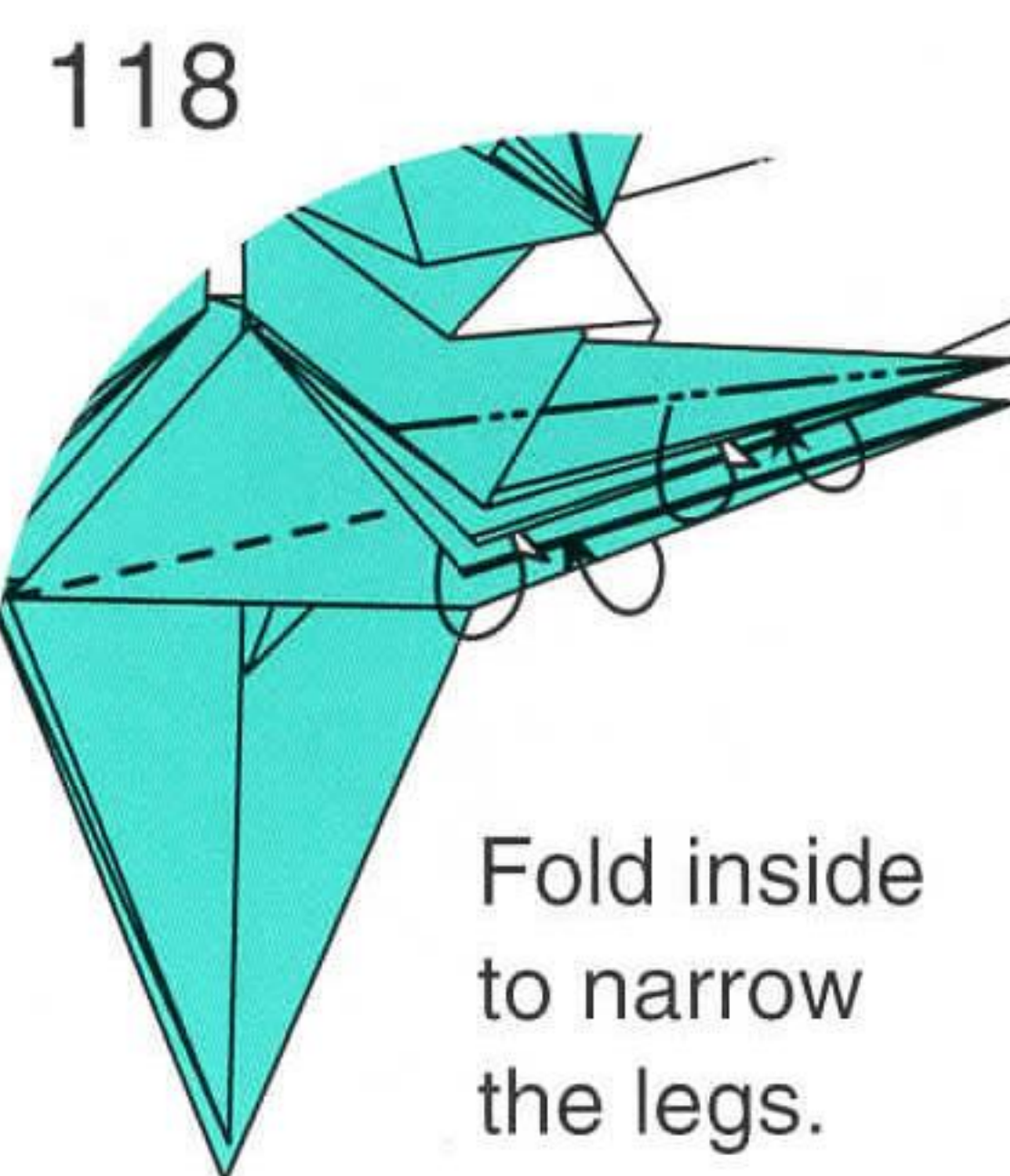
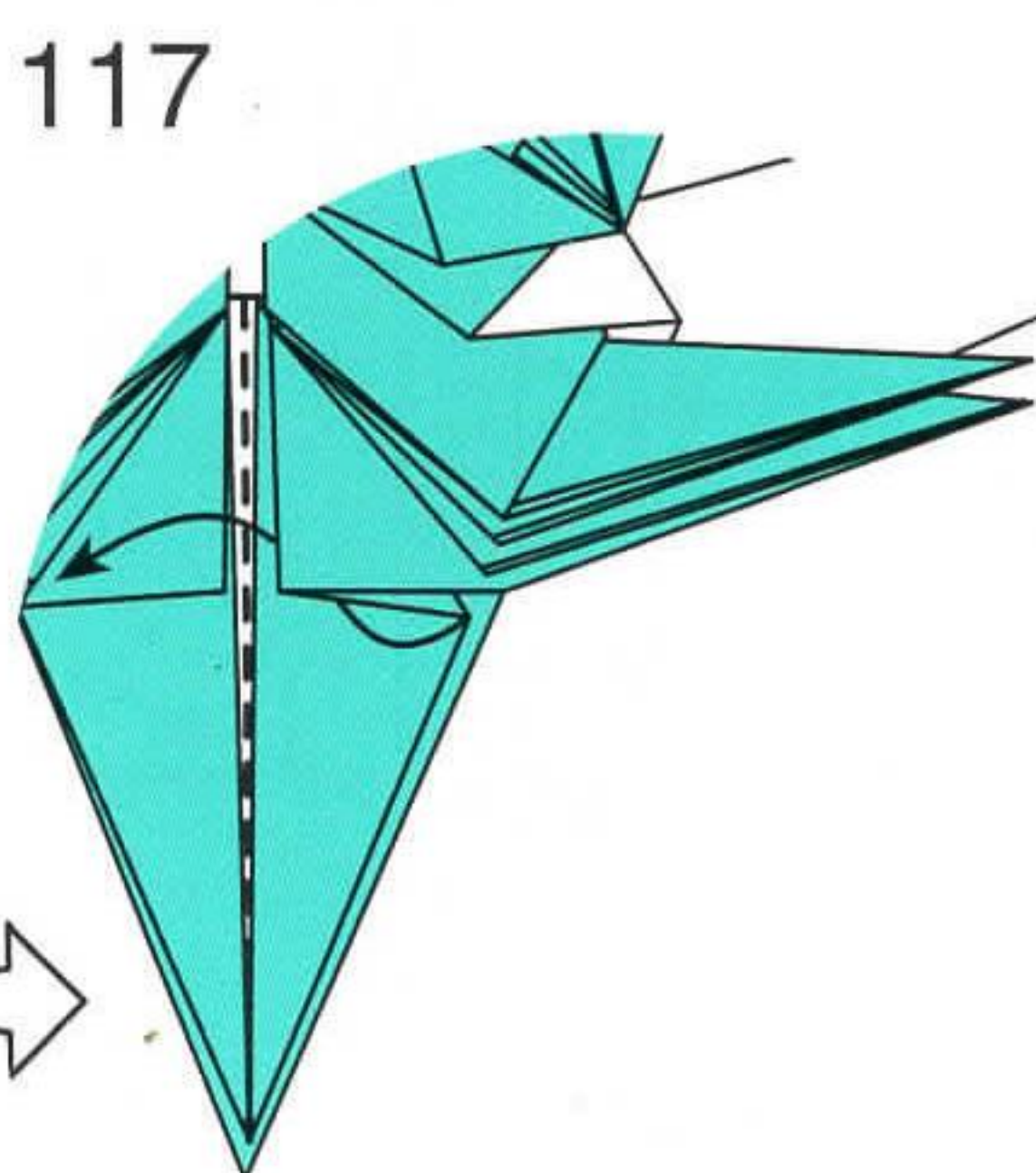
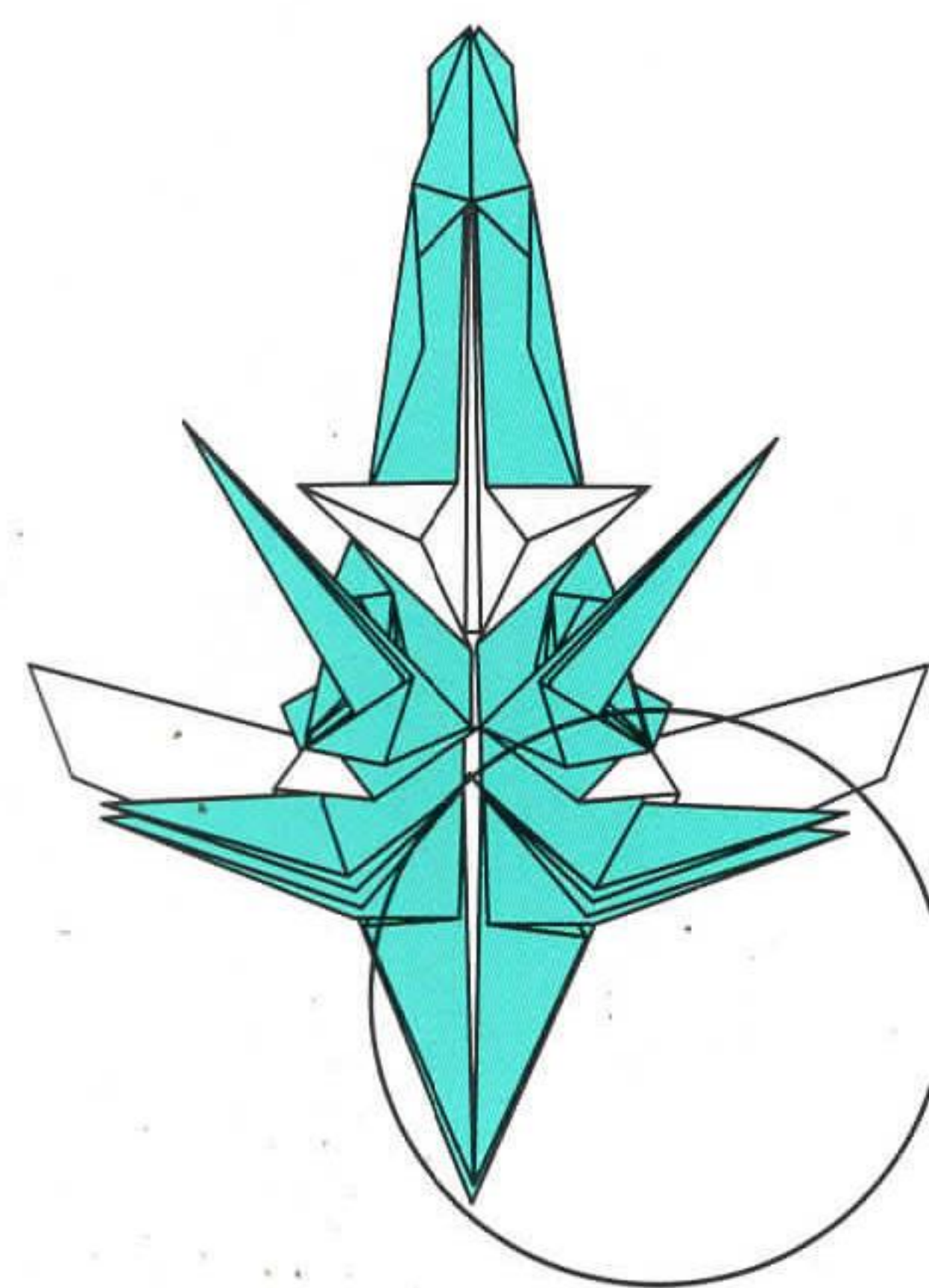


Repeat step 111.

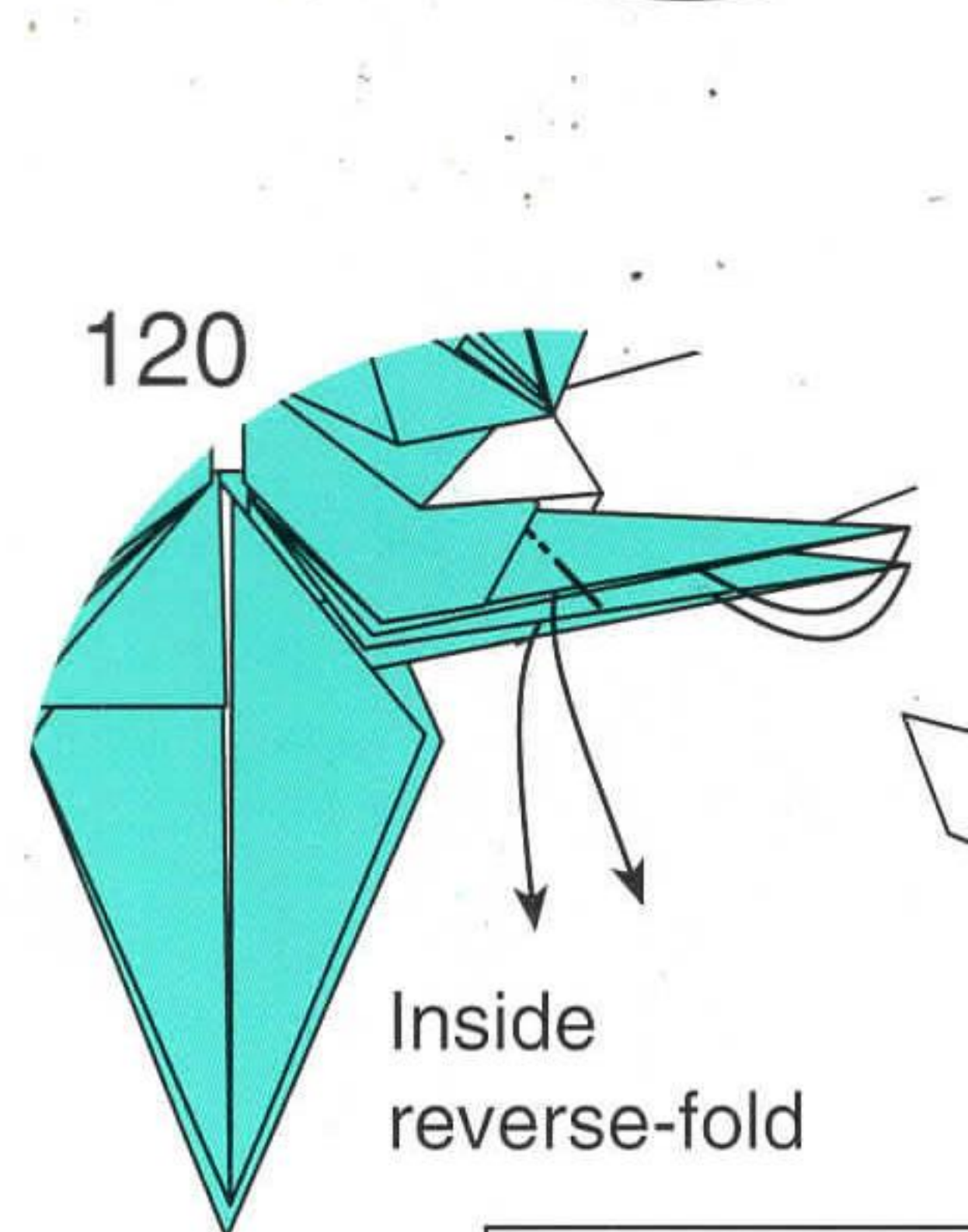
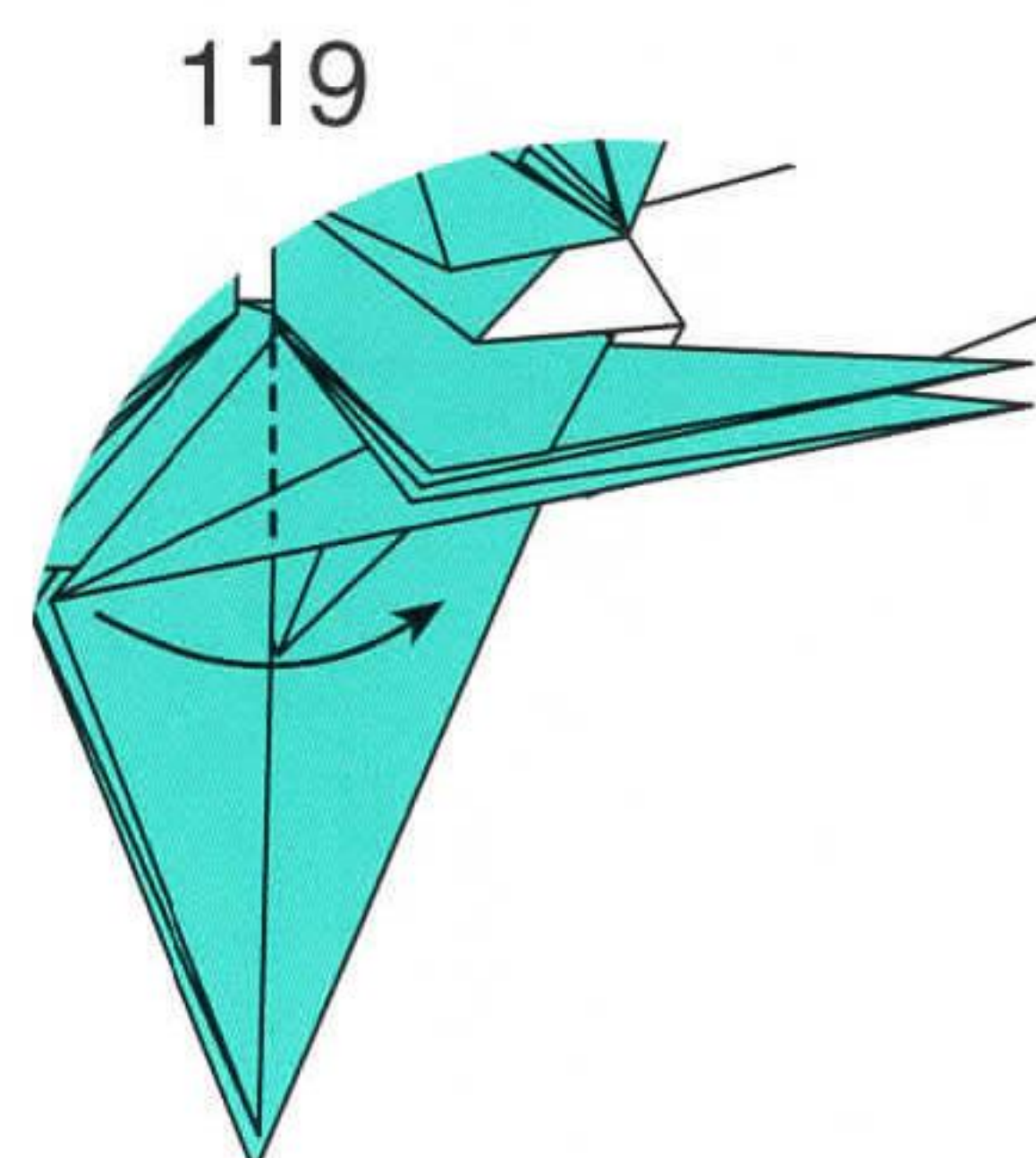


Swivel-fold

Inside reverse-fold at the roots

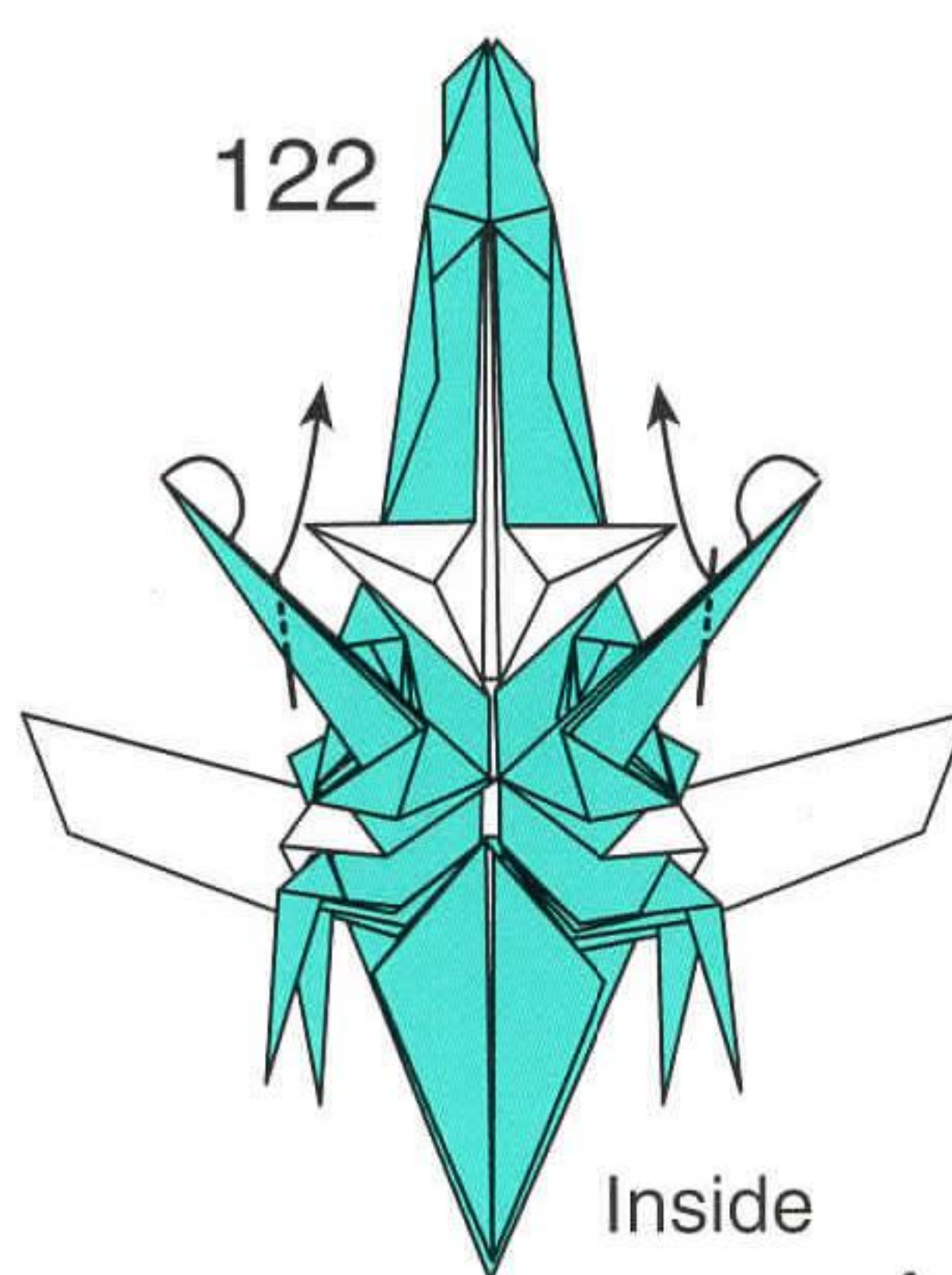
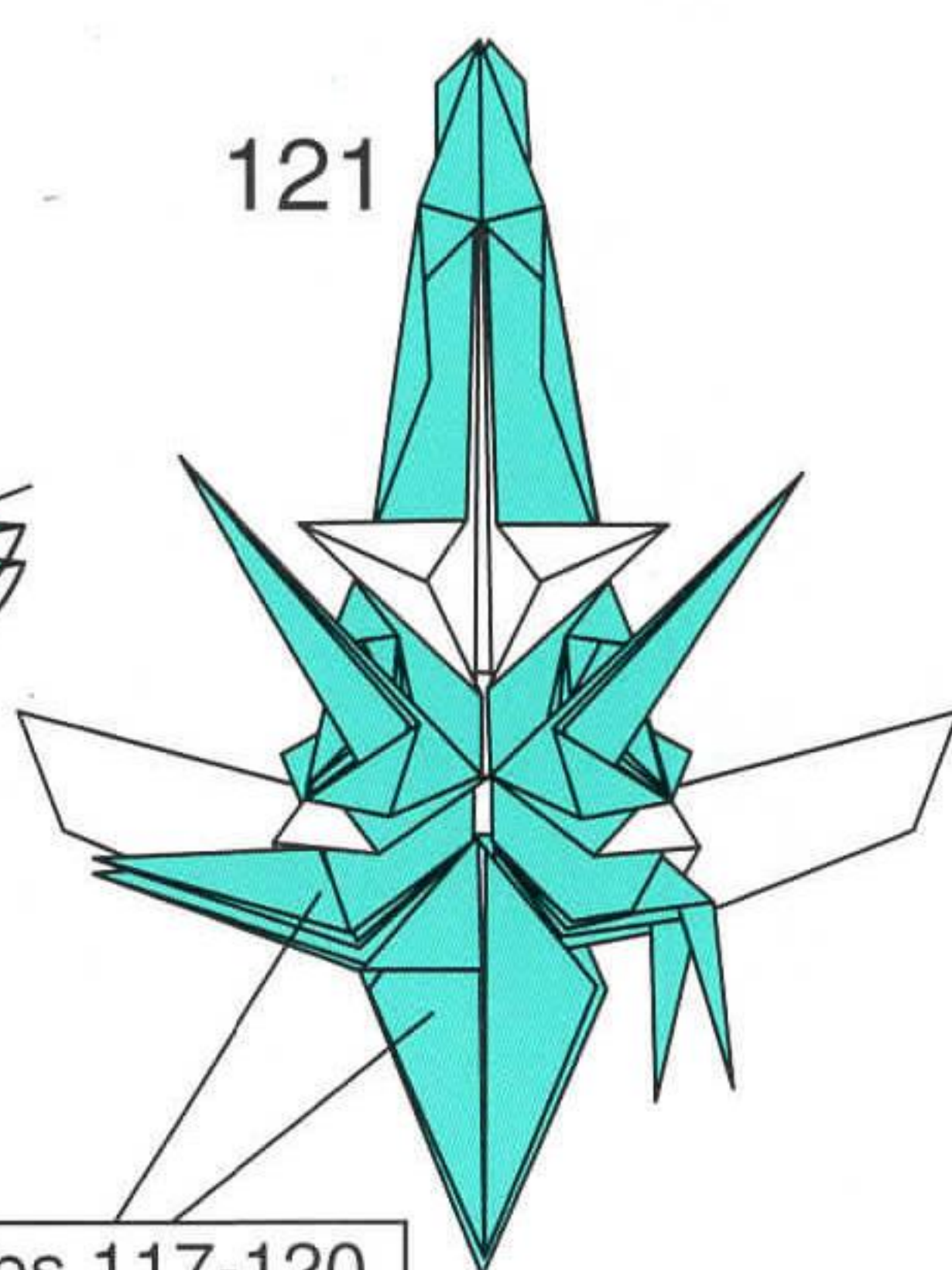


Fold inside to narrow the legs.

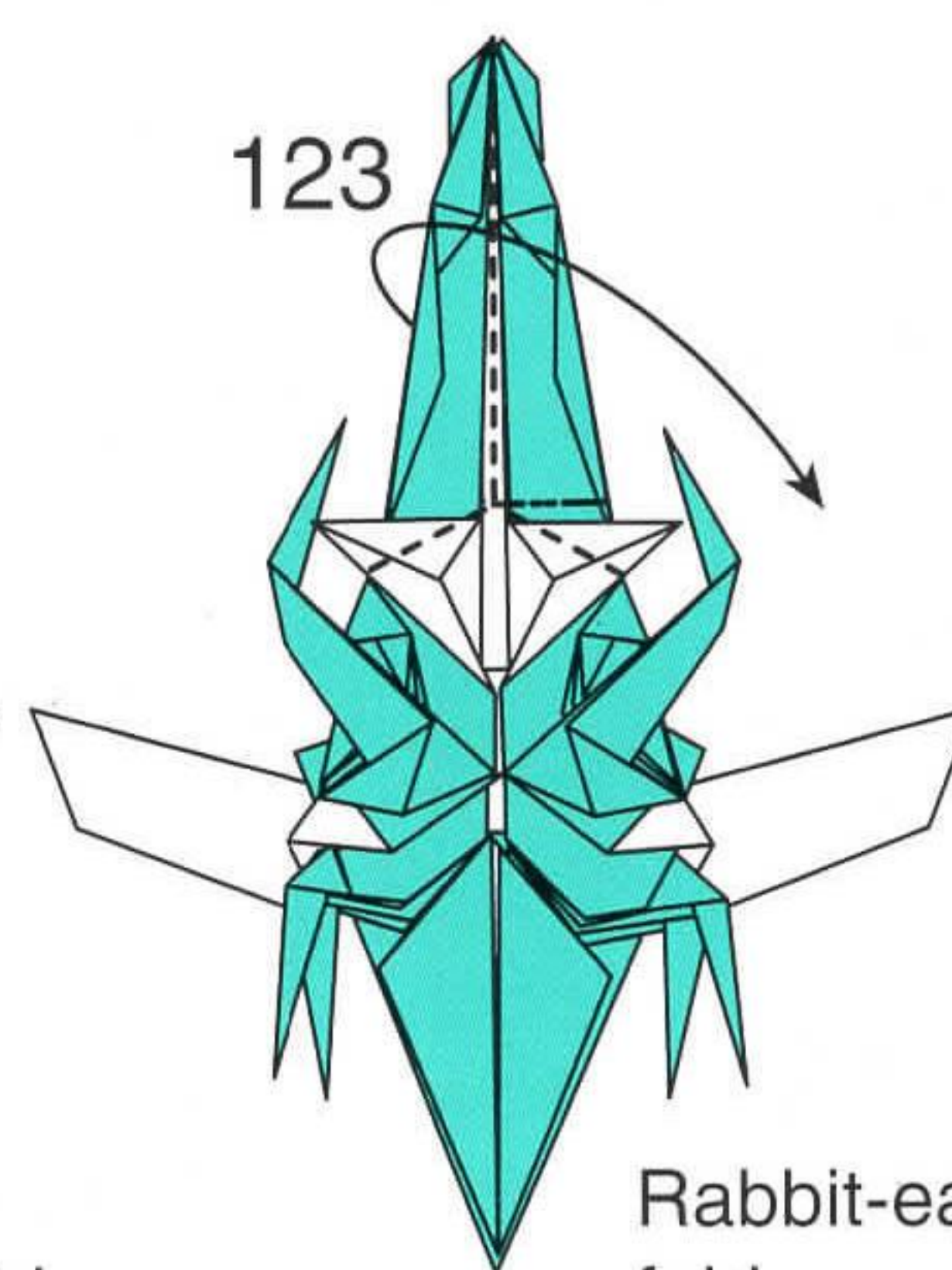


Inside reverse-fold

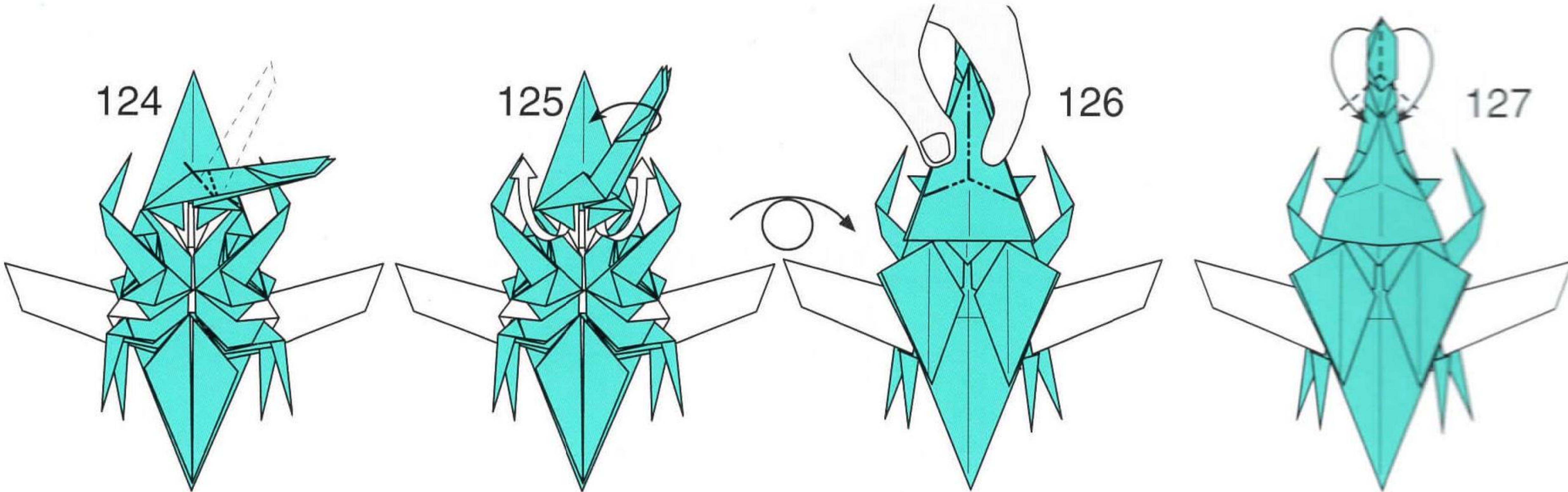
Repeat steps 117-120.



Inside reverse-fold



Rabbit-ear-fold

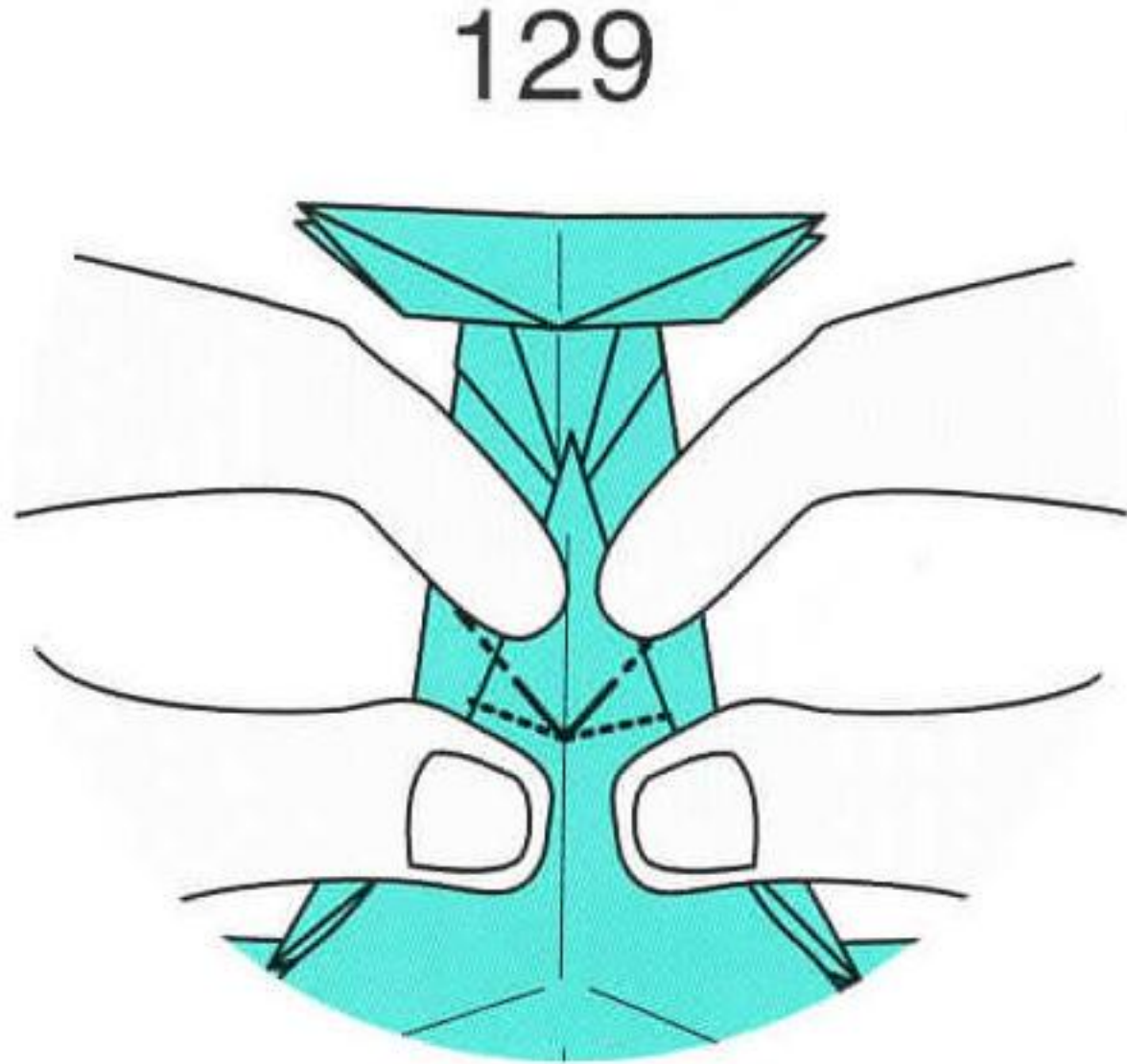
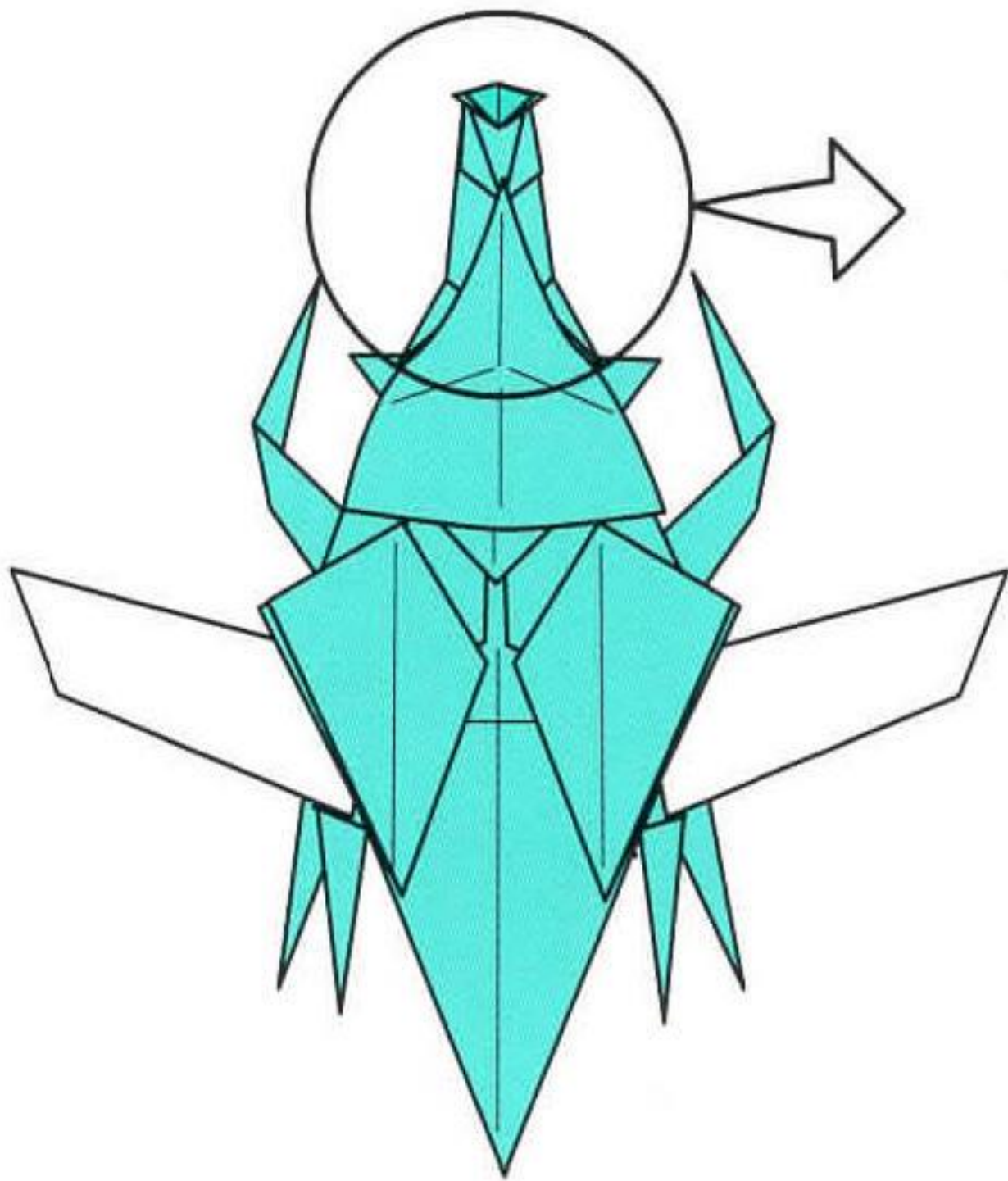


Inside reverse-fold twice to create an angle of the horn.

Pull out the antennae while standing up the horn.

Pinch.

Outside reverse-fold

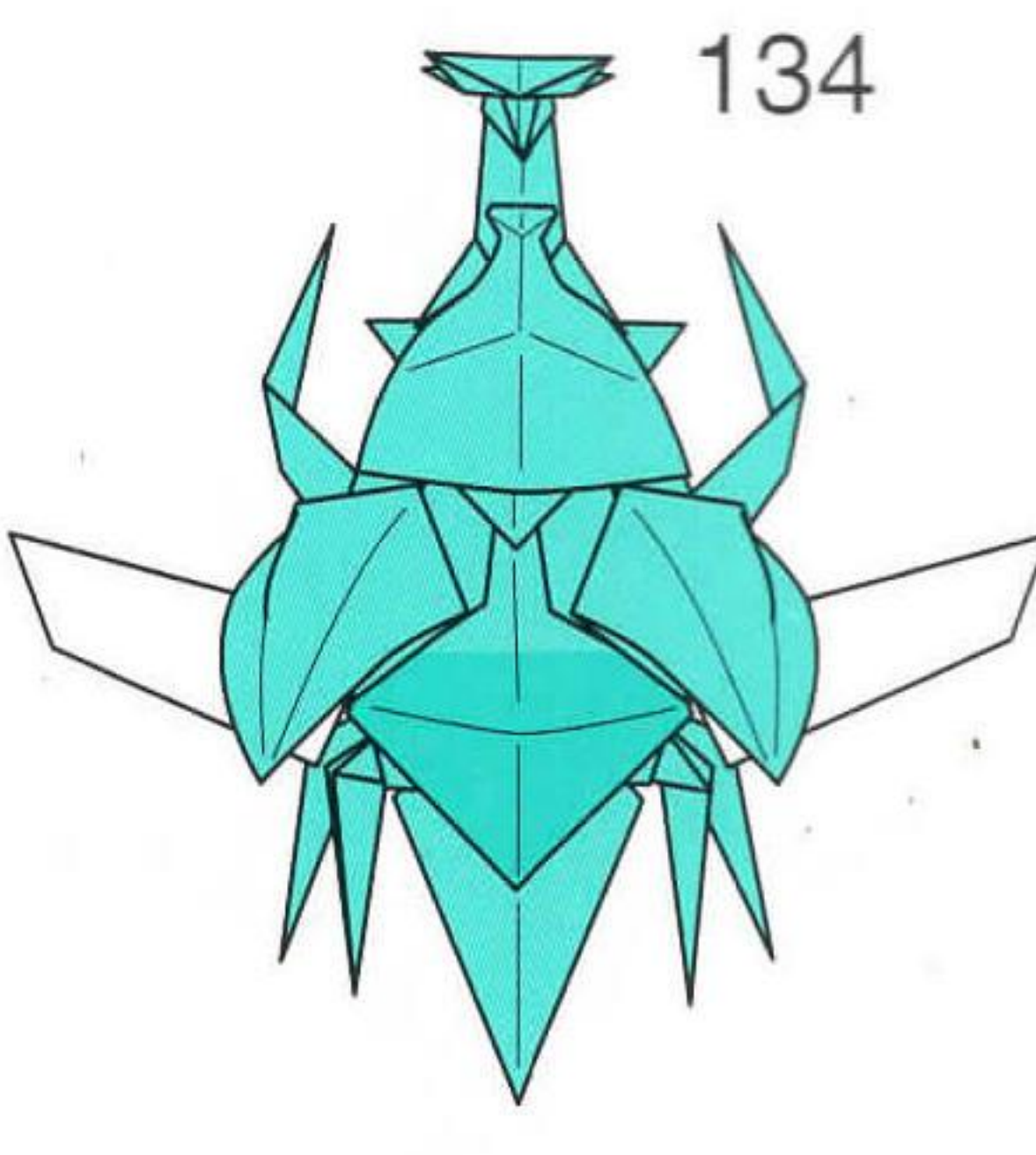
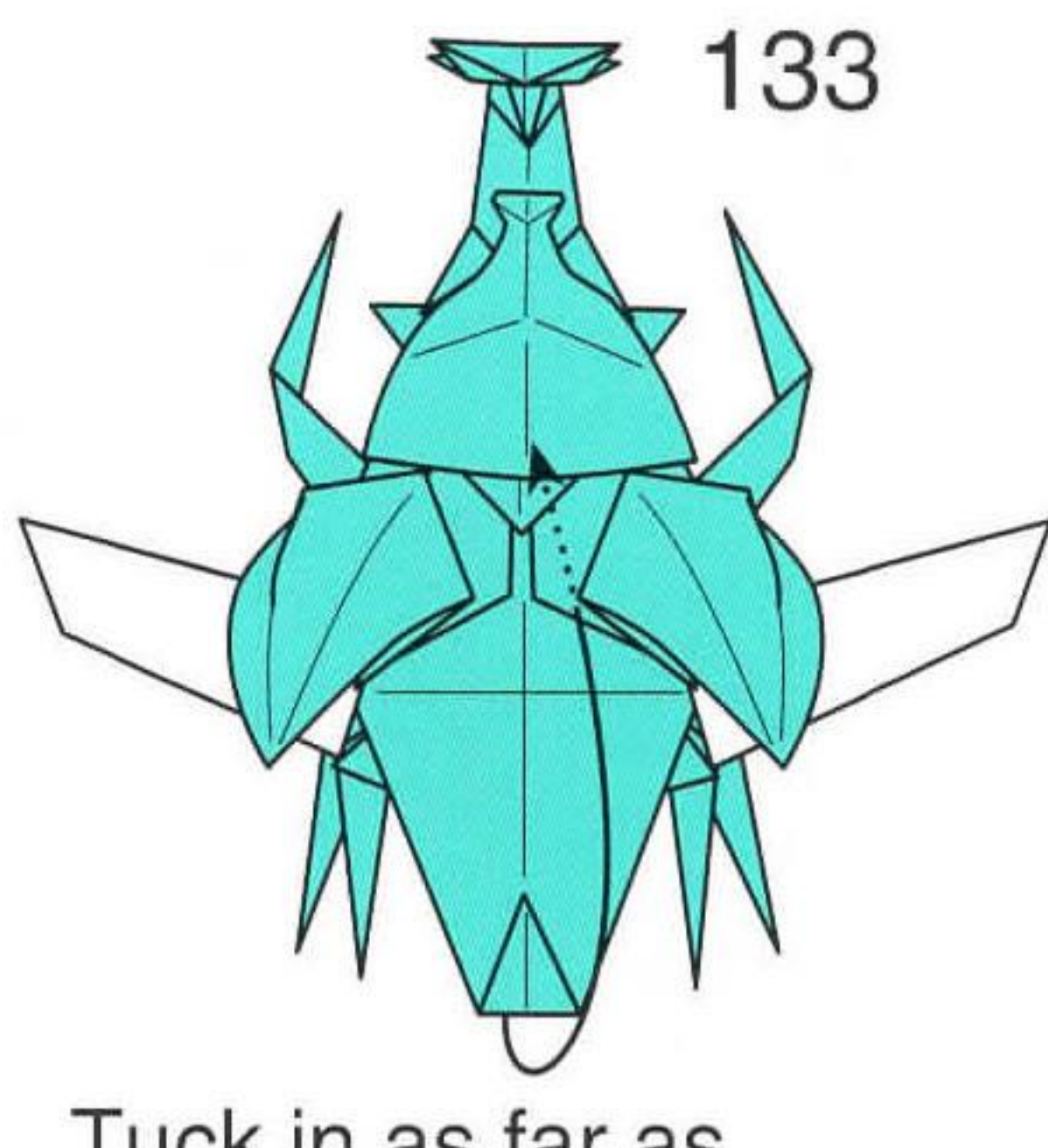
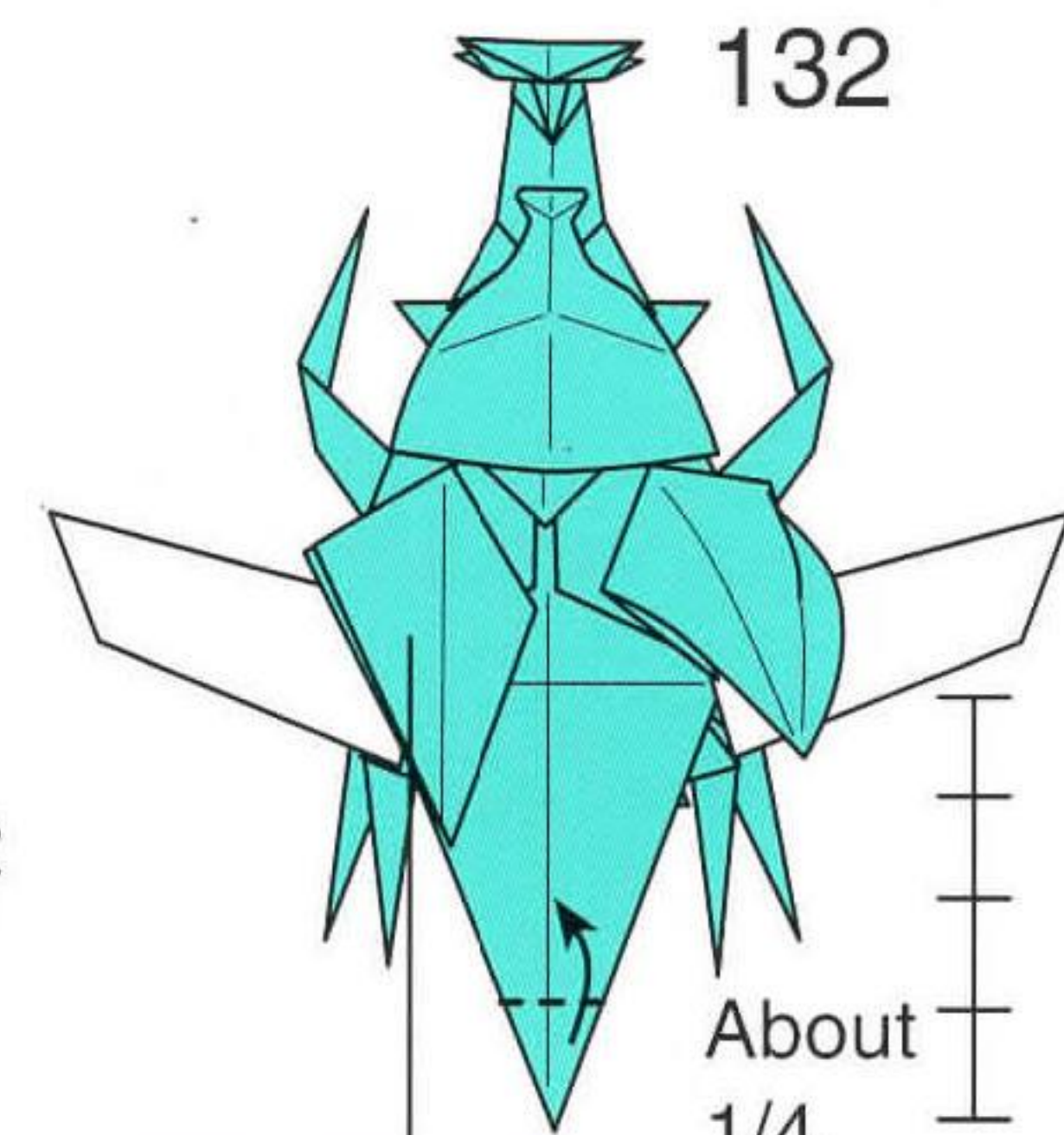
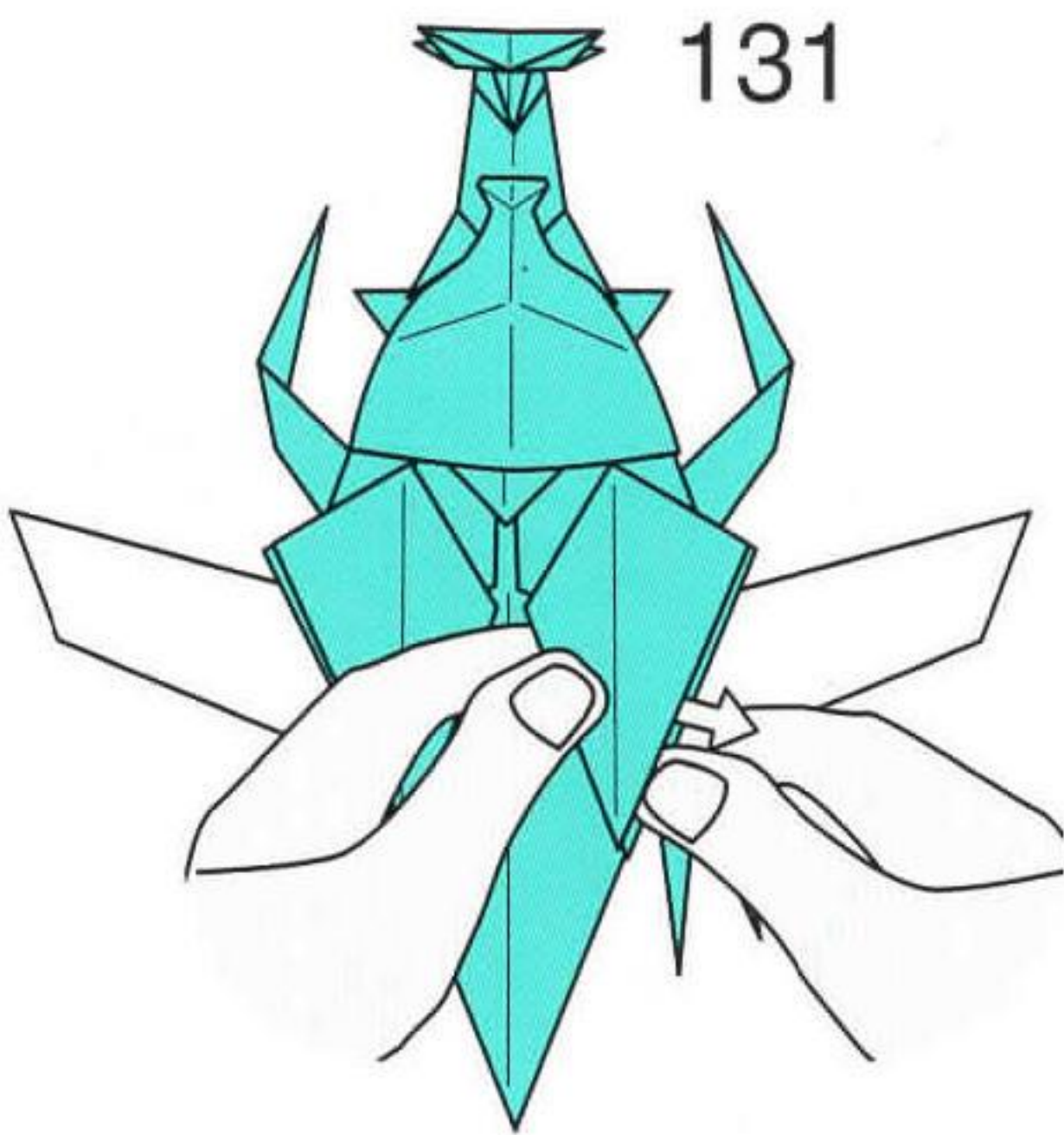


128

129

130

Pinch.



131

132

133

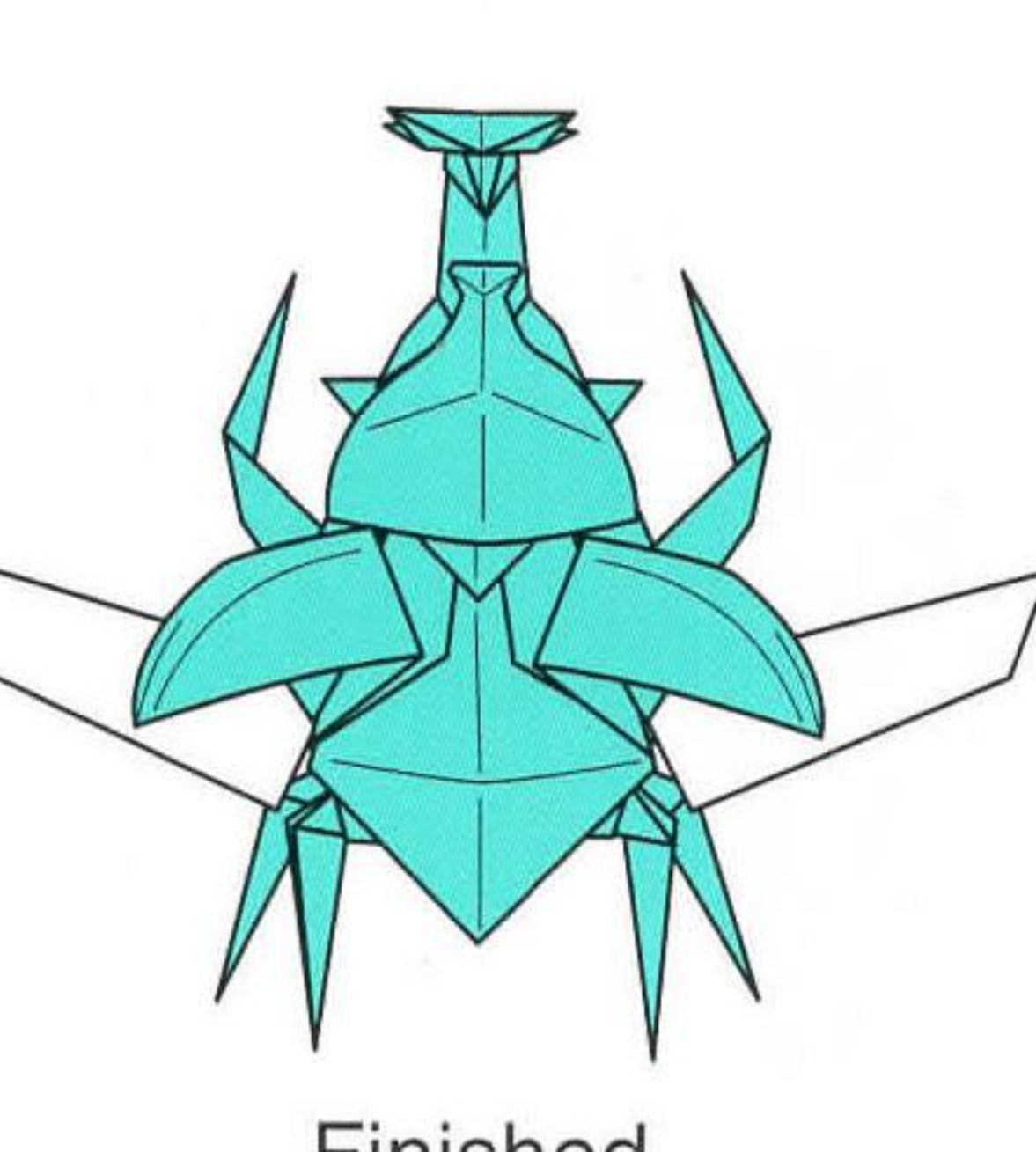
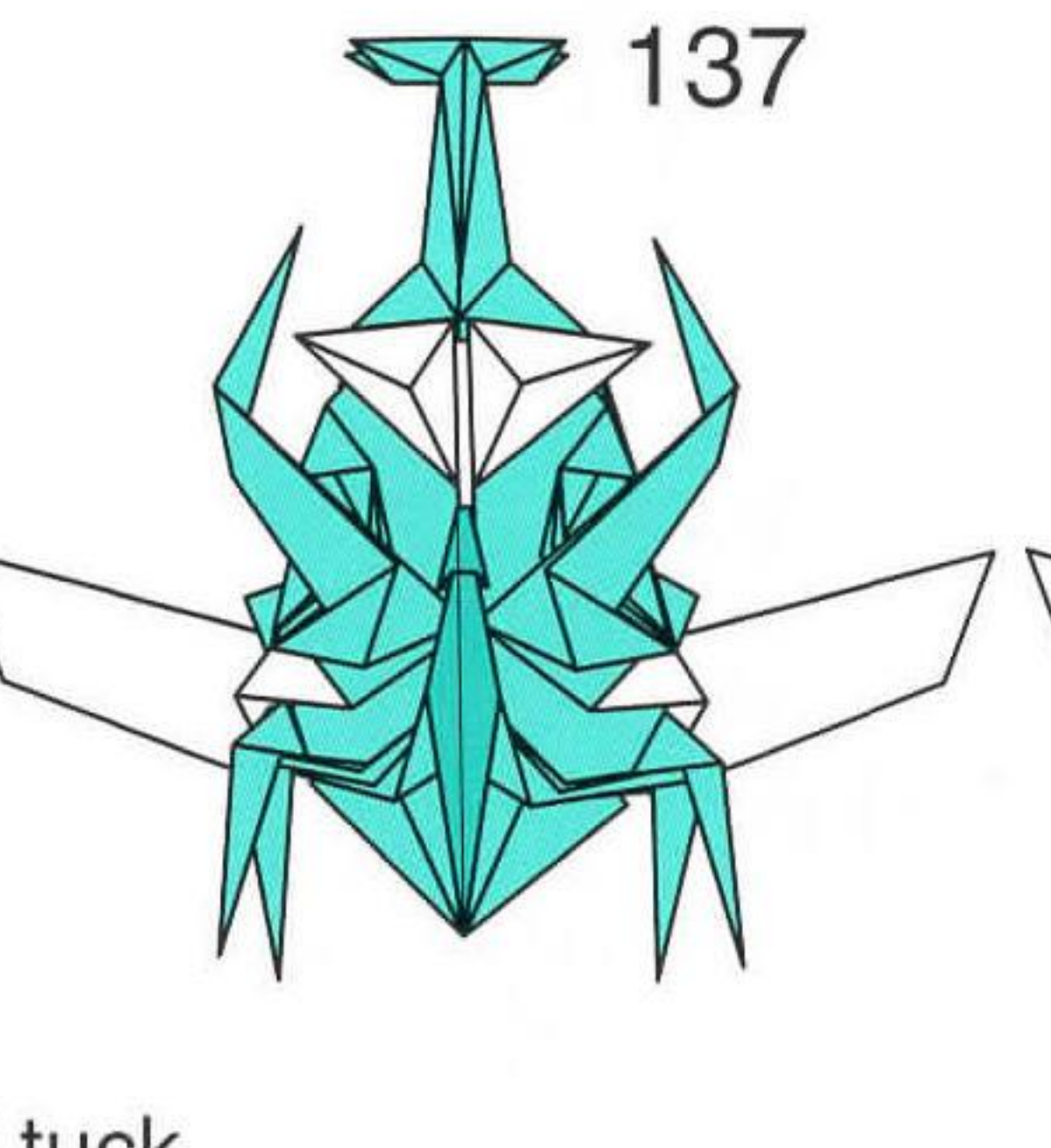
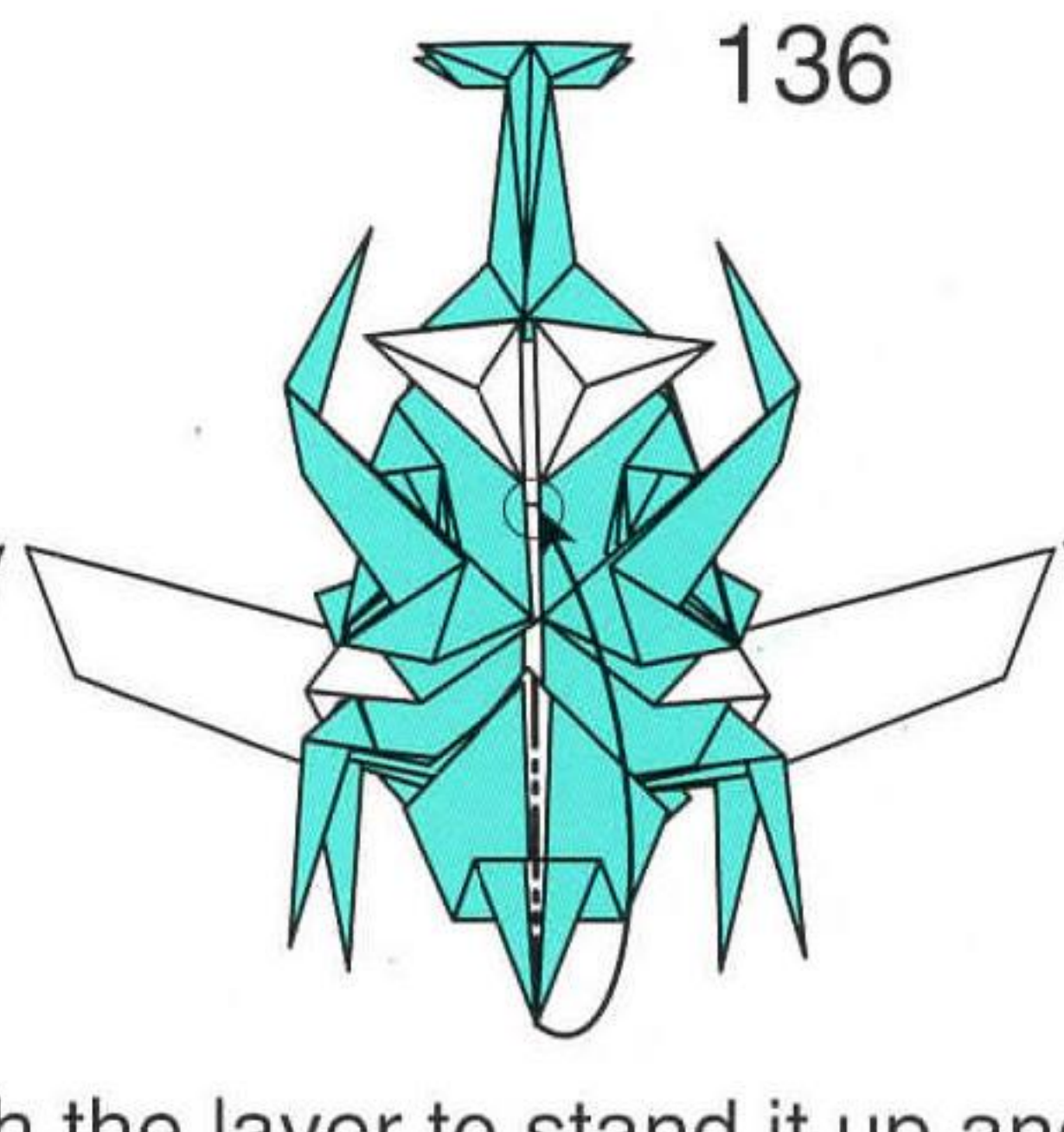
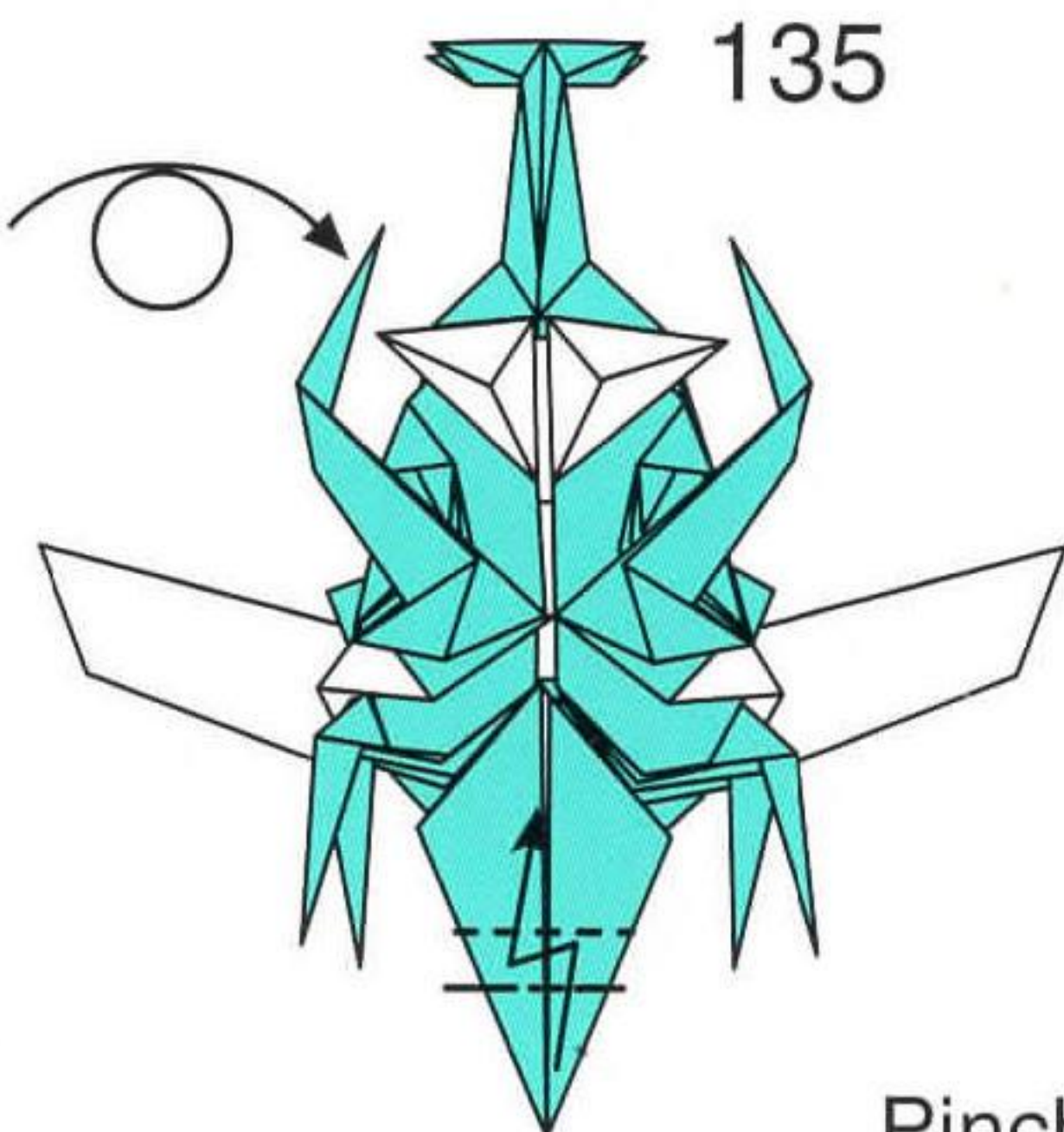
134

Pull out the second layer to round the wing cases.

Repeat step 131.

About 1/4.

Tuck in as far as possible. The abdomen becomes round.



135

136

137

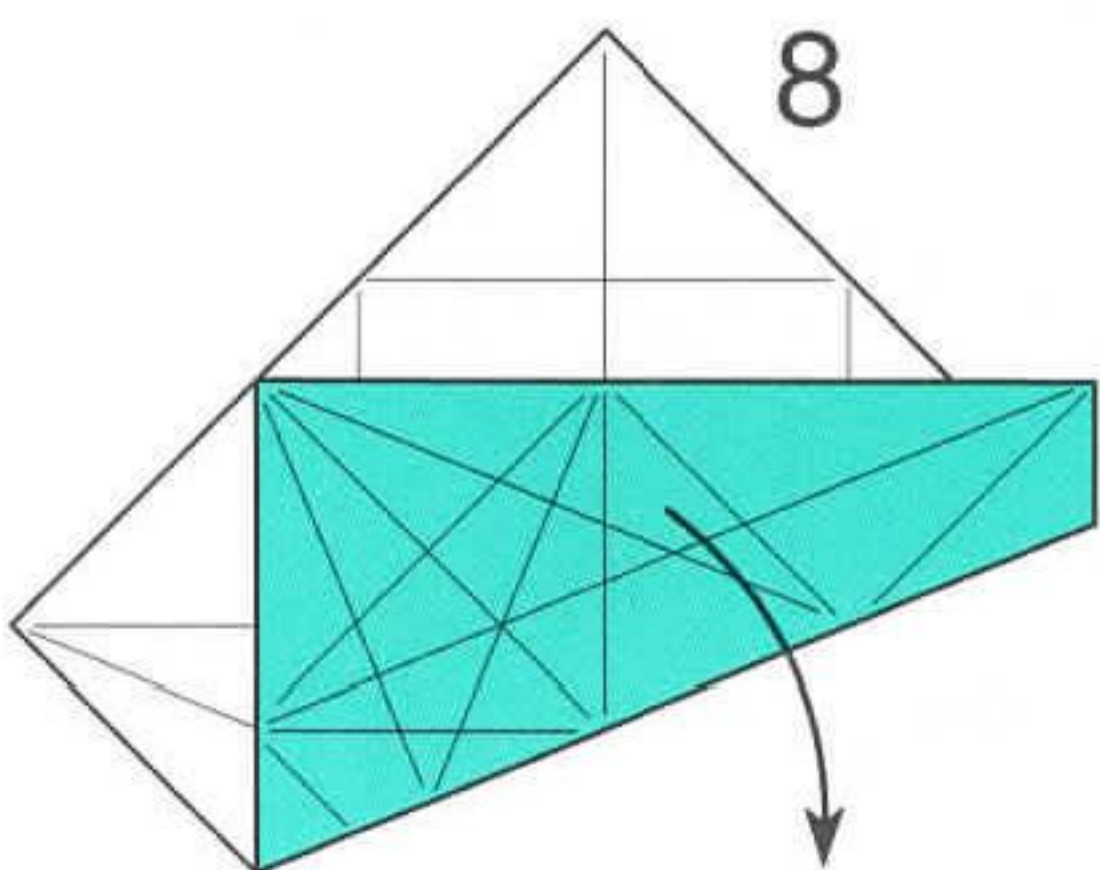
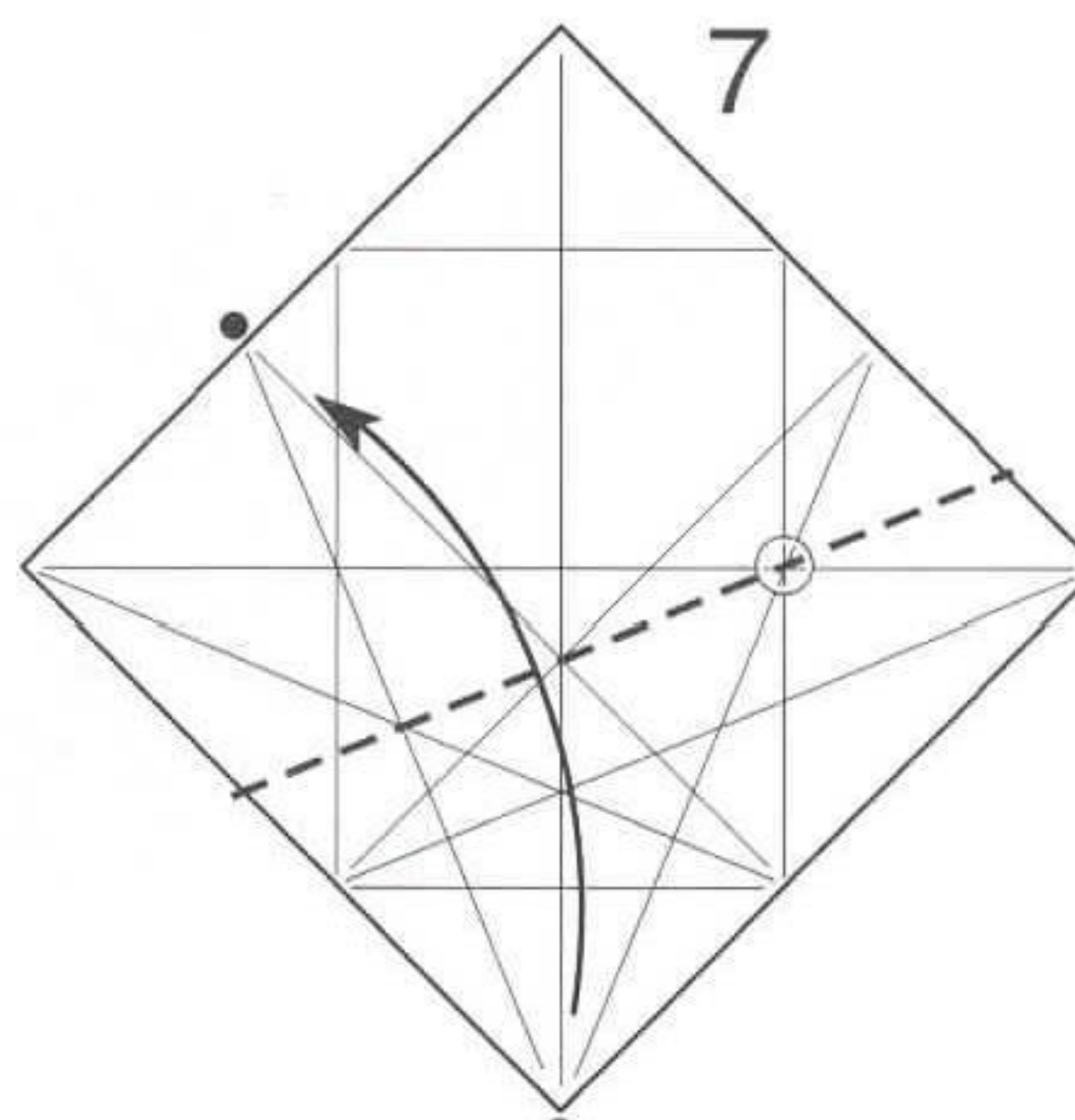
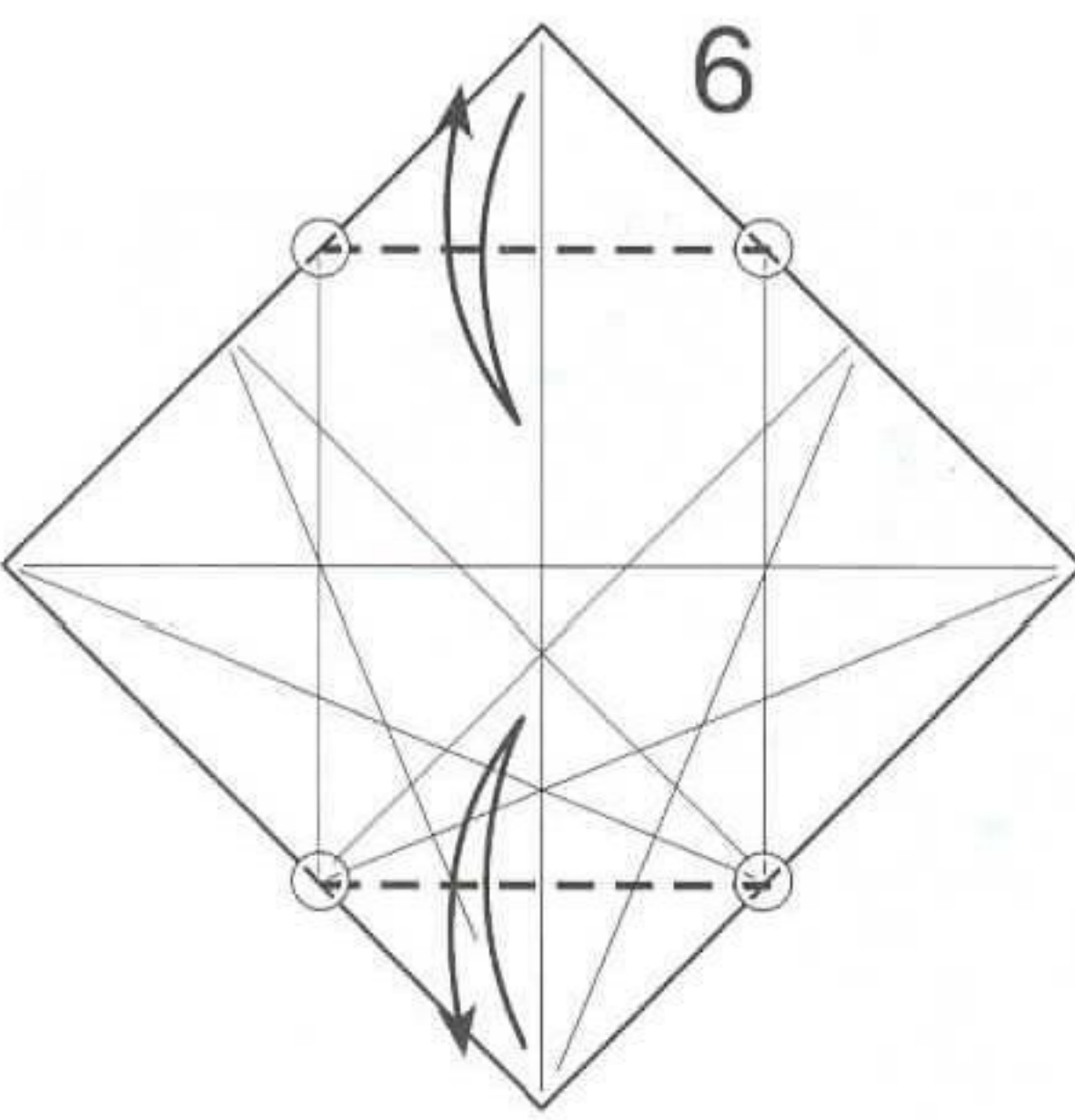
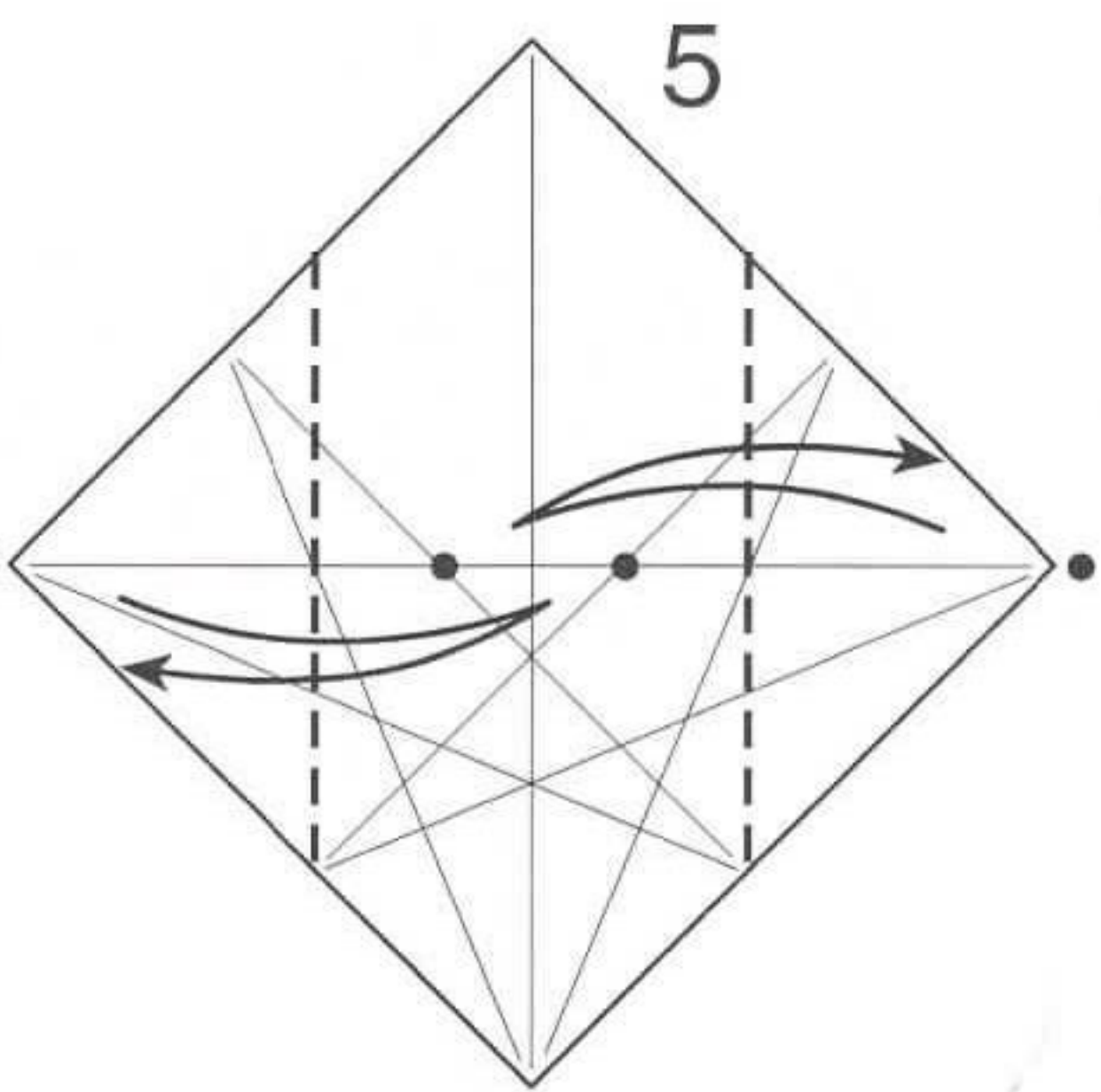
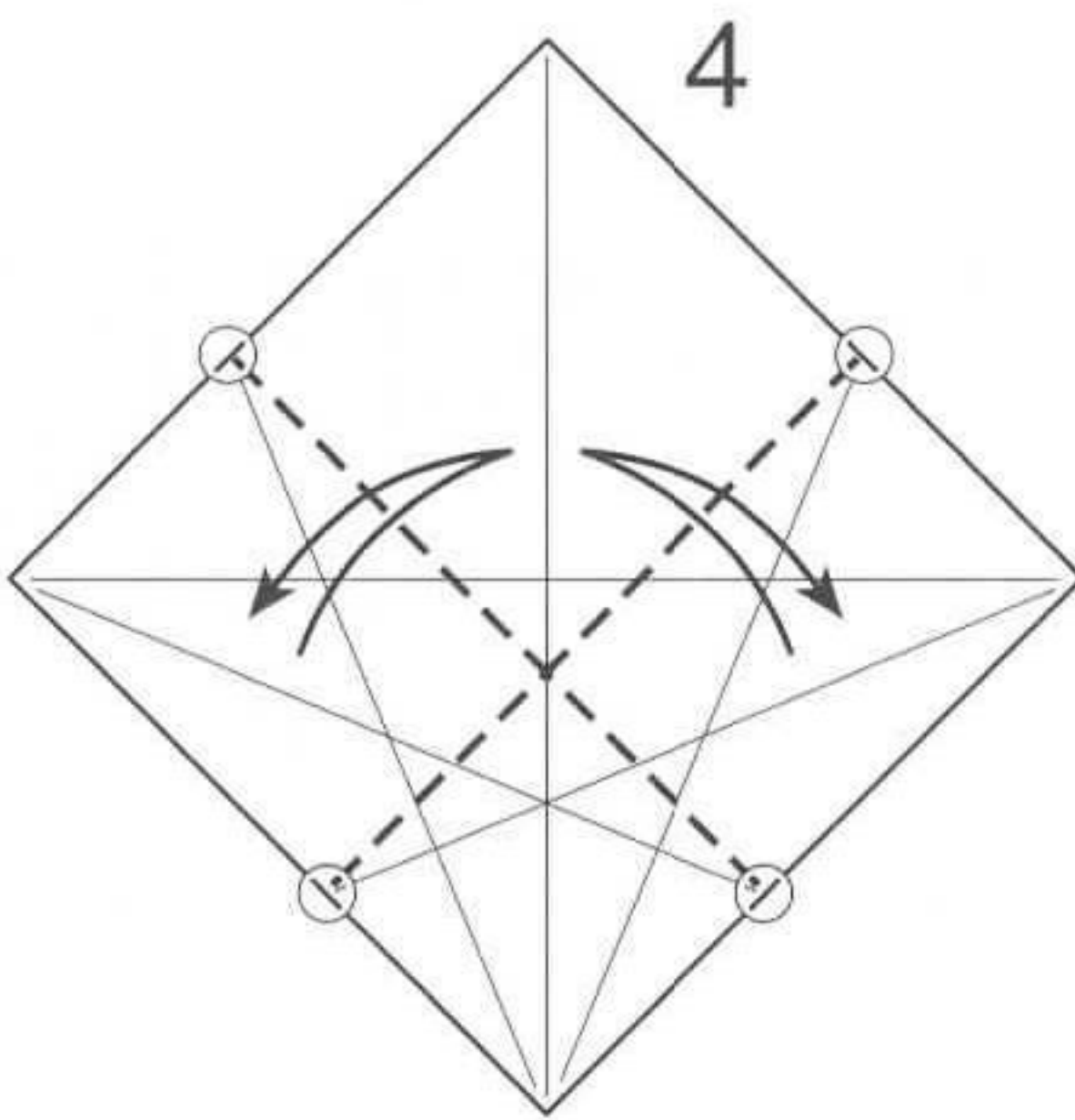
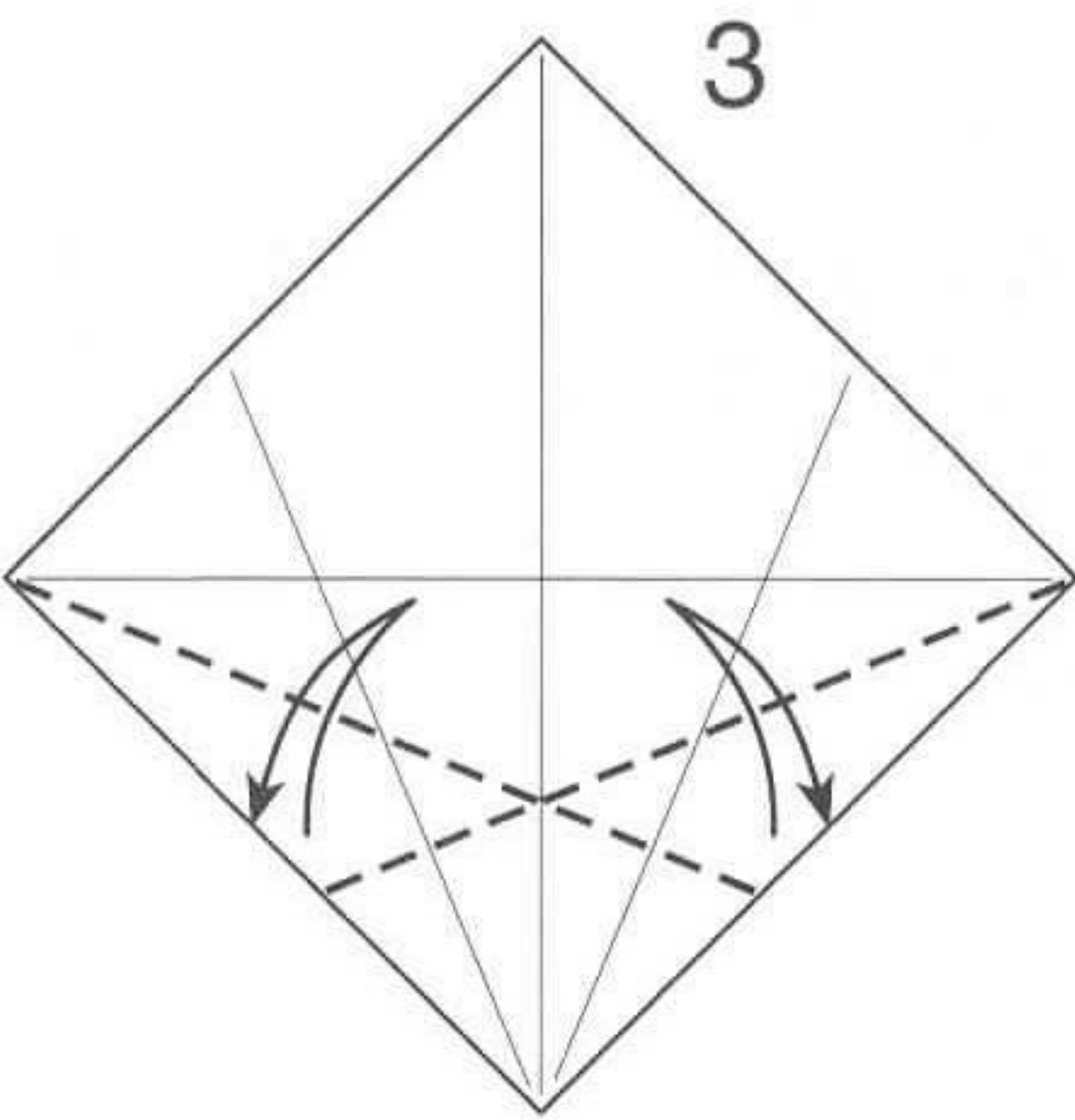
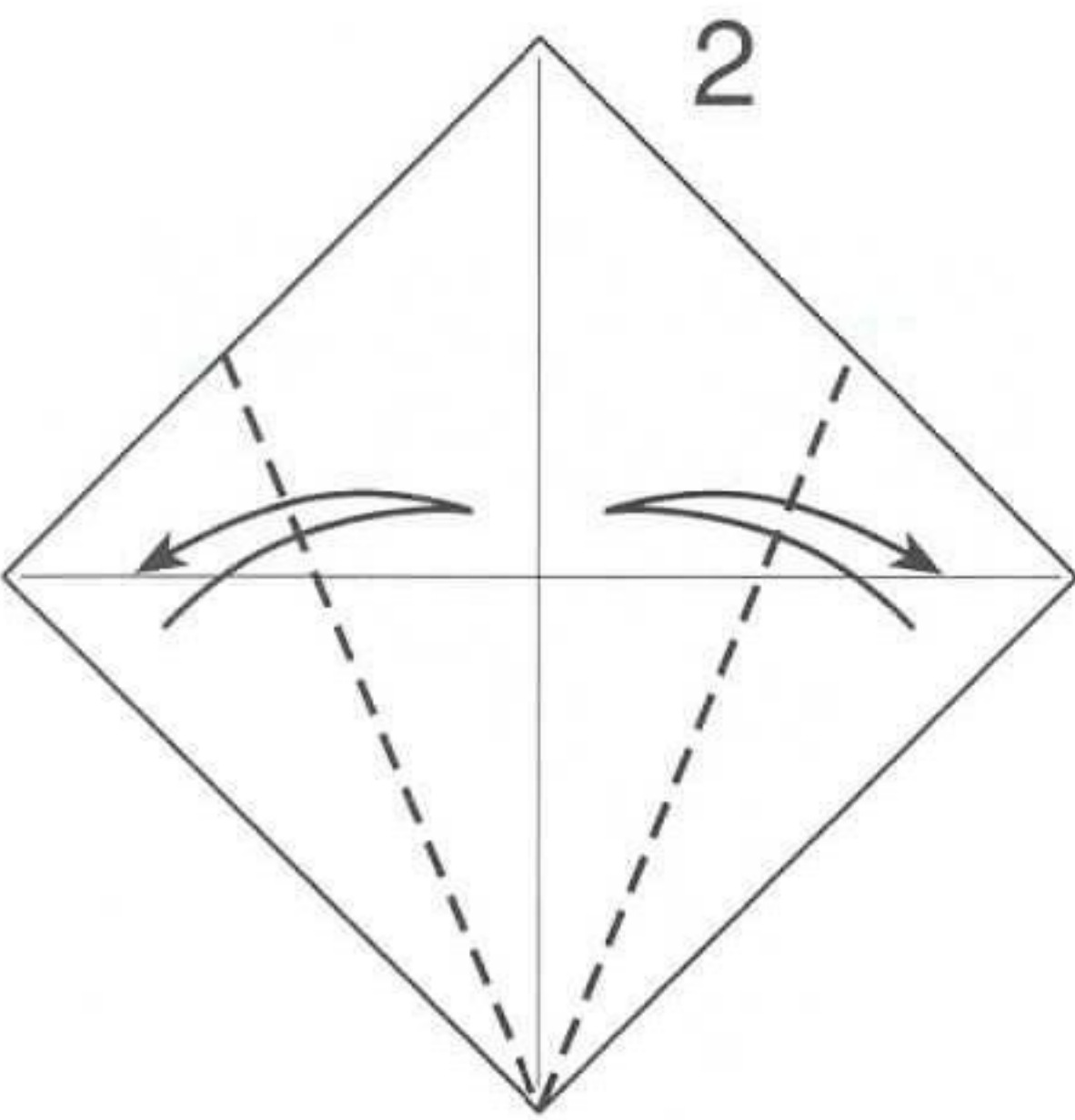
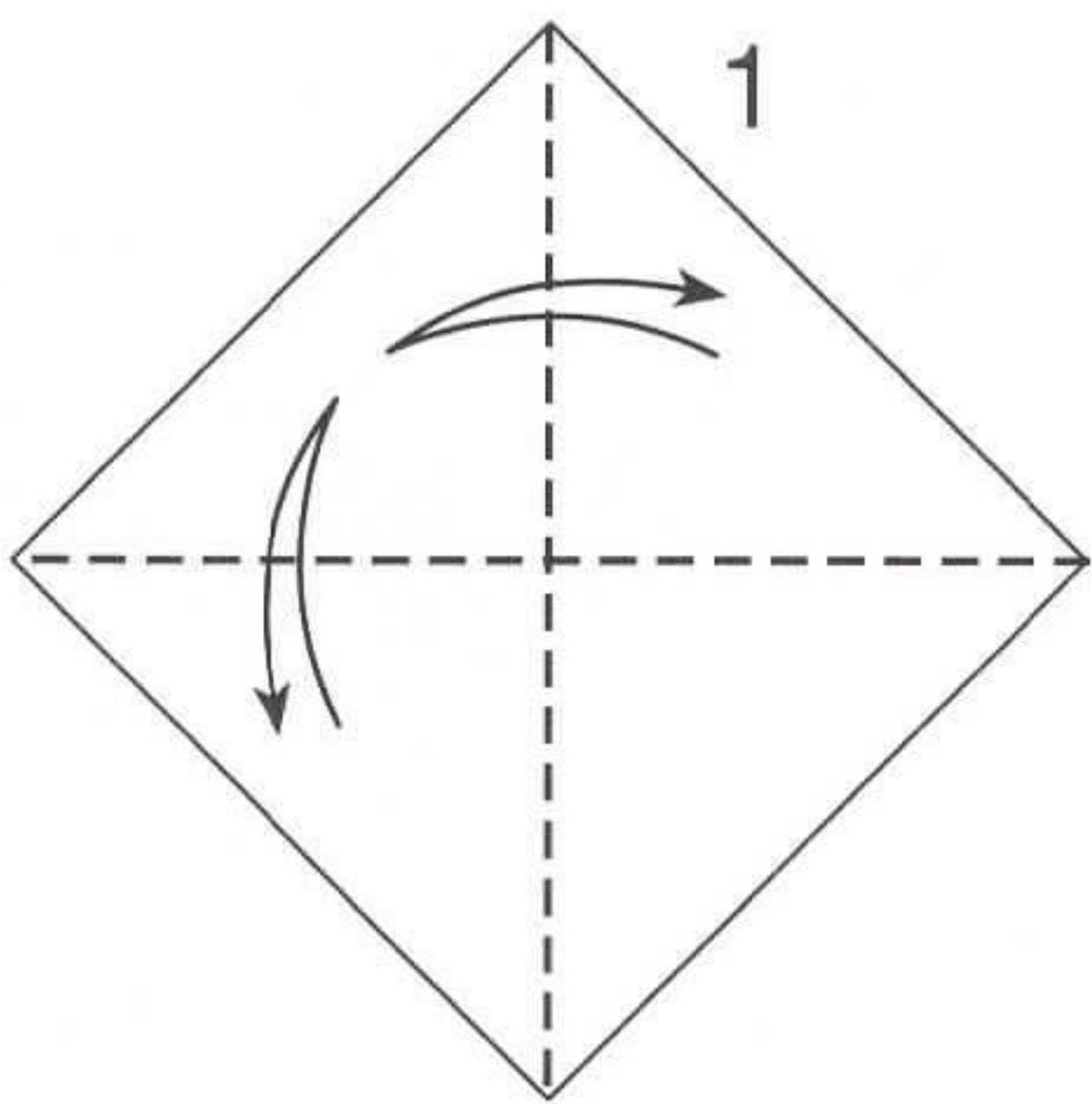
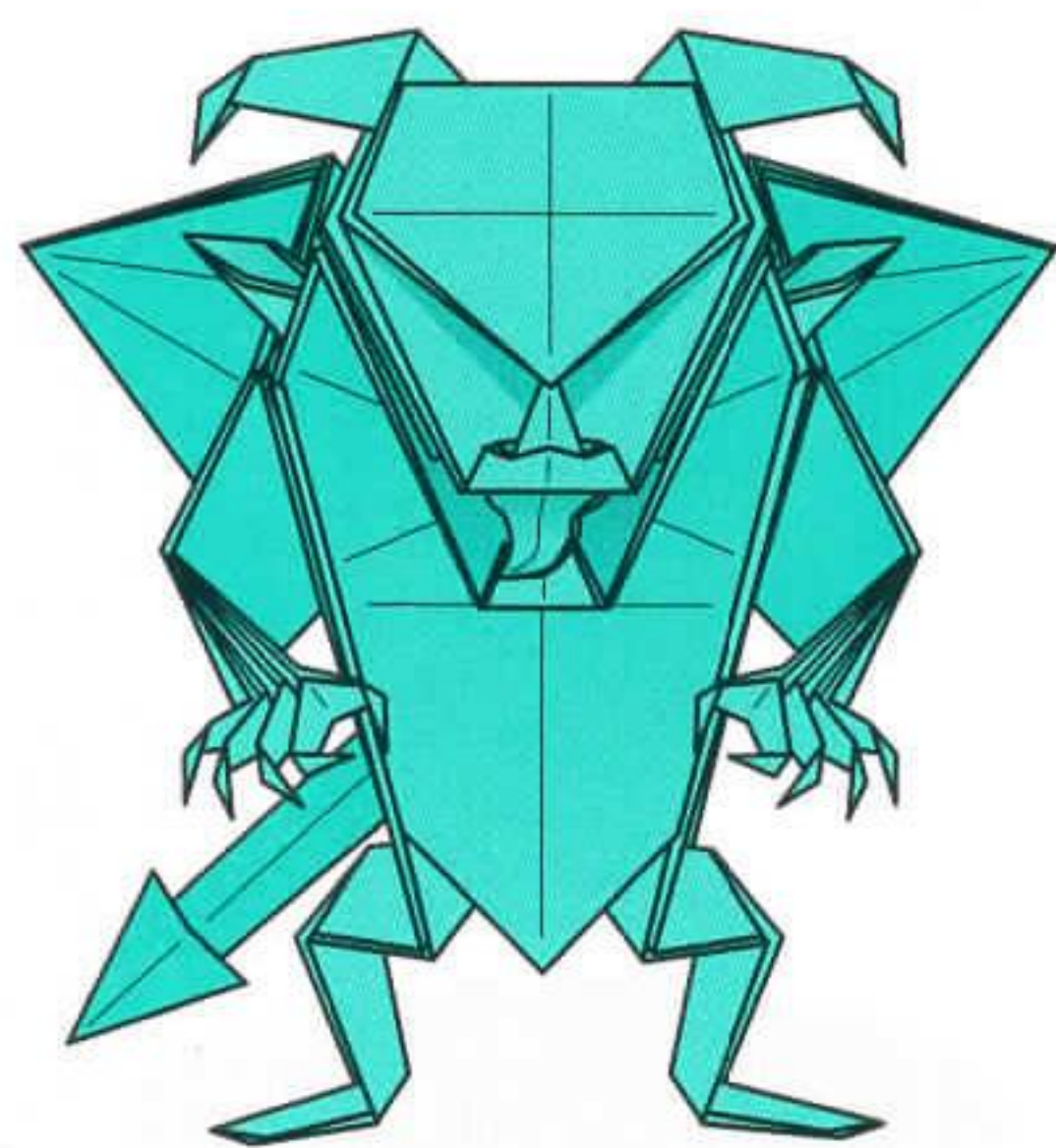
Pinch the layer to stand it up and tuck into the gap indicated by the circle.

Finished.

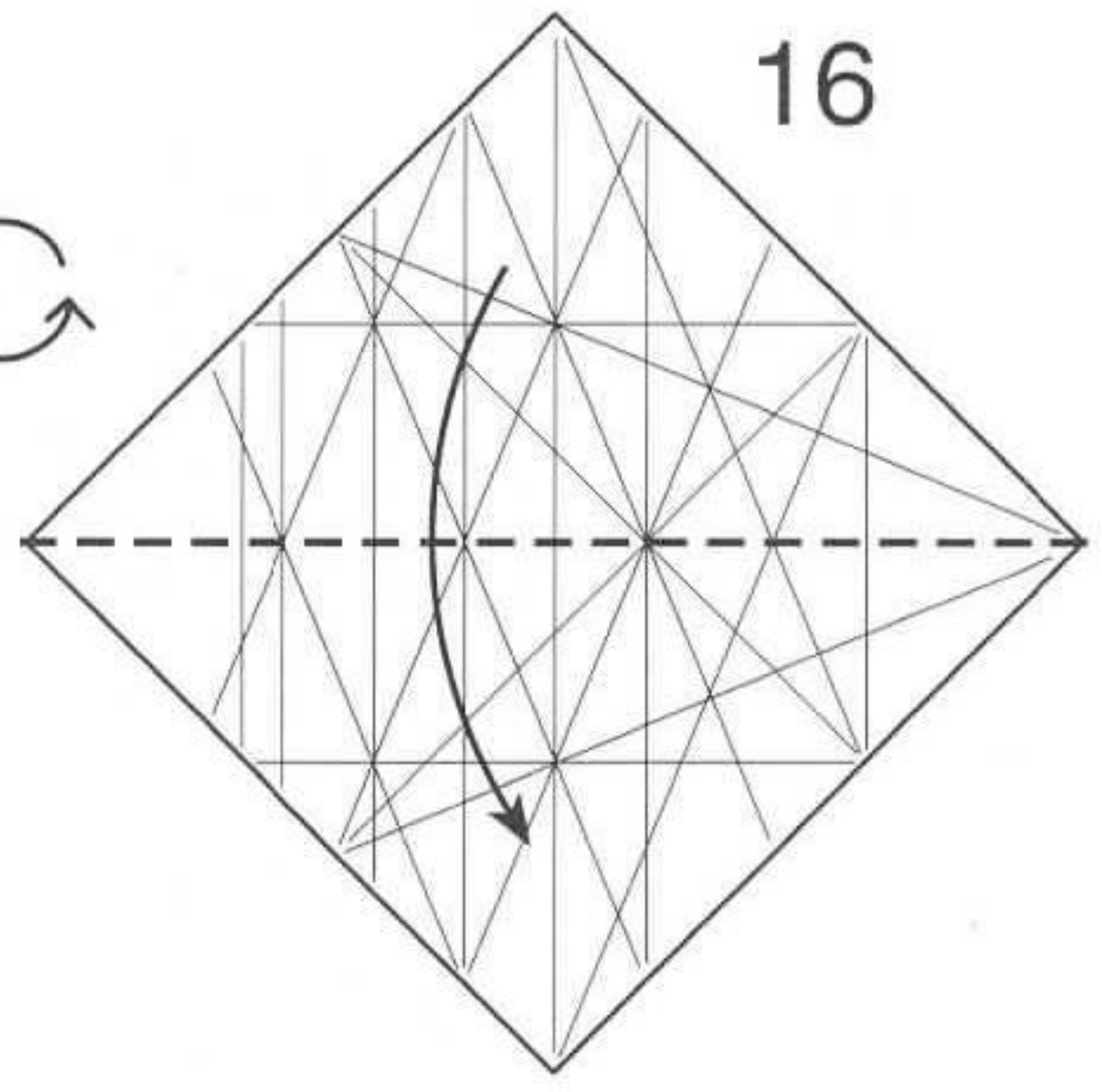
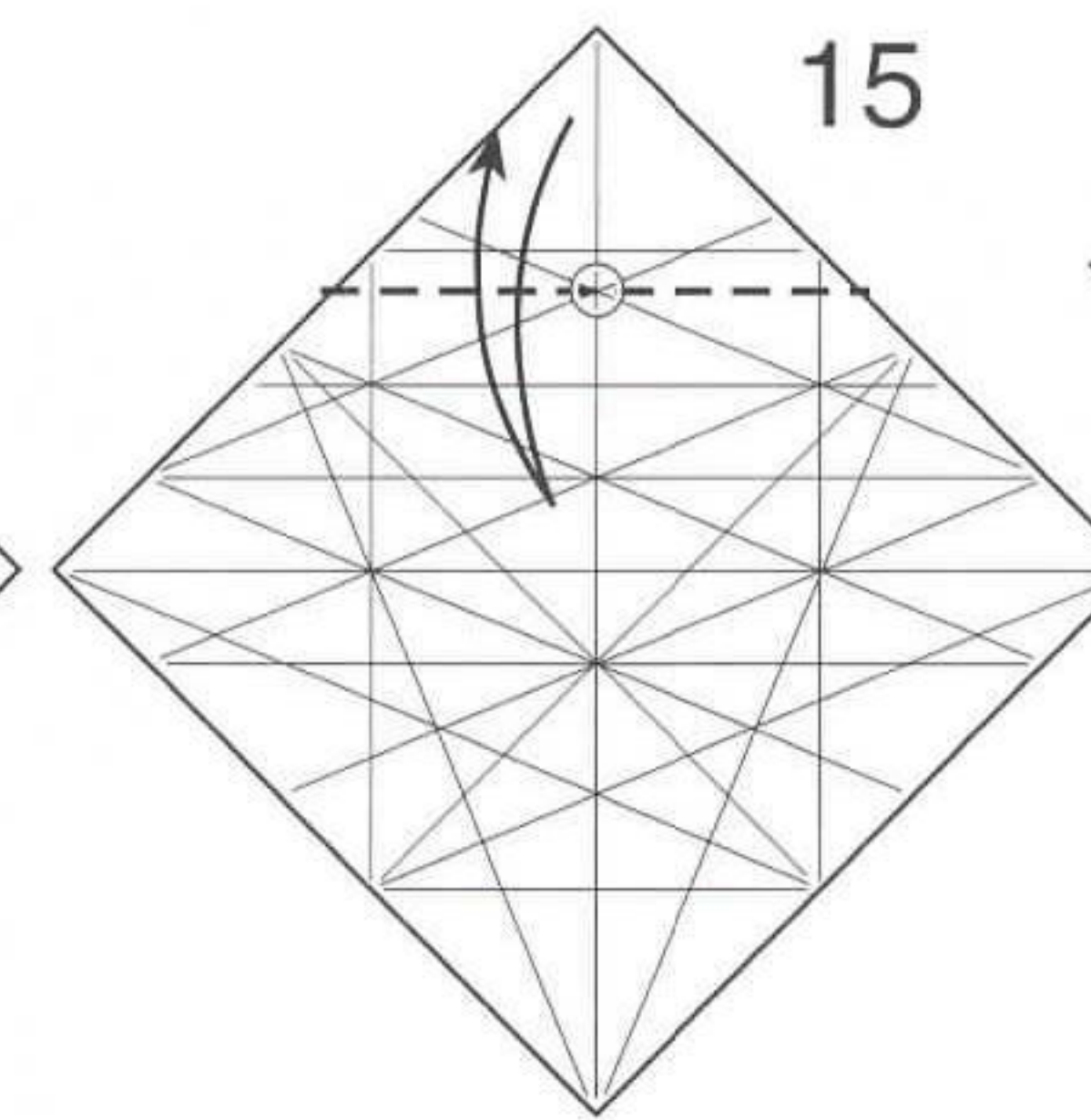
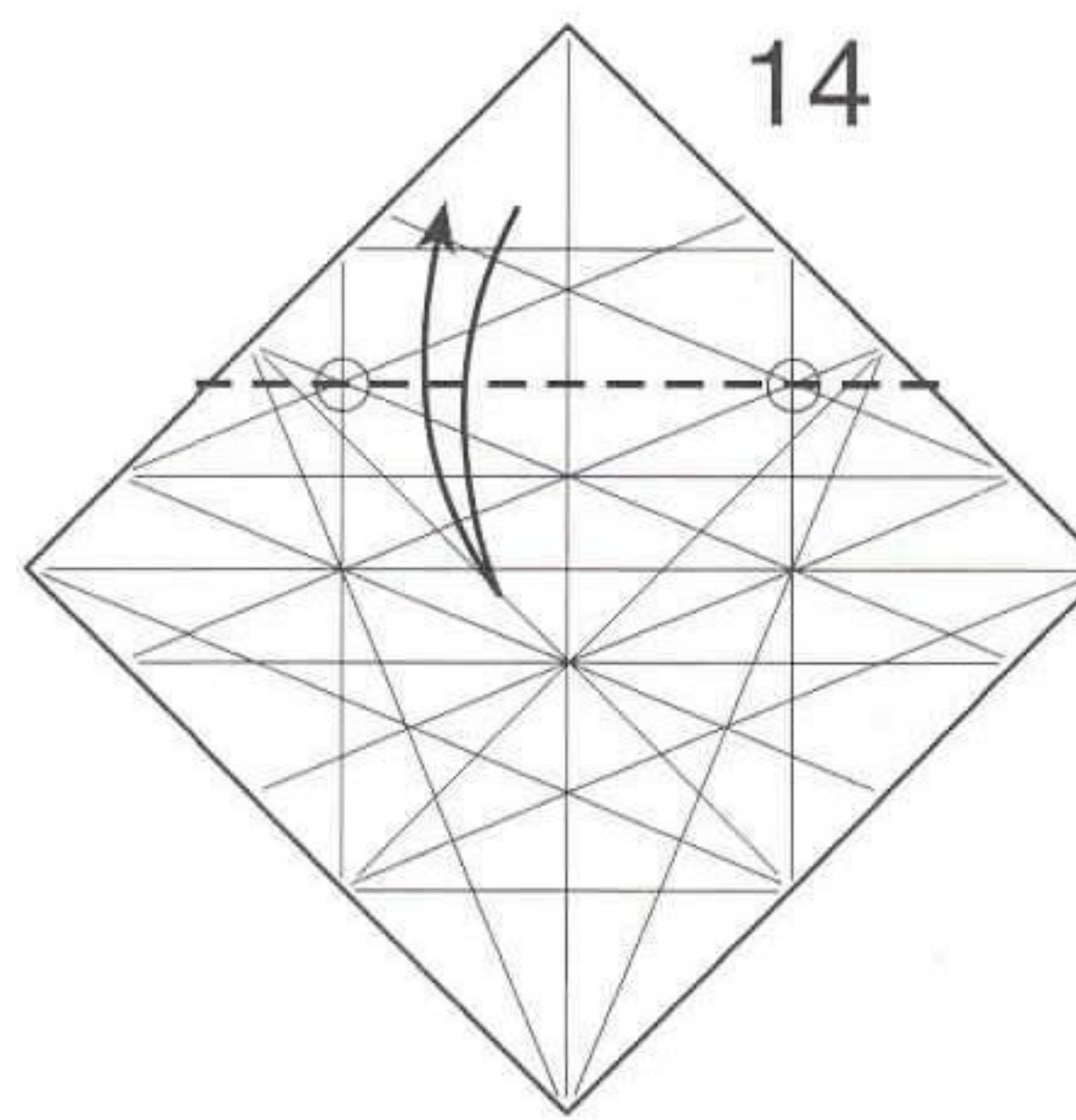
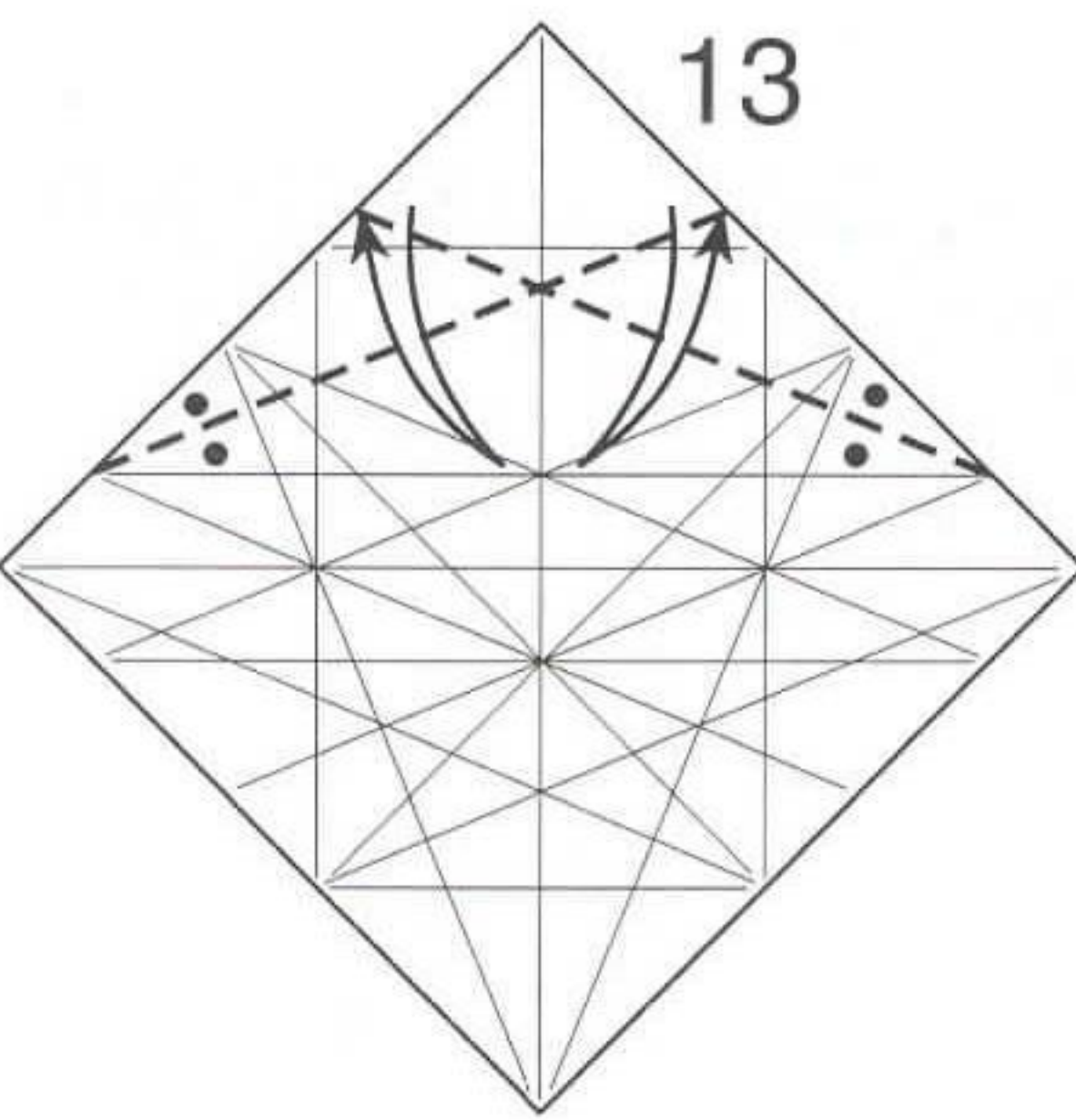
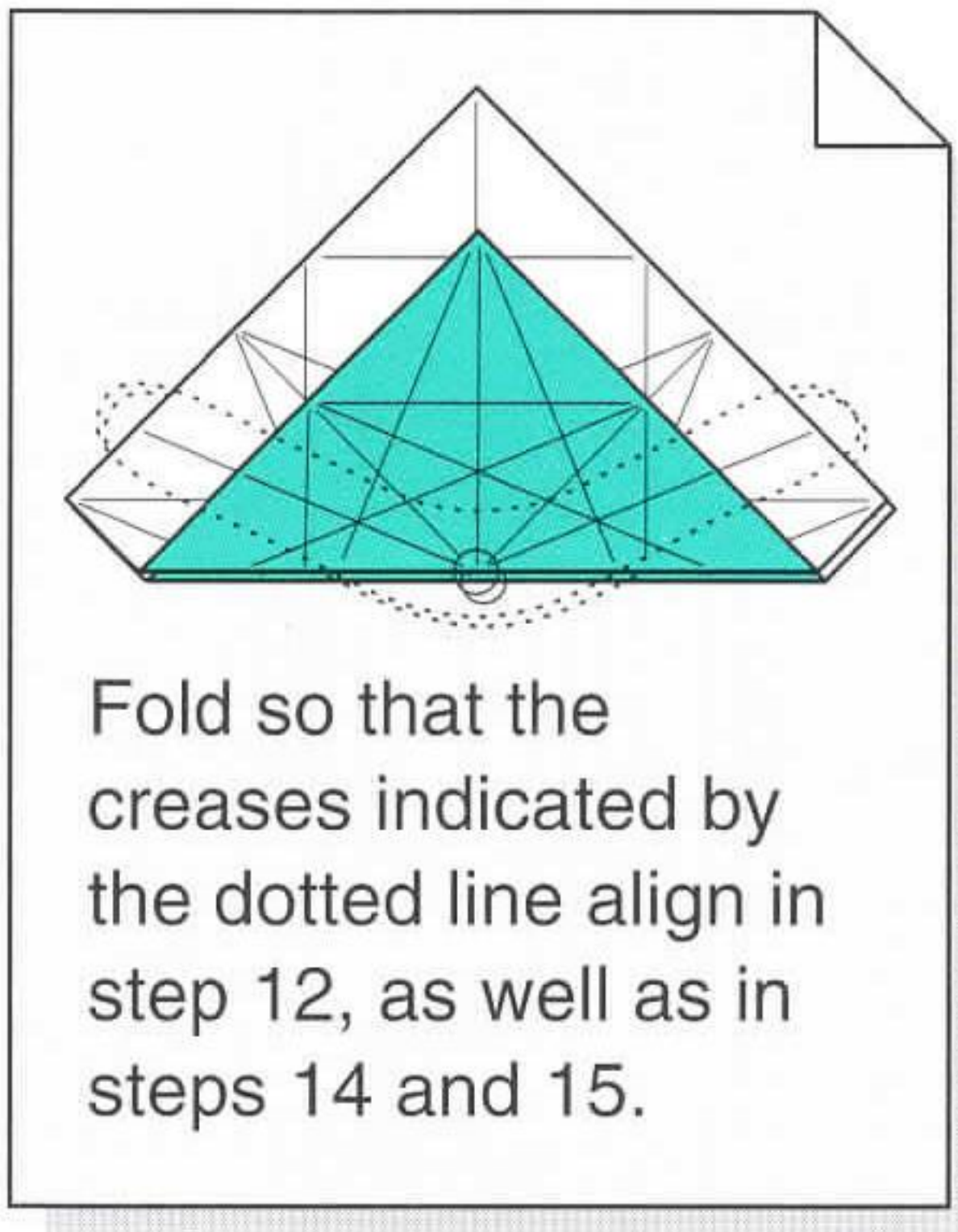
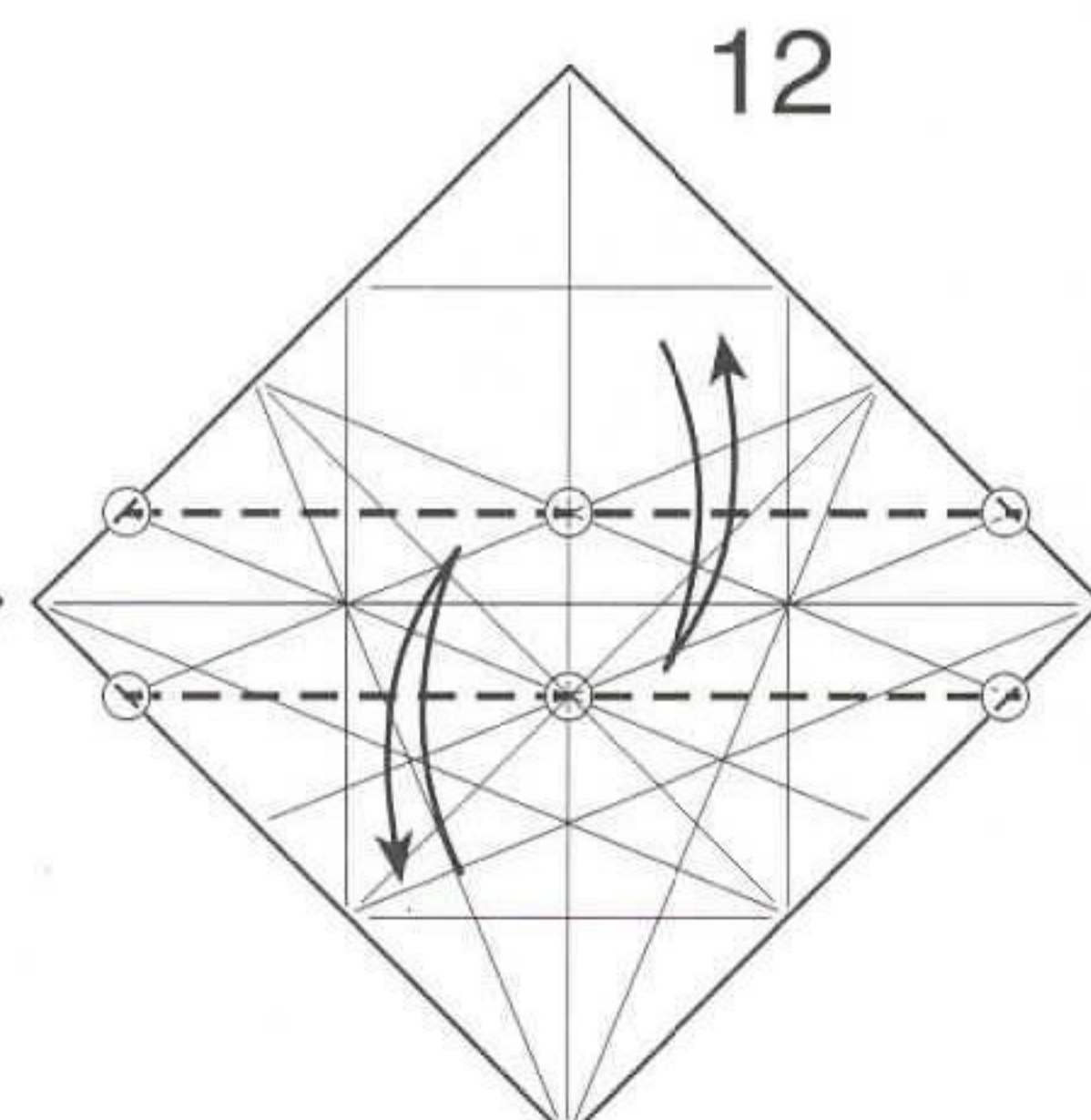
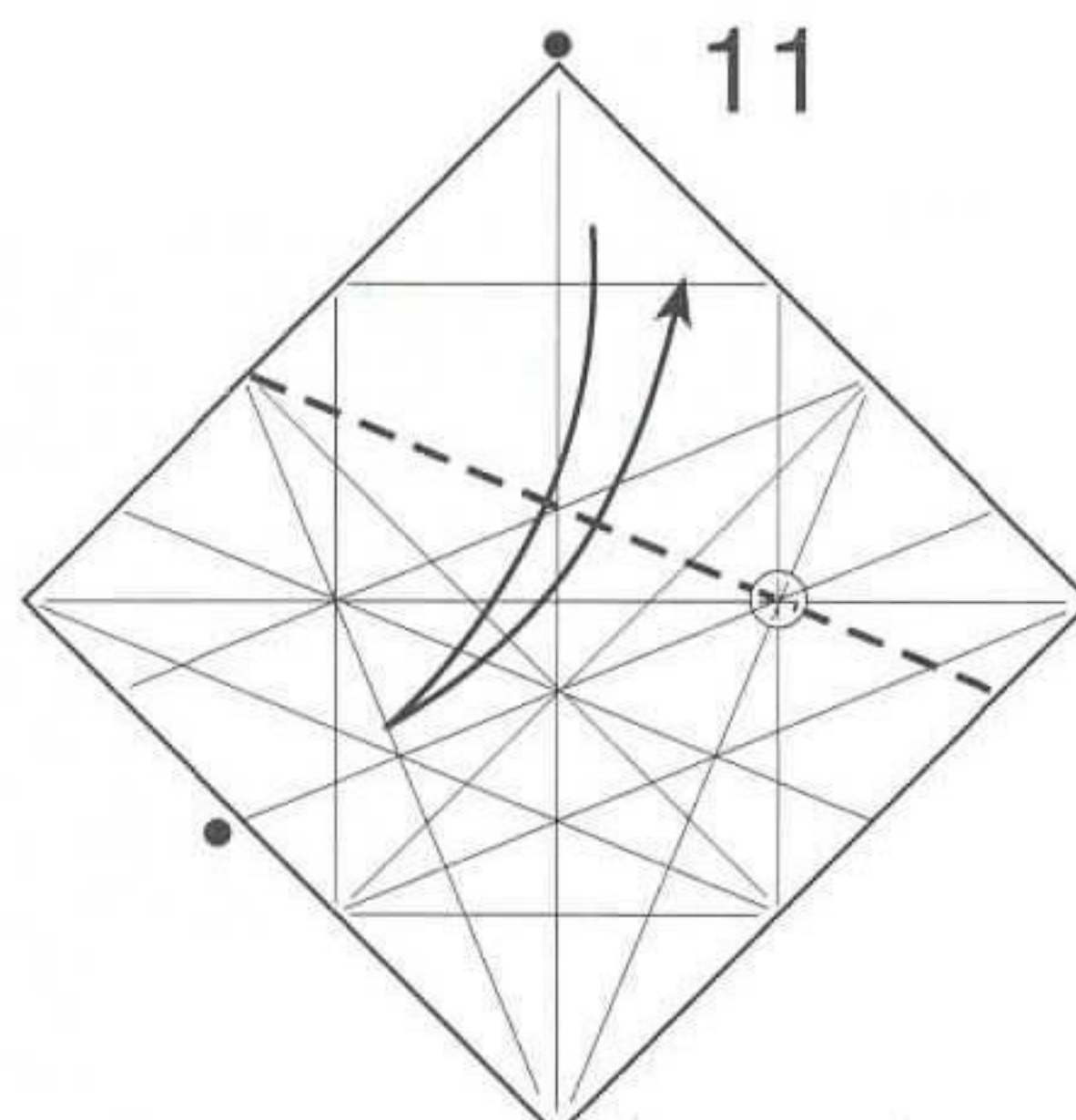
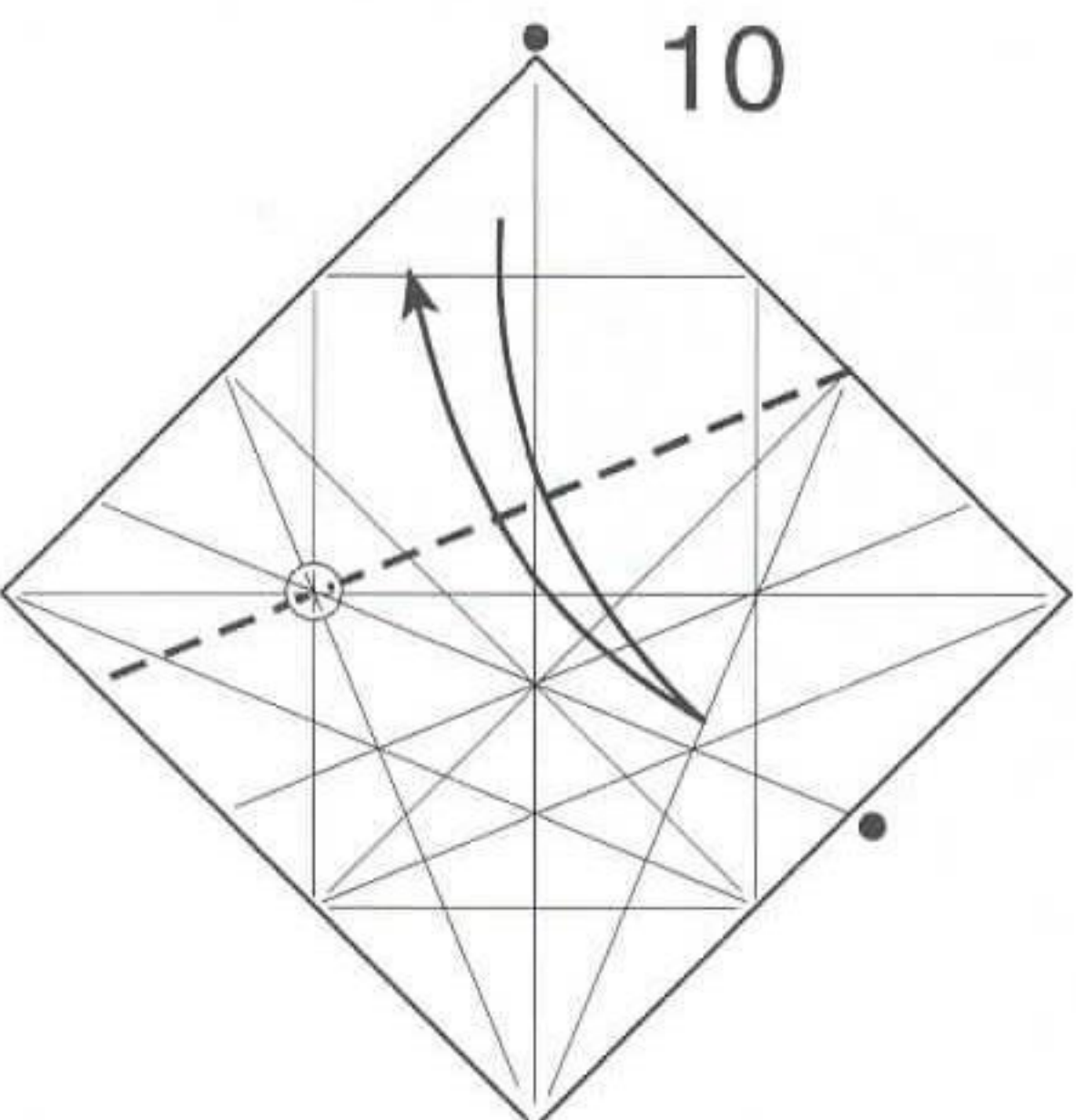
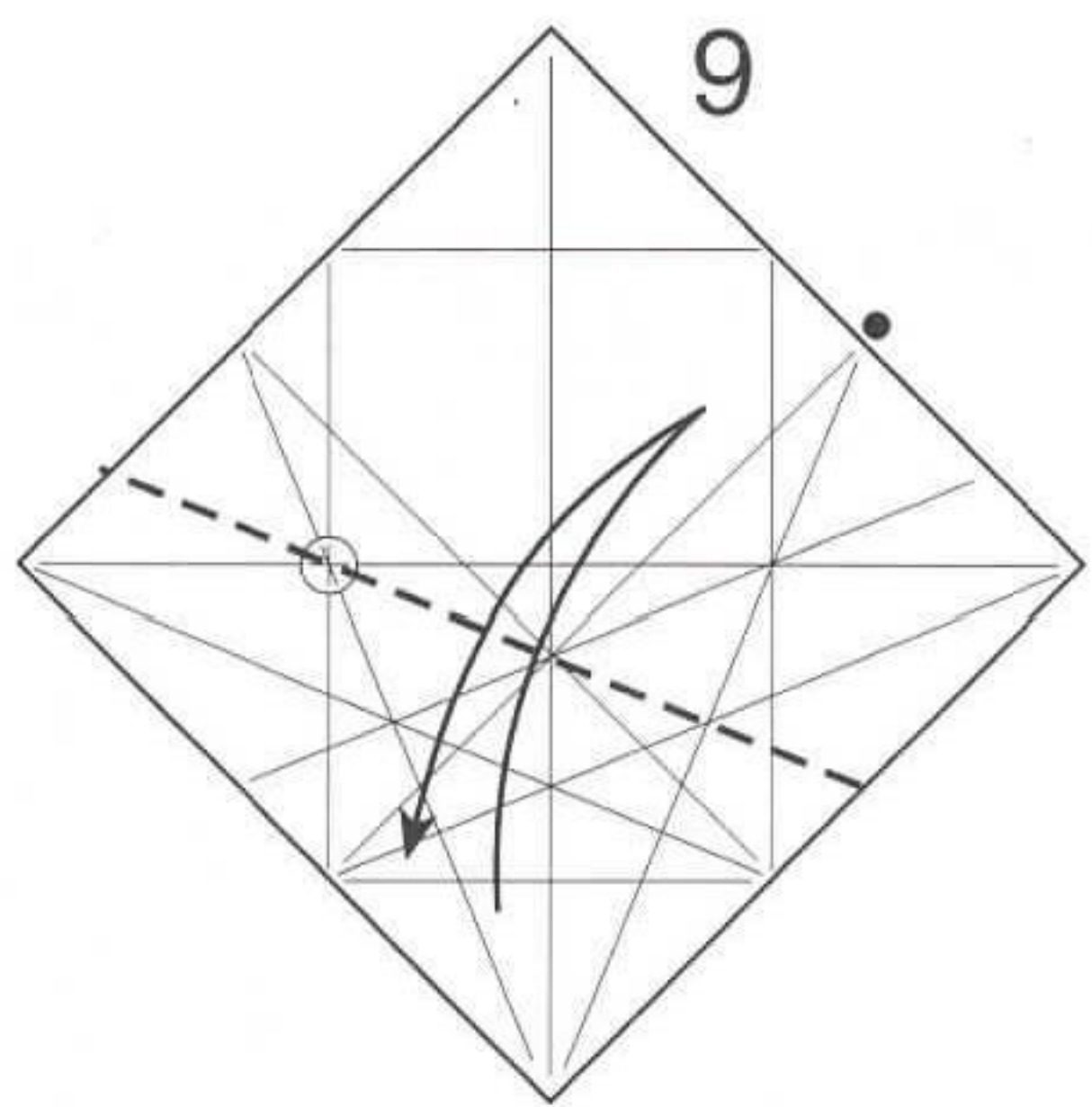
Devil

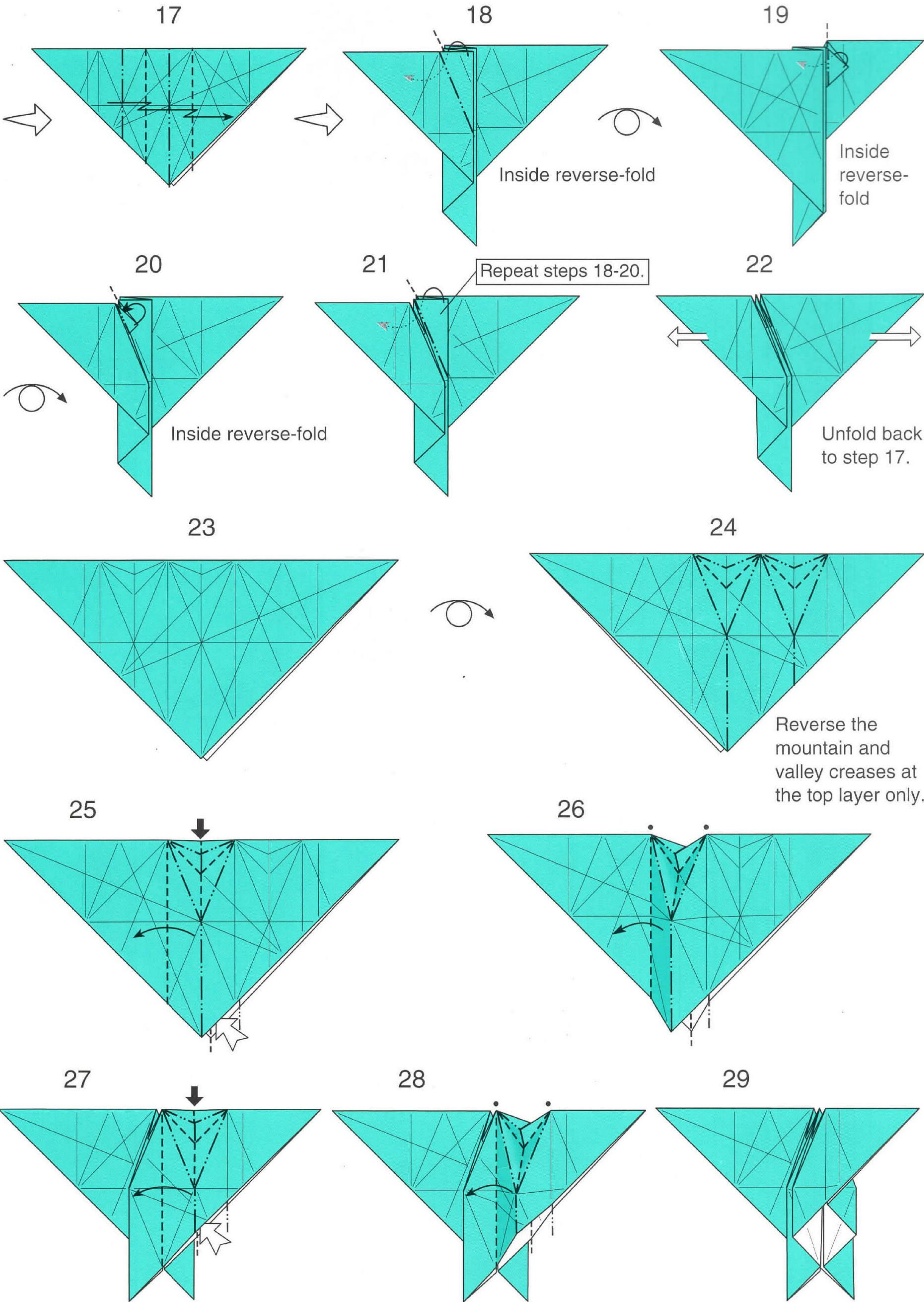
Theme: Taming the devil

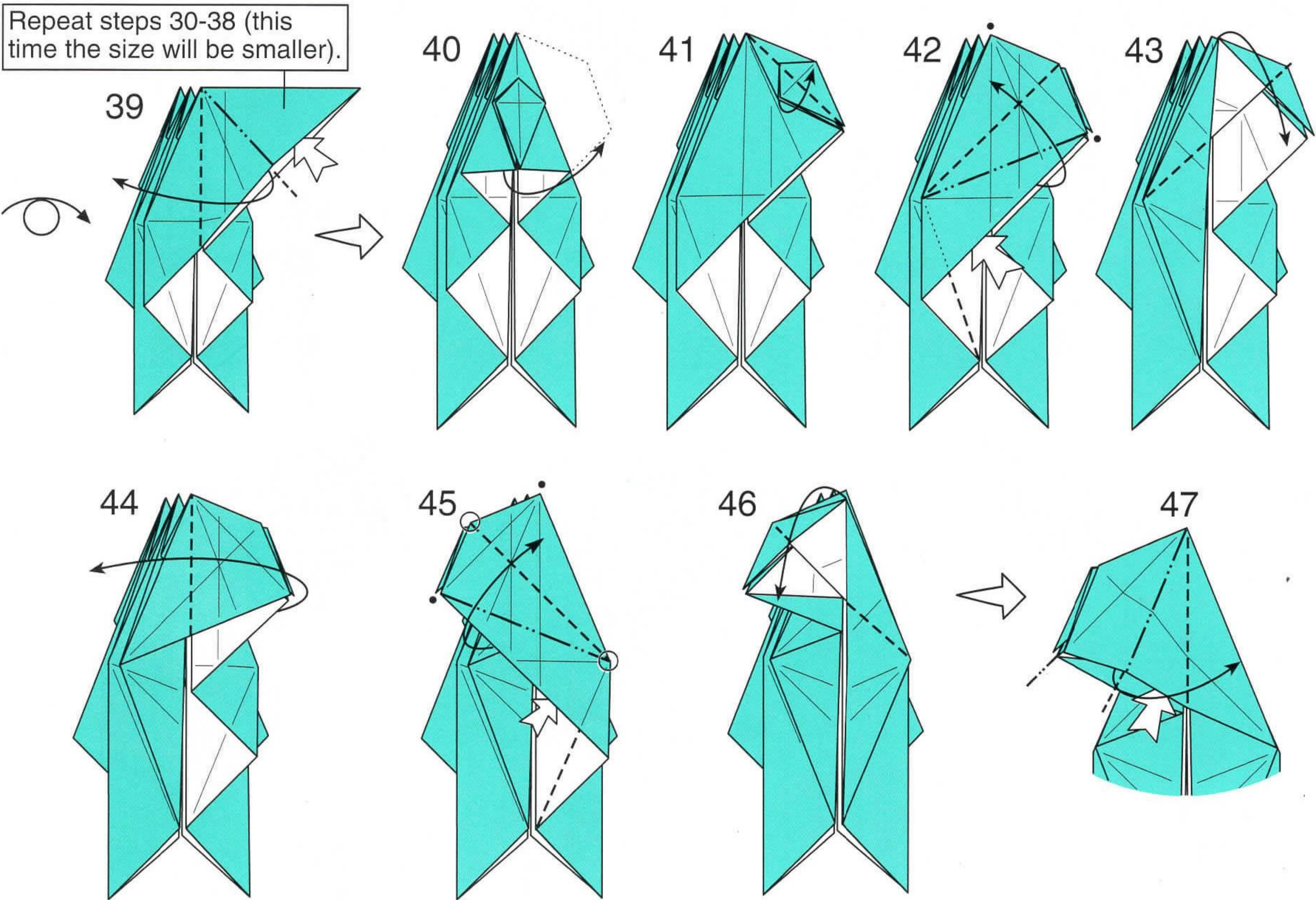
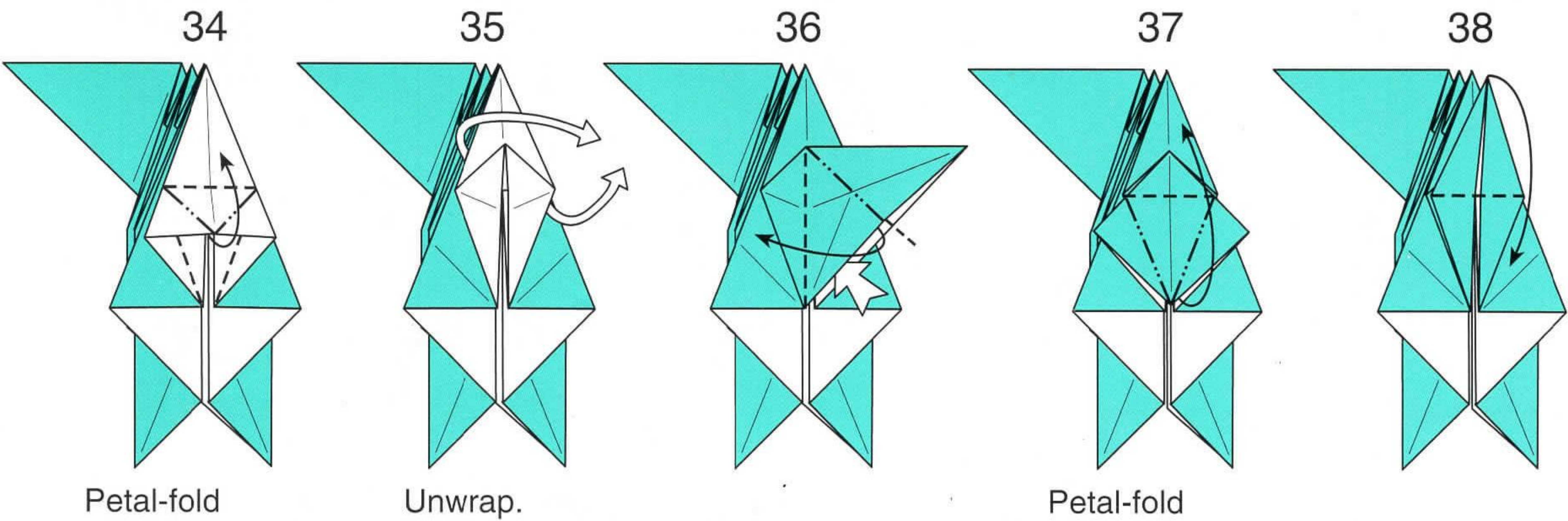
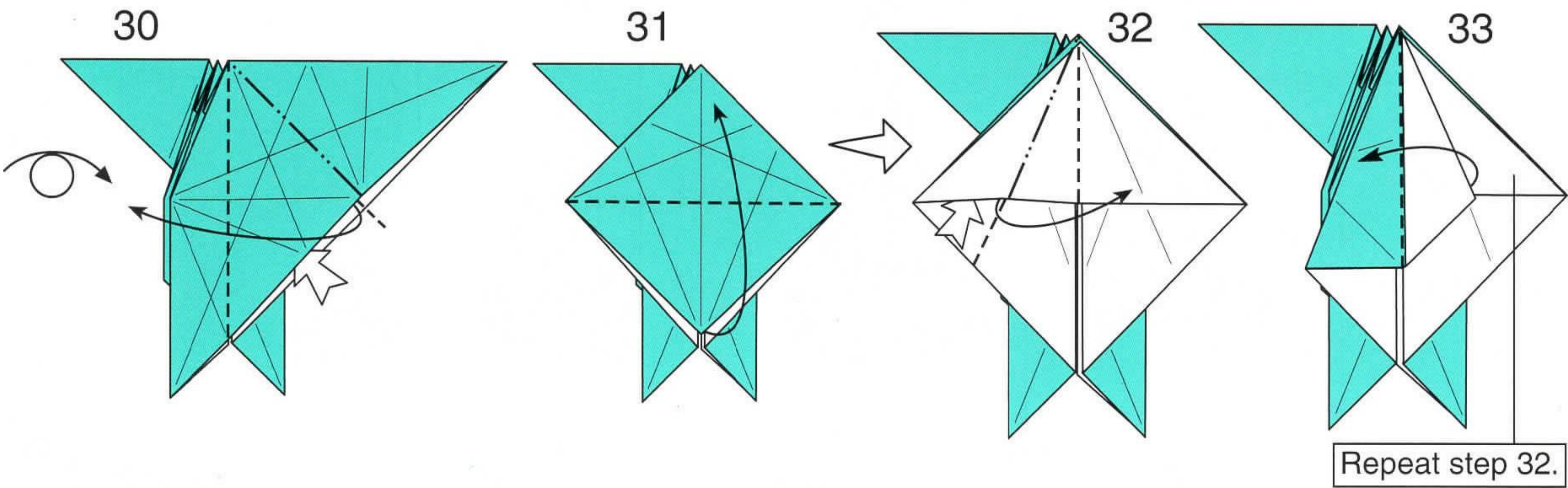
Difficult to fold using 6" (15 cm) origami paper.
10" (25 cm) or larger paper is suggested.

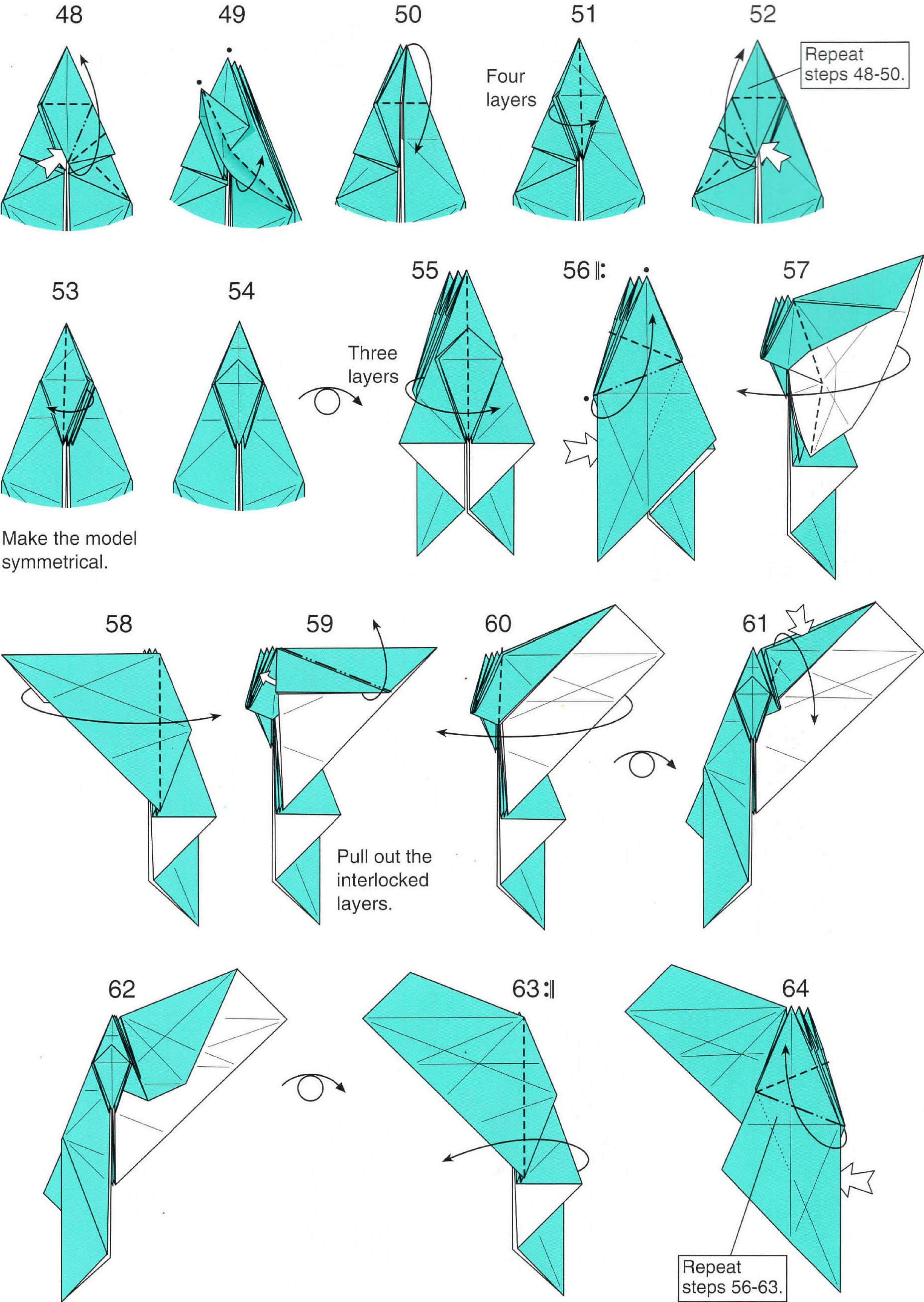


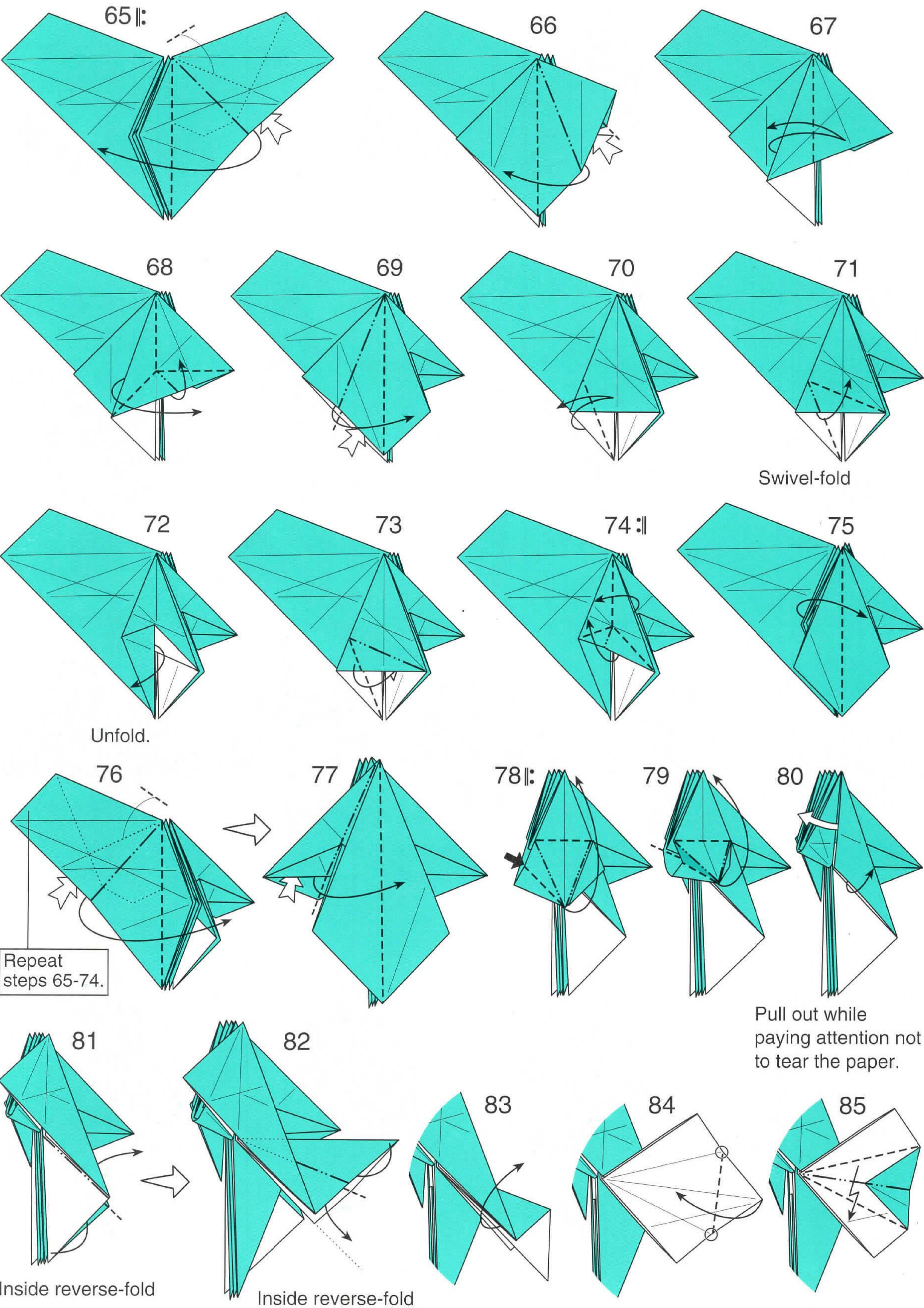
Unfold.

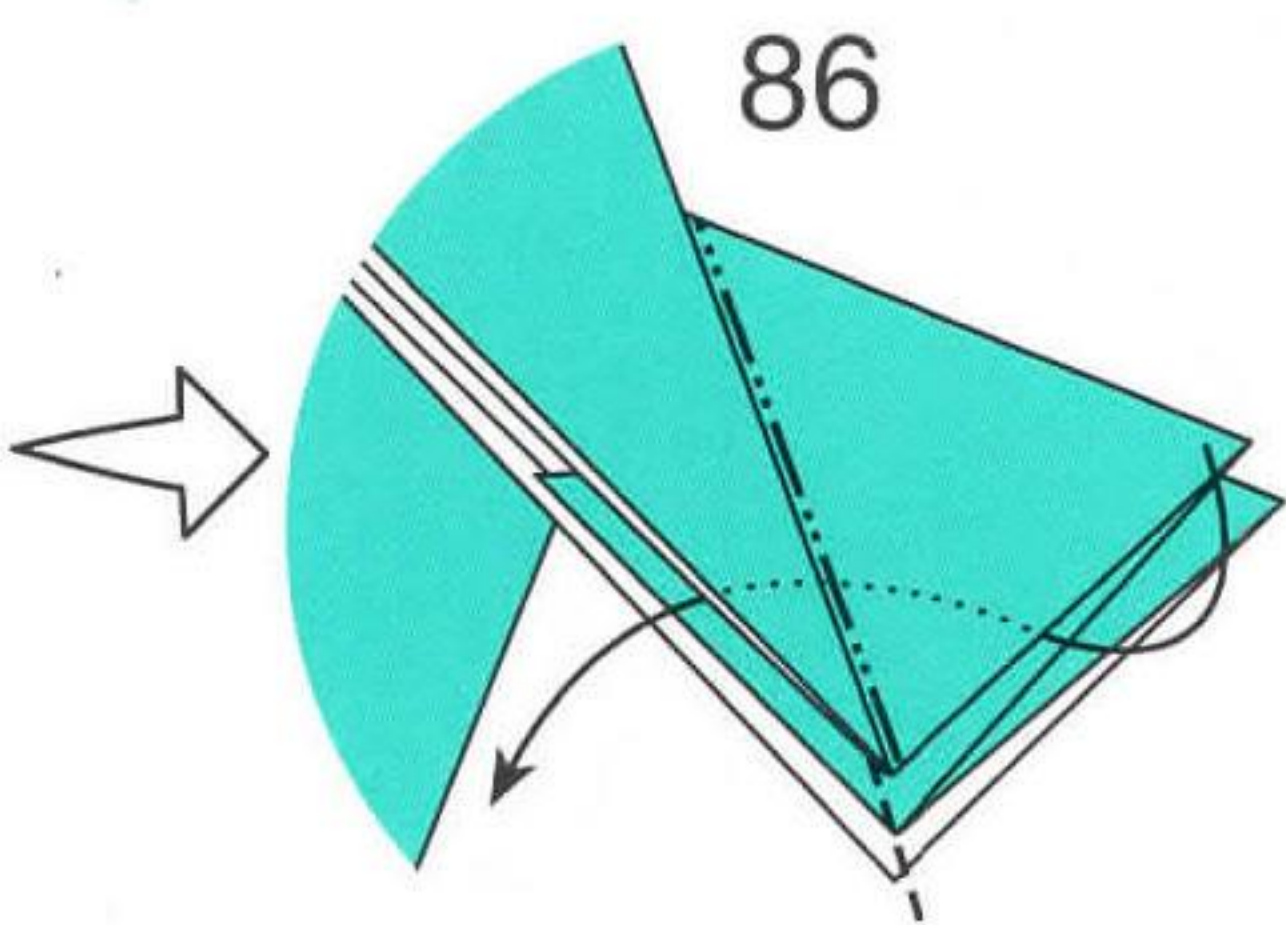




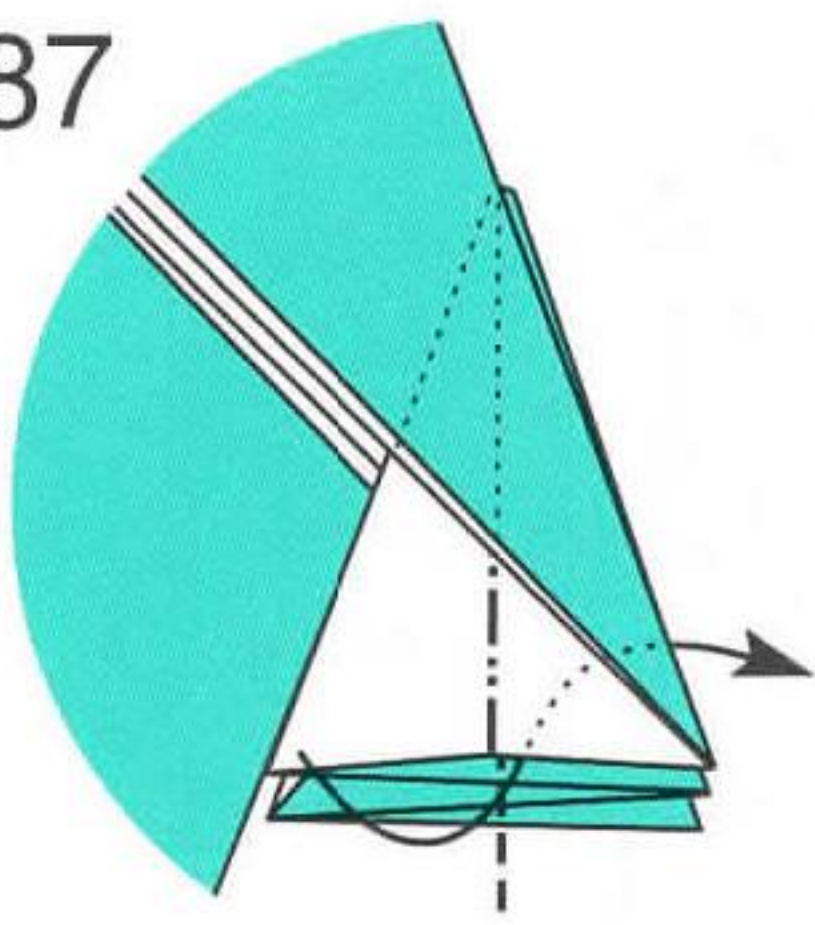




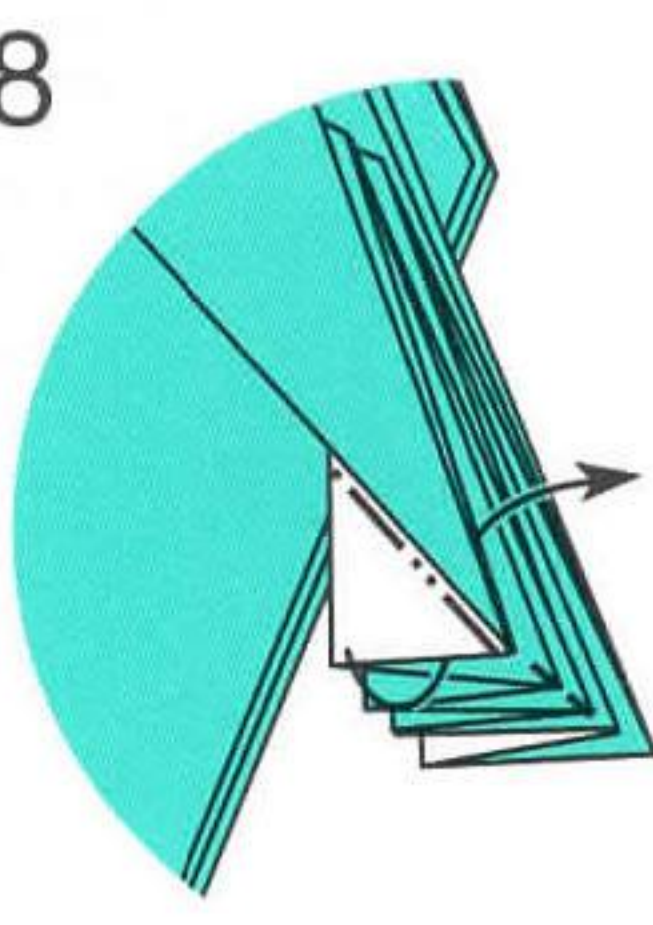




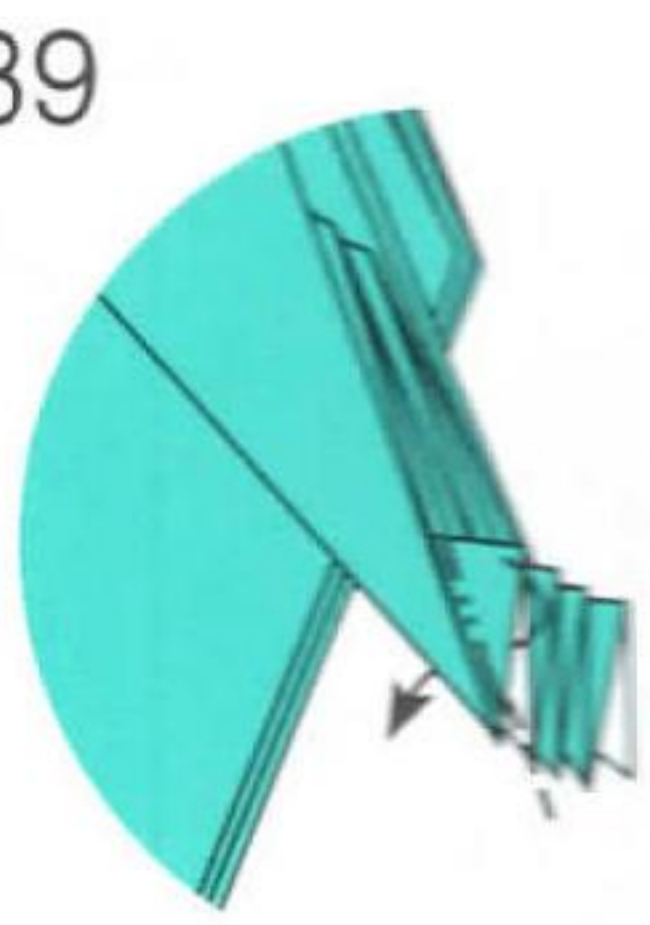
86 Inside reverse-fold twice



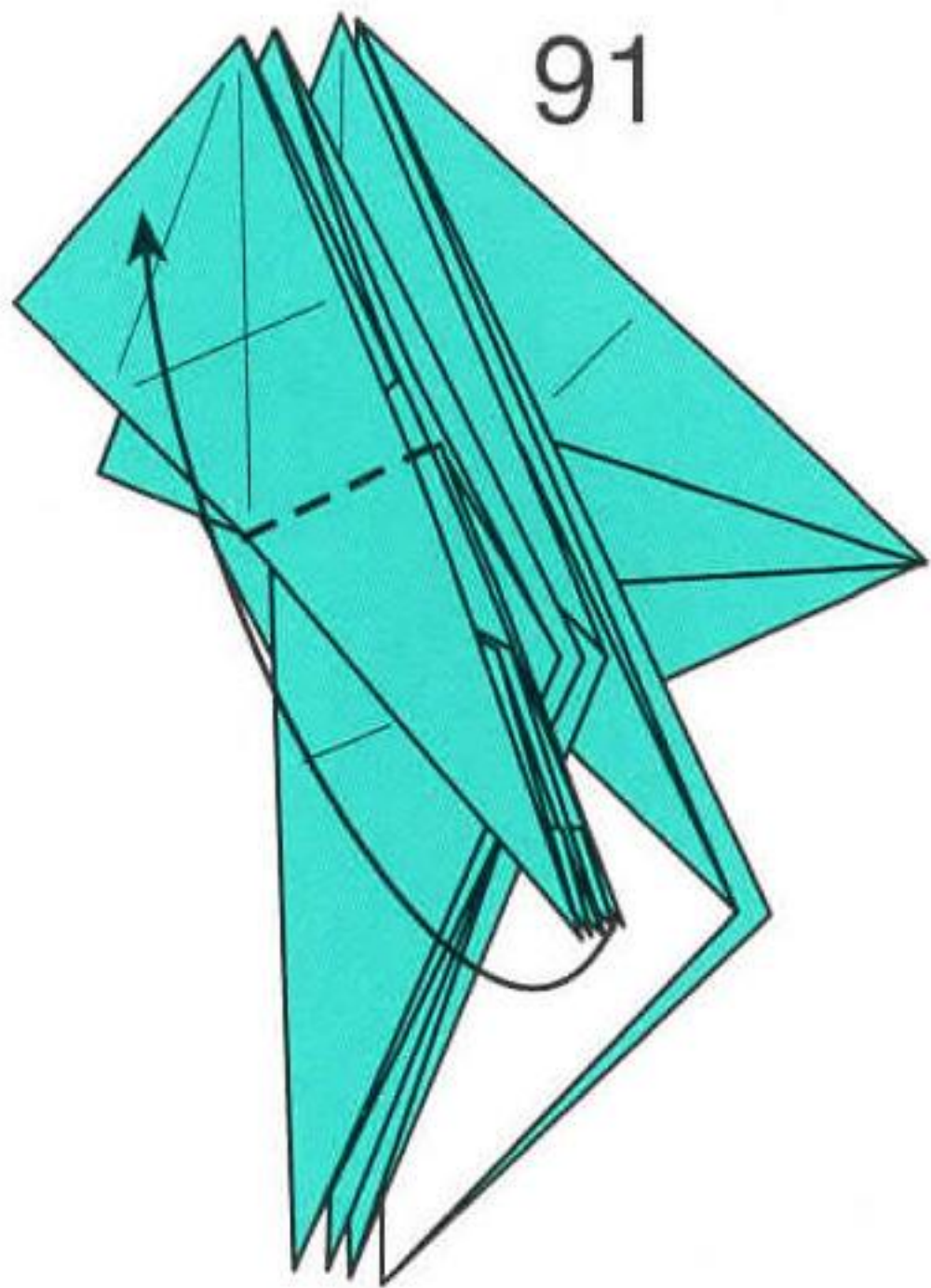
87 Inside reverse-fold twice



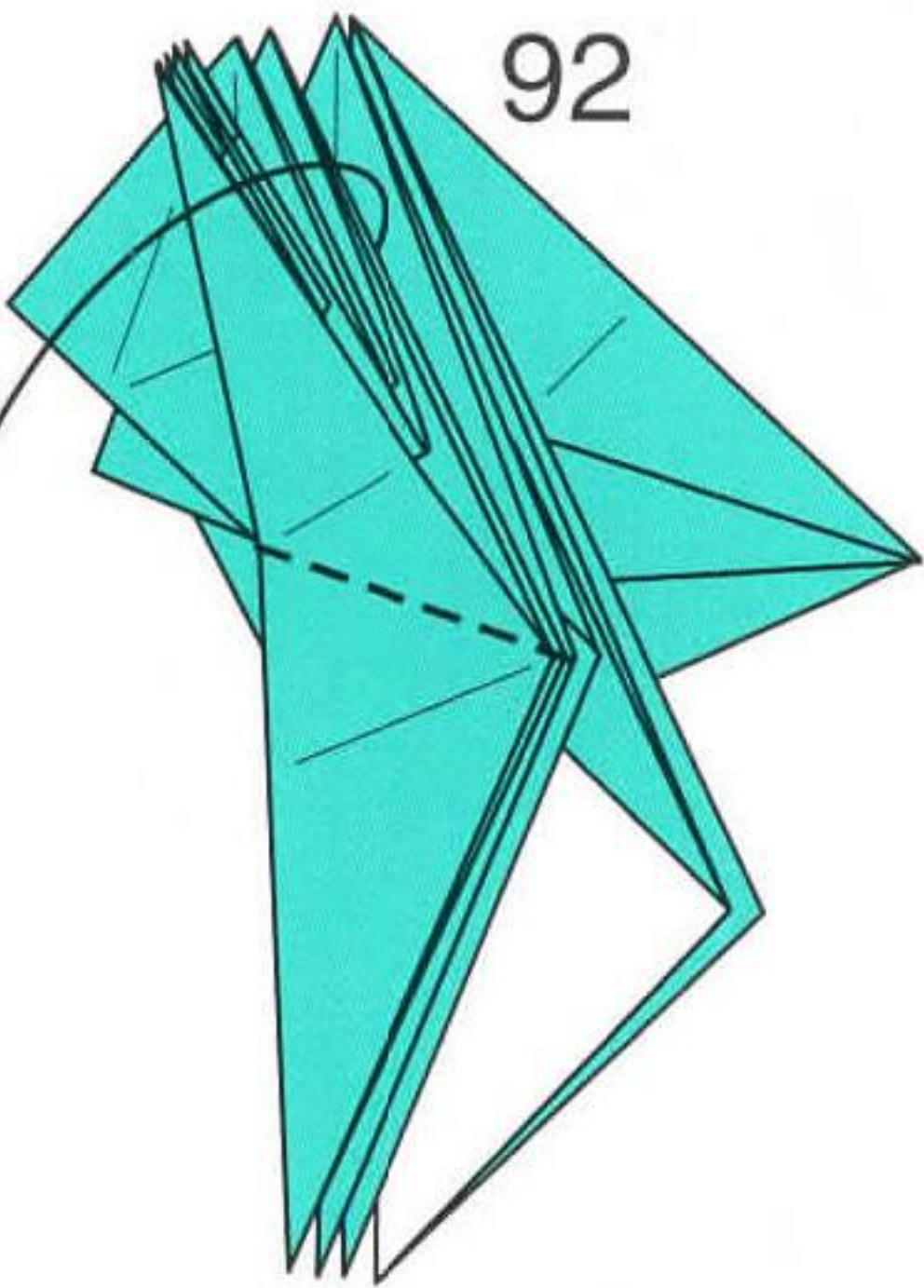
88 Inside reverse-fold four times



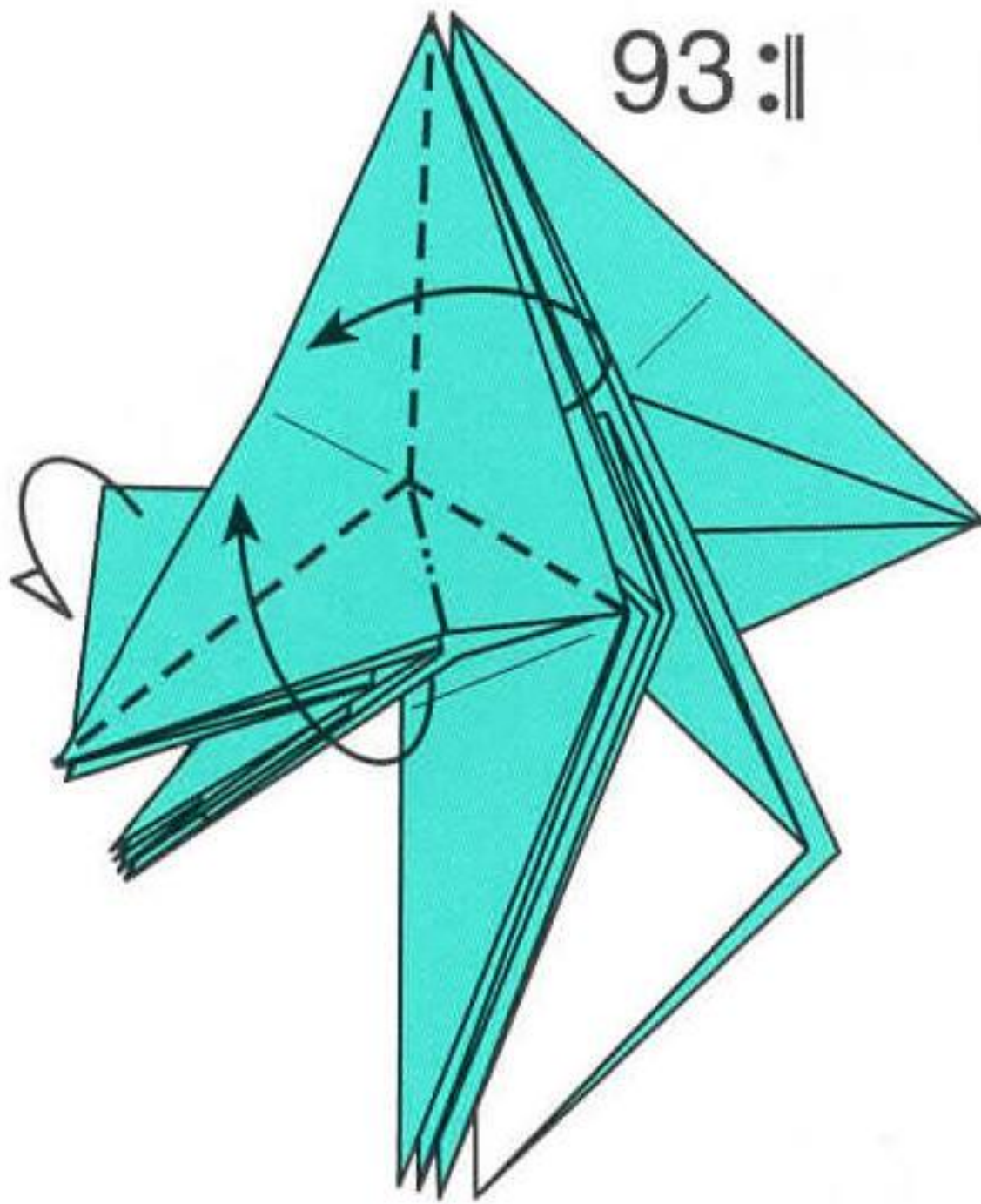
89 Inside reverse-fold four times



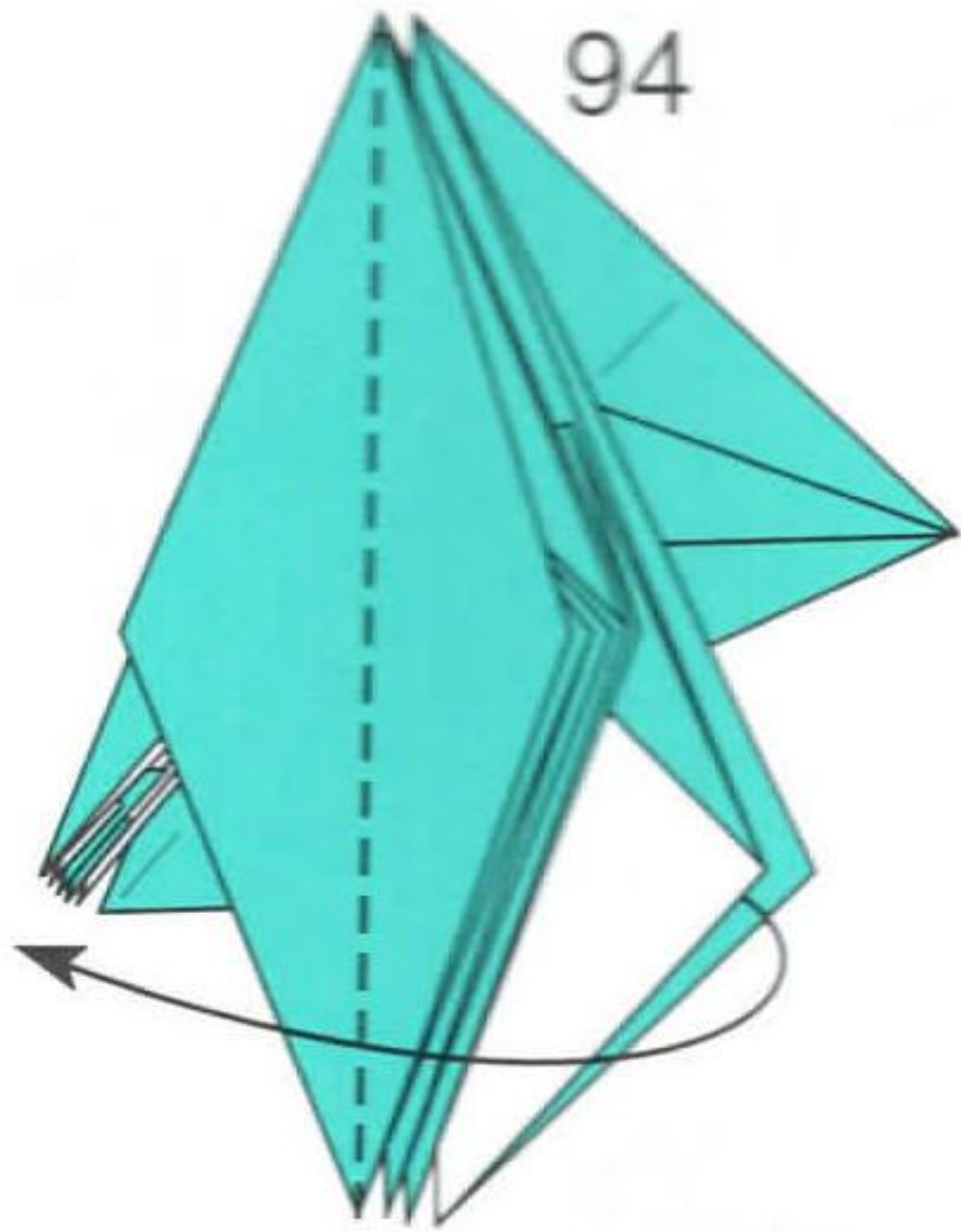
91



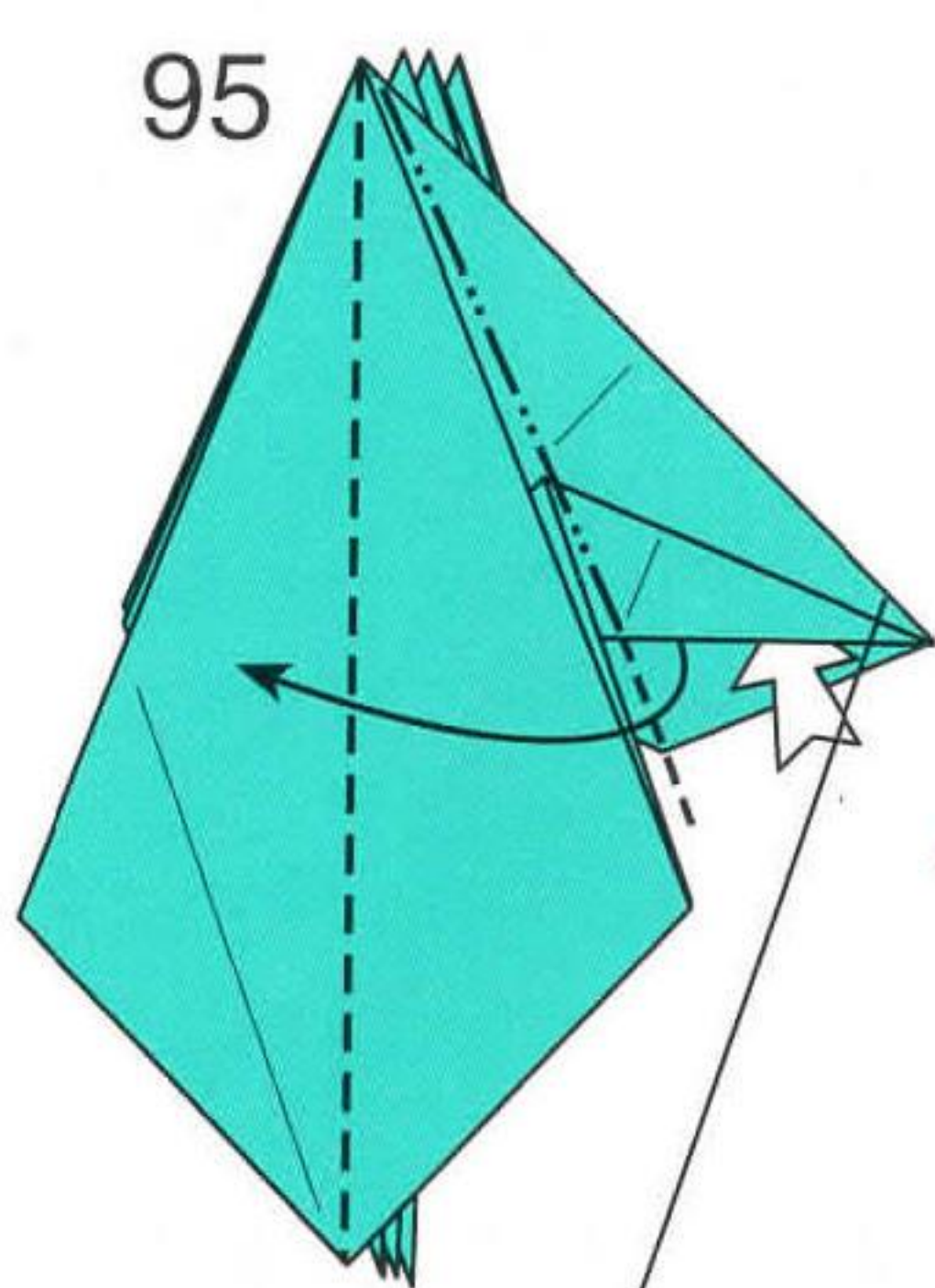
92



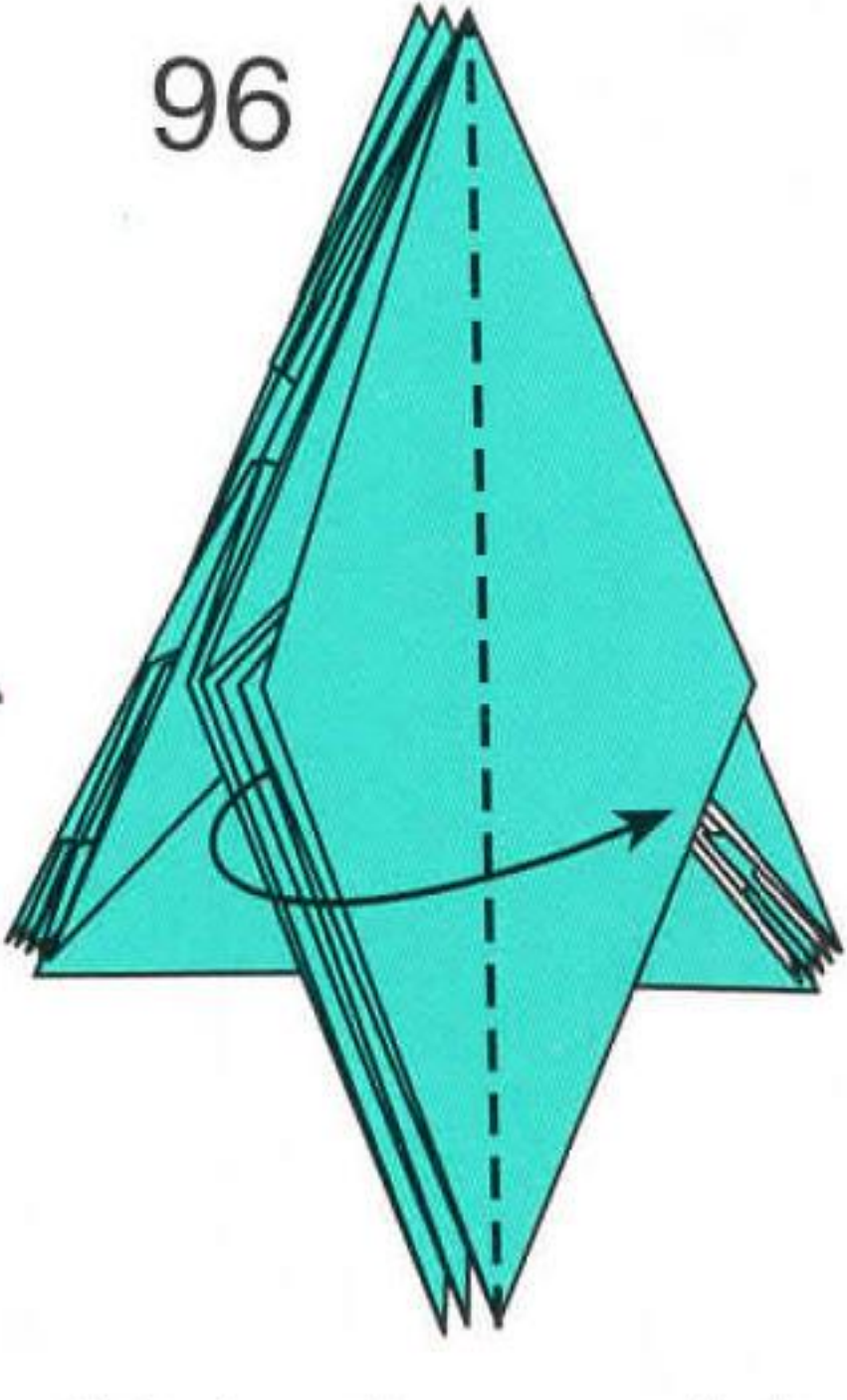
93



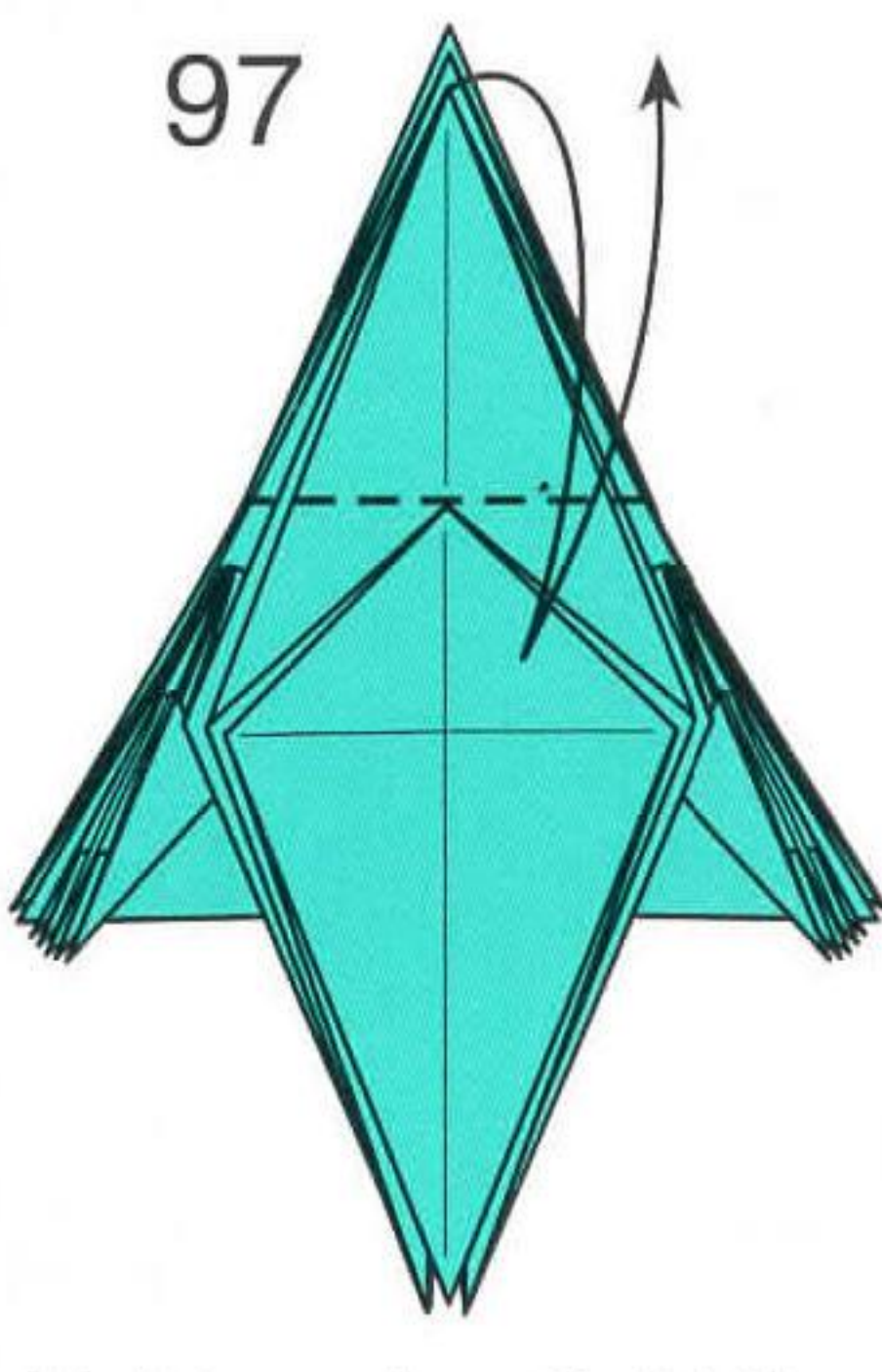
94



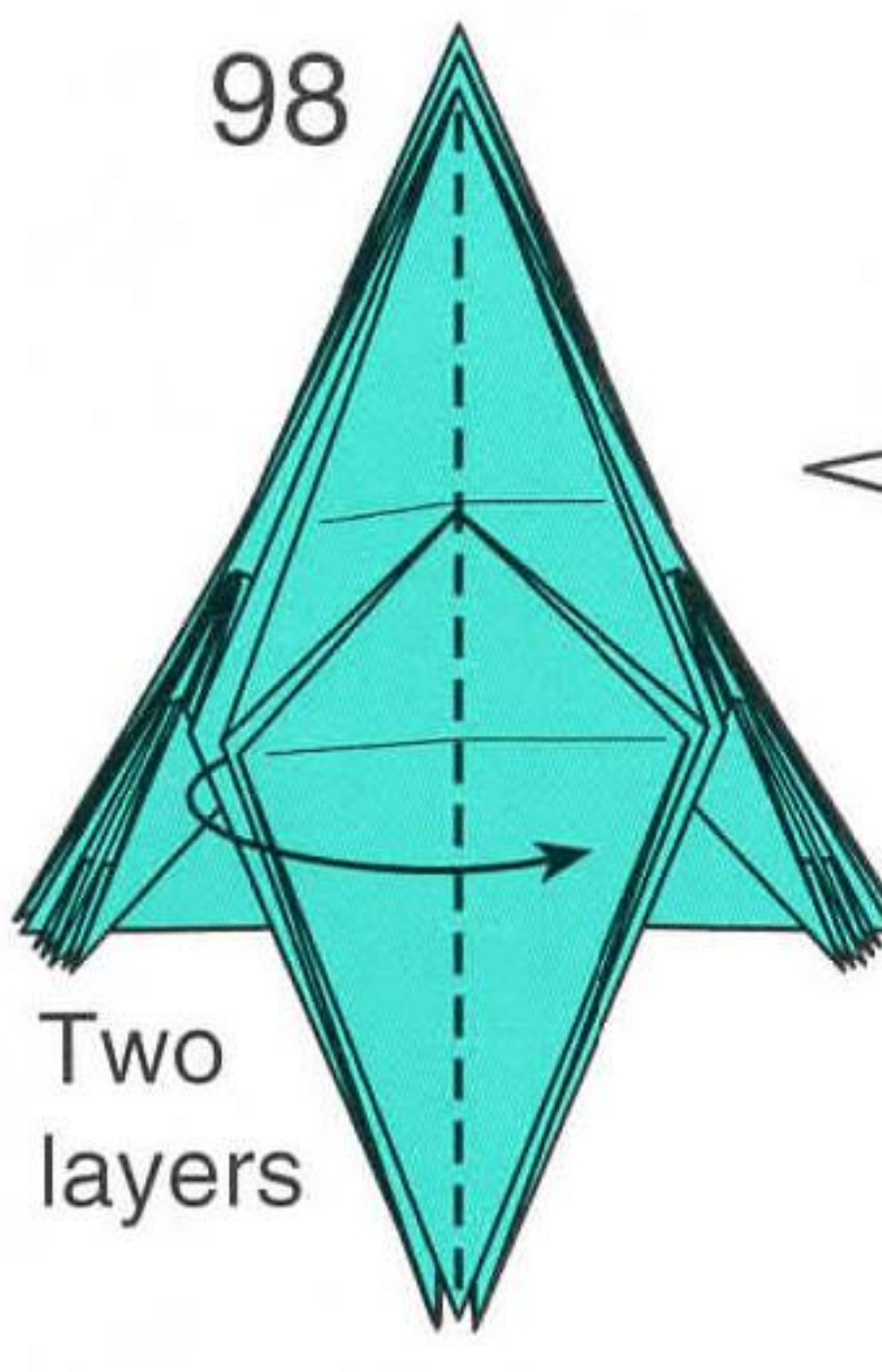
95



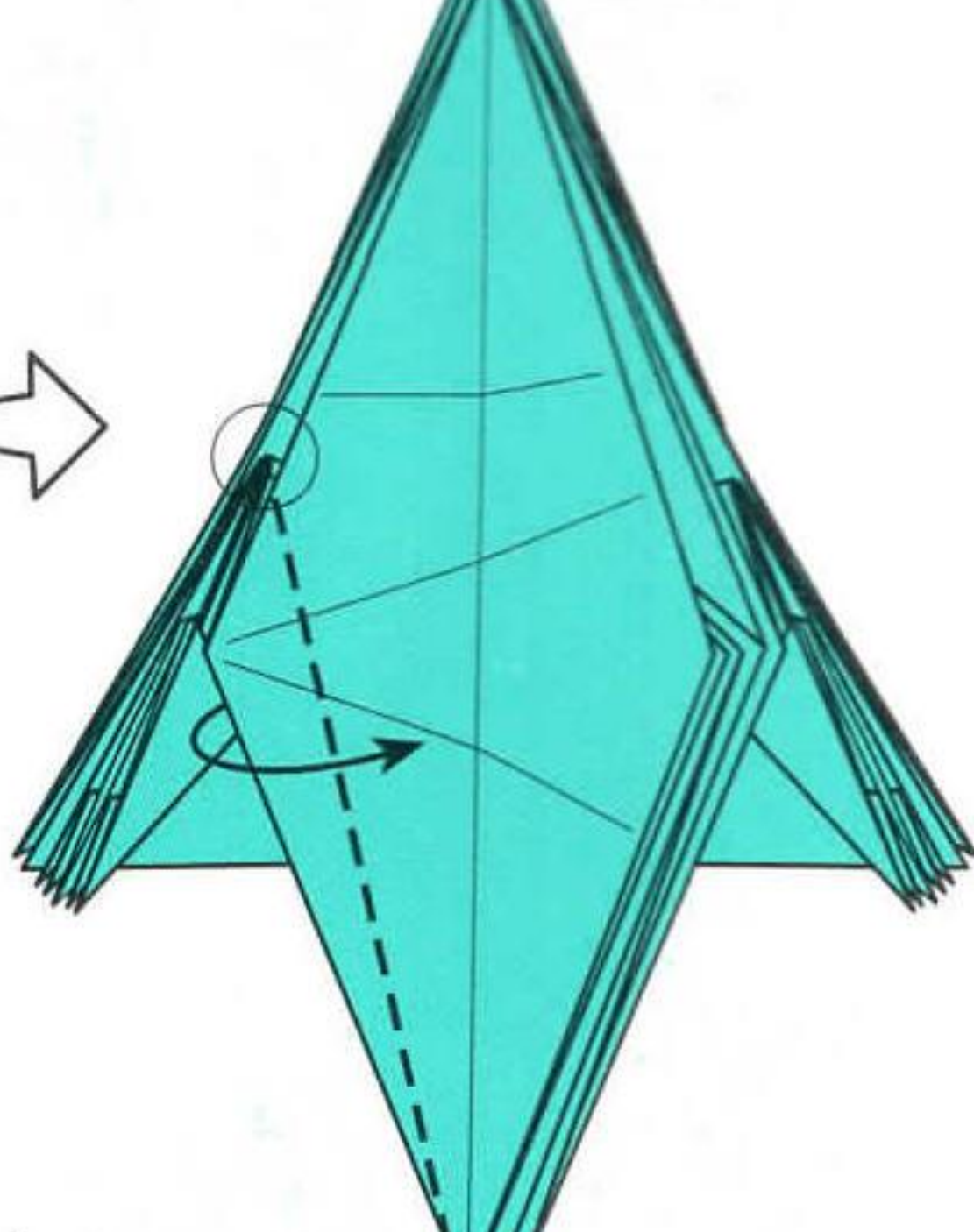
96



97



98



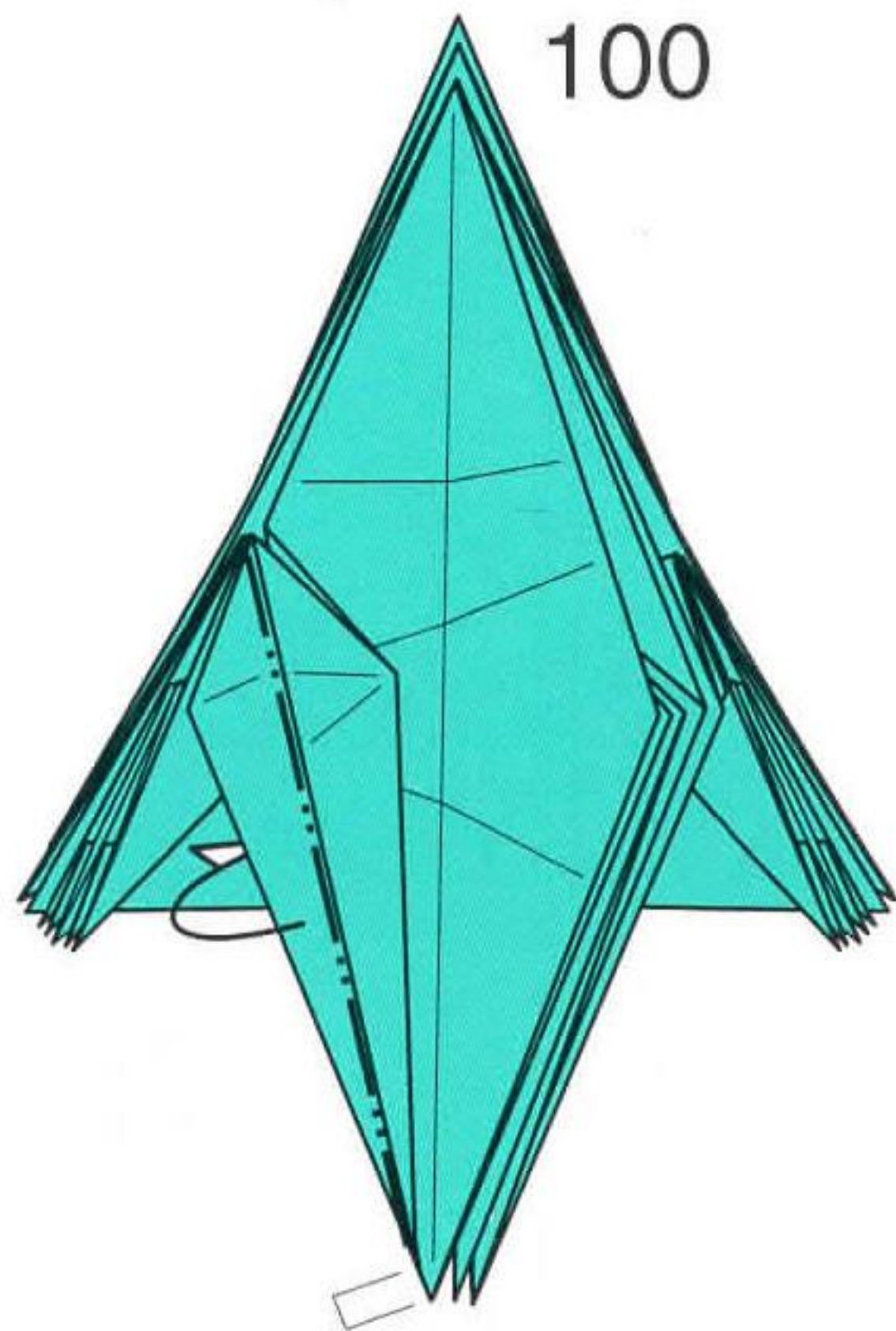
99

Repeat steps 78-93.

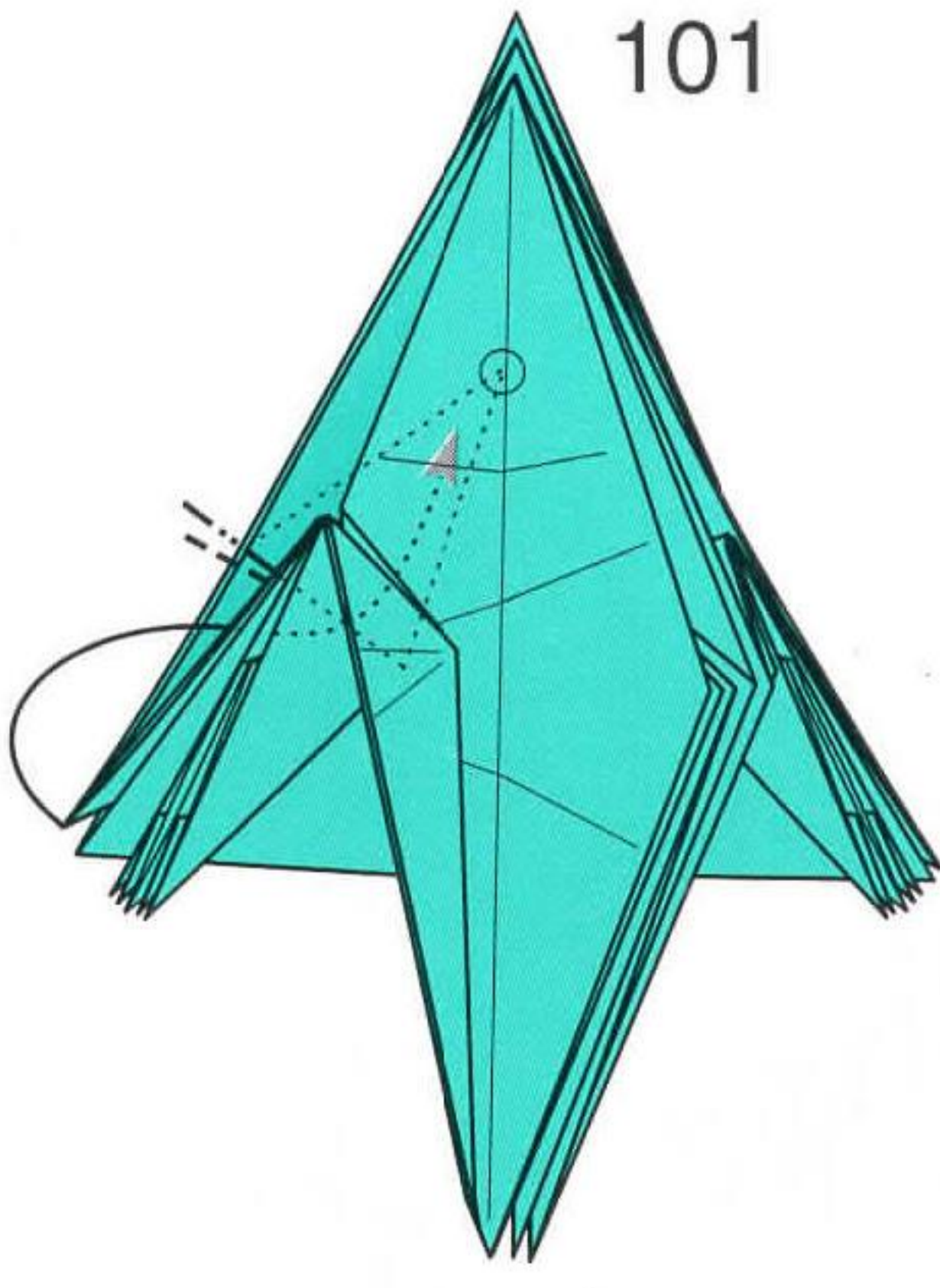
Make the model symmetrical.

Fold and unfold the top layer only.

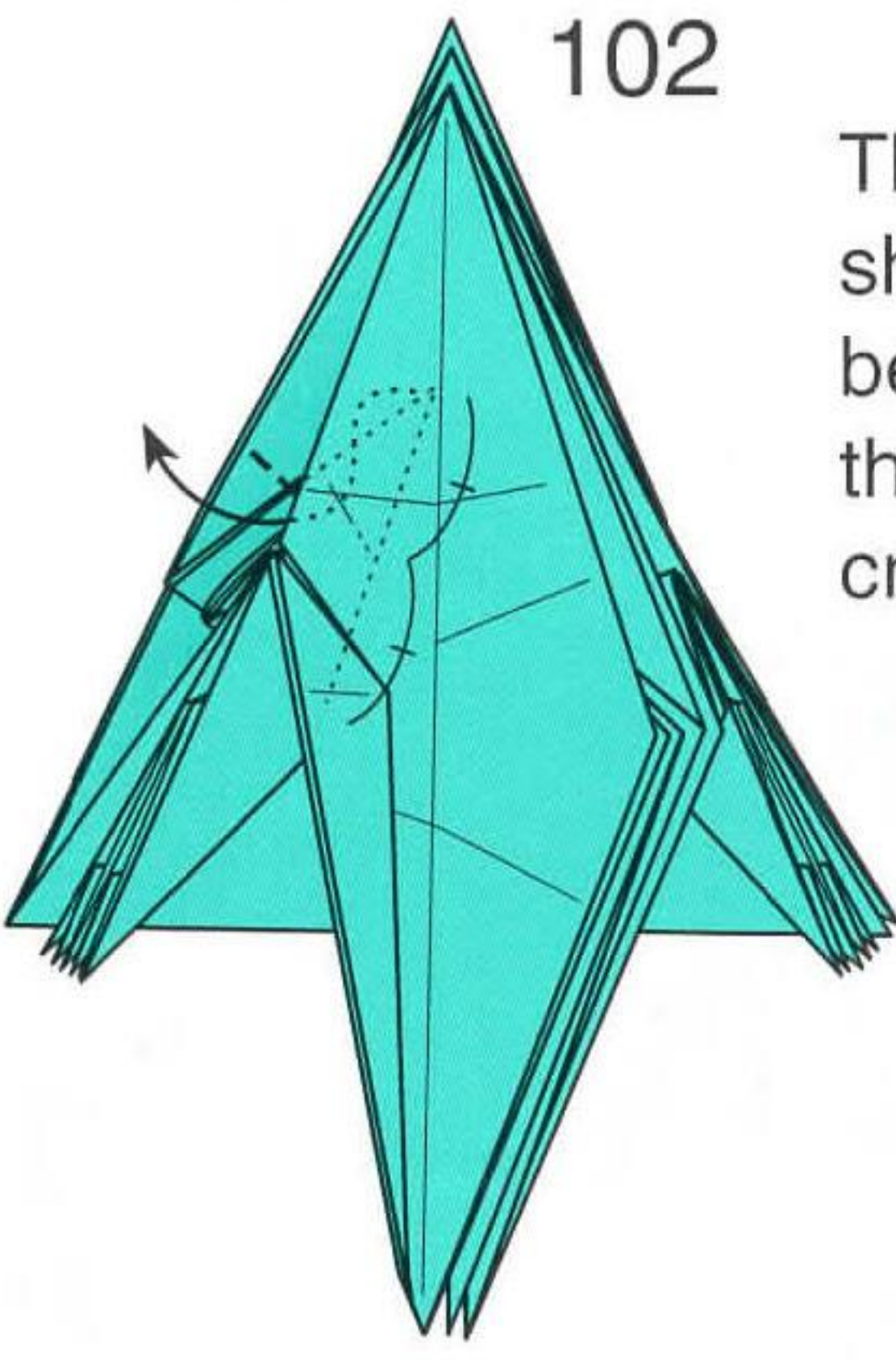
Leave a small gap.



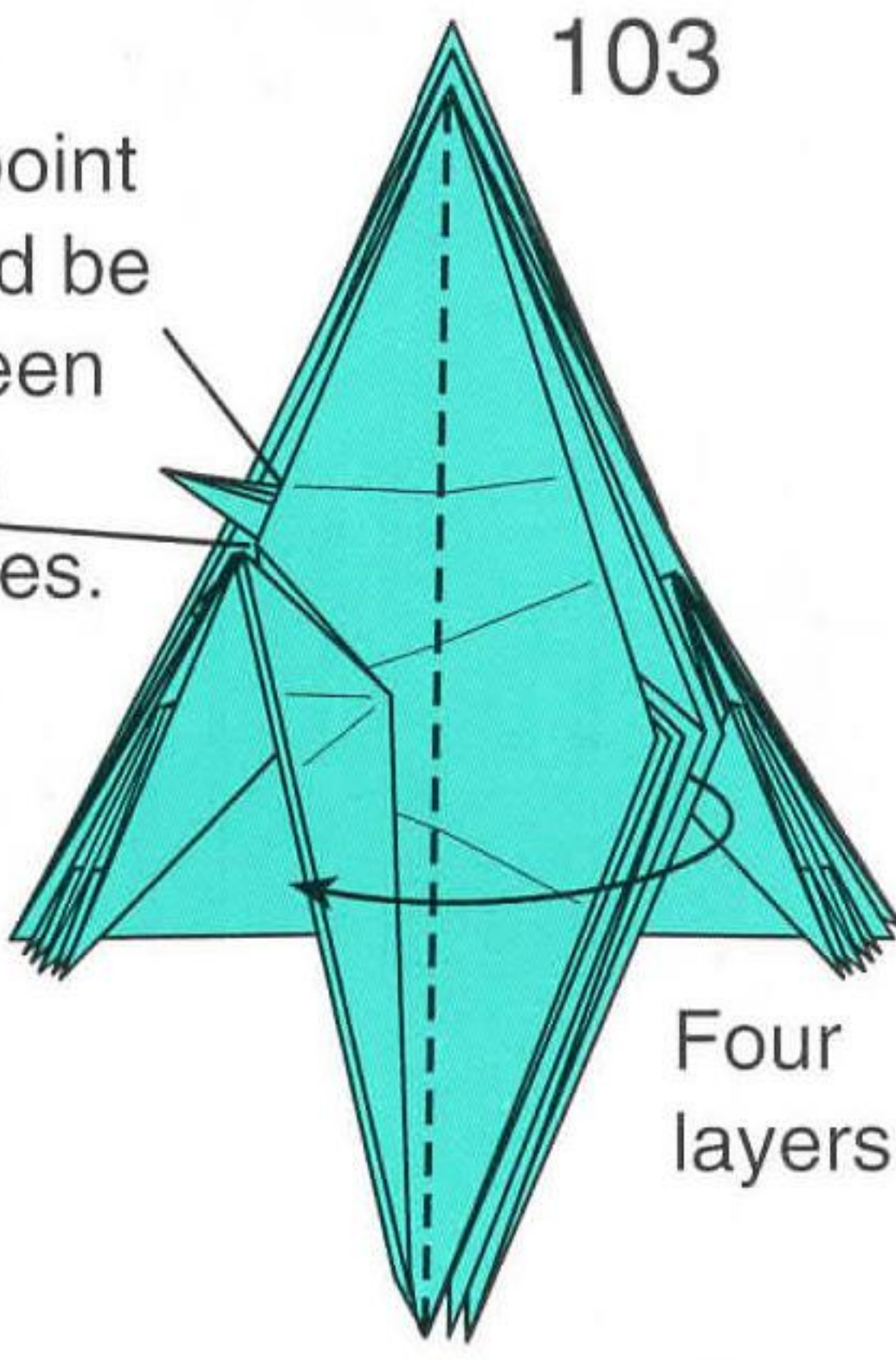
100



101



102



103

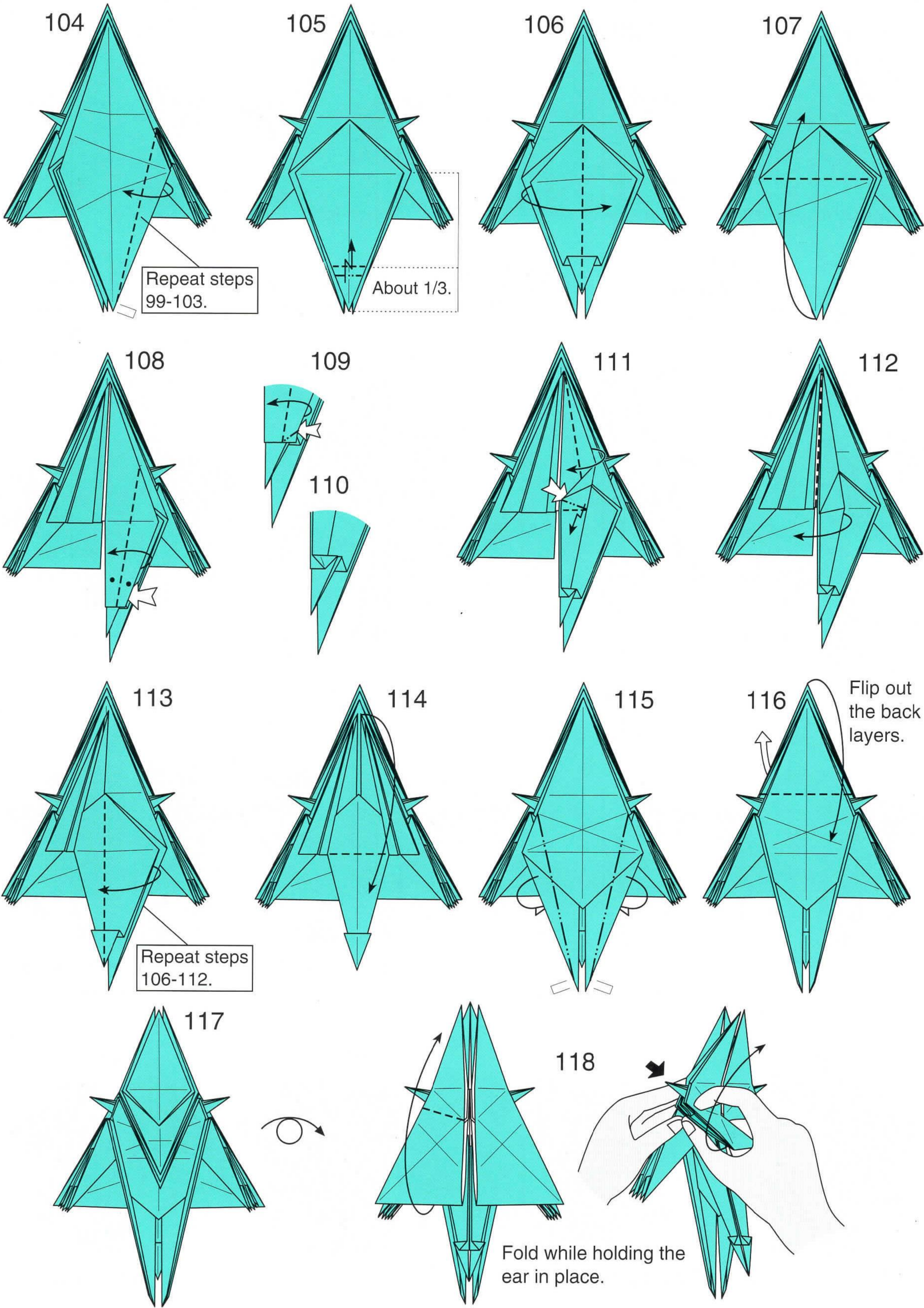
The point should be between these creases.

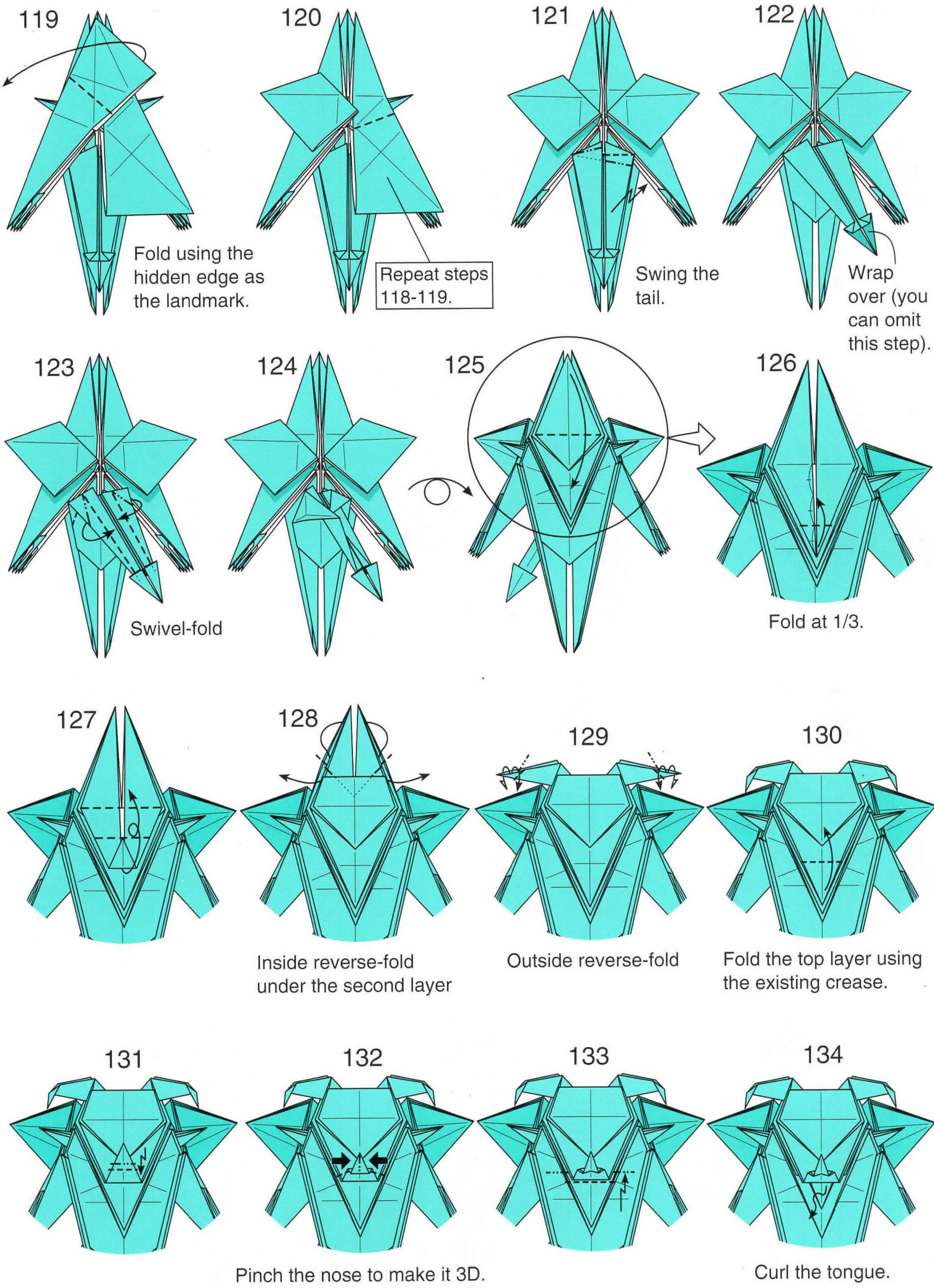
Four layers

Fold along the edge made in step 99.

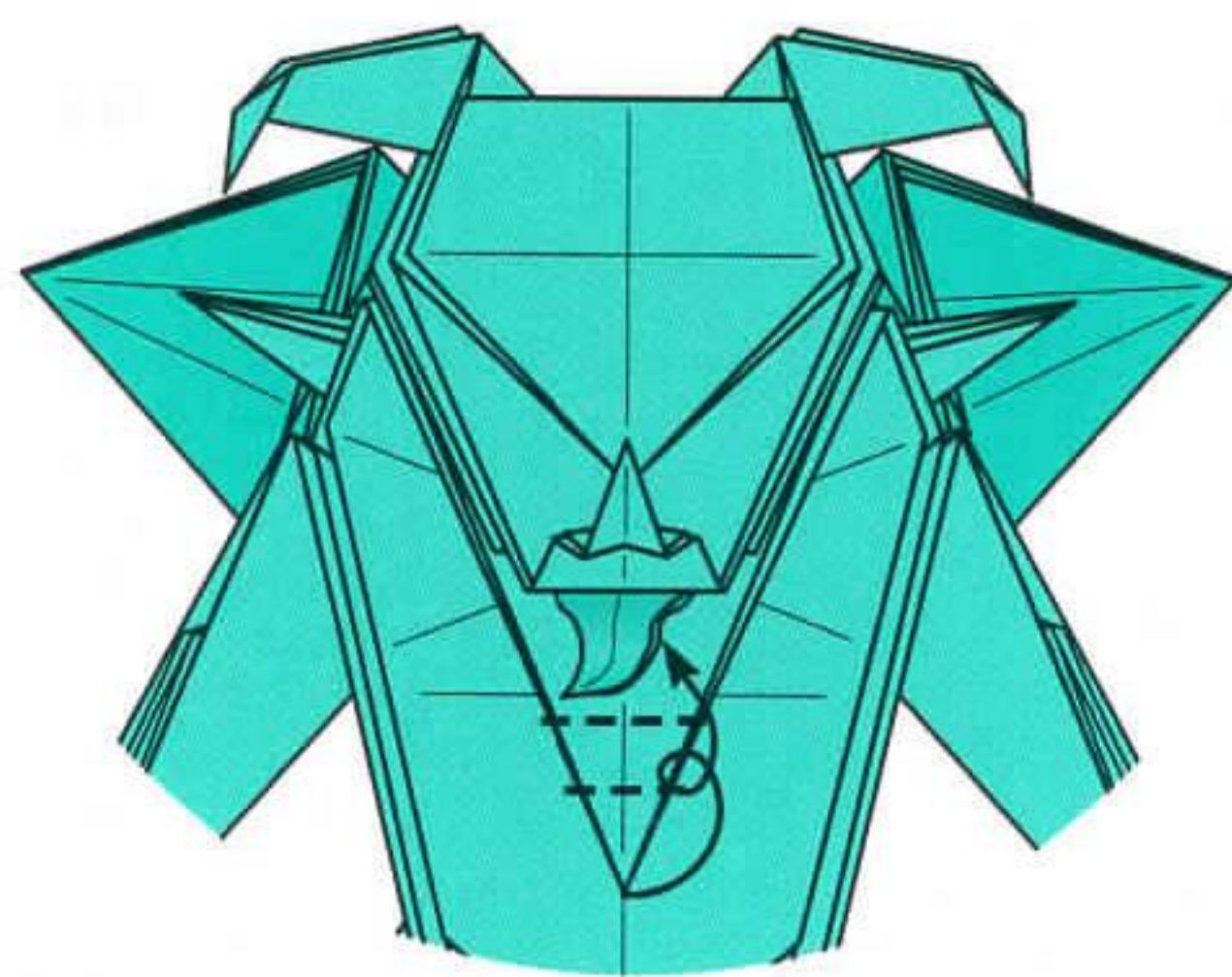
Inside reverse-fold the inner point at its root

Inside reverse-fold at about a half length



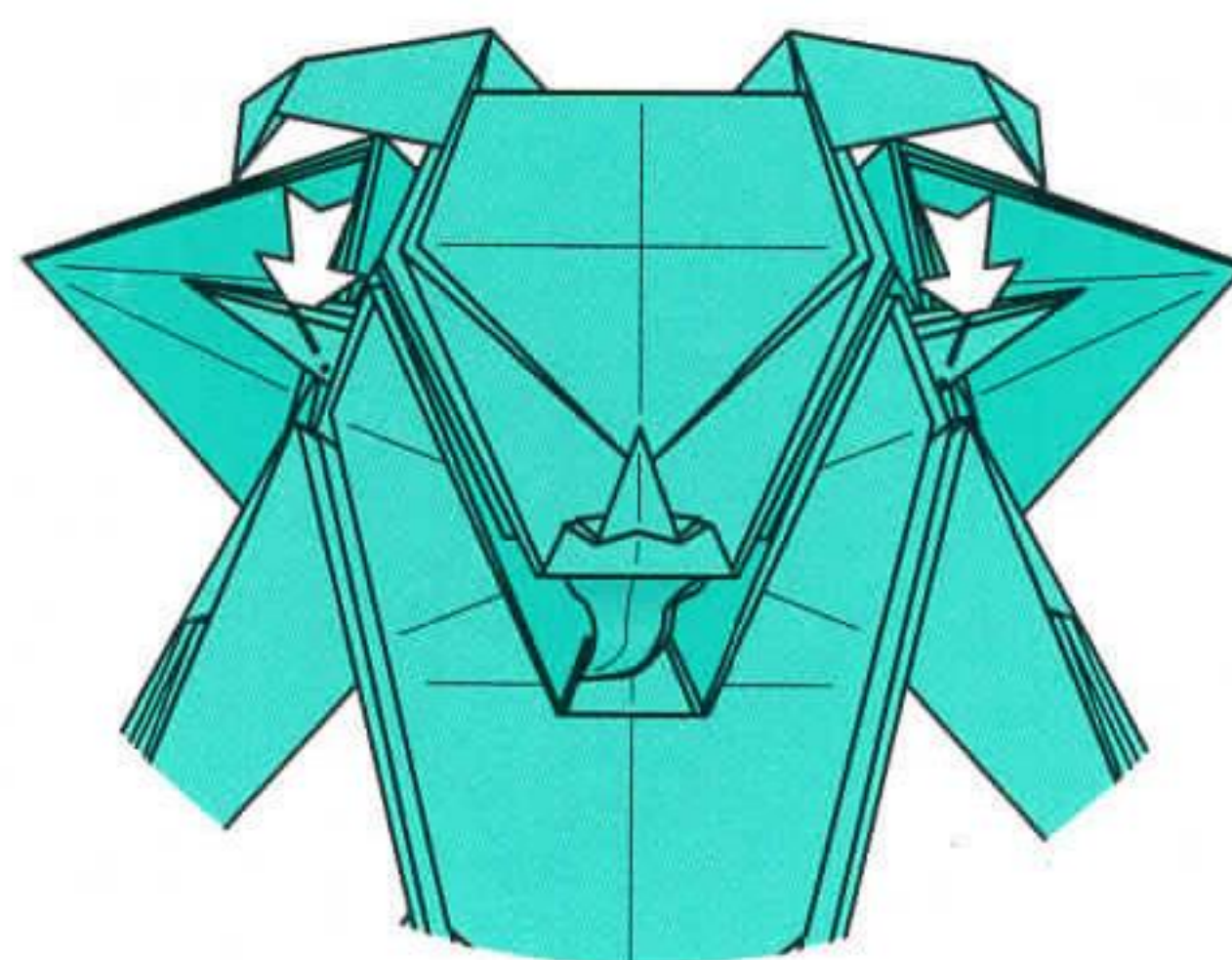


135



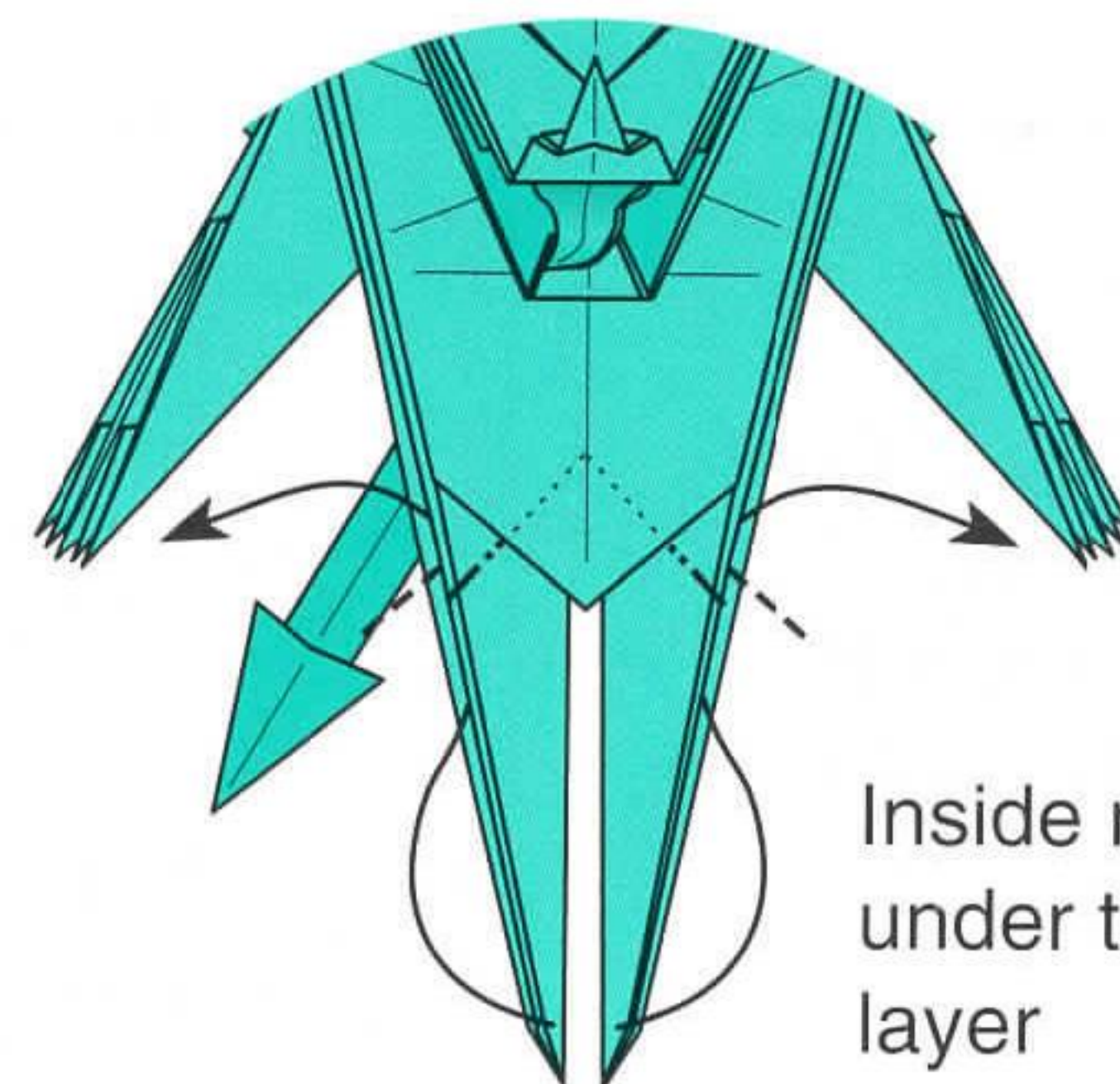
Fold twice to make the lower jaw.

136



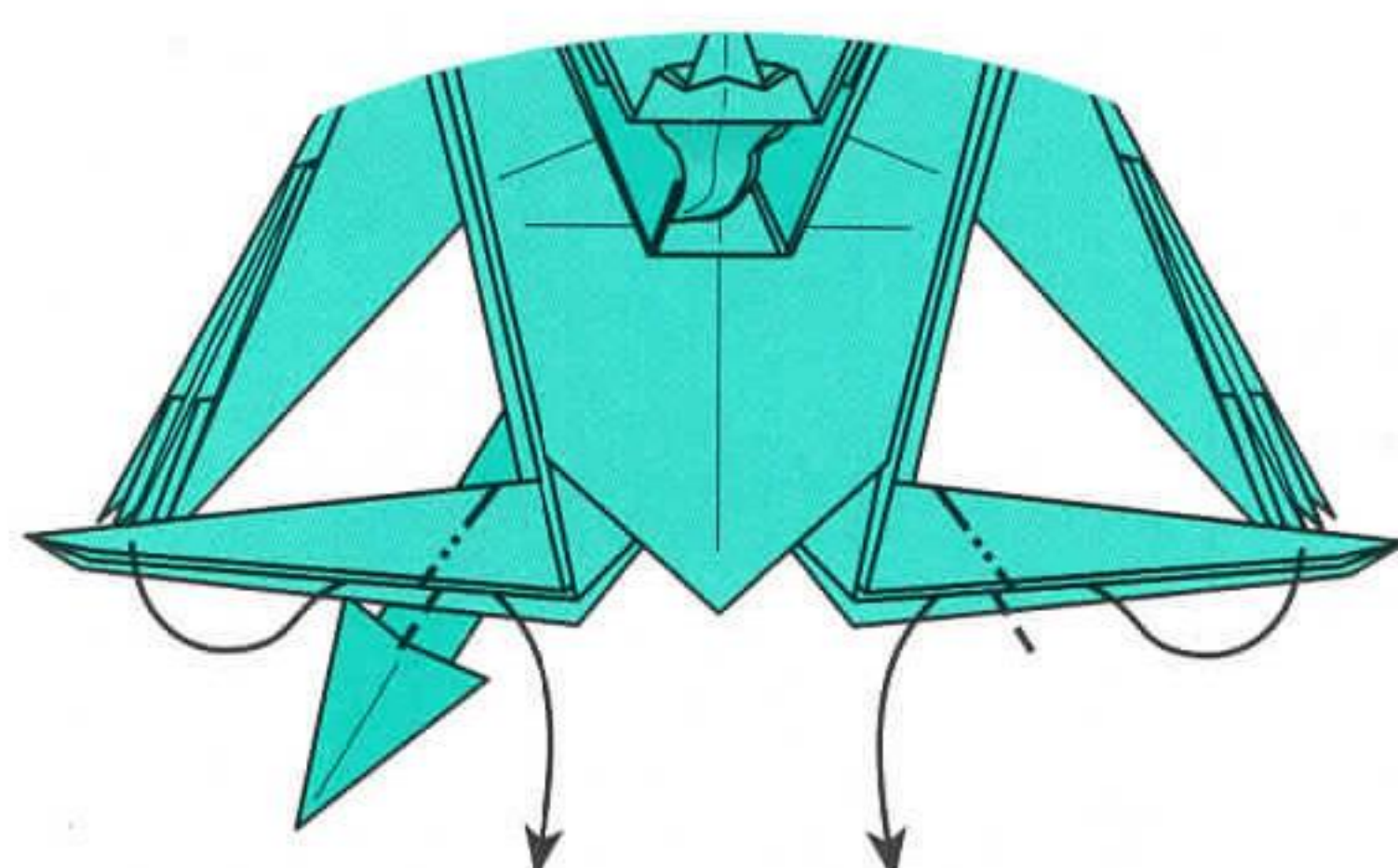
Open the ears.

137



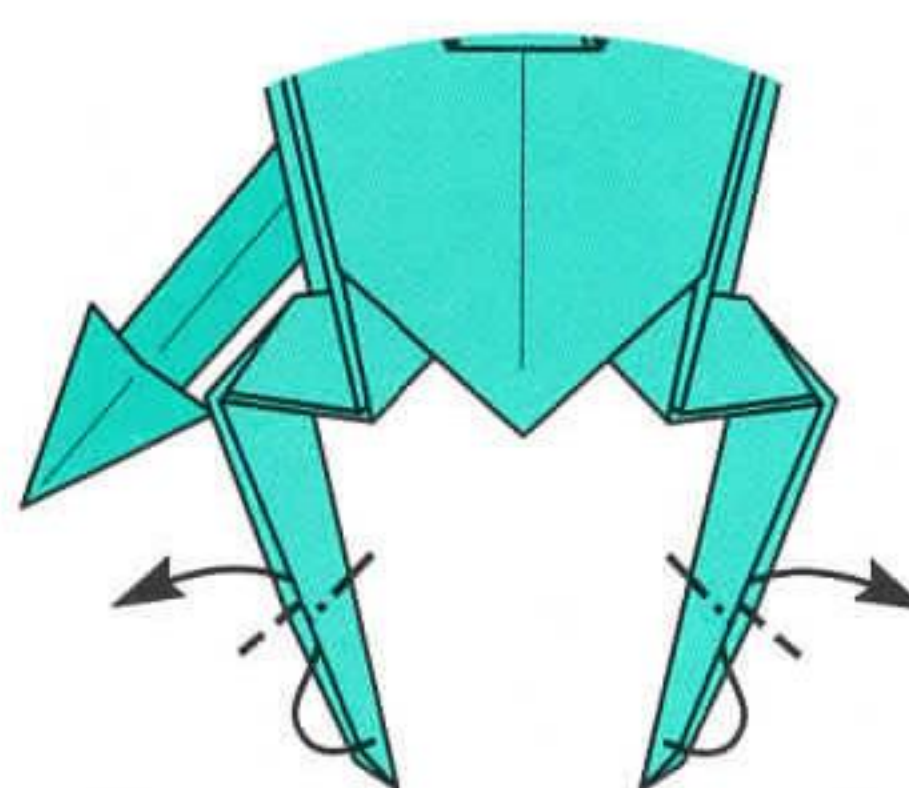
Inside reverse-fold under the second layer

138



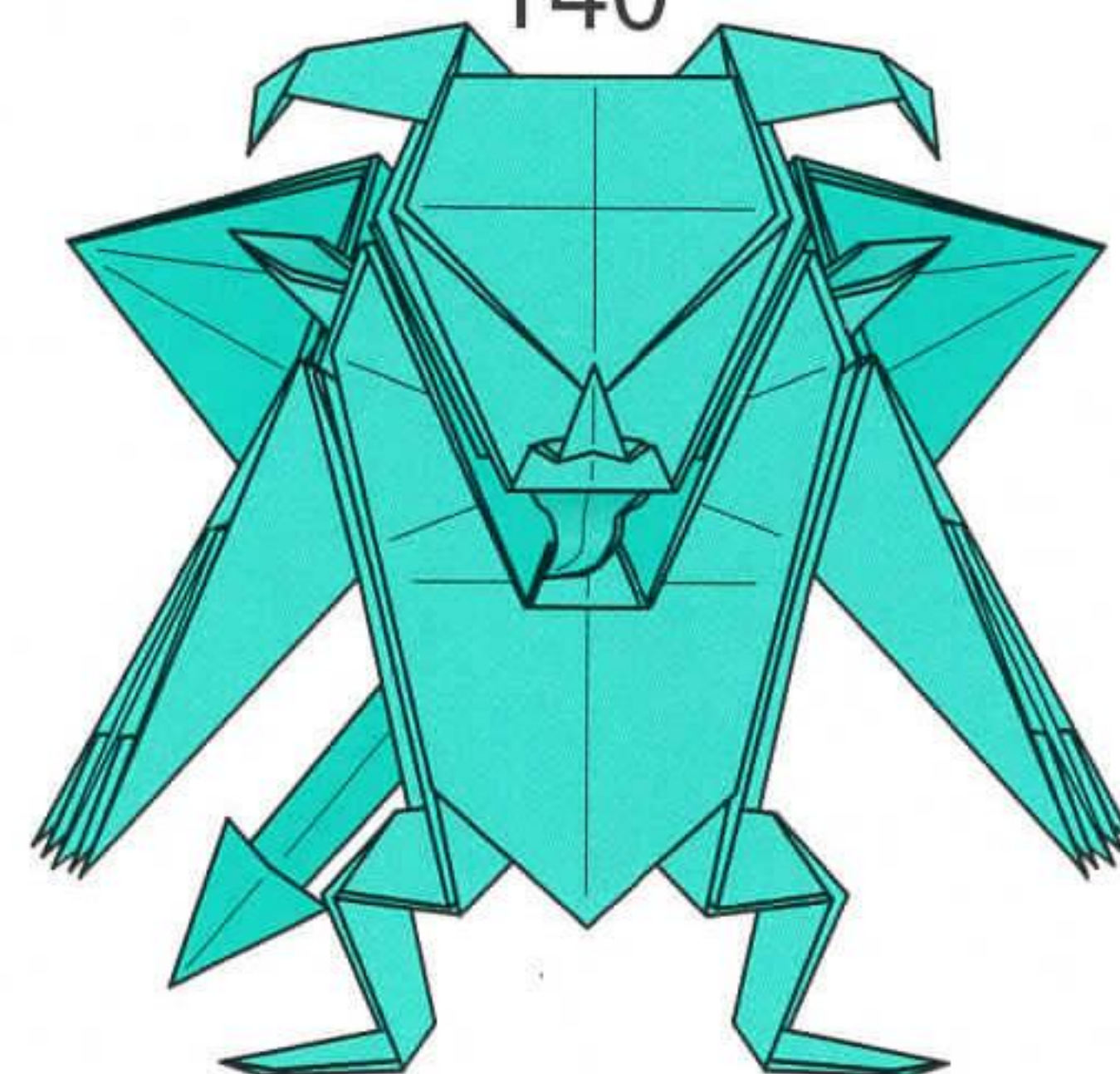
Inside reverse-fold

139

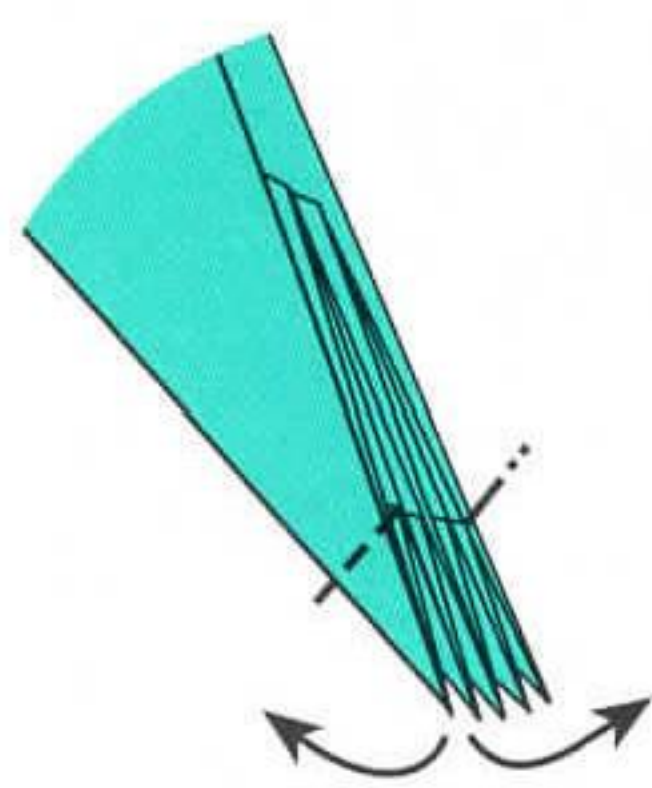


Inside reverse-fold

140

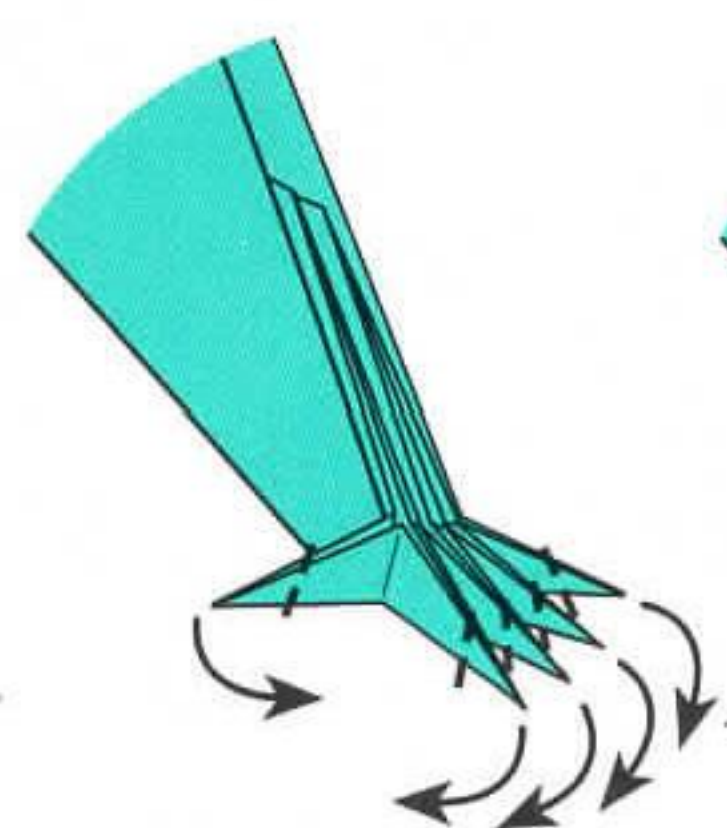


141

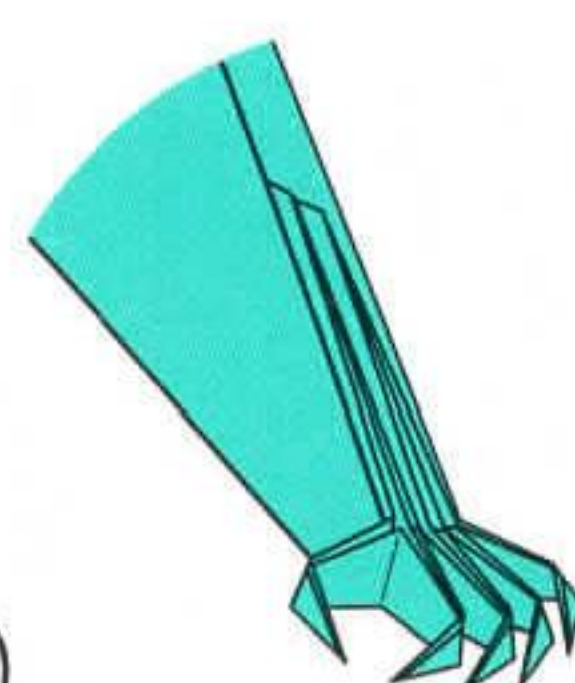


Spread the thumb and fingers.

142

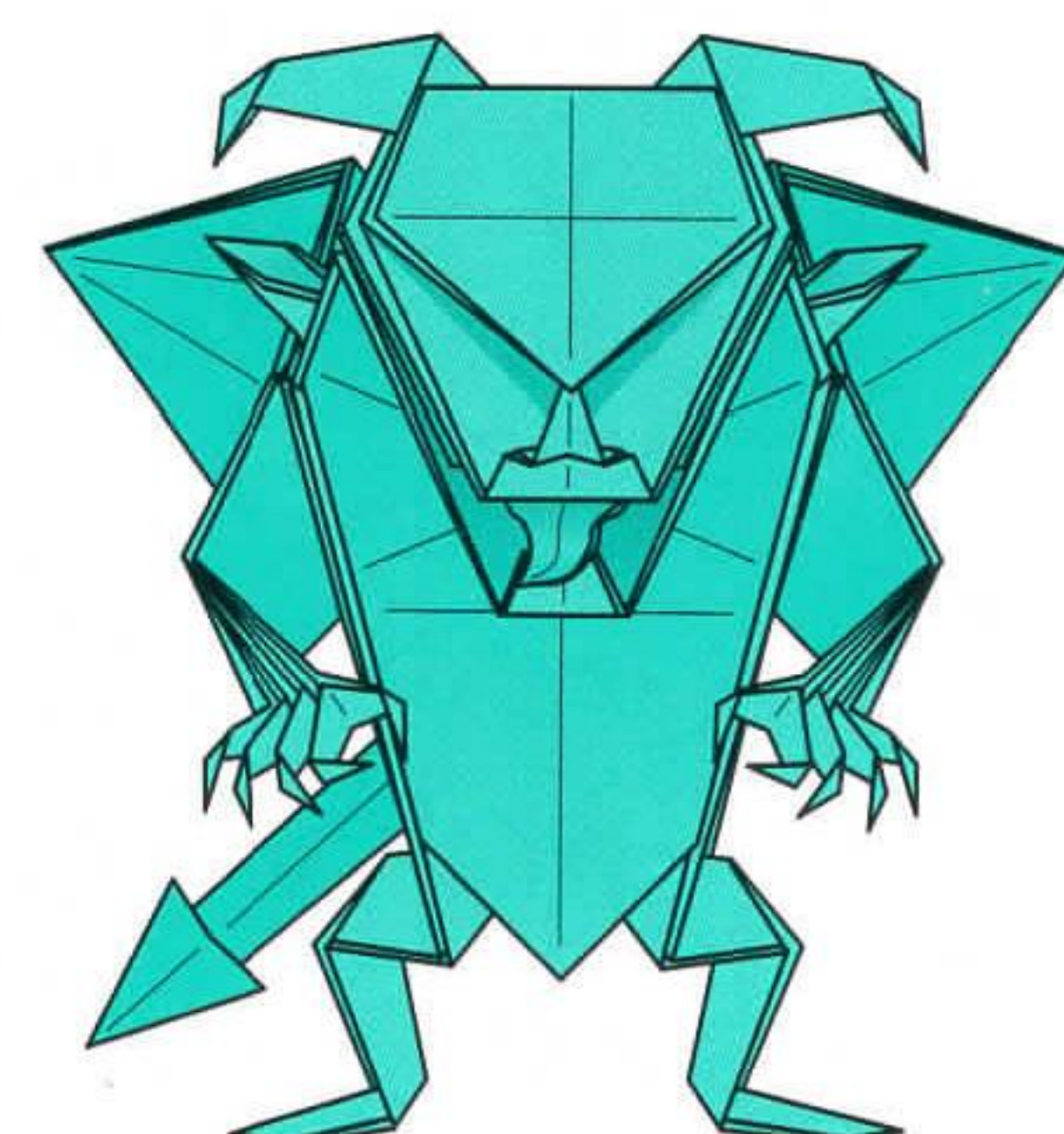
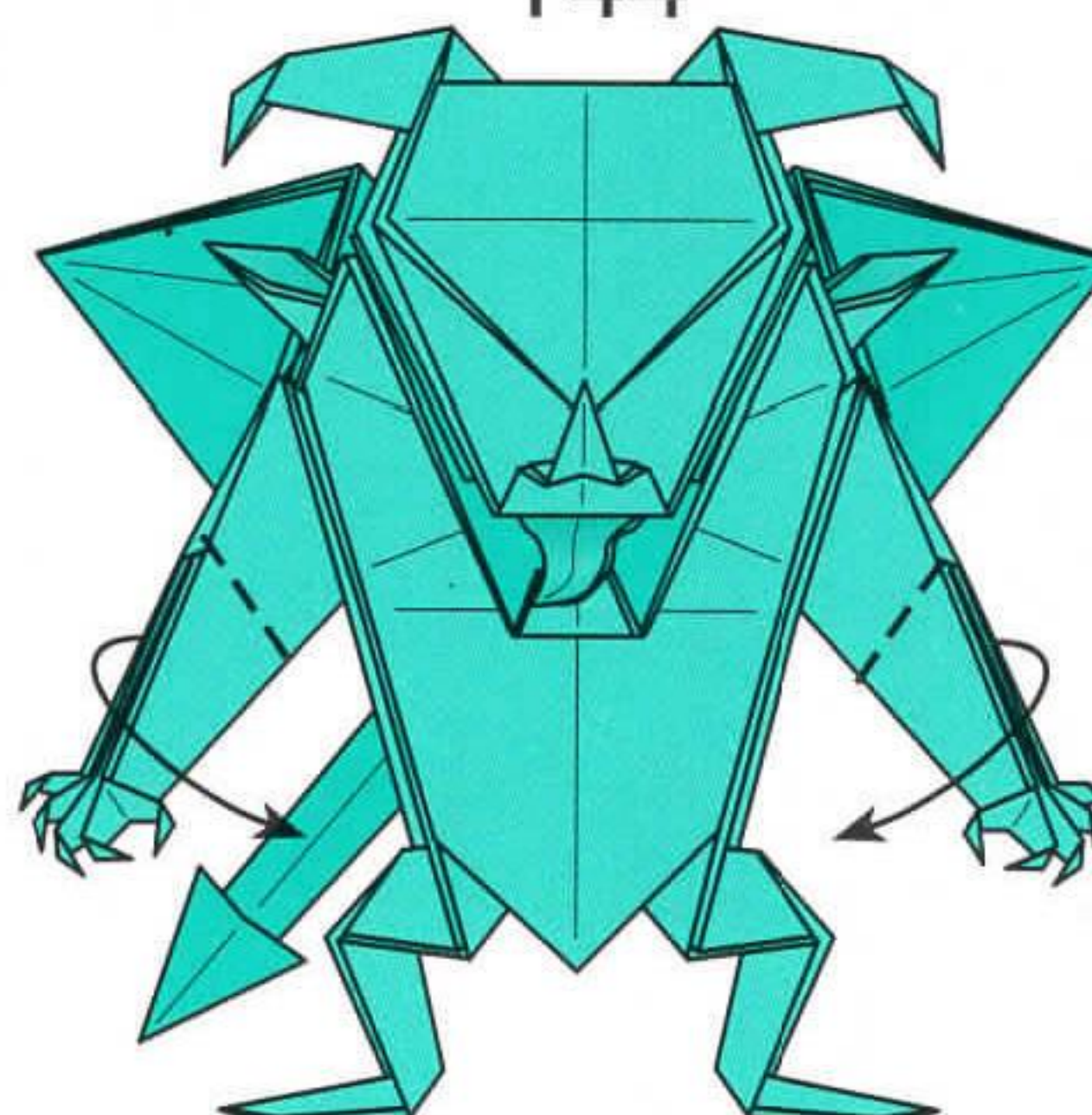


143



Repeat on the other side.

144



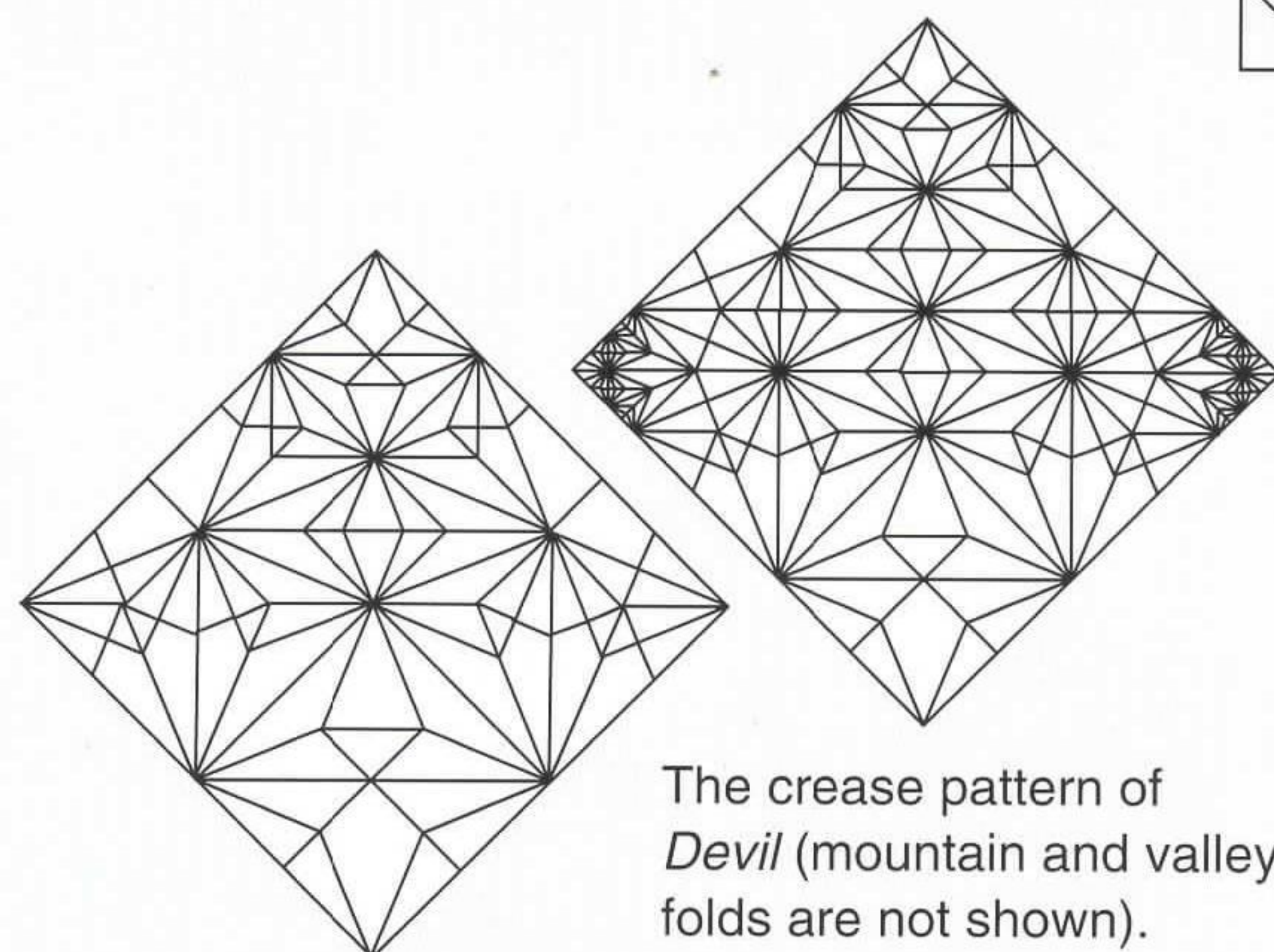
Make the model stand on its legs and the tail to finish.

This *Devil* is my first published model (published in the appendix of *Nikkei Science* in 1980). At the same time, it is my masterwork.

The fact that my masterpiece is a quarter of a century old may indicate that my origami has not developed since then. But now I feel this model to be more a kind of objective theorem of geometry than just a model of mine.

My design note at that time was titled "An emotional study on division of the plane and superposition of paper." Though it is too pretentious, typical of the young I was at the time, I still think the title do not miss the target.

To play with a material called paper, based on geometry, but sensuously rather than analytically. That seems to be the long-standing fascination of origami for me.



The crease pattern of *Devil* (without the fingers) (mountain and valley folds are not shown).

The crease pattern of *Devil* (mountain and valley folds are not shown).



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